A Dataflow / von Neumann Hybrid Architecture

by

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Submitted in partial fulfillment
of the requirements for the
degree of

Doctor of Philosophy

at the

Massachusetts Institute of Technology

May, 1988

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ABSTRACT

Dataflow architectures offer the ability to trade program-level parallelism in order to overcome machine-level latencies in accessing memory and in communicating with other processors. Dataflow further offers a uniform synchronization paradigm, representing one end of a spectrum wherein the unit of scheduling is a single instruction. At the opposite extreme are the von Neumann architectures which schedule on a task, or process, basis. As a basis for scalable, general purpose multiprocessors, traditional von Neumann architectures are unsuitable due to their inability to tolerate latency and to provide means for fine-grained synchronization.

This thesis examines the spectrum by proposing a new architecture which is a hybrid of dataflow and von Neumann organizations. The analysis attempts to discover those features of the dataflow architecture, lacking in a von Neumann machine, which are essential for tolerating latency and synchronization costs. These features are captured in the concept of a parallel machine language which can be grafted on top of an otherwise traditional von Neumann base. In such an architecture, the units of scheduling, called scheduling quanta, are bound at compile time rather than at instruction set design time. The parallel machine language supports this notion via a large synchronization name space.

It is shown that the combination of dataflow-style explicit synchronization and von Neumann-style implicit synchronization in the same instruction set results in an architectural synergism. Using an instruction set which is strictly less powerful than that of the MIT Tagged-Token Dataflow Architecture (TTDA), the hybrid architecture can exploit the same kinds of parallelism as the TTDA. Given that a compiler can generate scheduling quanta of two or three instructions, the hybrid architecture will execute approximately the same number of instructions as the TTDA. Larger quanta can result in the hybrid actually executing fewer instructions than the TTDA, demonstrating the power of passing state implicitly between program-counter sequenced instructions.

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Key Words and Phrases: architecture, context switching, dataflow, hybrid, I-structure storage, latency, multiprocessor, name space, parallel machine language, process state, split transaction, synchronization, von Neumann
Acknowledgments

This thesis describes research done at the Laboratory for Computer Science of the Massachusetts Institute of Technology. Funding for the Laboratory is provided in part by the Advanced Research Projects Agency of the Department of Defense under Office of Naval Research contracts N00014-83-K-0125 and N00014-84-K-0099. The author is employed by the International Business Machines Corporation.

That being said, I am especially grateful to my thesis supervisor, Arvind, who coached and encouraged me through seven years and six versions of The Two Fundamental Issues. I wish to thank Andrew Chien, David Culler, Bert Halstead, Steve Heller, Greg Papadopoulos, Ken Traub, and other members of the Computation Structures and Parallel Processing Groups for their interest in and enthusiasm for this work. I am grateful to Jack Dennis, Arvind, and Mike Dertouzos for having worked so many years to establish the dataflow research environment of the second floor at Tech Square in which this project was done. I also thank the people of First Presby for their encouragement. In particular, I thank Mike "Rambo" Hale for providing such rewarding (read: time-consuming) distractions from graduate studies. I also wish to thank Lee Howe, Ev Shimp, Bobby Dunbar, Bill Hoke, Lucie Fjeldstad, Frank Moore, Dick Case, Hum Cordero, Bob Corrigan, Carl Conti, John Karkash and my other sponsors at IBM who made this work possible.

I am grateful to my parents and family, especially to my father who provided me with a role model for engineering excellence, and to my mother who in so many ways took an active part in my education. The encouragement and support never stopped, with the possible exception of the time Mom tried to discourage the purchase of my first computer. In retrospect, she must have understood its architectural shortcomings. After all, it wasn’t a multiprocessor.

I am grateful beyond words for the love, concern, encouragement, and support given me by my wife Susan and my son Robbie.

Most of all, I thank my Lord who made the path clear and who guided each step.
Dedication

To Susan and Robbie with all my love.
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Chapter One

Introduction

It has become apparent that the lessons learned in 40 years of designing von Neumann uniprocessors do not necessarily carry over to multiprocessors. Compiler technology coupled with simple pipeline design is now used effectively [36, 48, 49, 51] to cover bounded memory latency in uniprocessors. Unfortunately, the situation is qualitatively different for multiprocessors, where large and often unpredictable latencies in memory and communications systems cannot be tolerated by using similar techniques. This is attributable at the architectural level to poor support for inexpensive dynamic synchronization [8]. Specifically, latency cost is incurred on a per-instruction basis, but synchronization on a per-instruction basis is impractical. A scalable, general purpose multiprocessor architecture must address these issues. Traditional compile time sequencing is too weak a paradigm for general purpose machines (c.f., ELI-512 [29], the ESL Polycyclic processor [50]), and traditional run time sequencing mechanisms are not sufficiently flexible (c.f., The IBM 360 Model 91 [1, 56], the Cray-1 [51]).

Dataflow architectures offer such synchronization at a per-instruction level as the normal modus operandi. Each instance of an instruction can be though of as an independent task with specific dependence requirements which must be satisfied prior to initiation. A dataflow machine provides the mechanism to detect efficiently the satisfaction of these requirements and to process all such enabled tasks. Given the means to express a computation as a graph of such interdependent tasks, one has a natural means for executing, at any instant of time, all and only those instructions for which the synchronization constraints have been satisfied. To the extent that the number of such candidate instructions exceeds by some suitable amount the instantaneous capacity of the machine to process them, latencies inherent in the physical machine can be hidden, or masked. Heretofore, seeking these benefits has implied a significant departure from the von Neumann camp of architectures, leaving a very substantial and important body of knowledge behind.

This thesis offers a framework for understanding the tradeoffs between these two points in the space of computer architectures. The overall goal of this study is to discover the critical hardware structures which must be present in any scalable, general-purpose parallel computer to effectively tolerate latency and synchronization costs. This investigation is based on demonstrating that von Neumann instruction sequencing simplicity and dataflow sequencing generality are but the ex-
trema of a continuum. To explore this continuum, a new architecture is developed as a synthesis of the best features of von Neumann and dataflow ideas. Evaluation of this architecture is based on characterizing the differences in various architectural figures of merit (e.g., number of instructions executed, instruction complexity) between the new machine and the well-studied MIT Tagged Token Dataflow Architecture (TTDA) [10, 18].

Analyses of von Neumann and Dataflow Architecture

Chapter 2 examines the strengths and weaknesses of both the von Neumann and dataflow regimes as bases for a parallel computer. In von Neumann architecture, it is shown that the desire to scale a general-purpose machine from the level of tens to hundreds of processors implies the need for changes in the basic processor architecture. The desire to switch from a single processor to a connection of many introduces unavoidable latencies. The requirement to similarly decompose a single problem into communicating parts implies the need for efficient, fine-grained synchronization. It is shown that von Neumann machines have only a limited ability to deal with the former, and little or no ability to handle the latter.

In a dataflow machine, synchronization is not only available at the lowest hardware levels, it is unavoidable. The key sequencing mechanism in a dataflow machine is based on the matching of names from a large space. Activities, or instances of instructions, are uniquely named. Data for a given instruction are tagged with the activity name. Hardware provides the means for bringing identically-tagged data together and for scheduling the denoted instructions. It is shown that such matching is not strictly necessary in all cases. Moreover, it is shown that in these cases the inability to eliminate such synchronization results in lost locality.

Synthesis of a Hybrid

Chapter 3 presents a new architecture which is developed by taking the essential features of a dataflow machine and integrating them into a von Neumann machine. The notion of a parallel machine language is presented which captures the following key features:

- The instruction set is designed in such a way that instruction execution time is always independent of unbounded latencies.
- Synchronization events are named. Names are drawn from a large space, and names can be manipulated as first-class hardware data types.
- Both explicit and implicit synchronization can be expressed - programs are represented as partial orders of sequential threads.

Two execution models are presented. The first, an idealized model, captures the notion of executing computations expressed in the parallel machine language, but with few other constraints. The number of processors is assumed to be unbounded, and the communication latency is assumed to
be zero. This model provides the means for studying the effects that architectural assumptions have on the behavior of a given program, e.g., the best-case parallelism which can be uncovered. The second model is more realistic. By presenting the high-level design of a realizable processor capable of handling partially-ordered computations, a set of constraints is developed and applied on top of the idealized model. This provides a vehicle for studying the architecture's response to a variety of applications, and a means for evaluating the efficiency of various implementation devices such as operand caches.

**Code Generation**

Chapter 4 considers the issues of compiling code for a hybrid architecture. In the von Neumann world, compilation is complicated by numerous instances of static resource allocation. Doing a good job of this, however, can result in excellent locality i.e., efficient use of high-bandwidth storage and a solidly packed pipeline. In the dataflow world, many of these problems cum opportunities evaporate in the face of implicit management of token storage and the near-zero cost of naming synchronization events. In the hybrid paradigm, compile-time tradeoffs between these two are possible. This significantly complicates the task of generating "optimal" code.

A simple approach is presented for choosing between these two domains. Dependences between instructions are classed as either static or dynamic, the difference being that a dynamic dependence is sensitive to unbounded latency. Instructions are partitioned into chunks called Scheduling Quanta (SQ). All instructions in a given SQ depend, transitively, on the same set of dynamic arcs. Having partitioned a computation thus, von Neumann style sequencing is used within an SQ, and dataflow sequencing is used between them. By this means, latency can be masked by excess parallelism as in a dataflow machine.

**Analysis of the Hybrid Approach**

Chapter 5 presents results of emulation experiments run on the idealized and realistic models, using SQ partitioned code derived from Id program graphs. A comparison is made between the hybrid machine and the MIT Tagged-Token Dataflow Architecture (TTDA). In general, it takes two hybrid instructions to equal the computational power of a TTDA instruction. However, it is shown by experimental result that, given the same program graph, the hybrid machine and the TTDA execute approximately the same number of instructions. By this observation it is posited that the full power of TTDA instructions is not used in general, and that a large fraction of this unused power is attributable to unnecessary synchronization generality in the TTDA.

**Convergent Efforts**
Chapter 6 reviews other related efforts which seek to reconcile, or at least understand, the differences between von Neumann and dataflow architectures. Directions for future research are sketched.
Chapter Two
The Importance of Processor Architecture

Current-day multiprocessors represent the general belief that processor architecture is of little importance in designing parallel machines. In this Chapter, the fallacy of this assumption will be demonstrated on the basis of two issues: latency and synchronization. The argument is based on the following observations:

1. Physical parallelism implies latency for both processor-to-memory and processor-to-processor communications.
2. Latency scales up with the number of processors.
3. Traditional processors employing simple von Neumann style instruction scheduling will idle when executing any instruction which incurs this latency.
4. Attempting to go beyond this limit implies the need for efficient, hardware-level synchronization means.
5. Based on the cost of using such hardware, only certain types of parallelism can be exploited efficiently.

Section 2.1 defines the class of machines which are of interest in this study. In Section 2.2, the shortcomings of von Neumann architecture are explored in more detail. A framework is developed for defining the issues of latency and synchronization. The traditional methods used to reduce the effect of memory latency in von Neumann computers are examined, and their limitations are discussed. A similar discussion of synchronization methods is presented. Section 2.3 looks critically at dataflow architecture and attempts to articulate its strengths and weaknesses. Section 2.4 seeks to compare the two architectures and the types of parallelism which can be exploited. On the negative side, this comparison highlights the inflexibility of the von Neumann approach and shows the inefficiency of the dataflow approach. From a positivist's view, the example focuses attention on the attributes of each existing architecture which one would like to combine into a new architecture.

2.1 Scope
The present discussion pertains specifically to scalable, general purpose parallel computers. "Parallel Computer" denotes a collection of computing resources, specifically, some number of identical, asynchronously operating processors, some number of identical memory units, and
some means for intercommunication, assembled for the purpose of cooperating on the solution of problems. Such problems are decomposed into communicating parts which are mapped onto the processors. "General purpose" means simply that such computers can exploit parallelism, when present, in any program, without appealing to some specific attribute unique to some specific problem domain. "Scalability" implies that, given sufficient program parallelism, adding hardware resources will result in higher performance without requiring program alteration.

The scaling range is assumed to be from a single processor up to a thousand processors\(^1\). Parallelism significantly beyond this limit demands yet another change in viewpoint for both machines and languages.

In the remainder of this thesis, the terms \textit{parallel computer} and \textit{multiprocessor} will be used interchangeably.

2.2 von Neumann Architectures

In this section, it is argued that latency and synchronization are fundamental issues which must be faced by all architects of scalable, general purpose parallel computers. Various mechanisms have been invented to deal with uniprocessor latency and synchronization issues - these are analyzed and are shown to be ineffective in a parallel computer.

2.2.1 Latency and Synchronization

A parallel computer is, by definition, a collection of computing resources. Because the processors and memories in the collection occupy physical space, there will necessarily be limitations on the time to communicate between them. The organization of a parallel computer, therefore, gives rise to communication latency. Similarly, by definition, general purpose parallel computers are to cooperate. Therefore, problems must be logically decomposed into communicating fragments, implying the need for synchronization. These issues are examined in depth in the following sections.

2.2.1.1 Latency: The First Fundamental Issue

Any multiprocessor organization can be thought of as an interconnection of the following three types of modules (see Figure 2-1):

1. \textbf{Processing elements (PE)}: Modules which perform arithmetic and logical operations on data. Each processing element has a single \textit{communication port} through which all data values are received. Processing elements interact with other process-

---

\(^1\)By Bell's metric [11], this is an architectural \textit{dynamic range} of 30 dB.
ing elements by sending messages, issuing interrupts or sending and receiving *synchronizing signals* through shared memory. PE’s interact with memory elements by issuing LOAD and STORE instructions modified as necessary with atomicity constraints. Processing elements are characterized by the rate at which they can process instructions.

2. **Memory elements** (M): Modules which store data. Each memory element has a single communication port. Memory elements respond to requests issued by the processing elements by returning data through the communication port, and are characterized by their total capacity and the rate at which they respond to these requests\(^2\).

3. **Communication elements** (C): Modules which transport data. Each nontrivial communication element has at least three communication ports. Communication elements neither originate nor receive synchronizing signals, instructions, or data; rather, they retransmit such information when received on one of the communication ports to one or more of the other communication ports. Communication elements are characterized by the rate of transmission, the time taken per transmission, and the constraints imposed by one transmission on others, *e.g.*, blocking. The maximum amount of data that may be conveyed on a *communication port* per unit time is fixed.

*Latency* is the time which elapses between making a request and receiving the associated response. The above model implies that a PE in a multiprocessor system faces larger latency in memory references than a uniprocessor does because of the transit time in the communication network between PE’s and the memories. This argument is quite independent of notions of locality and network topology. Given a physical parallel computer, any computation running on

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\(^2\)In many traditional designs, the "memory" subsystem can be simply modeled by one of these M elements. Interleaved memory subsystems are modeled as a collection of M’s and C’s. Memory subsystems which incorporate processing capability can be modeled with PE’s, M’s, and C’s.
it is constrained to occupy nonzero volume, and any communication within that volume is subject to speed-of-light limits.

In a von Neumann processor, memory latency determines the time to execute memory reference instructions. Said another way, von Neumann instruction sets are traditionally designed with instructions whose execution time is latency dependent. When this latency cannot be hidden by some means, a tangible performance penalty is incurred.

2.2.1.2 Synchronization: The Second Fundamental Issue

For the sake of the discussion, call the basic units of computation into which programs are decomposed for parallel execution computational tasks or simply tasks. A general model of parallel programming must assume that tasks are created dynamically during a computation and die after having produced and consumed data. Tasks are made up of a static component, representing program text, and an invocation-specific component representing the state of the computation. Tasks are mapped onto processors and operate in mutual asynchrony.

Synchronization is the time-coordination of the activities within a computation. In a von Neumann machine, instruction execution is implicitly synchronized by the dispatching circuitry, using a program counter for sequential instruction initiation. In a parallel computer, a qualitatively different kind of synchronization is required between tasks due to their assumed mutual asynchrony. Historically, much effort has been devoted both to developing high-level programming primitives (which are inevitably tied to the metaphors of the language) and to designing efficient implementations which rely minimally on specific hardware synchronization features, thus assuring their generality.

One may choose to view the space of high-level primitives a number of ways, but the essential activities involve creation of parallel work, coordination of parallel work, and prevention of parallel work. The following three metaphors illustrate these activities:

1. Fork / Join Parallelism (creation): A task is created as a result of a fork operation, and can run concurrently with the creating task until encountering a join operation. The join enforces synchronization and ultimately results in the termination of the forked task.

2. Producer-Consumer Parallelism (coordination): Given two extant tasks, one task produces a data structure that is consumed by the other. If producer and consumer tasks are executed in parallel, synchronization is needed to avoid the read-before-write race.

3. Mutual Exclusion (prevention): Extant tasks share some serially reusable resource, and means must be provided to guarantee that only one task at a time may have access to it. Because the behavior depends on the time-ordering of requests, non-determinism is implied.
Synchronization involves two or more participants and a common *meeting ground*. The meeting ground has a specific name known to the participants. The meeting ground minimally encodes a single bit of information, and is commonly called an *event* which either has occurred or not. Operationally, a synchronization operation involves testing to see if an event has happened. If it has, the computation may proceed normally. If it has not, some alternative action must occur to prevent the normal computation from proceeding. This may take the form of an enforced busy-waiting for the event which inevitably wastes computing resource. Alternatively, the task making the synchronization test can be put aside to have the test tried again at a later time. Such putting
aside is called context switching in which the task’s private state is evacuated from the processing resource and, optionally, another task’s state is installed. Often, the terms rolling out and rolling in are used to describe this process.

Extant tasks may be viewed as being in one of the following states at any given time: ready-to-execute, executing, or suspended, with state transitions happening at synchronization, scheduling, and context switching points, respectively (see Figure 2-2). Synchronization operations incur two kinds of cost: testing and evacuation. Every synchronization test takes some amount of time. If the test has to be repeated, the cost is, of course, cumulative. Further, in a model which evacuates tasks upon failure of a synchronization test, time will be lost to performing the context switch.

There are several subtle issues in accounting for synchronization costs. Because events are named, synchronization cost should also include the instructions that generate, match and reuse the names. It may not be easy to identify the instructions executed for this purpose. Nevertheless, such instructions represent overhead because they would not be present if the program were written to execute on a single sequential processor.

Another subtle issue has to do with the accounting for intra-task synchronization. Because most high performance computers overlap the execution of instructions belonging to one task, techniques used for synchronization of instructions within the task, e.g., because of pipeline delays at a branch point, are often quite different from techniques for inter-task synchronization. In these cases, busy-waiting in the form of pipeline interlock or the execution of compiled-in NOP instructions is usually safer and cheaper than context switching. This is usually done under the assumption that the idle time will be strictly less than the time to switch tasks. These lost cycles are as much a synchronization cost as are those associated with context switching.

More subtle yet is the cost which arises when the synchronization name space is small (as it usually is in schemes employing registers or interrupt levels as the meeting places). Synchronization name space implies a coupling of two, necessarily efficient mechanisms: the ability to name a meeting place and the ability to enforce synchronizing behavior (e.g., context switching) in testing for an event. In this sense, registers with reservation bits plus an instruction dispatcher which tests the bits represents a synchronization name space. Traditional semaphores in main memory do not. While the name of the meeting place, an address, can be generated cheaply, the enforcing of synchronizing behavior is expensive. The issue of a small synchronization name space is that names themselves are serially reusable resources which must be managed. Often this management is done at compile time, and the cost takes the elusive form of a restricted number of simultaneously pending synchronization events.
In summary, synchronization incurs cost, but the total cost is a function of the efficiency of the mechanism and the degree to which synchronization is used. Unfortunately, in models where the cost is much more than the cost of, say, an arithmetic instruction, these two factors (efficiency and degree of use) are seldom independent. The efficiency function may be highly nonlinear (e.g., the cost of generating and using another synchronization name may be zero until some hardware-specific limit is reached - the cost then becomes infinite). This may result in some reduction in use of the mechanism. In so doing, another cost has been incurred: loss of parallelism.

2.2.2 Processor Architectures to Tolerate Latency

In this section, the changes in von Neumann architectures that have directly reduced the effect of memory latency on performance are described. All of these seek to uncouple memory reference performance from processor performance either by migrating "essential" data to reside within the processor proper (registers, data caches) and/or by hiding memory latency behind an otherwise occupied processor (instruction prefetching, instruction caches, pipelining, LOAD/STORE organization).

Consider the model that either all memory modules in a multiprocessor form one global address space out of which any processor can read any word, or a model in which processors communicate directly with one another via messages, the memories being strictly local to processors. Either model demonstrates that latency means much more than simply "delay," to wit:

- **Latency is Variable**: The time to fetch an operand / communicate a value in a message may not be constant because some memories / processors may be "closer" than others in the physical organization of the machine.

- **Latency Cannot be Bounded**: No useful bound on the worst case time to fetch / send a value may be possible at machine design time because of the scalability assumption.

- **Chaos Arises out of Order**: If a processor were to issue several (pipelined) requests to different remote memory modules / processors in a given order, the responses could arrive in a different order.

Before tackling these very hard problems, the traditional solutions for uniprocessors are examined in some detail. These solutions share the interesting property that solving latency problems invariably introduces synchronization problems.

2.2.2.1 Increasing the Processor State

In the earliest computers, such as EDSAC, the *processor state* consisted solely of an accumulator, a quotient register, and a program counter. Memories were relatively slow compared to the
processors, and thus, the time to fetch an instruction and its operands completely dominated the instruction cycle time; arithmetic performance was incidental.

By investing in some additional high-speed storage, e.g., multiple accumulators, a new game was possible: a computation could be organized to load these accumulators from memory, to perform some computation using only the accumulators, and to store the final results. The increase in processor state meant that, at least for the accumulator-only instructions, instruction execution time could be made independent of the long-latency memory. However, the enlarged processor state still did not help reduce the time lost during memory references and, consequently, did not contribute to an overall reduction in cycle time. Perhaps the most significant effect of increased state was the introduction of index registers which eliminated the need for self-modifying code, bringing an attendant reduction in the total number of instructions executed.

2.2.2.2 Instruction Pre-fetching

The time lost to instruction fetching can be totally hidden, and the cycle time thereby improved, if fetching is done during the execution phase of the previous instruction (pre-fetching). If instructions and data are kept in separate memories, it is similarly possible to overlap some amount of operand fetching as well (The IBM STRETCH [13] and Univac LARC [25] represent two of the earliest attempts at implementing this idea).

Instruction pre-fetching works well only when the execution of instruction $i$ does not have any effect on either the choice of instructions to fetch (as in the case of BRANCH) or the content of the fetched instruction (self-modifying code) for instructions $i+1$, $i+2$, ..., $i+k$. The latter case is usually handled by simply outlawing it. However, effective overlapped execution in the presence of BRANCH instructions has remained a problem. Techniques such as pre-fetching both BRANCH targets have shown little performance/cost benefits. However, the microprogramming trick of delayed BRANCH instructions has been incorporated, with success, in LOAD/STORE architectures. The idea is to delay the effect of a BRANCH by one instruction. Thus, the instruction at $i+1$ following a BRANCH instruction at $i$ is always executed regardless of which way the BRANCH at $i$ goes. One can always follow a BRANCH instruction with a NOP instruction to get the old effect. However, experience has shown that seventy percent of the time a useful instruction can be put in that position.

Operand pre-fetching is subject to similar dependence constraints from previously issued instructions. In sequential code, it is quite common that an operand for instruction $i$ is the result of instruction $i-1$. It is necessary to synchronize these two instructions so as to guarantee that instruction $i$ gets the correct value. One method, called bypassing, is to force the operand prefetch hardware to ignore the value it would have normally fetched and to substitute the value
to be produced by instruction \( i-1 \) when this kind of dependence is detected. A variant on this scheme is to delay the fetching of operands for instruction \( i \) until instruction \( i-1 \) has stored its result. This technique is referred to as interlocking. The attendant delay, or idle time, is commonly called a bubble.

Because overlap is not applicable to all cases of all instructions, an architect must pay the price of increased complexity in terms of synchronization hardware to detect and deal with the special cases, or he must forego these optimizations.

### 2.2.2.3 Instruction Buffers, Operand Caches and Pipelined Execution

The time to fetch instructions can be further reduced by providing a fast instruction buffer, further increasing the processor state. In machines such as the CDC 6600 [55] and the Cray-1 [51], the instruction buffer is automatically loaded with \( n \) instructions in the neighborhood of a referenced instruction whenever the referenced instruction is found to be missing. Similarly, operand fetching can be optimized by providing operand caches which prefetch and store data values which are in the neighborhood of a referenced datum. Both of these techniques rely on locality: because of sequential instruction interpretation, given the execution of instruction \( i \), the next instruction to be executed will be, with very high probability, \( i+1 \). Transitivity further implies the need for \( i+2 \), \( i+3 \), and so on. The probability density function of likely successor instructions, given \( i \), is strongly centered about \( i \) as opposed to being uniformly distributed. Therefore, there is economic value in pre-fetching program text in the neighborhood of a referenced instruction from a slow storage (main memory) into a higher speed buffer in the processor. If many such instructions can be pre-fetched with a single memory reference, the total number of references can be reduced, and the memory access time will become more a function of buffer speed. If the PDF of instructions can be used to infer a similar PDF for the associated operands, operand caches can magnify the main memory's apparent speed for data as well. This class of locality, called spatial locality, relates characteristics of one fetch operation with the characteristics of other fetch instructions. In subsequent chapters, the kindred concept of temporal locality will be exploited. This relates characteristics of one store operation with the characteristics of other fetch instructions (i.e., that a value, once produced, will likely be consumed shortly thereafter).

As each stage of instruction processing is optimized, the natural generalization is to organize the processor as a pipeline, dividing the total instruction execution task into a number of equivalently-sized subtasks, e.g., fetching the instruction from the instruction cache in the first stage, decoding it in the second stage, fetching the operands from the operand cache in the third stage, and so on. The hope is to be able to dispatch instructions with a periodicity (called the pipeline step or beat) equal to the time taken by the slowest pipeline stage, rather than the time taken by the sum of the stages.
Designing a well-balanced pipeline requires that the time taken by various pipeline stages be more or less equal, and that the "things", i.e., instructions, entering the pipe be independent of each other. Obviously, instructions of a program cannot be totally independent except in some special trivial cases. Instructions in a pipe are usually related in one of two ways: Instruction $n$ produces data needed by instruction $n+k$, or only the complete execution of instruction $n$ determines the next instruction to be executed (the aforementioned **branch** problem).

Limitations on hardware resources can also cause instructions to interfere with one another. Consider the case when both instructions $n$ and $n+1$ require an adder, but there is only one of these in the machine. Obviously, one of the instructions must be deferred until the other is complete. A pipelined machine must be able to prevent a new instruction from entering the pipeline temporarily when there is a possibility of interference with the instructions already in the pipe. Detecting and quickly resolving these hazards is very difficult with ordinary instruction sets, e.g., IBM System/370, DEC VAX, or Motorola 680x0, due to their complexity.

A major complication in pipelining complex instructions occurs when the stage time is not strictly bounded, e.g., when memory / communication latency is involved. Even more troublesome is the possibility that responses to such long-latency operations may arrive out-of-order, necessitating some form of synchronization (refer to Figure 2-3).
2.2.2.4 Load/Store Architectures

A variety of instruction sets, pioneered in the 1960s [55], divide instructions into two disjoint classes. In one class are instructions which move data unchanged between memory and high speed registers. In the other class are instructions which operate on data in the registers. Instructions of the second class cannot access the memory. This rigid distinction simplifies instruction scheduling. For each instruction, it is trivial to see if a memory reference will be necessary or not. Moreover, the memory system and the ALU may be viewed as parallel, non-interacting pipelines. An instruction dispatches exactly one unit of work to either one pipe or the other, but never both.

Such architectures have come to be known as LOAD/STORE architectures, and include the machines built by Reduced Instruction Set Computer (RISC) enthusiasts (the IBM 801 [49], Berkeley RISC [48], and Stanford MIPS [36] are prime examples). The design of the instruction pipeline is based on the principle that if an instruction gets past some fixed pipe stage, it should be able to run to completion without incurring any previously unanticipated hazards.

LOAD/STORE architectures are much better at tolerating latencies in memory accesses than are other von Neumann architectures. In order to explain this point, consider a simplified model which detects and avoids hazards in a LOAD/STORE architecture similar to the Cray-1. Assume there is a bit associated with every register to indicate that the contents of the register are undergoing a change. The bit corresponding to register R is set the moment an instruction is dispatched which will update R. Following this, instructions are allowed to enter the pipeline only if they don't need to reference or modify register R or other registers reserved in a similar way (a kind of interlocking). Whenever a value is stored in R, the reservation on R is removed. if an instruction is waiting on R, it is allowed to proceed.

This simple scheme works under the assumptions that registers whose values are needed by an instruction are read before the next instruction is dispatched, and that the ALU or the multiple functional units within the ALU are pipelined to accept inputs as fast as the decode stage can supply them, subject to the other kinds of resource and control flow dependences discussed above.

The benefit is that, to the extent memory fetches can be issued far in advance of the need for the data, the latency incurred in the fetches can be masked behind the execution of other, independent instructions. Herein is the hook: the compiler must be able to discover opportunities for fine-grained parallelism in order to separate the memory references from the instructions which use the fetched data. Said another way, the extent to which this technique can be used to mask latency cost depends critically upon the compiler's ability to uncover instruction level parallelism.
An equally necessary requirement is the synchronization support provided by the machine: reservation bits on processor registers. Assuming that the compiler can detect opportunities for instruction level parallelism, the following problems remain:

- Each fetch requires a target register. Therefore, the degree of parallelism which can be exploited, and the latency which can be tolerated, is bounded by the number of registers. Viewed more abstractly, registers are synchronization names, and the small size of the register set artificially constrains the synchronization name space.

- The instruction set lacks the means for expressing this parallelism - the instruction dispatcher must intuit it dynamically, and must be prepared to deal with bad intuition. Specifically, the instruction dispatcher may very quickly find its hands full of instructions which are not quite ready to execute in the search for those which are.

Some LOAD/STORE architectures have eliminated the need for reservation bits on registers by making the compiler responsible for scheduling instructions, such that the result is guaranteed to be available. The compiler can perform hazard resolution only if the time for each operation \textit{e.g., ADD, LOAD}, is known; it inserts \textit{NOP} instructions wherever necessary. Because the instruction execution times are an intimate part of the object code, \textit{any} change to the machine's structure (scaling, redesign) will at the very least require changes to the compiler and regeneration of the code. This is obviously contrary to the definition of scalable, general-purpose parallel computers.

Current LOAD/STORE architectures assume that memory references either take a fixed amount of time (one cycle in most RISC machines) or that they take a variable but predictable amount of time (as in the Cray-1). In RISC machines, this time is derived on the basis of a cache hit. If the operand is found to be missing from the cache, the pipeline stops. Equivalently, one can think of this as a situation where a clock cycle is \textit{stretched} to the time required. This solution works because, in most of these machines, there can be either one or a very small number of memory references in progress at any given time.

### 2.2.3 Synchronization Methods for Multiprocessing

As discussed above, solving latency problems requires some sort of synchronization mechanism. This section examines the synchronization problem from a different perspective: having decomposed a program into communicating parts, explicit time-coordination is required which is quite independent of latency concerns.

To form the basis for a multiprocessor, a von Neumann engine must support inter-task synchronization in some form, but at what cost and with what granularity? Consider that the cost of any synchronization mechanism will almost certainly dictate the granularity of the tasks lest the machine spend all of its time synchronizing. Once the granularity is determined, so is the exploitable parallelism.
2.2.3.1 Global Scheduling on Synchronous machines

For a given problem on a totally synchronous multiprocessor, it is possible to envision a master plan which specifies operations for every cycle on every processor. An analogy can be made between programming such a multiprocessor and coding a horizontally microprogrammed machine. Recent advances in compiling [28] have made such code generation feasible and have encouraged researchers to propose and build several different synchronous multiprocessors [29, 50]. These machines are generally referred to as very long instruction word (VLIW) machines because each instruction actually contains multiple smaller instructions (one per functional unit or processing element). The strategy is based on maximizing the use of resources and resolving potential run-time conflicts in the use of resources at compile time. Memory references and control transfers are "anticipated" as in RISC architectures, but here, multiple concurrent threads of computation are being scheduled instead of only one. Given the possibility of decoding and initiating many instructions in parallel, such architectures are highly appealing when one realizes that the fastest machines available now still essentially decode and dispatch instructions one at a time.

This technique is effective in its currently realized context, i.e., FORTRAN-based computations on a small number (less than several dozen) of processors. Compiling for parallelism beyond this level, however, becomes intractable. It is unclear how problems which rely on dynamic storage allocation or require nondeterministic and real-time constraints will play out on such architectures. It is clear, however, that this technique can and should be combined with other approaches which address dynamic synchronization.

2.2.3.2 Interrupts and Low-level Context Switching

Almost all von Neumann machines are capable of accepting and handling interrupts. Not surprisingly, multiprocessors based on such machines permit the use of inter-processor interrupts as a means for signalling events (i.e., triggering inter-task synchronization). However, interrupts are rather expensive because, in general, the processor state needs to be saved. The state-saving may be forced by the hardware as a direct consequence of allowing the interrupt to occur, or it may occur explicitly, i.e., under the control of the programmer, via a single very complex instruction or a suite of less complex ones. Independent of how the state-saving happens, the important thing to note is that each interrupt will generate a significant amount of traffic across the processor-memory interface.

In the previous discussion, it was suggested that larger processor state is helpful in reducing latency cost. Observe, however, that the use of interrupts for inter-task synchronization would bid instead for small, easily-switched processor state. Thus, reducing the cost of synchronization by making interrupts cheap would generally entail increasing the cost of memory latency.
Uniprocessors such as the Xerox Alto [60] and the Symbolics 3600 [45] have used the technique of microcode-level context switching to allow sharing of the CPU resource by the I/O device adapters. This is accomplished by duplicating programmer-visible registers, in other words, the processor state. In one microinstruction, the processor can be switched to a new task without causing any state-saving memory references. This dramatically reduces the cost of processing certain types of events that cause frequent interrupts. Few machines have used the idea of keeping multiple task contexts in a multiprocessor setting (one important exception is the HEP, to be discussed in Section 6.3.1) although it should reduce synchronization cost over processors which can hold only a single context.

The limitations of this approach are obvious. High performance processors may have a small programmer-visible state (number of registers) but a much larger implicit state (caches). Low-level task switching does not necessarily take care of the overhead of flushing caches\(^3\). Further, one can only have a small number of independent contexts without completely overshadowing the cost of the ALU hardware.

