#### MAC TR-134

### CSG MEM0-106

#### SEMANTICS OF DATA STRUCTURES AND REFERENCES

David J. Ellis

August 1974

This research was supported by the National Science Foundation under research grant GJ-34671.

MASSACHUSETTS INSTITUTE OF TECHNOLOGY

PROJECT MAC

CAMBRIDGE

MASSACHUSETTS 02139

## SEMANTICS OF DATA STRUCTURES AND REFERENCES

by

## David J Ellis

Submitted to the Department of Electrical Engineering in September, 1974 in partial fulfillment of the requirements for the.degrees of **Maeter** of **Science** and Electrical Engineer

#### **ABSTRACT**

Each progranuning language that **handles** data structures has its own set of rules for working with them. Notions such as assignment and construction of structured values appear in a huge number of different and complicated versions. This thesis presents a methodology which provides a common basis for describing **ways** in which progranuning languages deal with data structures and references to them. Specific concern is paid to issues of sharing.

The methodology presented here consists of two parts. The base language model, a formal **semantic** model introduced by Dennis, is used to give the work here a precise foundation. A series of "mini-languages" are defined to make it simpler and more convenient to express and describe the semantics for a variety of constructs found in contemporary programming languages.

THESIS SUPERVISOR: Jack B. Dennis TITLE: Professor of Electrical Engineering

 $-2-$ 

#### Acknowledgments

I wish to express thanks to my thesis supervisor, Professor Jack Dennis, for the many ways he helped me along. in this work. He welcomed me into the Computation Structures Group when I was still looking for a group to *join; ...* brought the base language model to my attention: encouraged my ideas at every turn, even when I felt I was in a dead ... erid: smoothed over numerous technical rough spots: and exhibited patience and acceptance throughout, ...

Thanks are due to Jack Aiello, Mark Laventhal and Nimal Amerasinghe, who read drafts of the thesis and made many helpful comments and suggestions. Anne Rubin provided technical assistance while I was typing the thesis.

Generous financial support was provided over the past three years by the Woodrow Wilson Fellowship Foundation, the M.I.T. Electrical Engineering Department, and Project MAC.

Finally, special gratitude goes to my family, for always giving me support and advice, standing by me in difficult times, and helping me overcome doubts about where  $\tau$  should be I should be.

santys guide in

**Administration** Handel Hallahee Booth  $\alpha_{\rm N} = \gamma_{\rm D} \cos \left( \gamma_{\rm D} \sin \left( \gamma_{\rm D} \right) \right)$ 

网络海绵 网络阿尔伯 网络阿尔伯 2014년 12월 3월 10일 - 2월 10일<br>대한민국의 대한민국의 대

(4) 不是 化利普加特比特 (1) (1) (1) (2) 化转移程序

# TABLE OF CONTENTS



 $\sim$   $\sim$ 

## Chapter 1

-5-

### INTRODUCTION

날짜 이 아버지를 했다.

### 1.1. General Goals

r·

I· i '

> Students of computer science are confronted at a very early stage with a great variety of general-purpose programming languages. Descriptions of **these** languages place heavy emphasis on common features such as assignment, procedures, conditionals, input/output and block structure. Aside from variations in notation, there are numerous rules, exceptions and special cases which make fof differences between comparable constructs in different languages. For example, the body of a DO-loop in FORTRAN must be executed at a v stromnom storenjalstva (POSI)



least once, while in PL/1 it is to be skipped if the index is out of range (figure 1.1-1). Such differences can be studied by examining the semantics of different programming languages. The semantics of a programming language is the ນ ປະຊຸມສັງສ**າດຫຼືບ່ວນ** ອີງຄົນຫຼາຍຂຶ້ນສີ ທີ່ສະພາບຊາດ ຕ<sup>ໍ່</sup> **ໂ**ລ ເ**ອລັດອະ**ນີດ ເ study of the meaning of its constructs, or in other words "我的我,你的想要我的一个真实的,你不会一定做,你的人。"我的人的话,"我的人的。"我的话,"我们的话,你们的话。" the effect of executing programs in the language. The par-This property and the contract of the second property  $\alpha$ ticular concern of this thesis is the notion of data strucerino vinciminte**le** de conserva e seguidan la modo de la final de vincia e de la conservación de la conservació tures and the semantics pertaining to them as they appear ໄດ້ໂຮງລະຫວ່າຍ **ທົ່ວເ**ປີປີ ວິນສ໌ ລິມທຸກໃນປ່ຽນຜູ້ນີ້ ເສໄຄລິມໄດ້ມີກິດຕາລີ້ເສ**ື້**ເຮີຍໃຫ້ວ່ in programming languages. Conservation companies and income and the conservation of

en de la provincia de la companyación de la constitución de la provincia de la companyación de la companyación

 $-6-$ 

There are many areas of application in which the use of -so rencamella **v**o structured data is both helpful and convenient in problem. solving. Some example areas are symbol manipulation, artig ficial intelligence, computer graphics, and simulation studies : "Generally speaking, a data structure is an aggregate data object containing other data objects as components. Typical instances of data structures include arrays, sequences, vectors, tuples and lists. We will not dwell on the -2000 i characteristics peculiar to each of these different varieties of data structure; our emphasis will be on more general properties relating to data structures and their compon-

ents.

தல் நடவடிருந்துப் கலை உண்டை

الركابي الأراب ستجرأ أنبرى المرجود بمعونها ستوانية

en sproglegge in Stereopere partition of the control

Typically, a programming language provides two basic

Responding ( ow that southern the girls of the form of

operations for handling data structures: component objects of a data structure can be individually accessed and manipulated, and data structures can be constructed from designated objects as components. These operations interact with the assignment operation of a programming language in performing several other tasks, such as assigning structured values to identifiers, or updating components of a structure. There is a great similarity in appearance among constructs for performing such tasks in various programming languages. On the surface, from a casual examination of language descriptions, distinctions between analogous constructs in different languages appear to be mostly notational. But we shall see important semantic distinctions, particularly in the area of data being shared between different structures.

Since each programming language has its own set of rules for dealing with data structures and sharing, it is desirable to seek a rigorous method for describing what happens. Our goal, then, is to gain a more precise understanding of the semantics of data structures. This will provide a unified and coherent viewpoint for describing the different approaches to data structures aa they are found in

-7-

1.2. 机分子放下 计编码化 化硫代硫酸钠

programming languages. We will pay specific attention to 新婚の いっかん かいかんしゃん the difficult and important issue of properties of sharing. Anti-January of the structure These issues depend ultimately on the concepts of cells 39. 化水气搅拌 (14) 经同等额同年 (4) - 30.8 m , 11 m , 30.0 m m m m m m m m m m m m m m m m (which model computer memory locations) and references to cells. References are also commonly known as pointers. We will first discuss general questions of programming language 身体分泌 ほうきょう エービーけい k na sa sa Siri semantics, and then move towards a more specific treatment → 約束 (長い) 「長い出口になる is a strike extr of data structures and references.

## 1.2. Background on Formal Semantics and all

i ande≸gnise

្រុងមួយចេញ ការអង្គរជាតិ ការស្រុក ក្រុងប្រទេសក

A programming language provides a notation in which the 化异戊基异戊二甲醇 人名英贝布林格特里尔 医环境炎 计数据数据 化双羟基 经费得资金 人名卡尔 programmer can model computational processes and the infor-පදි විද ගැහැණුලිකත්ව අත**ුරි ය**ිප්පුදෙන්නේ මුද මහරෙහි මෙමම දී*රියාදීර* mation on which they operate. Programming language seman- $\mathscr{E}_{\mathbb{R}^n \times \mathbb{R}^n}$  , and the second control of the control of the second second control of  $\mathbb{R}^n$ tics deals with the relationship between programs and the objects they represent. A formal semantics for a programming language is a precise description of such a relations pailund ship. There has been much study of formal semantics of programming languages. Wegner (Weg 72a) distinguishes three ja ∄ a≴oleja drži nu 医胸部的第三人称单数 医血管 classes of formal semantic models:

医腹股膜骨髓炎 医额骨软骨 化氯丙酸去甲酯 人名科格拉斯 医扁桃

(1) Abstract semantic models. In this approach, the <u>VIS den van Douwaard op</u> objects being modeled are treated as mathematical entities ವುದರಿ ದಾಗ ತಂದ್ರಾದರು ಚುಟ್ಟಿತ ಸೆಸ್ಟ್ ಸಿಕ್ಕಿ ಪ್ರ 電話 しゅうぼうし  $\mathcal{A}^{\mathcal{L}}(\mathcal{G}) \subset \mathbb{Q}(\mathcal{H}^{\mathcal{L}})$ independent of any particular representation. Models of

しちがない あいがい おこしょうぶつ

this class aim towards providing a formal mathematical de-化苯甲基苯基苯 计设备代码化磁盘设计 聚合学学家公司 医异常 医学 scription of the computational notions being studied. One tret att halter and the second of the same well-known example of this approach to semantics has been  $\mathbb{R}$  and  $\mathbb{R}$  and  $\mathbb{R}$  . The set of  $\mathbb{R}$ the use of the lambda calculus as a semantic model for programming languages. The lambda calculus, which is described in [Der 74, Morr 68, Weg 68], is basically a mathematical formalism for the definition and application of functions. It is ideally suited for describing so-called applicative features of programming languages, such as evaluation of expressions, use of procedures, and block structuring. Landin demonstrated its usefulness in these areas [Lan 64] and pre-A Chierophil sented a scheme for extending the lambda calculus formalism to model the language ALGOL 60 [Lan 65]. More recently, different extensions of the lambda calculus have been devised for describing data types [Reyn 73].

A second major example of the abstract approach to se-ាង ដើម្បី និង បានបង្កើត ដែលបានបង្កើត ដែលមាន ដែលប្រាប់ និង ដើម្បីការប្រាប់ និង ដើម្បីការប្រាប់ និង ដើម្បីការប្រ mantics is found in the work of Scott [Scot 70, Scot 71]. Scott makes use of the mathematical theory of fattices [San 73] to construct sets which are the domains of functions that represent the behavior of programs. The Scott formalism has been used recently to describe the semantics D. 2018 (18) (18) (18) (18) (18) (18) of ALGOL 60 [Mos 74].

an y fail an Alban agus an Alban an Al

-9-

이번 번 중에 가장

With Sam Clarestic We can briefly summarize abstract semantic models by saying าลูกไกล์ ( ) และติดต่อออก <mark>แ</mark>สดุ 3.6 สดีกว่า 的解决的 电弹性硬化 that they characterize the action of programs as functions!  $\langle \partial_t \tilde{\mathcal{R}}^{\mathcal{L}}_{\mathcal{M},\mathcal{L}'} \rangle = \langle \partial_t \partial_t \partial_t \partial_t \partial_t \partial_t \partial_t \partial_t \rangle$ 医阴道囊 经国 しょう 自我の協会 しゅうかつき セイラ over various domains.

in Turkita L

on Alt al Bawl

(2) Input-Output models. Models of this class use statements of mathematical logic as assertions about the state of a computer system at various points during the execution of programs on it. The sementics of a program is viewed as the relation between input assertions (the state) of the system before execution) and output assertions (the state after the program is run). This approach to semantics, more frequently called the axiomatic approach, was developed by Floyd [Floy 67] and Hoare [Hoar 69, Hoar 71]; there has been much further work on it. Axiomatic semantics is most useful in proving correctness of programs, i.e. establishing that the effect of executing a program fulfills mathematical conditions the program is supposed to satisfy.

(3) Operational models. This approach to semantics concerns itself specifically with modeling the changing states of a computer system performing computations. Such a task is usually accomplished by means of a state-fransition system, in which a state of the model represents the information in the computer system at a given time. The effect

 $-10-$ 

医中心弹性纤维性表重新控制性心包 网络

of a program on its input data is reflected in the sequence of transitions of the model. It is important to observe that given a state-transition system corresponding to some . 1944年1月18日 SEA 1945年11月17日 program, the sequence of states that models the execution of this program defines the, action of an interpreter for the program. For this reason, the approach to formal semantics using operational models is called interpretive semantics.

We can describe the way in which an interpretive semantic model gives the semantics for a program written in some source language. A translator transforms the program into うい はまけい an equivalent program in· another language which we call an abstract language. Programs in an abstract language are. acted upon by an interpreter; this action results in a Sand Carlos sequence of state transitions of the model. The semantics of the original source-language program is given by such a sequence of transitions. One reason we make use of translators is that source programs are usually represented as character strings rather than as data objects suitable for **TEST AREA SERVER** processing by the interpreter.

Although the use of interpreters to implement programming languages was (and still is) commonplace, McCarthy [McC  $62$ ] was the first to use an interpreter to define a

-11-

والمجلوب والمتعالم المستور والمساحة

 $\label{eq:4} \frac{1}{\sqrt{2}}\sum_{i=1}^n\sum_{j=$ 

ويهدى المحافظة المستقرب والمستعمل والمستقلعة والمستقلعة والمستقلعة والمستقلعة والمراقصة والمستعمل والمستعمل والمستقلة

language (LISP). The semantics of LISP is given formally by an interpreter written in LISP. Landin [Lan 64, Lan 66b] uses an interpreter called the SECD machine to define the lambda calculus, even though the lambda calculus is a mathematical formalism with a rigorous definition of its own. A more recent discussion of definitional interpreters is found in [Reyn 72].

Of these three approaches to formal semantics of programming languages, the interpretive approach is best suited 小儿 超速的 for our goals of understanding the semantics of data structures and references. In order to properly explain the semantics of a program that handles data structures, we will need to know how the data structures are formed, their composition, the relationships between the structures and their components, sharing properties, and other items of information. The best way to get a handle on this kind of information is to consider the state of the system at various moments during the execution of the program. The interpretive approach is the only one which lends itself directly to working with states of the system. Both of the other approaches are better suited for proving assertions about programs and establishing their correctness; but these

 $-12-$ 

المجرد بالمراجع وجرجتهما

issues are outside our main concern here. A treatment of data structures from the viewpoint of axiomatic semantics may be found in [Lav 74]. We will work towards developing an interpretive model to be used as a semantic foundation for dealing with the important issues of data structures and references.

计复变时 经公司承兑额 化溴化合金

in el escrito

The most prominent interpretive model for semantics is the VDL model. VDL, the Vienna Definition Language, is a metalanguage for writing interpreters of programming languages. VOL interpreters **have** been written for languages such as ALGOL 60 [Lau 68], PL/1 [Walk 69, Luc 69], BASIC, and<br>second as a second s 2014/02/2015 12:20:20 PDP-8 machine language [Lee 72]. An elementary introduction to VDL may be found in [Weg 72b]. Just as LISP works with lists, VDL 'WOrks with tree-like data objects (which we call labeled trees). The basic operation of the VOL model is as  $\mathcal{A}_2=\mathcal{A}_1\oplus\mathcal{A}_2$  ,  $\mathcal{A}_2=\mathcal{A}_1$  $-4.4 - 1.7$ follows: for each source language **whose** semantics we wish to describe, we define a translator and an interpreter. The translator transforms a source language program into an abstract program, which is a form of labeled tree suitable for manipulation by the interpreter (for each source language the corresponding abstract language will be some Set of labeled trees; the structure of an abstract program varies

กับสูงสำคัญ <u>กลุ่ม แต่ตลอด ตัวเด็กที่</u> จะเป็น Constant Political Constant from language to language). The interpreter, which consists of VDL code, accepts a labeled tree as input and interprets 

the effect of the program on its input data. For different වැයිස් සිත්වා සිටි සඳහා කිරීමෙන් වෙන විවර්ධනය විවිධ කිරීමට සිත්වීමෙන් කිරීමේ කිරීමේ lanquages, different interpreters are defined.

Service Security to the country of the property and figure

The fact that VDL uses treelike data objects reduces its desirability as a semantic model for our work on data AR TELEVISION AND DESCRIPTION OF A STRAIGHT AND THE STRAIGHT OF A structures. We will be studying data structures in which The Side Hitler Class (当社第19年) كالعمامة المسرمية components may be shared between different objects; VDL's is a class program of the construction of the constant of the common common of the common of the common of the labeled trees do not directly admit sharing of any kind. ລັງເລື້ອນ ແລະ ເພື່ອເປັນ ເພື່ອມີຄວາມເຊື້ອນ ແລະ ເພື່ອມີຄວາມ ແລະ ເພື່ອມີຄວາມເຊິ່ງ ແລະ Thus in order to model in VDL structures such as we will  $\mathfrak{g}_{\mathcal{B}}$  ,  $\mathbb{Z}$  ,  $\mathbb{$ study, it would be necessary to go through the inconvenience r deroksol voladskrift som utill erop vpall stadium i ligg. of simulating the memory of a computer. Since the study of the office was about the country infinite and the state of the state sharing is fundamental to our work, it is desirable to work a Galifa Meirleanna an Antil Geir Ann an Caracte This Theod with objects in which sharing is represented directly. We and the last as the state of the second state of the second state of the second state of the second state of the therefore prefer for our goals' a semantic model that ง 2014 ส.วิทยายังคลิง พลังกรณ์ โดยมีการกระโดยที่ ครั้ง ครั้งที่ 1 เจ้าสุดีไป manipulates data objects of a more general nature than VDL's ා කොට කොට්ටිකට කත්තික විට බිම්මාන්ත විසින් කොට්ටික යන මෙයි.<br>මේ බිම්මාන්ත විද්යාලනය කොට්ටික බිම්මාන්ත විදේශය විද්යාලනය විද්යාලනය විද්යාලනය විද්යාලනය විද්යාලනය විද්යාලනය වි labeled trees.

In [Denn 71], Dennis outlines an interpretive semantic model called the base language model. The data objects manipulated by this model are variants of directed graphs and can directly model sharing. As with VDL, for each language whose semantics we wish to describe, we must specify a

light securities as a statements and the second

translator which transforms programs in the language into data objects suitable for consumption by the model. These objects are called procedure structures in the base language model. Procedure structures, like VDL's abstract programs, are acted upon by the interpreter to produce state transitions. But the base language model differs from VDL in that the composition of a procedure structure generated by the translator from some source program does not depend on the language in which the program was written. As a result, there is no need to define a separate interpreter for each programming language. There is a single,  $p_{\text{X}}e$ -supplied in $\pi_{\text{X}}$ terpreter for the base language model which accepts arbitrary procedure structures and interprets them as programs. Thus we see that the translators for the base language model translate programs from their respective source languages into a single, common language. We call this language the base language. A procedure structure represents a program in the base language, which consists of a sequence of instructions. The individual base language instructions specify the fundamental state transitions of the model.

In order to achieve the language-independence of the interpreter in the base language model, the translators must

 $-15-$ 

णूडम् <del>अनुसारमण्डला पुरस्का का अ</del>पि एक वि

do more work than their VDL counterparts. A VDL translator simply converts a program from character string to labeled tree. while a translator for the base language model must perform functions similar to those of a compiler. Thus, once we specify the semantics of the base language, i.e. decide on a formal specification of the actions performed by the interpreter in the base language model, the semantics of a particular programming language is determined by its translation into the base language.

The base language model is extremely well suited for our work. The primitive instructions of the base language are particularly convenient for manipulating structured objects and dealing with sharing. We can view the base lanquage as the machine language for a computer with heapstructured memory and symbolic address space. In this respect, programs in the base language will be similar to conventional assembly language programs. This similarity is a source of further convenience in using the base language as. a programming tool.

Amerasinghe [Amer 72] described the translation of a block-structured language BLKSTRUC into the base language. In BLKSTRUC, procedures are "first-class objects" [Stra 67]

 $-16-$ 

which can be used in contexts as general as objects of other types. BLKSTRUC's treatment of procedures is more general than ALGOL 60's. The action of a translator for a language with non-local goto's is described in [Amer 73). Translators for the languages SNOBOL4 and Simula 67 are discussed in [Dra 73] and [Cou 73]. These works show the use of the base language model in describing the semantics of various powerful programming languages. We will be using a version of the base language model as the semantic foundation for our study of data structures.

## 1.3. Plan for the Thesis. The Solid Contract of the Thesis and the Theorem of the Theorem is a state of the Theorem of the Theorem is a state of

we outline here the topics.covered in the rest of **this**  thesis. chapter 2 describes the base language model as we will be using it. The action of the interpreter is given by describing the effect of the instructions of the base language. The approach in Chapter 2 is informal; a more rigorous treatment is found in the **Appendix.** once the behavior of the base language interpreter is known, we have a handle on the semantics of the programming-language constructs that interest us. All that wi11 then need to be done to supply a formal semantic definition is simply to

医异性糖 医单叶 化重新分子 化聚合合金 化自动机 医神经性神经性神经神经神经神经神经神经神经神经神经神经神经

describe the action of a translator which produces base language code.

In the remainder of this **thesis we** will be using the base language model aa a semantic foundation for describing the different ways various programming languages deal with data structures. We want to make clear distinctions between comparable constructs in different languages. Although the semantics of data structuring constructs can be precisely expressed by using the base language model, there is a certain respect in which the model **is leas** than ideal as a descriptive vehicle. Data structures as they are found in programming languages are tied up with the notions of variables and **values**. We would like to make use of these notions in talking about the semantics of data structures. But the descriptive level of the base language is only. equipped for talking about primitive transformations on the objects which comprise the interpreter states. In this sense the **base** language is too "low-level" for describing data structures in a manner suitable for our purposes.

To provide a better descriptive mechanism, we will follow the approach taken by Ledgard [Led 71] in defining a series of "mini-languages." Mini-languages provide de-

scriptive levels appropriate to our needs, yet at the same time avoid the syntactic and semantic complexity of fullscale programming languages. The Primary advantage of the mini-language approach is that we can isolate the concepts we wish to describe by eliminating all the conceptually extraneous notions that are needed in a full-size language. Accordingly, in a mini-language for describing data structures, there are no procedures, conditional expressions, loops, goto's or operators. Mini-languages are not meant to be viable languages for actual programming; they are used for descriptive purposes only. The syntax and semantics of a mini-language are simple enough to be readily understood  $\{w_{i},w_{i}\}_{i=1}^{N}$  , and  $\{w_{i},w_{i}\}_{i=1}^{N}$  ,  $\{w_{i},w_{i}\}_{i=1}^{N}$ on an informal basis; the semantics can then be formalized () 相似的 机化合金 网络康顿斯勒森 电空台放大器 化乙烯酸 化气管 by specifying translation into the base language. In this manner, the semantics of data-structuring constructs in fullscale programming languages can be given by describing how to express these notions in a suitable mini-language.

Chapter 3 presents mini-languages for describing the notions related to assignment, data structures, pointers and sharing. These mini-languages are then used to describe the data structuring semantics of several full-scale programming languages.

 $-19-$ 

<u>na sa sa sana sa sa sa sa sa sa sa sa sababan sa sa sa sana basan sa sa saba aban a sa sa sa sa sa sa sa sa s</u>

In Chapter 4, we treat the additional notion of static typechecking, which has a direct bearing on the semantics of data structures in many important programming languages. This notion of static typechecking differs from Ledgard's in that it deals with structured types, where Ledgard [Led 71] deals with functional types and the types of arguments and returned values. As in Chapter 3, we treat the data structuring facilities of three full-size languages; in these languages the concept of static typechecking is directly tied in with the semantics of data structures (specifically assignment).

Chapter 5 presents a summary of what we cover in this thesis and suggests extensions for further study.

### Chapter 2

#### THE BASE LANGUAGE MODEL

#### 2.1. Overview of the Model

计对比分析 化四硝基甲醛磺酰胺磺酸医磺胺

الراحية بالأقا

We have chosen as the semantic foundation for our work. a version of the base language model set forward in. [Denn, 71] and [Amer 72]. The base language model centers around a base language interpreter, which is essentially a statetransition system that we shall use to express the meaning of computations. The interpreter specifies the behavior of an entire computer system. We represent a computation by a sequence of interpreter states. A state of the interpreter will be a certain kind of mathematical object embodying the information contained in the computer **system** at a particular point in time. We shall define **a base** language called BL each of whose programs consists of **a sequence** of instructions. Signess of County and States 产品 子教者修好 Each instruction specifies a functional transformation betransvenski koledarju dobio tween interpreter **states.** The **langua99 BL is** adapted from the rudimentary language described by Dennis in [Denn 71},.

