Automated Reaction Mechanism Generation Including Nitrogen as a Heteroatom

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Abstract

The open source rate-based Reaction Mechanism Generator (RMG) software and its thermochemical and kinetics databases were extended to include nitrogen as a heteroatom. Specific changes to RMG and the mining of thermochemistry and reaction kinetics data are discussed. This new version of RMG has been tested by generating a detailed pyrolysis and oxidation model for ethylamine (EA, CH\textsubscript{3}CH\textsubscript{2}NH\textsubscript{2}) at ~1400 K and ~2 bar, and comparing it to recent shock tube studies. Validation of the reaction network with recent experimental data showed that the generated model successfully reproduced the observed species as well as ignition delay measurements. During pyrolysis, EA initially decomposes via a C–C bond scission, and the CH\textsubscript{2}NH\textsubscript{2} product subsequently produces the first H radicals in this system via β-scission. As the concentration of H increases, the major EA consuming reaction becomes H abstraction at the α-site by H radicals, leading to a chain reaction since its product generates more H radicals. During oxidation the dominant N\textsubscript{2} producing route is mediated by NO and N\textsubscript{2}O. The observables were found to be relatively sensitive to the C–C and C–N EA bond scission reactions as well as to the thermodynamic values of EA; thermodynamic data for EA were computed at the CBS-QB3 level.
and reported herein. This work demonstrates the ability of RMG to construct adequate kinetic models for nitrogenous species, and discusses the pyrolysis and oxidation mechanisms of EA.

**Keywords**

Automatic reaction mechanism generation, Ethylamine, Fuel bound nitrogen, Oxidation, Pyrolysis, Chemical kinetics
1. Introduction

Nitrogen chemistry attracts great attention, especially in combustion science, because of the abundance of bound nitrogen in various conventional and alternative fuel sources. Despite decades of research on nitrogen reaction kinetics, summarized in seminal reviews by Miller and Bowman\textsuperscript{1} and by Dean and Bozzelli,\textsuperscript{2} detailed reaction mechanisms of many nitrogen-containing species remain a largely unexplored field.

Coal and crude oil contain significant amounts of fuel-bound nitrogen\textsuperscript{3–5} which, unless entirely removed prior to combustion, leads to NO\textsubscript{x} formation (predominantly NO and NO\textsubscript{2}) that are subject to stringent environmental regulations due to their contribution to smog and acid rain. De-nitrogenation units in crude oil refinery streams are also essential since nitrogen in heterocyclic compounds poisons many catalysts, especially those used in desulphurization units.\textsuperscript{6–8} Moreover, biomass-derived fuels contain a substantial amount of fuel-bound nitrogen.\textsuperscript{3}

Nitrogen chemistry in combustion is also crucial for describing and predicting the behavior of nitrogenous fuel additives. For example, 2-ethylhexyl nitrate (2-EHN) is a commercially available cetane number improver which has been added to diesel fuels for decades to increase reactivity and improve engine fuel economy.\textsuperscript{9,10} However, 2-EHN additives could negatively impact diesel NO\textsubscript{x} emissions.\textsuperscript{10} Additionally, amine fuel additives are widely used to control fuel injector deposits,\textsuperscript{11} yet relatively little is known about their high-temperature chemistry. Furthermore, describing and predicting combustion processes of nitrogen-based fuels, such as ammonia\textsuperscript{12} and aqueous ammonium-containing monofuels,\textsuperscript{13–16} heavily depend on understanding nitrogen chemistry in combustion. Finally, nitrogen is present in its molecular form in air, the most common fuel oxidizer. While the above is only a partial list, it clearly justifies the incentive for pursuing
and generating complete yet efficient chemical kinetic mechanisms for nitrogen-containing species.

Recent experimental studies have investigated the reaction mechanisms and combustion properties of model nitrogen-containing compounds that represent different characteristic fuel types such as nitroethane,\textsuperscript{17} amines,\textsuperscript{18} or morpholine.\textsuperscript{19,20} However, detailed reaction mechanisms are only available for relatively small nitrogen-containing compounds composed of up to three or four heavy (non-hydrogen) atoms.\textsuperscript{18} For morpholine, only skeletal mechanisms describing the most important steps have been proposed.\textsuperscript{19,20} It would be desirable to be able to quickly construct kinetic models for any mixtures containing C/H/N/O compounds.