2.2.3.3 Semaphores

A commonly supported feature for synchronization is an atomic operation to test and set the value of a memory location. A processor can signal another processor by writing into a location which the other processor keeps reading to sense a change. Even though, theoretically, it is possible to perform such synchronization with ordinary read and write memory operations, the task is much simpler with an atomic TEST-AND-SET instruction. TEST-AND-SET is powerful enough to implement all types of synchronization paradigms mentioned earlier. However, the synchronization cost of using such an instruction can be very high because TEST-AND-SET normally implies busy waiting. This results in lost ALU cycles and extra memory references. Implementations of TEST-AND-SET which permit non-busy waiting imply context switching with the attendant expense.

It is possible to improve upon the multiprocessor behavior of TEST-AND-SET by generalizing it to the atomic FETCH-AND-OP as suggested by the NYU Ultracomputer group [26]. The instruction requires an address and a value, and works as follows: suppose two processors, \(i\) and \(j\), simultaneously execute FETCH-AND-ADD instructions with arguments \((A,v_i)\) and \((A,v_j)\) respectively. After one instruction cycle, the contents of \(A\) will become \((A)+v_i+v_j\). Processors \(i\) and \(j\) will receive, respectively, either \((A)\) and \((A)+v_i\), or \((A)+v_j\) and \((A)\) as results. Indeterminacy is a direct consequence of the race to update memory cell \(A\).

\(^3\)However, solutions such as multicontext caches and multicontext address translation buffers have been used to advantage in reducing this task switching overhead, (c.f., the STO stack mechanism in the IBM 370/168).

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Different implementations realize different kinds of savings as a result of using \texttt{FETCH-AND-OP}. The NYU proposal calls for a \textit{combining} packet communication network which connects $n$ processors to an $n$-port memory. If two packets collide, say \texttt{FETCH-AND-ADD(A,v_i)} and \texttt{FETCH-AND-ADD(A,v_j)}, the switch extracts the values $v_i$ and $v_j$, forms a new packet \texttt{(FETCH-AND-ADD(A,v_i+v_j))}, forwards it to the memory, and stores the value of $v_i$ temporarily. When the memory returns the old value of location $A$, the switch returns two values $(A)$ and $(A)+v_j$.

This has the effect of reducing the total number of network packets in transit and of limiting the number of fetch requests converging on a given memory address. Some synchronization situations which would have taken $O(n)$ time can be done in $O(\log n)$ time. It should be noted, however, that one memory reference may involve as many as $\log_2 n$ additions, and implies substantial hardware complexity.

In the Cedar project [44], combining happens in the memory controller. This results in a similar limitation of fetches against an address, but does nothing to reduce network packets. Implementation in software by interpretation is a logically possible third alternative, but realizes little, if any benefit.

In none of these schemes is the issue of processor idle time due to latency addressed. In the worst case, the complexity of hardware support for combining may actually increase the latency to the point of overshadowing the benefits of combining.

\textbf{2.2.3.4 Cache Coherence Mechanisms}

While highly successful for reducing memory latency in uniprocessors, caches in a multiprocessor setting introduce a serious synchronization problem called \textit{cache coherence}. Censier and Feautrier [17] define the problem as follows:

\begin{quote}
\textit{A memory scheme is coherent if the value returned on a \texttt{LOAD} instruction is always the value given by the latest \texttt{STORE} instruction with the same address.}
\end{quote}

It is easy to see that this may be difficult to achieve in a multiprocessor.

Consider a two-processor system tightly coupled through a single main memory. Each processor has its own cache to which it has exclusive access. Suppose further that two tasks are running, one on each processor, and it is known that the tasks are designed to communicate through one or more shared memory cells. In the absence of caches, this scheme can be made to work. If, on the other hand, it happens that the shared address is present in both caches, the individual processors can read from and write to the address and \textit{never} see any changes caused by the other processor. Using a store-through design instead of a store-in design does not solve the problem either. What is logically required is a mechanism which, upon the occurrence of a \texttt{STORE} to location $x$, in-
validates copies of location x in caches of other processors, and guarantees that subsequent LOADs will get the most recent (cached) value. This can incur significant overhead in terms of decreased memory bandwidth.

Solutions to the cache coherence problem center around reducing the cost of detecting the possibility of incoherence, typically by using a logical directory of cached data. Each entry in the directory reflects the state of the associated cache line, e.g., private, read-only, shared, etc. The directory is updated as necessary when lines change state, and can be used to detect the possibility of incoherence. For example, when an attempt is made to write to a shared line, the directory detects the need to inform others to purge their copies. Obviously, a centralized implementation of the directory does not scale. The directory may be distributed, and in some cases the state information can be stored economically as a few extra bits on each cache line. The problem now becomes one of keeping the distributed directory coherent. Many opportunities exist to reduce the amount of coherence-maintaining communication based on the state information (e.g., writing to a cache line marked as private requires no communication), but some nontrivial communication will always be required\(^4\), and the amount of communication will likely not diminish as a machine is scaled. The machine's performance will ultimately be limited by the rate at which directories can process this coherence-maintaining traffic from their peers. Many other schemes have been proposed for handling caches in small-degree multiprocessors such as making caches partially visible to the programmer, allowing explicit state annotation and explicit flushing of lines.

It is worth noting that, while not obvious, a direct trade-off often exists between decreasing the parallelism and increasing the cachable or non-shared data. It is further noteworthy that latency and synchronization are inextricably intertwined here: to reduce latency, caches are introduced. This results in a synchronization problem (coherence). Solutions to the synchronization problem such as implicit and explicit purging of cache lines will result in poorer cache hit rates and increased average latency.

2.2.4 Analysis and Summary

The von Neumann model, by virtue of its simplicity, offers some tremendous advantages. Consider, for example, that given the static structure of a compiled program and nothing more than the value of the program counter during execution, a tremendous amount of information can be deduced, e.g., the satisfaction or lack thereof of data dependences, the termination of predecessor instructions, the non-initiation of successor instructions, and so on. Consider also that a

\(^4\)One exception is the case of embarrassingly parallel applications which decompose into non-communicating tasks.
sequential thread of computation, occupying a pipeline, has, by definition, exclusive access to the entire state of the underlying machinery. This implies that the cost of communicating data values between instructions can be made extraordinarily low, and that the compiler has tremendous leverage in managing the machine state per its own criteria of optimality. Do these facts in any way imply that von Neumann machines should be the basis for scalable, general purpose parallel computing?

Advocates of non-von Neumann architectures (including the author) have argued that the notion of sequential instruction execution is the antithesis of parallel processing. This criticism is actually slightly off the mark. Rather, a von Neumann machine in a multiprocessor configuration does poorly because it fails to provide efficient synchronization support at a level low enough to permit its liberal and free use. Why is this so?

The participants in any one synchronization event require a common ground, a meeting place, for the synchronization to happen. This may take the form of a semaphore [19], a register [51], a buffer tag [56], an interrupt level, or any of a number of similar devices. In all cases, one can simply think of the common ground as being the name of the resource used (e.g., register number, tag value, etc.). The participants also require a mechanism to trigger synchronization action.

When viewed in this way, it should be clear that the number of simultaneously pending synchronization events is bounded by the size of this name space as well as by the cost of each synchronization operation. More often than not, this name space is tied to a physical resource (e.g., registers) and is therefore quite small, thereby limiting support for low level dynamic synchronization. For most existing von Neumann machines, synchronization mechanisms are inherently larger grain (e.g., interrupts) or involve busy waiting (e.g., the HEP5 [41, 53]). Therefore, the cost of each event is quite high. Such mechanisms are unsuitable for controlling latency cost. Moreover, since task suspension and resumption typically involve expensive context switching, exploitation of parallelism by decomposing a program into many small, communicating tasks may not actually realize a speed-up.

It is important to observe that these arguments together favor the alteration of the basic von Neumann mechanism, and not its total abandonment. For situations where instruction sequencing and data dependence constraints can be worked out at compile time, there is still reason to believe that a von Neumann style sequential (deterministic time order) interpreter provides better control over the machine's behavior than does a dynamic scheduling mechanism and, arguably, better

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5The HEP also exhibited several synchronization namespace problems: the register space was too small (2K), there was a limit of one outstanding memory request per process, and there was a very serious limit of 64 user process status words per processor.
cost-performance. It is only in those situations where sequencing cannot be so optimized at compile time, e.g., for long latency operations, that dynamic scheduling and low-level synchronization are called for. One must also keep in mind that, despite any desire to revolutionize computer architecture, von Neumann machines will continue to be the best understood base upon which to build for many years.

2.3 Dataflow Architectures

Dataflow architectures [3, 24, 31, 37] represent a radical alternative to von Neumann architectures because they use dataflow graphs as their machine language [5, 23]. Dataflow graphs, as opposed to conventional machine languages, specify only a partial order on the execution of instructions and thus provide opportunities for parallel and pipelined execution at the level of individual instructions. For example, the dataflow graph for the expression

\[(a\times b) + (c\times d)\]

only specifies that both multiplications be executed before the addition. The multiplications can be executed in any order, even in parallel. The advantage of this flexibility becomes apparent when considering that the order in which \(a, b, c\) and \(d\) become available may not be known at compile time. For example, computations for operands \(a\) and \(b\) may take longer than computations for \(c\) and \(d\).

The instruction execution mechanism of a dataflow processor is fundamentally different from that of a von Neumann processor. Consider the MIT Tagged-Token architecture, as depicted in Figure 2-4. Rather than using a program counter to determine the next instruction to be executed and then fetching operands accordingly, a dataflow machine provides a low-level synchronization mechanism in the form of a Waiting-Matching store which dispatches only those instructions for which data are already available. This mechanism relies on tagging each datum with the address of the instruction to which it belongs and the context in which the instruction is to be executed. One can think of the instruction address as replacing the program counter, and the context identifier as replacing the traditional frame base register. It is the machine’s job to match up data with identical tags and then to execute the denoted instruction. In so doing, a new datum will be produced, with a new tag indicating the successor instruction(s). Thus, each instruction represents a synchronization operation. Note that the number of synchronization names is limited by the size of the tag, which is intentionally large. Note also that the processor pipeline is non-blocking: given that the operands for an instruction are available, the corresponding instruction can be executed without further synchronization.

In addition to the waiting-matching section which is used primarily for dynamic scheduling of
Figure 2-4: The MIT Tagged-Token Dataflow Machine
instructions, the MIT Tagged-Token machine provides a second synchronization mechanism called \textit{I-Structure Storage}. Each word of I-structure storage has two bits associated with it to indicate whether the word is empty, full or has pending read requests. This greatly facilitates overlapped execution of a producer of a data structure with the consumer of that data structure. There are three instructions at the graph level to manipulate I-structure storage. These are \textsc{Allocate}: to allocate an array of \textit{n} empty words of storage, \textsc{I-Fetch}: to fetch the contents of the \textit{i}th word of an array, and \textsc{I-Store}: to store a value in a specified word. Generally, software concerns dictate that a word be written into only once before it is deallocated.

The dataflow processor treats all I-structure operations as \textit{split transactions}. For example, when the \textsc{I-Fetch} instruction is executed, a packet containing the tag of the destination instruction of the \textsc{I-Fetch} is forwarded to the proper address, possibly in a distant I-structure storage module. The actual memory operation may require waiting if the datum is not present, and thus the result may be returned many instruction times later. The key is that the instruction pipeline need not be suspended during this time. Rather, processing of other instructions may continue immediately after \textit{initiation} of the operation. Matching of memory responses with waiting instructions is done via tags in the waiting-matching section.

One advantage of tagging each datum is that data from different contexts can be mixed freely in the instruction execution pipeline. Thus, instruction-level parallelism of dataflow graphs can effectively absorb the communication latency and minimize the losses due to synchronization waits.

In summary, the MIT Tagged Token Dataflow Architecture (TTDA), and other dataflow architectures like it [31, 37], provide well-integrated synchronization at a very basic level. By using an encoded dataflow graph for program representation, machine instructions become self-sequencing. One strength of the TTDA is that each datum carries its own context identifying information. By this mechanism, program parallelism can be easily traded for latency because there is no additional cost above and beyond this basic mechanism for switching contexts on a per-instruction basis.

However, it is clear that not all of the distinguishing characteristics of the TTDA contribute towards efficient toleration of latency and synchronization costs. One very sound criticism is that intra-procedure communication is unnecessarily general. Intuitively, it should not be necessary to create and match tokens for scheduling \textit{every} instruction within the body of a procedure - some scheduling can certainly be done by the compiler, for example, in the evaluation of an arithmetic expression. In a dataflow machine, however, data driven scheduling is \textit{de rigueur}.

The notion of a nonblocking, context-interleaving pipeline is a two-edged sword. It provides the
ultimate flexibility in context switching, but implies that the notion of locality must be reconsidered. Intuitively, given a dataflow pipeline of depth \( n \), the working set size for instruction and operand caches must be on the order of \( n \) times the working set size for the threads of computation which coexist in the pipe. This also implies that the time to execute the instructions in a graph's critical path is \( n \) times the critical path length. One is left to wonder if it might not be possible, even desirable, to optimize this by performing the necessary synchronization explicitly, and relying on more traditional (read: well-understood) mechanisms for instruction sequencing in the remainder of the cases. The uncertainties in this argument are the fraction of time wherein synchronization is necessary, and the complexity of the mechanisms required.

2.4 Comparison of von Neumann and Dataflow Approaches

Given this discussion of von Neumann and dataflow architectures, it is illustrative to consider an example program and to examine the kinds of parallelism which can be exploited under the two models.

Presented below is a simple program called WaveFront. It takes as input an initialization vector of length \( n \). The program allocates a matrix of dimension \( n \times n \), fills in the first row and first column from corresponding elements of the initialization vector, then proceeds to compute the remaining elements as follows: each empty element’s value is the average of three near-neighbor values - the north, west, and northwest. The example is written in Id.
def wavefront edge_vector =
   {l, u = id_bounds edge_vector;
    m = matrix ((l, u), (l, u));
    m[l, 1] = edge_vector[l];
    for i from l+1 to u do
        m[l, i] = edge_vector[i];
        m[i, 1] = edge_vector[i];
    for i from l+1 to u do
        for j from l+1 to u do
            m[i, j] = (m[i-1, j] + m[i, j-1] + m[i-1, j-1]) / 3;
    in
    m};

After having filled in the first row and first column, the computation proceeds as shown in Figure 2-5, with all unfilled cells along any one diagonal being candidates for parallel execution. The available parallelism in an ideal situation as a function of time can be plotted as a parallelism profile\(^6\) (Figure 2-6).

The small blips around \(t=15\) represent initialization of the first row and first column of the array. The bulk of the execution time belongs to the doubly-nested loop which performs the wavefront

---

\(^6\)Parallelism profiles are derived by compiling a program into a dataflow graph of elementary instructions (ADD, I-FETCH, etc.) which preserves only the essential data dependences. The compiled graph is interpreted, with each instruction in the graph taking unit time. Intercommunication latencies are assumed to be zero. At any time step, all and only those instructions which are logically enabled are executed. The profile plots the number of such instructions as a function of time.
Figure 2-7: Available Instruction Parallelism in 15x15 MultiWave

computation proper. As expected, the parallelism rises essentially linearly until the computation diagonal reaches the middle of the array (corresponding to the linear increase in number of elements computed on the wave front). After this point, a corresponding linear decline is seen.

The parallelism exposed here takes a number of forms. While it is beyond the scope and intent of this work to discuss the linguistic underpinnings which make the exposure of parallelism possible, it is useful and instructive to examine the types of parallelism which combine to give the results here:

- At the most basic level, the *expression* in the loop body has a certain amount of parallelism built into it. Given the loop variables *i* and *j*, three elements can be fetched from the two-dimensional array *m* in parallel. Such parallelism is difficult to exploit across processors, but as is discussed later in this thesis, this class of parallelism is essential for keeping the pipeline full in the presence of long latencies.
• At a higher level, multiple instances of the inner loop are active simultaneously. In the compilation scheme used here, procedures are represented as sets of codeblocks. A codeblock may have no more than one loop and, consequently, inner loops are represented as separate codeblocks. Nonstrictness is preserved across an inter-codeblock interface, so invocation and partial computation are entirely possible despite the temporal absence of one or more arguments.

• Higher yet, multiple iterations of the outer loop are concurrently active. It is the outer iteration which spawns multiple inner loop instances.

The dataflow machine which supports I-Structure storage can easily exploit all three forms of parallelism. The dynamic result is that each diagonal is the producer of data consumed by the next diagonal. Moreover, a dataflow machine can exploit additional producer/consumer overlap between multiple, dependent instances of the same program. Consider the MultiWave program below:

```python
def multiwave edge_vector n =
    {m = wavefront edge_vector;
     in
     {for i from 1 to n do
      next m = wave m;
      finally m});
```

Here, the function Wave is similar to WaveFront above, except that the input is the matrix produced by WaveFront instead of an initialization vector, and that the loop body is changed thus:

\[
m[i,j] = (m[i-1,j] + m[i,j-1] + m[i-1,j-1] + previous_matrix[i,j]) / 4;
\]

That is, a dependence has been added: \(m[i,j]\) now also depends upon its previous value. The parallelism profile is shown in Figure 2-7a. When it is realized that a dataflow machine can exploit this parallelism as well, the result is quite remarkable. The peak (and average) parallelisms have simply doubled, and the critical path time has increased a mere 12.4% (c.f., Figure 2-6).

Needless to say, a traditional von Neumann machine would be able to exploit virtually none of this parallelism without significant effort. First of all, the program would have to be expressed differently. In the Id approach, it is quite correct to think the program is giving a definition for the value of each cell, and that the time-ordering of instructions necessary to compute that value is dynamically determined by the dataflow hardware. It is therefore transparent to the programmer.

The point that von Neumann architecture offers a very different paradigm is clearly made if one considers transliterating the Id code to FORTRAN. There, the program becomes a specification of how to compute instead of what to compute. Simply iterating over rows and columns,
FORTRAN semantics would in fact hide the opportunity for inner loop parallelism because there is a data dependence between inner loop iterations (consider the first invocation of the inner loop with \( i=1 \) and \( j=1..u \). Loop interchange won't help in this situation. The program would have to be re-coded to literally express computing the diagonals, with each inner loop instance running along one diagonal. Aside from the aesthetics of doing this, it is hard to argue that such transformations could be done automatically.

Given that the program can be re-coded by some means [4], the question of what kinds of parallelism are exploitable remains. It is conceivable that a compiler could exploit some amount of expression-level parallelism through instruction reordering with the objective of partially masking latency cost. It is also conceivable that inter-iteration parallelism in the inner loop (one iteration corresponding to the computation of one element in a diagonal) could be exploited, say, by the use of vector instructions.

It is difficult to imagine an efficient way, however, of exploiting the outer loop parallelism depicted in Figure 2-7a without further re-coding because of the required fine-grained synchronization. At best, the compiler would have to enforce barrier synchronization at the end of each outer loop iteration before letting the next iteration begin. The effect of such a barrier can be simulated by introducing an inter-iteration dependence on the availability of the lower-right element in the matrix. The not-too-surprising result for two iterations is shown in Figure 2-7b. Given \( n \) iterations over an \( m \times n \) array, the best-case running time is proportional to \( m \times n \). Under the dataflow model (Figure 2-7a), however, the best-case running time is proportional to \( m + n \). The cost of not having fine-grained synchronization support is clear, yet from the criticism of dataflow architectures, the cost of one such type of fine-grained synchronization is also clear.

2.5 Summary
Processor architecture plays a critically important role in the making of a multiprocessor. Dataflow architectures embody something which is sufficient for tolerating low-level latencies while simultaneously providing fine-grained synchronization support to programs decomposed for multiprocessing. While von Neumann machines are clearly superior in the execution of long sequential threads, the inability to provide cheap, fine-grained synchronization has left doubts as to whether von Neumann architecture can reasonably be a basis for building multiprocessors.

The obvious question is can a new architecture be synthesized out of the best features of dataflow and von Neumann architectures which adequately addresses the shortfalls of both? Arvind has suggested that an architecture formed on the principles of split transaction I-Structure memory references in a von Neumann framework, coupled with data driven rescheduling of suspended instructions would be interesting. Such a machine has the potential of tolerating memory latency
and of supporting fine-grained synchronization and yet, in the strict sense, is neither a von Neumann machine nor a dataflow machine. In the next chapter, the question of synthesis is explored.
Chapter Three
A Dataflow / von Neumann Hybrid

3.1 Synthesis

In the previous Chapter, it was concluded that satisfactory solutions to the problems raised for von Neumann architectures can only be had by altering the architecture of the processor itself. It was further observed that dataflow architectures do address these problems satisfactorily. Based on observations of the near-miss behavior of certain von Neumann multiprocessors (e.g., the Denelcor HEP [41, 53]), it is reasonable to speculate that dataflow and von Neumann machines actually represent two points on a continuum of architectures. The goal of the present study is to develop a new machine model which differs minimally from the von Neumann model, yet embodies the same latency and synchronization characteristics which make dataflow architectures amenable to parallel processing.

Starting with the observation that the costs associated with dataflow instruction sequencing in many instances are excessive, others have suggested that dataflow ideas should be used only at the inter-procedural level [43] thereby avoiding dataflow inefficiencies while seemingly retaining certain advantages. This view is almost correct, but ignores the importance of the fundamental issues. Restricting architectures to this "macro dataflow" concept would amount to giving up what is possibly a dataflow machine's biggest feature - the ability to context switch efficiently at a low level to cover memory latency.

Given this, one is led to ask the following question: what mechanisms at the hardware level are essential for tolerating latency and synchronization costs? Based on various studies of parallel machines [2, 14, 22, 41] and on the observations presented thus far, the following conclusions are drawn:

- In general, on a machine capable of supporting multiple simultaneous threads of computation, executing programs expressed as a total ordering of instructions will incur more latency cost than will executing a logically equivalent partial ordering of the same instructions. In fact, for any lenient programming language [59], expressing programs as a partial ordering is a necessary condition for avoiding deadlock. It is assumed, therefore, that the machine language of any scalable, general purpose parallel computer must be able to express partial ordering.

- In any multiprocessor architecture, certain operations will take an unbounded amount of time to complete (e.g., those involving communication). Such operations can be
either atomic, single phase operations or split transaction, multiphase operations\textsuperscript{7}. Multiphase processing will always minimize latency cost over single phase processing because the potential exists for covering processor idle time. Based on the frequency of the occurrence of such long latency operations [2] in all but the most trivial parallel computations, efficient multiphase operation requires specific hardware mechanisms [7, 22].

The proposed architecture embodies these beliefs and reconciles the criticisms of von Neumann and dataflow architectures. Such an architecture is characterized by its machine language which can be viewed as a superset of both von Neumann and dataflow machine languages. In the sequel, the term \textit{parallel machine language} (PML) will be used to describe this superset. A proper PML must have the following characteristics:

- The execution time for any given instruction must be independent of latency. Traditional latency-sensitive operations, \textit{e.g.}, \texttt{LOAD}s from memory, are re-phrased as \textit{split transactions} which separately initiate an operation and later explicitly synchronize on the availability of the result.

- Each explicit synchronization event must be named. Names must be drawn from a large name space and it must be possible to manipulate the names as first-class hardware data types.

- Means for expressing both implicit (\textit{i.e.}, program counter based) and explicit (named) synchronization must be provided.

The remainder of this chapter is devoted to the definition of a PML (Section 3.2) and to the definition of a concrete architecture which executes it efficiently (Section 3.3).

\textbf{3.2 Compilation Target Model}

In this section, the notion of a parallel machine language is introduced as the basis for any reasonable general-purpose programming model. Such a language provides a metaphor for parallel threads of activity which must encompass means for \textit{naming} parallel threads and means for time-coordinating, or \textit{synchronizing} the threads. A key idea is that the thread size should not be bound by the parallel machine language but rather that the machine language should support threads of arbitrary size in a completely general way.

While the focus of this work is not on languages and compilers for general purpose parallel computers, it is convenient to make use of extant languages and tools for the purpose of assisting in the development and characterization of the architecture. To that end, Id and its compiler have been used in this study. This choice has brought with it certain complications (discussed later),

\footnote{\textit{A multiphase} operation is one which can be divided into parts which separately \textit{initiate} the operation and later \textit{synchronize} prior to using the result.}

41
but provides a flexible vehicle for generating dataflow graphs from a high level language. Because of their generality, dataflow graphs are assumed as the preferred starting point in generating PML code. The approach will be to consider how dataflow graphs can be re-represented so as to express implicit and explicit synchronization.

### 3.2.1 A Suitable Program Representation

Sequential execution of parts of a dataflow graph is a clear departure from the dataflow model. While a dataflow graph expresses a partial ordering of instructions, the idea of sequential interpretation implies some additional mode of representation. It becomes desirable to map a dataflow graph into a partial ordering of threads or totally ordered clusters of instructions where such clustering can be shown to improve execution efficiency by some measure.

**Definition 3-1:** An instruction cluster is a nonempty set of instructions.

**Definition 3-2:** A partition of a dataflow graph is a mapping of each instruction in the graph to exactly one cluster.

Providing an architectural notion of clustering is a step beyond both dataflow and von Neumann architectures. In the dataflow paradigm, each instruction is its own cluster. In the von Neumann case, at least with conventional languages, the entire compiled program is the cluster.8

It is reasonable to hypothesize that the clustering methodology should not be bound by the architecture as it is in both the dataflow and von Neumann cases. Rather, clustering should be left as a degree of freedom for the compiler, and the architecture should provide explicit support for this. That is, an architecture should not be judged on its stated clustering methodology but rather on its support for a variety of methods (sequential, fine-grained parallel, coarse-grained parallel, etc.). Such an architecture must, therefore, simultaneously support efficient sequential threads of execution and multiple execution contexts with minimal costs for naming and synchronizing. In the dataflow execution model, each instruction has a static identity (instruction number within a given compiled procedure) and, when the procedure is invoked, a set of dynamic identities (based on invocation instance). In the hybrid model, a similar distinction is made.

**Definition 3-3:** A scheduling quantum (SQ) is a compiler-identified instruction cluster in which a total ordering is imposed on the instructions. Each SQ belongs to exactly one compiled procedure. The first instruction in an SQ is said to name the SQ.

---

8 Compiling dataflow graphs derived from functional languages for a von Neumann machine will force the issue in that clusters will in many cases have to be much smaller than the entire program. This will imply some sort of interpretive mechanism to schedule the clusters with the attendant overhead.

9 As described by Traub [59], such a mechanism may well serve other purposes and is justifiable as a means for supporting the class of lenient programming languages.
Definition 3-4: A *continuation* is a dynamic (run-time) object which denotes an instance of an SQ, that is, its instruction text plus its instance-specific state.

The term *thread* has been used loosely, and its definition can now be made slightly more precise. In a static context, the term refers to an SQ. Dynamically, the term refers to a continuation.

3.2.2 Support for Synchronization

Synchronization in the von Neumann architecture is both a very old and a relatively new notion. In the strictest sense, synchronization has always been necessary for correct operation - operands must always be created before they are consumed. However, under sequential execution semantics, synchronization is implicit in instruction ordering. Having concluded that programs should be expressed as SQ’s invalidates this assumption, and explicit means must be provided. In general it is not possible to impose a total ordering on a set of SQ’s (this in essence is von Neumann instruction sequencing, and with lenient programming languages such as Id may lead to deadlock). SQ sequencing can only be determined at run time.

Architectural support for synchronization and scheduling of SQ’s depends on a number of issues, but the most basic is that of *strictness*. Within any arbitrary cluster of instructions, it is possible (likely) that the total input requirement for the SQ will exceed that of the first instruction. The architecture may provide *strict* scheduling where all SQ inputs must be present prior to invoking the SQ, or *nonstrict* scheduling where invocation is based solely on the requirements of the instruction to be executed next. The former case is explored by Buehler and Ekanadham [15]. It seems likely that, given a set of synchronization requirements and the need to express these succinctly, support for strict scheduling will result in a larger number of smaller SQ’s than will nonstrict scheduling. This conjecture follows from the observation that it is not possible to transform a nonstrict partition into a strict one simply by moving all synchronizations to the beginning of a thread without introducing the possibility of deadlock. It will be necessary to split the larger, nonstrict threads into separate smaller ones at the intermediate synchronization points. Moreover, given a nonstrict scheduling mechanism, the compiler can choose to partition so as to mimic the behavior of strict scheduling. For the sake of this study, then, the more general nonstrict scheduling policy is assumed. It is further assumed that synchronization overhead, whatever the mechanism, is efficient to the extreme of not being a first-order concern in code generation. Moreover, it is assumed that a large, global synchronization namespace is available, and that the cost of allocating names from this space is also negligible\(^{10}\).

The instruction firing rules under this scheduling discipline must guarantee that instructions do

\(^{10}\)In later chapters, these assumptions will be tested.
not execute until the required inputs are present. In a dataflow machine, this simply means that appropriate tokens (operands) must arrive on all input arcs in order for an instruction to fire, and the detection of arrival is a run-time action taken by the hardware. In a machine which supports clusters of instructions, the constraint of operand arrival must still be satisfied. However, the hardware behaves somewhat differently than a dataflow machine, and seeks to distinguish operands on the basis of their origin, for only some of them require synchronization at run time. Having partitioned a graph into a set of nontrivial SQ's\footnote{A trivial SQ contains no instructions or has no input/output dependence relationships with other SQs.}, it is possible to distinguish different type of arcs as follows:

**Definition 3-5**: A *static unsynchronized arc* is any explicit arc between two instructions in the same SQ.

For such arcs, the sequencing constraint can be satisfied via proper instruction ordering within the SQ. That is, sequential execution within the SQ captures the ordering constraint of the arc, and no run time synchronization is necessary.

**Definition 3-6**: A *static synchronized arc* is any explicit arc between two instructions in different SQ's.

For such arcs, the sequencing constraint can only be satisfied, in general, by some dynamic mechanism in that SQ executions are not totally ordered. There are interesting special cases of arcs crossing SQ boundaries which do not require run time synchronization; these will be discussed in Section 5.2.2.

While not expressed explicitly in a dataflow program graph, there is an implicit *dynamic arc* between every I-STORE instruction and I-FETCH instruction which refer to the same structure and element. The arc is properly drawn from the output of the I-STORE to the input of the I-FETCH only in the sense that the output of the I-FETCH appears, at the graph level, to be strict in this "input." However, the desired behavior of I-FETCH, as discussed below, is that the fetch operation itself should not depend upon the state of the slot (e.g., Empty) from which a value is being fetched. I-FETCH should merely initiate the fetching, and some kind of synchronization mechanism must guarantee that instructions to receive the result of the fetch do not execute until the value is indeed available. Hence, the arc from the I-STORE is *gated* by the execution of the I-FETCH, as depicted in Figure 3-1.

Every instruction which exhibits this kind of implicit, synchronizing behavior will be treated specially:

**Definition 3-7**: A *FETCH-like output* of an instruction is one which gates a dynamic arc connecting an I-STORE with the sink instruction which receive its value. An instruction itself is FETCH-like if at least one of its outputs is FETCH-like.
As shall become clear below, a FETCH-like output is an abstraction of a synchronized, long-latency operation. The actual dynamic arc begins at the I-STORE, and terminates at the virtual gate. A static arc connects the virtual gate to each sink instruction. There is, clearly, a one-to-one correspondence between these arcs and the actual arcs in the graph which connect I-FETCH instructions to the sinks. These arcs have particular significance:

**Definition 3-8:** A dynamic synchronized arc is any arc which connects a FETCH-like output to a sink instruction.

The problem of managing synchronized arcs is analogous to the problem of coordinating producers and consumers at a higher level by the use of I-structure storage [34]. The idea is to associate state bits with each slot in such a storage which indicate written or unwritten status. When written, read operations perform as in a normal memory. When unwritten, read operations are deferred; operationally, the read request itself is stored in the offending slot to wait for a write request to come along. When this happens, the deferred read request is satisfied by forwarding the newly arrived value. Significant time may elapse between arrival of the read request and arrival of the write request. This is of no consequence to the I-structure storage unit per se. In the event that multiple read requests must be deferred, a list is created and associated with the slot. This causes practical, but not conceptual, problems. Engineering solutions depend on the statistics of list length which is related to a number of factors.

This idea can be applied to the problem of synchronizing SQ invocations as follows: with each invocation of a procedure is associated a frame of slots. A slot is provided for the output of each
Each slot has I-structure-store-like behavior in that the slot has status bits indicating its emptiness or fullness. Fetching from an empty slot causes the associated continuation to enter the suspended state. A subsequent store operation into the slot causes the suspended continuation to enter the enabled state. Like I-structure storage, values may be fetched repeatedly. Fetching does not, in general, reset the status bits.

Continuations can be thought of as being in one of the following states (Figure 3-2):

{ Uninitiated, Enabled, Active, Suspended, Terminated }

Upon initiation, a continuation becomes Enabled. Enabled continuations compete for processor resources, and eventually become Active when scheduled. When an Active continuation encounters a synchronization blockage, its state changes to Suspended. Upon satisfaction of the synchronization blockage it again becomes Enabled. A continuation may be suspended a number of times between initiation and termination. One can think of a continuation as behaving like a more traditional task in a demand paged system which, upon encountering a missing memory page, becomes suspended until the page is made available.

### 3.2.3 Latency

With this powerful hardware-level synchronization technique, it is straightforward to devise a method of tolerating long latencies. Dynamic synchronized arcs represent the instances of latencies which cannot be bounded at compile time, and always occur at the outputs of instructions which initiate long latency operations. Within the von Neumann paradigm, it is most commonly the case that such long latencies are imbedded in instructions and directly result in processor idle time (Figure 3-3). In order to prevent long latencies from causing the processor to idle, the following is assumed:

---

12While not considered here, re-use of slots within an invocation is possible. The problem is similar to that of re-using registers with the exception that reference patterns are often not statically determined.
Proposition 3-9: Dynamic synchronized arcs must never occur within a non-preemptible unit of execution, and may only exist between such units of execution.

In a von Neumann machine, this condition is violated because instructions are in general non-preemptible\(^\text{13}\) and may contain dynamic synchronized arcs, \textit{e.g.}, \texttt{LOAD}.

Thus, the proposition can be narrowed to say that dynamic synchronized arcs must never occur inside an instruction. That is, instruction execution time must never be a function of the long latency. This is most easily guaranteed by splitting all instructions with imbedded dynamic arcs into two parts which separately initiate and then synchronize. In the case of \texttt{LOADing} a value from a remote memory unit, one instruction would simply initiate the \texttt{FETCH} without waiting for the value to arrive. It would then be the responsibility of any instructions which use the \texttt{FETCHed} value to synchronize, or check for its presence, before proceeding. Such instructions are commonly called split transactions.