We represent interpreter states by mathematical objects known as BL-graphs. Suppose we are given a set ELEM

e staget et te samme staget av formandelige de de formandelige de la production de de la secondation de la produ<br>Secondation de la production de la produc

of elementary objects and a set SEL of selectors. (For our purposes, ELEM consists of integers, real numbers and strings; SEL consists of integers and strings.) Then a BL-graph is a variant form of directed graph; it consists of nodes and arcs. Each arc connects two hodes in a specified direction and is labeled with a selector. We may associate an elementary object with each node from which no arcs lead out. There must also be a distinguished subset of the nodes (called the root nodes) from which each node of the graph can be reached along some directed path of arcs. We give a formal mathematical definition of BL-graphs in the Converted to the Carlos et al. Appendix.

i ang inaklopas pang mitok ini na matang kalimban ing Piliping Military 2010, ata na makali populasi A BL-graph with a single root node is called a BL-object. .<br>Listo ta juga le con conseguencia cella che di detallazione esti la gastrichi pr We identify a BL-object by its root node. Specifically, where the contraction of the contraction of the contraction of  $\overline{\mathcal{A}}$  , and  $\overline{\mathcal{A}}$  , where  $\overline{\mathcal{A}}$  is the contraction of  $\overline{\mathcal{A}}$ for any node  $\alpha$  in a BL-graph G, we associate With  $\alpha$  the substandard the state of the state o graph of  $G$  whose nodes and arcs are accessible from  $\alpha$ . This  $\sim$  10 most much and in the contraction of  $\delta$  it equal to contract the  $\delta$  -size. subgraph is a BL-graph with a as its root node; we call it 化二甲基 电视网络电脑 幽囊 的第三人称形式 化三硫酸 .<br>De la resigna de la provincia de 10 mes the object of a.

If there is a directed path from one node of a BL-graph (1) 12 年至1944年至10月1日1月1日1日,全国博士的《高速移传报》(4) 第41章 《建筑数据链点资本集》 to another node, then the second node is called a descendant .<br>The six of manufacts of assignation of the state of the st of the first node. All nodes in a BL-graph are descendants of some root node. A node from which no arcs emerge is

化分析线路 医联合体动脉 人名英威尔克 机波尔利法 人名德博斯

<u>I I Marta professor</u>

called a leaf node. An elementary object attached to a leaf node is called the value of that node. If there is an arc from a node  $\alpha$  to another node  $\beta$ , then  $\beta$  is called a com- $\frac{1}{2}$ ponent of  $\alpha$ , and the object of  $\beta$  is called a component of the object of *a.* components are named by the selectors on the arcs leading into them. If an object is a component of two distinct objects, it is said to be shared between them. Nodes in a BL-object are denoted by pathnames. A pathname for a node is a sequence of selectors labeling a directed path to that node from the root node. If the object of a node is shared, then the node will have distinct pathnames. The property of sharing is of major significance; we will have much to say about it.

We will be making heavy use of pictorial representations of BL-objects. An elementary object **is drawn as** an encircled value (figure  $2.1-1$ ). For a general BL-object, the nodes are drawn as heavy dots. The root node is at the top. Arcs emerging from a node are  $\overline{\wedge\cap\cap}$  $Fig. 2.1-1.$  Sample alementary objects

drawn downwards from a horizontal line attached to the node. Selectors are written across the arcs that they label. If a

 $-23-$ 

8월10 7 연주의 10m 10m 10m 10m

 $\mathbb{E}[\mathcal{L}^{(2)}_{\text{max}}, \mathcal{L}_{\text{max}}]$  and selector is a string, we do not enclose it in quotes. Elemi na i districti popular (sed pri la c entary objects attached to root nodes hang downwards from ge og Aceae påkroppp (1941) Kor 付 賞 歌 them. Thus our pictorial conventions for BL-objects differ and you be more than the second to the slightly from those used in [Denn 71].

ta an salah 1952 (Provincing selama kacamatan sa

Sample BL-objects are pictured in figures 2.1-2 and 2.1-3. The object in figure 2.1-2 has three components, <sub>Jame</sub>r – Francuský b**otad**a, P







named k, c and a, The c-component is empty. The k-component has two components, both of which are leaf nodes. The leaf node with value 9 has pathname k.c. The leaf node with value

sa per

'hi' is shared between nodes k 计设备系统 医心包分裂 医骨间的 医心包的

> and a and has path-A TV 1997) en Belk dir. 통해 han bau

names k.u and a.6. In hygplak ents, folkrikbör fiqure  $2.1-3$ , the obinerda-ut Estenebid Mor ject with value 1.6 is ්ය**යේ** මුළි අම්පෝර්ෆ් දියේ කලේ shared between the ob-(1889) 安全 (1985) 1986年(1988年) 中国教授 jects s.b and s and Arthur Thorn (March 1973) has pathnames s.b.5

Heart in In and  $\boldsymbol{s} \cdot \boldsymbol{4}$ . The object

the and secred advocation and the store of the shared

between the object of the root node and the object c.y. Since the node c is a descendant of itself, it has infinitely many pathnames c, c.y.2, c.y.2.y.2, c.y.2.y.2.y.2, and so on. The path joining this node to itself is a directed <u>cycle</u>.

A basic difference between out BL-graphs and the graphs of [Denn 71] is that Dennis does not allow directed cycles in his objects. Cycles seem to impair the management of storage and the handling of parallelism in computation. However, cycles occur in many of the structures we shall be modeling. Moreover, they are difficult to detect and remove (see {Amer 72} for more details on the problems of cycles). We shall therefore not rule out cycles here.

We follow [Denn 71] in giving the structure of a BLobject which represents a state of the interpreter. An interpreter state is a BL-object having three components as follows:

(1) The universe-component models system-resident information, both data and procedures. Generally speaking, this information is independent of which computations are currently active or how far various computations have progressed.

 $-25-$ 

冷心 ベルー 外地樹 旅館

(2) The local-structure-component of an interpreter state has as components a series of activation records for the various procedures being interpreted in the system. These components are called local structures; there is one local structure for each activation of each base language procedure. A local structure represents the environment for its activation, primarily identifiers and their associated values. Thus the local structure component of an interpreter state records the progress of cempatations by modeling their changing environments. The control of

(3) The control-component has as components a number of sites of agtivity, which indicate for each current computation the next instruction to be executed, the appropriate environment (local structure) for the computation, and other information.

We shall not go into the details here of representing the universe- and control- components of interpreter states. The interested reader can consult the Appendix for that kind information. We will be dealing almost exclusively with local structures in the remainder of this chapter. In the next section, we describe the action of a number of primitive BL instructions.

 $-26-$ 

### 2.2. Base Language Instructions

We introduce the primitive instructions of BL, which define state transitions of the interpreter in our model. Each BL instruction executed by the interpreter belongs to some procedure written in BD and is interpreted during an activation of the procedure. We call the local structure corresponding to this activation the current local structure  $(c.1.s.)$  for the instruction.

A BL instruction consists of Anoperation code and up to three operands. The operation code is underlined. Most of the operands of the various instructions are selectors, which are frequently used to denote names of components of the root node of the c.l.s. We reserve the tetters x, y, and z for selector names used in this fashion. Business and the property of legacy

yta nggala ya kwakazi wa mafina kuto We shall give informal descriptions of the effects of nnan sama mistir ikis filipun hodi (44 BL instructions, accompanied by sample "before" and "after" callege which could as also a live once diagrams of the c.l.s. A more formal definition of these where  $\mathbf{s}_i$  is chosen two two typical . The sum  $\mathbf{s}_i$  is a graph sign of  $\mathbf{s}_i$ instructions may be found in the Appendix. t the second contraction of the state of the second states of the second second second second second second second

Each instruction is designed to perform a specific<br>contract to the set of the s .<br>గ్రామం నుండి function in changing the c.l.s. This is called the primary

 $-27-$ 

일 가능 네 스웨어의 발표장 <del>/ 역사</del>

्दिः अङ्ग्लिकार्थियो <del>सर्वत्रे सार्वपूर्णम्</del> अस्य प

**Completed in the Complete** 

role (or, more simply, the role) of the instruction, and depends on certain conditions being fulfilled (e.g. the presence or absence of specific components in the c.l.s.). The effect of an instruction when such conditions do not hold is called a subsidiary effect, or subsfiect.

The oreste instruction is used to create a new com-



ponent in the c.l.s. Provided that the c.1.s. has no x-component, the primary role of the instruction greate x is to add one  $(figus) = 2.2+1$ . The new  $x$ component will be an empty leaf node. if the c.l.s. already has an x-component, then the in-

struction create x has a subsidiary effect of changing the arc with selector x from the root node to point to a newly allocated node. For this subeffect the former x-component node will remain as part of the c.l.s. only if it was shared with some other node. Figures 2.2-2 through 2.2-4 illustrate subeffects of the instruction create x and its interplay with the sharing property. Portions of a diagram enclosed in dotted lines are no longer part of the c.l.s.

 $-28-$ 



and can be thought of as garbage-collected.

مستقطع المتعارف والمستور

The clear instruction is used to make a node empty; clear x detaches whatever hangs downward from the node x7 leaving x with an empty value. The old value of x is lost even if it was shared with some other node. Figures 2.2-5 and 2.2-6 illustrate the role of clear x. If there is no x-component in the c.l.s., clear x acts like create x and generates one (fig. 2.2-7).

The delete instruction removes arcs from the c.l.s. The arc from the root node to the node x is removed by the instruction delete x (figs. 2.2-8 and 2.2-9). The arc



with selector m from the node x is removed by the twooperand form delete x, m (figs.  $2.2-10$  and  $2.2-11$ ). If an arc to be removed does not exist, then the subeffect of the delete instruction is that no action be taken.



The const instruction is used to attach elementary ob-オーはえばくさい ルーケー jects to nodes. If v is any elementary object, then const v.x causes the value v to be attached to the node x. ya bol wilayikin w The old value of x, if any, is lost. Figure 2.2-12 illustrates the role of the instruction const 5, x (where x is a leaf node), and figure 2.2-13 shows a subeffect of the same instruction (for the case when x is not a leaf node).





Arithmetic instructions such as add, subtr, mult and div are used to manipulate elementary values. For example,



the instruction  $\frac{add}{ }$  x, y, z adds the values attached to nodes x and y and places the sum in node  $z$  (figure 2.2-14). It is an error to attempt to execute an arithmetic instruction

if one of the first two operand nodes fails to exist or contains an improper value (not a leaf node or empty or wrong type of elementary object). We leave the effect of such an attempt undefined. 小说的 法婚姻

The link instruction is used to initiate sharing between nodes. The instruction link x, n, y causes the node y to become the n-component of x (so that y will be shared





between the node x and the root node). This is done by adding an arc with selector n from node x to node y. Figures ුණු කොට් දැන කර ගිනුව ජන**ම හිටදු** හිමි පිට 2.2-15 and 2.2-16 illustrate the role of the instruction satori shekara a a a shekara a ba Ta If x already has an x-component or is a leaf  $link x, n, y.$ ARTIST CHARACTER STORE NORTH AND SATISFIED node with some elementary value, then the subeffect of the te sa colaser en robbordada said same instruction causes the old value of x to be lost (figs. ුහු ඉඩකා යාධාල කණ්ඩිය වුරම්මල් වා කරම්මට 2.2-17 and 2.2-18). The nodes for x and y must be present

ි අප ලොපන්නම බුස්සි<sup>ල්</sup>බිස් ස්ර*මාල වශයේ* අපේ**නා** or else the instruction is illegal.



Fig. 2.2-17. Subeffect

of be link x, n, y

The select instruction satisfies a dual purpose. If a wa solinezhak Kalz a node x has an n-component, then the instruction select x, n, y **ARTICLE IN A SUPER CONTROL OF A STATE OF A ST** makes the n-component of x the y-component of the root node (so that it can now be "addressed" by further BL instruc-Then the basic contribution of any second the contribution of the second se

**2-18. Subeffect of** 

**ne x/n/y distr** 

tions). In this manner a BL procedure may gain access to นที่ได้ที่ได้ให้เพิ่มให้เพิ่มให้ **หลัง**เรื่อง หน้า เรื่อง เพราะ และ เรื่อง เรื่อง เรื่อง เรื่อง เรื่อง เรื่อง เ arbitrary nodes of a c.l.s. If x has no n-component, then three is the street, who immunities are the street of the

the instruction select x,n,y generates one first, then, makes it the y-component of the root node. This is the in the form of the second control of the second control of the second control of the second control of the second principal way to construct BL-objects, i.e. by using the select instruction to add on components. These two roles of the select instruction are depicted in figures 2.2-19 and 2.2-20, respectively. The root node may or may not have a y-component prior to the execution of select x,n,y. If it does, then the value is lost unless it was shared.



The apply instruction provides for the activation of BL procedures. Let the p-component of the c.l.s. represent the BL code for some procedure (i.e. be a procedure structure). Then the instruction apply p,x activates this procedure in the following manner: First, **a new,** empty local structure is created. The x-component of the c.l.s. is then made

 $-34-$ 

the \$par-component (parameter linkage) for the new local structure (we refer to the BL-object x as an argument structure). Finally, control is passed to a new site of activity. This means that the newly-created local structure becomes the c.l.s. and the old site of activity is made dormant. The interpreter will now execute instructions from the procedure p until it is told to return.

The return instruction provides for termination of the execution of a BL procedure and for return to the calling procedure. Upon execution of a return instruction, the c.l.s. is deleted. All its components vanish. The parameter ていまなさけてあるとし é ca linkage, since it shares with the argument structure of 的过去分词 化混合合配 的复数地名德  $-24.4$ the invoking procedure's local structure, remains. Control (おましわす) 网络石油がす ぽのとのほかな is returned to the dormant site of activity for the invoking procedure, and its local structure becomes the new c.l.s. The invoking procedure resumes from where it left off.

In order to invoke a procedure, it must be represented la theire trial white beach as a sample and bi as a component of the c.l.s. The move instruction makes data in the universe available for invocation as a BL procedure. We will not have occasion to use this instruction here; further details are found in the Appendix.

长虫粉的 蜂窝的

The instructions of a BL procedure are labeled with

 $-35-$ 

**SANS AND THE CONSTRUCTION** 

ு த≤ வரைத

natural numbers; execution of a BL procedure consists of the successive execution of its instructions in sequence according to the numbers labeling them. The remaining BL instructions provide for changes in the control sequence. Each of them has as one of its operands a label  $\mu$  which must be a natural number labeling some instruction of the procedure currently being executed.

The instruction  $\phi$  qoto  $\ell$  transfers control to the instruction in the current procedure whose label is the natural number  $l$ .

The instruction elem?  $x, \ell$  tests whether the x-component in the c.l.s. is a leaf node (elementary object). If. not, control passes to instruction number 1.

The instruction empty?  $x, i$  checks whether the  $x$ component of the c.l.s. is an empty leaf node (i.e. no components and no elementary value). If not empty, control transfers to instruction number  $l$ .

The instruction nonempty? x, t performs the same test as the corresponding empty? instruction, but control passes to  $\ell$  if the x-component is empty.

The instruction eq?  $x, y, \ell$ looks at the x- and y-
components of the c.l.s. Both must be leaf nodes, or else the effect of this instruction is undefined. These nodes are checked to see if they have the same elementary value. If the test fails (i.e. their values are not equal), then control passes to *J,.* 

The instruction  $has 2 \times m, t$  checks whether the xcomponent object of the c.l.s. has an m-component. If not, control passes to  $\mathbf{L}$ .

The instruction same?  $x,y,t$  checks whether the xand y-components of the c.l.s. share the same node. If <u>not</u>, i.e. they are distinct nodes, control passes to  $\iota$ .

In all the above conditional instructions, if the c.l.s. fails to have a component indicated by some operand, then the effect is undefined.

other conditional instructions analogous to the above ones can be defined (e.g. testing whether one elementary value is less than another) • We. will **have·** no need here for such additional instructions.

Finally, we discuss one more instruction that will be needed. Given a BL object, we will want to be able to access each of its components, without knowing beforehand

تاعية فالمواسطة والمستعبر والمناسب المستور

To popular professional state to the mo

아직하게 막기의 대학에 대통하는 생활에 대한 일부 대학 사람들이 없다. 이 가장 나는 아이가 있다.

the names of the selectors. The getc instruction serves this purpose. Successive executions of the same instruction getc x, i,  $\ell$  extract successive components of the x-component of the c.l.s. by causing the i-component of the c.l.s. to assume as its successive values the selectors on the arcs leading from the node x. No component will be extracted more than once, and control passes to  $\ell$  when no more components of x remain to be accessed.

#### 2.3. Programming Conventions for BL

In this section we introduce a few programming conventions which will make BL procedures easier to write and understand. We can view BL as the machine language for a hypothetical computer. Our conventions are then similar to the programming features provided by a macro-assembler.

Although individual instructions in a BL procedure are



labeled by natural numbers, we shall use symbolic labels. For example, suppose that x and y denote leaf nodes in the c.l.s. Then the BL code of figure 2.3-1 places the

string value "yes" in the node ans if the values of x and y are equal, "no" if they aren't.

The nodes addressed by operands in the BL instructions must be direct components of the root node of the c.l.s. With the select instruction, we can access nodes further



down in the c.l.s. For instance, suppose we wish to change the value 3 in figure 2.3-2 into the value 4. This is done by the const instruction, but in order to access the proper node, we must use the select instruction three times. In the BL code that performs our task (figure 2.3-3), the reserved



selector \$temp acts as a temporary variable. By using a "dotted pathname" convention to refer to appropriate nodes, we can abbreviate this BL code as the single instruction const 4, x.b.d.e. This can be viewed as a macro-instruction whose expansion gives the re-

quired select instructions. Alternatively, we can look at

this convention as extending "addressability" to arbitrary  $\mathbb{Q}^{n_1 \times n_2}$  . nodes in the c.l.s.

We will make frequent use of a macro-substitution capability, which is provided by a "\*" convention. If z is a leaf node containing some elementary value, then \*z denotes this elementary value. For example, in the c.l.s. of figure 2.3-2,  $\star$ z denotes the value 6. The abbreviation const  $\star$ z, y specifies the same transition as the instruction const 6, y when the c.1.s. is in this state. In the c.1.s. of figure

> 2.3-4, the leaf node with value 2 can be addressed by any of the forms x.a.  $x^*z$ ,  $xy$ , a, or  $xy$ ,  $z$ , while the value 2 itself can be denoted by any of the forms  $*(x,a)$ ,  $*(x.*z)$ ,  $*(xy,a)$ , or  $*(xy, *z)$ . As a third example, the

> > BL code of figure 2.3-5 sets all the components of the object x to sero. Note that the leaf node i contains as successive values the names of the selectors from x. Thus

the dotted pathname x. i refers to the successive com-

 $P1q. 2.3-4.$ 

loop: getc x.i.out  $0, x, *1$ **const** 9929 LOOD out:  $\bullet\hspace{0.1cm} \bullet\hspace{0.1cm}\bullet\hspace{0.1cm}\bullet\hspace{0.1cm}\bullet\hspace{0.1cm}\bullet$  $Fig. 2.3-5.$ 

# ponent nodes of x.<br>In the special companies of a semi-memory constant of the semi-memory of the semi-memory of the semi-memory of

the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of the state of t

We now define several macros for BL to denote commonly performed functions. The .setl macro (set up local structure) is used to set up new components in the c.l.s. Figure 2.3-6 shows the definition of the set1 macro, and figure  $2.3-7$  gives an example of its effect. Seter



The remaining macros. ;we will use **deal** with linkage be- ,, tween BL procedures. We first define a procedure closure to be a BL-object with two components. The \$text-component : contains BL text of a procedure, and the \$env-component contains references to the global variables named in the procedure. (Note that "\$" is a legal character in BL.)

- 長妻座像

The .call macro expands into BL code to invoke a procedure. In the definition in figure 2.3-8, the node **p** must be a procedure closure, and al, ..., an are selectors



kassaya (Alia 1998) olan Elizabeth S

leading to the arguments, which may be arbitrary BL-objects.

Figure 2.3-9 gives an ex-The Sounded Theorems, Res ample of the invocation of es de bard e<sup>vo</sup> (erstande, ó a procedure p having a i oli said seanna laos an choi single global reference w; **Read Collection Road** the procedure p is called with arguments x and y. local structure of the invoking procedure, and the new c.l.s." is the local 10.32.2 (全体)

Sean Aprová († 18. září 14

.<br>Tanan dia tanàna amin'ny faritr'i

structure of the called procedure p. The "after" picture

shows both the old c.l.s. and the new c.l.s. when control is passed to the procedure p. y 'en l' vai diendi y 17 decen



The .getp macro (get parameters) serves to bind the formal parameters of a procedure to the actual arguments with which it was invoked. The .getg macro (get globals) makes the global variables named in a procedure accessible 三分子类 法经济 in its body. These two macros are defined in figures  $\label{eq:4} \begin{split} \mathcal{L}_{\mathcal{A}}(\mathcal{L}_{\mathcal{A}}(\mathcal{L}_{\mathcal{A}})) = \mathcal{L}_{\mathcal{A}}(\mathcal{L}_{\mathcal{A}}(\mathcal{L}_{\mathcal{A}})) \end{split}$  $2.3 - 10$  and  $2.3 - 11$ . 850-8



a kalifornia da wakati wa m

The first actions a procedure normally performs when given control are the retrieval of parameters and global variables (using the .getp and .getg macros respective $ly$ ). Figure 2.3-12 is a "continuation" of figure 2.3-9, showing both c.l.s.'s after the invoked procedure p executes the two macros .getp  $(u,v)$  and .getg  $(w)$ .

With the BL programming conventions that have been defined here, we are now ready to use BL as the language of our semantic model.

को अनुसार का साथ का प्राप्त का का साथ साथ कर रहा है। अनुसार को साथ को साथ को साथ को साथ की साथ की साथ की साथ क<br>जनसङ्ख्या



kalendar (\* 1938)<br>1930 - Johann Barnett, frantzistan frantziar<br>1930 - Johann Barnett, ingilariar frantziar

u Sil

The Burger Allen Arthur

 $\Delta\phi\sim 10$ 

 $\label{eq:1} \mathcal{L}^{(2)} = -\mathbf{g}(\mathbf{r}) - \mathbf{g}(\mathbf{r})$ 

Carl Constant

ことがなください マー・アウト

 $\frac{1}{\sqrt{2}}\sum_{i=1}^{n} \frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\left(\frac{1}{\sqrt{2}}\right)^2\left(\frac{1}{\sqrt{2}}\right)^2.$ 

Section.

and the state of the state of the state of the state of the state

 $\label{eq:2.1} \mathcal{L}_{\mathcal{A}}(\mathcal{A})=\mathcal{L}_{\mathcal{A}}(\mathcal{A})=\mathcal{L}_{\mathcal{A}}(\mathcal{A})\mathcal{A}(\mathcal{A}).$ 

过度, 海中建立公司或各地区中心的原来和一个

a provincia de la provincia de

iliya katika 198

 $\mathcal{L}^{\mathcal{L}}$  and  $\mathcal{L}^{\mathcal{L}}$ 

 $\mathcal{L}_\mathbf{z}$  and

 $\frac{1}{k}$  .  $\frac{1}{k}$ 

 $\mathcal{L}(\mathcal{R}_\mathcal{A}) = \mathcal{L}(\mathcal{R}_\mathcal{A})$ 

 $\mathcal{L}_{\text{max}} = \frac{1}{2} \sum_{i=1}^{n} \mathcal{L}_{\text{max}} \left( \mathcal{L}_{\text{max}} \right) \left( \mathcal{L}_{\text{max}} \right)$ 

-44-

## Chapter 3

## STRUCTURES, POINTERS AND SHARING

#### 3.1. Mini-Languages

의원

In this chapter we present a series of mini-languages which treat the issues of structures, pointers and sharin9. The progression of mini-languages is hierarchical in that it starts from a few basic concepts and proceeds outward by extension. Mini-Language 0 is the "kernel" language, isolating the notions of variables, values and assignment. These basic concepts form the core for our domain of discourse. Mini-Language 1 is a direct extension of Mini-Language 0, adding to it structured **values** and the notions of construction of structured objects and selection of components from structures. Mini-Language 2 extends Mini-Language 1 by including pointers and the two operations of building and following pointers. Finally, Mini-Language 3 treats the idea of sharing of components between objects. By revising the concept of structured value found in Mini-Language 1, the notions relating to pointers are subsumed in Mini-Language 3 by notions relating to sharing.