The open-source Reaction Mechanism Generator (RMG) software\textsuperscript{21,22} automatically explores possible intermediate species and elementary reactions for a given reacting mixture based on reaction families and libraries using a flux-based algorithm. Given initial temperature, pressure and reactant composition, the software estimates all the relevant reaction kinetics and thermochemistry; the generated model includes the most important species and reactions, where the “importance” is defined by the user using a tolerance parameter. The procedures implemented by RMG to expand the kinetic model were extensively discussed elsewhere.\textsuperscript{22–25} Previously, RMG has successfully generated reaction mechanisms for diverse C/H/O chemical systems such as butanol isomers,\textsuperscript{25,26} diisopropyl ketone,\textsuperscript{27} JP-10 jet fuel,\textsuperscript{28–30} and neopentane.\textsuperscript{31}

The main objectives of the present work are to report upon extensions made to RMG and its thermochemistry and kinetics databases to account for reactive nitrogen species, and to show that RMG can successfully generate reasonable predictive kinetic models for pyrolysis and oxidation of nitrogenous systems. This makes RMG the first reaction mechanism generator to automatically generate models for nitrogen-containing systems (except RMG cannot yet model aromatic
compounds containing heteroatoms in the aromatic ring, that capability is under development). The extensions are applied and tested by generating a reaction mechanism for pyrolysis and oxidation of ethylamine (EA, CH$_3$CH$_2$NH$_2$) and comparing the predictions to results of recent shock tube experiments.$^{32}$ The EA molecule was chosen for this study since it contains important characteristic chemical bonds (i.e., C–C, C–H, C–N, and N–H bonds), it is a representative of aliphatic amines, and also serves as a model species for nitrogen-containing compounds found in fuel additives and biofuels.$^{33}$

Previously key reactions of EA$^{32-37}$ and EA derivatives$^{38}$ were studied, yet a complete detailed kinetic mechanism for EA was until now absent from the literature. Specifically, an important initial decomposition reaction of EA, the C–C bond scission reaction, was missing from some works,$^{36,37}$ or manually tuned to improve agreement with experimental data in others.$^{32}$ The ab-initio model presented herein was generated automatically using RMG for EA concentrations of 500–2000 ppm and physical conditions of ~1400 K and ~2 bar. A similar model could be regenerated using RMG to be valid at different conditions.

2. Model

2.1. RMG algorithm development and database extension

The reaction mechanism reported herein was generated using the Python version of the Reaction Mechanism Generator software (RMG-Py) v2.1.0.$^{21}$ Species thermochemistry was either determined by using the existing RMG’s thermochemistry libraries or estimated using the Benson’s group additivity method$^{39}$ extended with the nitrogen group values derived by Ashcraft and Green$^{40}$ computed at the CBS-QB3 level (the CBS-QB3 method$^{41}$ is briefly described in Section 2.2). Kinetics of reactions involving nitrogen reviewed by Dean and Bozzelli$^2$ were added
as a kinetic library to RMG. If the software finds a matching reaction within its libraries, these parameters are used; otherwise, RMG applies its reaction family templates to estimate rate coefficients. The Dean and Bozzelli\textsuperscript{7} nitrogen kinetics data was also used to enhance the rate rules of various RMG reaction families.

To correctly account for unimolecular pressure-dependent reactions and estimate pressure fall-off effects, RMG databases have been extended by adding characteristic vibrational frequencies for nitrogen-centered groups adopted from the literature.\textsuperscript{42} The modified strong collision approach\textsuperscript{43} was used for subsequent automatic pressure dependence calculations in RMG.\textsuperscript{44}

Nitrogen is the first element included in RMG that commonly changes its valence: from monovalent (e.g., a terminal nitrogen on an azide) all the way to pentavalent (e.g., HNO\textsubscript{3}). Accordingly, the number of lone electron pairs of a nitrogen atom could vary between zero, one, or two. Consequently, RMG was extended to keep track of the number of lone electron pairs as well as unpaired electrons on all atoms. RMG has also been extended to recognize two additional classes of resonance structures that are specific to lone electron pairs (Table 1): (a) the resonance of a nitrogen atom between a single–triple bonded structure and two double bonds, as in N\textsubscript{2}O; and (b) the interaction between a lone electron pair and an adjacent radical site, as in NO\textsubscript{2}. In RMG, the lone electron pair / radical resonance class has so far been limited to nitrogen adjacent to oxygen atoms because of the current paucity of thermochemical properties in the RMG database for carbenes and carbanions.

2.2. Quantum chemistry calculation

Rate coefficients were calculated at the high pressure limit using the conventional transition state theory. The energy barrier $\Delta E^\ddagger$ was calculated using the CBS-QB3 method. This composite method combines low level geometries and zero-point vibration energies with higher level
calculations to obtain relatively accurate total molecular energies.\textsuperscript{41} Partition functions were obtained using the B3LYP/6-311G(2d,d,p) level of theory, while scaling the obtained frequencies by 99.8\%.\textsuperscript{45} For addition reactions the hybrid meta-GGA BMK/6-311G(2d,d,p) method was used for the partition functions.