In the context of the present discussion, it is useful to view these arcs as hinge-points between

\(^{13}\)There are certainly exceptions to this rule. The IBM System/370 architecture [39] recognizes that system integrity is a function of bounded I/O interrupt response time and, therefore, instructions which may run for a long time, \textit{e.g.}, Move Long (\texttt{MVCL}), are specified as being \textit{segmentable} at well-defined intermediate points in their execution. The time between such segment boundaries is typically much longer, \textit{e.g.}, 256 memory cycles, than what is being considered here.
units of execution (SQ's). Specifically, it is logical to push the unbounded latencies so that they occur *between* rather than *within* SQ's. The intuition is that while SQ A may initiate a number of long-latency operations, in order to mask the effect of latency, the consumers of the long-latency results *must* be asynchronous to A. This notion will be refined in Chapter 4. In this way, the proposition may be phrased that dynamic synchronized arcs must never occur inside an SQ. The partitioning of a graph must in some way be based on the dynamic synchronized arcs within it.

It is therefore assumed that all long latency instructions will be split transactions. In this model, the initiating instruction causes enough information to be sent, say, to the memory subsystem so that the result can be sent back and stored into an appropriate frame slot. Any attempt to use the value prior to its arrival in this slot will result in suspension as described above. Note that the remote storage unit itself need not be an I-structure store for this mechanism to work properly.

### 3.2.4 Overview of the Model

The compilation model proposed herein is intended to be representative of a variety of von Neumann machines, to which one might add mechanisms for dealing with SQs. The machine executes a three-address instruction set, with operands fetched from frame slots and/or a set of registers. Scalar results are stored into frame slots and/or registers. Registers are *not* part of the private state of the invocation but rather are shared across invocations. This is significant in that the architecture assumes no automatic save/restore facility and, therefore, registers cannot be used to hold computation state across potential suspensions.

#### 3.2.4.1 Hardware Types

While specifics of hardware datatypes and number systems are somewhat orthogonal to the architectural issues of interest in this thesis, it is difficult to make convincing arguments about performance and efficiency without taking some stand on many of these. For this reason, the following assumptions are made. While it was expedient in the implementation of arithmetic to assume that types are explicitly represented at the hardware level\(^{14}\), this issue is unimportant for the points to be made and can be ignored. That is, while each instruction's operand types are explicitly defined, the architecture under study takes no stand on the issue of hardware typing.

The following *hardware types* are defined. Each is a word-sized object which can fit into a register or local memory slot:

---

\(^{14}\) In the results presented herein, the *only* form of autocoercion actually used is for numbers (*integer* and *floating-point number*) and is defined more precisely in [6].
Integers (INT): Two’s complement encoding.
Floating Point Number (FP): Encoding of a signed number expressed as a mantissa and a signed exponent. The representation is not significant for this investigation.
Boolean (BOOL): Encoding of boolean TRUE and FALSE. Again, the actual representation is of little significance.
Codeblock (CB): A pointer to a codeblock in program memory.
I-Structure Descriptor (ISD): A pointer to an I-Structure in global I-Structure storage which also encodes the bounds of the structure.
I-Structure Address (ISA): A pointer to an element in global I-Structure storage.
Instruction Address (INSTR): A pointer to an instruction in a loaded codeblock.
Closure Descriptor (CD): An encoding of a codeblock pointer, an integer arity, an integer number of arguments as yet unspecified, and the I-Structure address of the argument list.
Frame Descriptor (FD): A pointer to a frame in frame storage.
Iteration Descriptor (ID): A tuple of a program counter, two boolean flags and three index offsets used to implement the k-bounded loop schema, described in detail in section 4.3.5. Format is

< PC FLAGS P C N>

where P, C, and N are the index offsets denoting areas in the frame for the previous, current, and next iterations respectively.

Continuation Descriptor (CD): A tuple containing a pointer to the next instruction to be executed (program counter), a pointer to a frame base, and three index registers. The format is strongly similar to that of an iteration descriptor:

< PC FBR P C N>

The Arithmetic pseudo-type (ARITH) is used notationally to indicate an INT, FP, or BOOL as will be clear from the context. The Any pseudo-type (ANY) is used notationally to indicate any hardware type. These meta-types are not meaningful at the hardware level.

3.2.4.2 Name Spaces

Code is to be compiled, named, and loaded on a per-codeblock basis. No limit is assumed on the size of a codeblock, nor is a limit assumed on the size of program, I-Structure, or frame memories. The register namespace is, however, assumed to be finite and small.
3.2.4.3 Instruction Set

The instruction set is simple and regular in structure, with addressing modes and instruction functions being largely orthogonal.

3.2.4.3.1 Addressing Modes

The basic addressing modes are

- **Immediate**: a literal value small enough to be encoded directly in the instruction.

- **Register**: The registers are a small, fixed size array of words which provide no synchronization capability, nor are their values guaranteed to persist across potential suspensions\(^{15}\).

- **Frame Direct**: The Frame is an array of words (slots) whose size is determined at compile time for each procedure. A procedure may only access its own frame slots. Each slot has several presence bits associated with it. The frame holds the state of an invocation. Frame Direct addressing specifies an offset from the frame base to select a slot. The Frame addressing mode has two important sub-modes:

  - **Suspensive**: FETCHing with this mode causes the presence bits to be checked and, if no value is present, the current continuation is suspended as described above.

  - **Nonsticky**: Successful execution of an instruction which has performed a FETCH in nonsticky mode will cause the presence bits to be reset, \(i.e.,\) to indicate the slot is now empty.

- **Frame Indexed**: This mode is identical to Frame Direct mode save that the slot is addressed by adding the specified slot number to the frame base plus one of the three index offsets in the continuation. Suspensive and Nonsticky submodes are available here as well.

Unless otherwise noted, input operand addressing may use immediate, register, frame direct, or frame indexed modes. Output operand addressing may use register, frame direct, or frame indexed modes.

3.2.4.3.2 Instructions

The instruction set being used as the compilation target is intentionally unspectacular with the possible exception of the iteration, forking, and closure support instructions which will be

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\(^{15}\)Intuition leads one to believe that such a scheme results in degraded performance in the form of additional memory references for loading and unloading registers. As shall become clear in a later section, this is an oversimplification because frame storage can be cached easily without a coherence problem.
<table>
<thead>
<tr>
<th>Instruction Syntax</th>
<th>Operand Types</th>
<th>Comments</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>NOT</strong> DEST, SRC, etc.</td>
<td>ARITH⇒ARITH</td>
<td>monadic arith/logical</td>
</tr>
<tr>
<td><strong>ADD</strong> DEST, SRC, SRC, etc.</td>
<td>ARITH×ARITH⇒ARITH</td>
<td>dyadic arith/logical/reational</td>
</tr>
<tr>
<td><strong>MOVE</strong> DEST, SRC</td>
<td>ANY⇒ANY</td>
<td>intra-inovation data movement</td>
</tr>
<tr>
<td><strong>MOVR</strong> DINDX, SRC, SRC, SRC, SRC</td>
<td>FD×ANY×INT⇒∅</td>
<td>inter-inovation data movement</td>
</tr>
<tr>
<td><strong>LOAD</strong> FDEST, SRC, SRC, SRC, SRC</td>
<td>ISD×INT⇒ANY</td>
<td>indexed I-Fetch to a frame slot only</td>
</tr>
<tr>
<td><strong>STOR</strong> DEST, SRC, SRC, SRC, SRC</td>
<td>ISAXANY⇒BOOL</td>
<td>unindexed I-Store with signal</td>
</tr>
<tr>
<td><strong>IXCC</strong> DEST, SRC</td>
<td>INT⇒FD</td>
<td>compute new frame base from current</td>
</tr>
<tr>
<td><strong>IXSA</strong> DEST, SRC, SRC, SRC</td>
<td>ISDXINT⇒ISA</td>
<td>compute structure element address</td>
</tr>
<tr>
<td><strong>IXID</strong> DEST, SRC, SRC, SRC</td>
<td>ID×INT⇒ID</td>
<td>compute iteration descriptor</td>
</tr>
<tr>
<td><strong>STRP</strong> SRC</td>
<td>INT⇒∅</td>
<td>set previous iteration offset in AC</td>
</tr>
<tr>
<td><strong>STCR</strong> SRC</td>
<td>INT⇒∅</td>
<td>set current iteration offset in AC</td>
</tr>
<tr>
<td><strong>STNX</strong> SRC</td>
<td>INT⇒∅</td>
<td>set next iteration offset in AC</td>
</tr>
<tr>
<td><strong>STIM</strong> DEST, SRC, SRC, SRC, SRC</td>
<td>ID×BOOL⇒ID</td>
<td>set/reset TMP; conditionally queue</td>
</tr>
<tr>
<td><strong>STPC</strong> DEST, SRC, SRC, SRC, SRC</td>
<td>ID×INSTR⇒ID</td>
<td>set PC and CNTL; conditionally queue</td>
</tr>
<tr>
<td><strong>RST1</strong> SRC</td>
<td>ANY⇒∅</td>
<td>reset frame presence bits</td>
</tr>
<tr>
<td><strong>RST2</strong> SRC, SRC, SRC, SRC, SRC, SRC</td>
<td>ANY×ANY⇒∅</td>
<td>reset frame presence bits</td>
</tr>
<tr>
<td><strong>TST1</strong> DEST, SRC</td>
<td>ANY⇒BOOL</td>
<td>test frame presence bits with signal</td>
</tr>
<tr>
<td><strong>TST2</strong> DEST, SRC, SRC, SRC, SRC, SRC</td>
<td>ANY×ANY⇒BOOL</td>
<td>test frame presence bits with signal</td>
</tr>
<tr>
<td><strong>TGST0</strong> SRC, SRC, SRC, SRC, SRC, SRC</td>
<td>ID×INT⇒∅</td>
<td>test loop termination</td>
</tr>
<tr>
<td><strong>BR</strong> TARGET</td>
<td>INSTR⇒∅</td>
<td>unconditional branch</td>
</tr>
<tr>
<td><strong>BRF</strong> SRC, SRC, TARGET</td>
<td>BOOL×INSTR⇒∅</td>
<td>branch if FALSE</td>
</tr>
<tr>
<td><strong>BRT</strong> SRC, SRC, TARGET</td>
<td>BOOL×INSTR⇒∅</td>
<td>branch if TRUE</td>
</tr>
<tr>
<td><strong>BRNZ</strong> SRC, SRC, TARGET</td>
<td>INT×INSTR⇒∅</td>
<td>branch if ≠0</td>
</tr>
<tr>
<td><strong>BRZ</strong> SRC, SRC, TARGET</td>
<td>INT×INSTR⇒∅</td>
<td>branch if =0</td>
</tr>
<tr>
<td><strong>CINT</strong> SRC, SRC, TARGET</td>
<td>INSTR⇒∅</td>
<td>fork a new continuation</td>
</tr>
<tr>
<td><strong>CNTT</strong> SRC, SRC, TARGET</td>
<td>ANY×INSTR⇒∅</td>
<td>fork a new continuation, test slot</td>
</tr>
<tr>
<td><strong>MKIC</strong> DEST, SRC</td>
<td>INT⇒ISD</td>
<td>allocate a CONS cell of given kind</td>
</tr>
<tr>
<td><strong>MKIS</strong> DEST, SRC, SRC, SRC, SRC, SRC</td>
<td>INT×INT⇒ISD</td>
<td>allocate an I-Structure w/ bounds</td>
</tr>
<tr>
<td><strong>MKIV</strong> DEST, SRC, SRC, SRC, SRC, SRC, SRC</td>
<td>INT×INT⇒ISD</td>
<td>allocate a vector wrapper bound and kind</td>
</tr>
<tr>
<td><strong>GETC</strong> DEST, SRC</td>
<td>CB⇒FD</td>
<td>allocate an invocation context</td>
</tr>
<tr>
<td><strong>RET</strong> DEST, SRC</td>
<td>FD⇒BOOL</td>
<td>deallocate an invocation context</td>
</tr>
<tr>
<td><strong>CARR</strong> DEST, SRC</td>
<td>CD⇒INT</td>
<td>closure’s number of arguments remaining</td>
</tr>
<tr>
<td><strong>CARC</strong> DEST, SRC</td>
<td>CD⇒INT</td>
<td>closure’s arity</td>
</tr>
<tr>
<td><strong>CCGH</strong> DEST, SRC</td>
<td>CD⇒CB</td>
<td>closure’s codeblock identifier</td>
</tr>
<tr>
<td><strong>CCHG</strong> DEST, SRC</td>
<td>CD⇒ISD</td>
<td>closure’s argument chain pointer</td>
</tr>
<tr>
<td><strong>CMCD</strong> DEST, SRC, SRC, SRC, SRC</td>
<td>CD×ISD⇒CD</td>
<td>build a new closure</td>
</tr>
<tr>
<td><strong>CRDY</strong> DEST, SRC</td>
<td>CD⇒BOOL</td>
<td>test a closure for application</td>
</tr>
</tbody>
</table>

Described and justified below. The instruction set has the following notable characteristics:

- Each instruction produces, at most, a single explicit result. Instruction outputs represent registers or frame slots within a given execution context. All other "outputs" are viewed as side effects.

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16Given the goal of making cogent comparisons to the TTDA, two instruction set design issues were taken as constraints. First, the TTDA claims that closures can be represented as objects no bigger than a floating point number. Consequently, closure manipulating instructions are of the same complexity as ADD. Second, resource management instructions represent calls to a manager, the instructions of which are not counted. Hence, manager ops (marked with a superscript M) and closure ops (marked with a superscript C) are implemented and counted as single instructions.
• Each instruction is simple enough to be executed in a single cycle, modulo the costs of operand references which are discussed in detail in Section 3.3. There are no long-latency instructions.

There are primitive instructions for the usual set of arithmetic and logical operations plus the usual complement of relational. The MOVE opcode encodes all intra-invocation data movement. The MOV R (MOVE Remote) opcode is used for procedure linkage, and is the only way one procedure can store into another's frame. There is no sanctioned way for one procedure to directly read from another's frame.

Data can be moved between the global I-Structure memory and slots/registers only via the LOAD and STOR instructions. LOAD takes a structure base address (ISD) and an offset (INT), adds them to produce a structure element address, and forwards this along with the target frame slot address to the appropriate remote memory unit, again, without waiting for the result. The name of the instruction implies that the result must be returned to the frame (as opposed to a register). The reason should be clear - the fetched value will return asynchronously, therefore, all consumers must be able to synchronize. Since registers are both volatile and non-synchronize, they are unsuitable as targets for a fetch-like operation.

STOR performs no indexing (three-address instruction format limit). The structure element address (ISA) and the value are forwarded to the memory. A signal value is produced. This is useful for termination detection as discussed in Sections 4.2.4 and 4.3.5.

Indexing for STORs is done explicitly by the IXSA (IndeX Structure Address) instruction. The IXCC (IndeX Current Context) instruction derives new frame base addresses from the context’s frame base address, allowing the construction of sub-frame blocks, e.g., for procedure linkage. IXID (IndeX Iteration Descriptor) takes an iteration descriptor and adds a given amount to all three of its index offsets.

Index offsets in the active continuation (AC) are explicitly set by the STPR (Set Previous iteration), STCR (Set Current iteration), and STNX (Set Next iteration) instructions. Iterations are conditionally enabled by use of the STPC (Set Program Counter) and STIM (Set Import flag) instructions which set flags in the iteration descriptor which, when all true, allow the corresponding iteration to begin. The TSTL (Test Loop termination) instruction tests for termination of an iteration by examining the flags in an iteration descriptor.

The explicit TSTN (Test 1 or 2 slots) and RSTN (Reset 1 or 2 slots) instructions are not

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17 This has an important implication for the way frame storage can be implemented, in particular, it avoids the coherence problem should it become desirable to cache frame data.
necessary in that their functions can be synthesized from other instructions. For example, \texttt{TST1}
is the same as \texttt{MOVE}ing a value, using the suspensive sub-addressing mode, to another slot.\texttt{RST1} is the same as nonsuspensively \texttt{MOVE}ing the contents of a slot, using the nonsticky sub-addressing mode, to a scratch register. However, for the sake of instrumentation, separate instruction codes are used in this study.

The branch-like opcodes do the obvious things, causing the PC in the continuation to be replaced (conditionally or unconditionally, as appropriate). The \texttt{CNTN} (CoNTineu) opcode creates (forks) a new continuation. The corresponding join operation is implemented implicitly through frame slot synchronization. \texttt{CNTT} (CoNTinue and Test) is functionally identical to \texttt{CNTN} (it is \textit{not} a conditional fork), but is used as part of an important optimization discussed in Section 4.3.7.

Allocation of processor and memory resources is viewed as the responsibility of the architecture. However, the compilation target only includes the instructions used to call some processor-local facility to request these services. Such instructions are \texttt{MKIS} (MaKe I-Structure, the general case of a linearly addressed, 1-dimensional array of slots with arbitrary lower and upper bounds - the instruction returns the base address of the structure), \texttt{MKIV} (MaKe I-Vector, the less general case of a I-Structure whose lower bound is always 0), \texttt{MKIC} (MaKe I-Cons, the less general case of an I-Vector whose upper bound is always 1), \texttt{GETC} (GET Context, which allocates an invocation context somewhere in the machine for a given codeblock and returns the base address of the frame), and \texttt{RETC} (RETurn Context, which allows a context’s resources to be recycled).

The closure management instructions manipulate closures which are represented as word-sized objects. Such closures are discussed in [57]; the instructions here mimic the functions of the instructions described there. Given such a representation, manipulation of closures in a single machine cycle is indeed plausible.

### 3.2.4.4 Architectural State

The primitive instructions which allocate and deallocate invocation contexts do so at the level of \textit{codeblocks}; an instance of an invoked codeblock is called an \textit{invocation context} or simply an \textit{invocation}. A codeblock is a collection of SQ’s, and may differ from a \textit{user} procedure depending on the compilation strategy used\textsuperscript{18}. The \textit{state} visible to an executing codeblock (more precisely,

\footnote{As presented in the Compiler chapter, a user procedure is translated into a set of codeblocks by \textit{lambda-lifting} [40] internal procedure definitions to top-level and replacing all instances of calls to such procedures with partially-applied closures. Such lifted procedures are compiled separately. The remaining procedure is examined for iterations and all but the first, outermost iteration is removed from the procedure. The remaining code is compiled into a single codeblock. The extracted iterations are further broken down into codeblocks (one iteration per codeblock). Hence, a single user procedure containing internal definitions and multiple, nested loops will be compiled into a number of separate codeblocks. This strategy is not the only one possible, but the rationale for splitting user procedures along these lines does make certain architectural problems, such as allocating dynamic storage and constant areas for loops considerably easier. The interested reader is directed to [57].}
Figure 3-4: The Hybrid Machine

to the continuations of its SQ’s) includes the slots in the invocation’s frame, the general purpose registers, the I-Structure storage, and the descriptor for the current continuation itself. The continuation’s descriptor is the root of the accessible state. It points to the next available instruction and to the frame. The frame is entirely local to the invocation. The registers, as described, are shared and cannot be relied upon across instructions which may potentially cause suspension.

3.3 Execution Models
In this section, idealized and realistic execution models are presented. At the coarsest level, both the idealized and the realistic machines share a number of common characteristics. In overall structure (Figure 3-4, yet another incarnation of the general model of Figure 2-1) they both follow the dance hall paradigm of a number of identical processors on one side of a routing network, with a number of memory modules on the other side of the network. A processor may send a message either to a memory module or to another processor.

It is assumed that the memory units are actually I-Structure Storage units (per [34]); their structure will not be reiterated here. It is sufficient to assume that the storage units collectively implement a single global address space, and that each accepts requests to load, store, or allocate in a pipelined fashion. Further, the service latencies (independent of communication latencies) for allocating or storing are assumed to be bounded. The service latency for loading from an I-Structure is unbounded in that it implies synchronization.
Figure 3-5: The Ideal Processor
The network's internal structure is of little concern here, save that the transit latency through the network is some reasonably slowly-growing function of the number of inputs (e.g., \( \log(n) \)), that messages can be accepted in a pipelined fashion, and that the acceptance/delivery rate speed-matches both the processor and the structure memory. It is not essential for the sake of this study that the network preserve orderings of messages; however, other higher and lower level concerns may deem it essential.

Instructions may make operand references to a processor's registers or to slots in the processor's large, local data memory. Slots may be read and written imperatively or via the checking of synchronization bits associated with each word. The local memory's behavior is as discussed previously. Local memory is referenced relative to a frame base address in the current continuation.

Each processor also has a small array of registers (eight to sixteen). Registers may be used freely between instructions which make suspensive references to the frame, but since no register saving takes place when a suspension occurs, register contents cannot be considered valid across potentially suspensive instructions.

3.3.1 The Ideal Processor

The idealized hybrid architecture can be thought of as a von Neumann machine augmented with a synchronizing local memory, and means for manipulating continuations as first class hardware types (Figure 3-5, an embodiment of the concepts in Figure 2-2). This machine has the following attributes:

- Each codeblock invocation is assigned its own local memory unit which is only used for that invocation's frame storage. Connected to each such local memory are processors - one for each continuation created by the invocation. Each processor may operate on a single continuation if it is active, or it may sit idle.

- Instructions are executed exactly when they are enabled. Each instruction takes unit execution time and, within any given continuation, instruction \( i \) which follows instruction \( i-1 \) must necessarily execute at some time \( t_i \) such that

\[
    t_i \geq t_{i-1} + 1
\]

At any given time \( t \), then, as many instructions will execute as there are processors holding active continuations.

- An instruction may access zero, one, or two operands, either in registers or in the local memory (frame slots) without incurring a time penalty. Processors sharing a local memory can access the memory without conflict. Processors may not access any of the other local memories in the machine.

- Performing a synchronizing operand fetch from an empty slot in the local memory causes the affected continuation to be removed from its processor and to be stored in
the empty slot. Multiple synchronizing reads against the same slot cause additional
continuations to be stored in the same slot. Upon writing a value to a slot containing
continuations, the continuations are extracted and returned to their processors.

The idealized model provides a means for studying the effects that architectural and compiler-
induced assumptions have on program execution, without imposing further, hardware-specific
constraints. In the next Chapter, experimental results will be presented showing the behavior of a
number of programs under the idealized model. These results will provide an interesting com-
parison to similar results from the TTDA. Also, they will provide a backdrop for studying the
behavior of the same programs when executed on a realistic machine model which is discussed
next.

3.3.2 The Realistic Processor
The idealized processor represents, in some sense, the best that any hybrid machine can hope to
do given the compilation constraints. In this section, the intractable aspects of the idealized
machine are explored in some depth, and architectural directions are identified which will result
in a realistic machine whose behavior can mimic that of the idealized machine in key ways. The
basis of this discussion is a concrete instance of a processor (Figure 3-6). In order to translate its
physical characteristics into constraints, its behavior will be described on a per-pipeline stage
basis.

3.3.2.1 Unrealizability
At the most basic level, the idealized model is unrealizable because

- The number of processors is necessarily finite, and each processor has its own local
  memory. In general, the local memory of each processor must hold the invocation
  frames of more than one codeblock instance. Moreover, of all the invocations which
  are mapped onto a given processor, at most one instruction from the set of all those
  which are logically enabled may execute at any given time.

- Access to the local memory is subject to hard engineering constraints. Unlike the
  idealized model which permits multiple accesses from multiple continuations at any
given time, it will be difficult to provide access to more than a handful of local
addresses during a pipeline beat.

- Using local slots to hold suspended continuations is constrained by the size of the
  slot: at most a single continuation can be stored into a slot. Hence, queueing of
  multiple suspensions requires some additional mechanism.

Moreover, the model of unit instruction execution time is subject to countless engineering con-
cerns. It is this issue which has made pipelining such a popular implementation technique. By
this method, the rate of dispatching instructions can be uncoupled from the total execution time of
any given instruction. The difficulty in pipelining a processor arises when there are inter-
dependences between instructions in the pipe.
The model presented in the following sections is claimed to be realizable. Instructions are dispatched into a rather shallow pipeline. Inter-dependence between instructions is managed with the aid of low-level context switching, made possible by the expression of programs as partial orderings of totally ordered chunks (SQ's). This section briefly examines the hazards of trying to use a pipelined organization to mimic the behavior of the idealized machine.

At each time step, the ideal model will execute all and only those instructions which are enabled.
This implies a means for identifying the set of enabled continuations and the corresponding set of enabled instructions. The former problem is easy to deal with in a pipelined machine - continuations are always sorted by their state, specifically, enabled continuations reside exclusively in their own queue or set of queues. The latter problem is also relatively easy to deal with in a pipelined machine. The PC in each enabled continuation denotes the instruction to be executed next. Given sufficient instruction memory bandwidth, all such instructions can logically be
fetched in parallel. The hard problem is to know which of these instructions are actually executable.

In a dataflow machine, the construction of the set of enabled instructions is done automatically by the waiting-matching hardware. In the hybrid machine, the approach is different - an instruction can be attempted, and if the synchronization constraints are not met, the instruction is aborted. Efficient means are available for preventing busy-waiting (viz., storage of such suspended continuations in the frame slot which caused the synchronization fault), but in a non-ideal setting, the cost of the faulted instruction cannot be ignored. Moreover, in a real pipeline, several instruction dispatch cycles may pass between the time that a potentially suspensive instruction is initiated until it can be determined that the instruction will actually suspend. Careless dispatching of logical successor instructions behind a potentially suspensive one can result in the flushing of not one, but many instructions, depending on the pipe depth. The result on performance may be disastrous.

Given this, consider a method for approximating ideal behavior: means are provided for pre-fetching a subset of the enabled instructions. At each time step, the instruction dispatcher may examine the pre-fetched instructions and choose between them to optimize the behavior of the pipeline. How does the dispatcher make such a decision?

Instructions are to be dispatched so as to keep the pipeline full of useful work. Non-useful work includes execution of NOPs (i.e., pipeline bubbles) and instructions which suspend. Optimal dispatching of instructions is impossible without foreknowledge of which instructions in the set will suspend. However, simple decoding of instructions allows the dispatcher to at least know if the instruction cannot suspend (e.g., those which only reference registers or which make non-suspensive references to frame memory) or if it might possibly suspend. The strategy presented below builds on this observation, attempting to dispatch instructions from a single SQ instance until an instruction is encountered which might possibly suspend. Dispatching from that SQ instance is deferred long enough to obviate the purging of multiple instructions on the occasion of a fault. During this interval, inter-SQ parallelism is exploited by dispatching instructions from another SQ instance. The number of such pre-fetched instructions is directly related to the number of stages between the dispatching stage and the fault-detecting stage.

### 3.3.2.2 Pipeline Overview

The pipeline is synchronous, with registers serving as inter-stage interfaces. In the Figures, registers are depicted as short rectangular boxes with a heavy top-bar (symbolizing an element with state). Stage boundaries are further emphasized with dashed lines. At every pipe beat, each stage stores its current outputs into the appropriate interface registers (see Figures 3-6 and 3-7).
3.3.2.2.1 Continuation Queues

The first pipeline stage is quite simple (Figure 3-8). Continuations are fetched on demand from the second pipeline stage and are loaded into registers at the interface. The enabled continuation queue holds those continuations which are in the enabled state, while the suspended continuation queue holds continuations which are waiting on slots which already contain a suspended continuation. Continuations are fetched from the enabled queue when it is nonempty. Only when the enabled queue is drained is work fetched from the suspended queue.

3.3.2.2.2 Instruction Fetch / Dispatch

The instruction dispatching logic (Figure 3-9) for the realistic machine is inherently simple. Using two candidate continuations, two such enabled instructions can be considered and the "better" one dispatched at each time step. At any given time, one of the continuations will be called active, the other passive. During each pipe beat, the PC's in each continuation are extracted and are dereferenced through separate instruction caches in order to produce two can-
didate instructions\textsuperscript{19}. The instructions are analyzed according to the following rule\textsuperscript{20}:

Algorithm 3-10:

\textbf{IF the active continuation causes a CACHE MISS,}
THEN Refill the active cache.

\textbf{IF the passive continuation causes a CACHE MISS,}
THEN Refill the passive cache.

\textbf{Restart \{ Pipeline Bubble \}.}

\textbf{ELSE Dispatch the passive instruction\textsuperscript{21}.}
\textbf{IF the passive instruction is a TERMINATE}
THEN Signal that the interface register should be refilled.
ELSE IF the passive instruction is neither SUSPENSIVE nor a BRANCH
THEN Exchange the sense of active and passive.

\textbf{ELSE Dispatch the active instruction.}

\textbf{IF the active instruction is a TERMINATE}
THEN Signal that the interface register should be refilled.
Exchange the sense of active and passive.
ELSE IF the active instruction is either SUSPENSIVE or a BRANCH\textsuperscript{22}
THEN Exchange the sense of active and passive.

Dispatching means that the interface registers to the third pipeline stage are to be loaded with the selected instruction and its corresponding continuation (Figure 3-7). The continuation so loaded contains the PC pointing to the selected instruction, not its successor. This PC must be carried forward in the event that the instruction suspends.

By this method, instructions are dispatched from the active continuation until termination, dispatching of a suspenseful instruction, cache miss, or branching. In the case of branching, having another continuation on "hot standby" is a generalization of the delayed branch paradigm in that low-level parallelism is used to mask the effects of instruction fetch latency. The difference here, of course, is that the method is dynamic. The compiler need not know precisely how long an instruction prefetch might take. Moreover, unlike the delayed branch technique, a broader range of candidate instructions may be used to fill in the gap between a branch and the next sequential

\textsuperscript{19}Implementing this function with two caches is simpler than a single, dual-ported cache, but the performance is likely inferior. Because any continuation may be assigned to either interface register as it goes through cycles of suspension and resumption, contents of both caches would tend toward the same contents. By combining the storage, duplicate entries could be avoided and cache misses could be reduced.

\textsuperscript{20}It is assumed that TERMINATE instructions are not separately encoded but rather that the SQ termination condition is indicated as an opcode modifier for every instruction.

\textsuperscript{21}This algorithm relies on there being two banks of registers, active and passive, corresponding to the active and passive continuations. This level of sophistication is not strictly necessary. In fact, the realistic emulator used to evaluate this architecture does not interleave continuations in this way. The performance penalty is program dependent, and the option to interleave at this level is left as an engineering decision. The effects on locality are not well understood.

\textsuperscript{22}Interleaving on BRANCH instructions forces the compiler to treat them as potentially suspenseful.
instruction, such as instructions from disparate sections of the program or even other branch instructions\(^\text{23}\).

For straight-line, non-suspensive code, instructions will dispatch sequentially, with von Neumann like locality. For code with interspersed unconditional branches, two separate continuations will tend to swap the processor between them - one will compute while the other resolves a branch. Assuming that cache resolution takes about the same amount of time as branch resolution, this behavior will also be observed in the presence of cache faults. Only when synchronization faults occur will this behavior change. Thus, known-short latencies are masked by parallelism without significantly degrading operand locality, and other latencies are masked by parallelism with the cost in terms of lost locality being, to first order, proportional to the time spent waiting for synchronization.

\[ \text{Figure 3-10: Stage 3 - Operand Fetch} \]

3.3.2.2.3 Operand Fetching

The operand fetching stage (Figure 3-10) takes a continuation and an instruction, decodes the addressing modes, and fetches the operands (Opnd.0 and Opnd.1 in the Figure). Each instruction

\(^{23}\text{This kind of parallelism and synchronization can also be used to mask the instruction fetch latency of conditional branches, but the mechanism is necessarily more complex. One approach is to dedicate additional instruction memory bandwidth to parallel exploration of conditional branch targets as in the IBM 370/168 and its descendants. Another, less expensive technique is to refine the notion of suspension. In general, suspension due to a dynamic dependence across SQ's may take unbounded time to resolve. The situation in the case of of the conditional branch is very different. The dependence upon the conditional test will always be resolved within a pipe beat or two of successful operand fetch. For this reason, it is worth considering removing the continuation from the active register upon dispatching a conditional branch. If the boolean operand is not available, a normal suspension will occur. If the operand is available, the continuation can be reinserted in the enabled queue (LIFO, perhaps) or into a new queue which has higher priority than the enabled queue, once the correct PC has been determined. Giving preferred status to this continuation assures that the presence of conditional branches does not adversely affect locality.} \]
has three fields for operand specification named Dest, Source.0, and Source.1. Within each operand specifier is an addressing mode field and a value field. Section 3.2.4 describes the addressing modes. These modes select from among the different possible inputs to an operand register:

- **Immediate:** The value is found in the corresponding operand specifier, *i.e.*, an immediate for Opnd.0 would be found in the value field of Source.0.
- **Register:** The value is found in the register file at the offset given in the operand specifier.
- **Frame Direct:** The value is found in the local memory at the offset given by adding the continuation's FBR to the offset given in the operand specifier.
- **Frame Indirect:** The value is found in the local memory at the offset given by adding the continuation's FBR and index register (P, C, or N in the Figure) to the offset given in the operand specifier.

Computation of the destination address is also done at this stage. The result, which specifies either a register or a local memory slot, is stored into the Dest L/A (destination literal/address) interface register. This may involve either passing the Dest field directly from the instruction (in the case of a register or literal) or modifying it by adding the FBR and possibly an index register.$^{24}$

If either source specifier indicates a synchronizing reference, the corresponding presence bits are tested. If a synchronization failure occurs (*i.e.*, a required frame slot is empty), an abort is signalled by transforming the instruction into a command to suspend. Subsequent processing will ignore the operand registers and will cause the continuation to be stored into the faulting frame slot. The address of this slot is stored in the Dest L/A register in lieu of the actual destination address.

A special case of source addressing occurs when the destination address of the immediately preceding instruction is the same as one of the source addresses in the current instruction (the case of a sequential dependence). In this case, synchronization testing and operand fetching may be ignored, and the previous instruction's result may be used directly as an input operand. This commonly-used technique is called pipeline bypassing, and obviates pipe bubbles which would otherwise occur while fetching a recently-computed result which has not yet been stored away.

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$^{24}$Having a "literal" as a destination means only that the destination field contains a literal value to be used in further computing the destination target for the instruction. An important application of this option occurs in the MOV instruction, described below.
3.3.2.2.4 Computation

The computation section of the pipeline (Figure 3-11) seems anticlimactic when compared to the previous pipeline stages. In this section, a new result is computed and/or a network request (e.g., to initiate a **LOAD**, **STOR**, or **MOVR**) is formulated. In parallel, the destination address is copied to the corresponding interface register. The ALU and Form Request units are conditioned on the Opcode which may indicate a suspension - if so, the value loaded into the Result register is the continuation. The destination address will have been set to denote the slot causing the synchronization fault. All inbound network traffic is queued (FIFO) in this stage and presented to the local memory via an interface register.