Each mini-language is treated in a separate section of

 $-45-$ 

<sub>的复</sub>路通报 医心中障碍 医心包 医骨髓神经

this chapter. In each section, we first discuss in general terms the concepts addressed by the mini-language under consideration. New terminology is introduced, and we describe the relation to previous and/or succeeding mini-languages. We then supply a BNF-style syntax together with a description of tbe syntacitic classes and What they represent. The semantics of the mini-language is stated informally, a la . . ALGOL 60. We then formalize the semantics by giving samples of rules for translation from the mini-language into the base language BL. Each section is concluded by a "movie" illustrating the interpretation of the  $BL$  program produced by the translator from a sample program in the mini-language.

The final section of this chapter applies these minilanguages to the task of describing the data structuring semantics of "real-world" programming languages. The langUages PAL, QUEST and SNOSOL4 are **uaed aa** examples.

#### 3.2. Mini-Language 0 -- Basics

Mini-Language 0 (ML-0) is the foundation upon which we build our mini-language setup. In introducing the concepts, of value, location and assignment, ML-0 serves as a kernel for our set of mini-languages. The notions of structures,

-46-

pointers and sharing will emerge as extensions to ML-0 in succeeding mini-languages. .<br>1998년 - 대한민국의 대학 대학 대학 대학 대학 대학 대학 대학

All our mini-languages, starting with ML+0, operate within the conceptual world of values stored in locations which we call cells. The relationship between a cell and the value stored in it is called the contents mapping. A 网络花 cell with no value stored in it is said to be empty and has -<br>他は話<sup>1</sup>。 **「不是」の解説「そう」を取得す** no contents. We are concerned here with the fundamental op-医亲麦叶兰白脑 哈隆縣 电分解变换字路下段点 计字符时段 eration of assignment, which is used to change the contents 今日はこままの機動する。長治線に近藤丁目線で絶対の anderman mapping. In fact, the entire purpose in creating ML-0 was ねこ カード・デザー たんだつきする to isolate the concept of assignment by placing it in as minimal and austere a set of surroundings as possible. This notion of assignment will remain unchanged in the remaining mini-languages of this chapter. The assignment statements reportai of these languages will be "consistent" extensions of what 腹位置缺陷的 we define in this section.

Another important concept we deal with here is the notion of binding. Each identifier in an Mi-0 program is associated with a unique and distinct cell. This association is called the binding of an identifier. The value of an identifier will be the contents of the cell to which it is bound. (An identifier bound to an empty cell has no

 $-47-$ 

Al provinciamente inter

認知 小形体

فكالمحرب ال

value.) Unlike the contents mapping, the binding relation ៈកស remains invariant throughout the execution of an ML-0 program. This invariance is a property not only of ML-0, but of all the mini-languages in this thesis.

#### Syntax of ML-0

We give a BNF-style syntax for ML-0. Informal use is made of the ellipsis ("...") to indicate repetition. Two syntactic classes are primitive: (integer) denotes integer constants, and (identifier) denotes alphanumeric strings 经经济改变利润 网络煤焦质混合 starting with a letter. ടാണ് ആളി ചെയ്ത

 $\langle \texttt{assignment} \rangle$ ; ...;  $\langle \texttt{assignment} \rangle$ (program)  $: : =$  $\langle$  assignment) ::=  $\langle$  destination > +  $\langle$  expression >  $\langle$ expression)  $\cdot$   $\cdot$   $\cdot$   $\sim$   $\langle$  destination)  $\mid$   $\langle$   $\langle$  denerator)  $\mid$  nil  $\langle generator \rangle$  :=  $\langle integer \rangle$ 的复数人名法葡梅梅尔法德 不可不可赞 天母的

그 모자들이 나서 달라서 생각하는 것이 나 좋을 때 좋다.

#### Description

To understand assignment, we explain the syntactic classes relating to values and cells. A (generator) is a piece of program text denoting a value. All values in Mi-0 are integers; subsequent mini-languages include other types of values as well. A (destination) is a piece of program text referring to a cell; (destination)s in ML-0 are simply

<u> Alexandro Senador (Alexand</u>

(identifier)s, i.e. variable names. The reserved word nil will be used to signify empty cells. An (expression) is a piece of program text which "yields" a value. The semantic description below discusses evaluation of (expression)s in ML-0.

An ML-0 (program) is simply a sequence of (assignment)s, each of which consists of a (destination) and an (expression). The basic meaning of an  $\langle$  assignment $\rangle$  is to cause the value yielded by the  $\langle$  expression $\rangle$  to be stored into the cell referred to by the (destination).

## Semantics of ML-0 (informal}

1.

The notions we have just introduced will now be made more precise. We give the semantics aasociated with each significant syntactic class of ML-0 (now as a description in English, later more formally via translation into BL).

(1)  $\langle program\rangle s:$  The execution of an ML-0  $\langle program\rangle$ ..-' consists of two steps. First bind each (identifier) occurring in the (program) to a distinct, empty cell. Then execute all of the (assignment)s sequentially, left to right. This rule giving semantics of (program)s will remain intact for all the subsequent mini-languages in this chapter.

 $\label{eq:2} \mathcal{P}(\mathcal{S},\mathcal{P}_{\mathcal{S}}^{\mathcal{A}}) \leq \mathcal{P}(\mathcal{S}_{\mathcal{S}}^{\mathcal{A}}) \leq \mathcal{P}(\mathcal{S}_{\mathcal{S}}^{\mathcal{A}})$ 

(2) <u>(assignment)s</u>: The execution of an (assignment) 的复数强烈的复数形式 经成员 consists of three steps

- (i) Identify the cell referred to by the **(cWatinaticm)** '.can,~,tlle~:~i.~.\_\_. **,INJde,** of 1::he (aaaigmnent) **(see** rule (3) below).
	- (ii) Obtain the value yielded by the (expression}' on the right-hand side (see rule (4) below).

kini mata sungi **kika sagun**an m

 $(iii)$  Make the value from step  $(ii)$  the new contents of the cell from step  $(i)$ . المستوفية والمتركون

Thus the effect of executing an (assignment) is a change in the contents mapping. This rule, like rule (1), will govern the semantics of the remaining mini-languages.

(3)  $\langle destination \rangle$ s and  $\langle identifier \rangle$ s: A  $\langle destination \rangle$ ं कारी गाँगे in ML-0 **is always some** {identifier), **and refers** to the cell bound to this (identifier). Thia binding **is determined** at the beginning of program execution; as we have already said, who go they in good about it remains constant throughout execution.

(4) (expression)s: There are three varieties of " (expression} in ML-0. We describe their **aemantics** in rules 冷な子ど s de la **しょみく (腺帯)と** (5), (6) and (7) below.

(5)  $n$ il: The special symbol  $n$ il indicates the absence of a value. Any time we are directed to store in some cell the value yielded by an (expression) which is  $n$ il, this means to make the cell empty. All of our mini-languages

treat nil in precisely this manner.

(6)  $\langle destination \rangle$ s as  $\langle expression \rangle$ s: When a  $\langle$  destination $\rangle$  occurs as an instance of an  $\langle$  expression $\rangle$   $\langle$  in  $ML-0$ , this means on the right-hand side of an (assignment)), it yields the value contained in the cell to which it refers (see rule (3) above). If this cell is empty, the (expression) is treated like nil (see rule (5) above). This semantic rule (known elsewhere as "dereferencing") will hold verbatim for all our mini-languages.

(7) (generator)s: A (generator) in ML-0 is an (integer), which is the decimal representation of some integer value. It is this value which is vielded by the - şiv (generator).

The above seven rules constitute our informal description of the semantics of ML-0.

#### BL Representation

The semantic rules we just gave are a bit long-winded and imprecise. A rigorous description of the semantics of ML-0 can be obtained by "translating" these rules into BL instruction sequences. Before doing this, we discuss our basic conventions for representing mini-language programs in

the base language model. To each program in one of our mini-languages, there is a single local structure. The cells used by the program are represented by nodes in the looal structure. For each identifier occurring in the program, there is a correspondingly named component of the local structure which gives its binding. In other words, the cell bound to an identifier x will be the x-component acde of the local structure. The contents of this cell is the object of its node. Thus the BL translation of any program in one of our mini-languages will have a "prologue" to bind the identifiers of the program. For example, the prologue for an ML-C (program) whose (identifier)s are x, y and z will be the BL macro-instruction .setl  $(x, y, z)$ , which expands into the sequence create x; create y; create z, creating nodes for the cells bound to these (identifier)s. Integer values are represented in the base language model by elementary objects of type integer.

As for the translation rules themselves, we give sample ML-0 statements ((assignment)s) and the BL code they are translated into. Each example is illustrated by one or two "before and after" pictures showing the change the statement makes in the local structure. Although our examples are

 $-52-$ 

meant to be indicative rather than exhaustive, they should be more than sufficient to give the reader a complete picture of the rules for translation from ML-0 into BL.

There are essentially three kinds of (assignment)s in  $ML-0$ :

 $(1)$  (identifier) +  $n11$ e.g.  $x + \underline{nil}$  is translated into the BL code clear  $x$  (fig. 3.2-1).



海水,于门口一看,<u>家门路的酒香酒</u>是的奶油味,但很好开口。 计程

(2)  $\langle$  identifier  $\rangle$   $\leftarrow$   $\langle$  integer $\rangle$ 

e.g.  $y + 2$  is translated into the BL code

const  $2, y$  (figs.  $3.2-2$  and  $3.2-3$ ).



(3) (identifier)  $\leftarrow$  (identifier)

e.g.  $y \leftarrow x$  is translated into the BL code .call assign0, (x, y). This code invokes a BL procedure named u sbæ

assign0, which performs the operation specified by the ML-0  $9.74$  (1995) 200 (assignment). The definition of the procedure assign0 is shown in figure 3.2-4, and two examples of the ML-0 (assignment)  $y \leftarrow x$  are pictured in figure 3.2-5.



The three translation rules here give us a precise formulation for the semantics of ML-0 in terms of the semantics of the base language model.

#### ML-0 Movie

We conclude this section by giving a sample ML-0 (program) together with its BL translation. Our example is n a mhisteadar an t-网络图 accompanied by a sequence of pictures forming a "movie" to かよこけげぬか デーカー illustrate the changing state of the local structure as the 人名英克 医脑膜炎 医血细胞 医单纯的人 program is interpreted, statement by statement.



3.3. Mini-Language 1 - Structures

Mini-Language 1 (ML-1) adds the notion of data structures to the foundation provided by ML-0. As we have said before, a structure is a data offect which consists of indiv-

 $-55-$ 

ka <del>ka katalog na katalog n</del>

iksigete (Cit

"小陆说,哪里是个做着做家的人的。"《本书本题》,她提醒了。

idually accessible component objects. There are two fundamental operations relating directly to this concept of structures: (1) construction of a structured object whose components will be objects with given values, and (2) selection of component objects from a structure. ML-1 provides for these operations while retaining intact the concepts and mechanisms of ML-0. In particular, the notions of cells, values, contents, binding and assignment are exactly as before.

In addition to the integer values found in ML-0, ML-1 provides a new class of structures. A structured value consists of a sequence of component values (which may be integers or structures). To store away a structured value, we require one cell for the structure, and also separate cells to hold the values of its components. This requirement is a departure from ML-0, in which all cells in use are bound to identifiers. Component cells must now be handled by some kind of free-storage management technique or gell allocator. التفقية والمحالي والأوطول  $\sim p_{\rm max}$  ,  $\sigma_{\rm e}^{\rm h}$ 

In ML-1, a cell may assume successive values of different types (an integer one moment and a structure the next, or vice versa). There are no restrictions on what values

 $-56-$ 

may be stored in which cells. There is a need, however, to detect references to nonexistent components of a structure. Such error-checking will have to be performed by the defining interpreter. ● IP: E → 「 TOP IT D PA」の基本

#### Syntax of ML-1

There is a new primitive syntactic class here, namely (selector), which denotes alphanumeric strings together with integers.

しゃくちょう いっきょう にゅうまく うぎいざい アイチンド

 $\lambda_{\rm eff} = 30 \pm 100$  .



#### Description

Structures in ML-1 are sequences of component values. Each component in a structure has associated with it a (selector). The selection operation gives individual access to the components of a structure by using the (selector)s to indicate the appropriate components. **Thus, for example, the**  $\langle$  selection $\rangle$  a of x refers to the component of the structure x having the (selector) named "a".

 $\label{eq:4} \frac{1}{2}\sum_{i=1}^n\sum_{j=1}^n\frac{1}{2}\sum_{j=1}^n\frac{1}{2}\sum_{j=1}^n\frac{1}{2}\sum_{j=1}^n\frac{1}{2}\sum_{j=1}^n\frac{1}{2}\sum_{j=1}^n\frac{1}{2}\sum_{j=1}^n\frac{1}{2}\sum_{j=1}^n\frac{1}{2}\sum_{j=1}^n\frac{1}{2}\sum_{j=1}^n\frac{1}{2}\sum_{j=1}^n\frac{1}{2}\sum_{j=1}^n\frac{1}{2}\sum_{j=1}^n\frac{1}{2}\sum_{$ 

The notion of (destination) is extended in ML-1 to include selections of component objects from structures. In particular, (selection)s may appear on both sides of (assignment)s. This allows for selective updating of components of a structure. A (selection) occurs as an instance of a (destination) and refers to a component cell for a structure. In this way, ML-1 preserves the ML-0 association between (destination)s and cells.

Also as in ML-0, distinct (destination)s refer to distinct cells. There is no sharing of data.

All values in ML-1 are created by instances of (generator)s. A (construction) is a special kind of (generator) provided by ML-1 for building structured values. In a (construction), we simply supply (expression)s yielding values for the components with the associated (selectors). Each component name/value pair is called a (field). Thus the two kinds of (generator)s, namely (integer)s and (construction)s, produce the two kinds of values in ML-1.

#### Semantics of ML-1 (informal)

**SHOP BREAKERS PERIOD** 

As with ML-0, in order to lend precision to the notions we have introduced, we give an informal description of the

 $-58-$ 

医骨髓中间的 医皮肤病 医不安的 化反应的电阻

semantics associated with each significant syntactic class of ML-1.

(1) {program)s: The semantic rule for an ML-1 {program) is identical to rule (1) in the previous section for ML-0 (program)s.

(2) (assignment)s: ML-1 (assignment)s work by the same principles as in ML-0, but there is a new factor here. Suppose the value yielded by the (expression) on the right-hand side of an (assignment) is some structure. Then new cells must be allocated to store the component values of this structure. The component cells are said to be subordinate to the cell for the structure'they belong to (i.e. to the cell referred to by the (destination) on the left-hand side of the (assignment)). Moreover, if a cell containing a structured value is assigned some new value, then the component cells subordinate to this cell are detached and left for the cell allocator to garbage-collect. Structured values are copied on assignment, component by component (and recursively for structure-valued components).

**(3)** (destination)s: There are two kinds of (destination)s in ML-1. (identifier)s are handled exactly

man ya ku Koshi Ang Milit

I I I I

as in rule (3) for ML-0. We now discuss (selection) s.

(4) (selection)s: A (selection) consists of a (selector) and an (expression). The value yielded by the (expression) (see rule (5) below) is determined. This value must be a structure, or the effect of the (selection) is undefined. Furthermore, this structure must have some component with the given (selector). Finally, this component must be stored in some component cell (which was allocated when the structured value was constructed). Then this component cell is the by the (selection). cell referred to

(5) (expression)s: With respect to the three kinds of (expression)s in ML-1, the occurrence of the indicator nil or of a (destination) is treated exactly as in ML-0. As for (generator)s, the only aspect we need to explain here is the semantic rule for (construction)s.

(6) (construction)s: A (construction) consists of a sequence of (field)s, each with a (selector) and an (expression). Each (field) represents a component with the indicated (selector) and with value yielded by the (expression). The rule for interpretation of a (field)

-60-

#### consists of three steps --

subscription of a second to the complete and the second control of the second control of the second control of

.<br>Sundan Sebagai

 $\Delta_{\rm R}$  .

그 있다

松叶素海岸 201

- Martyrett, with You Instral Andulasi Gau Affal and the confidence that the control (i) Evaluate its  $\langle$  expression $\rangle$ .

(ii) Allocate a new cell and store the value from step (i) in it (the new cell remains empty if step (i) yields no value).

(iii) Associate the mewly allowated component cell (and the value it now contains) with the  $\langle \texttt{selector} \rangle$  of the  $\langle \texttt{field} \rangle$ . The second

The semantic rule for a (construction) is to interpret its  $\langle$  field)s sequentially, left to right, as specified above, This results in a series of component values stored in component cells and accessible by (selector) . . . . . . . . . . . . better know it, a structure. There is one additional restriction on (construction)s: the (selector)s of its (field)s, must be distinct, or else such a (construction) is illegal and has 高单 编立想教 "我的一起,我的人,我的人的女性,他的人,你的心理,可是这样,你们这样 undefined effect.

人名卡格纳 一条建立 计布尔 医魏斯特氏综合征 电超级 计多数 的过去分词 化热力

## BL Representation and the company of the second state of the s

**We represent structures in the BL-6bjects in Wich** the root node corresponds to theseell westere the structure in, and in which the ascs are labeled with the (selectorys of the structure and lead into nodes representing the corresponding component cells. An example we have already seen is the environment (local structure) for a mini-language. program, which is a structured value whose (selector)s are

his an Asperance is the charge of the second state of the context of the context of the

the variables used in the program. Another example is the structure generated by the (construction)  $[a:1; b: [c:2; d:n11]']$ , whose BL rep-

resentation is pictured in fig. 3.3-1.

A valid ML-1 (destination) corresponds to a node addressable by a compound pathname. For instance, if the structured value of figure 3.3-1 is



assigned to the (identifier) x, then the cell referred to by the (destination) c of b of x will be represented by the node x.b.c.

As with ML-0, a ML-1 (program) whose (identifier)s are  $x1$ , ..., xn has in its BL translation the proloque setl (x1, ..., xn). We now treat translation of various ML-1 (assignment)s into BL, illustrating general translation techniques that can be readily applied to any M1-I statement. The following cases are representative:

(1) (identifier)  $\leftarrow$  nil

 $(2)$  (identifier) + (integer) and

are both handled exactly as in ML-0 by the respective BL primitives clear and const. Note that the action of these BL instructions disconnects any subordinate component cells

that need to be detached.

어머니 한 시장 전 개

ા આવ્યક પશુપ

(3) (identifier)  $\leftarrow$  (identifier)

المحروم والمحافظ والأراد والمحرومية

e.g.  $y \leftarrow x$ . This kind of ML-1 (assignment) poses a problem in translation when the source (expression) x has a structured value. In that **case, the** structured value for x.must be copied component by component into y, creating new cells as required to hold new components of  $y$ . This kind of



action is illustrated in figure 3.2-2. We shall translate the  $\langle$ assignment $\rangle$  y + x as a call on a BL pro**cedure** named assign!, so the BL code for the **etatenaent** y ~ x will

be .call assignl,  $(x,y)$ . The code for the BL procedure assignl is shown in figure 3.3-3. If x is empty or has an integer value, then **usignl works like tne·aasignO** procedure which translates the corresponding ML-0 (assignment). If x has a structured value, then for **each component** of **x**, we generate a corresponding component for **y** (allocating a new cell) and call assignl recursively to give this component

of y the proper value. Here, the parameter u corresponds



to x, and the parameter v corresponds to y.

 $(4)$  (identifier) + (selection)

e.g.  $y \in b$  of x.

The pitfall here is that we must check to verify that x indeed has a b-component. The following BL code takes care of this test:

has? x, b, error .call assignl,  $(x.b,y)$ 



The label "error" refers to some unspecified place we branch to if x has no b-component.

(5) (selection)  $\leftarrow$  (identifier)

e.g. c of a of y + x is translated into the BL code has? y,a,error has? y.a,c,error . call assignl, (x,y.a.c) (figure 3.3-5) •

 $(6)$  (identifier)  $\leftarrow$  (construction) e.g.  $y \leftarrow [a:3; b:nil; c:x]$  translates into clear y const 3,y.a clear y.b  $\text{.call assignl}, (x, y, c)$  (figure 3.3-6).





There is a subtle pitfall in these translations. Special care must be taken in translating (assignment)s in which the left-hand side and the right-hand side both refer to

cells in the same structure. **Suppose,** for example, that y has the structured value depicted in figure 3.3-7. Translating the (assignment) b <u>of</u> y + y into the BL code<br>has? y,b,error . <br>will not vield the correct r .call assignl, (y,y.b) will not yield the correct results of figure 3.3-8. Instead, there would be a nonterminating sequence of recursive calls of the procedure assignl (figure 3.3-9). **We must therefore translate the** 



has? y,b,error

.call assignl, (y, \$temp)

.call **assignl,** (\$temp,y~b)

With this translation, the recursion terminates because we are not updating the structure. \$temp during the process of recursively going through its components.

For other cases of "overlapping" assignment, we adopt

similar translations. For example, we translate the  $\langle$  assignment):  $y \leftarrow [\alpha:1; b:y]$  into the BL code .call assignl, (y, \$temp) clear y const  $l$ ,  $y$ . a .call assignI, (\$temp, y.b); and we translate  $y \leftarrow [$  c:a of y ] into has? y, a, error clear \$temp  $link$  \$temp,  $q$ ,  $y$ ,  $a$ clear y  $\sim$   $\sim$ .call assignl,  $(\text{stem}, q, y, c)$ .

Note that in ML-1, the translator can detect any occurrences of these "overlapping" assignments and make the according adjustments.

ML-1 Movie

 $x + 4$ ;

 $ML-1$ 

As in the previous section, we conclude with a movie of a sample ML-1 (program) and its translation into BL.

## $BL$

.setl  $(x, y)$ const  $4/x$  $y \in [a:2; b:x; c:nil]$ : clear y const 2, y.a .call assignl,  $(x, y, b)$ 

clear y.c

en de la completa de la producción de la completa de completa de la producción de la completa de la completa d<br>Completa de la completa de la compl

والمستوقف والمسارق المتحرم والحامل والمحافظة



849.LT

 $2: [r:min; s:4]$ ;

 $-68-$ 

## $s$  of  $2$  of  $y + a$  of  $x$ ;

 $c \underline{of} x + x$ 

has? y, a, error .call assignl, (y.a.x) has? y, a, error const 3,y.a .call assignl,  $(y, x)$ clear y has? x, a, error .call assignl, (x.a, y.l) clear  $y.2$  $\sim 100$ clear y.2.r const  $4, y.2.8$  $h$ as?  $y$ , 2, error  $has 2 \, y, 2, s$ , error

**BL** 

- has? x, a, error
- .call  $\overline{a}$ ssignl,  $(x.a,y.2.s)$
- has? x,c,error
- .call assignl, (x, \$temp)
- .call assignl, (\$temp, x.c)







## 3.4. Mini-Language 2 -- Pointers

Mini-Language 2 (ML-2) extends the concepts we have developed and treats the notion of pointers (references). A pointer is a means by which one can' indirectly access a cell and its contents. As with structures, there are two basic operations inherent in the concept of pointers: (1) creation of a pointer value which refers to a given cell, and (2) accessing the cell a pointer "points" to. We wish to

provide for these operations while preserving the concepts and mechanisms that have already been developed in this chapter.