To account for the anharmonicity of low-frequency torsional vibrations, internal rotations of both stable species and transition states were treated as one-dimensional hindered rotors (1D-HR). The 1D-HR partition function uses the energy levels obtained from solving the exact Schrödinger equation for the 1D potential energy surface, calculated from relaxed scans of the corresponding dihedral angles in 10° increments at the B3LYP/6-31G(d) or BMK/6-31G(d) levels of theory. CBS-QB3 enthalpies of formation were adjusted using the bond-additivity corrections (BAC) recommended by Petersson \textit{et al.}\textsuperscript{46}

\textbf{2.3. Model generation}

The mechanism was generated using RMG-Py\textsuperscript{21,22} incorporating the above mentioned algorithm and database extensions. The model was built using RMG’s thermodynamic libraries including updated parameters for small species of the H\textsubscript{2}/O\textsubscript{2} system.\textsuperscript{47} An EA kinetic library (Table 2) was used and added to the software libraries. RMG calculated k(T,P) expressions from relevant k(T) expressions using procedures and approximations detailed previously.\textsuperscript{44} The selected tolerance for the network generation was 0.02,\textsuperscript{48} as a tighter error tolerance (0.01) did not add new nitrogen chemistry to the model. The model was generated for \textasciitilde1400 K and 1.2–2.1 bar to be valid at the measured experimental conditions. Simulations of the model as well as rate of production calculations were carried out in Chemkin-Pro\textsuperscript{TM} \textsuperscript{49} in an adiabatic homogeneous batch reactor. Ignition delay times were calculated using Cantera,\textsuperscript{50} and sensitivity coefficients were generated by RMG.
The final model consists of 79 species and 1771 reactions and is available both as RMG and as Chemkin input files in the supplemental material. A species dictionary is also supplied.

3. Results and discussion

3.1. Ab initio calculations

Most of the small molecule reactions that are relevant for EA pyrolysis and oxidation have been documented by Dean and Bozzelli. However, the complete initial decomposition reactions and the various possible pathways leading to the initial radical pool formation in this system have not been documented before. As these are very important to describe the decomposition of EA, we studied these reactions using the above-mentioned methods.

Figure 1. EA BDE values and geometries of selected TS. Geometries were calculated at the B3LYP/6-311G(2d,d,p) level of theory, bond lengths are in pm. (A) CBS-QB3 BDE for the various bonds in EA. TS geometries and energy
barriers for (B) the 1,2 elimination of ammonia, and for the three hydrogen abstraction reactions by the H atom: (C) from the β-site, (D) from the α-site, and (E) from the N-site in EA.

The weakest bond in EA is the C–C bond, having the lowest bond dissociation energy (BDE) of 348 kJ mol⁻¹. This is 12 kJ mol⁻¹ lower than the BDE of C–N, and 25–80 kJ mol⁻¹ lower than BDE values for H atoms in EA (Fig. 1 A). EA is known to undergo four possible elimination reactions; while most elimination routes have an activation energy greater than 420 kJ mol⁻¹, the 1,2-elimination reaction yielding NH₃ has a relatively low activation energy of 286.6 kJ mol⁻¹. This reaction, which proceeds via the transition state (TS) in Fig. 1 B, is considered the most significant elimination reaction of EA. The relatively low barrier for this elimination makes it a significant unimolecular decomposition channel at most conditions and a non-negligible competitor to the main radical decomposition pathways at higher temperatures.

The calculated BDE values (Fig. 1 A) suggest that a radical mechanism in EA pyrolysis will be initiated primarily by the C–C bond scission reaction. Once the radical pool has been generated, EA undergoes various H abstraction reactions. The hydrogen atom bonded to the α-carbon has the lowest BDE of all H atoms in EA (386 kJ mol⁻¹). The BDE for hydrogen atoms bonded to nitrogen or β-carbon atoms are 32 and 42 kJ mol⁻¹ higher, respectively. Hence, hydrogen abstraction reactions from EA are expected to occur preferably at the α-site.

The lowest barrier for H abstraction reactions in EA was found to be at the α-site (Fig. 1 C–E), as expected from the BDE values in Figure 1 A. The barriers for H abstraction at the nitrogen or the β-site are computed to be significantly higher. The barrier heights are also reflected in the transitional bond lengths between the C or N atoms in EA to the respective abstracted H atom; while abstraction from the α-site increases the bond length by 11.8% at the TS, the bond lengths increase by ~24–27% for abstraction from the nitrogen and the β-carbon sites. This large difference
is mainly due to the adjacent lone electron pair of the N-atom, which stabilizes the radical that results from the α-site H abstraction.

Previously calculated H abstraction reaction rates were adopted from literature (Reactions 1–12). Rates of other H abstraction (Reactions 13–17), β-scission (Reactions 18–24), and intramolecular hydrogen transfer (Reactions 25–26) reactions, as well as the 1,2-elimination reaction yielding NH₃ (Reaction 27) were calculated as part of the present work (Table 2). It is noted that Reactions 18–27 are pressure dependent, and Table 2 lists their high pressure limit rate only; the k(T,P) rates were calculated by RMG as described above.