3.3.2.2.5 Storing of Results

As the last phase of instruction execution, the result is stored (Figure 3-12). The Dest A (destination address) register indicates the target as local memory or the register array, and specifies the offset. The value to be stored is found in the Result register. Stores to the register array are straightforward, while stores to the local memory require checking and updating of presence bits:
Figure 3-13: Flow of Data for Normal Instructions

Algorithm 3-11:

*IF presence bits indicate the slot currently holds a waiting continuation*

*THEN IF a continuation is being written*  
  *THEN Send the new continuation to the Suspended queue (point "D").*
  *ELSE Extract the stored Continuation*  
    *Send it to the Enabled queue (point "C")*  
    *Write the value.*  
    *Set the presence bits to Written.*

*ELSE IF a continuation is being written*

*THEN Write the continuation.*  
*Set the presence bits to Waiting.*  
*ELSE Write the value.*  
*Set the presence bits to Written.*

Network responses are stored in the frame just as are non-continuations. They extract a waiting continuation and queue it, if there is one, and they set the presence bits to Written.

3.3.2.3 Sequencing and Interlock

This section presents the temporal behavior of the pipeline. First, several instruction examples are given to show how various resources are used. Then, several resource contention problems are investigated, and solutions are proposed.
3.3.2.3.1 Instruction Examples

The majority of instructions (e.g., arithmetic, logical, closure) execute by the paradigm of performing synchronized or unsynchronized operand fetch, computing a new value, and storing of that value. Selection of the next instruction to be executed depends on the success of operand fetching, as described above, but the normal case will choose the next sequential instruction. The flow of data for this class of instructions is shown in Figure 3-13. In this case, operands may reside in the frame or in registers. Literal operands are also permitted but the data path is not shown in the Figure (see Figure 3-7 for details). Presence bits are tested for any synchronizing reference to the frame, and synchronization failure causes the instruction to be aborted as described above. These instructions produce no network messages.

**MOVR**, the sole instruction for moving a datum from one execution context directly to another, is shown in Figure 3-14. Operand Src.0 will be the frame descriptor of the destination frame, and the Dest field will contain an immediate index into that frame. Operand Src.1 will be the datum to send. Hence, only the frame descriptor and the datum may cause a synchronization event. The main ALU adds the immediate index to the frame descriptor, and the Form Request unit takes this result and the datum, and forms a network request packet. Although not shown in the Figure, it is
Figure 3-15: Flow of Data for the LOAD Instruction

possible for MOV R to suspend just as a normal instruction would. In this case, the continuation would be stored as shown in Figure 3-13. MOV R initiates a split transaction and does not block the pipeline awaiting the remote store. It is possible to optimize this in the case that the destination frame resides on the same processor - the result can be stored as in a MOVE instruction.

LOAD takes an ISD and an index, computes an ISA by adding the index to the base address in the ISD, computes the frame address into which the result is to be stored, and forms a network request made up of the ISA and the FD. The flow is shown in Figure 3-15. Like MOV R, LOAD initiates a split transaction operation. Unlike MOV R, the result can only return to the processor on which initiation took place. That is, at some future time a network response will arrive carrying the requested datum, and bearing the FD computed by the MOV R.

STOR takes an ISA and a datum, constructs a network request to store the datum at the indicated address, and generates a signal.\(^{25}\)

\(^{25}\)Logically, this operation produces no local result. The signal is necessitated for termination detection as in the TTDA, but subject to the optimizations discussed in Section 4.3.5, \textit{i.e.\textit{,}} that the signal need only be tested across SQ boundaries. There are many other instructions in the instruction set which logically produce no local result but which do not generate a signal. Signal generation is only necessary to preserve the connectedness of the program graph - in the case of these other instructions, they are consistently used in such a way that the connectedness is guaranteed by other means. STOR implements the second half of the I-STORE program graph instruction and necessarily must generate a signal. See Section 4.3.5.
As mentioned previously, the TSTN instructions are simply special codings of instructions which synchronize on one or two operands and which simply produce a dummy result (such coding is used for instrumentation purposes only). RSTN is similar in that is a special coding of a non-sticky MOVE to a null destination. These instructions reset the presence bits for one or two frame slots. The data flow is straightforward and is shown in Figure 3-17. Neither a local result nor a network request is produced.

The BRXX instruction executions fall into the following categories:

- **Synchronization Failure**: The predicate argument is read with synchronization enabled and the value is not present. This results in a standard suspension as per the normal case. The unmodified continuation is stored into the predicate slot.

- **False Predicate**: The predicate argument is read and the resulting test computes \texttt{FALSE}. The PC is incremented in the main ALU, and the continuation is re-queued.

- **True Predicate**: The predicate argument is read and the resulting test computes \texttt{TRUE}. The instruction-specified target, interpreted as a relative offset, is added to the PC in the main ALU and the resulting continuation is re-queued. This case is shown in Figure 3-18.

The CNTX opcodes are similar. CNTN fabricates a copy of the existing continuation in the main ALU by adding the relative target to the current PC, and then queueing it as an enabled continua-
tion, (without suspending the current continuation). **CNTT** provides a slight variant in that it tests the given slot in conjunction with building a new continuation. If the slot has not been written to, the new continuation is stored directly into it. Otherwise, the new continuation is queued. The intention is to avoid wasting cycles scheduling a continuation which will predictably suspend.

To support multiple, concurrent iterations, each continuation contains three index registers (P, C, and N, for *previous iteration*, *current iteration*, and *next iteration*, respectively) which may be used via the frame indexed operand addressing mode. Each iteration has an area of the frame set aside for it (the format is shown in Section 4.3.4), and the first slot is reserved for an iteration descriptor whose structure is identical to that of a continuation, save the replacement of the frame base register in the continuation with a set of boolean flags. These flags indicate the necessary iteration enabling conditions described in Section 4.3.5, specifically, that the $i$-$i$ iteration's predicate has computed a **TRUE** predicate ($\text{CNTL}_{i}$) and that the $i-K+1$ iteration has ended ($\text{IMPT}_{i-K+1}$). These iteration descriptors are precomputed and loaded into slots zero of each iteration subframe, and are used in the construction of continuations when iterations become enabled.

The **STNX**, **STCR**, and **STPR** instructions are monadic and have the side effect of inserting the next, current, and previous iteration indices, respectively, into the current continuation. The **IXID** instruction behaves as a normal, dyadic instruction, and has the effect of incrementing all three indices in an iteration descriptor by the same amount\(^{26}\). **TSTL** is dyadic and is used to detect termination of the iteration clean-up code as a necessary precondition to exiting the LOOP.

**STPC** and **STIM** are slightly more complex. **STPC** sets the PC field of the iteration descriptor and also asserts the **CNTL** condition, *i.e.*, it sets the flag. **STIM** sets or resets **IMPT**. In addition,

\(^{26}\)It is a straightforward matter to logically partition a wide ALU/adder into several smaller ALUs/adders by appropriate gating in the carry lookahead logic, thereby permitting **IXID** to execute three additions in a single cycle.
both of these instructions check the flags to see if the corresponding iteration has become enabled. If so, a continuation is fabricated by substituting the current FBR from the current continuation into the iteration descriptor, thus creating a new continuation. This continuation is queued, and the iteration descriptor with both flags reset is stored. If instead the iteration is not yet enabled, the iteration descriptor is simply stored; no continuation is fabricated. The flow is shown in Figure 3-19.

The MKIC, MKIS, MKIV, GETC, RETC instructions provide linkage to local managers (they may be though of as supervisor calls). The opcode implicitly specifies a code entry point at some fixed address in program memory, and the instruction denotes the arguments to be passed and the destination target. No state-saving takes place, and it is a matter of choice as to whether these instructions are always considered to be suspensive (independent of addressing modes). It is believable that certain managers could be written as nonsuspensive routines and, therefore, that the manager-calling instruction could be treated as such. In the general case, however, the manager-calling instruction is an abstraction of an arbitrary code sequence underneath. It is safe for the compiler to view manager calls as suspensive (meaning that the compiler does not rely on the contents of registers across the call).

Because manager calls represent an implicit break in the flow of control, the instruction dispatcher will have to forestall the dispatching of other instructions from the same continuation by treating a manager call as branch-like.
Figure 3-19: Flow of Data for the STPC Instruction

With this understanding of the basic operation of each instruction, attention now turns to the effects of instruction sequences, e.g., network loading, pipeline balance, and resource overcommitment.

3.3.2.3.2 Network Traffic Load

There is an important asymmetry between the ALU's path to the local memory and the network's path. Given ongoing contention between these two paths for the local memory, it is possible to consider suspending the ALU path (and thereby holding up the entire pipe) in order to resolve the conflict. Choosing instead to suspend the network path admits the possibility of deadlock. This does not mean, however, that a given network response must take absolute priority over all instruction results in competing for access to the local memory. Rather, the last pipe stage is free to hold the store for a network response in abeyance until the execution of an instruction which produces no local result subject to the constraint that the network response queue does not overfill. At the system level,

- The number of network responses is equal to the sum of LOAD and non-local MOVR instructions.
- The number of time-slots for handling network responses is the sum of instructions producing no local result, specifically, LOAD, RSTN, BRXX, CNTX, and non-local MOVR.
Figure 3-20: Local Memory Subsystem with Cache

It is a matter for further analysis to determine the relationship between the necessary queue size as a function of the statistics of RESTN, BRXX, and CNTX instructions. The difficult issue will, of course, be locally significant variations from average numbers, causing response queues to fill. In order to guarantee that a processor can always accept network responses, queue filling should be a sufficient condition for pipeline suspension to allow responses to be stored.

3.3.2.3.3 Overcommitment of the Local Memory

Despite the machine's appearance as a simple five-stage pipeline, in reality the third and fifth stages share key resources, viz., the register file, the presence bits, and the frame store. In any one pipe beat, two operands will be fetched for the current instruction, one result will be stored for a preceding instruction and, if that result is destined for a frame slot containing a continuation, the continuation must be fetched. Building a small register file which supports two reads and one write in a pipe beat is entirely reasonable. Presence bits are harder to handle both because there are more of them (a few bits per local memory slot) and because of the need for three reads instead of two. The hardest problem, however, is implementing three reads and one write for the local memory.

One approach, used in the IBM 43xx and in other machines, is to observe that the address for the write operation is available at the very beginning of each pipe beat, while the read addresses must be computed and will therefore not be available until later in the cycle. There is, therefore, an opportunity to reduce the number of simultaneous accesses by performing one access (either
reading a stored continuation or writing a new value) prior to performing the operand fetches. With a memory whose cycle time is half a pipe beat, the requirement can be relaxed to two reads and one write instead of three and one. Building a two-read, one-write memory then requires simply duplicating the memory with the appropriate cycle time constraints.

This is both wasteful and impractical for large memories. Another tack is simply to suspend pipeline operations until all local memory operations can be resolved. Thus, if the memory runs at the rate of one access (read or write) per minimum pipe beat, three references will cause the introduction of two additional bubble cycles downstream in the pipe. This technique can be practical, however, when instruction statistics indicate an average of less than one frame access per instruction (e.g., register-intensive sequential threads). An extreme instance of this is to impose constraints on the compiler which explicitly limit the number of local memory references as a function of time.

A better solution is to exploit the locality that the machine works so hard to preserve. By introducing a triported, store-through operand cache in parallel with the local memory, it is possible in principle to significantly reduce the number of read requests which the local memory must satisfy to the point where it only handles writes (one per beat). Such a cache subsystem is depicted in Figure 3-20.

Possibly the best approach would be to use a pipelined local memory subsystem [38] whose pipe beat is significantly faster than that of the processor. This approach is not investigated here. Another technique not studied is to not store continuations in frame slots at all but rather to use the Suspended queue to contain all suspended continuations. This has the advantage of reducing the absolute worst-case requirements on the frame to two reads and one write per cycle. The potentially deleterious effects on locality and exposed parallelism of this technique are not well understood.

### 3.3.2.4 Exploiting Parallelism

It is worth reviewing how all this mechanism allows the exploitation of the various forms of parallelism outlined in Section 2.4.

- Expression-level parallelism is best used for masking latency by keeping the pipeline full, as in a von Neumann machine. The sequential dispatching of instructions from a given instance of a given SQ allows exactly this behavior. Fast context switching between SQ instances (continuation exchange at the instruction dispatch stage) further allows low-level parallelism to be used in masking latency. The manner of using registers between suspensive instructions allows high-speed, multiport access to data while keeping the cost of context switching very low.

- Inner-loop parallelism is supported by representing each loop as a codeblock and providing efficient means for sending data between codeblocks. The mechanisms
here are the GETC/RETC instructions for allocating and deallocating contexts, the MOVIR instruction for argument/result transfer, and the fine-grained synchronization on frame slots which can be used to support nonstrict invocations (at the same level is procedure call parallelism - the same mechanisms can be used).

- Outer-loop inter-iteration parallelism is supported by representing the storage for an iteration explicitly, and allowing multiple storage areas to be named and addressed. The mechanisms provided include the continuation-specific index registers, iteration descriptors, and instructions for manipulating them (setting, testing, and conditionally scheduling).

3.3.2.5 Modeling Latency

For the purposes of performing the emulation study presented in the next chapter, some assumptions must be made regarding latencies. In fact, transit latency is left as a degree of freedom and, in the experiments, latency will be varied to measure the latency-tolerating effectiveness of the model. It will be assumed throughout, however, that instruction service latency (the pipe beat) is unity, and that the I-Structure storage processor is similarly pipelined.

3.3.2.6 Handling Finite Resources

Questions of how this architecture manages its finite resources are beyond the scope of the present work. It is claimed that solutions applicable to machines such as the TTDA are equally applicable here because of the following relevant architectural similarities:

- Demand for context-specific storage is not only bounded, but is known a priori. Each codeblock carries with it a record of the number of frame slots necessary for invocation (the actual value is a function of $K$, the invocation-time parameter which controls loop unfolding). It is a purely local decision to determine if a given processor has sufficient space to invoke a given codeblock with a given value of $K$.

- Register requirements are likewise bounded at compile time.

- Invocation requests are processor-nonspecific. The response to a GETC is a frame descriptor which identifies both the frame base address and the processor in which the frame resides. Thus, if a local manager cannot satisfy a GETC request based on local information, the request can be handled by any other processor in the machine. The question of how best to make such decisions is an open problem for this machine, the TTDA, Monsoon [47], and other similar machines.

- The queue overflow problem, related to the codeblock invocation problem, is analogous to the same problem on machines like the TTDA and Monsoon. One minor difference is that those machines queue continuations for single instructions, while the hybrid machine queues continuations for SQ's. That is, because expression-level parallelism is represented by properly-ordered sequential code in the hybrid model, there will necessarily be fewer extant continuations at any given time during program execution than in a machine supporting single-instruction parallelism. This has some engineering, but little theoretical, significance.

- As in the TTDA and Monsoon, and unlike machines such as MASA [30, 33, 54], there is no notion of migrating or transporting a "task" and its state to another processor after invocation.

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3.4 Summary

Latency and synchronization have been shown to be fundamental issues in the development of scalable, general purpose multiprocessors, and the issues seem related in fairly incestuous ways. Basic changes to traditional architecture are necessary for dealing with them. One such change is that the execution time for any given instruction must be independent of latency (giving rise to split transactions). A second change is that synchronization mandates hardware support: each synchronization event requires a unique name. The name space is necessarily large, and name management must be efficient. To this end, a compiler should generate code which calls for synchronization when and only when it is necessary. A natural approach is to extend instruction sets to express the concepts of both implicit and explicit synchronization. Such an instruction set, which captures the notions of bounded instruction execution time, a large synchronization name space, and means of trading off between explicit and implicit synchronization is called a parallel machine language (PML).

A compilation target has been defined which satisfies these requirements. The instruction set is not unlike that of a von Neumann machine but has been explicitly augmented with synchronization bits on each local memory slot, addressing modes to support synchronization, instructions for dynamic resource allocation, and an execution model which admits concurrent execution of declared sequential threads. Ideal and realistic execution models have been developed. Basic engineering concerns regarding realizability have also been addressed. It has been claimed that this architecture is capable of exploiting the same types of parallelism as a dataflow machine, albeit in somewhat different ways. If true, this architecture is demonstrably superior to a von Neumann machine for the purpose of building a scalable, general-purpose parallel processor.
Chapter Four
Compiling for the Hybrid Architecture

This chapter considers the task of transforming dataflow program graphs into partitioned graphs, and thence into PML. Section 4.1 examines dataflow program graphs as the input language for the code generator. Section 4.2 discusses the issues involved in generating partitioned code from program graphs. Section 4.3 presents the design for a working code generator which addresses these issues.

4.1 Dataflow Program Graphs

Dataflow program graphs [57] are a powerful and elegant intermediate representation for programs. They are largely architecture independent, and have a precise semantics. In this section, the structure of dataflow program graphs [57] is reviewed through the use of an example. Dataflow program graphs form the basis for the compiler work presented here; an understanding of their overall structure and the semantics of the instructions contained therein is essential.

4.1.1 Expressions

This section examines the instructions that make up this program fragment's graph, the types of data which traverse the arcs of the graph, and the presumed execution rule. Recall that the code for WaveFront's doubly nested loop looks like this:

```
{for i from 1+1 to u do
  {for j from 1+1 to u do
    m[i,j] = (m[i-1,j] + m[i,j-1] + m[i-1,j-1]) / 3;
  }
}
```

Figure 4-1 shows the program graph as generated by the Id compiler. Given the value of j, three elements are fetched from the matrix, they are arithmetically averaged, and the result is stored into the matrix. The matrix is represented as a column-vector of I-Structure descriptors for the rows. Fetching the $i_j^{th}$ element, then, requires first fetching the $i^{th}$ I-Structure descriptor from the column-vector and then fetching the $j^{th}$ element. Because of the addressing pattern implicit in the expression, the graph for the body of the inner loop requires the I-Structure descriptor of both the $i^{th}$ and $i-1^{st}$ rows. Furthermore, because these descriptors are invariant across iterations, their fetching from the column vector has been lifted out of the loop.

In execution, data values are represented as logical entities called tokens which appear to flow
Figure 4-1: Program Graph for WaveFront's Inner Loop Body
across the arcs from one instruction's output to another's input. Instructions may be executed when and only when their firing rule is satisfied. The firing rule is a predicate on the presence or absence of tokens at the instruction's inputs. A token is said to be present on a given input of a given instruction if and only if a token has been placed on the corresponding arc. Firing, or executing, an instruction consumes tokens on input arcs and produces side effects and/or tokens which are placed on output arcs.

Consider first the inputs to this graph. The most obvious is the integer value of \( j \), the inner loop index. Implicit in the semantics of the LOOP-CONSTANT instructions are other execution-context specific inputs.

**LOOP-CONSTANT** Instructions: Within the basic blocks of a LOOP instruction (below), these retrieve a particular loop constant value upon receipt of a trigger. They produce no side effects.

In the case of the graph shown here, first loop constant (LOOP.0) will be the I-Structure descriptor for the \( i-1 \)st row of matrix \( M \). The second loop constant (LOOP.1) will be the I-Structure descriptor for the \( i \)th row. These descriptors are "produced" when the trigger, \( i.e., \) the loop index, becomes available.

In addition, literal input values are also explicitly represented in the program graph.

**LITERAL** Instructions: These produce literal constant tokens when a trigger arrives. They produce no side effects.

Thus, loop constant and literal inputs to a graph are not represented as tokens until an appropriate constant instruction generates them. In the case of the WaveFront graph, then, no computation will take place until the token carrying the value of \( j \) arrives.
Arithmetic and logical operations are represented in the graph by monadic and dyadic instructions, as appropriate.

**MONADIC/DYADIC Instructions**: These include the usual spectrum of arithmetic and logical operations. These instructions fire only when all input tokens are present, produce an output token, and have no side effects. A number of special monadic instructions extract fields (codeblock name, argument chain) from closures and have no side effects.

In the example graph, it is now easy to see how the indices for the three I-Structure references are expressed: addressing of the $i^{th}$ and $i-1^{st}$ rows is done by selecting the appropriate I-Structure descriptor. In this case, since the descriptors were loop invariants, this means simply using the right loop constant. Addressing of the particular element in the row is done via the I-FETCH instruction and the appropriately-calculated index.

**I-FETCH Instructions**: Given a token carrying an I-Structure descriptor and a token carrying a slot offset, these instructions fire and produce a token which is the value of the given slot of the given structure. TUPLE-FETCH instructions are similar, except that the offset is coded as a parameter of the instruction itself. HD and TL instructions are also similar, except that the offset is implicit in the opcode.

Thus, the three I-FETCH instructions will fetch, respectively, elements $i-1,j$, $i,j-1$, and $i-1,j-1$. These values are averaged, and the result is stored in element $i,j$.

**I-STORE Instructions**: Given a token carrying an I-Structure descriptor, a token carrying a slot offset, and a token carrying a value, these instructions fire, write the value into the given slot of the given I-Structure (a side-effect), and produce a signal token. TUPLE-STORE instructions are similar, except that the offset is coded as a parameter of the instruction itself. STORE-HD instructions and STORE-TL instructions are also similar, except that the offset is implicit in the opcode.
Figure 4-2: Program Graph for WaveFront’s Inner Loop
The sole explicit output of this expression is the signal emanating from this I-STORE instruction.

4.1.2 Loops

This expression is compiled into the textual context of a LOOP instruction (Figure 4-2). LOOP is an abstract representation of an instruction schema which Traub [57] refers to as an encapsulator: in addition to its exterior surface, it has interior surfaces which enclose other program graph instructions. Sets of instructions so enclosed by a given input/output surface pair are called basic blocks.

LOOP Encapsulators: These encapsulate a Predicate basic block and a Body basic block, and hide the details of loop invocation, loop constant management, bounding, and recycling of per-iteration resources. Upon arrival of the loop constant tokens and any loop input tokens, the predicate is evaluated, producing a boolean token. If TRUE, the loop body is executed, producing a new set of loop variables which are recirculated to the predicate associated with the next iteration. If FALSE, the loop variables are routed to the output of the LOOP encapsulator.

In the Figure, the predicate consists of a relational instruction which compares the loop index $j$ with the loop limit (available as the third loop constant, LOOP.2). The body consists of the entire graph of Figure 4-1, instructions to increment the loop index, and a signal-tree instruction which tests for termination of the iteration.
4.1.3 Codeblocks

As described previously, the compilation of a procedure will result in the creation of one or more codeblocks subject to the constraint of one loop per codeblock. Hence, in a nesting, inner loops such as this one are always contained in a separate codeblock. See Figure 4-3. The codeblock invocation and parameter passing mechanisms are represented abstractly by the FASTCALL-DEF encapsulator. Codeblocks for a procedure's top level are encapsulated in the related DEF encapsulator.
DEF Encapsulators: These enclose the bodies of codeblocks, and hide the details of parameter passing and argument chain unpacking. They are implicitly triggered by invocation of the codeblock by an appropriate APPLY-like instruction. DEF encapsulators have no inputs or outputs on the exterior surface, and enclose only a single basic block called the Body. Outputs which feed the body are the codeblock's arguments and a trigger. Inputs are the codeblock's result and a termination signal. FASTCALL-DEF encapsulators are similar except that they perform no argument chain unpacking and may have multiple result inputs.

Although not shown in the example graph, codeblocks are invoked with the APPLY and FASTCALL-APPLY instructions, as appropriate.

APPLY Instructions: These accept a closure token and an argument token. If, given the argument, the arity of the codeblock denoted by the closure is satisfied, the codeblock is applied to the arguments collected in the argument chain along with the argument on the input token. If the arity is not satisfied, a new closure is created which is a copy of the input closure save that the argument chain has been extended with the new argument. DIRECT-APPLY instructions accept a codeblock descriptor and a set of arguments. The codeblock is applied to the arguments. APPLY-UNSATISFIED instructions behave like APPLY instructions with the exception that it is assumed the arity will not be satisfied by the argument. In all cases, codeblock application is strict in the closure or codeblock descriptor but nonstrict in the arguments. Also, such codeblock application will return at most a single result. FASTCALL-APPLY instructions are nearly identical to DIRECT-APPLY instructions save that they may return multiple results.

The DEF- and APPLY-like instructions presume the following skeletal procedure linkage mechanism. Codeblocks may represent top level procedures, e.g., user procedures or lambda-lifted internal definitions, or they may represent inner loops. The procedure linkage conventions are different for the two cases.

Top-level procedures are represented at the program graph level by a DEF encapsulator enclosing the procedure body. The implied protocol between an APPLY instruction and the corresponding DEF involves
1. Notifying a resource manager to set up a suitable execution environment for an instance of the invoked procedure (APPLY).

2. Forwarding of the argument chain and the last argument, when available, to the invoked procedure (APPLY).

3. Return of the result (if there is one) to the invoker (DEF).

4. Return of a termination signal to the invoker (DEF).

5. Notifying a resource manager to deallocate the execution environment (APPLY).

The DEF is responsible for unpacking the argument chain (an I-Structure) then feeding these values, when available, plus a trigger to the body. The same DEF is also responsible for fielding invocations where the argument values are sent directly from the invoker, bypassing chain construction and unpacking (this is the DIRECT-APPLY variation on procedure invocation).

Internal loop codeblocks are represented at the program graph level by a FASTCALL-DEF encapsulator enclosing the codeblock body. The implied protocol between a FASTCALL-APPLY instruction and the corresponding FASTCALL-DEF involves

1. Notifying a resource manager to set up a suitable execution environment for an instance of the invoked codeblock (FASTCALL-APPLY).

2. Forwarding of the arguments, when available, to the invoked codeblock (FASTCALL-APPLY).

3. Return of the results to the invoker (FASTCALL-DEF).

4. Return of a termination signal to the invoker (FASTCALL-DEF).

5. Notifying a resource manager to deallocate the execution environment (FASTCALL-APPLY).

The major difference is that there is never an argument chain. Arguments are always sent as in DIRECT-APPLY. Further, there may be multiple results.

4.1.4 Miscellaneous

On occasion, it is necessary for the compiler to represent explicit copying of a value. In other situations, it is necessary to control the visibility of a value until some condition has been satisfied (gating). Both of these operations are handled by the IDENTIFY instruction.
**IDENTITY Instructions:** These produce an output token which is a copy of the first input token. In practice, Identity instructions may have additional trigger inputs which are necessary for firing but which otherwise take no part in the production of the output token. They produce no side effects.

The general case of conditional execution is expressed by the **IF** encapsulator:

**IF Encapsulators:** These encapsulate a *Then* basic block and an *Else* basic block. Upon arrival of a boolean token at the *predicate* input, subsequent data tokens arriving at IF inputs are routed appropriately to either the Then or Else blocks. Outputs from the Then or Else blocks are passed to IF outputs.

Finally, the explicit allocation of I-Structure storage is represented by the **MAKE-I-STRUCTURE** instruction.
MAKE-I-STRUCTURE Instructions: Upon arrival of a token indicating a lower bound and a token indicating an upper bound, these have a side effect of allocating an I-Structure of the indicated size out of the available I-Structure storage, and producing a token which carries an appropriate I-Structure descriptor. The MAKE-TUPLE instructions are similar, but the lower bound is assumed to be zero. Likewise are the MAKE-CONS instructions, but both lower and upper bounds are assumed (0 and 1) and produce a descriptor upon receipt of a trigger. ARRAY instructions allocate and produce a token describing a multi-dimensional array of I-Structure elements given a set of lower and upper bound tokens as input. MAKE-STRING instructions are similar to MAKE-TUPLE instructions, but they not only allocate a structure, they also store the characters of the given string into the structure. The CLOSURE-NCDR instruction is functionally related, in that it extends a closure’s argument chain by allocating a Cons structure and then building a new closure using the extended chain.

4.1.5 Data Types

Tokens in dataflow program graphs may represent scalar values or pointers to I-Structures. Scalars may be integers, floating point numbers, booleans, or symbols (e.g., codeblock names). I-Structure descriptors (reference to a Cons, Tuple, String, Vector, Structure, or Array) and Closure descriptors are both pointers. Excepting certain special monadic and dyadic instructions not described above, this set of data types is closed under the operations defined by the program graph instruction set.

4.2 Strategic Issues for Partitioning

The remainder of the compiler for the TTDA consists of macroexpansion of the encapsulators, transliteration of low-level program graph instructions to actual machine instructions, peephole optimization, and assembly. For the hybrid machine, however, the program graph must first be partitioned into SQ’s. This section investigates the issues of doing so.

4.2.1 Possible Constraints

Starting with a dataflow program graph, partitioning may be done in a number of ways. Issues of concern include

- Maximization of exploitable parallelism: Poor partitioning can obscure inter-
procedural and inter-iteration parallelism. The desire to aggregate instructions does not imply any interest in restricting or limiting useful parallelism - in fact, those cases where instructions may be grouped into SQ's are quite often places where parallelism is exploited in instruction ordering to mask latency.

- **Maximization of run length:** Longer SQ's will ultimately lead to longer intervals between context switches (run length). Coupled with proper runtime support for suspension and resumption, this can lead to increased locality. Run lengths which are long compared to the pipeline depth have a positive effect on shortening critical path time and increasing locality. Short run lengths (frequent instruction aborts due to suspension of a frame reference) tend to bubble the pipeline.

- **Minimization of explicit synchronization:** Each arc which crosses SQ boundaries will require dynamic synchronization. Since synchronization operations are pure overhead\(^{27}\), it is desirable to minimize them.

- **Deadlock avoidance:** Non-sequentiality and lenience imply that instruction execution order cannot be made independent of program inputs or, said another way, instruction execution order cannot be determined *a priori*. It is necessary to understand where this dynamic ordering behavior will manifest itself in the generated code. Such dynamic ordering must be viewed as a constraint on partitioning since two instructions whose execution order is dynamically determined cannot be statically scheduled in a single SQ.

- **Maximization of machine utilization:** Given a set of costs for instruction execution, context switching, synchronization, and operand access, partitions can be compared on the basis of how well they "keep the pipeline full". This metric is fairly machine specific and is in that sense less general than those previously described but no less important.

### 4.2.2 Scope

It is not the focus of this work to develop optimal partitioning techniques, but rather, to develop an architecture which can adapt to a spectrum of partitioning strategies per the requirements of the programming language. To that end, this study focuses on development of a *safe* (deadlock-avoiding) partitioning algorithm for Id program graphs. This choice is based on three important facts:

1. **Availability of Tools:** At the most pragmatic level, the Id compiler is highly accessible, and provides an excellent vehicle for constructing a prototype hybrid code generator.

2. **Availability of Data:** Id applications have been well-studied on the MIT Tagged-Token Dataflow architecture. By using these same applications, meaningful architectural comparisons can be made.

\(^{27}\)Coming from a von Neumann uniprocessor mind set where explicit synchronization is virtually unheard of except in situations which require multitasking, it is natural to view synchronization in this way. Coming from the dataflow world where synchronization is unavoidable in every instruction execution and where there is no opportunity to "optimize it out", it is also reasonable to view explicit synchronization instructions as overhead. In a later section, these perspectives are reconciled with the view that explicit synchronization instructions are both necessary and, in some sense, beneficial.
3. Difficulty of Partitioning Safely: Because Id is a lenient language, it does not admit simple, sequential interpretation [59]. In that sense, efficient support for a lenient language will be harder to provide (read: will depend more on efficient dynamic synchronization) than will support for non-lenient languages.

Traub [59] investigates partitioning rules which are provably both safe and efficient. It is his goal to develop the means for maximizing sequential thread size given these constraints. For the purposes of developing the present architecture, the latter constraint has been relaxed, thereby putting the burden back on the architecture of handling even very small threads efficiently.

4.2.3 Examples

![Diagram](image)

**Figure 4-4:** Partitioning which Leads to a Static Cycle

Safe partitioning involves the analysis of both the static structure of a dataflow program graph and the dynamic behavior of the graph. This dichotomy leads to two distinct kinds of partitioning problems. Consider first the program graph fragment in Figure 4-4. In this example, an acyclic graph is partitioned into two SQ's, each to be executed sequentially. If the partitioned graph is viewed in the abstract with SQ's as the graph nodes, it is curious that the trivial, acyclic graph now has a cycle in it. This results when additional control arcs are inserted. Because this kind of cycle is a function of the graph's static structure, it is called a static cycle.

A very different kind of problem is illustrated with the following Id program fragment:

```plaintext
{ a = vector (0, 2);
  a[0] = 0;
  a[2] = a[j] - 2;
  in a[1] - a[2]}
```
and its associated graph\textsuperscript{28} in Figure 4-5. I-FETCH instructions are assumed to follow split transaction semantics with a non-busy waiting deferred read mechanism [35]. Such a graph would terminate under a dataflow instruction execution rule. However, without exercising some care, partitioning this graph into SQ’s can lead to deadlock. Putting all of these instructions into a single partition won’t work, nor will a partitioning such as that shown in Figure 4-6. Such partitionings result in code which may never terminate, despite the absence of static cycles.

The problem, of course, is that the actual instruction execution order in the dataflow case depends on the indices used in the structure operations, where no such dependence is allowed in the partitioned case. Figure 4-7 shows two instruction execution orderings which must be possible in any correctly compiled version of this program. These orderings demonstrate the dynamic dependences between I-STOREs and I-FETCHes. If these dependences were fixed, and if it were possible to determine them at compile time, SQ partitioning to avoid deadlock would be straightforward. Since this is not the case, the problem is one of developing a safe partitioning strategy which is insensitive to the arrangement of dynamic arcs. One approach is to make each partition exactly one instruction long, \textit{i.e.}, the dataflow method. This, of course, is at odds with the desire to exploit static scheduling.

\textsuperscript{28}The descriptor for vector $A$ is depicted as a constant to simplify the drawings. This is done without loss of generality.
4.2.4 Latency-Directed Partitioning

Extant partitioning algorithms [12, 27] can be classified as depth-first or breadth-first. Depth-first algorithms [12] partition by choosing a path from an input to an output of a graph and making it into an SQ, removing the corresponding instructions from the graph in the process. The algorithm is repeated until no instructions remain unpartitioned. Such partitionings tend to be the best at minimizing critical path time and rely heavily on pipeline bypassing since, by definition, instruction \( n \) depends directly on instruction \( n-1 \). Breadth-first algorithms [27] tend to aggregate instructions which have similar input dependences but only weak mutual dependences.

It is interesting to observe the relationship between the problem of partitioning a program graph and the dynamic "partitioning" of a program which occurs in a multiprogramming environment. Aside from the discretionary kind of context switching which occurs to guarantee fairness among competing tasks, context switching is most often invoked when the running program attempts to synchronize with a long-latency parallel activity, e.g., reading from a disk. Note that it is not in general the initiation of a long latency operation which causes the context switch. It is the attempt to waste time by waiting for the satisfaction of a synchronization constraint. Elaborate
mechanisms are designed into such operating systems to allow the waiting task to be put aside and then re-awakened when the event being waited on happens. For such a system to work, the time to switch contexts must be significantly shorter than the time which would, on average, be wasted in waiting.

It is possible to identify the arcs in a dataflow program graph which represent long latency operations and the attendant required synchronizations. It is natural to pursue this analogy and to perform SQ partitioning such that no useful work will be postponed simply because a part of the program is waiting for the result of such a long latency operation.

