Macro Design Models for a Single Route

Outline

- **1. Green Line Dwell Time Model**
- **2. Introduction to analysis approach**
- **3. Bus frequency model**
- **4. Bus size model**
- **5. Stop/station spacing model**

Models with Crowding Term

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Predicted Dwell Times

Findings

- **• Dwell times for ALRVs are quite sensitive to:**
	- **• Passenger flows**
	- **• Passenger loads**
- **• The crowding effect may well be non-linear.**
- **• Dwell times for multi-car trains are different form those for one-car trains.**
- **• The dwell time functions suggest high sensitivity of performance to perturbations**
- **• Effective real-time operations control essential**
- **• Running mixed train lengths dangerous**
- **• Simulation models of high frequency, high ridership light rail lines need to include realistic dwell time functions.**

Introduction to Analysis Approach

- **• Basic approach is to establish an aggregate total cost function including:**
	- **• operator cost as** *f***(design parameters)**
	- **• user cost as** *g***(design parameters)**
- **• Minimize total cost function to determine optimal design parameter (s.t. constraints)**

Variants include:

- **• Maximize service quality s.t. budget constraint**
- **• Minimize consumer surplus s.t. budget constraint**

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Bus Frequency Model: the Square Root Model

Problem: define bus service frequency on a route as a function of ridership

Total Cost = operator cost + user cost

$$
Z = c \cdot \frac{t}{h} + b \cdot r \cdot \frac{h}{2}
$$

where $Z = \text{total}$ (operator + user) cost per unit time

 $c =$ operating cost per unit time

 $t =$ round trip time

 $h =$ headway – the decision variable to be determined

 b = value of unit passenger waiting time

 $r =$ ridership per unit time

Minimizing *Z* w.r.t. *h* yields:

$$
h = \sqrt{\frac{2ct}{br}} \text{ or } \sqrt{2\left(\frac{c}{b}\right)\left(\frac{t}{r}\right)}
$$

Square Root Model (cont'd)

This is the Square Rule with the following implications:

- **• high frequency is appropriate where (cost of wait time/cost of operations time) is high**
- **• frequency is proportional to the square root of ridership per unit time for routes of similar length**

Ridership Frequency Capacity Constant Load Factor

Frequency-Ridership Relationship

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Square Root Model (cont'd)

• load factor is proportional to the square root of the product of ridership and route length.

Bus Capacity-Ridership Relationship

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Square Root Model (cont'd)

Critical Assumptions:

- **• bus capacity is never binding**
- **• only frequency benefits are wait time savings**
- **• ridership** ≠ *f* **(frequency)**
- **• simple wait time model**
- **• budget constraint is not binding**

Possible Remedies:

- **• introduce bus capacity constraint**
- **• modify objective function**
- **• introduce** *r=f(h)* **and re-define objective function**
- **• modify objective function**
- **• introduce budget constraint**

Bus Frequency Example

- **If:** *c* **= \$90/bus hour,**
	- *b* **= \$10/passenger hour.**
	- *t* **= 90 mins,**
	- *r* **= 1000 passengers/hour,**

Then: h_{OPT} = 11 mins

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Bus Size Model

Problem: define optimal bus size on a route

Assumptions:

- **• Desired load factor is constant**
- **• Labor cost/bus hour is independent of bus size**
- **• Non-labor costs are proportional to bus size**
- **• Bus dwell time costs per passenger are independent of bus size**

Using same notation as before plus:

- *w* **= labor cost per bus hour**
- *p =* **passenger flow past peak load point**
- *k* **= desired bus load - the decision variable to be determined**

Then
$$
Z = w \cdot \frac{t}{h} + b \cdot r \cdot \frac{h}{2}
$$

\nNow $h = \frac{k}{p}$ by assumption above
\n
$$
\therefore Z = \frac{wtp}{k} + \frac{brk}{2p}
$$
\nMinimizing Z w.r.t. **k** gives: $k_{OPT} = \sqrt{\frac{2p^2wt}{rb}}$

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Bus Size Model (cont'd)

Result is another square root model, implying that optimal bus size increases with:

- **• round trip time**
- **• ratio of labor cost to passenger wait time cost**
- **• peak passenger flow**
- **• concentration of passenger flows**

Previous example extended with:

- *p* **= 500 pass/hour,**
- **w = \$40/bus hour;**

all other parameters as before:

Then: h_{OPT} = 55

Stop/Station Spacing Model

Problem: determine optimal stop or station spacing

Trade-off is between walk access time (which increases with station spacing), and in-vehicle time (which decreases as station spacing increases) for the user, and operating cost (which decreases as station spacing increases)

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Stop/Station Spacing Model (cont'd)

$$
Z = \frac{T_{st}}{s} (c + N \cdot v) + \frac{c_s}{s} + \frac{s}{4} \cdot D \cdot \frac{v_{acc}}{w}
$$

Minimizing Z w.r.t. s gives:

$$
s_{OPT} = \left[\frac{4w}{Dv_{acc}} \left[c_s + T_{st} (c_v + Nv) \right] \right]^{1/2}
$$

Yet another square root relationship, implying that station/stop spacing increases with:

- **• walk speed**
- **• station/stop cost**
- **• time lost per stop**
- **• vehicle operating cost**
- **• number of passengers on board vehicle**
- **• value of in-vehicle time**

and decreases with:

- **• demand density**
- **• value of access time**

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Bus Stop Spacing

U.S. Practice

- **200 m between stops (8 per mile)**
- **shelters are rare**
- **little or no schedule information**

European Practice

- **320 m between stops (5 per mile)**
- **named & sheltered**
- **up to date schedule information**
- **scheduled time for every stop**

Stop Spacing Tradeoffs

- **Walking time**
- **Riding time**
- **Operating cost**
- **Ride quality**

Walk Access: Block-Level Modeling

Results: MBTA Route 39*

Adapted from: Furth, P.G. and A. B. Rahbee, "Optimal Bus Stop Spacing Using Dynamic Programming and Geographic Modeling." Transportation Research Record 1731, pp. 15-22, 2000.

AM Peak Inbound results •**Avg walking time up 40 s** •**Avg riding time down 110 s** •**Running time down 4.2 min** •**Save 1, maybe 2 buses**

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Bus Stop Locations and Policies

- **Far-side (vs. Near-side)**
	- **• less queue interference**
	- **• easier pull-in**
	- **• fewer ped conflicts**
	- **• snowbank problem demands priority in maintenance**
- **• Curb extensions benefit transit, peds, and traffic (0.9 min/mi speed increase)**
- **• Pull-out priority (it's the law in some states)**
- **• Reducing dwell time (vehicle design, fare collection, fare policy)**