3.2. Ethylamine pyrolysis

The RMG-predicted NH₂ concentration profile during EA pyrolysis was compared to experimental shock tube values as reported by Li et al. (Fig. 2). The model reproduced well the rise and fall of NH₂ levels, and predicted a peak concentration about 50% higher than the experimental peak value. The times at which the concentrations peaked were relatively close: 42 and 45 μs for the simulated and experimental profiles, respectively. Overall, the generated model captures well the NH₂ concentration profile during EA pyrolysis, and the overestimation of the peak concentration is reasonable.
A rate of production (ROP) analysis for EA (Fig. 3 A) indicates that during the first few microseconds of pyrolysis, prior to the establishment of the radical pool, EA primarily decomposes via C–C and C–N bond scission reactions, as well as the 1,2-elimination reaction yielding NH₃. The fastest unimolecular decomposition reaction is the C–C scission, in agreement with the BDE analysis above (Fig. 1 A).

During the first 10 µs, while the EA C–C scission is the fastest decomposition route, H radicals are mainly being produced by β-scission of CH₂NH₂, a product of the EA C–C scission (Reaction 10 in Figs. 3, 4). As the radical concentration in this system increases, rates of EA H abstraction reactions, mainly by H atoms, become significant, and the dominant EA consumption route becomes the α-site H abstraction by H, which is also the fastest H radical consumption pathway in this system (Reaction 4). The higher reactivity of the H bonded to the α-carbon relative to other H atoms in EA is also in agreement with the BDE analysis (Fig. 1). The EA α-site H abstraction reactions produce CH₃CHNH₂ radicals, which later become the main source for H radicals in the system (Reaction 9). Since H radicals induced the formation of the α-site radicals in the first place, and are formed at a significant rate through this pathway, a chain reaction is formed, leading to an accelerated consumption of EA and to the formation of CH₂=CHNH₂ (Figure 4). The EA C–N scission reaction (Reaction 2) is the major NH₂ source in the system at early times, while β-scission of the β-site radical CH₂CH₂NH₂ (Reaction 13) becomes the dominant NH₂-generating reaction at later times as the concentration of radicals increases.
Figure 3. Reactions with highest flux for (A) EA, (B) H, and (C) NH₂ at the conditions in Fig. 2. The inset in (A) is a semi-log representation for shorter times.
An EA pyrolysis diagram is proposed based on reactions’ ROP (Fig. 4). The diagram illustrates the important chain reaction of EA H abstraction by H at the $\alpha$-site followed by a $\beta$-scission reaction generating H radicals (Reactions 4, 9). The branching ratio of the major H abstraction reactions of EA could also be qualitatively inferred from this diagram, showing a clear tendency to produce the $\alpha$-site radical. All EA radicals formed by H abstraction have a relatively small quasi-steady state concentration in the system since their production is rate limiting.

The pyrolysis diagram in Fig. 4 represents the major fluxes in the systems at 20 $\mu$s. At this point in time, the system is close to the peak rate of small radical generating reactions (Fig. 3 B, C), yet the three major initial EA decomposition pathways are still significant.
Many of the channels lead to HCN formation. Both the C–N scission and the NH$_3$ elimination reactions mainly lead to the formation of C$_2$H$_4$ while the C–C scission leads to CH$_2$NH. The pathways via the various H abstraction reactions all involve a more interesting chemistry with more steps. The α-site radical leads to the formation of almost equimolar amounts of HCN and CH$_4$ as well as some unsaturated C/C/N structures such as CH$_2$CNH and CH$_3$CN. The β-site and N-site radicals, on the other hand, mainly produce C$_2$H$_2$, while the N-site radical produces some HCN as well. Both α-site (through CH$_2$CHNH$_2$) and N-site radicals may also be converted into the β-site radical. N$_2$ is formed by the NH$_2$ + N reaction.$^2$
Figure 5. (A) Kinetic and (B) Gibbs Energy change normalized sensitivity coefficients of NH$_2$ at the conditions in Fig. 2 showing the top five influential reactions and species during the first 100 $\mu$s. Reaction numbers correspond to those from Fig. 3 for consistency.

The branching ratio of EA decomposition is crucial in determining the amount of NH$_2$ formed, as can be seen from the top five reactions to which NH$_2$ levels are sensitive (Fig. 5 A). The two major NH$_2$ production routes, C–N scission and $\beta$-scission of the $\beta$-site EA radical (Figs. 3, 4), are reflected in the sensitivity analysis either directly (Reaction 2) or indirectly (Reaction 5). The system is also sensitive to the EA H abstraction at the $\alpha$-site by NH$_2$ (Reaction 7), the major NH$_2$ consumption pathway. The NH$_2$ concentration was most sensitive to the rate of the C–N bond scission reaction, with a normalized sensitivity coefficient in the order of one at relatively early times when this reaction dominates NH$_2$ production.
The sensitivity analysis suggests that a better agreement, if desired, between simulated and experimental NH$_2$ levels (Fig. 2) could be obtained by decreasing the uncertainty in rates of major reactions that produce and consume NH$_2$. While EA H abstraction reaction rates by H and NH$_2$ are known at the CBS-QB3 level,$^{33}$ both C–N and C–C scission reaction rates were estimated by RMG. RMG was recently trained with various C–C scission reactions in hydrocarbon systems calculated at the CASPT2/cc-pvdz level using variable reaction coordinate transition state theory (VRC-TST).$^{53}$ However, due to insufficient literature data, RMG's estimates of bond scission reaction rates involving nitrogen currently have much greater uncertainties. Since the system discussed herein is sensitive to the C–N scission, it would be beneficial to calculate the rates of reactions of that type. This, however, does not interfere with the present work's objective of demonstrating RMG's ability to generate reasonable models involving reactive nitrogen.