A necessary condition for this kind of analysis is that all such arcs are manifest in the graph, and that none are implicit in the internal behavior of an instruction. Reviewing the program graph instruction set shows that this condition is violated in several instances:

- APPLY and FASTCALL-APPLY hide the procedure linkage arcs, in particular, the argument and argument chain arcs which must be synchronized at the called codeblock, and the result and signal arcs which must be synchronized at the caller.
- DEF hides the argument chain unpacking (I-Structure references).

The obvious source of long-latency operations is the I-FETCH instruction which always implies synchronization prior to use of the fetched value. Less obvious are the HD, TL, and TUPLE-FETCH instructions which are (implicitly) I-FETCH instructions. Such outputs of such instructions are
called **FETCH-like**\(^{29}\). See Section 3.2.2.

Handling of the DEF case is straightforward - all DEFs are explicitly translated into a simpler form consisting of a set of HD and TL instructions to unpack the argument chain, plus the body, enclosed by a FASTCALL-DEF. By this technique, the imbedded **FETCH-like** instructions are made explicit, and the long-latency arcs are likewise represented explicitly.

A similar approach can be taken for APPLY instructions. The remaining issue is the handling of the "invisible" dynamic arcs which link the invoker and the invoked codeblock across the FASTCALL-APPLY interface. With DEFs rewritten as FASTCALL-DEFs, and APPLYs rewritten as FASTCALL-APPLYs, the synchronizing end of the invoker-to-invoked arcs (arguments and trigger) are simply the output arcs of the FASTCALL-DEF (Figure 4-11). Similarly, the synchronizing end of the invoked-to-invoker arcs (results and termination signal) are the output arcs of the FASTCALL-APPLY. It is necessary then to consider both FASTCALL-DEF and FASTCALL-APPLY as **FETCH-like**.

An additional problem arises from the semantics of APPLY-like instructions. Upon receipt of the results and the termination signal, these instructions are responsible for deallocating the invoked context’s resources. Because this is part of the instruction *and* because it depends on long-latency arcs, it violates the principle of imbedded arcs. For this reason, all instances of FASTCALL-APPLY (including those which were originally APPLY instructions) are rewritten into component parts which *initiate* the invocation and separately *deallocate* it. Doing this introduces two new program graph instructions: FASTCALL-APPLY-INITIATE which initiates the procedure invocation, and SYNCHRONIZING-RETURN-CONTEXT which frees the invoked context’s resources. Rewriting is discussed in detail in Section 4.3.2.

### 4.2.5 Summary

In summary, the decision has been made to base partitioning on the location of long-latency arcs in the graph rather than to pursue otherwise unguided depth-first or breadth-first partitioning strategies. To make any such scheme work, all long-latency arcs must be directly visible at the program graph level, and none may be "buried" in the operational semantics of a program graph.

\(^{29}\)Instructions which invoke a manager, *e.g.*, MAKE-I-STRUCTURE, are potentially long-latency depending upon their implementation which is *not* implicit in program graph semantics. One can conceive that such instructions package up a manager request and ship it off in the same way that an I-FETCH packs and ships its fetch request. In such cases, synchronization would be implied anywhere the instruction’s output was used. An equally viable implementation is that the manager will always be resident on the same processor as the executing instruction. In this case, such system calls can be viewed as inline macro expansion, in which case there is no busy waiting. Another perspective is that such instructions consume multiple pipeline cycles, and consume all of the processor resource (productively) in the process. This is the view taken here, therefore, such instructions are not classified as **FETCH-like**.
instruction. By rewriting certain program graph instructions into simpler forms, this constraint can be met. It remains to describe an algorithm which can use this information to safely partition program graphs.

4.3 Code Generator

With an understanding of the new target model and the existing program graph structure, it is possible to describe a method of generating code for the hybrid architecture from programs originally written in Id [9]. This section presents the details of the process. A number of interesting problems arise which are characteristic of code generation for parallel machine languages. Solutions to these problems are presented.

4.3.1 Overall Goal and Method

Compiling Id code to the target model is done with extensions to the Id Compiler, Version II [57]. Its modular organization and well defined inter-module interfaces made addition of a new code generator possible with only minor effort. This section discusses the design of the code generator for the target compilation model presented in the previous chapter.

A goal of the code generator was to allow existing Id programs to be used as benchmarks for the new architecture. One constraint was not to modify the compiler itself, but rather to use selected modules, intact, to which are added new modules. The overall architecture of the existing Id compiler is described in [57]. Each major phase of the compiler is a separate module with a well-defined input/output interface (e.g., annotated parse tree, annotated dataflow program graph, dataflow machine graph). The modifications consisted of a set of new code generation phases, the first of which maintained the annotated dataflow program graph interface. The resulting compiler (collection of phases) has the structure shown in Figure 4-8. Boldface phase names represent those which were added to the existing compiler.

Rather than simply discuss each new phase in turn, it is more illuminating to understand the issues in compiling dataflow program graphs into SQ's for the given compilation model. In the following sections these issues are raised, and suitable solutions are given. Where appropriate, references are made to the phases which actually perform the work.

4.3.2 Simplifications

Program graph instructions and encapsulators [57] define a rewrite language which can be shown equivalent to Id. In the Id Compiler, program graphs are transliterated to machine graphs through a process of simultaneous macroinstruction expansion and context-free substitution of machine
graph instructions for program graph instructions. The program graph abstraction is useful in that it admits powerful manipulations with relative ease where parse trees would be cumbersome and machine graphs would be too microscopically detailed.

The code generator for the hybrid machine preserves the program graph interface. Input to the code generator is a well-formed (acyclic compositions of the basic schemata), well-connected (output arcs, called signals, have been added from instructions which otherwise produce no output, e.g., I-STORE; and input arcs, called triggers, have been added to instructions which otherwise receive no inputs, e.g., constants) graph.

Code generation begins with macroexpansion of certain program graph instructions and encapsulators into lower-level program graph equivalents. Examples necessitated by instruction
semantics for partitioning have already been discussed. The primary purpose in performing further rewrites at the program graph level is to simplify later stages of the code generator by restricting the input language, i.e., reducing the size of the set of possible program graph instructions. It is particularly important to perform this transformation prior to assigning frame slots - as they exist following signal and trigger addition, program graphs do not have the property of a one-to-one correspondence between instruction outputs and frame slots. Many required frame slots are "hidden" inside complex program graph instructions. More troublesome, however, is the realization that the number of such hidden slots is a function of the program graph instruction encoding. Hence, this module transforms program graphs into program graphs with a one-to-one correspondence between outputs and slots.

This macroexpansion is done by context free substitution of a subgraph for a single, complex instruction. Some analysis is performed on instructions to build a proper subgraph. The expansion is recursively applied to the subgraphs until the resulting program graph contains only those instructions in the restricted set. In each case, the new subgraph has the same number of inputs and outputs as the old instruction.

4.3.2.1 Structure Handling Instructions

Program graph instructions for creating strings, tuples, and conses are rewritten into a simpler
form which uses a parameterized MAKE-I-STRUCTURE instruction\(^{30}\) and, as needed, literal constant instructions to represent the I-structure kind and the bounds. This rewriting takes advantage of the ability to imbed small literal constants as arguments to any instruction. After this transformation, only one program graph instruction is required to allocate I-structures of any kind. In Figure 4-9, a four-element tuple creation instruction is rewritten into a MAKE-I-VECTOR instruction with an implicit lower bound of zero. The upper bound of three is specified by a literal instruction. The \textit{kind} of vector is encoded as an integer\(^{31}\).

In a similar fashion, instructions to read or write the elements from strings, tuples, and conses are rewritten to a form using only I-FETCH and I-STORE, plus literal constants as necessary. Figure 4-10 shows TUPLE-FETCH.2 rewritten as an I-FETCH and a literal offset. In both this case and in the previous example, triggers for the literal instructions were derived from inputs to the original program graph instruction.

Array creation instructions are expanded in a manner similar to that for the TTDA. Specifically, one dimensional array creation instances are expanded into MAKE-I-STRUCTURE instructions, while higher dimensioned array creations are expanded into calls to library routines.

\(^{30}\)The operation to allocate an area of the I-Structure storage space can be implemented with a single opcode. However, because of the three-address format of the abstract machine and the desire to collect more fine-grained statistics on storage allocation patterns, three opcodes are used. In this example, MAKE-I-VECTOR is an instance of the generic I-Structure creation operation with an implicit lower bound of zero.

\(^{31}\)For the MAKE-I-VECTOR instructions, the possibilities are \textit{tuple} and \textit{string}. 
4.3.2.2 DEF

All DEF encapsulators (outermost encapsulator of any procedure codeblock) are rewritten to parameterized FASTCALL-DEFs. DEF abstracts both the mechanism of passing arguments between contexts and the mechanism of conditionally unpacking argument chains sent from APPLYs. Rewriting separates these two abstractions. The argument chain unpacking is explicitly represented by a set of HD and TL instructions which take apart the list of arguments. Conditional execution of these unpacking instructions is a consequence of the method of triggering SQ's. The gist of the method relies on

- Suspension of the argument chain continuation, which contains the first HD and TL instructions. Both of these require the argument chain. If no chain is sent, as in the DIRECT-APPLY case, these instructions will not execute.
- Initiation of continuations for the remainder of the unpacking as part of the argument chain continuation.

Figure 4-11 shows the complete transformation. The FASTCALL-DEF is parameterized with the number of non-trigger arguments \( n \) of the original DEF encapsulator.
4.3.2.3 APPLY, DIRECT-APPLY, and APPLY-UNSATISFIED

APPLY instructions are rewritten into IF encapsulators which test the closure arguments for readiness, i.e., that all arguments are present, and conditionally invoke the procedure via FASTCALL-APPLY if ready (Figure 4-12). If the closure is not yet ready, the existing argument chain is extended by one CLOSURE-CONS cell, the head of which contains the argument and the tail of which contains a pointer to the old argument chain. A new closure containing a pointer to the new chain is created, and the counter of arguments remaining is decremented.

DIRECT-APPLY is rewritten, essentially, into the true-branch of an APPLY save that all arguments are connected to the FASTCALL-APPLY rather than just one. APPLY-UNSATISFIED is rewritten into the false branch of an APPLY.
4.3.2.4 FASTCALL-APPLY

All instances of FASTCALL-APPLY, including those created by rewriting APPLY and DIRECT-APPLY, are rewritten into a form which exposes the imbedded dynamic arcs. Essentially, this is consistent with the split-transaction nature of I-FETCH: one instruction initiates the fetch while others synchronize prior to using the result. In the case of FASTCALL-APPLY, one instruction initiates the invocation, and a second instruction (SYNCHRONIZING-RETURN-CONTEXT) synchronizes on the return signal and then deallocates the invocation's resources. The translation is depicted in Figure 4-13.

4.3.3 Partitioning Constraints

In this section, the notion of safely partitioning a program graph is developed. It is again assumed that the input graphs are well-formed and well-connected. Since there is the potential of introducing deadlock as a result of partitioning a program graph, the major goal of this section is to develop a set of partitioning constraints which will demonstrably avoid the introduction of deadlock.

Partitioning a graph into SQ's, wherein the instructions are totally ordered, may imply the addition of arcs into the graph to effect sequentialization. The first section defines the issues which arise from the introduction of additional arcs into an otherwise acyclic graph. The second section presents the Method of Dependence Sets, a simple algorithm for partitioning dataflow program
graphs, which only introduces arcs in a highly restricted fashion. The third section examines the algorithm's behavior and shows that, despite the introduction of arcs, deadlock-inducing cycles are not created.

4.3.3.1 Adding Arcs

In order to guarantee liveness of the partitioned graph, it is essential no cycle be introduced into the partitioned graph which cannot be resolved. Recall that the partitioned graph contains only SQ nodes, each representing some nonempty subset of the nodes in the unpartitioned graph. Moreover, the instructions in each such subset are totally ordered. This sequentialization can interact with existing dependences in the graph, leading to a static cycle. Depending upon the interpretation model for sequentialized SQ's, deadlock may result.

Definition 4-1: An unresolvable static cycle is a directed cycle of SQ's in a partitioned dataflow graph for which no schedule of SQ executions can terminate.

Given that instructions within an SQ are to be interpreted sequentially, it is clear that arbitrary partitioning of an acyclic graph into SQ's can result in unresolvable static cycles, a sufficient condition for deadlock. This is reasonably obvious - the partial order represented by a program graph captures all and only the necessary inter-instruction dependences. Imposing further constraints, viz., sequential execution, on a graph is tantamount to adding additional dependence arcs. Doing so in a haphazard fashion can clearly introduce a cycle where there was none.

An example of how partitioning can give rise to a static cycle was shown in Figure 4-4. In order to avoid deadlock, it is necessary either to prohibit such cycles or to devise methods for resolving them. Sarkar and Hennessy [52] choose the former tack and impose a convexity constraint on the partitioning - static cycles can therefore never arise. As an alternative to their technique, it is possible to use an SQ interpretation model which allows such cycles to be resolved. One can imagine a partitioning in which the ability to resolve a cycle only means that the order of instructions in an SQ must follow the topological ordering of the program graph and that there must be a notion of SQ suspension and resumption based on the absence and presence, respectively, of data on inter-SQ arcs. One possible mechanism which allows this behavior and which is efficient was addressed in Section 3.3.

Unfortunately, in order to avoid partitioning-induced deadlock, it is not sufficient to simply resolve all static cycles. I-Structure storage has introduced the notion of dynamic arcs between producer and consumer. Since these arcs are input-dependent, they are not explicitly expressed in the graph and are therefore not amenable to static analysis. They impose no less of a constraint, however. Consider an unpartitioned graph, augmented with all potential arcs from producers to consumers through I-Structure slots. This graph would form the basis for a kind of static analysis; partitioning would be constrained by the ability to resolve any cycles so introduced.
Definition 4-2: An unresolvable dynamic cycle is a directed cycle of SQ’s in a partitioned dataflow program graph, augmented with the input-specific dynamic arcs, for which no schedule of SQ executions can terminate.

The algorithm presented in the next section allows the partitioning of program graphs without the introduction of either static or dynamic cycles.

4.3.3.2 The Method of Dependence Sets

The Method of Dependence Sets (MDS) is a simple algorithm for safely partitioning program graphs. It seeks to avoid the problems of static and dynamic cycles by uniquely naming each FETCH-like output, and then grouping together all and only those instructions which depend directly or indirectly upon the same set of names. The following definitions are in order:

Definition 4-3: The input dependence set for an instruction (written ISD(i)) in a well-connected graph is the union of the output dependence sets of all instructions from which it receives input. The input dependence set of the root instruction is $\emptyset$. The input dependence set for instructions with no inputs is likewise defined as $\emptyset$.

Definition 4-4: The output dependence set for a given output of a given instruction (written ODS(i,o)) is either the instruction’s input dependence set if the output is not FETCH-like, or the union of the instruction’s input dependence set with a singleton set made up of an identifier which uniquely names the given output if it is.

Note that it is a FETCH-like instruction’s output, and not the instruction itself, with which is associated a change of dependence set.

Now, assume a well-connected dataflow program graph $G=(V,E,R)$, where

- $V$ is the set of program graph instructions and encapsulators.
- $E: \{(i,j) \mid i,j \in V \text{ and } j \text{ depends directly on } i\}$ (the set of static dependence arcs)
- $R \in V$ and $R$ is the root instruction.
Algorithm 4-5: METHOD OF DEPENDENCE SETS(G)
For each output o of R, compute ODS(R,o). Traverse graph G from R per topological ordering\(^{32}\), selecting an instruction or encapsulator \(i \in V\) to expand. For each such instruction.

- Calculate IDS\((i)\).
- Assign the generated machine instructions, in order, to an SQ corresponding to IDS\((i)\). SQ's are selected such that for any two program graph instructions \(i,j \in V\)

\[
IDS(i) = IDS(j) \iff SQ(i) = SQ(j)
\]

The SQ denoted by IDS(R)=∅ is defined as the distinguished SQ.

- For each output o of instruction i, calculate ODS\((i,o)\).

Per the characterization of dynamic arcs in the last Chapter, FETCH-like outputs represent long-latency operations. Viewed another way, it is the virtual gate (c.f., Figure 3-1) which must be pushed to the boundary of the unit of schedulability. This is done by forcing all sink instructions fed by the gate into a new SQ. These sink instructions execute only when the I-FETCH and I-STORE upon which they depend have completed.

Applying the definitions to the graph in Figure 4-5 and using \(\alpha, \beta,\) and \(\gamma\) for unique names results

\(^{32}\)Such an ordering is specified in Algorithm 4-11, p. 115.
in the following assignments of input dependence sets to instructions (assume that vector A and the indices \( i, j \) are derived from the root with dependence set \( \emptyset \)):

<table>
<thead>
<tr>
<th>Instruction</th>
<th>Dependence set</th>
</tr>
</thead>
<tbody>
<tr>
<td>I-STORE(0)</td>
<td>( \emptyset )</td>
</tr>
<tr>
<td>I-FETCH(i)</td>
<td>( \emptyset )</td>
</tr>
<tr>
<td>I-FETCH(j)</td>
<td>( \emptyset )</td>
</tr>
<tr>
<td>I-FETCH(1)</td>
<td>( \emptyset )</td>
</tr>
<tr>
<td>I-FETCH(2)</td>
<td>( \emptyset )</td>
</tr>
<tr>
<td>+1</td>
<td>( { \alpha } )</td>
</tr>
<tr>
<td>STORE(1)</td>
<td>( { \alpha } )</td>
</tr>
<tr>
<td>-2</td>
<td>( { \beta } )</td>
</tr>
<tr>
<td>STORE(2)</td>
<td>( { \beta } )</td>
</tr>
<tr>
<td>-</td>
<td>( { \gamma } )</td>
</tr>
</tbody>
</table>

Since each distinct combination of dynamic arcs denotes a single SQ, dynamic scheduling can change to match the dynamic dependences. The correctly partitioned graph is shown in Figure 4-14. The determination of synchronization points is also straightforward: each dependence (arc) which crosses SQ boundaries must be explicitly synchronized by the consumer, or sink, SQ. Consumers in the same SQ as the instruction producing a value need not perform synchronization. It is implicit in the static scheduling of instructions within the SQ (these are exactly the static synchronized and static unsynchronized arcs of Section 3.2.2).

### 4.3.3.3 Properties of MDS

The Method of Dependence Sets collects together into SQ's all and only those instructions with identical dynamic dependence requirements. That is, every instruction in an SQ depends directly or indirectly on the same set of FETCH-like outputs and I-STores. Each resulting SQ is a set of subgraphs. Disjoint subgraphs in an SQ have neither a static dependence nor a dynamic dependence between them. The former is obvious - otherwise, they would not be disjoint. The latter is less obvious, but follows immediately from the definitions. A dynamic dependence would imply FETCH-like instruction outputs feeding sink instructions, which would necessarily have forced the sink instructions to appear in a different SQ.

This simple assertion has a powerful effect on the manner in which SQ instructions can be sequentialized. For an SQ which contains but a single subgraph, the ordering must adhere to the subgraph's topological constraints. For an SQ with more than one subgraph, the instructions from any one subgraph must be topologically ordered, but there is no cross-subgraph constraint. Consequently, in an SQ containing subgraphs \( A \) and \( B \), instructions from \( B \) may follow all the instructions of \( A \), or conversely. Alternatively, instructions from \( A \) and \( B \) may be interleaved. The point is that, because there cannot be a dynamic dependence between them, introduction of sequentializing arcs cannot interfere with essential dynamic instruction ordering.
Can cycles, either static or dynamic, ever arise among the SQ's partitioned by MDS? The following two theorems address this question directly.

**Theorem 4-6:** Partitioning an acyclic program graph by the Method of Dependence Sets results in a program graph which is free of static cycles.

In order to prove this, it is necessary first to establish a few other facts, specifically, (1) that there is a dependence between two SQs, there is a proper subset relationship between their dependence sets and (2) that transitivity of this relation holds.

**Lemma 4-7:** Inter-Instruction Dependence: For all instructions \( i, j \in V \), if \((i, j) \in E\) then \(IDS(j) \supset IDS(i)\).

**Proof:** Follows directly from Definition 4-3.

\( \Box \)

**Lemma 4-8:** Cross-SQ Dependence: For all instructions \( i, j \in V \), if \((i, j) \in E\) and \(SQ(i) \neq SQ(j)\) then \(IDS(j) \supset IDS(i)\).

**Proof:** (by contradiction)

From Lemma 4-7, \(IDS(j) \supset IDS(i)\). Assume that \(IDS(j) = IDS(i)\). But from Algorithm 4-5, it then follows that \(SQ(j) = SQ(i)\).

\( \Box \)

**Lemma 4-9:** Dependence Transitivity: For all instructions \( i, j, k, l \in V \), if \((i, j) \in E\), \((k, l) \in E\), \(SQ(j) = SQ(k)\), and \(SQ(i) \neq SQ(j) \neq SQ(l)\), then \(IDS(l) \supset IDS(i)\).

**Proof:**

\[
\begin{align*}
IDS(j) & \supset IDS(i) \quad [1] \text{Lemma 4-8} \\
IDS(i) & \supset IDS(k) \quad [2] \text{Lemma 4-8} \\
IDS(j) & = IDS(k) \quad [3] \text{Algorithm 4-5} \\
IDS(l) & \supset IDS(j) \quad [4] \text{by 2 and 3} \\
IDS(l) & \supset IDS(i) \quad [5] \text{transitivity, 4 and 1}
\end{align*}
\]

\( \Box \)

The theorem can now be proved rather simply.

**Proof:** (by contradiction)

Consider a cycle of dependence arcs among a set of distinct SQs \(A, B,\ldots\). Then, by Lemma 4-9 it follows immediately that \(IDS(A) \supset IDS(A)\).

\( \Box \)
Theorem 4-10: Partitioning an acyclic program graph by the Method of Dependence Sets results in a program graph which is free of dynamic cycles.

Theorem 4-6 states that the partitioning of an acyclic graph by MDS is itself acyclic. Augmenting this graph with all possible input-specific dynamic arcs raises the possibility of cycles containing one or more dynamic arcs. It follows from the definitions that a dynamic cycle cannot occur within a single SQ (as discussed above). It remains to show that no cross-SQ cycles exist.

Proof: (by contradiction)

Assume a cycle among two or more SQ's wherein one or more of the cycle-forming arcs is dynamic. Because a dynamic arc is involved, there must be an I-STORE instruction \( i \) in the cycle. Consider this I-STORE instruction and the SQ in which it resides. By the assumption and Algorithm 4-5, this SQ must depend on the dynamic arc. But, again by Algorithm 4-5, all instructions in the SQ, including \( i \), depend on the dynamic arc. This is true independent of any sequentializing arcs which may or may not be added to the SQ. Here is a situation of a dependence which violates I-structure semantics. Hence, either there is an error in the original program, or the assumed cycle cannot exist.

\[ \square \]

4.3.3.4 Summary

In this section, a partitioning algorithm has been introduced which groups together all and only those instructions with identical dynamic arc dependences. It has been shown that the extra arcs introduced by the algorithm do not interfere with essential instruction orderings, that static cycles are not created, and that dynamic cycles are not possible.

4.3.4 Operand Storage Allocation

This section examines the mapping of arcs in the program graph into proper dynamic storage. Such storage is invocation specific and, by analogy with von Neumann machines, a frame, or array of directly indexed slots is the model.

The problems of allocating invocation-specific operand storage can be divided into two categories: those which can be reduced to analogous ones in a von Neumann environment and those which are unique to parallel processing. For the sake of completeness, both are presented here. The latter category has received considerably more attention in this study, however. To that end, a number of known storage conservation techniques which apply to the former category were simply not implemented in the prototype compiler in order that more time could be given to the latter category. It was therefore deemed sufficient to allocate one slot in the frame for each
Figure 4-15: Procedure Frame

instruction output in the program graph\textsuperscript{33} with the following exceptions:

- Merged arcs, \textit{e.g.}, the outputs of the \textit{then} and \textit{else} blocks of an IF encapsulator, cause instruction outputs to be mapped to the same frame slot.

- Loop variables are mapped statically to frame slots, but the slots are re-used in a carefully controlled fashion across iterations. This important optimization is described in Section 4.3.5.

\textsuperscript{33}Frame slots are assumed to be inaccessible outside of the given execution context. Moreover, the values held in frame slots have a lifetime which is generally much less than the lifetime of the frame. It is possible and highly desirable to fold the compiled codeblock such that slots can be re-used. This problem is equivalent to register assignment for traditional architectures with the added constraint of multiple continuations per codeblock. This introduces nondeterminism into the matter of deciding when a slot will no longer be referenced; in the case that the producer of a value and \textit{all} of its consumers are not within the same SQ, dynamic methods (or loosely bounded static methods) are necessary. In that the compilation scheme proposed here does not partition a codeblock into SQs until \textit{after} frame slot assignment, such folding is not possible.
### Figure 4-16: Inner Loop Frame

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>0:</td>
<td>FD of Caller</td>
</tr>
<tr>
<td>1:</td>
<td>ISD of Argument Chain</td>
</tr>
<tr>
<td>2:</td>
<td>K</td>
</tr>
<tr>
<td>3:</td>
<td>First LOOP Constant ↓</td>
</tr>
<tr>
<td></td>
<td>First Argument ↑</td>
</tr>
<tr>
<td></td>
<td>First Scratch Slot ↓</td>
</tr>
<tr>
<td></td>
<td>Last Scratch Slot</td>
</tr>
<tr>
<td></td>
<td>Area for Iters 0 MOD K</td>
</tr>
<tr>
<td></td>
<td>Area for Iters K-1 MOD K</td>
</tr>
</tbody>
</table>

#### 4.3.4.1 The Frame

Codeblocks are classified as *procedure* or *inner loop* as described in Chapter 4.1. Their frames differ in the way arguments and constants are handled. The remainder of the frame structure is identical.

Slots are reserved in both kinds of frames as follows: the first slot contains a frame descriptor which points to the return area in the caller's own frame. This frame descriptor, therefore, must denote a globally unique frame address. The second slot contains the argument chain I-structure descriptor unless any of the following is true, in which case the slot will be empty:

- It is an inner loop codeblock, in which case arguments are sent directly and no chain is used.
- It is a procedure codeblock but the arity is zero or one, in which case a chain is unnecessary.
- It is a procedure codeblock but is being invoked by `DIRECT-APPLY`, in which case the arguments are sent directly as in the inner loop case.

The third slot is reserved for the invocation-time value of $K$, the bound on the degree of loop
The major difference between procedure and inner loop codeblocks shows up in the argument/constant area.

**Procedure Codeblocks** (Figure 4-15): A procedure codeblock may or may not include an outer LOOP, but in any event, it includes at most one. This LOOP may require a constant area to hold loop invariant values. Such constants are computed after procedure invocation but prior to execution of the loop. Therefore, constants are distinct from procedure arguments and are stored separately in the frame. Loop constants are assigned ordinal indices in the program graph, and these indices are mapped to offsets in the constant area of the frame. Arguments are handled by mapping the last to a fixed offset (3) in the frame, with the second-to-last occupying offset 4, and so on. Arguments are thus mapped in reverse order, from last to first, in the frame. The reason for this is slightly subtle.

The procedure linkage constraints imposed by the closure-based application scheme dictate that the APPLY instruction which detects that the arity is satisfied will forward the last argument (as supplied to the APPLY) and the argument chain descriptor (part of the closure) to the invoked procedure. Since the arity of the called procedure is not known, in general, at the time the caller is compiled, the means of sending the last argument must be independent of arity. Hence, it is the last argument, rather than the first, which appears at a fixed address in the frame. Note that this limitation does not affect the implementation of DIRECT-APPLY since it is specifically in this case that the called procedure's arity is known.

**Inner Loop Codeblocks** (Figure 4-16): An inner loop codeblock always includes a LOOP encapsulator. The loop constants are handled differently than in the case of a procedure codeblock. Here, the arguments to the codeblock include the loop constants. Therefore, there is no explicit constant area separate from the argument area, and the overhead of storing constants is subsumed by the passing of arguments to the codeblock.
Following the arguments and constants, slots are used as necessary to store arc values for the remainder of the codeblock. This area is largely unstructured, and slots are individually allocated. The exception to this rule is the case of codeblock invocation. Since procedure codeblocks in general return a result and a signal, and inner loop codeblocks return multiple results and a signal, a decision must be made. The caller can send multiple slot pointers to the called codeblock, one for each thing to be returned, or the caller can reserve a contiguous block of slots and send only a single pointer with the understanding of how multiple pointers should be derived from it. The latter scheme is by far more economical. Such contiguous blocks of slots are *procedure call subframes*, and their format is depicted in Figure 4-17.

Up to this point, all slots have been allocated statically. At compile time, the size of the frame so far is always known. Further, the use of such slots will always adhere to the write-once, read-many discipline.

Not surprisingly, loops confuse this order. From experience with the MIT Tagged-Token Dataflow machine [10] the benefit of exploiting inter-iteration parallelism is enormous, so enormous in fact that the resource requirements must be controlled [20]. These facts imply that there must be a way to have multiple iterations active concurrently, and that the resources consumed by such iterations must be reusable. The scheme used here is to map the frame storage requirements of a loop iteration (loop variables and temporaries) to a virtual frame, called an *iteration subframe*, and to allocate at codeblock invocation time enough frame storage for $K$ instances of the iteration subframe (Figure 4-18).
The 0th slot in each subframe is reserved for an Iteration Descriptor, whose function is discussed in section 4.3.5. The next n slots hold the n loop variables, with the remainder of the frame for loop temporaries. It is assumed that these subframes will be recycled modulo K, and the assumptions about write-once slots break down. These issues are addressed in section 4.3.5.

### 4.3.4.2 Assignment, Propagation, and Constraints

<table>
<thead>
<tr>
<th>Instruction or Encapsulator</th>
<th>Port Name</th>
<th>Slot Mapping</th>
</tr>
</thead>
<tbody>
<tr>
<td>LITERAL</td>
<td>Output</td>
<td>none if immediate</td>
</tr>
<tr>
<td></td>
<td></td>
<td>assigned - shared otherwise</td>
</tr>
<tr>
<td>LOOP-CONSTANT</td>
<td>Output</td>
<td>assigned - loop constant area</td>
</tr>
<tr>
<td>I-FETCH</td>
<td>Output</td>
<td>assigned - argument area if argument</td>
</tr>
<tr>
<td></td>
<td></td>
<td>assigned otherwise</td>
</tr>
<tr>
<td>IF</td>
<td>IfOutput</td>
<td>assigned</td>
</tr>
<tr>
<td></td>
<td>ThenInput</td>
<td>propagated - IfInput</td>
</tr>
<tr>
<td></td>
<td>ElseInput</td>
<td>propagated - IfInput</td>
</tr>
<tr>
<td></td>
<td>ThenOutput</td>
<td>constrained - IfOutput</td>
</tr>
<tr>
<td></td>
<td>ElseOutput</td>
<td>constrained - IfOutput</td>
</tr>
<tr>
<td></td>
<td>IfInput</td>
<td>none</td>
</tr>
<tr>
<td>LOOP</td>
<td>LoopOutput</td>
<td>assigned</td>
</tr>
<tr>
<td></td>
<td>PredicateInput</td>
<td>assigned - predicateOutput</td>
</tr>
<tr>
<td></td>
<td>BodyInput</td>
<td>assigned - loop variable area</td>
</tr>
<tr>
<td></td>
<td>BodyOutput</td>
<td>constrained - loop variable area</td>
</tr>
<tr>
<td></td>
<td>LoopInput</td>
<td>none</td>
</tr>
<tr>
<td>FASTCALL-DEF</td>
<td>Argument</td>
<td>assigned - argument area</td>
</tr>
<tr>
<td></td>
<td>Trigger</td>
<td>assigned - frame descriptor</td>
</tr>
<tr>
<td>FASTCALL-APPLY-INITIATE</td>
<td>Signal</td>
<td>assigned - termination signal</td>
</tr>
<tr>
<td></td>
<td>Result</td>
<td>assigned - result area</td>
</tr>
<tr>
<td>OTHERS</td>
<td>Output</td>
<td>assigned</td>
</tr>
</tbody>
</table>

After rewriting, the only remaining encapsulators are IF, FASTCALL-DEF, and LOOP. Encapsulators have outputs on both the "exterior" surface and on surfaces which enclose the basic blocks. Certain of these outputs are nontransparent, i.e., in the final expansion of the encapsulator, instructions will be generated which themselves produce the value associated with the output. Other outputs are transparent - the value associated with the output will have been created by an instruction other than the encapsulator itself and will appear elsewhere as an input to the encapsulator. It is possible to statically classify every output of every encapsulator as transparent or nontransparent, and for transparent outputs to identify the input or inputs from which the value will come.
Frame slots must be *assigned* to nontransparent outputs and *propagated* to transparent ones. Assignment implies that an output is marked as the originator of a value or set of values which will occupy a specified frame slot. In the event that arcs are merged (as in the LOOP and IF encapsulators), there will be two distinct instructions whose output arcs are mapped to the *same* slot number. This presents no problem of semantics for the same reason that MERGEs in the TTDA present no problem - the one-in, one-out property is always preserved when the schema (encapsulator) is viewed as a whole. In this case, the mapping to slot numbers is called *constrained*. The table shows, for each type of instruction port, the kind of frame slot mapping which applies.

### 4.3.4.3 Method

The method of mapping arcs to frame slot numbers in a codeblock is to traverse the graph from the root, which is always a single FASTCALL-DEF, first assigning nontransparent frame slot numbers to the root’s outputs, then mapping body arcs to frame slots. The former process is straightforward; for each argument output of the FASTCALL-DEF to which is connected a sink instruction, assign the corresponding predefined frame slot number. If this FASTCALL-DEF was the result of having rewritten a DEF, there will be two argument outputs, the argument chain (slot 1) and the last argument (slot 3). Otherwise, there will be *n* arguments, assigned to slots beginning with slot 3. If the trigger output has a sink instruction, it is assigned slot 0 (the return frame descriptor).

The latter process of mapping arcs in a basic block to frame slots is slightly more complex. First, for each instruction in the basic block, nontransparent frame slot numbers are assigned. Then, for each encapsulator, transparent frame slot numbers are propagated, constraints are applied, and mappings of arcs within the encapsulator’s basic blocks are done recursively.

In the case of literals, several optimizations are preformed. First, because certain literals are representable as immediate values, no frame slots need be assigned. A majority of literals are covered by this case, *e.g.*, small integers used to index conses and tuples. Second, it is unnecessary to reserve more than one frame slot for the same non-immediate literal value; instead, an association list is built during frame slot assignment to record the hardware type and value of each non-immediate literal and its assigned frame slot. Multiple literal instructions calling out the same value will use the same frame slot. Such frame slots are initialized during the prelude of the codeblock, and references to these slots need never cause suspension.