In ML-2, there is a new class of pointer values. As with ML-1. cells can accommodate successive values of different classes. We will not, however, allow indirect references through values which are not pointers.

One respect in which the notion of pointer differs from previous concepts is that a pointer value contains information about the cell it refers to. Previous concepts of value had nothing to do with cells. We shall see some of the difficulties caused by this extension.

In this section, we treat ML-2 as an extension of ML-1. However, it is not necessary to include structures in order to hundle the new notion of pointers. One could alternatively ondt structures from ML-2 and view it as a direct extension to ML-0.  $\{x_1,\ldots,x_n\}$  ,  $\{x_1,\ldots,x_n\}$ 

#### Syntax of ML-2

The "boxed" portion of the ML-2 syntax is that part of ML-2 that deals with structured values and the basic operations on them.

o pro stato di padde possibili possibili si se se se della participa di partiti di secondo di partiti di finan



#### Description

There are two new syntactic classes in ML-2.  $\mathbf{A}$ ಾತ್ಮಮೀಟಿ ಡಿ.(ಡೆ. (pointer), consisting of the symbol ptr and a (destination), 以平衡的成功 specifies the creation of a pointer value which will refer to the same cell as the (destination). The only way to build pointer values in ML-2 is by means of (pointer)s; we therefore classify the (pointer) syntactically as an instance of a (generator). An (indirect), consisting of the symbol val and a (pointer-valued) (expression), is ML-2's way of accessing the cell referred to by a pointer value. As such, an (indirect) is a kind of (destination).

医红 计混合语句解语词

りにん あざまもあかしあしい めいね キンロー We have already seen all the other ML-2 syntax classes. 道长 网络以下线

ing tigap aya kara

 $-71-$ 

### Semantics of ML-2 (informal)

All we need to give here are informal semantic rules corresponding to the two new syntactic classes. All the other semantic rules for ML-2 are identical to the corresponding rules for ML-0 or ML-1.

(1) (pointer)s: This kind of (expression) contains a (destination) and vields a pointer value which refers to the same cell as the (destination).

(2)  $\langle$  indirect > s: An  $\langle$  indirect > contains an  $\langle$  expression >. The value yielded by the (expression) is determined. If it isn't a pointer, the (indirect) has undefined value. Otherwise the (indirect) specifies the cell referred to by this pointer value.

#### BL Representation

Deciding on a way to represent pointer values in BL presents difficulties. In most conventional systems, pointer values are simply the numeric addresses of cells. However, in the base language model, referencing of cells is symbolic. The most straightforward approach to this problem is to view a cell's pathname (i.e. sequence of selectors from the root node of the current local structure) as its

-72⊷∴
address. A pointer value would then be represented in the base language model by an elementary string value encoding the pathname of the cell pointed to. Under such a scheme,

after executing the ML-2 instructions

 $x + 3$ ;  $y + ptx$ ;  $z + y$ ;  $w + val y$ the environment would appear as in figure 3.4-1. After the further instructions

 $z \leftarrow x$ ; val  $y \leftarrow ptr z$ 

are executed, the environment would then appear as in figure 3.4-2. Under such a scheme, translation into BL would not be difficult. However, this approach breaks down in the presence of structures. For

example, execution of the sequence of **ML-2** instructions

be inaccessible through y. In other words, under this

 $x \leftarrow [a:2]$ ;  $y \leftarrow ptr$  a of x would result in y having as value the pathname "x.a" (figure 3.4-3). If we then execute the (assignment)  $x + 3$ , x would no longer have an a-component; the cell containing the value 2 would therefore no longer have the pathname x.a and would hence







scheme there is no way to provide for retention of cells referred to by pointers. The main conceptual weakness of this scheme is that the address of a cell depends on a par ticular path of access to it. Such a dependence is to be  $^\dagger$ avoided.

*<sup>A</sup>*second way to refer to a cell is by directly linking to it, that is, sharing it. It is imperative that the pointer have a separate cell for itself as well as the cell it points to. Otherwise, after executing the ML-2 instructions  $x \leftarrow 3$ ;  $y \leftarrow ptx$  x we would have a situation as pictured in figure  $3.4-4$  in which the (assignment)  $y + 2$  would erroneously affect x (we want to access x  $3.4 - 4$ Fig. through y only by use of the (indirect)

 $val(y)$ . To insure separate cells, we will make a pointer value an instance of a structure, where the cell pointed to

will be the sole component cell. Thus

the result of executing the instructions

 $x \in [a:2]$ ;  $y \in ptr$  a of x

will be as in figure 3.4-5, and after the further instruction  $x + 3$ , we see that the cell containing the value 2 is proper-





ly retained (figure 3.4-6). Note that we have adopted the reserved name "\$val" as the selector for the single component of ' an ML-2 pointer value under our representation scheme (to avoid clashes with the  $\langle selector\rangle s$  of ML-2 structures).



Now that we have settled on a BL representation for pointer values, translation of  $ML/2$  into BL is straightforward. We only need consider four new cases of (assignment)s:

(1)  $\langle$  identifier $\rangle$   $\leftrightarrow$   $\langle$  pointer $\rangle$ 

e.g.  $y \leftarrow ptr$  x is translated into the BL code clear y link y, \$val, x

(2) (identifier)  $\leftarrow$  (identifier)

e.g.  $y + x$  is translated into the invocation .call assign2,  $(x,y)$ , where the dafinition, of the BL procedure assign2 is shown in figure  $3.4-7$ . The difference between assignl and assign2 is that assign2 has additional code to handle assignment of pointer values, preventing us from attempting to copy the contents of a cell referred to by some pointer. An example of the assigning of a pointer value is depicted in figure 3.4-8.



 $\mathcal{F}_{\mathbf{A}}(\mathbf{z},\mathbf{z})$  is not be  $\mathcal{F}$ Fig. 3.4-8. Effect of the ML-2 (assignment)  $y + x$  when  $x$  has a pointer value.

 $(3)$  (identifier) + (indirect)

 $z \leftrightarrow y \rightarrow y$ is translated into the BL code  $e.g.$ 

 $7.853.8$ 

display your

e i dwy iv

has? y, \$val, error

.call  $assign2, (y, $val, z)$ 

and a state of the company of the second and the company of the first product of the company of the company of

(4)  $\langle$  indirect  $\rangle$  +  $\langle$  expression  $\rangle$ 

e.g. val  $x + 3$ is translated into the BL code has? x, \$val, error const 3, x. \$val

Using these translation schemes, it is easy to produce BL code corresponding to any ML-2 (program). However, the presence of "overlapping" assignments can no longer dlways be detected by the translator. For example, in the state ত হ'ব উহস্ depicted in figure  $3.4-9$ , we want the (assignment)

b of  $y \leftarrow y$  al x to result in the state shown in figure  $3.4 - 10.$ The BL code



other words, the trans- \*

lator must produce BL code to perform extra copying whenever there is a possibility of overlap. This is a major source of inefficiency, since overlep is probably an infrequent event.

ML-2 Movie

 $ML-2$ 

 $x \leftarrow [\n a:4; b:nil]$ 

 $y$  + ptr b of x;

 $val  $y + 5$ ;$ </u>

 $b \nsubseteq f \times \bullet 6;$ 

 $x + z$ 

 $z \leftarrow$  [ c:y; d:yal y; e:ptr z ];

**BL** 7377843 .setl  $(x,y,z)$ clear x  $const$  4,  $x$  .  $a$ clear x.b has? x, b, error clear y link y, \*val, x.b has2 y Sval error const 5, y. \$val has? y, \$val, error .call assign?, (y. \$val, \$temp) clear z .call assign2,  $(y, z, c)$ .call assign2, (\$temp, z.d) link z.e. \$val?z has? x, b, error  $const$   $6, x.$ b

(在本) (1947年12月)

 $\mathcal{J} \in \mathcal{I}$ 

 $22.3647$ 

 $-78-$ 

.call assign2,  $(z, x)$ 





### 3.5. Mini-Language 3 -- Sharing

So far in this chapter, we have progressed through three mini-languages in developing our semantic model for data structures and pointers. Although ML-2 handles all of 들렸 these concepts, there are some respects in which the design we so carefully built up becomes cumbersome and inelegant. In this section we shall look at some of the weaknesses of ML-2 and see how they reflect a conceptual shortcoming in

our design. The mini-language ML-3 is devised to remedy these deficiencies. By revising the notion of structures, ML-3 becomes not only more powerful and efficient than ML-2, but conceptually simpler as well. In fact, the entire apparatus of pointers that was developed in the previous section is subsumed within the re-definition of structured value.

The main difficulty with ML-2 emerges when we consider the way pointer values are represented in the base language model. This is admittedly a rather strange way to examine the merits of a language, namely in terms of a representation decision with respect to a particular semantic model. But the base language model is special in that it was specifically designed for the purpose of describing the concepts of sharing which we are studying. So it is perfectly valid to use insights provided by this model to aid in designing mini-languages which deal with data structures and sharing.

In the last section, we chose to represent a pointer value in the base language model as a one-component structure whose component cell is precisely the cell pointed to. In other words, pointer values are instances of structures

-80-

whose components share with other data objects. It is this much more general concept of shared **data** objects that concerns us in this section. The only kind of sharing provided in ML-2 is the pointer, which is a structure having exactly one component cell, shared with some object. In the course of trying to model aspects of real-world programming languages in ML-2, this limitation becomes a stumbling block. For example, the notion of tuple in languages like BASEL is that I, of a vector of addresses, i.e. a structure with an arbitrary number of components sharing with other objects. In ML-2, this can be modeled only as a structure whose components are pointers. These components, when represented in the base language model, take up an extra level of indirection, which becomes a bit clumsy. 1000000

To give a better treatment to this generalized notion of sharing, we revise our concept of structure. In ML-2, as  $\sim$ in ML-1, the notion of structured values as being composed of components with (selector)s and values does not directly utilize the concept of cells. Cells are part of only pointer values. What we've done in ML-2 is represent, pointers like structures but use a different setpef rules to manipulate them. This conceptual distinction puts the two

एका अनुसार संस्कृत सम्बद्ध के लिए स्थिति

きんきゅう しょうしゅんしょうかい しょうしょう こうこうしゅう

notions -- structured values and pointer values -- almost at odds with each other in ML-2. We include cells in our revised concept of structured values in ML-3; as a result of this, the need for a separate class of pointer values vanishes.

A structured value in ML-1 and in ML-2 was a collection of components, each consisting of a value and an associated (selector). In ML-3, we define a component of a structure to now be a (selector)-cell pair, rather than a (selector)value pair. The value of a structured object is still the set of its components.

# Syntax of ML-3



### Description

The syntactic classes of ML-3 are identical to those of ML-1, with two additions. First, there are now two kinds of expressions in ML-3: an (expr) yields a value, and a (cell expr) yields a cell. The only occurrence of  $\langle$  cell expr $\rangle$ s is within the  $\langle$  field $\rangle$ s of a  $\langle$  construction $\rangle$ - 海緑は、香山にんぷり降き変は輝く、枯ら、青緑色標。 (where there used to be (expr)s in ML-1 and ML-2). **The** rules for evaluating both kinds of expressions are given 医次 骨数料件 나치 마음 출장 below. The second addition is a new kind of (expr), namely the (modification) which yields structured objects built from other structures. All other syntactic classes are exactly as they were in ML-1.

# Semantics of ML-3 (informal)

The semantic rules for (program)s, (assignment)s,  $\langle$  destination $\rangle$ s,  $\langle$  identifier $\rangle$ s and  $\langle$  selection $\rangle$ s are identical to the rules given for ML-1. The remaining elements warrant some discussion.

白色の かるねえげる まいりょうのう 薬のない

(1)  $\langle \text{expr}\rangle$ s: The occurrence of nil or of a (destination) as an (expr) is handled just as in ML-0 and ML-1. (generator)s are either (integer)s, which are handled as before, or (construction)s, which are described in

「この行政者はちゃ」 とうどう とうしんせいどう

アーティッチ ぬり しゅんかいそうかん

rule (2) below. (modification)s are discussed in rule (6) below.

(2) (construction)s: The semantics of (constructions) and (field)s follows directly from the new ML-3 notion of structures. A (construction) denotes the value of a structure which is generated on the spot. A (construction) consists of a series of (field)s, each with a (selector) and <sup>a</sup> (cell expr). Each (field) represents a component consisting of this (selector) and the cell yielded by the (cell expr) (see rule (3) below). Finally, the structured value yielded by the (construction) is the set of components given by its (field)s. We make one restriction on (construction)s: the (selector)s of its (field)s must be distinct, or else the (construction) is invalid and has undefined effect.

(3) (cell expr)s: The two kinds of (cell expr) are discussed in rules (4) and (5) below.

(4) shared (destination)s: A (cell expr) of the form share (destination) yields the cell referred to by the (destination). This is the basic source of sharing in ML-3; shared (destination)s are used to build structures **having**  components whose cells are already in use. It is this facility which subsumes the ML-2 notion of pointers.

(5)  $\langle \text{expr} \rangle$ s as  $\langle \text{cell} \text{expr} \rangle$ s: The cell yielded by an (expr) occurring as a (cell expr) *is* a newly-allocated cell distinct from all cells *in* use and containing the value yielded by the  $\langle \text{expr} \rangle$ . Evaluation of a  $\langle \text{cell expr} \rangle$  of form (expr) *is* the only way to allocate new cells *in* ML-3.

(6) (modification)s: A (modification) consists of a  $\langle$  construction $\rangle$  and an  $\langle$  expr $\rangle$ . The value of the  $\langle$  expr $\rangle$ (which we call the modificand) must be a structure or the indicator nil, or else the effect of the (modification) *is*  undefined. The value yielded by the (modification) will be a newly-generated structure whose components are obtained as follows:

- (i) Each component of the modificand whose (selector) belongs to no (field) of the (construction) will be a component of the new structure.
- (ii) For each (field) of the (construction) there will be in the new structure a component with the same (selector) and as its cell the cell yielded by the (cell expr) of the (field).

Alternatively, we can view each (field) of the (construction) as either replacing or appending a component to the modificand depending on whether or not its (selector) belongs to some component of the modificand. Note that evaluation of a (modification) may cause allocation of new cells, but it

-85-

(5) <u>(expr)s as (cell expr)s</u>: The cell yielded by an does not in any way affect the contents of existing cells. (expr) occurring as a (cell expr) is a newly-allocated mell Strictly speaking, (modification)s are redundant in ML-3. distinct from all gells in use and containing the value If, for example, the (identifier) x has a structured value yielded by the (expr). Evaluation of a (cell expr) of form with two components whose (selector)s are a and b, then the  $U_{\rm C}$  . Is the only way to allocate new cells in Mi-3.

 $(modification)$  [b:3; c:share y] x will yield the same value

as the construction, a linguide a signification) (3).

Gonstructions and an fexpry. The value of the (expry BL Representation

(which we call the modificand) must be a structure or the

We represent a structured value in ML-3 by a BLTObject whose arcs lead into the nodes for the component cells and are labeled with the corresponding (selector)s. This is a

.awolfol:

straightforward, simple and clean.

We pow give assess that is a miss (assignment) s (selector, belongs to no (field) of the into Ble to inencamos a possible decidentado o shopped web

stad**el (Aidentister) es<u>nir</u>e (Assala**tion 1999) 41 iw dnezogstoo's etooputos well som die 114 and ( 12) of identifier but Kinteger) iss sense suit

yfeldad by che (cell'expr) of the (field). are both handled as in ML-0 and ML-1. Alternstively, we can view each (field) of the communication)

(3) (identifier) + (identifier)<br>a line of the discograph a papproced as the last regiin as

e.g. y + x is translated into .call assign3, (M.X) . Where the BL procedure assign3 is defined in figure 3.5-demographene code is the same as for the procedure assignl for empty and integer values of the source (identifier) x, except for the

the presence of the same? x,y, out test which makes sure the (assignment) is nontrivial (otherwise the clear instruction would destroy the value we want to keep). If  $x$ has a structured value, then y will get the same structured value. This means, by the new definition of structured value, that the components of y will now share with the components of x (figure 3.5-2). In executing any (assignment),



that this is a vast gain in efficiency for ML-3 over ML-1 and ML-2. The "meaning" of the (assignment)  $y \leftarrow x$ , then, differs between ML-1 and ML-3. For **example,** after executing

2000年1月10日1月1日 1月1日

unis (generalis en la la especient anno 199

roch keigde doktho labi duoly, <u>Solika</u> ody in aymetro otr the instructions  $x + [a:3; b:4]$ ;  $y + x$ ; a of  $y + 5$ , the fassignmently is nontrivitely (chhanwise cho of the trans then the expression a of x will yield the value 3 in ML-1 application would comment the visible vant to able to keep in the (and ML-2), but will evaluate to 5 in ML-3. r till hans for meddel till fra List og finde for till for till till till till t

地理系统 医甲状腺炎 人名英法拉伯

(4)  $\langle$  identifier) +  $\langle$  selection) irojnda ∄o *nos* 

e.g. y b of x is translated into the BL code ... . . . . has? x, b, error drooks at the soul because in the conservation of the second  $\texttt{.call assignment}$ ,  $(x.b,y)$ 

(5) (selection) + (identifier) 33.875.20 a Mareka a  $\mathfrak{g} f^* \overline{V} + \mathfrak{F}$  is translated into the BL code  $e.g.$ 梦。 在那场走货 has? yva.error SOOM STATERIAL  $-$ 0211  $-$ 282492 $\mathcal{Q}(\mathcal{L}_V(\mathcal{A})\)$ ານລາເລືອ*∖ນ* (ທຣ.)  $(6)$  (identifier) + (construction) = sace

Lamougass) C-IM sda e.g.  $y \leftarrow \{\varphi_{\beta} x : d : b \varphi f(x) \text{ e} : \text{share } x \}$  is translated into 而释放了功 まいじょましび 150.0% *auter Gaindoprit* has? x,b, error どおき

.call assign3, (x.b, clear y of film time wife .call assign3,  $(x, y, c)$ Ø 0 .call assigns, (stemp, <u>galaya (</u>y.d)<br>Tinakari 100 kata ta Fig. 3.5-3. Effect of  $y + [c:x; d:b of x; e: share z]$  $\lim k$  y,e,  $z$ desvik et zir  $in M<sub>b</sub>+3$ is the same health and somet

Note that overlapping (assignment)s pose no problem at all<br>policies and the oldsse to the source of the section at all for statements of types (4) and (5). This is due to the

menter a los los distanciones se el controlario de la contra de la contra

fact that component cells of a structure are no longer copied on assignment. However, we do need the use of temporaries in (assignment)s involving (construction)s, for instance, to take care of the case when *y* shares with b of x before executing the  $\langle$  assignment $\rangle$  in example  $(6)$ above.

Finally, we note that pointers in ML-2 have been subsumed in ML-3. In place of the ML-2 ptr (destination) we can write the ML-3 (construction) [val:share (destination)], and wherever ML-2 uses val (expr), ML-3 substitutes val of  $\langle$  expr $\rangle$ .

ML-3 Movie





### $ML-3$   $BL$

 $\underline{\text{rk}}$  y,p,x  $\underline{\text{rk}}$ all  $assign3, (y,y.p)$  $y^2$  z,b,error all  $\texttt{assign3, (z.b.y)}$  $x+1$  assign3,  $(z, x)$  $st$  5, $x.b$  $\frac{3?}{16}$  y, q, error<br> $\frac{1}{2}$  z, c, y, q<br> $\frac{3?}{16}$  z, b, error z, b, error 11 assign3, (z.b, \$temp) .call  $assign3, (x, y)$ .call assign3, (\$temp,y.a)  $link$   $y, c, z$ 







"'

-90-



3.6. Discussion and Examples

In this chapter we have built up a hierarchy of minilanguages, culminating in ML-3. We now relate this development to the main issues that were raised in Chapter 1. A. major concern with respect to a given "real-world" programming language is the effect of its assignment operation on an environment containing structured data objects. We know

ไม่อย่างและเป็นอย่างส่วนที่ ออกและเป็นอยู่หลายเป็นอย่าง คือ ครั้ง คือ ครั้ง ครั้ง ครั้ง ครั้ง ครั้ง ครั้ง ครั้

 $-91-$ 

that executing an assignment statement of the form  $X := e$ will result in the identifier X having the value associated with the expression e. What is uncertain is the effect of such an assignment upon the sharing relationships among the various cells in the environment. Variations in sharing properties can in general induce differences in the effect. of subsequent assignments.

We give an example adapted from [Bur 68]. The only data structures in the environment will be LIBP-like lists with two components selected by the respective selectors head and tail. Burstall compares analogous programs in two lanquages: List-Algol, which combines ALGOL 60 assignment with structures essentially equivalent to LISP lists, and ISWIM ("If you See What I Mean"), which is based on the same functional lambda-calculus notions as LISP. In both languages, the two-argument function cons returns a list whose head is the first argument and whose tail as the second argument; the functions head and tail select the components from a list. Burstalle two programs are shown in figure 3.6-1. Program A, we are told, sprints 3 while program B prints 1 "since it does not cater for the side effect on y of the assignment to x." This explanation gives little insight

 $-92-$ 

into why there should be such a difference in the first place. The obvious distinction between the two programs



lies in line 4. ISWIM, being a functional applicative lanquage, has no direct counterpart to the List-Algol component "女人最好美国,就给这就给我们,再经过。" 电最高级转移器 update statement HEAD(x) := 3. But this is not the root of 当時の一回会に「このあり通事機関」をいいの the semantic difference between the two programs. Burstall a Jard Rogelyrdiga, italien neglects to say that even if we change line 4 in Program A presented with a reported to to  $x := \text{CONS}(3, \text{TAIL}(x))$ , Program A will still print 3.

టి అత్య తేషారు

The source of the trouble lies in a subtle difference between the cons functions in the two languages. We can pinpoint the distinction by translating both programs into ML-3. Line 2 in both programs can be translated into.  $x \leftarrow$  [ head: 1; tail: nil ], with the resulting environment as in figure 3.6-2. Line 3 in Program A is nouivalent to the

e e a seriest**a chantai** 

at possible da presenta santa controll**ado financiales** to felicidade

ML-3 statement  $y \leftarrow +$  head: 2; tail: share w 4% while line 3. in Program B is equivalent to  $y \leftarrow$  [ head: 2; tail: x ]. The respective results are shown in fligures 3.6-3 and 3.6-4.



Provident Report Finally, the revised line 4 for Program A, which reads しんしゃそう 利息の残忍の強い しょとねんえい かいこうかい fan Bergen しゃくしゃ しゅうしょう  $x = \text{CONS}(3, \text{TAIL}(x))$ , is equivalent to the ML-3 statement TAGET IN ALSO AN ANY MONEY OF A SALE REPORT OF A STRONG AND THE REPORT OF A STRONG AND THE REPORT OF A STRONG AND A  $x \leftarrow$  [ head: 3; tail: share tail of x ], while line 4 of Pros pall etgda myök maa dud von 10 alut 1 rizatuan ing ka gram B is equivalent to  $x \leftarrow$  [ head: 3; tail: tail of x ]. tê de li dinav tê kompêxwera di Adolf Mariz (1891) wa (分类型) The respective results are shown in figures 3.6-5 and 3.6-6.



of ABI control of the Annual School

 $-94-$ 

We can see that the ML-3 expression head of tail of y yields 3 in figure 3.6-5 and 1 in figure 3.6-6.