The NH$_2$ concentration was found to be relatively sensitive to the $\Delta$G value of EA, as well as to the products of both the C–C and C–N bond scission reactions (Fig. 5 B). In fact, the normalized sensitivity coefficients of each scission reaction product pairs resemble each other, yet slightly deviate at later times due to the importance of the smaller radicals (i.e., NH$_2$, CH$_3$) for EA H abstraction reactions. The $\Delta$G sensitivity coefficients for C$_2$H$_5$ and NH$_2$ have relatively large absolute values at early times that gradually decrease, similarly to the sensitivity to Reaction 2 (Fig. 5). This decreasing trend stems from the decreasing significance of the C–N scission reaction in NH$_2$ generation (Fig. 3 C).

The sensitivity to the $\Delta$G values of the C–C scission reaction products is negative at first, yet changes its trend after ~10 µs and becomes positive, which is consistent with the sensitivity to the rate of Reaction 1 (in an opposite sign). This interesting shift in trends is explained by the role of
the C–C scission reaction in the generation of NH₂. At first H radicals are mainly produced from CH₂NH₂, and they are important agents in EA H abstraction reactions including its conversion into the β-site radical which is a major source for NH₂. However, once the radical pool is established, the chain reaction via the α-site radical becomes the dominant source for H radicals (Fig. 3 B), and the C–C scission reaction consumes EA via a pathway which is not constructive to the fastest NH₂ generation route.

The sensitivity of NH₂ to the ΔG value of EA interestingly decreases with time and becomes slightly negative. The role of EA in NH₂ generation is clear, and as expected the sensitivity coefficients to its ΔG value are positive at early times. However, since EA is involved in the major sink of NH₂ as well (Reaction 7), the trend of these sensitivity coefficients shifts over time and changes its sign. The thermodynamic parameters of the CH₃, NH₂, C₂H₅, and CH₂NH₂ radicals in the current model are given at the CCSD(T)F12A/cc-pVTZ-F12//B3LYP/6-311++g(d,p) level of theory, taken from an RMG library. The thermodynamic parameters of EA, on the other hand, were taken from Yaws’ Property Data for Chemical Engineers and Chemists handbook; further calculations and the uncertainty of these values are discussed in Section 3.5.

3.3. Ethylamine oxidation

The predicted concentration profiles of NH₂ and OH radicals during EA oxidation were compared to respective experimental shock tube values under slightly lean fuel conditions (ϕ=0.94) as reported by Li et al. (Figure 6).³² Measurements of OH radicals were conducted in a more diluted atmosphere than NH₂ measurements to reduce the temperature rise, and consequently reduce the uncertainty in the OH absorption coefficient which is sensitive to the temperature.
Figure 6. Concentration profiles of selected radicals during EA oxidation. (A) NH$_2$ concentration vs. time during oxidation of 2000 ppm EA with 8000 ppm O$_2$ in Ar at 1441 K and 2.13 bar. (B) OH concentration vs. time during oxidation of 500 ppm EA with 2000 ppm O$_2$ in Ar at 1399 K and 1.96 bar. The estimated experimental uncertainty for NH$_2$ and OH is 10–30%$^{51,52}$ and 12%$^{55}$, respectively.

The model adequately reproduced the rise and fall in NH$_2$ concentration (Fig. 6 A), and predicted a peak NH$_2$ concentration $\sim$60% higher than the experimental peak value. These peaks were observed at relatively close times of 21 and 25 $\mu$s in the model and experiment, respectively. The model over-predicted the small pre-ignition OH concentration rise, yet captured exceptionally well the OH time profile during ignition as well as the post ignition OH consumption rate (Fig. 6 B). Overall, the mechanism successfully reproduced the NH$_2$ and OH concentration profiles during EA oxidation. The following analysis and discussion relate to the conditions at which the EA oxidation experiment monitoring NH$_2$ was conducted (Fig. 6 A), i.e., 2000 ppm EA, 8000 ppm O$_2$ in Ar at 1441 K and 2.13 bar.
Figure 7. Simulated concentration profiles at the conditions in Fig. 6A during EA oxidation of top 10 species with the highest concentration except for Ar and O$_2$.

The concentration of EA decreased exponentially, and at 100 $\mu$s its conversion reached $\sim$98%. The major products of the first 100 $\mu$s, prior to ignition, are H$_2$O, H$_2$, HCN, CO, NH$_3$, and C$_2$H$_4$. As the oxidation proceeds, H$_2$, HCN, NH$_3$, and C$_2$H$_4$ are consumed, while the concentration of H radicals and N$_2$ increase by an order of magnitude (Fig. 7).