LOOPs present a special problem in addition to the issue of merged arcs discussed above. Since slots associated with circulating loop variables will be re-written from iteration to iteration, it must be the case that
• no rewriting of a slot is visible outside the LOOP (as would be the case of instruction A feeding instruction B as well as a LOOP input). A similar problem exists for non-immediate literals used as inputs.

• immediate literals used to initialize circulating variables are copied to frame slots prior to LOOP entry (an immediate can’t be re-written).

• no body input slot may be rewritten until the existing value is no longer needed in the current iteration.

• LOOP outputs are not accessible until the LOOP terminates. Using frame slots as the sole means of synchronization could potentially lead to the interpretation of an intermediate result as the final LOOP output.

Non-LOOP codeblocks are acyclic and, as a result, each arc will denote at most one value for each invocation. Consequently, the corresponding frame slots are written at most once per invocation. LOOPS present the possibility of re-writing slots during an invocation. Because of this, mapping of arcs within a LOOP is handled specially. While all other codeblock arcs are mapped into a single frame namespace, LOOP arcs are mapped to a separate namespace. When a codeblock is invoked, space is allocated to hold a single copy of the non-LOOP slots, and additional space is allocated to hold $K$ copies of the LOOP slots with the intent of allowing $K$ consecutive iteration bodies to run concurrently. The benefits of doing this are discussed [20] and are assumed to be a necessary requirement of any successful parallel execution model.

Keeping changes local to the LOOP is easily handled by simple analysis of each LOOP input - if it is not the sole sink, an IDENTITY instruction is inserted between the source and the LOOP input$^{34}$.

### 4.3.4.4 Summary

This section has reviewed the problem of allocating dynamic storage for an invocation as an extension to von Neumann methods. It has been shown that in order to exploit parallelism, e.g., across iterations, it is necessary to allocate significantly more storage than would be necessary in a sequential von Neumann paradigm. Another manifestation, although not explored here, is the difficulty (and additional storage space) of folding the program graph to permit re-use of slots during execution in the manner of traditional register allocation techniques. The difficulty, again, arises out of the multi-threaded (parallel) nature of the model.

---

$^{34}$Note that it is not enough that the LOOP encapsulator is the only sink for each source - it is possible that a single source feeds two distinct LOOP inputs. Unless these are explicitly separated by an IDENTITY instruction, the two LOOP variables will be aliases.
4.3.5 Machine Code Generation and Partitioning

After the program graph is re-written into a simpler form and frame slots have been assigned, machine code can be generated. This process is done by simultaneously translating program graph instructions into machine instructions and partitioning the generated instructions into SQ's. Both activities involve correctly reflecting the data dependences in the final codeblock module. As shall become clear, the process is distinctly different than that in the TTDA. Static dependences constrain code order within SQ's; dynamic dependences constrain the partitioning of code into SQ's and the choice of synchronization points.

4.3.5.1 Representation of Scheduling Quanta

As the program graph is translated, it is partitioned according to the constraints in Section 4.3.3. The internal representation of a scheduling quantum is shown in Figure 4-19. This abstraction is responsible for being the repository of translated instructions in the SQ. More importantly, this abstraction is used to enforce the constraints imposed by the architecture regarding register usage (fixed number, values not preserved across suspensions). The abstraction also summarizes the inputs to the SQ (these will always be frame slots - immediate literals are uninteresting, and registers can never be SQ inputs) and the termination signal slots.

Within the compiler, virtually all register references are symbolic. Allocation and deallocation of register numbers is automatic. The mapping of register names to register numbers is handled by the SQ abstraction, and invalidation of names across potentially suspensive instructions is enforced.

4.3.5.2 Mechanism for Translating a Program Graph Instruction

Program graph translation proceeds in a straightforward manner. The algorithm is divided into a driver, which understands graph structure but nothing of the semantics of the instructions to be translated, and a set of expanders, one for each program graph instruction. Expanders know nothing of graph structure and simply specify the translation of a program graph instruction to machine code as a function of the program graph instruction's properties, e.g., number of inputs and outputs, instruction parameters, and opcode. The specification of an expander is mechanically transformed (via a macro) into a function which performs the translation and then recursively calls the driver on the instruction's outputs. The driver selects program graph instructions for expansion when and only when all of the instruction's inputs have been expanded. This simple technique produces code within SQ's which is sequentialized according to the topological ordering of the original program graph.
4.3.5.2.1 The Driver

The driver is expressed as a few very simple functions which traverse the program graph. The Expand function invokes the appropriate expander for each program graph instruction; the expander in turn invokes ExpandOutputs as appropriate. This process treats encapsulators as instructions.

**Algorithm 4-11: GENERATE(ProgramGraph)**

- For each Instruction in ProgramGraph, mark it with an EnablingCount equal to the number of arcs incident on its Exterior surface.

- Invoke EXPAND on the Root Instruction.

**Algorithm 4-12: EXPAND(Instruction)**

Unless Instruction is marked,

- Mark it

- Invoke its Expander
Algorithm 4-13: EXPANDOUTPUTS(Instruction)

- For each Output on all surfaces of Instruction, Invoke EXPANDSINK on Instruction and Output

- If Instruction is an encapsulator, note the subordinate SQ descriptors created in expanding the instructions connected to the non-exterior outputs.

Algorithm 4-14: EXPANDSINK(SourceInstruction,SourceOutput)

For each SinkInstruction connected to SourceOutput of SourceInstruction, When the arc to SinkInstruction is incident on its Exterior surface,

- Decrement its EnablingCount.

- When the resulting EnablingCount is zero, mark the arc and invoke EXPAND on SinkInstruction.

4.3.5.2.2 The Expanders

The following operations are common to the expansion of each type of program graph instruction. They are added automatically to the specification of the semantics of each program graph instruction, thereby hiding details of the representation of scheduling quanta and the vagaries of the synchronization mechanisms of the model.

- Selection of an SQ: Partitioning by the method of dependence sets requires, for each program graph instruction, the computation of its input dependence set which uniquely defines the scheduling quantum to which the expanded instructions belong. At compile time, an association is maintained between dependence sets and scheduling quanta. New quanta are allocated each time a computed dependence set fails to map to an existing quantum. Scheduling quanta are static objects which must be explicitly triggered at runtime; therefore, the creation of a new quantum implies the need to install a trigger in an existing SQ.

- Computation of addressing modes: In translating a program graph instruction, reference is made to the input operands in the abstract - each input is an arc which logically denotes a value held in some physical resource, e.g., in the frame, in a register, or in the instruction itself as in the case of an immediate literal. Each arc and the instruction which feeds it uniquely define the hardware resource represented. The operand addressing information can therefore be computed by simple analysis of the instructions which feed the one in question. See Figure 4-20.

The compiler records a history of registers as output operands. Because the driver traverses the program graph according to topological ordering, it is possible to flag invalid references to registers at compile time.

- Addition of Synchronization: By the method of dependence sets it is known where synchronization will be required - for any input to any program graph instruction, synchronization is necessary at operand fetch time if the input comes from another scheduling quantum, directly (a static arc) or indirectly (a dynamic arc). The compile-time representation of scheduling quanta makes this determination straightforward.

- Test for Suspensiveness: Once synchronization tests have been applied, it is known (again, at compile time) if an instruction cannot suspend. When an instruction can be
[1] Binary Ops Abstract Translation:
<BinaryOp> Output, Input.0, Input.1

[2] Program Graph Instance:

[3] Resulting Concrete Translation

\[ SQ.9: \ldots \]
\[ \text{ADD Frame.39, Frame.3 (SYNC), Frame.18} \]
\[ \ldots \]

---

Figure 4-20: Abstract vs. Concrete Translation

proved non-suspensive, no updating of the register allocation information in its SQ is necessary. If, however, this cannot be proved, the instruction’s scheduling quantum abstraction is updated to show that no subsequent instruction may make reference to a value previously stored in any register.

4.3.5.3 Machine Code Generation

This section examines the (nearly) context-free expansion of program graph instructions into machine instructions, with no concern for the issues of partitioning, operand addressing / register allocation, synchronization, and so on as discussed above. The expansion is, however, a function of opcode, number of inputs and outputs, and other local, instance specific information.

4.3.5.3.1 Signals and Triggers

Signals and triggers were introduced into program graphs to make them well-connected, i.e., to guarantee that each instruction which should fire does fire (triggering), and that it is possible to determine when every instruction in a block which should fire has fired (signalling). Triggering and signalling are implicit under the von Neumann instruction execution model because there is only one locus of control. In a dataflow machine, however, it is much less straightforward. Certain instructions which themselves require no input, e.g., constant generators, must be explicitly initiated, hence the need for triggers. Other instructions which produce no output but are
only executed for effect, e.g., I-STORE, must be explicitly tested for completion, hence the need for signals.

How do signals and triggers apply to the hybrid instruction execution model? Not surprisingly, the von Neumann style of implicit signalling and triggering applies within an SQ, but the dataflow model of explicit signals and triggers must be enforced between SQ's. It would not do, for instance, to construct an SQ which receives only constant inputs and not to provide a means to initiate this SQ. Similarly, it would be necessary to provide some mechanism to detect termination of an SQ which produces no arc-carried results.

A simple technique would be to explicitly represent signal and trigger arcs in the compiled hybrid program. This, of course, is unnecessary and misses the opportunity for some good optimizations. Assume that the program graph is well connected. In what situations are signals and triggers essential?

**Triggers:** Literal constant instructions are the prime motivator for triggers. But as described previously, constants are handled by first eliminating all those which can be represented as immediate values, and second by loading frame slots during the codeblock's prelude with all other literals. Moreover, the method of dependence sets will never create an SQ which only has literal inputs. This follows by definition - an SQ depends directly on some set of dynamic arcs. It can be argued, therefore, that explicit representation of trigger arcs across SQ boundaries because of the need to trigger literal constants is unnecessary.

Note, however, that the mechanism of synchronization relies on an eager reading of a frame slot, possibly resulting in suspension of the SQ which attempted the read. Hence, it is necessary to initiate, or trigger, every SQ which will ultimately be expected to compute. This does not mean that all SQ's within a codeblock should be triggered at codeblock initiation. Rather, it means that SQ's should be triggered when and only when the program graph implies a triggering of any instruction in the SQ.

Such triggering is most conveniently done when a new SQ is formed by virtue of a dynamic arc. That is, the compilation of an instruction such as I-FETCH will include both the code to perform the fetch and the (implicit) code to trigger the SQ which was generated to receive the result\textsuperscript{35,36}.

\textsuperscript{35}The exception to this rule occurs in the SQ which reads the argument chain slot. There, the trigger is installed in the *distinguished* SQ. This allows the codeblock to be properly triggered irrespective of the way it was invoked (APPLY or DIRECT-APPLY).

\textsuperscript{36}A pathological case arises, using this method, whereby SQ's may be created which are completely empty or which contain nothing other than triggers for other SQ's. This case is handled by the SQ structural optimizer, discussed in a later section.
Signals: Signals are synthetic outputs generated by instructions which would otherwise have none, \textit{e.g.}, \textsc{i-store}. In the dataflow paradigm where each instruction is its own scheduling quantum, the primary evidence of an instruction having fired and, hence, the proof that a codeblock has terminated is the production of an output value. Signals are therefore necessary for proving that instructions like \textsc{i-store} have fired. Signals are collected by \textsc{signal-tree} instructions, and summary signal information is preserved and propagated from the innermost levels of a codeblock all the way to the signal input of the \textsc{fastcall-def}.

In the hybrid paradigm, signal generating instructions may be compiled within scheduling quanta along with other instructions. For that reason, adding signal outputs to \textsc{i-store} instructions in order to detect firing is not strictly necessary. The requirement is more appropriately to be able to detect \textsc{sq} termination and to be able to deduce firing. Moreover, explicit representation of signal arcs as synchronizable frame slots is only necessary between \textsc{sq}'s. Intra-\textsc{sq} signalling can be implicit in instruction order.

\textsc{signal-tree} instructions, therefore, need not be compiled as a tree of instructions which serve to test each individual signal. It is sufficient to generate code which merely tests for termination of all the \textsc{sq}'s whose instructions are connected to the \textsc{signal-tree}. This can be done by arranging the storing of a value into some frame slot as the last activity of an \textsc{sq} and then testing that slot. In many cases, this is an easily satisfied constraint on code order in the \textsc{sq} which requires no additional instructions and no additional slots. In the rare case that this is not possible, \textit{e.g.}, in an \textsc{sq} which must end with an instruction which does not unconditionally write to a known slot, an extra instruction and slot can be used as a dummy signal. In any case, there is no need to test signals which originate in the same \textsc{sq} as the \textsc{signal-tree} itself. The compiled signal tree tests each such slot in turn, suspending execution until the signal is written.

If codeblock termination detection were the only need for signals (it is not), signal arcs and \textsc{signal-trees} could be eliminated entirely, and a simple reference counting scheme could be
implemented to detect termination of all codeblock continuations. If the other uses for signals could be handled in a different way, this reference counting optimization could save instructions and frame slots. This is a matter for additional study.

4.3.5.3.2 UNARY and BINARY Instructions

![Diagram](image)

<Binary0p> Output, Input.0, Input.1

**Figure 4-22:** A BINARY Instruction and its Translation

Unary and binary instructions (arithmetic, logicauls, relationals) expand by a simple rule: generate a machine instruction with the same opcode as the program graph instruction, mapping input arcs to input frame slots, registers, or literals, and the output arc to the output frame slot or register (Figure 4-22).

4.3.5.3.3 I-FETCH and I-STORE

![Diagram](image)

IXSA Address, Structure, Index
STOR Signal, Address, Value

**Figure 4-23:** An I-STORE Instruction and its Translation

Recall that during program graph rewriting, all references to arrays, strings, tuples, and conses were simplified to I-FETCH and I-STORE. The translations of these to machine graph instructions are similar but not symmetric. The reason is, quite simply, that an indexed I-FETCH fits neatly into a three-address format while an indexed I-STORE does not. Hence, I-FETCHes are translated to single LOAD instructions, while I-STOREs are translated into a two-instruction suite: Index
Structure Address (IXSA) followed by STOR (Figure 4-23)\(^{37}\).

4.3.5.3.4 IF

![IF Encapsulator Diagram]

**Figure 4-24:** An IF Encapsulator and its Translation

The IF encapsulator represents both an opportunity and an obstacle. The advantages of having the entire IF and its enclosed instructions within a single SQ are significant, *cf.*, myriad SWITCH instructions in the TTDA. The biggest obstacle is in the firing semantics of the IF. As defined by the rewrite rules, IF is necessarily nonstrict. This is perfectly clear when IF is expanded to its lowest level form (SWITCHes and MERGES).

In order to reap the benefits of IF as an aggregate, it must be interpreted as a strict operation. Traub has demonstrated plausible, if contorted, instances of IF which are inherently non-sequential, *i.e.*, the order of instruction execution both inside and outside the IF depends on program input. Such non-sequential instances of IF can potentially be recognized by cycles through the IF in the program graph. For the sake of the present work, it was decided to compile IFs as if they were strict and to explicitly rewrite non-sequential IFs into their lower-level, *i.e.*, SWITCH based, representations.

Strict IFs are easily translated. The predicate is evaluated and a conditional branch around the

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\(^{37}\)In general, such multi-instruction suites benefit by having intermediate results stored in registers instead of frame slots. However, it is not always possible to do so when the suite may suspend at some point after the first instruction. This concern can be resolved at compile time by using registers for intermediates when the compiler can prove that such suspensions will not occur and frame slots otherwise. In the example, a register can be used for Address if and only if the access to Value is provably nonsuspensive.
recursively expanded THEN basic block is taken. At the end of the THEN code, an unconditional branch is inserted to redirect the flow of control to the end of the ELSE block. See Figure 4-24.

4.3.5.3.5 LOOP

Several assumptions are made in defining the expansion of LOOP encapsulators. As in the case of IF, the encapsulator is assumed to be strict in all of its arguments. Further, as in the TTDA, each codeblock is assumed to contain at most one LOOP. LOOP instances are restricted to execute on a single processor, unlike the TTDA which permits mapping of iterations across multiple processors. However, on that processor, \( K \) successive iterations may be active concurrently. In the event that there is inter-iteration parallelism in the program, this provides an additional source of work for hiding long-latency operations. In the frequent case of nested loops, \( K \)-unfolding of the the outer loop will allow \( K \) initiations of the next-innermore loop which are candidates for initiation on up to \( K \) processors, and so on. The argument also holds for loops which contain procedure invocations in either their predicate or body\(^{38}\).

Figure 4-25 gives the overall structure of LOOP translation. The wide arrows represent control flow within the LOOP SQ while thin arrows denote data dependences. LOOPs are translated as a sequence of instructions within a single SQ. This instruction sequence may fork subordinate SQ's within the predicate and body per the method of dependence sets, but the computation of such SQ's is constrained to complete prior to termination of a given iteration.

- **Loop constants** are stored in the frame’s constant area. For an inner loop, putting constants into the constant area is a side-effect of the codeblock invocation - the constant area is part of the argument area (see Section 4.3.4). For an outer loop, however, the arc-carried constants must be explicitly stored in the constant area. In both cases, references to constants can be nonsuspensive because no predicate or body instructions may execute until storage of constants is complete.

- **ITERATION-DESCRIPTORS** are initialized for each of the \( K \) iteration areas in the frame. An iteration area is a block of linearly addressed frame slots as described in Section 4.3.4. The first slot of each area holds the iteration descriptor (ID) for that area (section 3.2.4). The procedure is described below.

- The **first iteration** is started (described below).

- The **predicate** is evaluated.

- A **conditional branch** is taken to the loop epilog code if the predicate is **FALSE**, otherwise,

\(^{38}\)Experience with the TTDA has demonstrated the importance of unravelling in exploiting the parallelism inherent in a program. On the hybrid model, this argument is equally true. While a number of different translations are possible, the chosen one demonstrates the hybrid model's ability to permit parallel execution of successive iterations in a general way. While the technique does not map iterations across processors, the fact that each instance of an inner loop represents a separate invocation (potentially on a different processor) still permits a substantial multiplicative effect on available parallelism. Other compilation techniques can be used to support loop spreading without changes to the model. These are not investigated here but rather are identified as an opportunity for future work.
Figure 4-25: A LOOP Encapsulator Translation
• The next iteration is triggered.

• The body is evaluated.

• A barrier synchronization is performed on the termination of all subordinate SQ’s in the predicate and body, if there are any. Note that the initiation of the next iteration is independent of this barrier.

• Synchronizing slots are reset so that the iteration area can be reused.

• Termination of the iteration is signalled.

An iteration consists of the evaluation of the predicate and the subsequent evaluation of either the body or the loop epilog. Starting a given iteration requires the coincidence of three separate events:

1. Control Flow: The previous iteration has computed a TRUE predicate (call this CNTL\textsubscript{i}), and

2. Recycling: The \(i\)-\(K\)th iteration has terminated, thereby making the \(i \mod K\)th iteration area available for re-use (call this RECYC\textsubscript{i-K}), and

3. Importation: The \(i-K+1\)st iteration has indicated that its loop variables have been consumed, thereby permitting the slots in which they reside to be re-written (call this IMPT\textsubscript{i-K+1}).

This is depicted in Figure 4-26. It is straightforward to show that, of these conditions, the second is a necessary consequence of the first and third.

**Theorem 4-15:** For any iteration \(i\), the necessary and sufficient conditions for starting iteration \(i\) (INVOKE\textsubscript{i}) are CNTL\textsubscript{i-I} and IMPT\textsubscript{i-K+1}, or simply

\[
\forall i, \text{INVOKE}_{i} \iff \text{CNTL}_{i-I} \land \text{IMPT}_{i-K+1} \tag{1}
\]

**Given:** The invocation condition as stated above,

\[
\forall i, \text{INVOKE}_{i} \iff \text{CNTL}_{i-I} \land \text{IMPT}_{i-K+1} \land \text{RECYC}_{i-k} \tag{2}
\]

**Assume:** The recycling and importation conditions are logically separate. However, in general, freeing the loop variable slots prior to iteration termination implies explicit copying of the variables out of these slots. It is assumed that there is little, if any, benefit in doing this and that it is reasonable to assume that both conditions are equivalent, i.e.,

\[
\forall i, \text{RECYC}_{i} \iff \text{IMPT}_{i} \tag{3}
\]

Moreover, since predicate evaluation for a given iteration implies that the iteration must have been invoked,

\[
\forall i, \text{CNTL}_{i} \Rightarrow \text{INVOKE}_{i} \tag{4}
\]

**Proof Idea:** At the point of invocation INVOKE\textsubscript{i}, the condition RECYC\textsubscript{i-K} can be deduced. In the proof below, the universal quantifiers have been dropped but are implicit.
Figure 4-26: Constraints on Recycling of Iteration Areas

Proof: \((\Leftarrow)\)

\[
\begin{align*}
\text{CNTL}_{i-1} \land \text{IMPT}_{i-K+1} & \quad \text{antecedent} \\
\text{CNTL}_{i-1} \land \text{IMPT}_{i-K+1} \Rightarrow \text{INVOKE}_{i-1} \land \text{IMPT}_{i-K+1} & \quad \text{by [4]} \\
\text{INVOKE}_{i-1} \land \text{IMPT}_{i-K+1} & \quad P \land \neg(P \lor Q) \\
\text{INVOKE}_{i-1} \iff \text{CNTL}_{i-2} \land \text{IMPT}_{i-K} \land \text{RECYC}_{i-k} & \quad \text{by [2]} \\
\text{CNTL}_{i-2} \land \text{IMPT}_{i-K} \land \text{RECYC}_{i-k} \land \text{IMPT}_{i-K+1} & \quad \text{substitutivity} \\
\text{IMPT}_{i-k} & \quad \text{selection} \\
\text{RECYC}_{i-k} & \quad \text{by [3]} \\
\text{CNTL}_{i-1} \land \text{IMPT}_{i-K+1} \land \text{RECYC}_{i-k} & \quad \wedge \text{antecedent} \\
\text{INVOKE}_{i} & \quad \text{by [2]}
\end{align*}
\]

Proof: \((\Rightarrow)\)

\[
\begin{align*}
\text{INVOKE}_{i} & \quad \text{antecedent} \\
\text{CNTL}_{i-1} \land \text{IMPT}_{i-K+1} \land \text{RECYC}_{i-k} & \quad \text{by [2]} \\
\text{CNTL}_{i-1} \land \text{IMPT}_{i-K+1} & \quad \text{selection}
\end{align*}
\]

It is now easy to understand the function of the STPC and STIM machine ops. STPC (SeT Program Counter) signals the CNTL\(_{i}\) condition, meaning that the predicate has evaluated to TRUE in iteration \(i\). It is represented as a boolean flag in the iteration descriptor for iteration area \(i+1 \mod K\). The STIM (SeT IMport flag) op signals IMPT\(_{i}\), meaning that iteration \(i\) has ended and that no further access to the loop variables for that iteration will be made. It is represented as a boolean flag in the descriptor for iteration \(i-1 \mod K\).

Termination of an iteration implies that all BodyOutput\(,n\) inputs to the LOOP have produced
results and that subordinate SQ's triggered in the process have terminated. The former condition is subsumed by the latter and that all predicate and/or body instructions in the LOOP's SQ have executed (a simple assertion to make based on the program counter). Thus, the only problem is to detect SQ termination. For this, an iteration area slot is allocated per subordinate SQ (there may be none), and each subordinate is amended to store into this slot upon termination. In the LOOP's SQ, then, it is only necessary to probe (suspensively) these slots with TSTN ops as appropriate.

Prior to issuing the STIM, signalling the end of the iteration, all slots in the iteration area which are used for explicit synchronization (i.e., those which will be read suspensively) must be reset\textsuperscript{39}. The iteration area slots which must be reset are exactly the following:

- The loop variables. These synchronize production of values in iteration \( i \) and consumption in iteration \( i+1 \).
- Inputs to subordinate SQ's. These synchronize the action of threads of computation which go on in parallel with the LOOP SQ.
- BodyOutput\textsubscript{n} inputs to the LOOP which are dynamic arcs.

An interesting optimization results if loop variables are constrained in their fanout such that

- within the body of the current iteration they have no sinks (e.g., a nextrified variable used on the right hand side in a loop body).
- within the predicate of the next iteration they have but a single sink, or, within the predicate they have no sink but within the body they have but a single sink.

Under these conditions, it is possible to use the nonsticky addressing mode on the single predicate sink or the single body sink, as appropriate, to obviate the need for explicitly resetting the slot. A tradeoff exists in that loop variables which do not satisfy the constraints can be transformed into ones that do, but the cost of doing so (essentially introducing MOVE instructions as identities so as to guarantee unity fanout) in some cases outweighs the benefit of eliminating explicit RSTNs.

For other slots requiring reset, unity fanout implies that the resetting can always be done by the reader. Further, non-unity fanout within a single SQ can be similarly optimized by making the last reader perform the nonsticky reference.

\textsuperscript{39}In models such as Monsoon [47], slots are self-cleaning in that they are associated with instructions in a graph which self-clean at the abstract interpreter level. Slots in the hybrid model are instead associated with instruction outputs with unrestricted fanout, the readers of which may be in different SQ's. In general, then, no reader of any slot may be labeled \textit{a priori} as the last reader, because the readers are at best partially ordered. In the body of a codeblock (outside of any LOOP), slots are written at most once, and cleanup is implicit in the process of frame allocation and deallocation. It is only within a LOOP that the issue of slot-resetting arises.
4.3.5.3.6 FASTCALL-DEF

FASTCALL-DEF implements the *invoked* half of basic procedure linkage\(^{40}\). It is responsible for triggering the enclosed codeblock, returning the codeblock results to the invoker, and finally sending a termination signal. This is implemented in a straightforward fashion by expanding the body of the FASTCALL-DEF and then generating suspensive Move Remote (MOVR) instructions for each result. The procedure linkage protocol mandates the return of a signal - if the codeblock generates one, it is returned to the invoker via a suspensive MOVR. If no signal is generated, a dummy signal is sent after the results have been sent. See Figure 4-27.

4.3.5.3.7 FASTCALL-APPLY-BEGIN

FASTCALL-APPLY-BEGIN implements the *invoker* part of basic procedure linkage\(^{41}\). It is responsible for allocating a fresh context and sending the arguments to the new frame.

---

\(^{40}\)Recall that DEF argument chain unpacking is, at this point, handled by program graph instructions which are separate from the FASTCALL-DEF.

\(^{41}\)Recall that APPLY and DIRECT-APPLY have been re-written by this point into instances of FASTCALL-APPLY, which subsequently get rewritten into instances of FASTCALL-APPLY-BEGIN and one other instruction which disposes of the called context.
The frame descriptor (FD) for Codeblock is allocated and stored in the InvokedContext frame slot. A procedure call subframe for the returned signal and the result(s) has already been allocated during frame slot assignment, starting at the signal slot (see section 4.3.4). This slot number is added to the current context (frame descriptor), yielding a new frame descriptor which points to the procedure call subframe. This descriptor (stored in a register) is forwarded to the 0th slot of the invoked frame (per section 4.3.4) by a MOVFR instruction. The arguments are likewise forwarded to the appropriate argument slots by MOVFR instructions. See Figure 4-28.

4.3.5.4 Summary
This section has presented the issues which surround the translation of program graphs into partitioned machine code, and a set of methods for handling them. Significant among the issues are the dichotomy of synchronization methods, implicit and explicit, and the optimizations which are made possible thereby.

It is clear that this dichotomy, if it is to be used to advantage, makes the task of code generation significantly harder than in the TTDA case and, arguably, than in the von Neumann case. This is because both paradigms (read: both sets of problems) are present in the hybrid model.

The techniques developed in this study demonstrate the benefit of keeping the issues of partitioning and operand addressing separate from the semantics of code generation. Here, both partitioning and operand addressing are done algorithmically, and the specification of these algorithms is completely independent of the specification of program graph instruction translations. At a pragmatic level, this made experimentation with the instruction set possible. At a higher level, it demonstrates that the complexity of the hybrid model is entirely manageable within a traditional compiler mind set.

4.3.6 Optimizer
Two types of SQ structural optimization are performed on the codeblock after all program graph instructions have been translated.

4.3.6.1 Optimization 1: Null SQ Elimination
The first of these optimizations strips out degenerate SQ’s which are a consequence of the implementation of the Method of Dependence Sets. Because abstract translation is specified separately from the mechanism of allocating and installing triggers for SQ’s, it occasionally the case that an SQ shell is eagerly created into which no machine instructions are actually generated. Here, a distinction is made between instructions which trigger SQ’s and all others. The latter instructions are called live instructions. A null SQ is defined as one with no live instructions. For
each null SQ, the SQ and its trigger (which appears in some other SQ) can be removed. This will remove both the truly empty SQ's and those which merely contain triggers for other SQ's. In the latter case, the triggers are moved backwards toward the distinguished SQ until a non-null SQ is found\(^{42}\). Suppose, for example, non-null SQ A triggers SQ B. B contains no instructions - only a trigger to C. Therefore, B can be eliminated, as can be the trigger for B which appears in A. In its place, the trigger for C is installed.

4.3.6.2 Optimization 2: Tail Call Elimination

For all the cases where SQ A ends with a trigger to SQ B, a new SQ is formed by appending B to the end of A. It is easily shown that neither of these transformations corrupt the assertions previously made about the introduction of cycles as a function of the partitioning.

4.3.7 Assembler

The final phase in the compilation is the Assembler, which translates the partitioned graph of machine instructions into a format suitable for the emulator. At this stage, the partitioned program graph looks like a set of instruction lists, one per SQ. The distinguished SQ is so marked. The output file format consists of some codeblock property information (e.g., number of base and iteration frame slots to be allocated upon invocation) followed by the contents of the SQ’s, distinguished first\(^{43}\).

As SQ’s are written, triggers are transformed into Continue (CNTN) instructions. CNTN, when executed, causes a new continuation to be formed and executed. By definition, all non-constant arcs which are input to an SQ imply synchronization. Therefore, the most common situation is that the first instruction of the SQ, when executed, makes a suspensive reference to one or more frame slots. Consider the reference to the very first slot. If it is full, instruction execution proceeds normally. If it is empty, the newly-created continuation will immediately suspend.

An important optimization of this relies on the fact that the CNTN instruction which creates the continuation itself references no frame slots. A variant on this instruction, Continue Test (CNTT), can test exactly one frame slot for the presence or absence of a value. CNTT creates a continuation, and tests this slot. When a value is present, the continuation is scheduled for execution just as in the case of CNTN. If no value is present, the continuation is immediately put into the suspended state, potentially saving an explicit suspension. For each trigger, the assembler is

\(^{42}\)This process is guaranteed to succeed because all triggers are traceable to the distinguished SQ, and the distinguished SQ is always non-null.

\(^{43}\)Output files are encoded in CIOBL, a system-independent format which is described in [58].
responsible for determining which frame slot the denoted SQ will test first and for manufacturing an appropriate CNTT instruction.

4.4 Summary
In this Chapter, the structure, instructions and manipulated data types of the dataflow program graph have been reviewed. Dataflow program graphs are made up of both simple instructions and encapsulators, the latter capturing notions of iteration, conditional execution, and procedure linkage.

Also in this Chapter, the method of generating code under the new parallel machine language model has been presented in detail. Key problems in performing the translation include keeping the abstract translation of instructions separate from the issues of partitioning. The partitioning method and its properties have been formally presented.
This chapter presents experimental results from the first set of simulation studies of the hybrid architecture along with a comparison to similar results from studies of the TTDA. Section 5.1 considers the tradeoff between the dataflow regime and the von Neumann regime given the notion of explicit synchronization cost as motivated by the hybrid architecture. Section 5.2 considers the behavior of a collection of benchmark programs as compiled for the hybrid architecture and as executed by the idealized machine.\footnote{The compiler used in this study was version 3.5, and the interpreter was at version 5.0.} The results reflect the characteristics of the programs subject to the hybrid partitioning constraints. A comparison is made to the TTDA which shows how the hybrid’s less powerful instructions can be used in place of TTDA instructions with little change in dynamic instruction counts. Also in this section, the costs and benefits of dynamic loop unfolding are studied. Section 5.3 examines the behavior of the realistic model using these same benchmark programs. The costs of aborted instructions (due to synchronization tests which fail) and multi-ported access to the local memory are considered. Data cache effectiveness is studied.

5.1 Making Synchronization Costly

A prime thrust of the hybrid architecture, as viewed from the dataflow perspective, is that synchronization operations should be explicit rather than implicit. Said another way, the hybrid architecture offers a change in point of view: synchronization should cost something, and means should be provided for managing this cost. In this section, two simple example graphs are analyzed to show the tradeoff between implicit and explicit synchronization. To the extent that

![Sequence, Fork, and Join](image-url)
real costs can be assigned to this explicit synchronization under both the pure von Neumann and hybrid models, the economics of moving from pure von Neumann, through hybrid, to dataflow can be understood.

The analysis hinges on assessing the costs of the three forms of program graph instructions shown in Figure 5-1. These program graph instructions will have specific machine instruction realizations which make the differences more apparent. Each is considered, in turn, under the dataflow regime and the hybrid regime. For the sake of this analysis, it is assumed that the von Neumann regime is a degenerate case of the hybrid regime with presumably higher costs for synchronization due to lack of specific hardware support.

5.1.1 Sequential Execution

Under the dataflow model, execution of a sequential thread is conceptually straightforward. A token is created as the result of having executed one instruction, said token then enabling the execution of the next sequential instruction. From the standpoint of graph semantics, it is necessary that all information to be communicated from one instruction to the next be encoded on the token. That is, instruction execution must be independent of any pervasive "state." Operationally, because the stages in dataflow instruction execution (synchronization, instruction fetch, computation, token formation) are essentially sequential, the time to execute any such thread is proportional to the product of the pipeline depth and the thread length.

Under the hybrid and pure von Neumann models, execution of a sequential thread is notably different. Once initiated, a thread occupies the pipeline until termination, however short or long a time that may be. In an abstract sense, the execution of the thread is atomic in that intermediate state changes in the processor are invisible outside the thread, or, more importantly, that state can be communicated between instructions in the thread implicitly. Operationally, instructions can be dispatched at successive pipe beats, and the time to execute the thread is the sum of the pipeline depth and the thread length.

5.1.2 Forks

In the TTDA model and its derivatives, each invoked instruction can produce two (or more) tokens destined for distinct successor instructions. That is, the fork operation is implicit in virtually every instruction\textsuperscript{45}. There is no explicit cost for spawning a new thread of computation. Therefore, forks at the dataflow program graph level are represented solely by the machine instruction producing the value.

\textsuperscript{45}There are exceptions to this generalization which are beyond the scope of this discussion and which do not substantially alter this analysis.
In the hybrid paradigm, a new thread of computation must be explicitly started with the `CNTN` or `CMTT` instructions. The implementation of the depicted fork operation, then, would take two machine instructions - one to compute the value and another to perform the fork. Here, then, is one clear cost of expressing parallelism: each parallel thread of activity must bear the cost of at least one instruction to start it. In the pure von Neumann model, the cost will be substantially higher because instruction sets lack the general notion of a fork.