A STORE AND COMPANY OF THE STORE STORE AND THE STORE OF THE STORE AND THE STORE TO THE COMPANY OF THE STORE OF

**NO. ROSA PROPERTY** 

The difference between the two cons functions in Burstall's two languages should now be clear. If an argument to cons is a constant or nil, both languages specify allocation of a new cell to contain the argument value. But if an argument is some identifier, the Lisp-Algol CONS yields for the corresponding component the argument's location, while the ISWIM cons yields the argument's value. This property of the ISWIM cons function is not explicitly stated in Landin's descriptions of ISWIM [Lan 64, Lan 65, Lan 66a]. In fact, the only place from which this property could be readily ascertained was in Burstall's statement that Program B prints the value 1. The ML-3 code into which we translated the statements of the two programs was determined only from the stated results of those programs. What is to be concluded from this is not that Landin was sloppy or vague in his language design and definition, but rather that the language definition methods which are so widely used make it extremely difficult to extract some of the properties of significant practical importance. In other words, a lanquage which features data structures will be better under-

stood and better specified if it defines these facilities in some manner which makes clear the specific sharing relationships among locations.

In the remainder of this section we shall use our minilanguages to talk about the data structuring facilities ana mechanisms of several additional programming languages.

#### PAL

The language PAL [Ev 70] supports only one kind of data structure: the tuple. A tuple is a structure whose selectors are consecutive integers starting with 1. As with ML-3, the cell in which a component of a tuple is stored is considered an integral part of the value of the tuple. The PAL expression 4,5,6 specifies the construction of a tuple whose components have the respective values  $4,5$ , and 6; as such, it is equivalent to the ML-3 (construction)  $[1:4; 2:5; 3:6]$ . Selection in PAL is expressed by  $j$ uxta<sup>1</sup> position; if the tuple value 4,5,6 is assigned to the variable x, then the PAL expression x 2 evaluates to 5 (it selects the second component). This expression corresponds to the ML-3 (selection) 2 of x. The correspondences we have established are summarized in figure 3.6-7.

The concepts of value of a tuple in PAL and value of a .<br>1974 BAC SEMISTE ing kalima structure in ML-3 are very close, and we might expect simila si vijetlat∪ lar assignments to behave similarly. This is indeed the i,n/jessauko San Britain

case, as figure 3.6-8 confirms. of the life show of most (Ishi and shown)



PAL has a semantic rule that components of a tuple share with the items in the list expression that constructs it; an example of this rule is shown in figure 3.6-9. This sharing can be blocked using the PAL unshare operator ("\$"). Figure 3.6-10 gives an example of this.



医马克氏病 化二乙烯基乙烯酸 医马耳二氏试验检尿道 医心包 医阿斯特氏病 医中间性 医中间

 $-97-$ 

we discuss one more feature of PAL: the aug function. If t is an n-tuple (i.e. tuple with selectors  $1, 2, \ldots, n$ ) and e is any expression, then the PAL expression  $t$  aug  $e$ denotes an (n+l)-tuple whose first n components share with the components of  $t$ , and whose  $(n+1)$ -st component shares withe. Examples are shown in figures 3.6.11 and 3.6.12.

x := nil aug 3; <u>| PAI</u><br>y := nil **au**g x **X** + [1:3] <u>nil</u>; 1 i **X** .. [l:3] nil; d) y +- r1:share x] nll --- Pig. 3.6-11. Example of the use of the PAL function aug



The above features illustrate nearly all of PAL's data structuring capabilities, and they are easily expressed in ML-3. Even though the data-structure facilities of PAL bear a strong resemblance to ML-3, we have given a demonstration of

a full-scale, real-world programming language whose data structuring mechanisms have been successfully treated within our model. We discuss two more languages. 医外侧骨缝术 医血

**QUEST** 

The language QUEST [Fenn 73] provides data structures called lists that appear very much like PAL's tuples (see figure 3.6-13). However, the definition of assignment in **QUEST treats lists as** 



different properties of

special cases for which special rules apply. This reduces, essentially, to a treatment of lists in the way

标题, "国内、流程之类

ML-1 treats structures. Component values are copied on assignment rather than shared. Figure 3.6-14 presents an example. Note that componentwise copying is coded in ML-3



by repeated component updates, reflecting a lack of efficiency. QUEST assignments, unlike their counterparts in PAL, cannot be directly translated into ML-3 without knowing runtime values (i.e. exactly what components a structured value possesses at any given time, so they can be individually updated). ander an Fra

Like ML-2, QUEST handles sharing entirely by means of pointers (called references). Their use is illustrated in figure 3.6-15. There is no appreciable difference between the behavior of these pointers and those in ML-2. Translation into ML-3 would and the second state be trivially easy.



For the interested reader, the paper on QUEST [Fenn 73] specifies a way to express general ML-3-like structures in QUEST using lists and references. QUEST functions cons, car and cdr are defined, and it is claimed that they simulate their LISP counterparts. The simulation requires an extra level of indirection throughout, a major inefficiency (fig. 3.6-16). Thus we see that using our mini-languages, we have not only able to illustrate the data structuring semantics t Latin meachd dibu gro-chron mag mag Fanish Litter to Roll. of QUEST, but we have also perceived a shortcoming in the design of QUEST: like ML-2, QUEST fails to recognize the fundamental significance of the concept of sharing.



#### SNOBOL4

In the language SNOBOL4 [Gris 71], one finds data structures called "programmer-defined data types." An invocation of the function DATA causes selector and constructor functions to be defined. For example, the invocation DATA ('COMPLEX(R, I)') defines the constructor function 28. 2011年8月28日的大西方人民的研究教授者教授教授研究所的。 COMPLEX and the associated selector functions R and I, The process and of the Children badder for t setting up the correspondence depicted in figure 3.6-17. Beyond this aspect, in which these SNOBOL structures behave 化三氯化三氯甲基乙酸 医副腹膜炎 经按照 医红细胞 医单元 医单元化 exactly as do all the structures we have seen in other "一个孩子。" "好,你你喜欢出好嘛!"的母人说糊涂的被被骗弄到了一个地

- 日報主張の場合 2015年11月

ြေအတွင်း သမင်းသမင်းမှာ အဖွဲ့ပါး မြင်းများကို သ

phitupopusa adab edi sitettätuli urgalds vincolos. languages, the sharing relationships need to be considered. of ONEST, But we have also perceived a shortcoming in the



temper (1:5;2:1) - (free val) But semantic rules which would elahorate on such, properties are not to be found, instead, all that can be seen are a few examples. As with faring, careful examination of the exam-Fig. 3.5-16. QUEST Simulation of ITSP coor

ples is required to produce a consistent and unambiguous ML-3 representation for the data structuring facilities of Some detective work is needed here as well: SNOROL4. each of the two books [Gris 71, Gris 73] provides insufficient information to make such a determination, but using both together, enough clues can be gathered to resolve possible ambiguities. The eigenexe to a benited ad of anoitonul not

DATA (COMPLEX  $(R,1)$  ') defines the constructor function The translation into ML-3 may be straightforward, but a COMPLEX and the associated selector functions R and number of other possible translations which would result in setting up the correspondence depicted in figure 3.8 different sharing properties were ruled out only after seyond this aspect, in which these SWOBOL structures. painstaking examination of the examples in both books. exactly as do all the structures we have seen in tthe Surely a discussion of sharing in these books could have

-101-

shed much-needed light on the semantics of data structures AN HEALT BOOK AND UNGE GAT THROUGH HAT A MODEL in SNOBOL4.



#### Completeness of the state and that is a streament of the creat

In this chapter, we defined a series of mini-languages and used them to model data structuring facilities in three representative programming languages. An important question to ask is how complete our modeling is. In other words, how thoroughly have we covered the approaches to data structures found in these three languages? At first glance, our treatment seems rather incomplets because of the limited axpressive power of the mini-languages we defined. Sout most of the features not included in our mini-languages are independent of the notions of data structures in the sense that the way such features are defined in an actead programming language has no bearing on how the language approaches concepts of !!

r dan sel selger an**terior arbitiques distan**ces of the self-

i v viet i diberou una vega preda de tant

ilanda kana da da da da da da da shekara ma kana da ma kana da ta ta ka kana ka k

data structures. The fact that our mini-languages lack character strings and conditional expressions, for instance, does not reflect on their completeness for describing data structures.

In PAL, there are only two notions we have not covered which have a direct bearing on data structures. First, arbitrary integer-valued expressions can be used to select components from a tuple. For example, the selection x n refers to the component of the tuple x whose selector is the value of the variable n. This cannot be translated into our mini-languages, which allow only constant (selector)s (the ML-3 (selection) n of x would look for a component with selector "n"). The second uncovered feature in PAL is the built-in function Order, which when applied to a tuple yields the number of components in the tuple.

Neither of these two notions can be expressed in our mini-languages, but it was not our goal to be able to do so. For these two data structuring features, the semantic, issues are well understood, we don't really need to treat them in our mini-languages. Extending the mini-languages to handle extra notions like these would only serve to ruin the syntactic and semantic simplicity of the mini-language

 $-104-$ 

approach.

rang pangalangan ang pangabawang n

In QUEST, the only data-structuring features we did not treat are the use of expressions to select components from a list, and several built-in functions that operate on lists. As with PAL, we feel that the issues raised here are outside the area of our main concern.

With SNOBOL4, we completely neqlected the area of arrays. Although arrays are highly relevant to the issues we are interested in, they present some difficult problems for whose solutions additional mechanisms are needed. We discuss some of these problems in Chapter 5.

The three languages covered in this section are all "typeless" languages in the sense that there are no declarations associating identifiers with particular data types. In the next chapter, we deal with "typed" languages and some new semantic issues they introduce.

n de Brasilia (1990).<br>Constitution de Carlos (1990).

s kin grup (bol so

 $-105-$ 

# Chapter 4 TYPES AND TYPECHECKING **DATA** ネーほか 「毎回リーら」

# 4.1. Why we want a Type System

In this chapter we will add a new facet to the design of our previous mini-languages. Consider the ML-3 (assignment) y + x, which directs that the contents of the cell for x be placed into the cell for y. We translated this (assignment) into an invocation of the BL procedure assign3 (defined back in fig. 3.5-1). Bvery time this procedure is called, there is a separate set of tests performed to check whether the cell for the first parameter (which corresponds to x) contains an integer or a structure. The set of BL instructions chosen to perform the assignment operation depends on the result of these tests. In practice, however, a programmer will usually know in advance whether the identifier x will take on integer or structured values. This knowledge makes these runtime type tests in assign3 superfluous. We would like some way of telling the translator not to make such tests where they are not needed.

The technique of static typechecking achieves these goals. Its basic idea is to partition the set of values

 $-106-$ 

into convenient subsets called **types.** The translator can be informed of the programmer's intentions of keeping values . ' only of a certain type in some given cell. With this knowledge, redundant runtime type tests can be eliminated. But it is still necessary to prevent type errors. For example, suppose we tell the translator that the variable x will take ak magébol on only structured values. Each time we **access** the value of x, the BL code produced by the translator will fetch the components of x. If we somehow place an integer value in the cell bound to x, then during execution the interpreter  $-36.5$ would attempt to extract components where there are none, i si a dunis yielding undefined, probably erroneous results. To prevent sdia list SP. such type errors from occurring, we would like to have the translator test each (assignment} to make sure it couldn't i specify the placing of a value of one type into a cell intended to hold values of another type. Any (program) containing (assignment)s which fail this test is invalid; the translator will notify the user of such an error in the same way that it flags syntactically erroneous (program)s.

In testing (assignment)s for validity, it will be useful for the translator to know for each (destination) the type of values intended to be stored in the associated cell.

-107-

This criterion can help us decide how to partition the ML-3 values into types. If we divide values into just two types, integers and structures, then the above criterion is not always satisfied. Suppose the (identifier) x is specified as assuming only structured values. Then the values yielded by both of the  $(expression)$ s [  $a:3$  ]  $b:4$  ] and  $[a:3; b:[ct5; d:6]$  an be stored in the cell bound to x, but we cannot say anything about the type of the (destination) b of x. In one case it has an integer value; in the other case, a structure. **Thus** finer type classifications are called for. We will want to ascertain from the type of a structured value what components it has and the type of each component. Such a type system is the basis for our next mini-language.

### 4.2. Mini-Language 4 -- Static Typechecking

Mini-Language 4 (ML-4) adds the notions of data types and static typechecking to the concepts we developed in the previous chapter. Specifically, it is an extension to ML-3, associating to every (expression) and to every cell a particular data type. For our purposes, we consider data types as sets of values. The set of integers is an ML-4 data type. Further, the set of all structured values with a

그 사회 보는 눈이 가장 제 이 일까.
given set of component (selector)s such that the type of the component associated to each specific (selector) is given also is an ML-4 type. With this collection of data types, if we associate a type to each (identifier) mentioned in a (program), then we shall be able to determine the type associated with each cell referred to in the (program). Moreover, for any particular data type, one can determine whether the value yielded by a given (expression) belongs to this type.

### Syntax of ML-4

The rules here govern the syntax of that part of ML-4 which is not found in ML-3 (namely the type system). We introduce the new primitive syntactic class (typename) to denote the set of underlined alphanumeric strings beginning with a letter. The distinguished (typename) int has particular significance, which will be discussed below.

 $::=$  (prelude) ; (assignment) ;...; (assignment)  $\langle$  program $\rangle$  $\langle$  prelude $\rangle$  $\rightarrow$ :=  $\langle$ defn $\rangle$   $\rightarrow$ ...;  $\langle$ defn $\rangle$ ;  $\langle$ decl $\rangle$   $\rightarrow$ ...;  $\langle$ decl $\rangle$ .  $::=$   $\langle$  typename  $\rangle = \langle$  structype  $\rangle$  $\langle$ defn $\rangle$  $\langle$ structype $\rangle$  : = [ $\langle$ comp decl $\rangle$  ;...;  $\langle$ comp decl $\rangle$  ] のほむ手とない きょうえつけい みん  $\langle comp \text{ decl} \rangle :: \langle typename \rangle \langle selector \rangle$  $: i = \langle \text{typename} \rangle \setminus \text{identity} \rangle$  $\langle {\rm dec} 1 \rangle$  . s valentina The remainder of the ML-4 syntax is identical to the syntax presented for ML-3, with two exceptions. First, ML-4 has no

 $-109-$ 

en 1990 en 1991 en 1991 en 1991 en 1991 en la forma de la form<br>Constituir de la forma de

(modification)s (which we simply won't have occasion to make use of), and second, (construction)s appear slightly differ-. The contribution of the constant  $\lambda$  is a contribution of the contribution of  $\lambda$  , and the contribution of  $\lambda$  $ent:$ 

 $\lceil \cdot \cdot \cdot \cdot \cdot \cdot \cdot \cdot \rceil$  )  $\lceil \cdot \cdot \cdot \rceil \rceil$  (typename)  $\lceil \cdot \cdot \cdot \cdot \rceil$  (field)  $\lceil \cdot \cdot \cdot \rceil$ work: Cell expresser Mac More Montered  $\langle$ field $\rangle$ (The (selector)s that no longer explicitly appear in the (field)s of a (construction) may be found in the (defn) for the  $\langle$  typename  $\rangle$  of the  $\langle$  construction  $\rangle$ .)

tent is astronisht noong beko<sup>n</sup> (paler so f

Ardan Bol

### Description

We need to interpret the new syntactic classes. A (program) in ML-4 is essentially a (program) in ML-3. preceded by a (prelude). The (prelude) is a sequence of type definitions ((defn)s) followed by a sequence of declarations  $(\langle \text{dec}1 \rangle s)$ . A  $\langle \text{dec}1 \rangle$ , consisting of a  $\langle \text{typename} \rangle$  and a list. of (identifier)s, specifies that those (identifier)s are to assume values only of the type given by the (typename). 그리스 전 전 시간들이 Types in ML-4 are denoted by members of two syntactic vek sprovinski kompleta od provinskom koprovinskom k classes as follows: A LOCULES I MOTOR COMPANY PROPERTY IN THE LOCAL CONTRACTOR

- (1) A (typename) is either the symbol int (which denotes the type consisting of integer values) or the
- (2) A (structype) denotes a structured type (i.e. a type consisting of structured values). The (selector)s and types of the associated components of a value of such a type are specified by the

Thursday Allo, and disagreemed for deed up the

 $\omega_{\rm{c}}(\lambda_{\rm{c}},\lambda_{\rm{c}}^{\rm{c}},\lambda_{\rm{c}}^{\rm{c}})$ 

as present

しょごげん やせ うるとのしがいい Observe that if we know the type of a structured value, then as the second thread part is seen as we know the type of each of its components. There are two 1940年前第46回44日 1977年2月1日に basic purposes for using (typename)s: first, to provide for multilevel structures (i.e. structures with components which are structures), and second, to allow for recursion in type definitions. We discuss recursive types later.

### Semantics of ML-4 (informal)

RESORT OF THE RESORT OF THE RESORT OF THE RESORT OF THE STATE OF THE SECOND SECOND OF THE STATE OF THE STATE O

(1) Data types and type definitions: We define the data types that are specified by the syntactic units of Elements of the classes (typename) and (structype)  $ML-4$ . define data types according to three rules:

- (i) The (typename) int denotes the class of all integer values.
- (ii) Suppose  $s_1, \ldots, s_k$  are  $\langle$  selector  $\rangle$  and  $t_1, \ldots, t_k$  are syntactic items denoting data<br>types. Then the (structype)  $[t_1 s_1^2,...,t_k s_k]$ denotes the class of all structures with exactly k components with (selector) shows a  $s_1, \ldots, s_n$  such that for each  $i = 1, \ldots, k$  the value (if any) contained in the component cell selected by  $s_j$  belongs to the type  $t_j$ .
- (iii) If this the (typename) of a (defn), then t denotes the type specified by the (structype) of that (defn). In this case we say that the (defn) defines the (typename) t.

1940年,我们在1940年,1940年,我们**就过**去。

These rules give the semantics for type definitions in ML-4.

Note that according to rule (ii), if xis a value belonging to a structured type t, then the types of all the component cells of x are determined.

As examples, the objects of figure 4.2-1 belong to the type int. In the presence of the (defn)s

 $pt = [ int p ] and t = [ int a; pt b ],$ the objects depicted in figure 4.2-2 belong to the type t (which is the class of all two-component structures with



a-component of type int and with b-component a one-component structure whose p-component is of type int). Note particularly that a cell constrained by our type mechanism to hold values of a given type can be empty. A value may belong to more than one type (par-

ticularly if it is a structure some of whose component cells are empty). But given any value v and any type t, one can always tell whether or not v belongs to t.



A <typename) does not have to be defined textually be-

fore it is used in a (prelude). For instance, the (defn) sequence  $t_1 = [t_2 \ c]$ ;  $t_2 = [int d; int e]$  is perfectly legal. A nontrivial application is the definition of recursive data types, which arise in ML-4 when a (typename) is used as part of the (structype) in its definition. Consider, for example, the  $\langle \text{defn} \rangle$  <u>r</u> =  $\left[ \underline{\text{int}} \underline{a}; \underline{r} \underline{b} \right]$ . This<br>defines a type named <u>r</u> consisting of two-component structures for which the a-component cell can hold only integer values and the b-component cell can hold values only of type  $r$ . Although it sounds circular, it is perfectly well defined. Values of a recursively defined type can have substructures nested to an arbitrary depth, and M-objects representing such values frequently contain directed cycles.

We make three restrictions on (defn)s in ML-4. First, the (selector)s occurring in a (structype) must be distinct. Second, a (typename) can be defined only once in a (program). Third, the (typename) int must not be redefined. Any  $\langle$  program $\rangle$  not obeying these restrictions is syntactically invalid (i.e. is *to* be rejected by the translator). The meaning of an invalid (program) is undefined.

(2) Declarations: As with (defn)s, the semantics for a (decl) does not specify any particular actions to be per-

x ara

**このことで、これについても、これに、これを見て、事務局をもうという** 

ségéna du Ter formed at runtime. The effect of a (decl) is to cause the Po 万将一字。 [42] 2010 - [4] 오래드 그의 개월 10% (일)] 3 (identifier)s in it to be associated with the type named in ies vai košo krašės. Juži su robitos k**igris Vadvinda**is the (decl). เริ่ม (มายประชาวส์ชาวิสริย์) พระเจ้ารูป (มายประชาชนเดีย) ( an Gamasyahan I

In order for a (program) to be syntactically valid, every (identifier) occurring in some (assignment) must appear exactly once in the (program)'s (decl)s. Busry (typename) occurring in some (decl) must be defined exactly once in the (defn)s.

Prom the above semantic rales for (defn)s and (decl)s, it is possible to uniquely determine the type of any (expression) - in a syntectically waidd (program): This is done as follows:

- $\sim 44$ ) Suppose the (expression) is  $z^o$  (dustination). If  $z^c$  it is an (identifier), then this (identifier) occurs in ⋰⋰⋰⋫⋐⋐⋐⋦⋦⋛⋌∊**Ѻ⋑⋐⋋⋵⋞⋐⋐⋐⋚⋧∊⋐₹⋐**⋵∊⋦⋦⋐⋦⋪⋛⋐⋛⋦⋛⋰⋢⋑⋋⋐⋤⋖⋐⋢⋋₽⋳⋛⋦⋐⋋<sub>⋰</sub>⋰⋰ (typename) of the (decl). If it is a (selection), then it consists of a (selector) and an (expression). The type of the (expression), which can be determined recursively, will be some atructured type designated by a (structype). The type of the (selection), then, is given by the (typename) in the (comp decl) of the (structype) that contains the given (selector).
	- (ii) If the (expression) is a (generatory, there are two cases: (integer)s are of type int and (construction)s - and of the *topic given by their (tymename). <sup>201</sup>*

Thus we can determine from the (prelade) of a syntactically valid (program) the type of any (expressiony; this type is ! given by precisely one (typename). For example, in the presence of the (prelude) xtype = [int as xtype b]; ytype = [int c; int d]; xtype x; ytype y the type correspondences shown in figure 4.2-3 are valid.

网络海峡





tem forces the cell referred to by the (destination) to hold  $\mathbb{R}^{n\times n}$  . The set in  $\mathbb{R}^{n}$  . In  $\mathbb{R}^{n}$ values only of a certain type. Thus the translator must verify that the value of this *(expression)* matches this type.

A (construction) in which the components fail to match the types of the corresponding fields in the  $\langle$  defn $\rangle$  of its  $\langle$  typename) is an invalid  $\langle$  expression) and has undefined type. For example, if we define  $z = [\underline{int} a; \underline{int} b]$ , then the  $\langle$  construction $\rangle$  <u>z</u>[1,2,3] is invalid because of its extra the (construction)  $\underline{z}[1; \underline{z}[2;3]]$  is also invalid component; because its b-component is of type z rather than int as required. We also call a (construction) invalid if its (typenarne) is not defined in the (prelude).

化氯化氢 医心脏炎 化有量 医白血 经货币 建美国亚斯卡尔

en de la stranda de la proprieta de la porta de la proprieta de la proprieta de la proprieta de la proprieta d

o presitenti stranovni ne medne suce i An ML-4 (program) is invalid if in any of its weitenents: tetwerden (assignment)s the type of the (expression) is undefined or fails to match the type of the (destination).  $\sim$  $\sim$  and the realistic mass of  $\sim$  and  $\sim$ Each of these two types is given by precisely one ing Bird counterpart, in addition (typename) these types are defined to match if and ans de las directed (co des only if their (typename)s are identical. The mechanrA (chapt Jagofffbba plansebloor) of h<u>avo</u>us gi isms we shall define for the translator insure that it can eseienco ... etoisd as library data always determine whether or not a given ML-4 (program) is RE bas: (norralideel) 机高压率 的过程 valid. There is no need for runtime type tests, nor are likava Nulle<sup>r</sup>lam l ディになり 接着のなない さき there any runtime type errors. However, a runtime error will occur if there is an attempt to extract components from nushend edi ettii (orkimistues é id kuu seblek an empty cell of a structured type. For instance, the ML-4  $\langle program \rangle$   $\underline{\bullet 1} = [\underline{\text{int}} a; \underline{\bullet 2} b]; \underline{\bullet 2} = [\underline{\text{int}} c]; \underline{\bullet 1} x;$  $x \leftarrow \texttt{sl}[3;\texttt{nil}]$ ; c of b of  $x \leftarrow 4$  will fail on interpretation of its last (assignment) (since the interpreter will look for a nonexistent c-component in the empty cell for b of x) blleva, ne a. even though the type of the (destination) c of b of x (int) (*nordne*s matches the type of the (expression) 4. Thus we require runtime tests to check the (selection)s in ML-4. Generally speaking, testing for empty cells is usually much easier than testing the type of the contents of a cell at runtime. studena) sú mi bonilob for al Comp, a If we strip off the (prelude) from a valid ML-4

 $-116-$ 

(program), then we will have in essence an ML-3 (program) in which each cell takes on values of only one type. Moreover, the effect of executing this ML-4 (program) is identical to the effect of executing its ML-3 equivalent.