During the first 100 $\mu$s, H radicals are mainly being produced and consumed via similar pathways as shown and discussed above (Fig. 3 B), with the exception of the important branching reaction $\text{H} + \text{O}_2 = \text{OH} + \text{O}$, which significantly consumes H radicals (Reaction A3, Fig. 8). After a chemical induction time required to build the degenerate branching step ($\sim$350 $\mu$s), the system ignites as seen from the increased production and consumption rates of H (Fig. 8 A), consuming NH$_3$ and C$_2$H$_4$ (Fig. 7).

The major NH$_3$ production pathways during the first 100 $\mu$s resemble those discussed above in the pyrolysis case, namely EA C–N scission which dominates at early times followed by $\beta$-scission of the $\beta$-site radical CH$_2$CH$_2$NH$_2$, as well as the well-skipping reaction consuming the N-site radical CH$_3$CH$_2$NH (Reactions B1-B3, Fig. 8). Other than attacking EA principally at the $\alpha$-site (Reaction B4) to form NH$_3$, NH$_2$ is also consumed by reacting with HO$_2$ and O radicals.
(Reactions B5, B8). During ignition, the NH\textsubscript{3} formed initially is converted back into NH\textsubscript{2} by the OH radicals (Reaction B7). The NH\textsubscript{2} formed in this way is consumed a little later, mainly by reacting with NCO radicals (Reaction B6).
Figure 8. Reactions with highest flux for (A) H, (B) NH$_2$, and (C) OH during EA oxidation.
Initially OH radicals are generated via $\text{H} + \text{O}_2$ or $\text{H} + \text{HO}_2$ (Reactions C2, C4, Fig. 8), while the main OH consumption routes are $\alpha$-site and N-site H abstractions from EA (Reactions C3, C5). The relatively high sensitivity of OH levels to the EA C–C scission reaction (Fig. 9 A) is due to the role of this scission reaction in determining the initial H concentration in the system, which is essential for the major OH producing reactions. This reaction rate was estimated, and errors in its rate may cause the OH over-prediction by the model at early times (Fig. 6 B).

During ignition, OH participates in classic and well-studied\textsuperscript{47} small radical chain branching and propagation reactions (Reactions C1, C2, C6, Fig. 8). Its major source is the main branching reaction, $\text{H} + \text{O}_2 = \text{OH} + \text{O}$, to which it is also highly sensitive (Fig. 8 C, Fig. 9 A). Since H is the limiting factor in this reaction, OH levels are expected to be relatively sensitive to H-generating reactions. However, the fastest H-producing pathway at these conditions ($\text{H}_2 + \text{OH}$) consumes one OH radical per OH radical generated from the H product via the main branching reaction. Since the rates of these two reactions are the same order of magnitude at these conditions, OH levels are relatively insensitive to this pathway. It is noted, however, that not all H radicals react this way. The reaction with the second highest flux generating H radicals at these conditions is $\text{HCO} = \text{H} + \text{CO}$, to which OH levels were indeed found to be sensitive during ignition. During ignition, OH levels were also sensitive to two important chain terminating reactions, $\text{H} + \text{CH}_3 = \text{CH}_4$ and $\text{C}_2\text{H}_4 + \text{O} = \text{oxirane}$, with a negative sensitivity coefficient (Fig. 9 A). Oxirane (cyclic $\text{C}_2\text{H}_4\text{O}$) is indeed a known isomer on the $\text{C}_2\text{H}_4+\text{O}$ surface.\textsuperscript{56} This experimentally observed but spin-forbidden product forms via intersystem crossing to the singlet surface. At the relatively high temperatures and low pressures considered in this study, reactions via the spin-allowed triplet surface are expected to be formed at rates about 3x higher than the singlet products.\textsuperscript{57} Here, on the other hand, during the automatic exploration of the pressure-dependent network, RMG predicted the spin-
forbidden products (oxirane, CH₅+HCO) to be generated at a rate faster by about 3x than the spin-allowed products (CH₂+CH₂O, and CH₂CHO+H). This branching ratio eventually affects the predicted ignition delay in this system. Teaching machines to correctly predict rates involving intersystem crossing remains a challenge, mainly due to the variable position of the crossing point.

![Figure 9](image)

**Figure 9.** (A) Kinetic and (B) Gibbs Energy change normalized sensitivity coefficients of OH showing top six influential reactions and species during the time ranges 0-100 µs and 200-500 µs.

The ΔG values that affect the concentration of OH the most are of OH, H, species participating in the initiating C–C scission reaction (EA, CH₃, CH₂NH₂), and HCN (Fig. 9 B). The role of the EA C–C scission reaction in the system and its effect on OH was discussed above. The effect of the ΔG value of HCN on the OH levels may stem from the two reactions H₂ + O = H + OH and
HCN + O = H + NCO competing for O radicals; if HCN was more reactive, less OH would form.