5.1.3 Joins
In both the dataflow and hybrid regimes, synchronization of two threads of computation can be done in a single instruction, although there are still subtle differences. In the dataflow model, the synchronization name is the instruction itself, known to both threads. In the hybrid model, it is the arc, and not the instruction, which is the basis for synchronization naming.

5.1.4 Analysis
Given these constraints, consider the following two examples (Figure 5-2). In the first, the program graph to be executed is a simple linear sequence of instructions. In the second, a binary tree of fork operations is followed by an inverted tree of join operations. These examples are chosen not purely for their simplicity: the first is the limiting case of sequentiality, and the second is the limiting case of parallelism given binary fan-out, a single graph input, and a single graph
output. In execution, it is interesting to count the number of pipeline beats required for execution as a function of the number of instructions $n$. Assume unit time for each instruction.

In the sequential case, a dataflow machine will clearly take $Pn$ cycles, where $P$ is the pipeline depth of the machine. The hybrid and pure von Neumann machines will take only $n$ cycles.

In the parallel case, for sufficiently large values of $n$, the idle cycles in a dataflow machine at the very beginning and very end of execution can be ignored. The dataflow machine, therefore, will take $n$ cycles to compute the graph. In the hybrid case, however, extra instructions will be executed to fork the parallel computation. It is easy to show that the number of extra instructions is exactly

$$\frac{n-1}{3}$$

This assumes unit execution time for fork instructions. Therefore, the total number of cycles in the hybrid case is

$$\frac{4n-1}{3}$$

It is possible to estimate the equivalent number for the pure von Neumann case by assuming a non-unit cost $T$ for each fork instruction, corresponding to the overhead of creating and managing a software task. The cost is exactly

$$\frac{3n+Tn+2T-3}{3}$$

or, for $T \gg 1, n \gg 1$,
The ensuing tradeoff between the three regimes, as a function of degree of parallelism (or sequen-
tiality, depending on one’s point of view)\textsuperscript{46}, is depicted in Figure 5-3. While the exact shape of
the curves is not known, it is clear that the endpoint constraints must be met. Assuming these
functions are monotonic, it can be argued that above some level of parallelism, the pure dataflow
approach is better, but the degradation factor of compiling even the most highly parallel graph for
the hybrid machine results in only a modest increase in cycle count (33\% by this simplistic analysis)\textsuperscript{47}. However, below this level of parallelism, the hybrid model has the potential of
executing fewer total cycles than either the dataflow or the pure von Neumann models.

It remains to be demonstrated that this crossover point does indeed occur for real programs. In
the next section, a number of benchmarks are presented which demonstrate an even more remark-
able characteristic - that the hybrid model is capable of executing fewer cycles than a dataflow
machine by actually \textit{executing fewer instructions}, while still retaining the ability to exploit fine-
grained parallelism. This savings comes from the elimination of unnecessary forking, fan-out
\textbf{IDENTITY}, and signalling instructions which is attributable to program counter sequencing
within an SQ.

\subsection*{5.2 Idealized Model}

This section examines static and dynamic characteristics of a number of small benchmark
programs using the hybrid code generator and an implementation of an idealized model inter-
preter. The purpose is to better understand the effects of partitioning dataflow graphs, and to
establish a baseline of performance for studies to be done on the realistic model. In the course of
these experiments, comparisons are made to the TTDA. These comparisons come from executing
exactly the same programs (same sources, actually) on the GITA interpreter. This provides some
insight as to where these applications sit on the sequential / parallel axis presented in the last
section. It is shown that, for a number of cases, it does indeed happen that the hybrid model
executes fewer instructions (and thereby fewer cycles) than the TTDA.

\begin{footnotesize}
\footnote{\textsuperscript{46} The software cost of forking, $T$, is assumed to be \textit{minimally} on the order of tens of instructions, although it is more probably in the thousands.}

\footnote{\textsuperscript{47} The single input / single output constraint bears on this outcome. However, relaxing this to the point where each instruction must be implemented in the hybrid case as an individual thread, the penalty over the dataflow model is only a factor of two.}
\end{footnotesize}
5.2.1 Static Statistics

A number of example programs\footnote{These programs were taken from the ID Library and were not created by the author. Most, if not all, of these are attributable to R. S. Nikhil and K. R. Traub.} have been chosen to characterize this architecture. This section presents the static characteristics of a cross-section of these programs, chosen according to the architectural features which they exercise. The table gives the total static instruction count, the total number of SQ's, length of shortest and longest SQ's, and the mean SQ length.

<table>
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<th>Codeblock</th>
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<td>54</td>
<td>31.50</td>
</tr>
<tr>
<td>MULTIWAVE</td>
<td>68</td>
<td>10</td>
<td>1</td>
<td>32</td>
<td>6.80</td>
</tr>
<tr>
<td>WAVEFRONT</td>
<td>67</td>
<td>11</td>
<td>1</td>
<td>15</td>
<td>6.09</td>
</tr>
<tr>
<td>WAVEFRONT-0</td>
<td>56</td>
<td>7</td>
<td>1</td>
<td>31</td>
<td>8.00</td>
</tr>
<tr>
<td>WAVEFRONT-0-0</td>
<td>53</td>
<td>7</td>
<td>1</td>
<td>34</td>
<td>7.57</td>
</tr>
<tr>
<td>WAVEFRONT-1</td>
<td>51</td>
<td>8</td>
<td>1</td>
<td>33</td>
<td>6.37</td>
</tr>
</tbody>
</table>

Procedures from the first group were taken from the Id Basic Library. The instruction count is attributable primarily to the parameter passing overhead. Recall that arguments to a procedure are treated as dynamic synchronized arcs. Hence, the number of SQ’s will be bounded from below by one (the distinguished SQ) plus the number of arguments. Hence, the monadic function ABS is made up of two SQ’s, while the dyadic AND is made up of three. The number of instructions is similarly bounded from below: there will be one instruction to trigger each SQ other than the distinguished one, one instruction to return the termination signal, one instruction for each result value, plus the body of the function. In the case of ABS, there is one result and one instruction (ABS) in the body. Although AND has a single-instruction body, the counts
reflect the addition of another SQ which *conditionally* unpacks the argument chain in the case that DIRECT-APPLY linkage is not used. Statically, two additional instructions are added (one to trigger the extra SQ, and one instruction in that SQ to read the first argument in the chain). Dynamically, however, the situation is a bit different as discussed below. The dynamic instruction count depends on the method of invocation - if DIRECT-APPLY is used, the dynamic instruction count will be less than the static figure.

Procedures in the next group are slightly more complex. The simplest procedure is EXPRESSION, which evaluates $b^2 - 4ac$. Its longest SQ is the distinguished one which triggers five other SQ's, then synchronizes on the availability of the result, returns it, and then returns a signal. A more elaborate procedure is IF_EXPR, which compares two numbers and then returns a tuple consisting of the larger number followed by the difference between the two numbers. At the other end of the spectrum are recursive Fibonacci (FIB) and triply-nested loops in matrix multiplication (MM). Because no codeblock may contain more than one loop, MM is split by the compiler into three codeblocks - one for the main procedure and outermost loop, and one each for the remaining two loops. The interface to these two subordinate codeblocks is via the FASTCALL protocol. The next group represents the codeblocks for MERGESORT which operate on lists. As in the case of the previous group, procedures which invoke subordinate codeblocks (either nested loops or procedures) and/or involve the manipulation of structures (a dynamic arc per reference) have a significant number of SQs and a correspondingly short mean SQ length.

The next group is the If Transcendental Library. These procedures are interesting in that they involve no loops but rather the evaluation of a Maclaurin series expansion as a large expression. Because there are no subordinate codeblocks and no I-structures, there is a higher ratio of computational instructions to dynamic arcs, resulting in fewer, longer SQs.

WaveFront and MultiWave are also included, and are discussed below.

5.2.2 Dynamic Characteristics
<table>
<thead>
<tr>
<th>Codeblock</th>
<th>Instr</th>
<th>Critical Path</th>
<th>Aborts</th>
<th>% Aborts</th>
<th>Arith</th>
<th>% Arith</th>
<th>Run Length</th>
</tr>
</thead>
<tbody>
<tr>
<td>ABS 1</td>
<td>4</td>
<td>4</td>
<td>1</td>
<td>25.00</td>
<td>1</td>
<td>25.00</td>
<td>1.3</td>
</tr>
<tr>
<td>AND ST $T$</td>
<td>5</td>
<td>5</td>
<td>1</td>
<td>20.00</td>
<td>1</td>
<td>20.00</td>
<td>1.7</td>
</tr>
<tr>
<td>ARRAY $&lt;0 10&gt;$</td>
<td>7</td>
<td>8</td>
<td>1</td>
<td>14.29</td>
<td>0</td>
<td>0</td>
<td>1.7</td>
</tr>
<tr>
<td>+ 12</td>
<td>5</td>
<td>5</td>
<td>1</td>
<td>20.00</td>
<td>1</td>
<td>20.00</td>
<td>1.7</td>
</tr>
<tr>
<td>EXPRESSION 1 2 3</td>
<td>11</td>
<td>8</td>
<td>1</td>
<td>9.09</td>
<td>4</td>
<td>36.36</td>
<td>1.8</td>
</tr>
<tr>
<td>FIB 10</td>
<td>3,265</td>
<td>187</td>
<td>265</td>
<td>8.12</td>
<td>441</td>
<td>13.51</td>
<td>3.4</td>
</tr>
<tr>
<td>FOR_LOOP 1000</td>
<td>7,030</td>
<td>7,028</td>
<td>1</td>
<td>0.01</td>
<td>3,001</td>
<td>13.51</td>
<td>42.69</td>
</tr>
<tr>
<td>IP_EXPR 1 2</td>
<td>17</td>
<td>11</td>
<td>3</td>
<td>17.65</td>
<td>2</td>
<td>11.76</td>
<td>2.4</td>
</tr>
<tr>
<td>MM 10x10</td>
<td>23,569</td>
<td>21,924</td>
<td>2,432</td>
<td>10.32</td>
<td>4,352</td>
<td>18.46</td>
<td>3.7</td>
</tr>
<tr>
<td>MERGESORT &lt;20...1</td>
<td>16,053</td>
<td>2,910</td>
<td>3,104</td>
<td>19.34</td>
<td>430</td>
<td>2.68</td>
<td>2.2</td>
</tr>
<tr>
<td>ATAN 0.1 1</td>
<td>110</td>
<td>70</td>
<td>5</td>
<td>4.55</td>
<td>22</td>
<td>20.00</td>
<td>10.0</td>
</tr>
<tr>
<td>COS 0.1</td>
<td>42</td>
<td>42</td>
<td>1</td>
<td>2.33</td>
<td>23</td>
<td>53.49</td>
<td>14.3</td>
</tr>
<tr>
<td>LOG 0.1</td>
<td>34</td>
<td>32</td>
<td>1</td>
<td>2.94</td>
<td>17</td>
<td>50.00</td>
<td>11.3</td>
</tr>
<tr>
<td>SIN 0.1</td>
<td>42</td>
<td>41</td>
<td>1</td>
<td>2.38</td>
<td>21</td>
<td>50.00</td>
<td>14.0</td>
</tr>
<tr>
<td>SQRT 0.1</td>
<td>51</td>
<td>49</td>
<td>1</td>
<td>1.96</td>
<td>23</td>
<td>45.10</td>
<td>17.0</td>
</tr>
<tr>
<td>MULTIWAVE 15x15x2</td>
<td>12,769</td>
<td>5,694</td>
<td>538</td>
<td>4.21</td>
<td>2,787</td>
<td>21.83</td>
<td>5.4</td>
</tr>
<tr>
<td>WAVEFRONT 15x15</td>
<td>5,894</td>
<td>5,030</td>
<td>262</td>
<td>4.45</td>
<td>1,294</td>
<td>21.95</td>
<td>5.6</td>
</tr>
</tbody>
</table>

In this section, the example programs are analyzed using an idealized mode emulator for the hybrid architecture. The emulator is described in more detail in Appendix A. As part of the emulation, a number of statistics are gathered, and a subset of these are presented in the table. They are

- **Instruction Count**: Each successfully-executed instruction is counted. Aborted instructions (those which do not complete due to a synchronization blockage) are not counted.

- **Critical Path**: Given a notion of one instruction executing in unit time and a time axis with zero corresponding to the initiation of the procedure, this is the least time after which the parallelism profile is identically zero.\(^{49}\)

- **Aborts**: Each aborted instruction is counted - if an instruction aborts more than once (e.g., two synchronizing input operands), it is so counted. Aborts are also expressed as a percentage of Instruction Count. While it has never happened in practice, it is possible to have a value greater than 100% here.

- **Arithmetic Instructions**: Each successful ALU operation (arithmetic, logical, relational) is counted - the value is also expressed as a percentage of the Instruction Count.

- **Run Length**: A measure of the mean time between context switches (see Section 4.2.1).

\(^{49}\)This definition is due to Arvind.
5.2.2.1 Assumption

It is assumed that multiple suspended reads against a single frame slot are rare. This assumption is borne out by the relatively low percentage of aborted instructions (each abort causes a suspension against a slot). Given a low percentage of total aborts, the probability of multiple, simultaneous suspensions against a single slot is correspondingly low. Hence, multiple suspensions are "stored" in a single slot in the same way a single suspension is.

The statistics gathered establish a "best case" baseline for additional analysis in later sections. To that end, $K$ has been set to its minimum value of two. In a later section, the effect of $K$ will be analyzed in some depth.

5.2.2.2 Analysis

In the first group of benchmarks, the dynamic cost of procedure invocation is demonstrated. As expected, the instruction count for monadic procedures matches the static instruction count (c.f., the Static table), while procedures with more than one argument show fewer dynamic instructions\textsuperscript{50}. Arithmetic counts correspond to the "useful" instruction in the body. Abort percentages are artificially high only because the number of instructions is so low. Mean run length is correspondingly short.

In the second group, FOR_LOOP shows a mean run length of 7.0. The loop itself is 7 instructions long, and because inter-iteration arcs are treated as dynamic, each inner loop instance is a separate SQ invocation. Thus, a sequence break occurs between iterations. By contrast, the run length in MM (matrix multiplication) is shorter because the inner loop body contains imbedded dynamic arcs (two I-FETCH instructions for the elements being multiplied) and, consequently, several short SQ's instead of a single, longer one. MM will be revisited in Section 5.2.2 where the cost of $K$-unfolding is studied.

As expected, the trigonometric procedures are very efficient: because there are no imbedded procedure calls, inner loops, or structures, there are no internal dynamic arcs. Further, these routines are all monadic (excepting ATAN). The resulting partitioning maps all instructions into the same dependence set, and no dynamic synchronizations (save references to the argument) are done\textsuperscript{51}.

\textsuperscript{50}The interpreter uses the DIRECT-APPLY protocol for invocation at top level.

\textsuperscript{51}Although possible, the existing code generator does not optimize the case of multiple references to a dynamic arc's slot within the same SQ; all references are coded as synchronizing. Dynamically, of course, only one suspension can actually take place for a given SQ\slash operand pair. However, the instruction dispatcher will treat each such reference as potentially suspensive, admitting context swapping. Such an optimization is worthwhile and relatively straightforward to implement.
5.2.2.3 The Cost of K-Unfolding

The ability to unfold successive iterations of a loop has significant value in the dataflow environment for exposing parallelism. In the hybrid case, the motivation is similar, but given that no mechanism is provided at the hardware level for spreading iterations of a single loop across processors\(^{52}\), there is little benefit to unfolding inner loops in some cases. Moreover, the cost of inner loop unfolding is noteworthy, particularly for simple inner loops where the loop body is on the order of the size of the iteration set-up code.

Unlike the TTDA scheme, there is a clear cost in the hybrid model for loop unfolding in terms of additional synchronization instructions and frame area, and this cost scales with \( K \). Hence, for any one program instance, there must be some optimum value of \( K \) which balances exposed parallelism against execution of overhead instructions.

<table>
<thead>
<tr>
<th>MM, Various Unfoldings</th>
</tr>
</thead>
<tbody>
<tr>
<td>Loops</td>
</tr>
<tr>
<td>-------</td>
</tr>
<tr>
<td>1</td>
</tr>
<tr>
<td>2</td>
</tr>
<tr>
<td>10</td>
</tr>
<tr>
<td>16</td>
</tr>
<tr>
<td>1</td>
</tr>
<tr>
<td>2</td>
</tr>
<tr>
<td>3</td>
</tr>
<tr>
<td>4</td>
</tr>
<tr>
<td>5</td>
</tr>
<tr>
<td>6</td>
</tr>
<tr>
<td>7</td>
</tr>
<tr>
<td>8</td>
</tr>
<tr>
<td>9</td>
</tr>
<tr>
<td>10</td>
</tr>
<tr>
<td>11</td>
</tr>
<tr>
<td>12</td>
</tr>
<tr>
<td>13</td>
</tr>
<tr>
<td>14</td>
</tr>
<tr>
<td>15</td>
</tr>
<tr>
<td>16</td>
</tr>
</tbody>
</table>

The first set of matrix multiplications (MM) was chosen specifically to show the effects of large values of \( K \) on inner loop unfoldings. The table shows, as a function of the number of concurrent iterations (Loops) and \( K \) (\( K = \text{Loops} + 1 \)), the instruction counts, the critical path, and the average parallelism (instruction count divided by critical path) for a 10×10 example. In all cases, the run length was constant at 3.7, and the number of arithmetic operations was 4,352.

As was expected, the cost of increasing \( K \) by 1 is on the order of \( 4n^2 \), or 400: the difference in

\(^{52}\)It is possible to do limited loop spreading by compiling specifically for it.
instruction count between two runs whose $K$’s differ by one is 448 (higher-order effects account for the remainder of the instructions, e.g., $4n$ overhead instructions for the $n$ middle loops). However, over the range where $K$ is increasing toward $n$, the change in $K$ has a profound effect on the critical path and the average parallelism. The optimal value for this case occurs with ten concurrent iterations, or $K=11$. Beyond this point, the increasing time spent in overhead instructions for each inner loop instance causes an increase in critical path time. The run length also increases, but only for pathological reasons - the loop initialization code is a tight, unsynchronizing loop dependent upon the value of $K$. As $K$ increases, this loop dominates the computation,
Figure 5-5: Available Parallelism under the Hybrid Model in WaveFront

and the mean run length tends toward the dynamic length of this loop\textsuperscript{53}.

The second set of matrix multiplications shows an interesting effect. In this case, the outer and middle loops were $K$-unfolded, but the inner loops were prohibited from unfolding (i.e., $K=2$). Despite this, the average parallelism is on the same order, and the run length is unchanged. Moreover, the incremental cost of unfolding has been dramatically reduced from 448 to 48. Thus, the total number of instructions is a much weaker function of $K$. Deciding how and when to unfold loops is a difficult problem which is explored by Culler in his dissertation [21].

The critical path and average parallelism values show some interesting discontinuities which are better visualized with the aid of Figure 5-4. For $n$ iterations, where $K-1$ are allowed to proceed concurrently, there will necessarily be $\left\lceil \frac{n}{K-1} \right\rceil$ sequentialized sets of iterations. It is this non-linearity which gives rise to the discontinuities.

Just as in a dynamic dataflow machine, the benefits of loop unfolding can be exploited in the hybrid regime. The costs can be managed at compile and/or load times in that the unfolding mechanism is dynamic and is simply controlled by the invocation constant $K$. Costs are a weak function of $K$, but the effect for nested loops is necessarily multiplicative.

\textsuperscript{53}Culler has pointed out an interesting optimization, not explored in this work, to spawn a separate SQ to perform initialization of the iteration descriptors for each of the $K$ iteration areas. This would result in a nearly trivial increase in instruction count, but would have a very noticeable effect of shortening the critical path time.
5.2.3 WaveFront Revisited

In motivating this architecture, three forms of parallelism were described using the WaveFront example. An idealized parallelism profile was presented for WaveFront and its companion program MultiWave. It was argued that von Neumann machines were inherently incapable of exploiting all three forms, and that hardware changes were required to support the necessary fine-grained synchronization. The hybrid model was developed in response to the challenge of keeping the von Neumann machine's ability to mask latency using expression level parallelism and instruction reordering (a big improvement in locality over a dataflow machine) while simultaneously exploiting the other two kinds of parallelism.

<table>
<thead>
<tr>
<th>Codeblock</th>
<th>Instr</th>
<th>Critical Path</th>
<th>Aborts</th>
<th>% Aborts</th>
<th>Arith</th>
<th>% Arith</th>
<th>Run Length</th>
<th>Average Parallelism</th>
</tr>
</thead>
<tbody>
<tr>
<td>MultiWave, K=2</td>
<td>12,769</td>
<td>5,694</td>
<td>538</td>
<td>4.21</td>
<td>2,787</td>
<td>21.83</td>
<td>5.4</td>
<td>2.2</td>
</tr>
<tr>
<td>MultiWave, K=16</td>
<td>14,729</td>
<td>679</td>
<td>1,063</td>
<td>7.22</td>
<td>2,787</td>
<td>18.92</td>
<td>5.1</td>
<td>21.7</td>
</tr>
<tr>
<td>WaveFront, K=2</td>
<td>5,894</td>
<td>5,030</td>
<td>252</td>
<td>4.45</td>
<td>1,294</td>
<td>21.95</td>
<td>5.6</td>
<td>1.2</td>
</tr>
<tr>
<td>WaveFront, K=16</td>
<td>6,846</td>
<td>534</td>
<td>533</td>
<td>7.79</td>
<td>1,294</td>
<td>18.90</td>
<td>5.1</td>
<td>12.8</td>
</tr>
</tbody>
</table>

Figure 5-5 shows the parallelism profile which results from executing the WaveFront example under the idealized hybrid model. The vertical axis represents the number of concurrently executable SQ's as a function of time (c.f., Figure 2-6, p. 35). Figure 5-6 shows two iterations of the MultiWave example, also under ideal assumptions (c.f., Figure 2-7a, p. 36). As is obvious
from the figures, the hybrid model is capable of exploiting the parallelism inherent in this application by virtue of the fine-grained synchronization mechanisms. Details of these experiments are shown in the table. Full unfolding of outer and inner loops was performed for the $K=16$ cases. The increase of average parallelism as $K$ is scaled to its optimum value is not nearly so dramatic as in the matrix multiplication case simply because the algorithmic parallelism is $O(n)$ vs. $O(n^2)$ for matrix multiplication.

5.2.4 Power of a Hybrid Instruction

Assuming all other things equal, e.g., the opcode set, hybrid instructions are strictly less powerful than TTDA instructions (viz., forking). An interesting question, as alluded to earlier, is whether the full generality of TTDA instructions is used frequently or infrequently. By using the identical program graphs in generating code for both the TTDA and the hybrid machine, it has been possible to study this question in some detail.

<table>
<thead>
<tr>
<th>Codeblock</th>
<th>Hybrid Instr</th>
<th>Critical Path</th>
<th>TTDA Instr</th>
<th>Critical Path</th>
</tr>
</thead>
<tbody>
<tr>
<td>ABS 1</td>
<td>4</td>
<td>4</td>
<td>9</td>
<td>5</td>
</tr>
<tr>
<td>AND $T$ $T$</td>
<td>5</td>
<td>5</td>
<td>9</td>
<td>5</td>
</tr>
<tr>
<td>ARRAY $&lt;0$ 10&gt;</td>
<td>7</td>
<td>8</td>
<td>11</td>
<td>6</td>
</tr>
<tr>
<td>+ 1 2</td>
<td>5</td>
<td>5</td>
<td>9</td>
<td>5</td>
</tr>
<tr>
<td>EXPRESSION 1 2 3</td>
<td>11</td>
<td>8</td>
<td>13</td>
<td>7</td>
</tr>
<tr>
<td>FIB 10</td>
<td>3,265</td>
<td>187</td>
<td>3,708</td>
<td>115</td>
</tr>
<tr>
<td>FOR_LOOP 1000</td>
<td>7,030</td>
<td>7,028</td>
<td>10,023</td>
<td>6,011</td>
</tr>
<tr>
<td>IF_EXPR 1 2</td>
<td>17</td>
<td>11</td>
<td>18</td>
<td>9</td>
</tr>
<tr>
<td>MM 10x10</td>
<td>23,569</td>
<td>21,924</td>
<td>20,118</td>
<td>11,228</td>
</tr>
<tr>
<td>MERGESORT &lt;20..1&gt;</td>
<td>16,053</td>
<td>2,910</td>
<td>17,549</td>
<td>1,280</td>
</tr>
<tr>
<td>ATAN 0.1 1</td>
<td>110</td>
<td>70</td>
<td>96</td>
<td>27</td>
</tr>
<tr>
<td>COS 0.1</td>
<td>43</td>
<td>42</td>
<td>35</td>
<td>24</td>
</tr>
<tr>
<td>LOG 0.1</td>
<td>34</td>
<td>32</td>
<td>30</td>
<td>20</td>
</tr>
<tr>
<td>SIN 0.1</td>
<td>42</td>
<td>41</td>
<td>33</td>
<td>22</td>
</tr>
<tr>
<td>SQRT 0.1</td>
<td>51</td>
<td>49</td>
<td>41</td>
<td>27</td>
</tr>
<tr>
<td>MULTIWAVE 15x15x2</td>
<td>12,769</td>
<td>5,694</td>
<td>9,584</td>
<td>2,701</td>
</tr>
<tr>
<td>WAVEFRONT 15x15</td>
<td>5,894</td>
<td>5,030</td>
<td>4,523</td>
<td>2,477</td>
</tr>
</tbody>
</table>

The Table shows dynamic instruction counts for the benchmark programs as executed on both the hybrid machine and on the TTDA\textsuperscript{54} using the same source program for both\textsuperscript{55,56}. The counts do

\textsuperscript{54} The TTDA compiler used in this study was at level 3.22, and the GITA interpreter was at level 24.24.

\textsuperscript{55} In neither case is the type of simulation model (idealized or not) relevant for instruction counts. Instruction counts do not vary across these models.

\textsuperscript{56} Some care is needed in interpreting TTDA critical path numbers in that the GITA interpreter counts instructions, and instructions are not cycles in the strict sense. The hybrid interpreter also counts instruction, but the assumption of instructions being cycles is more reasonably made.
not favor either architecture but rather show that, for a variety of program types, instruction counts are comparable to first order. If hybrid instructions are less powerful, how can this be?

One part of the answer lies in the reduced number of overhead operators in the hybrid code resulting from fewer independent threads. In the TTDA, termination detection is done via trees of \texttt{IDENTITY} instructions. The leaves of these trees are the instructions which otherwise produce no tokens, \textit{e.g.}, \texttt{STORE} operations. In the hybrid model, it is only necessary to test for termination of the SQ in which such instructions reside. Hence, \(n\) \texttt{STOREs} in one SQ imply only \textit{one} explicit synchronization operation instead of a binary tree of \(n-1\) \texttt{IDENTITY} instructions.

Another part of the answer is elimination of the need to perform explicit fan-out of \texttt{FETCH}ed values; the associated frame slots can simply be re-read. In the TTDA, however, \texttt{FETCH} operations can have only a single destination instruction. Multiple destinations imply the need for an \texttt{IDENTITY} instruction as the destination for the \texttt{FETCH}.

It is likely that the remainder is attributable to the fact that it does \textit{not} in general take two hybrid instructions to displace a single TTDA instruction. There are many instances of TTDA instructions in typical programs where the full generality and power of the instruction is not being used in the sense that the hybrid partitioning strategy chooses to eliminate it rather than mimic it. In the hybrid model, parallelism is retained in the machine code only when dictated by dynamic arc constraints. According to this view, the remainder of the parallelism in TTDA code and it associated forking is superfluous.

In the next section, the effect of this reduced parallelism in terms of the hybrid machine's ability to tolerate latency is examined.

\section*{5.3 Realistic Model}

In this section, the benchmark programs are used to characterize the realistic model. In particular, critical path time is evaluated as a function of data cache parameters, the number of processors, and communication latency. First, the matrix multiplication example is used to establish an operating point for the data cache. Using this, the remaining benchmarks are run with no cache, with the cache at the operating point, and with an infinite cache to demonstrate the robustness of the operating point. Then, the number of processors is allowed to vary. Finally, latency is introduced.

In the realistic emulator, codeblock invocations are assigned to a specific logical processor. At most one instruction may be executed at any given time on any given processor. Moreover, a one cycle time penalty is charged for each aborted instruction, and extra cycles are accrued for frame
accesses above one per instruction in the absence of cache hits. Thus, an instruction making two frame references where one operand is found in the cache will take unit time, while the same instruction will take two time units when neither operand is found in the cache. Register accesses are considered to be free. The minimum communication latency $L$ is one instruction time. This is charged against all packets formed by MOV, LOAD, and STOR instructions.

I-Structures are handled by an idealized processor which services requests without imposing queue penalties. However, communication latency $L$ also applies to the results returned by LOAD packets. Hence, in the best case, a LOAD will incur $2L$ units of latency in addition to the actual service time charged by the I-Structure processor (a minimum of one additional instruction time).

5.3.1 Cache Operating Point

In the realistic interpreter, each processor has a single data cache. All operand fetches are directed at the cache. Both successful fetches (hits) and unsuccessful fetches (misses) are counted. Hit rate is computed as the ratio of hits to accesses. The cache is organized as $S$ sets, each with $A$ associativity classes, and is referred to as an $S\times A$ cache. The denoted cache line is a single local memory word. The cache performs no prefetching, and ALU results are stored through to the local memory. Hence, cache flushing is never necessary. Mapping of local memory addresses into set addresses is done by simple hashing (exclusive-or folding) of the address.
<table>
<thead>
<tr>
<th>Cache</th>
<th>Critical Path</th>
<th>Hit Rate</th>
<th>Effective Hit</th>
</tr>
</thead>
<tbody>
<tr>
<td>None</td>
<td>5,980</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>Infinite</td>
<td>4,996</td>
<td>63.5</td>
<td>100.0</td>
</tr>
<tr>
<td>1x1</td>
<td>5,475</td>
<td>26.2</td>
<td>41.3</td>
</tr>
<tr>
<td>2x1</td>
<td>5,261</td>
<td>33.4</td>
<td>52.6</td>
</tr>
<tr>
<td>4x1</td>
<td>5,184</td>
<td>41.2</td>
<td>64.9</td>
</tr>
<tr>
<td>8x1</td>
<td>5,105</td>
<td>48.1</td>
<td>75.7</td>
</tr>
<tr>
<td>16x1</td>
<td>5,080</td>
<td>53.4</td>
<td>84.1</td>
</tr>
<tr>
<td>32x1</td>
<td>5,014</td>
<td>58.7</td>
<td>92.4</td>
</tr>
<tr>
<td>64x1</td>
<td>5,005</td>
<td>60.3</td>
<td>95.0</td>
</tr>
<tr>
<td>128x1</td>
<td>5,000</td>
<td>61.6</td>
<td>97.0</td>
</tr>
<tr>
<td>256x1</td>
<td>4,997</td>
<td>62.7</td>
<td>98.7</td>
</tr>
<tr>
<td>1x2</td>
<td>5,474</td>
<td>28.3</td>
<td>44.6</td>
</tr>
<tr>
<td>2x2</td>
<td>5,066</td>
<td>42.7</td>
<td>67.2</td>
</tr>
<tr>
<td>4x2</td>
<td>5,057</td>
<td>51.1</td>
<td>80.5</td>
</tr>
<tr>
<td>8x2</td>
<td>5,022</td>
<td>56.6</td>
<td>89.1</td>
</tr>
<tr>
<td>16x2</td>
<td>5,007</td>
<td>60.1</td>
<td>94.6</td>
</tr>
<tr>
<td>32x2</td>
<td>4,998</td>
<td>61.9</td>
<td>97.5</td>
</tr>
<tr>
<td>64x2</td>
<td>4,996</td>
<td>62.5</td>
<td>98.4</td>
</tr>
<tr>
<td>128x2</td>
<td>4,995</td>
<td>63.0</td>
<td>99.2</td>
</tr>
<tr>
<td>1x4</td>
<td>5,061</td>
<td>43.5</td>
<td>68.5</td>
</tr>
<tr>
<td>2x4</td>
<td>5,046</td>
<td>53.7</td>
<td>84.6</td>
</tr>
<tr>
<td>4x4</td>
<td>5,013</td>
<td>57.9</td>
<td>91.2</td>
</tr>
<tr>
<td>8x4</td>
<td>5,000</td>
<td>61.6</td>
<td>97.0</td>
</tr>
<tr>
<td>16x4</td>
<td>4,998</td>
<td>62.1</td>
<td>97.8</td>
</tr>
<tr>
<td>32x4</td>
<td>4,996</td>
<td>63.2</td>
<td>99.5</td>
</tr>
<tr>
<td>64x4</td>
<td>4,996</td>
<td>63.4</td>
<td>99.8</td>
</tr>
<tr>
<td>1x8</td>
<td>5,034</td>
<td>56.5</td>
<td>89.0</td>
</tr>
<tr>
<td>2x8</td>
<td>5,005</td>
<td>58.6</td>
<td>92.3</td>
</tr>
<tr>
<td>4x8</td>
<td>4,999</td>
<td>61.9</td>
<td>97.5</td>
</tr>
<tr>
<td>8x8</td>
<td>4,999</td>
<td>62.1</td>
<td>97.8</td>
</tr>
<tr>
<td>16x8</td>
<td>4,996</td>
<td>63.4</td>
<td>99.8</td>
</tr>
<tr>
<td>32x8</td>
<td>4,996</td>
<td>63.4</td>
<td>99.8</td>
</tr>
</tbody>
</table>

The Table shows the effects of various cache organizations on the critical path time for a 5x5 matrix multiplication example, using a single processor, LIFO queuing, and \( K=2 \). For this example, an infinite cache results in a hit rate of 63.5% and a critical path time of 4,996\(^{57}\). The idealized hit rate of less than 100% is understandable because all references to the cache are counted, not just those from successful instructions. Readers of unwritten slots will, by definition, cause cache misses no matter how big the cache is. Hence, it is useful to factor out this program-specific behavior by calculating an effective cache hit rate as the ratio of actual hit rate to ideal hit rate. This is shown in the table.

Run length was uniformly 3.7 in these experiments.

\(^{57}\)The difference between this value and the raw instruction count is attributable to nonzero latency which was not masked by parallel activity and to instruction aborts.
It is clear, at least with this simple example, that a fairly small, simple cache has a profound effect on eliminating the multiple frame access penalty. In the next section, the robustness of the 64×4 cache is tested with the other benchmark programs. This organization and size will be used for the remainder of the realistic mode experiments as the cache operating point.