### Translation into BL

To give a precise formulation for the semantics of ML-4, we describe the translation of ML-4 (program)s into BL. With the previous mini-languages, it sufficed to show the BL code corresponding to various program constructs, namely the different kinds of assignment statements. This is no longer sufficient in the case of ML-4, since the semantics now contains rules for typechecking by the translator. We must therefore also describe the typechecking procedures performed by the ML-4 translator.

In discussing how the translator performs typechecking of ML-4 (program)s to determine their validity, we begin by describing the information supplied to the translator by the (prelude) of a (program). We shall treat the translator as a BL procedure. As it processes the (prelude), the translator builds two component objects in its local structure: one component named \$defns which represents the type definitions, and one named \$decls which corresponds to the

the declarations. \$defns is a structure which has one component for each (typename) found in the (prelude). Each component of \$defns is a structure with information on the type associated with the (typename). For each (typename) defined in a (defn), the corresponding component of \$defns has an "n" fleld with the number of components in a value of that type, numbered fields giving the (selector)s of the components in the proper order, and a "val" fleld giving the types of the components (by means of links to the proper entries in Sdefns). The int-component of Sdefns has only a  $\texttt{val-component}$  containing the elementary value 'int'. Sdecls is a structure with one component for each (identifier) declared in the (prelude). If, say, the (fdentifier) x is declared to have type t, then the x-component of Sdecls shares with the t-component of testre. In each of figures  $4.2 - 4.4.2 - 5$  and  $4.2 - 6$  we give a (greaude) and exhibit the objects Sdefns and Sdecla constructed by the translator from the (prelade). The type with (typename) g in figure 4.2-5 is recursively defined; observe that Sdefns has a directed avalents this dase. The construction own abidual series

Once these objects have been constructed by the translator, all the information regulred for typechecking is

 $-118-$ 

promote from the

<u> San Millian an San Ang Bandarang Ba</u>

available. Each type to be associated with some cell referred to in the (program) is represented by a component node of \$defns. Two types match iff they have the same





 $(typename)$ . To describe how the translator performs the actual typechecking, all that needs to be shown is how to access the node for the type of any ML-4 (expression); once we can do this, the typechecking is straightforward:  $an$ (assignment) has a type error iff the nodes for the types of its (destination) and its (expression) are distinct.

The type of an (identifier) x is given by \$decls.x. The translator will mark a (program) invalid if any of its  $\langle$ identifier)s are undeclared. If  $\beta$  is the node-for the type of a (destination) D, then the type of the (selection) s of D is given by the node  $\beta$ . val.s. The translator verifies as part of its typechecking that values of the type of D do indeed have s-components. Thus we can astertain the node for the type of any (destination) in an ML-4 (program). Figure 4.2-7 illustrates some sample ML-4 (assignment)s involving only (destination)s and gives BL typechecking code



 $-120-$ 

to determine their validity. A branch to the label "no" t smiles exigencia difficul indicates that the (assignment) has a type error.

**Installed and interviews and pro-**

If an (expression) is an (integer), then its type is given by the node \$defns.int. The type of a (construction) whose (typename) is t is given by the node \$defns.t,  $pro$ vided the (construction) is valid. To check this, the types of the components in the (construction) must match the (typename)s in the (structype) that defines t; moreover, there must be the same number of components in both places. -Tomat Ix As praint 6 - Walio Barat, mwaka 20 Thus the translator can access by our scheme the node for the type of any (generator). As a result, we now see how the translator accesses the nodes for the types of arbitrary ML-4 (expression)s. Figure 4.2-8 gives some examples of 机烯 胎生 祥 定方断 ML-4 (assignment)s containing arbitrary kinds of (expression)s; along with each (assignment) we show BL code which tests its validity. This completes our picture of how the translator performs static typechecking; the mech-ปรรมสุดีนอย่ anisms should be clear from the examples in figures 4.2-7 and 4.2-8.  $\{d\mu(\mathbf{z},t)\in\mathbb{R}^n: \mathbb{R}^N\}$ 

The actual BL code generated by the translator (i.e. the BL code to be interpreted at runtime during the execualestrope decret ್ಮ ಅಡಲ tion of an ML-4 (program)) is similar to what we presented 1990、 Angler 2015、 Applexies 2017年10月18日, Angler 2018年11月18日。

(本) 的复数经职业 医神经性神经病理 in the section on ML-3. There are two differences reflect- $\sim$   $\gamma$  ) and there together that  $\sim$   $\sim$   $\sim$ ل علي الله

alian.<br>Alika



ing the switch of typechecking from runtime to translatetime. First, occurrences of (selection)s in ML-3 yield runtime type tests, such as the BL code has? x, b, error for

i della città sua della consegue della contra della contra della fine della contra della contra dell'

 $-122-$ 

the ML-3 (selection) b of x. In ML-4 this runtime type test is replaced by the simpler and faster test nonempty? x, error, which makes sure there is no erroneous attempt to access component cells of an empty cell.

The second change is that the complicated procedure assign3 with all its type tests is not needed at all. The BL code generated from the (assignment)  $y \leftarrow x$  depends on the type of the (destination) y. If its type is int, then by virtue of the translator's static typechecking we know that x can hold only integer values. In this case the BL



<u>Voltan essett für ein</u>

code in figure 4.2-9 is generated. If y is of a structured type, then the translator knows that its (selector) a s. .... s  $_{\odot}$  are given by

 $s_1 = * ($ \$decls.y.1), ...,  $s_1 = *$ {\$decls.y.\*(\$decls.y.n)). In this case the BL code in figure 4.2-10 is generated. The translator can always tell which case applies by testing whether the pathnames \$decls.y and \$defns.int lead to the same cell. The BL instruction same? \$decls.y, \$defns.int.go performs this test. A branch to the label "go" indicates

ing pandapat ng pangangang kaping kap

that y has a structured value and that the second case request home visquis entraved beceique habites applies. Thus, by sub-

Clear way the college dubby ( there is أتشفيهن stituting the nonempty? **NORTHWE A. ALLE IN STRONG RESOLUTION AND ALLE** test for the has? test  $X^* *_{1'} X^* *_{1}$ link appropriated and for the second to see the street of fig- $110$  and  $4.2-10$ skip: ...  $Fig. 4.2-10.$  BL code for the ML-4 (sesignment) Y = x p antiquit procedure, we when y is structured

yielded by the ML-4 translator. This completes our deseription of the transmition of ML-4 into BL and places the asula semantics of M5-4 on them and preside ground.

o Istalic Cycle op yan

82392

安,宋建于"三"。

VOID AV DE RANGERY DE 1972 BLACK **MARING HIS COOL** T

### Discussion and Examples  $4.3...$

o a thorough town to funks

**BWORK ROUB** 

abos 18.70-X Nost programming languages handling dess, strugtures sit v rans have a type system similar to that of Mi-4; the bulk of their typeghecking is done at translation time rather than minting. In this section we tract the data structuring facilities of three of these languages, weing Mi-4 as a vehicle for describing their semesters and communications **SALGOL** AND NOR (2008) On the Protection of Contracting Protection of the Contraction

**SECTIONAL DRUMBER** 

The Imaguage ALGOL W [Wir 66] has a relatively simple

# $-124-$

treatment of data structures. The structures are called records, and the ALGOL W analog to an ML-4 structured type is called a record class. An ALGOL W record class declaration can be represented by an ML-4 (defn). Figure 4.3-1 shows how the two languages define **classes** of structured objects: the ML-4 type **with (typename) .2!.!!:, corresponds** to the ALGOL W record class named pair. Structured objects are built in ALGOL W through the use of record designators, which are analogous to ML-4 (construction)s. Expressions in both languages which build structures from the "pair" class are also shown in figure 4.3~1.



There is a major difference between ALGOL W and ML-4 with respect to these elements. Although a record designator builds a structured object in ALGOL W, it does not yield as its value the object it constructs. In fact, records are not even values in ALGOL W. A record class is not a legitimate type in ALGOL W; records are accessed through values of reference types. For instance, the ALGOL W record

designator pair(3,4) in figure 4.3-1 yields a value of type reference(pair). ML-4 will treat reference expressions in ALGOL W similarly to the way ML-3 treats pointers in ML-2. The correspondence is depicted in figure 4.3-2. Note that

ALGOL w\ record pair (integer a, b) ; reference(pair) y,z;  $y := pair(3, 4)$ ;  $z := y$  $ML-4$  $pair = [ int a; int b];$  $refpair = [ pair ptr ]$ ; refpair y, z;  $y$  + refpair [ pair [3;4] ];  $z + y$ "<br>|-<br>| זי ) e I  $+ +$ **pl:r fb-K**<br>A +<br>a + 6 o.. b @® Fig. 4.3-2. Reference expressions in ALGOL W. respect to our

in dealing with ALGOL W records, we need an extra level of indirection (the "ptr" component). This (at least with scheme of rep-

resentation) is the same kind of inefficiency we encountered with ML-2. It is worse here, though, since ML-2 made use of the indirection only when sharing was needed.

Components of a record can be accessed by selector functions in ALGOL W. Figure 4.3-3 shows the correspondence between selections in ALGOL W and ML-4 (z is of type reference(pair) in ALGOL W, refpair in ML-4). language selection ALGOL W  $a(z)$ <br>ML-4  $a$  of **ML-4** a of ptr of z Fig. 4.3-3. Selection.

Once these differences concerning the construction and ಲೇಖಗಳು selection operations have been taken into account, we find かいせい しゃぶな 嫁え that assignment, sharing and typechecking in ALGOL W are almost identical to the "obvious" ML-4 counterparts (e.g. **Check fright!** 短裤 如果的过去分词 replace ":=" with " $+$ "). In this respect, ALGOL W is similar 29、 4、 2、 4、 6、 4、 4 to the language SNOBOL4 described in section 3.6.

 $PL/1$ 

PL/1 was one of the earliest languages to have compiletime typechecking and to treat both data structures and pointers. Most PL/1 constructs handling these notions look

markedly different from the

 $\mathcal{R}(\mathcal{L}_{\mathcal{K}}^{\mathcal{L}}) = 2\pi\lambda^2 \mathcal{L}^2$ 

1971年12月11日 1月11日 1月11日

wingstoning Web



SAN SERIA

.<br>මේ වා ගැන් පුරෝර් - කල්ලි ද වෙණෙන <mark>, එමගි සමු ග</mark>මේ ගුරේෂ්ට මිද්දමටද other languages. Figure 4.3-4 shows how PL/1 handles a ේ යන් අනු ගත්ත්, රාජයක් දිගියි දිගිය දිගිය විශේෂය සම්බන්ධයෙන් පිය දෙවිය. sample structure and gives an ML-4 equivalent. We make two The South County of the Barbara and the County of the County of the Town of the South of the South of the South America of the Town of the South of the Town of the South observations. First, all component cells of the PL/1 struc-Agel (1933) Proprietor<sup>6</sup> add 30 december 7 tures in this example are allocated when the declarations ikus mieros enin kriuu de diu turi are interpreted. With ML-4, component cells are allocated of hypercent of their seen programs scharges. when the structured value is actually constructed. Second, a PL/1 structure assignment like  $Y = X$  in fig. 4.3-4 slgnifies component by romponent copying (resursively for atructured components) as with stiel and court!

Unlike ALGOL W. there is no sharing among PL/l structures until we introduce pointers and the attribute BASED. if pis a PL/1 variable declared to be a pointer, then de-Mig CHXT claring a structured variable with the attribute BASED (P) ,aie critic t f. introduces a vast conceptual difference. This variable no. SR TIME X longer signifies a location where structured objects may be XvSudine en stored, instead, it plays the role of a structured type. Figure 4.3-5 exhibits a set of PL/1 declarations involving BASED structures and gives a corresponding ML-4 (prelude) and set of ALGOL W declarations.

Although the ML/1 declarations of figure 4.3-4 specify allocation of atorage to hold structured values (and allocation of component cells as well), the declaration of LIST

<u> de la construcción de la construcción de la c</u>

in figure 4.3-5 does no such thing. BASED structure values in PL/1 are constructed through the use of an ALLOCATE

------- . PL/1 DECLARE **(P,H,T)** POINTER; DECLARE 1 LIST BASED(P), 2 BACK POINTER, 2 FWD POINTER, 2 NUM FIXED BIN;  $ML-4$  $1ist = [list ptr];  
list = [ptrlist back;  
ptrlist fwd;$ </u> 1ist = [ptrlist back;<br>ptrlist fwd; int num]; ptrlist p,h,t ALGOL W record list= ( reference ( list) back; reference (list) fwd; integer num); reference (list) p,h,t; Fig. 4.3-5. PL/1 **BASED**  structures **as** types.

larations in figure 4.3-5, the PL/1 statement ALLOCATE LIST may be represented in ML-4 by the  $\langle assignment \rangle$  p + ptrlist [  $list[nil,nil,nil]$ . Since LIST is declared to be **BASED** on the pointer P, the allocation causes the value of P to be set to point to the newly-built structure. The result of

statement. Under the dec-



this allocation is shown in fig. 4.3-6. BASED structures in PL/1 are accessed through pointers. In our LIST example, a use of the name LIST refers to whatever the pointer P is currently pointing to (which will be the most re-

cently constructed structure BASED on P, unless P has been

subsequently updated). To refer to a previous allocation, one must use a qualified reference such as T -> LIST (which indicates whatever the pointer T is currently pointing to). Figure 4.3-7 draws the connection between PL/1, ALGOL W and ML-4 in accessing fields of structures (it is assumed that the declarations in fig. 4.3-5 are still in force).



The meaning of assignment in PL/1 is similar to ALGOL W except for its handling of structured values (which ALGOL W does not choose to handle). In this case, as we have said, PL/1 copies rather than induce sharing. All sharing of data in PL/1 is done through pointers.

Typechecking in PL/1 differs from ML-4 and ALGOL W in one major area, that of pointers. The ALGOL W translator insures that a reference value can point to records only from one record class; if cl and of are distinct record classes, then any attempt to make a value of type

reference(cl) point to a record from class c2 will be caught by the translator and marked as illegal. The type system for ML-4 imposes essentially the same restrictions. However, a variable of type POINTER in PL/1 can be set to point to values of any type at any time (including nonstructured values). This causes difficulties of the same kind that static typechecking is supposed to eliminate. For example, in the PL/1 program segment of figure 4.3-8, the assignment  $P = Q$  is legal, even though P points to a structure of type



Ml and Q points to the integer M2. The reference to Ml in the following line  $(M1.K = 5)$  designates whatever P will be pointing to (which is the integer M2 since P has just been assigned the value of Q). Thus there will be (depending on the implementation) a runtime error or at least an erroneous result as an outcome of the attempt to update a component of

the integer value M2. The ML-4 translation of this program, also shown in figure 4.3-8, is invalid since in the  $\langle$  assignment $\rangle$  p  $\leftarrow$  q the types fail to match (ptrml vs. ptrm2). If in the PL/1 program we had declared M2 to be BASED on P, then the corresponding ML-4 (program) would have two conflicting declarations for p, which would also render it invalid. Thus we see that the typechecking system in PL/1 fails to catch a whole class of programs which might have runtime type errors.

### **ALGOL 68**

The treatment of data structures and pointers in ALGOL 68 is linked to an intricate system of types and typechecking. ALGOL 68 is a difficult language to learn and understand; the defining documentation [VWij 69; VWij 73] presents an intimidating formalism to the uninitiated. However, there are works (e.g. [Lind 71]) which are immensely helpful.

Types in ALGOL 68 are called modes. The modes of relevance to us are the mode int (integer values) and the modes built from the mode-constructors struct and ref (structured and reference values, respectively). We describe a correspondence which assigns ML-4 types to ALGOL 68 modes:

ा इतरा

(1) To the ALGOL 68 mode int we assign the ML-4 type int.

s <del>ranguj</del>an se japoné n<del>a kap</del>angkat sa sa pang pag-at

**Connect Ago State Contract Section** 

- (2) If  $M_1$ ,  $\ldots$ ,  $M_k$  are modes and  $S_1$ ,  $\ldots$ ,  $S_k$  are tags.<br>(the conjurilant of (selector). then to the mo (the equivalent of  $\langle \text{selector} \rangle$ s), then to the mode  $\textrm{struct}(M_1, S_1, \ldots, M_k, S_k)$  we assign the Mi-4 type.<br> $[T_1, S_1, \ldots, T_k, S_k]$ , where the  $T_i$  are the Mi-4 types corresponding to the M<sub>issour</sub>
- $(3)$  If M is a mode then to the mode ref M we assign the type [T ptr], where  $T$  is the Mi-4 type corresponding to M.

i Kulusu siyi

医心室的第三人称单数 经遗产的过去分词

Mode-declarations in ALGOL 68 are just like type definitions in *ML-4*; for example the mode-declaration

mode pair = struct(int a, int b) is equivalent to the ML-4  $\langle$  defn $\rangle$  pair = [int a; int b].

A declaration in ALGOL 68, besides associating an iden-<br>A declaration in ALGOL 68, besides associating an identifier with a mode and imposing type restrictions on the rest of the program, has a two-fold runtime effect. Consider a declaration of form  $M X = E$ , for instance int  $x = 3$ , where M is a mode, X an identifier, and E an expression yielding a value of mode M. This declaration first binds X \_,,,, to a newly-allocated cell. Second, it places the mode M value yielded by E into this cell. What is peculiar about ALGOL 68 declarations is that this value can never be changed. It may, however, be a reference value (i.e. the mode M is <u>ref</u> N for some other mode N); in this case it refers to (points to) a cell holding values of mode N. This

latter cell (and not the former cell) can be updated by the assignment operation in ALGOL 68. Thus the meaning of assignment in ALGOL 68 differs from acsignment in the other languages we have discussed. Note that an identifier whose declared mode is not a reference mode serves essentially as a constant. An identifier of mode ref N in ALGOL 68 plays the same role as a variable of type N in another programming  $\omega_{\rm{max}}$ language.

The specific definition of ALGOL 68 assignment is as follows: let E be an expression yielding a value of mode M (M can be arbitrary) and D an expression of mode ref M. The value of D is a reference to a cell which can hold values of mode M. Then  $D := E$  is a valid assignment and specifies that the mode-M value of E is to be stored in the mode-M cell referred to by (the value of) D.

A particular kind of ALGOL 68 expression, known as a local generator, specifies allocation of a new cell when it is evaluated. If M is a mode, then evaluation of the local generator loc M causes a new cell (which can only hold values of mode M) to be allocated. The value yielded by loc M is a reference to this new cell and therefore belongs to the mode ref M.

 $-134-$ 

To obtain a variable in ALGOL 68, which will take on values of a mode M, we must declare an identifier X of mode ref M so that assignment can change the mode-M values. This may be accomplished by means of an ALGOL 68 declaration of form M X, which is really an abbreviation for the dec $l$  aration  $r$  ef  $M$   $x$  =  $l$ oc  $M$ . Consider, for example, the ALGOL 68 declaration int x (equivalent to the declaration ref int x = loc int), whose effect is depicted in figure 4.3-9. The identifier **x, which·is declared** hereto be of schements Falls ing again an Balancarus

mode ref int, is

•



evaluating the

 $\langle$  cell expr $\rangle$   $\overline{\text{nil}}$  in the  $\langle$  construction) reflnt[nil] in ... ML-4); and the upper cell receives as (permanent) value a pointer to the lower cell. Subsequent execution of the ALGOL 68 assignment  $x := 3$  would place the value 3 in the lower cell; therefore its ML-4 equivalent is the (assignment) ptr of  $x + 3$ . The static typechecking rules for ALGOL 68 医眼炎 医外皮病 医假静脉 医卡尔曼氏试验检尿道 医心包 医小脑

Edminent () **ALASSO B** insure that any assignment attempting to place a non-integer value in the lower cell is detected and indicated to be こんしゃがたしゃようがいしょ くみがいじょ Restarched 経路に ご 細いすいしやく invalid.

2012年(松) (1947年1月18日) 1948年 1948年 There is one aspect of the ALGOL 68 type system which iwana njiamba wa jimi*d*wa , a fa gmucha go is more lenient than the ML-4 system. Unlike PL/1, no type al paggi an la 44 la 913 li mar d'anyun errors can arise from this loosening. Consider the assign-ਾਰ ਦਿੱਤਾ ਸਿ **CONTACTES** -col - 1942 A ment  $y := x$ , where both identifiers x and y have been dein Brook light boils & The s de l'espè clared to be of mode ref int. This assignment specifies the งปี พื้นเทพ (เต. ซอร์วิ แม่ โดยงาลส่ updating of the mode int cell pointed to by y. But the right-hand side, which must them supply an integer value, is of mode ref int; according to ML-4 rules, the assignment is to be rejected by the translator as invalid. However,  $\sim 100$ ALGOL 68 recognizes that the ref int value of \* points to an int value, so all that needs to be done to obtain the re-Bereforth 分割(2) quired integer value is follow the pointer x. This process is called dereferencing. In general, the procedure for obtaining a value of a desired mode from a value of some other sa daliansk film medi ban ba mode is known as coercion or conversion. Thus, in the VVISOR Geed om 1999 (1999) e estacion ALGOL 68 type system, if the left-hand side of an assignment <del>有</del>的名词复数 医心动脉 医心病的 医心气透**热度的物质**有毒素的的。 is of mode ref M. then the assignment is valid provided the and the most completed in the second section of the second section o right-hand side is of mode M or can be coerced to yield a particle and research and planning distribution ing Society of mode M value. In our case, the procedure which translates

**MARINAL PRESS DESCRIPTION** 

**Marie College was the** 

**CHAPTER THAT** 

فجهوري والمجاوب معاذر بالأرائي والمجا

from ALGOL 68 into ML-4 must recognize that dereferencing is called for, mark the assignment  $y := x$  as legal and gen-,  $\gamma_{\ell}$  in the contract  $\{ \omega_{\ell} \}$  , where  $\{ \omega_{\ell}^{\ell} \}$  , where erate ML-4 code which takes the coercion into account.  $OC$ de Die wahren er eine Fragen the three assignments in the example shown in fig. 4.3-10, coercion takes place only in the second one (where y is dereferenced). The y on the right-hand side here is translated into the ML-4 (expression) ptr of y, yielding a valid ML-4  $\langle$  assignment $\rangle$ .

Note that the mode of x is int, and the mode of y and z is ref int.

The concept of structured values in ALGOL 68 is essentially the same concept when taken by itself as in ML-1 and ML-2 (as well as  $PL/1$ 

Sharing

and QUEST).