In this model, the thermodynamic values of CH₃, CH₂NH₂, and HCN come from CCSD(T)-F12a calculations. The thermodynamic parameters of EA, on the other hand, were taken from Yaws’ Property Data for Chemical Engineers and Chemists handbook; further calculations and the uncertainty of these values are discussed in Section 3.5.

Figure 10. Major reaction pathways in oxidation of EA at 350 μs. Arrow widths correspond logarithmically to respective reactions’ ROP. The diagram captures at least 95% of each species consumption pathways; reaction pathways of species with a total consumption rate lower than 10% of the respective production rate were not explored. Reactions of C₂H₃ with O and OH are not presented for simplicity. Circles highlight the reactive species with highest concentration (as seen in Fig. 7) and their diameter corresponds logarithmically to their concentration.

Figure 10 shows a qualitative flux diagram of significant reactions during ignition (at 350 μs). Four branches that are interconnected by small radical species are shown, each branch stems from one of the high concentration reactive species in the system during ignition, H₂, HCN, NH₃, or C₂H₄. Since EA is an N-containing biofuel model molecule, it is interesting to note its nitrogen transformation routes leading to the formation of benign molecular nitrogen. The major identified pathway forming N₂ involves H abstraction from HNO and subsequent reaction between the
formed NO with NH, yielding N₂O. The latter eventually produces N₂ by reacting with an H atom. NO also forms N₂ by reacting with an N atom.

3.4. Ignition delay

The predicted ignition delay times during EA oxidation were compared to respective experimental shock tube values under stoichiometric conditions at the 1200–1450 K and 0.86–2.03 bar temperature and pressure ranges, respectively, as reported by Li et al.³² (Figure 11). Since the experimental ignition delay measurements were conducted under different composition, temperatures, and pressures than the model reported above, a new mechanism was generated using RMG to be valid at these new conditions. The ignition delay time is defined herein as the time from the start of the simulation to the global maximum of OH concentration.

![Figure 11. Ignition delay times for a stoichiometric mixture (defined by the complete reaction CH₃CH₂NH₂ + 3.75O₂ = 2CO₂ + 3.5H₂O + 0.5N₂) of 1.07% EA and 4% O₂ in Ar for three pressures vs. reciprocal temperature. Experimental and simulated data are denoted by symbols and lines, respectively.](image)

As expected, the ignition delay times in both the model and experimental results decreased as the pressure or temperature increased. The model under-predicted the ignition delay times at low temperatures by up to a factor of three, which is reasonable for an automatically-generated model.
without any refinement, and successfully predicted the high temperature (T ≥ 1400 K) values with a discrepancy lower than a factor of 1.5. The ignition delay time trend with pressure is also in agreement between the model and the experimental values. Overall, the model predictions semi-quantitatively match the experimental results of this global parameter, which supports the model’s reliability.

### 3.5. Updated ethylamine thermodynamic values

Thermodynamic values of EA in the models presented in this work were taken from an RMG library of C\H\N containing species. In this library, the EA $H$ and $C_p$ values were taken from Yaws' Critical Property Data handbook, while the $S$ value was derived from a DFT calculation (Table 3). The Yaws value for $\Delta H_f^o$ differs from the NIST webbook value by ~10 kJ mol$^{-1}$. Since the model’s predictions were relatively sensitive to the $\Delta G_f^o$ values of EA (Figs. 5 B, 9 B), EA thermodynamic values were computed at the CBS-QB3 level, with frequencies and force matrix calculated at the B3LYP/CBSB7 level, and hindered rotors at the M06-2X/cc-pVTZ level. The reported 2$\sigma$ dispersion of the CBS-QB3 method is 13.0 kJ mol$^{-1}$.

All enthalpy values are well within the 2$\sigma$ dispersion of the CBS-QB3 value (Table 3). Constant pressure heat capacity values were similar throughout the different sources (deviated by ~3% or less). Nevertheless, the entropy value from Yaws' Critical Property Data handbook of -0.04 J mol$^{-1}$ K$^{-1}$ substantially deviates from the narrow 283.42–284.0 J mol$^{-1}$ K$^{-1}$ range of all other sources. This egregious disagreement in $\Delta S$ suggests that either Yaws' source was using a different standard state, or that its entropy value is either an unsuccessful estimate, or perhaps an editing error; it also leads to a discrepancy in the calculated $\Delta G_f^o$. 

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It is worth noting that group additivity values were in close agreement with the CBS-QB3 data, emphasizing the advantage of this simple predictive method. It is also noted that the NIST $\Delta H$ is based on the liquid phase standard enthalpy change of formation from a work published in 1907, which has no reported error bars, and the measured enthalpy change of vaporization, which has an uncertainty of $\pm 2$ kJ mol$^{-1}$.\textsuperscript{59}

The CBS-QB3 calculated values are in fair agreement (within 5 kJ mol$^{-1}$) with values used throughout this work (RMG’s C/H/N library), and the minor differences had a modest impact on the model predictions (Fig. 12).