5.3.2 Cache Robustness

<table>
<thead>
<tr>
<th>Codeblock</th>
<th>No Cache</th>
<th>Infinite Cache</th>
<th>Hit Rate</th>
<th>64x4 Cache</th>
<th>Hit Rate</th>
<th>Effective Hit</th>
</tr>
</thead>
<tbody>
<tr>
<td>ABS 1</td>
<td>7</td>
<td>6</td>
<td>12.5</td>
<td>6</td>
<td>12.5</td>
<td>100.0</td>
</tr>
<tr>
<td>AND ST ST</td>
<td>9</td>
<td>8</td>
<td>12.5</td>
<td>8</td>
<td>12.5</td>
<td>100.0</td>
</tr>
<tr>
<td>ARRAY $&lt;0 10&gt;$</td>
<td>15</td>
<td>14</td>
<td>8.3</td>
<td>14</td>
<td>8.3</td>
<td>100.0</td>
</tr>
<tr>
<td>+ 1 2</td>
<td>9</td>
<td>8</td>
<td>12.5</td>
<td>8</td>
<td>12.5</td>
<td>100.0</td>
</tr>
<tr>
<td>EXPRESSION 1 2 3</td>
<td>18</td>
<td>15</td>
<td>31.2</td>
<td>15</td>
<td>31.2</td>
<td>100.0</td>
</tr>
<tr>
<td>FIB 10</td>
<td>4,501</td>
<td>4,059</td>
<td>55.0</td>
<td>4,059</td>
<td>54.4</td>
<td>98.9</td>
</tr>
<tr>
<td>FOR_LOOP 1000</td>
<td>9,037</td>
<td>7,033</td>
<td>99.9</td>
<td>7,033</td>
<td>99.9</td>
<td>100.0</td>
</tr>
<tr>
<td>IF_EXPR 1 2</td>
<td>25</td>
<td>21</td>
<td>58.3</td>
<td>21</td>
<td>58.3</td>
<td>100.0</td>
</tr>
<tr>
<td>MERGESORT &lt;20..1&gt;</td>
<td>23,252</td>
<td>20,858</td>
<td>48.6</td>
<td>20,956</td>
<td>45.6</td>
<td>93.8</td>
</tr>
<tr>
<td>ATAN 0.1 1</td>
<td>157</td>
<td>118</td>
<td>90.4</td>
<td>118</td>
<td>90.4</td>
<td>100.0</td>
</tr>
<tr>
<td>COS 0.1</td>
<td>61</td>
<td>45</td>
<td>90.9</td>
<td>45</td>
<td>90.9</td>
<td>100.0</td>
</tr>
<tr>
<td>LOG 0.1</td>
<td>52</td>
<td>36</td>
<td>80.8</td>
<td>36</td>
<td>80.8</td>
<td>100.0</td>
</tr>
<tr>
<td>SIN 0.1</td>
<td>59</td>
<td>44</td>
<td>90.3</td>
<td>44</td>
<td>90.3</td>
<td>100.0</td>
</tr>
<tr>
<td>SQRT 0.1</td>
<td>67</td>
<td>53</td>
<td>85.0</td>
<td>53</td>
<td>85.0</td>
<td>100.0</td>
</tr>
<tr>
<td>MULTIWAVE 15x15x2</td>
<td>17,739</td>
<td>13,861</td>
<td>70.3</td>
<td>13,870</td>
<td>70.0</td>
<td>99.6</td>
</tr>
<tr>
<td>WAVEFRONT 15x15</td>
<td>8,114</td>
<td>6,417</td>
<td>71.6</td>
<td>6,418</td>
<td>71.5</td>
<td>99.9</td>
</tr>
<tr>
<td>MULTIWAVE, K=16</td>
<td>20,137</td>
<td>15,773</td>
<td>70.3</td>
<td>15,784</td>
<td>69.1</td>
<td>98.3</td>
</tr>
<tr>
<td>WAVEFRONT, K=16</td>
<td>9,305</td>
<td>7,355</td>
<td>71.4</td>
<td>7,359</td>
<td>70.4</td>
<td>98.6</td>
</tr>
</tbody>
</table>

The table shows the performance of the other benchmark programs given the assumptions of no cache, an infinite cache, and a 64×4 cache. For the infinite and 64×4 cases, the actual hit rate is shown. The effective hit rate for the 64×4 cache is also calculated. In all but the last two runs, K=2. For most of the K=2 cases except Mergesort, the ratio of local memory space used to the 256 word capacity of the 64×4 cache was 1:1 or less. For the remaining three runs, the ratios were 7:1 (Mergesort), 18:1 (MultiWave, K=16), and 15:1 (WaveFront, K=16). While higher local memory to cache ratios would make the case more convincingly, the hit rates indicate that a 64×4 cache is quite effective in a variety of cases.

5.3.3 Parallelism
Figure 5-7: Speedup for MM on the Realistic Model

<table>
<thead>
<tr>
<th>Processors</th>
<th>Critical Path</th>
<th>Average Parallelism</th>
<th>Hit Rate</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>33,457</td>
<td>0.8</td>
<td>58.5</td>
</tr>
<tr>
<td>2</td>
<td>17,137</td>
<td>1.6</td>
<td>38.5</td>
</tr>
<tr>
<td>4</td>
<td>9,069</td>
<td>3.0</td>
<td>57.7</td>
</tr>
<tr>
<td>8</td>
<td>4,751</td>
<td>5.8</td>
<td>55.8</td>
</tr>
<tr>
<td>10</td>
<td>3,919</td>
<td>7.0</td>
<td>55.9</td>
</tr>
<tr>
<td>16</td>
<td>2,616</td>
<td>10.6</td>
<td>56.0</td>
</tr>
<tr>
<td>32</td>
<td>1,734</td>
<td>15.9</td>
<td>58.7</td>
</tr>
</tbody>
</table>

Given a cache size of 64x4 on a single processor and LIFO queue discipline, the question of how well the realistic machine can exploit parallelism remains. This section presents the results of running a 10x10 matrix multiplication with the number of processors as the independent variable. The example is necessarily small due to the performance limitations of the emulator. It is significant only to note that parallelism can indeed be exploited, even on a small example.

The table shows critical path, average parallelism\(^{58}\), and aggregate cache hit rate. Figure 5-7 depicts the speedup (ratio of single-processor execution time to the execution time on n processors). In all cases, the number of aborted instructions was less than 3,648 (13.2% of successful instructions), and run length was consistently 3.7.

Recall that the optimal hit rate for the matrix multiplication benchmark on a single processor was

\(^{58}\)A low value here reflects low parallelism, a significant number of aborted instructions, or both.
found to be 63.5% by a previous experiment. Using this as a basis, the effective hit rates in this experiment are approximately 90%.

5.3.4 Tolerance of Latency

<table>
<thead>
<tr>
<th>Processors</th>
<th>Critical Path</th>
<th>Average Parallelism</th>
<th>Hit Rate</th>
</tr>
</thead>
<tbody>
<tr>
<td>32, L=10</td>
<td>1,899</td>
<td>14.5</td>
<td>59.5</td>
</tr>
</tbody>
</table>

No amount of "optimization" by packing instructions into larger chunks is worth much if it negates the architecture's ability to synchronize efficiently or to tolerate latency. It is reasonably clear that the hybrid architecture provides the necessary synchronization support at a basic level for the purposes of program decomposition. But what about the hybrid machine's tolerance of long latency operations?

The effect of physical partitioning, or distributing a program can be estimated by assigning a higher than unit latency cost to each inter-codeblock communication. Specifically, each codeblock-to-codeblock communication incurs communication latency $L$ (ignoring locality), STOR instructions incur latency cost $L$, and LOAD instructions incur latency cost $2L$.59

---

59Recall that the latency is attributable to the time between instructions and not time within an instruction.
Figure 5-9: 10x10 MM with Communication Latency = 10

Figure 5-8 shows the effect of unit latency on the 10x10 example, with $K=11$. In Figure 5-9, the inter-processor latency has been increased to 10 pipe steps, yet the increase in critical path time is only 9.52%. Two forms of parallelism have made this masking possible: first, multiple continuations are available on any one processor due to $K$-unfolding of loops. Second, each continuation contributes an average of half a run length's number of instructions to the pool of executable instructions at any given time.

5.4 Summary

This chapter has demonstrated the benefits of the hybrid architecture which argue for its superiority over von Neumann machines as the basis for a scalable, general-purpose parallel computer:

- **Synchronization**: Efficient synchronization mechanisms allow the exploitation of the same kinds of parallelism as on a dataflow machine, yet implicit synchronization is possible within a single thread. It has been shown that the architecture is capable of iteration unfolding and inter-procedural parallelism wherein the synchronization is not at all simple and straightforward, but rather requires a fine-grained approach.

- **Latency Tolerance**: The same synchronization mechanisms allow parallelism to mask latency.

The underlying theme of the hybrid architecture is that the cost of exploiting parallelism should be manifest and should not be "masked" by the architecture as it is in the dataflow regime. This belief manifests itself in explicit fork instructions and in loop unfolding costs. Given that this
architecture provides considerable leverage for reducing the critical path time of the body of a given inner loop, some re-thinking of compilation strategies along the lines of unfolding outer loops and mapping inner loops to a small number of properly-ordered SQ's is indicated.

It has been shown that, although the hybrid instruction set is less powerful than the TTDA instruction set, instruction counts are comparable, leading to the conclusion that the full synchronization generality of the TTDA can indeed be compiled into some amount of program-counter based synchronization.

Considerable work remains in evaluating and characterizing this architecture. While preliminary studies have demonstrated that the hybrid architecture does indeed have better locality than a TTDA-like machine and that even very small caches can be used effectively to relieve the local memory bottleneck, additional study is required to make engineering-level decisions about pipeline balance, memory sizes, and so on.
Chapter Six
Conclusion

This section reviews the work done to date in unifying the dataflow and von Neumann views of architecture. The first section summarizes the conclusions of the present work. The second section presents directions for future work. The last section analyzes related efforts by other researchers in light of the present work.

6.1 Summary of the Present Work

As stated in the Introduction, the overall goal of this study is to discover the critical hardware structures which must be present in any scalable, general-purpose parallel processor to effectively tolerate latency and synchronization costs. The main conclusion is that any such machine must execute a parallel machine language, having the following three characteristics:

- The execution time for any given instruction must be independent of latency. Traditional latency-sensitive operations, e.g., loads from memory, must be rephrased as split transactions which separately initiate an operation and later explicitly synchronize on the availability of the result.

- Each explicit synchronization event must be named. This implies efficient means for creating and re-using names as well as an efficient mechanism for enforcing synchronizing behavior based on the names. Names must be drawn from a large name space, and it must be possible to manipulate them as first-class hardware data types.

- Means for expressing both implicit and explicit synchronization must be provided. Implicit, i.e., program counter based, synchronization provides the means for passing state between instructions within an unbroken thread. Explicit synchronization is necessary at the programming level in the exploitation of parallelism and at the machine level in the masking of latency.

In that neither von Neumann nor dataflow machines exhibit all three of these characteristics, a new architecture has been synthesized and analyzed. It has been demonstrated through emulation experiments and analysis of the model that the new architecture, based on the principles of parallel machine language, has the ability to exploit the same classes of parallelism as a dataflow machine. Consequently, the hybrid architecture can control communication latency cost through the exploitation of parallelism. Moreover, the cost of synchronization is low enough to allow its free an unencumbered use in decomposing programs for parallel execution.
From the standpoint of pure von Neumann architectures, the hybrid is evolutionary in the addition of a synchronizing local memory, split transaction memory operations, and a large synchronization name space. Synchronizing local memories and register sets are not new. Most noteworthy of the previous machines in this regard is the HEP [41, 42]. As described below, however, the scheme proposed in this thesis is more general than that of the HEP. Similarly, split transactions in and of themselves are not new, but the hybrid architecture shows the importance of inexpensive context switching as the primary means for making the most of split transactions.

The biggest departure from the traditional von Neumann architectural view is the introduction of large name spaces for synchronization purposes in the hybrid. In particular, the number of low-level synchronization names is limited only by the size of local memory. Further, the number of processes is limited only by the number of meaningful continuations. In contrast, the HEP architecture allows only 64 processes per processor to be named simultaneously. From a hardware point of view, 64 processes is a sizable number. From the compiler's point of view, however, the number is far too small and implies that processes are a precious resource to be carefully managed. In the hybrid, this artificial restriction is lifted, resulting in more generality. It can be argued that any fixed number of hardware processes could be virtualized by an added layer of interpretation, but the cost of such schemes in terms of lost time makes them unattractive. Large synchronization name spaces add the flavor of dataflow machines to von Neumann machines.

From the standpoint of pure dataflow architectures, the hybrid is evolutionary in that it adds the means for the compiler to exercise some explicit control over the pipeline. Because a thread holds the pipeline until it executes a potentially suspensive instruction, the entire machine state can be brought to bear on the problem of efficiently communicating information between instructions. This class of compiler-directed pipeline control is absent in both the TTDA and in Monsoon [47]. The hybrid further takes the stance that synchronization should be explicit as should forking of parallel activity. This simplification of the instruction set demonstrably does not drive the instruction count up in many cases because much of the forking and its attendant synchronization is superfluous. Even so, in the limiting case, the hybrid machine can still emulate instruction level dataflow with an instruction count expansion factor of no more than two. This leads to the observation that explicit synchronization instructions, used when necessary, may in some sense be cheaper than paying the full cost of synchronization at each instruction. This is, perhaps, the equivalent of the RISC argument applied to multiprocessing.

In [8], the question of the possibility of "modifying" a von Neumann processor to make it a suitable building block for a parallel machine was raised. It was believed that the salient characteristics of a dataflow machine which made it a suitable building block were split-phase memory operations and the ability to context switch inexpensively. Given the addition of mechanisms like
these, there was some lingering doubt as to what kind of synchronization efficiencies could be achieved and how much of the von Neumann architecture would be left. As presented in this thesis, engineering arguments regarding efficient implementation of PML's and the persistence of program counter based sequencing in the hybrid model have dispelled much of the doubt.

As yet unanswered is the question of the effectiveness of the hybrid architecture, or architectures like it, for other parallel programming models (e.g., Halstead's MultiLisp [32]); this is explored in more detail in the next section. Of considerable practical interest is the possibility of targeting FORTRAN compilers to the hybrid paradigm.

6.2 Future Work

Opportunities for continuation of the present work abound, and are only outlined here.

- **Model:** This work investigates an architecture suitable for exploiting parallelism in single applications where all processors cooperate. Higher-level systems issues such as virtualization of the processor space and memory address space have not been considered for supporting multiprogramming and higher levels of tasking. It is believed that the right approach is to generalize the SQ mechanism upward to subsume higher-level tasks, but it is not clear how synchronization should be handled in the presence of dynamic address translation and demand paged memory.

- **Code Generation:** A number of schemes for improving dynamic instruction counts (e.g., RSTN elimination in LOOPS when all sinks are in a single SQ, TSTN elimination in SIGNAL-TREES for multiple sources from a single SQ, etc.) have been outlined but not implemented. It is reasonable that this work should be carried out by a peephole optimizer which operates on the partitioned graph. Such an idea has been considered but not developed in the present work. Also, techniques for register allocation need to be explored in the context of multiple, asynchronous readers. Optimizations such as the System/370 style BXLE instruction for decrementing, testing, and branching on an iteration variable are implementable in a straightforward way and need to be explored. Improvements to the LOOP implementation, e.g., the overlapping of iteration area initialization with useful computation, have been outlined but not tested.

- **Machine Structure:** A number of optimizations remain unexplored, e.g., reference-count slot resetting based on bounded fanout to make frames entirely self-cleaning, hardware support for tagged data (e.g., trapping, autocoercion, etc.). The local memory presence bits should be generalized along the lines of Monsoon [47] such that each operand fetch or store can specify one of a fixed number of state-transition functions. Such a mechanism can perform the existing functions, e.g., synchronizing and nonsynchronizing reads, nonstickness, etc., as well as more sophisticated functions (e.g., subsuming the flag bits of the iteration descriptor). Various engineering issues remain, especially in the area of implementing fast manager-call instructions (e.g., MKIS, GETC).
6.3 Related Work

This section explores related research efforts over the last 10 years or so. The common threads that bind these projects together are an understanding, at some level, of the two fundamental issues of latency and synchronization, and the beliefs that the von Neumann model is not sufficient, while the dataflow model is not necessary.

6.3.1 The Denelcor HEP

It is truly remarkable that the hybrid architectures under investigation today, including the present work, can trace so much of their low-level synchronization structure to Burton Smith's HEP architecture [41, 42]. The basic structure of the HEP processor is shown in Figure 6-1. The processor's data path is built as an eight step pipeline. In parallel with the data path is a control loop which circulates process status words (PSW's) of the processes whose threads are to be interleaved for execution. The delay around the control loop varies with the queue size, but is never shorter than eight pipe steps. This minimum value is intentional to allow the PSW at the head of the queue to initiate an instruction but not return again to the head of the queue until the instruction has completed. If at least eight PSW's, representing eight processes, can be kept in the queue, the processor's pipeline will remain full. This scheme is much like traditional pipelining of instructions, but with an important difference. The inter-instruction dependencies are likely to be weaker here because adjacent instructions in the pipe are always from different processes.

There are 2048 registers in each processor; each process has an index offset into the register array. Inter-process, i.e., inter-thread, communication is possible via these registers by overlapping register allocations. The HEP provides FULL/EMPTY/RESERVED bits on each register and FULL/EMPTY bits on each word in the data memory. An instruction encountering EMPTY or RESERVED registers behaves like a NOP instruction; the program counter of the process, i.e., PSW, which initiated the instruction is not incremented. The process effectively busy-waits but without blocking the processor. When a process issues a LOAD or STORE instruction, it is removed from the control loop and is queued separately in the Scheduler Function Unit (SFU) which also issues the memory request. Requests which are not satisfied because of improper FULL/EMPTY status result in recirculation of the PSW within the SFU's loop and also in reissuance of the request. The SFU matches up memory responses with queued PSW's, updates registers as necessary and reinserts the PSW's in the control loop.

Thus, the HEP is capable up to a point of using parallelism in programs to hide memory and communication latency. At the same time it provides efficient, low-level synchronization mechanisms in the form of presence-bits in registers and main memory. However, the HEP
The approach does not go far enough because there is a limit of one outstanding memory request per process, and the cost of synchronization through shared registers can be high because of the loss of processor time due to busy-waiting. A serious impediment to software development on the HEP was the limit of 64 PSW's in each processor. Though only 8 PSW's may be required to keep the process pipeline full, a much larger number is needed to name all concurrent tasks of a program.

In contrast, the present work recognizes the need for a synchronization name space whose size should be thought of in terms of the entire address space of a conventional processor and not simply in terms of an unusually large register set. Further, while the HEP was forced by its pipeline architecture to interleave at least eight execution contexts in order to keep the pipeline full, the present effort recognizes the deleterious effect this has on the "working set" size at the level of, say, an operand cache. It is believed that in order to support a spectrum of programming models from standard FORTRAN through the most highly parallelizable functional style, the ability to efficiently execute long sequential threads cannot be traded away. Moreover, unless the processor truly has nothing better to do, low-level busy waiting (e.g., in the main pipeline and in the SFU pipeline) is wasteful of cycles. Nevertheless, an important place in the history of computer architecture is rightly reserved for the HEP as the first machine which made a genuine attempt to address the two fundamental issues.
6.3.2 The MASA Architecture

Halstead at MIT and Fujita from NEC Corporation have jointly developed an architecture called MASA which is multithreaded, and intended specifically for parallel symbolic computation [30, 33]. MASA is a tagged architecture in order to support generic operations (with a fully general software trap handling mechanism), parallel, generation-based, incremental garbage collection, and efficient computation with futures [32]. From the machine’s perspective, a future is a value cell which may either be unresolved or resolved: initially, a future has no value and hence is unresolved. Subsequent computation can cause the future to mutate (resolve) into a cell which has a value which it retains for the remainder of its lifetime. It is this latter use of tags and associated mechanisms which is particularly novel. MASA provides a number of machine instructions which are nonstrict (e.g., copying, which if given a future as an operand only manipulate the reference to the value cell). These instructions are insensitive to whether the future is resolved or not. For those instructions which are strict in any argument which is a future, execution must either fetch the cell’s value if it is resolved, or cause a suspension of the associated task if it is not. The trick, of course, is to perform this so efficiently that the cost of using a future is negligible.

MASA provides explicit hardware resources (called task frames) to hold the state of a small number of tasks. This state consists of a small set of general purpose registers along with a program counter, and the identifiers of the parent and one child task frame. Memory words have a synchronizing bit (full/empty), but registers are nonsynchronizing. At the beginning of every instruction cycle, the processor may choose among the next instructions of all ready tasks, however, dispatching sequential instructions from a given task incurs a delay equal to the pipeline depth (in the case of the machine currently under study, this is four cycles). Instructions enable a number of trap conditions, which cause dedicated hardware to check tag fields, arithmetic overflow, a synchronization bit, etc., and if an enabled trap condition is met, to NOP the instruction, suspend the task, and invoke a software trap handler.

As compared to the hybrid architecture, the HEP-like instruction dispatching scheme of MASA relies on parallelism in excess of the pipe depth at all times in order to avoid dispatching bubbles. Halstead and Fujita recognize the importance of efficient operation in scalar mode, and have outlined strategies which will improve on this dispatching restriction. The practicality of techniques to further reduce this dispatch delay depend on the statistics of trap frequency. With additional study, this will become clearer.

MASA can only name and efficiently switch between a very small number of tasks. The frame saver does permit tasks to be rolled out and back in; however, the cost of doing so must be considered, and higher level synchronization must be imposed to decide when / what to roll.
the hybrid architecture, tasks (continuations) are word-sized objects which can be freely created and destroyed. Their number is not tied directly to a small physical resource\textsuperscript{60}. Again, only execution statistics can demonstrate the significance, or insignificance, of this limit.

At first blush, it may appear that the restriction of one child per context imposes a rather rigid restriction; however, it is possible to spawn, then detach, any number of children, relying on full/empty bits or futures for synchronization. In the hybrid model, a given codeblock can dynamically invoke any number of children, with all synchronization occurring through the various frames. This is more strongly similar to the action of MASA's notion of process creation, which requires allocation of futures for the passing of results. Tasks in MASA are clearly more than hybrid continuations in that they have private state, but they are less than codeblock invocations in that their private state is restricted to a small number of registers. There is, therefore, a not-too-surprising tradeoff between the cost of allocating lots of futures for the privilege of treating all child invocations as processes and the potential benefit of additional parallelism. One would clearly view the problem differently starting with an annotated MultiLisp program vs. starting with a dataflow program graph.

MASA provides the means for dynamic redistribution of work: the state of a task is easily transported because it is relatively small. The hybrid machine must make decisions about workload distribution at codeblock invocation time. It is not practical to consider picking up a hybrid codeblock invocation and moving it because of its size\textsuperscript{61}. Moreover, all continuations for a single codeblock invocation must reside on a single processor.

6.3.3 The UCI Process-Oriented Model Project

Bic at the University of California, Irvine, has been investigating methods of exploiting the apparent inefficiencies in dataflow systems by systematically eliminating dynamic synchronization operations [12]. His technique is based on translating graphs into sets of linear sequences of instructions. To the extent that the sequences contain more than a single instruction, dynamic synchronization is eliminated. His partitioning method is depth-first: Repeatedly apply this algorithm until the graph is empty:

- Initialize a new (empty) partition.
- Select and remove an instruction from the graph, called \textit{iast}, which has the property that it receives no input from any instruction in the codeblock.

\textsuperscript{60}This name space limitation is orthogonal to the large producer/consumer synchronization name space (futures as words in a large memory) which is strongly similar to the I-Structure storage name space used in the hybrid architecture.

\textsuperscript{61}Inter-codeblock naming is not a problem, however, because all inter-codeblock interactions happen with fully qualified names via the \texttt{MOVIR} instruction.
• Repeat while \( inst \) has an output used by some other instruction in the codeblock:
  • Add \( inst \) to the partition.
  • Remove \( inst \) from the graph.
  • Select one of \( inst \)'s outputs. \( Inst \) now becomes the instruction denoted by this output.
  • Add \( inst \) to the partition.
  • Remove \( inst \) from the graph.

The execution paradigm is as follows: Program memory contains a suitable representation of codeblocks as collections of partitions. Invocations are named according to U-Interpreter rules [5] with the exception that the statement (instruction) number \( s \) is divided into \( s1 \), naming a partition, and \( s2 \), naming an instruction within a partition. Rather than in the dataflow model where triggering is based on exact matching of activity names, names are matched associatively ignoring the \( s2 \) field. This is another way of saying that a partition is the unit of schedulability.

An associative waiting/matching store implements this mechanism, but much more is expected of it than simply associative matching. Each entry uniquely denotes an instance of a partition, contains a missing token count, and maintains a pointer to a list of tokens which have arrived for the instance. As tokens arrive for a given instance and which specify \( s2=0 \) (i.e., they are headed for the first instruction), the count is decremented. Until it reaches zero, tokens are accumulated in the list. When it reaches zero, there are sufficient tokens to execute at least one instruction in the partition. At this time, the actual instantiation of the partition takes place which involves copying a blank template of the code from program memory to execution memory. In the process, tokens in the list are merged with the code - values are stored into the appropriate operand slots. A process control block is created and entered into an array of such control blocks in the processor.

This model is interesting but may exhibit some implementation difficulties. From experience with dataflow program graphs, one would expect the partitioning to result in a large number of very small partitions. Moreover, experience with the TTDA has shown that, as a program's invocation tree is explored eagerly, the partially-computed state left behind as the wave of control proceeds toward the leaves is enormous. These two fact lead to the belief that the size of the PCB "register" array may have to be of a size which is comparable to execution memory in order to avoid frequent deadlock. Moreover, copy operations (with merging) are implied for each and every invocation. Assuming execution memory is not multiported, this will represent a tremendous number of cycles in which no useful computing can take place. In contrast, the hybrid model does not copy code and, to the extent that code can be generated to leave frames clean, invocation is extremely inexpensive.
It is not at all clear what implications the depth-first partitioning method will have on the operand working set size and how this will compare to breadth-first techniques such as the method of dependence sets. The author is most interested in seeing the analytic and/or experimental results as they are produced. It is clear, however, that depth-first partitioning will rely heavily on pipeline bypassing since, by definition, instruction \( n \) depends on the output of instruction \( n-1 \).

6.3.4 The IBM/ETH Project

Buehrer at ETH Zurich and Ekanadham at IBM Yorktown have developed a model for a hybrid machine which is remarkably similar to the present work. Details have been published elsewhere [15, 16, 27] and are only summarized here.

The authors assume a shared memory load/store multiprocessor of conventional origins augmented with features as follows:

- **Local Memory with Presence Bits**: Each processor has a memory to which it alone has access, and that each slot in said memory has state bits indicating full, empty, or awaited.

- **Send/Receive Instructions**: The instruction set supports a notion of one processor *sending* an instruction to either another processor or to a global memory unit. Received message/instructions are executed asynchronously. LOAD messages are an example - an address from which to load, and a tag are sent from the initiating processor to the appropriate destination.

- **Explicitly Split Read Transactions**: The IREAD instruction, given a LOCAL-ADDR and a GLOBAL-ADDR, resets the presence bit at LOCAL-ADDR and builds a SEND which will read GLOBAL-ADDR, return it to LOCAL-ADDR, and awaken any processes waiting on it.

- **Tag-to-Process Mapper**: Rather than having local processes busy-wait once a long-latency operation has been started, process state can be evacuated from the processor, and an identifier \(<\text{LOCAL-ADDR}, \text{Process}>\) can wait in an associative memory. The completion of the long-latency operation will include searching the memory for identifiers with matching LOCAL-ADDRs. The processes so denoted will be extracted and re-enabled for execution.

Based on these primitives, it is shown that I-Structure storage can be synthesized and, using I-Structures, producer-consumer parallelism can be exploited.

Their proposal for partitioning a dataflow graph involves coloring all primary input nodes in the graph with a single color, and each local-memory synchronizing read instruction (the target of a dynamic arc) with a separate color. For the remaining nodes, color is inherited as follows:

- If all of its immediate predecessors of color \( c \), the node inherits color \( c \).
- Otherwise, the node is assigned a totally new color.
Nodes with the same color form a sequential segment. In execution, all of these segments share access to the execution state of the codeblock. It is a simple matter to prove that the method of dependence sets will always produce the same number or fewer SQ's than Buehrer and Ekanadham (B+E) will; consider the common case of two instructions which each depend on the same set of dynamic arcs. The method of dependence sets will create a single SQ containing these instructions while B+E will create two, each containing a single instruction. This will tend to drive down the mean run length when it is clearly desirable to drive it up.

In the hybrid model, reawakening of tasks is expedited by storing the continuation of the suspended SQ into the empty frame slot. In the B+E model, associative matching is proposed with the attendant reliance on the size and cost of such a memory. The have recognized, however, the possibility of storing process identifiers directly into empty local slots when it can be guaranteed that there will never be more than a single reader.

There are other, less significant differences in the approaches. In B+E, a LOAD turns into two instructions, one to initiate and one to synchronize, while in the hybrid paradigm, the synchronization is always folded forward into the instruction which will use the value. In B+E, registers may be considered valid across suspensions, necessitating a means to save and restore them. In the hybrid approach, the maintaining of state in registers across potential suspensions is forbidden so as to eliminate the need for state saving. The issue here is much deeper than whether a compiler can be organized to do this - it is clear that it can. The issue is one of performance. The present work makes the statement that it is better to invest in operand cache technology than in register save/restore technology. It has been demonstrated through the experiments that this can be done, but it places a premium on reducing the working set size at the operand level.

### 6.4 Closing Remarks

It is heartening to see the harmony in all of the above efforts. The author fully expects that somewhere among all of these projects is the key to practical scalable, general-purpose parallel computing. All of these new efforts owe much to the language-based studies of the dataflow model pioneered by Arvind and Dennis over the last 20 years. But, just as importantly, these efforts seek to reconcile the apparent benefits with the tremendous base of knowledge surrounding the von Neumann model, viz., instruction set design, compilation, and optimization.
Appendix A

Emulator

An emulator for the proposed architecture was designed and implemented after the model of GITA and 1D-WORLD [46], although different in significant ways. While GITA was designed as a graph interpreter implementing dataflow instruction sequencing, the new emulator was designed as a sequential instruction stream interpreter. This permitted

- exploiting the inherent sequentiality of the underlying machine, yielding a significant improvement in emulation speed, and

- expressing the emulation as an extension of the underlying machine. The emulation, therefore, served as a touchstone by which to validate the assumptions of minimal change to von Neumann architecture.

A.1 Data Structures

The key emulator data structure is the continuation: a continuation is an object which denotes a frame descriptor, an instruction number, an invocation context, and a state. Interpreter continuations closely model architectural continuations. The other hardware types are also implemented as LISP structures with the exception of INTs and FLOATs which are implemented as LISP FIXNUMs and FLONUMs.

A.2 Organization of the Emulator

The emulation is controlled by three top-level functions:

- The MOVR Processor: Performs the remote store-in of values to frame slots for the MOVR instruction. Emulates the behavior of the "NetResp" port to the local memory.

- The I-Structure Processor: Handles all requests to fetch from or store to elements in the global I-Structure storage. Performs I-structure statistics gathering.

- The Continuation Processor: Handles sequential execution of instructions within an SQ invocation including suspension. Performs top-level instrumentation and timekeeping.

Of these, the CONTINUATION processor is the most significant. In order to describe its operation, a digression into the representation of codeblocks and machine instructions is necessary.

Each machine opcode logically represents a set of runtime behaviors. While the abstract behavior
of, say, an ADD op is obvious, the concrete behavior of any given ADD, parameterized by the addressing modes of the operands, is potentially very different from other ADDs. Each operand fetch, for instance, can be one of

- A register fetch
- A nonsuspensive frame slot fetch
- A suspensive frame slot fetch
- An immediate constant

Therefore, the behavior of each opcode is described abstractly by a LISP macro, using subordinate macros which encapsulate the mechanisms of operand access, cache reference, timekeeping, and so on. Constructing an executable instance of an instruction involves specifying a set of parameters (e.g., the addressing modes for each operand), called the instruction instance's signature, then instantiating, expanding, and compiling the corresponding macro as a LISP function. While complex, this approach has the advantage of avoiding a significant amount of function-calling overhead. In fact, the mean number of function calls per hybrid instruction emulated is, by instrumentation, on the order of 1.5.

As a codeblock is loaded into the emulator environment, functions are compiled for each unique signature. Signatures and their corresponding compiled code are memoized. Compiled instruction instances are shared when signatures match. This makes codeblock loading rather slow at first, but as the set of frequently-reused instruction instances is built up, loading speed increases substantially.

As compared to the purely interpretive method of GITA, the hybrid emulator has realized a speedup of a factor of three when running comparable experiments with comparable statistics-gathering. This difference is primarily attributable to the savings in function-calling overhead. Selective deleting of statistics when generating the compiled instructions has resulted in speed improvements which range from a factor of 15 to a factor of 30 faster than GITA.

A.3 Statistics Gathering

As in GITA, the emulator provides tools for collecting various statistics, both for the idealized model and for the realistic model, including

- Functions of emulated time: Based on the model (realistic or idealized), sets of rules govern the advancement of emulated time. In the idealized model, each instruction executes in unit time, transit latencies are zero, and aborted instructions (those which suspend) consume zero time. An unbounded number of instructions may execute in a given time step. Time advances in the sense that the satisfaction of all synchronization constraints for a given instruction (both static and dynamic) at the
end of cycle $t$ will cause the instruction to execute at cycle $t+1$. In the realistic model, however, the number of processors is fixed, codeblock invocations are bound to processors, transit latencies are nonzero, and aborted instructions consume time. In either model, successful completion of any event will be recorded at the time it occurs. Such events include

- ALU utilization (number of instructions executed at a given time).
- I-Structure Storage Utilization (numbers of fetches, stores, and allocations as a function of time).
- Local Memory Utilization (number of allocations and deallocations, plus the running sum of the excess of allocations over deallocations as a function of time).
- Cache Utilization in realistic mode (numbers of hits and misses as function of time).

- **Histograms**: Also based on the notion of emulated time, event frequency is recorded:
  - Dynamic Run Length Distribution.
  - Cache Address Distribution.
  - Store-to-Fetch Time Interval Distribution.

### A.4 The User Interface and Debugger

The interpreter for the hybrid machine provides a top-level for loading and running codeblocks, setting load-time and run-time parameters, collecting statistics, displaying program output and statistical results, and debugging. The debugger is implemented at the level of the instruction set. It is possible (and somewhat meaningful) to set breakpoints, to examine execution state, to perform tracing, and in general to treat the emulator as one would a pure von Neumann executor. The difference, of course, is that the state of a running computation consists of a tree of invocations, rather than simply a stack.
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