LGOL 68 t  $\frac{\text{int}}{\text{int}} \mathbf{x} = 3y$  $int y, zr$  $V: = X$  ) z '≴≔ ∘v ;..  $y := 4y$ **ME-4 1**  $refint = \{int \ pt\}$  $int x;$ refint y,z;  $x - 3x$  $y$  + refint[nil]; z + <u>refint[nil</u>]; ptr of  $y + x$ ; ptr of z + ptr of y; ptr of  $y + 4$ Fig. 4.3-10. An example of coercion in ALGOL 68.

arises only through the use of reference modes; assignment of structured values is done by componentwise copying. Figure 4.3-11 gives an example. The mode of z is pair; the mode of

x is ref pair. The expression (5,6) in the declaration - I Paker ing Par for z is called a structure display and simply gives values for the components of z.

i ya

ALGOL 68 mode pair = struct  $(int, a, b)$ ;  $pair z = (5, 6);$ pair x;  $X := Z$ ;  $ML-4$  $pair = [int a; int b];$  $refpair = [pair]$ pair z; refpair xy  $z + pair[5,6];$  $x + \text{refpair}[\text{pair}[n\text{min},n\text{min}]]$ a of ptr of  $x \leftarrow a$  of z; b of ptr of  $x + b$  of z Fig. 4.3-11. Structure assignment and in ALGOL 68.

The selection of components from a structure in ALGOL 68 is syntactically identical to ML-4. In fig. 4.3-11, the selection b of z, which refers to the b-component cell of z, is of mode int. There is a major complication concerning selection in ALGOL 68. We can legally form the selection b of x, where x is of reference-to-structure mode. The mode of the selection b of x is ref int, not int even though the b-component cell for the structure pointed to by x in figure 4.3-11 is of mode int. We say in this case that the

pointer is distributed over the components (in ALGOL 68 terminology, x is "endowed with subnames"). Thus, for example, the assignment bof  $x := a$  of z is legal; in the ALGOL 68 program of fig. 4.3-11 it would place the value 5 into the b-component cell of the structure pointed to by x. 化红氧化

Unfortunately, the "obvious" translation into ML-4 fails. The ML-4 type refint, defined as [int ptr], corresponds to the mode ref int, but in fig. 4.3-11 there is no cell of this type to associate to the (destination) that corresponds to the ALGOL 68 selection b of x. Thus, in translating from ALGOL 68 into ML-4, such cells must be added to the picture (these cells will hold pointers to the a di finish attitud da di sa individual components of the structure referred to by x). ា អង្គស្រុក និងតែសារ បានបានបាន ು ಕರ್ 5년) The corrected translation mechanism is shown in fig. 4.3-12; sum s an**os b**acking the



for each reference-to-structure identifier x we add to the local structure a reserved identifier x\$sub to hold the > subnames (distributed component pointers). By looking at the local structure pictured in fig. 4.3-12, we see that there are two ways to access component cells of the structure pointed to by x: through x (with (destination) b of ptr of x) as when updating the structure itself by componentwise copying; or through x\$sub (with (destination) ptr of b of x\$sub) as when explicitly selecting from x using subnames. Note that our translation conforms to the stipulations set by the ML-4 static typechecking system.

We give a final ALGOL 68 example, illustrating a recursive structured mode. The example is shown in figure 4.3-13. box is a structured mode, recursively defined, and a and b are of mode ref box. Note that the mode of the selection n of a is ref ref box. The only coercion in the program occurs in the last assignment, where a is dereferenced. A recursive mode definition such as mode badbox = struct(int v, badbox n) would be illegal; the "ref" inside the definition of the mode box, is necessary since there is no implicit nil in ALGOL 68's modes as there is with ML-4.

فيلمصها ويتطلب تشابه وسائد والمستناء

Thus we see that even with a language as complex as ALGOL 68, we can use ML-4 to make clear its approaches to the semantics of data structures.



### Completeness

In this chapter, we defined the mini-language ML-4 and used it to model data structuring facilities of the languages ALGOL W, PL/1, and ALGOL 68. As in the last chapter, we close with a few remarks on the completeness of our coverage of the approaches to data structures found in these three languages.

With ALGOL W. as with SNOBOL4 in the previous chapter, we covered nearly all the data structuring facilities thoroughly, with the exception of arrays. We comment on arrays and some of their special issues in Chapter 5.

For PL/1 and ALGOL 68, our treatment is far from complete. This is to be expected because of the sheer bulk and complexity of these two languages. There are numerous features dealing with data structures which we have not described. Yet we claim that those features which we did describe in PL/1 and ALGOL 68 constitute the "heart" of their data structuring facilities; thus our description of these features should make clear the underlying semantic approaches to data structures in these languages as well.

## Chapter<sub>5</sub>

ついかき せいしょう げばっしゅかんばん やね

うたいればい まない べいとう エコンスルジャン

### CONCLUSIONS AND EXTENSIONS

### 5.1. What We Have Done

There are a large number of programming languages which work with data structures. Because of the variety of approaches found in these languages, many subtle but important semantic distinctions crop up. With most languages, the semantics (including in particular the semantics for the data structuring facilities) are described informally in English. We consider such descriptive methods inadequate for our goals, since in many cases they fail to make clear some of the important semantic principles such as sharing. les andre del probabilità del **美国 网络无边缘的女子 化面积性 医减肥** As we have seen, a misunderstanding of the interaction beni to canval e lo the am scoutipossy p tween notions such as assignment and sharing can lead the 化水杨 医精生动脉切除术 "好!"他说道:"我想你找到这里去什么?你的人 programmer into erroneous conclusions about the effects of iv chimatori kaja ng kijad vodlodso programs.

We have therefore developed in this thesis a methodology for describing the semantics of data structures in programming languages. In order to precisely describe mechanisms found in programming languages which handle data 受到办公室的 化电子标准 化甲酸二乙基吗啡可以再加速 structures, we made use of the base language model, which is transitation of the more the hold from an wife is to

tante d'an santo

an interpretive model for formal semantics. The base lanquage model is essentially a mathematical formalism for modeling the changing states of a computing system on which various computations are performed. A mathematical treatment of the base language model is found in the Appendix; our approach emphasized the use of the base language as a programming tool similar to many conventional assembler languages. A major advantage of the base language model over other formal semantic models is that it manipulates data objects of a sufficiently general nature that we can make direct use of its data representations in our work without need for special encoding mechanisms.

The main portion of this thesis was concerned with the 分詞 (音) (字) 2012年10月 presentation and use of a series of mini-languages. With ารสุดของไรละคา ค.ศ. 5410 ผู้ใหญ่อย่าง เพิดจะปัง these mini-languages, we isolated the relevant conceptual 林村 1992年生緑、砂石や玉、サービルに abstractions such as assignment, value, construction, selection, sharing and typechecking. The mini-languages provided a "high-level" descriptive vehicle which made it simpler and more convenient to talk about semantic issues relating to data structures.

The basic structure of our methodology was to first a sa Pa <sup>1</sup>rist electronic distance make clear the semantics of our mini-languages by specifying

 $-144-$ 

stand and the complete the complete of the complete complete the complete of the complete of the complete section

linguay the creates and
their translation into the base language. Once this was done, we no longer needed to think in terms of the primitive operations of the base language. We were then able to describe the semantics of data structuring features in some programming language by simply using the appropriate minilanguage to describe how the relevant mechanisms worked.

In treating the data structuring semantics of several programming languages, we gave mini-language code into which constructs of these languages are translated. Determination of this mini-language code presents difficulties when the semantics of the source language is incompletely or ambiguously specified, reflecting the inadequacy of the descriptive methods in use. Of course, once we have obtained a consistent translation into the right mini-language, we have an unambiguous semantic specification of the relevant constructs.

Using the techniques we developed, we described the data structuring semantics of a number of representative programming languages. With the simpler languages, we were able to give a nearly complete treatment of the data structuring facilities. As to the more complex languages, we were able to cover most of the fundamental approaches to

-145-

data structures without getting caught up in the intricacies of features of relatively little semantic relevance to the issues we are concerned with. In the next section, we talk about some of the areas that were left uncovered.

# 5.2. Further Work

There are a number of semantic areas that we have not treated. In order to cover these areas, we would need to develop new mini-languages with additional mechanisms. In this section, we give brief mention to two such areas and what kinds of new mechanisms are required to treat them.

The first uncovered area is unions. With the type system of ML-4, every cell is constrained to hold values of only one type. In many programming languages, this restriction is weakened somewhat by defining union types. If type t is the union of types tl and t2, then a cell of type t can hold values of type tl as well as values of type t2. For example, suppose we declare z to be of type t in some lanquage that admits union types, and suppose that the expressions el and e2 yield values of types tl and t2, respectively. Then both the assignments  $z := e1$  and  $z := e2$  would be legal. This capability is not within the reach of the

type mechanisms we developed for ML-4. Suppose we declare x There yi a si add **nnstruper (objen**ges), shi para to be of type tl. Then the assignment  $x := z$  can be executed without type error precisely when the value of z is of type tl rather than of type t2. So in order to add to our mini-languages a capability to handle unions, some kind of additional runtime type testing mechanism must be intro- of duced into the design of the language is a change and supplied

**Construction of the Indian Beam Beam in the State** The second uncovered area is arrays. The type system a multiple of the conduction of the manual state of the second of the second of the second of the second second gen and s of ML-4 is simply not equipped to deal with arrays whose the sailed at the short bispa fait for extraget subscript bounds are flexible. The type of such an array nte lan a voca no esta città di tria rell'inglia **egeschial-**chim admini would contain structures having differing numbers of comen a gina shekara ya ke yang dalam gajakan ke praktirin fa ponents. A structured type in ML-4 requires a set of selecstada a Territoria da Gregoria da Reino a California tors which is known to the translator and cannot change. คราม การทางการ พร้าน 2 เรื่องออกซิวี (สมริมัก <mark>ถูกไฟขึ้ง</mark>คนูใน ซูร. Things 2 ซีลิติชี Even with unions, we are no better off. For instance, the AR THE THIS BELONGING HIGHLY BEEN WISHED TO LOSSER type consisting of all PAL tuples could not even be expressed ing ow' (or supposed sease and ofci as a finite union of ML-4 types, since a tuple can have any alt Bo rheakthainean in all a one of an infinite number of selector sets ({1}, {1,2}, LEVEQUE THOUGH MENT OF

 $\{1,2,3\}, \ldots$ ,  $\{1,2,\ldots,n\}, \ldots$ ).

There are many other complicated issues concerning arrays, such as different array type concepts, changeability of bounds, and assignments between fixed and flexible arrays. All of these issues introduce new complexity into the language, requiring the development of more techniques.

To sum up, our methodology for describing data structures has special advantages from each of its two portions. The use of the base language model provides for a precise, formal characterization of the semantic rules of the lanquages under study, while our mini-languages provide the convenience of high-level descriptions of the actions being modeled. In order to describe any programming language feature, all that needs to be done is construct an appropriate mini-language which handles only the concepts directly relating to that feature. The syntax and semantics of such a mini-language are naturally **easy** to work with and understand. By specifying translations from source languages into the mini-language and from the mini-language into the base language, we gain a precise but conceptually clear characterization of the semantics of the features we wish to study.

 $-148-$ 

# $-149-$

# Bibliography

- (Amer 72] Amerasinghe, S.N. The Handling of Procedure Variables in a Base Language. S.M. thesis, M.I.T. Department of Electrical Engineering, Sept. 1972.
- [Amer 73] \_\_\_\_\_\_\_. Translation of a Block Structured LangUage With Non-Local Go To Statements and Label Variables to the Base Language. M.I.T. Project MAC Computation Structures Group Memo 84, June 1973.
- [Bur 68] Burstall, R.M. Semantics of Assignment. Machine Intelligence 2, ed. E. Dale and D. Michie. Oliver and Boyd, Edinburgh, 1968, 3-20.
- [Cou 73] coueignoux, P. and Janson, P. Translation of Simula 67 into the Common Base Language. M.I.T. Project MAC Computation Structures Group Memo 87, June l.973.
- [Denn 71] Dennis, J.B. On the Design and Specification of a Common Base Language. M.I.T. Project MAC Computation Structures Group Memo 60, July 1971.
- [Denn 74] Private communication.
- [Der 74] Dertouzos, M.L. Computer Languages: Structure and Interpretation. Class notes for subject 6.031, M.I.T. Department of Electrical Engineering, Feb. 1974.
- [Dra 73] Drake, C. The Semantic Specification of SNOBOL in the Common Base Language. M.I.T. Computation Structures Group Memo 85, June 1973.
- [Earl 71] Earley, J. Towards an Understanding of Data Structures. CACM 14, 10, Oct. 1971, 617-627.
- [Ev 70] Evans, A. PAL Reference Manual and Primer. M.I.T. Department of Electrical Engineering, Feb. 1970.
- [Fenn 73] Fenner, T.I. et. al. QUEST: The Design of a Very High Level Pedagogic Programming Language. ACM SIGPLAN Notices, Feb. 1973, 3-27.
- [Floy 67] Floyd, R.W. Assigning Meanings to Programs. Proc. Symposium on Applied Mathematics. AMS,  $1967, 19-32.$
- [Gris 71] Griswold, R.E. et. al. The SNOBOL4 Programming Language, 2nd. ed. Prentice Hall, Englewood CILLES, N.J., 1971. Jolf Hundor
- [Gris 73] Griswold, R.E., and Griswold, M.T. SNOBOL4 Primer. Prentice-Hall, Englewood Cilifs, N.J., 1973. o koj tekn**erala.**<br>Virke drta op**rvi**j
- [Hoar 68] Hoare, C.A.R. Record Handling. Programming Lanquages, ed. F. Genuys. Academic Press, 1968.
- An Axiomatic Basis for Computer Programm-[Hoar 69] ing. CACM 12, 10, Oct. 1969, 576-580, 583.
- [Hoar 71] \_\_\_\_\_\_\_. Proof of a Program: FIND. CACM 14, 1,  $\sigma$ an. 1971. 39-45. PRODUCED A BANK
- [Hoar 72] \_\_\_\_\_\_. Notes on Data Structuring. Structured Programming, ed. E.W. Dijkstra. Academic Press, 1972. DIM Recampines C
- [Lan 64] Landin, P. The Mechanical Eveluation of Expressions. Computer J., 4, 1964, 308-320.
- $[lan 65]$ A Correspondence Between Algol 60 and Church's Lambde Notation. CACM B. 2, 3, Feb. and Mar. 1965, 89-101, 138-185.
- The Next 700 Programming Languages.<br>CACM 2, 3, Mar. 1966, 157-166.  $[$ Lan 66a]
- A λ-Calculus Approach. Advances in Pro- $[Lan 66b]$ gramming and Non-Winericel Computation. Pergamon Press, 1966.
- [Lau 68] Lauer, P. Formal Definition of ALGOL 60. Technical report TR25.088, IBM Laboratory, Vienna, 1968.
- [Lav 74] Laventhal, M. Verification of Programs Operating on Structured Data. M.I.T. Project MAC Technical Report TR-124, March 1974.
- [Led 71] Ledgard, H.F. Ten Mini-Languages: A Study of Topical Issues in Programming Languages. ACM Computing Surveys 3, 3, Sept. 1971.
- [Lee 72] Lee, J.A.N. Computer Semantics. Van Nostrand Reinhold, New York, 1972.
- [Lind 71] Lindsey, C.W. and van der Meulen, S.G. Informal . Introduction to ALGOL 68. Mathematisch Centrum, Amsterdam, 1971.
- [Luc 68] Lucas, P., Lauer, P. and Stigleitner, H. Method and Notation for the Formal Definition of Programming Languages. Technical Report TR25.087, IBM Laboratory, Vienna, June 1968.
- [Luc 69] Lucas, P. and Walk, K. On the Formal Description of PL/I. Annual Review of Automatic Programming  $6, 3, 1969.$
- [McC 62] McCarthy, J. et. al. LISP 1.5 Programmer's Manual. The Computation Center and Research Laboratory of Electronics, M.I.T. M.I.T. Press, Cambridge, Mass., 1962.
- [Morr 68] Morris, J.H., Jr. Lambda Calculus Models of Programming Languages. M.I.T. Project MAC Technical Report TR-57, 1968.
- 74] Mosses, P. The Mathematical Semantics of Algol  $MOS$ 60. Technical Monograph FRG-12, Oxford University Computation Lab, Programming Research Group, Jan. 1974.
- [Reyn 72] Reynolds, J.C. Definitional Interpreters for Higher-Order Programming Languages. Proc. 25th ACM National Conference, 1972, 717-740.
- ွေသက် ကို**ဝေ ကြည့်ဆုံး**ခဲ့သော ပြည်တွင် ၁ ကြီး မျဉ်းဆော်အောက်ခေါင် . Towards a Theograph Evne Structure, pre-Revn 731 lim. dragt. Syracuse Caimeraity, 1973.
- [San (73] Sanderson, J.G. The Lambda Galoulus, Dattice Theory and Reflexive Down ine, draft notes, Oxford University Committee Laboratory, Programming Research Group, 1973.
- Scott, D. Gutline of a Mathematical Theory of [Scot 70] Computation. Proc. 4th Annual Princeton Conf. on Information Sciences and Avetams, 1970. 169-**176** and 1970 and 1980 and 1980 orders
- [Scot 71] Semantics for Computer Languages. Proc. Sympordun on Commutars and Automatas Polytechnic Thstitute of Brooklyn, N.Y., 1971. 医心室的
- [Stra 66] Strachey, C. Towards a Formal Semantics. Formal Language Description Language . North-Holdand,  $\pm 2966$  . The last part of the set  $\mathbb{Z}$

ೋಯಿ ಸಾಹಿತ್ಯೆ<br>ಪರಿಣಾಮಿ ಸಾಹಿತ್ಯೆ

. Fundamental Concepts in Programming  $[Stra 67]$ Languages. NATO Conf., Copenhagen, 1967.

เปียนการจัด ช่วงนั้งมีมา ในกระจัด จะ จำกัดเกิด ส่งค์กรใช้

- [VWij 69] Van Wijngaarden, A. (ed.) Report on the Algorithmic Language ALGOL 68. Numerische Mathematik, 14, 2, 1969, 79-218.
- [VWij 73] 2000 Proposed Revised Report on the Algorithmic Language Ausok 62. MAXP, July 1973.
- [Walk 69] Walk, K. Revet als Abstract Suntay and Interpretation of RL/I. Version TEL: Technical Report TR25.098, IBM Laboratory Vienna, April 1969.
- [Weg 68] Wegner, P. Programming Languages, Information Structures and Machine Organisation. McGraw-Hill, 1968.
- 701 **Neg** nology, Computer Mathematics and Computer Science. Advances in Computers 10, 1970. **MENCHAND LANSAN ROOM**
- . Data Structure Models for Programming 711 iwea Languages. Proc. ACM Symposium on Data Structures in Programming Languages, ACM SIGPLAN Notices, Feb. 1971.
- [Weg 72a] Programming Language Semantics, Formal Semantics of Programming Languages, ed. R. Rustin. Prentice-Mall, Englewood Cliffs, N.J., 1972.
- sta Partition and the structure line, the linear Bibliother edge of the structure of a  $[Weq 72b]$ . The Vienna Definition Language. ACM Computing Surveys 4, 1, March 1972, 5-63.
- [Wir 66] Wirth, N., and Hoare, C.A.R. A Contribution to the Development of ALGOL. CACM 9, 9, Sept. 1966. August 21: Sange and that Tay Service bell 计功器 医动脉 计规则
- [Woz 69] Wozencraft, J.M., and Evans, A. Notes on Programming Linguistics. M.I.T. Department of Electrical Engineering, 1969.

人名英格兰人姓氏沃尔德住所名称来源于古英语含义是英语含义是美国英语含义是美国的变体

selek a salah kelah di sebuah pertama kelah kegada mendangan dalam k

ふまいいや風味などなに、まずいやはお食液、心をいっかけしますね。

sta sinderland erafle rammente i vid

for a limit of learn all annual axiomate

THE REAL PARTY AND REPORT OF THE REAL PARTY.

化十二烷基苯胺 医魏福德安斯福登 医红色 计立分位

a distribution of the state of the second of the state of t

### **Appendix**

A MORE FORMAL TREATMENT OF BL

#### $A.1.$ Interpreter States

ا الإل المؤود *للهام المسار بالمصارفة الإسلام الذي لا*لدية

An interpreter state embodies the information present at a given time in the computer system we are modeling. In this section we describe in detail the structure of BLgraphs representing interpreter states in the base language model. The treatment here differs somewhat from [Denn 71] and [Amer 72], but is essentially equivalent. In the next section we formalize BL-graphs and the BL instructions.

We assume that the reader is familiar with the concept of process as a locus of control. A process is represented in an interpreter state by a BL-object which we call a site of activity, or SOA. The BL-graph for an interpreter state is essentially a collection of SOA's. The root nodes of such a BL-graph are the root nodes of its SOA's. Thus an interpreter state is represented

by a BL-graph whose skeletal form is shown in fig. A.1-1.

We now describe the structure of the individual SOA's of

 $P1q. A.1-1.$ Skeletal structure of BL-graph for interpreter state

 $-154-$ 

**mar akrimin të pjesipës. L<sup>e</sup> dhe që një de nave** sa pre pjesipës nga e shpërfaqe <mark>ngërmin në prejs</mark>h

an interpreter state. A SOA is a BL-object with four components:

(1) The ep-component is a local structure, a BL-object representing the environment in which the SOA's computation takes place. (The name "ep" is an abbreviation for environment pointer.) Components of a local structure represent variables and temporaries used by the computation. Nearly all the BL instructions executed as part of the computation affect its local structure. We allow for the possibility of different SOA's sharing the same local structure, but usually the local structures of the different SOA's are distinct.

One distinguished SOA has as its ep-component a BLobject known as the universe. The universe represents the system-resident information present in the computer when no computations are in progress. Generally speaking, this information is independent of which computations are currently active or how far individual computations have progressed. This special SOA stands, so to speak, at the head of the system call chain, so that every **process** can trace its ancestry back to it. Access to the data in the universe is passed from caller to callee, so whatever access a particular SOA bas to the universe is determined by the call chain leading back to the one distinguished SOA.

Two kinds of objects are found as components in the universe: data structures and procedure structures. Each kind of object can **have** objects of either kind as components. A data structure in the model can be any arbitrary BL-object; a procedure structure is a special kind of BLobject representing a procedure **expressed** in the base language. A BL instruction **is easily represented as a** BLobject: for **example,** the instruction **conet** 3,x is depicted in figure A.1-2. The **components** 

with selectors  $1, 2, \ldots$  of a procedure structure are-simply representations of its instructions in order. A procedure structure may also have components which are procedure structures for nested procedures. Figure A.1-3 illus-



trates a <sup>1</sup> skeleton procedure structure for a procedure p with one procedure f **nested** inside.

(2) The in-component of a SOA gives the instruction currently being **executed** by the **SOA's** aomputation, as well as the procedure containing this instruction ("ip" stands

support the company of the second company

A STANDARD COMPANY AND THE RESPONDING OF THE RESIDENCE OF THE RESIDENCE OF THE RESIDENCE OF THE RESIDENCE OF THE

for instruction pointer). The ip-component *is* a twocomponent structure, whose proc-component gives the current

procedure structure from which instructions are being executed, and whose instr-component gives the number of the instruction currently being executed *in*  this procedure (fig. A.1-4). Thus the instruction currently being executed within a. SOA s is given by the dotted pathname ip.proc.\*(ip.inst), taken relative to the root node of s.

 $(3)$  The stat-component of a SOA, which gives its status, *is* an elementary object with the value 1 when the SOA is active *(i.e.* currently processing instructions), 0 if the SOA *is* dormant.