![Figure 12](image)

**Figure 12.** Concentration profiles of NH$_2$ vs. time during pyrolysis of 2000 ppm EA in Ar at 1428 K and 1.23 bar, comparing experimental results, model predictions using the EA thermodynamic values from the RMG CHN library, and model predictions using the EA thermodynamic values from the CBS-QB3 calculation.

4. Conclusions

This work reports the first automatically generated mechanism for pyrolysis and oxidation of an organic nitrogen-containing species. The model was generated using Reaction Mechanism Generator (RMG), an open source software package for automated rate-based mechanism generation. As part of this work, RMG’s thermochemistry groups, kinetic rate rules, and kinetic
libraries were extended to account for reactive nitrogen species. Additionally, RMG was also expanded to recognize two nitrogen resonance classes specific for lone electron pairs.

Pyrolysis and oxidation of ethylamine (EA) were studied, and important reaction pathways in the reaction network were identified. The model was generated for temperature and pressure ranges of 1400–1440 K and 1.2–2.1 bar, respectively, and was in satisfactory agreement with experimental shock tube observations of NH₂ and OH as well as ignition delay times.

The weakest bond in EA is the C–C with a dissociation energy value of 348 kJ mol⁻¹, and the weakest C–H bond is at the α-site with a dissociation energy value of 386 kJ mol⁻¹. During pyrolysis, prior to the establishment of the radical pool, EA decomposition is dominated by the C–C bond scission reaction, while at later times H abstraction at the α-site by H radicals becomes the dominant EA consuming reaction. The H radicals initially originate via β-scission of CH₂NH₂, which is a product of the EA C–C bond scission reaction. At later times H radicals are generated at a higher rate via β-scission of CH₃CHNH₂, which is a product of the EA α-site H abstraction reaction. At early times, NH₂ is formed via the EA C–N bond scission reaction, while after the establishment of the radical pool it is generated via β-scission of the CH₂CH₂NH₂ radical, which is a product of the EA β-site H abstraction reaction.

During oxidation, at first the EA concentration diminishes and four major reactive species are formed, H₂, HCN, NH₃, and C₂H₄. After a chemical delay time the mixture ignites and H₂/O₂ ignition chemistry dominates, accompanied by inflation in the H, O, and OH concentrations. As is typical of high temperature oxidation, the major branching reaction is O₂ + H ⇌ OH + O.

During pyrolysis conditions, N₂ was mainly generated via NH₂ + N, whereas during oxidation its production rate was significantly higher and was mediated by NO and N₂O. Reaction network
diagrams were constructed for pyrolysis and oxidation conditions, illustrating major nitrogen transformation routes and important chain reactions.

The model predictions were found to be relatively sensitive to the EA C–C and C–N scission reactions, as well as to the thermodynamic values of EA. While the latter were calculated as part of this work at the CBS-QB3 level and uncertainty boundaries were given, both scission reactions were estimated by RMG. Although the software was recently trained using high-level calculations for various C–C scission reactions, calculating the rates of these two reactions is expected to improve the agreement between the model and the experimental observables. However, it is worth noting that even without providing accurate rates for these specific reactions or thermodynamic values for EA, RMG’s predictions using existing database libraries, kinetic rate rules, and group additivity values are reasonable and in semi-quantitative agreement with the experimental results.

This new capability of RMG is expected to prove very helpful as the community incorporates nitrogen chemistry in chemical kinetic models. The present work demonstrates the abilities of RMG and its potential to adequately simulate nitrogenous species, as well as be extended to accurately account for other heteroatoms.

Acknowledgments

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Supplementary Material

1. RMG input file
2. Chemkin input file
3. RMG species dictionary (can be interpreted at http://rmg.mit.edu/)

Bibliography


16. Grinberg Dana, A.; Tvil, G.; Winter, L.; Shter, G.E.; Grader, G.S. Pressure effect on the


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<td>Lone electron pair / radical and partial charge</td>
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### Table 2
The EA kinetic library. Parameters are for the modified Arrhenius expression $k = A T^n \exp(-E_a/[RT])$.

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<th>No.</th>
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<th>n</th>
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[a] The ‘−’ sign denotes a double bond, ‘#’ denotes a triple bond.
[b] Units are s$^{-1}$, or cm$^3$ mol$^{-1}$ s$^{-1}$ for first or second order reactions in the forward direction, respectively.
[c] pw – present work, calculated at the CBS-QB3 level.
Table 3 Thermodynamic properties for gas phase EA. Units are kJ mol\(^{-1}\) (\(\Delta H^0\), \(\Delta G^0\)) and J mol\(^{-1}\) K\(^{-1}\) (\(\Delta S^0\), \(C_p\)).

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\[^a\] Calculated as \(\Delta G^0 = \Delta H^0 - T \cdot \Delta S^0\)

\[^b\] Taken from the C/H/N RMG thermodynamic library; used in the EA models presented in this work.

\[^c\] Group additivity values\[^39\] calculated by RMG; these values were not used in this work and are given here for comparison only.