# DETERMINATION OF SHEAR WAVE VELOCITY AND ATTENUATION FROM WAVEFORMS IN LOW VELOCITY FORMATIONS

by

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#### ABSTRACT

In boreholes where formation shear velocity is lower than borehole fluid velocity neither refracted shear waves nor pseudo-Rayleigh waves can propagate. When frequency response of the sonde does not extend to low frequencies (e.g.  $2 \ kHz$ ) Stoneley waves are not excited efficiently. In such cases refracted P, leaking modes (PL) and fluid waves become dominant phases on a full waveform acoustic log. The P wave velocity can be determined from the first arrivals. Then, using synthetic microseismograms and a waveform matching technique, formation shear wave velocity and attenuation can be determined. This method is demonstrated using data from a well in the Baltimore Canyon Trough area of the Atlantic margin.

#### INTRODUCTION

The determination of shear wave velocity in "soft" formations where shear wave velocities are less than the fluid velocity in the borehole is an important application of full waveform acoustic logs. The usual approach for low velocity formations has been to derive the shear velocity from the Stoneley wave phase velocities (Cheng and Toksöz, 1983; Barton *et al.*, this report). Stoneley waves are efficiently excited by low-frequency sources. In a typical borehole with a diameter of eight inches, most commonly used logging tools do not excite Stoneley waves when the shear wave velocity is below the fluid velocity. Mathematically this can be demonstrated in terms of the eigenfunctions of the borehole-formation system (see Figure 3, Toksöz *et al.*, 1983). Physically, as the formation shear wave velocity decreases, the phase velocity of the Stoneley wave, and hence its wavelength, decreases also. This implies that the amplitude of the Stoneley wave falls off more rapidly away from the borehole boundary. As a result, a source at the center of the borehole cannot excite the Stoneley waves as efficiently as its wavelength decreases.

In this paper we demonstrate an approach with which both shear velocity and attenuation values may be obtained from the detailed analysis of the Pwave train. We apply these to full waveform acoustic logging data obtained from a drill hole in the Baltimore Canyon region of the Atlantic Ocean.

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#### FULL WAVEFORM LOGS IN LOW VELOCITY SEDIMENTS

The data used in this study are from the Baltimore Canyon Trough, DSDP drilling Site 612 (Figure 1). The seismic section and the well location are shown in Figure 2. In addition to the logs, approximately 600 m of sediments were recovered at this site using the hydraulic piston corer (HPC) in the softer, unlithified sediments, and the extended core barrel (XCB) in the lower, more indurated sections. The stratigraphic column consists of an upper section of muds and glauconitic sands (135 m) overlying, on an erosional contact, a section of siliceous nannofossil oozes and chalks. At a very distinct level the biogenic silica in the sediments vanishes and is replaced by amorphous silica cement, creating a distinctive chalk-porcellanite unit. There is an excellent correlation between lithological units and the seismic reflectors (Figure 3).

At this time we have only a limited data set. The data was collected with the Schlumberger SLS-TA sonde. The Schlumberger logging tool has two sources and two receivers. The separation between the sources and between the receivers is 0.61 m (2 ft), with a distance of 2.44 m (8 ft) between the source and receiver arrays. Figure 4 shows typical full waveform acoustic logs. These sample traces are selected from actual data recorded at 60 cm depth intervals, with source-receiver separation of 2.44 m (8 ft). In this section of semiconsolidated oceanic sediments the P wave velocity is generally near 2.0 km/sec or less. The shear wave velocities measured on recovered cores are generally about 1.0 km/sec, much less than water velocity. In such cases there are no refracted shear waves, nor pseudo-Rayleigh waves.

The full waveform logs show a clear beginning of P waves followed by a long train that indicates the presence of a number of phases. In this case the borehole waveguide can propagate refracted P waves, leaky modes, fluid waves, and Stoneley waves.

The Schlumberger logging tool used at this site has a peak frequency response between 10 kHz and 15 kHz. In this frequency range the PL (Leaking P) modes are efficiently excited while Stoneley waves are not. The dispersions of these waves are best illustrated by the frequency wavenumber response of the borehole shown in Figure 5. This figure shows the refracted P wave (P), the first and second leaking PL modes ( $PL_1$ ,  $PL_2$ ), borehole "fluid" mode (FL) and Stoneley wave (ST). With the peak frequency response of the logging tool between 10 kHz and 15 kHz we expect to see primarily the P, PL, and FL modes.