(4) The ret-component of a

SOA s shares with the SOA that invoked (created) s. When s executes a return instruction, the SOA given by the retcomponent  $of$   $s$  is activated; the current SOA is put to sleep.





rus en la permission de la provincia de la pro With the structure of an interpreter state given above, Thin they in Brail and the state defining a statement like out as we can proceed to the next section, which describes how the TOWER RESERVES STATISTICS BL instructions transform interpreter states.

nonton The collect what good took

# A.2. BL-Graphs and BL Instructions

**FOR COMPANY SHOPLOWERS COMPANY OF A REPORT OF SHOPLOW** 

in April 2012, control

 $\mathcal{J}_1, \mathcal{I}_2$ 

We give a formal mathematical definition of BL-graphs. at tedingse taing Suppose the sets ELEM (elementary objects), SEL (selectors) Sternal and Carolina and State And Archives and NODES (nodes) are given. For our purposes, ELEM shall าที่มีเป็นอยู่ให้ระบวก เรื่องขับให้เรียน เรื่อง เรื่องไป consist of integers, truth values, real numbers and strings; AND THE REAL REPORT OF PROPERTY SEL shall consist of integers and strings; and MODES shall The State Read of the State of the State Company of the State of the State of the State of the State of the St be an arbitrary countably infinite set. Strings are taken atru tous sul an estella over some suitable alphabet which includes the alphanumeric characters together with some special characters. A BL-graph over these three sets is a 4-tuple  $g = (0, R, A, V)$ on the direct with an allowing the state of in which: - 사진 사람.<br>사건



We interpret  $(\alpha, \alpha, \beta) \in A$  to mean there is a directed arc with selector  $\sigma$  leading from node  $\alpha$  to node  $\beta$ . (d, b) E V to mean a is a leaf node with elementary value 8. A BL-graph g must satisfy the following four conditions:

in Sakita

- (1) If  $\alpha \in U$ ,  $\sigma \in$  SEL, then there is at most one  $\beta \in U$ for which  $(\alpha,\sigma,\beta) \in A$ .
- (2) If  $a \in U$ , then there is at most one  $\delta \in {\texttt{ELEM}}$  for which  $(\alpha, \delta) \in V$ .
	- (3)  $pr_1(A)$   $\cap$   $pr_1(V) = \phi$ , where  $pr_1$  is the firstcomponent projection mapping. Equivalently,  $\forall \alpha \in U: \sim [\exists \delta \in \text{ELEM}: ((\alpha, \delta) \in V)]$  $\& \pi(\sigma, \beta) \in \text{SEL} \times \mathbf{U}: (\alpha, \sigma, \beta) \in \mathbf{A}$ .
- (4)  $D^{*}(R) = U$ , where  $D^{*}$  is the reflexive transitive closure of the immediate-descendant mapping D:  $2^U$   $\rightarrow$   $2^U$  defined by

 $D(S) = \{\beta \in U: \pi \alpha \in S, \sigma \in SEL \ s.t. \ (\alpha, \sigma, \beta) \in A\}.$ 

Property (1) insures unique selection. i.e. that the selectors on the arcs emerging from a node are distinct. Property (2) asserts that no node may have more than one elementary value. Property (3) says that no node may have both components and an elementary value, i.e. that elementary values can be attached only to leaf nodes. Property (4) states that every node of a BL-graph is accessible along some directed path of arcs starting with a root node.

We now give a formalism for defining transformations on BL-graphs. The formalism is based on [Denn 74); it makes use of a set ID of identifiers and a mapping  $v:$  ID U ELEM U NODES  $\rightarrow$  ELEM U NODES which assigns values

to identifiers and acts as the identity function on elemantary values and nodes. A basic transformation maps a BL-graph  $g = (U, R, A, V)$  into a new graph  $g^* = (U^*)R^T, A^T, V^T$ and updates the valuation mapping  $\sqrt{1}$  into a new mapping  $\sqrt{1}$ . The notation  $\sqrt{(\alpha/x)}$  means  $\lambda y. (y \ast x \rightarrow \alpha, \frac{true}{true} \rightarrow \sqrt{y})$ , i.e. a mapping equivalent to  $\sqrt{ }$  except that it maps x into  $\alpha$ .

The following basic transformations and auxiliary 经无利的 有螺旋 心感病 人名法 代数 functions are defined for arbitrary BL-graphs:

AddElem(a,d): [defined provided  $\alpha$   $\in$  U,  $\delta$   $\in$  ELEM, where  $\alpha = \nu(a)$ ,  $\delta = \nu(d)$ ]

 $\mathbf{V}^{\leftarrow} = \mathbf{V} \cup \mathbf{V} (\alpha, \delta) + \mathbf{V} \equiv \mathbf{U}, \mathbf{R}^{\leftarrow} = \mathbf{R} \cdot \mathbf{A}^{\leftarrow} \mathbf{R}^{\leftarrow}$ 

DeleteElem(a,d): [defined provided  $\alpha \in \mathcal{U}$ ,  $\delta \in$  firm and  $(\alpha, \delta) \in V$ , where  $\alpha = \gamma(a)$ ,  $\delta = \gamma(d)$ ]  $V' = V - ((\alpha, \delta))$ ,  $U' = U$ ,  $R' = R$ ,  $A' = A$ ,  $v' = v$ .

[defined provided  $\alpha, \beta \in U$ ,  $\sigma \in \text{SEL}$ ,  $AddArc(a,s,b):$ where  $\alpha = \nu(a)$ ,  $\sigma = \nu(a)$ ,  $\beta = \nu(b)$ ]

 $A' = A \cup \{(\alpha, \sigma, \beta)\}, U' = U, R' = R, V' = V, v' = v.$ 

 $DeleteArc(a, a, b)$ : [defined provided  $\alpha, \beta \in U$ ,  $\sigma \in SEL$  and  $(\alpha, \sigma, \beta) \in \mathbb{R}$ , where  $\alpha = \sqrt{(\alpha)}$  ,  $\sigma = \sqrt{(\alpha)}$ ,  $\beta = \nu(b)$ ]

 $A' = A - \left[ (\alpha, \sigma, \beta) \right], U' = U, R' = R, V' = V, \psi' = \nu.$ 

DeleteComps (a): (defined provided  $\alpha \in U$ , where  $\alpha = \gamma(a)$ )  $\mathbb{R}^4$  =  $\mathbb{R}$  0 (60 = 60) x SEL x U),  $U' = U'$  = U, R,  $\mathbb{R}^+$  $V^+ = V, \quad v^+ = v.$ 

Same (1999) and a same indicate

Prune:

 $U' = D^{T}(R)$ ,  $R' = R \cap U'$ ,  $A' = A \cap (U' \times \overline{SEL} \times U'')$ ,  $V' = V \cap (U' \times ELEM) \cdot V' = V_{\frac{1}{2} \times C}$ 2. 【通用事实图片图片的概念】44。 HasComp(a,s): [defined provided  $\alpha \in U$ ,  $\sigma \in SEL$ , where  $\alpha = \nu(a)$ ,  $\sigma = \nu(s)$ ] if  $\pi\beta$  (  $U:$   $(\alpha, \sigma, \beta)$  ( A then true else false. Comp(a,s) + b: [defined provided  $\alpha$  (all  $\alpha$  f SEI and Has $Comp(a,s) = true$  i.e. I $\beta$   $\in U:$   $(\alpha,\sigma,\beta) \in A$ , where  $\alpha = \nu(a)$ ,  $\sigma = \nu(a)$ ] let  $\beta$   $\in$  U such that  $(\alpha, \sigma, \beta)$   $\in$  A;  $v' = y [\beta/b], U' = U, R' = R, A' = A, V' = V.$ HasElem(a): [defined provided  $\alpha \in U$ , where  $\alpha = \alpha$  ] if  $\pi_{\delta}$  (ELEM:  $(\alpha, \delta)$   $\in$  V then true else false. Elem(a)  $\rightarrow$  d: [defined provided  $\alpha$   $\in$  U and HasElem(a) = true i.e.  $\mathbb{E}_\delta$   $\in$  ELEM:  $\{\alpha,\{\delta\}\}$   $\in$  V, where  $\alpha = \nu(a)$  ] let  $\delta$   $\epsilon$  ELEM such that  $(\alpha, \delta)$   $\epsilon$  Vp is  $\beta$  $V' = V[6/d]$ ,  $U' = U$ ,  $R' = R/\sqrt{2}$ ,  $\gg \gg \sqrt{2}$ ,  $\gg \gg \sqrt{2}$ NewNode  $\rightarrow$  a: ,你们知道要没有事得赚的TW的事。虽是是 let  $\alpha \in$  NODES - U;  $v' = v[\alpha/a], U' = U \cup {\alpha}, R' = R, A' = R, V' = V.$ MakeRoot(a): [defined provided  $\alpha \in \mathcal{U} - R$ , where  $\alpha = \mathcal{U}(\mathbf{a})$ ]  $R' = R \cup \{ \alpha \}$ ,  $U' = U$ ,  $A' = A$ ,  $V' = V$ ,  $v' = v$ .

t efficit frames mg hentit ville **am**oet ti 2019. ਕ ਦੇ ਜਣ RemoveRoot(a): [defined provided  $\alpha \in \mathbb{R} \subset \mathbb{U}$ , where  $\alpha = \gamma(a)$ ]  $\mathbf{U}^{\top} = \mathbf{U}^{\top} - \{\alpha\}, \ \mathbf{R}^{\top} = \mathbf{R}^{\top} - \{\alpha\}, \ \mathbf{A}^{\top} = \mathbf{A}^{\top} \mathbf{W}^{\top} = \mathbf{V}, \ \ \forall \ \tau \in \mathbb{V}.$ 

The following transformations are composites of basic transformations: als in a car are been most by which should be a state of

າຍ ປະເທດຕໍ່ ຜູ້ຊາຍໃນ ຊາຍໃນ **‱∨່ຊ້ອງ ມີຕໍ່}ຍວ່າ ລາວ ເຊິ່ນ ຊານ ເຊິ່ນ** ແລະ ເຊິ່ນ ແລະ ໄດ້ມາເລີ

1947年(1992年)1985年1985年(1992年)1月10日,1992年10月,10月1日,10月1日,10月1日,10月1日,10月1日,10月1日,10月1日,10月1日,10月1日,10月

 $-161-$ 

 $NewComp(a, s) \rightarrow b:$ 

[n.b. the semicolon indicates com-NewNode  $\rightarrow$  b: position of transformations, with  $AddArc(a,s,b)$ . application in the order shown]

 $DeleteComp(a, s)$ :

if HasComp(a,s) " [the composite transformation in the set braces is then  $\text{[Comp(a_1 s) + b]}$  .  $\frac{1}{\text{app}!}$  and  $\text{if the node de}$ DeleteArc(a,s,b); noted by a has a component with selector denoted by s) Prune}. Such that (e.s.

MakeEmpty(a,  $s$ )  $\rightarrow$  b:

then  $\{$  Comp $(a, e) \rightarrow b$ ;

if HasElem(b)

fmakes b denote an empty if HasComp(a,s) leaf node which is the<br>determinant of the node denoted by a}

> So the Engry Book (Send  $\pm$  then  $\sum_{i=1}^{n}$  (Elen(h),  $\rightarrow$  drawn a second

> > Deleterlem(b,d)) - passed we point

 $\mathcal{L}_{\mathcal{G}}(\mathcal{L}_{\mathcal{G}}) = \mathcal{L}_{\mathcal{G}}^{\mathcal{G}} \mathcal{L}_{\mathcal{G}}^{\mathcal{G}} \mathcal{L}_{\mathcal{G}}^{\mathcal{G}} \mathcal{L}_{\mathcal{G}}^{\mathcal{G}} \mathcal{L}_{\mathcal{G}}^{\mathcal{G}} \mathcal{L}_{\mathcal{G}}^{\mathcal{G}}$ 

else {DeleteCompa (b);

 $Prune$  } }

else NewComp $(a, s) \rightarrow b$ .

We now have the machinery to describe the action of the BL interpreter. The basic action is to pick a root node, which will be some SOA, then to execute the next instruction and hershoot sachung (given by the ip-component of the SOA) with respect to the current local structure (given by the ep-component of this SOA). Figure A.2-I illustrates the skeletal structure of a sample SOA. In the procedure we will give to define the action of the interpreter, special names are used to designate nodes in the current SOA. These names appear as labels for the nodes in fig. A.2-1.



 $\widetilde{\mathcal{X}}$  and  $\widetilde{\mathcal{Y}}$ 

Before giving a procedure which specifies the action of the BL interpreter, we define several auxiliary transforma-呼唤法医诊疗现象 化 tions. These use the special names shown in fig. A.2-1,

PickActiveRoot → Root:

let  $\alpha \in R$  such that  $\beta \in U$ :  $(\alpha, 'stat', \beta) \in A$  &  $(\beta, 1) \in V$ ;  $v' = v[\alpha / \text{root}],$   $U' = U, R' = R, A' = A, V' = V.$ Se Rudger

**合成素 オール・出**入

 $3.331 - 64$ 

af te shoots

المتهاري فالمتعاري وألوالها

 $Succ \rightarrow next$ :

 $v' = v[u+1/next], U' = U, R' = R, A' = A, V' = V.$ where  $\mathbb{E}[\mathbf{y} \cdot \mathbf{x}]$  ,  $\mathbf{y}(\mathbf{k})$  , we define the set of the speaker

f Gyn

GetNextInstr:

DeleteElem(inum, k);

AddElem(inum, next).

[defined for  $\iota \in \{0, 1, 2, \ldots\}$  = ELEM,  $\texttt{Jump}(i) \rightarrow \texttt{next}:$ where  $u = \sqrt{(1)}$ 

 $v' = v[\nu/next], U' = U, R' = R, A' = A, V' = V.$ 

Empty(a): [defined for  $\alpha \in U$ , where  $\alpha = \nu(a)$  ]

if HasElem(a)

then false

else if  $I\sigma \in \text{SEL}$ ,  $\beta \in U: (\alpha, \sigma, \beta) \in A$ 

then false

else true.

The action of the BL interpreter is specified by the repetitive application of the transformation given by the following procedure:



va sta nava ali se se s

Finally, we define the operation of all the BL instructions by giving the transformation ExecuteBLInstruction. ExecuteBLInstruction(inst): in eng  $Comp(intst, 0) \rightarrow operation;$ a kacamatan ing Kabupatèn Bangkalén case operation of /\* choose the action that matches the operation code of the instruction  $\star$  / 'create': The second of the program of the program in the  $/*$  create  $x$ Comp(inst, 1)  $\rightarrow x;$  $\star$  /  $DeleteComp(cls, x)$ ; NewComp(cls,  $x$ )  $\rightarrow$  a. うっと バーチャー うまなばな めいてつ 'clear': thave to comments. Comp(inst, 1)  $\rightarrow x$ ;  $\sqrt{\star}$  clear x  $\star/$ MakeEmpty(cls, x)  $\rightarrow$  a. is a la Delligencia 'delete': Comp(inst, 1)  $\rightarrow x;$ **Signal** มา พลา<sup>กา</sup>รา if  $-MasComp(intst, 2)$ **ディベート戦でディー**。 then DeleteComp(cls, x)  $\frac{1}{2}$  delete x  $\star$  /  $/*$  delete x, m else { $Comp(ints1, 2) \rightarrow m$ ;  $\star/$ if  $HasComp(cls,x)$ then  $\{Comp(cls,x) \rightarrow a; \ldots \in \mathbb{R} \}$  $\texttt{DeleteComp(a,m)}$ .  $\ldots$ 'const': Comp(inst, 1)  $\rightarrow$  v;  $\mathbb{R}^2$  is a set Comp(inst, 2)  $\rightarrow x;$ **Example 12 /\* const v, x**  $\star/$ MakeEmpty(cls, x)  $\rightarrow$  a; 一、会身之人  $AddElement(a, v)$ . 'add':  $\mathbb{R}^{n\times n}$  is a subset of  $\mathbb{R}^{n\times n}$  . Comp(inst, 1)  $\rightarrow x$ ; Comp(inst, 2)  $\rightarrow$  y;

 $-165-$ 

```
Comp(intst, 3) \rightarrow z_7\sqrt{\phantom{a}} add x, y, z
Comp(cls, x) + a; Comp(cls, y) + b;
Elem(a) \rightarrow d; Elem(b) \rightarrow e; and the set of
MakeEmpty(cls, z) + c;
AddElement(c, y(d)+y(e)).
   /* other arithmetic instructions are similar
```

```
'link':
   Comp(inst, 1) \rightarrow x;Comp(inst, 2) \rightarrow n;
   Comp(inst.3) + y;
                                                     \sqrt{2 \ln k} x, n, yComp(cls, x) \rightarrow a; Comp(cls, y) \rightarrow b;
   if HasElem(a)
      then (Elem(a) \rightarrow d; DeleteElem(a,d)}
                                        1. 中国的复数 10 11 6 20 11 12 13 1
      else DeleteComp(a, n);
                                           The fact beaches of
   Addarc(a, n, b).
'select':
   Comp(intst, 1) \rightarrow x;Comp(1nst, 2) \rightarrow n;Comp(inst, 3) \rightarrow y;
                                                    \frac{x}{x} select x, n, y */
   Comp(cls, x) \rightarrow a;
   if -HasComp(a, n)then fif HasElem(a)
                 then f = \text{Lem}(a) + d;
                         DeleteElem(a,d) \frac{1}{2}NewComp(a,n) \rightarrow b}
      else Comp(a, n) \rightarrow b.
```
'apply':

Comp(inst, 1) +  $p_7$ 

 $\star/$ 

 $\star/$ 

```
Comp(inst,2) \rightarrow x; /* apply p,x */
```
 $Comp(cls, p) \rightarrow proc; Comp(cls, x) \rightarrow arg;$ 

 $Comp(proc, 'Stext') \rightarrow t;$ 

NeWNode ➔ newsoa;

Newcomp(newsoa,'ep') ➔ newels;

AddArc(newcls, '\$par', arg);

 $NewComp(newsoa, 'ip') \rightarrow newip;$ 

AddArc(newip,'proc',t);

 $Newtonp(newip, 'inst') \rightarrow newinum;$ 

AddElem(newinum,1);

NewComp(newsoa,'stat') → newstat;

AddElem(newstat,1);

AddArc(newsoa,'ret',root);

MakeRoot(newsoa);

 $Comp(root, 'stat') \rightarrow stat;$ 

DeleteElem(stat, 1); AddElem(stat, 0).

'return':

Comp(root,'ret') ➔ oldsoa;

Comp(oldsoa, 'stat') → oldstat;

DeleteElem(oldstat,O); **AddElem(oldstat,1);** 

\*/

\*/

RemoveRoot(root); Prune.

'move':

```
Comp(inst,1) \rightarrow f;Comp(inst,2) \rightarrow x;
```
 $Comp(proced, f) \rightarrow a;$ 

DeleteComp(cls,x); **AddArc(cls,x,a).** 

'goto':

```
Comp(inst, 1) \rightarrow \ell;
```
 $Jump(f) \rightarrow next.$ 

18、清爽性

and the second pro-

有时候的 计子程序

 $/*$  move  $f.x$ 

 $/*$  goto  $\ell$ 

```
'elem?':
    Comp(inst, 1) \rightarrow x;Comp(inst;2) \rightarrow i;
    Comp(cls, x) \rightarrow a;
    if -HasElem(a)
       then \texttt{Jump}(t) \rightarrow \texttt{next}.'empty?':
    Comp(\texttt{inst},1) \rightarrow x;Comp(intst, 2) \rightarrow t;Comp(cl.s, x) + a_{f} and a_{f} are a_{f} and a_{f}if -Empty(a)
       then \text{Jump}(t) \rightarrow \text{next.}'nonempty?':
    Comp(intst, 1) \rightarrow xComp(inst, 2) \rightarrow \mathbf{r}Comp(cls, x) \rightarrow a;if Empty(a)
       then Jump(t) \rightarrow next.
leg?l:
              医精神的 医磨牙
    Comp(intst, 1) \rightarrow x;Comp(inst, 2) \rightarrow y;
    Comp(inst, 3) \rightarrow \ell;
    \texttt{Elam}(x) \rightarrow d; \texttt{Elam}(y) \rightarrow e;
    if v(d) \neq v(e)then \texttt{Jump}(t) \rightarrow \texttt{next}.
                                              goran.
Thas?":
    Comp(inst, 1) \rightarrow x;
```
 $Comp(\texttt{inst.2}) \rightarrow m$ 

Subscription

かいほうしょういた

 $'$ \* elem? x, $t$ 

2. 编卷程 计实施设备 不可

Stephen Stern

 $/$ \* empty?  $x, t$ 

 $\mathcal{L}_{\mathcal{A}}\mathcal{L}_{\mathbf{X}}\mathcal{L}_{\mathbf{X}}=\mathcal{L}_{\mathcal{A}}\mathcal{L}_{\mathcal{A}}\mathcal{L}_{\mathcal{A}}\mathcal{L}_{\mathcal{A}}$ 

the commission of the will

The Post Late of Product 12 (2010) and

standard (geld a teach

 $\sqrt{2}$  nonempty? x,  $\ell$  \*/

 $\frac{1}{x}$  eq? x, y, t

化 10 钟

 $\star$ .

 $\star/$ 

 $\star$  /

Comp(inst.3)  $\rightarrow \ell$ :  $\sqrt{\star}$  has?  $x, m, \ell$  $\star$  / if -Hascomp(x,m) and a constant of the sum of the state of the then Jump (£) -> next: Man and where we have the set of the distribution is a more of the second control.  $'same?':$ Comp(inst, 1)  $\rightarrow x_i$ STERING ANGLE OUTLE CATE  $Comp(intst, 2) \rightarrow y;$  $\gamma$  same?  $\chi$ ,  $\gamma$ ,  $t$ Comp(inst.3)  $+1$ .  $\mathbf{if} \ \mathbf{v}(\mathbf{x}) \neq \mathbf{v}(\mathbf{y})$ then Jump(2) + next. All add at as go the second les /\* other comparison instructions are similar \* / H. O. L. Toshlvong henidshl (fr.s. more はてあい。 ちしゃしょ (のをしい 'getc':  $Comp(intst, 1) \rightarrow x;$ comp(inst.2) + it assessed between being reasonable Comp(inst, 3)  $\rightarrow$   $\ell$ ;  $\frac{x}{x}$  get  $x, x, t$ Comp(cls, x)  $\rightarrow$  a; MakeEmpty(cls, i)  $\rightarrow$  b; ுலான் கூடிய நிக்கி கேன் அனிகின் பிரி if HasUnmarkedComps(a) then feetumarked comp (a) with the side for the state  $Mark(a, s)$ ; Theoretic Landon advantage of Grift AddElem(b,s) } **else {UrmarkCompsOf(a)}** with an additional her Jump(4) + next}. Here are said , added the constant

endcase

This completes the definition of the transformation ExecuteBLInstruction. The getc instruction, however, requires some special additional mechanisms, which we now show.

and the annihilation of the control of the

HasUnmarkedComps(a): [defined provided  $\alpha \in U$ , where  $\alpha = \alpha$ (a)] if  $\mathbb{E}\sigma \in \text{SEL}: (\alpha, \sigma, \beta) \in \mathcal{A}$  for some  $\beta \in \mathcal{I}$ . and  $\sigma \notin$  MARKSET  $(\alpha)$ 

then true else false.

GetUnmarkedComp(a)  $\rightarrow$  s: [defined provided  $\alpha$   $\in$  U and HasUnmarkedComps (a) = true, where  $\alpha = \nu(a)$ ]

let  $\sigma \in$  SEL be as in the HasUnmarkedComps predicate;  $v' = v[\sigma/s].$ 

Mark(a,s): [defined provided  $\alpha$   $\in$  U and  $\sigma$   $\in$  SEL, where  $\alpha = \nu(a), \sigma = \nu(a)$ ]

MARKSET  $(\alpha)$  + MARKSET  $(\alpha)$  U  $\{\sigma\}$ .

UnmarkCompsOf(a): [defined provided  $\alpha \in U$ , where  $\alpha = \nu(a)$  ] MARKSET  $(a)$   $\div a$ .

We observe that each node  $\alpha \in U$  has a set MARKSET( $\alpha$ ) associated with it. All such marksets are initially empty.

There is one final remark to be made. Although our definitions of the BL instructions contain many composite transformations, the interpreter is to regard the effect of a BL instruction as an indivisible unit.