A synthetic microseismogram calculated using formation velocities  $(V_p = 2.0 \ km/sec$  and  $V_s = 1.0 \ km/sec$ ) and logging tool properties similar to those used in Site 612 is shown in Figure 6. *P. PL* and *FL* phases are indicated. The *ST* (Stoneley) phase is outside the time window because of its slow velocity  $(v_{ST} \approx 0.7 \ km/sec)$ . The theoretical log is similar to the traces shown in Figure 1. This is demonstrated more clearly in Figure 7 where synthetic microseismograms are plotted with the observed data.

The amplitudes of P and PL modes strongly depend on the shear velocities of the formation. This is illustrated in Figure 8, where  $V_s$  is varied systematically while all other parameters are held constant. Note that for lower formation shear wave velocity the PL mode becomes longer and more dominant. Even for very small changes in shear wave velocity, the change in wave train is obvious. Zhang and Cheng (1984), using contour integrals to generate synthetic P waves and PL modes, have found that the amplitude of the P wave packet depends strongly on the Poisson's ratio of the formation. This is due to the conversion of the P head wave into shear wave energy at the borehole boundary, as evidenced by the "snapshots," generated by the finite difference technique, of the propagating waves in the formation (Stephen and Pardo-Casas, 1984).

In Figure 9 we show the effects of the attenuation properties of the formation  $(Q_p, Q_s)$  on the waveforms. Increasing formation attenuation decreases the amplitudes of P and PL waves, but does not affect the fluid waves. The duration of the wave train is not affected. Based on these calculations, the parameters that best fit the observed data shown in Figure 4 are  $V_p = 2.0 \ km/sec$ ,  $V_s = 1.0 \ km/sec$ ,  $Q_p = Q_s = 20$  for formation and  $Q_{fluid} = 100$  for borehole fluid.

#### DISCUSSION

This short paper is a simple demonstration of how to determine formation shear wave velocity and attenuation using waveform matching in a low shear velocity formation in the absence of Stoneley waves. Since only a limited amount of logging data are available at this time, no systematic inversion was carried out. For routine applications a formal inversion algorithm needs to be developed.

An unusual character of these logs not normally seen in typical data is the presence of a prominent fluid arrival. This phase is generally attenuated by the drilling mud in typical cases where  $Q_f \approx 15$ . However, when mud attenuation is low relative to formation attenuation, and when there are no Stoneley or pseudo-Rayleigh waves to mask it, a fluid arrival can be seen if the frequency response of the tool is high. The fluid arrival can be an important phase for calibrating the relative amplitudes and determining the formation Q.

#### ACKNOWLEDGEMENT

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Figure 1: Locations of DSDP Sites 612 and 613. The sites are located along the U.S.G.S. multichannel seismic line 25 and downslope from the COST B-2 and B-3 wells.

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# USGS Line 25



Figure 2: A portion of U.S.G.S. line 25 indicating the location of the COST B-3 well and DSDP Site 612. Vertical scale is 2-way travel time.

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Figure 4: Full waveform acoustic log traces (microseismograms) from Site 612. Source receiver separation is 2.44 m (8 ft). Depth is below sea level.

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Vs from Leaky modes



Figure 5: Frequency wavenumber response of waves in a borehole drilled in low shear wave velocity ( $V_s < V_{fluid}$ ) formation. K = wavenumber. R = borehole radius (10 cm), P = refracted P waves,  $PL_1$ ,  $PL_2$  = leaking PL modes, FL = fluid wave, ST = Stoneley wave.



Figure 6: Theoretical full waveform acoustic log calculated using the method described in Toksöz *et al.* (1983). Parameters used  $V_p = 2 \ km/sec$ ,  $V_s = 1.0 \ km/sec$ ,  $\rho = 2.0 \ g/cm^3$ ,  $R = 12.5 \ cm$ ,  $\Delta z = 2.44 \ m$  (8 ft),  $V_{fluid} = 1.5 \ km/sec$ ,  $\rho_{fluid} = 1.38 \ g/cm^3$ ,  $Q_p = Q_s = 20$ ,  $Q_{fluid} = 100$ .

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Figure 7: Full waveform acoustic logs from Site 612 and their comparison with theoretical logs calculated using parameters given in Figure 6. Depth below sea level.

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Figure 8: Variation of full waveform acoustic logs with change in formation shear wave velocity. All other parameters are held constant, same as those in Figure 6.





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