



2 a) THERE ARE 10 SINGLE PARTICLE STATES INCLUDING SPIN.  
 # 3-PARTICLE STATES = # WAYS OF CHOOSING 3 FROM 10  
 WHEN ORDER DOES NOT MATTER =  $10 \times 9 \times 8 / (3 \times 2 \times 1) = \underline{\underline{120}}$

b)  $E = \Delta$ : 2 ELECTRONS IN a, 1 IN b OR c  $\rightarrow$  4 STATES  
 $E = 1.5\Delta$ : 2 ELECTRONS IN a, 1 IN d OR e  $\rightarrow$  4 STATES

$$\underline{\underline{Z = 4e^{-\Delta/RT} + 4e^{-1.5\Delta/RT} + \dots}}$$

c)  $E = 4.5\Delta$ : 3 ELECTRONS IN d AND e  $\rightarrow$  4 STATES  
 $E = 4\Delta$ : 2 ELECTRONS IN d AND/OR e  $\rightarrow$  6 WAYS  
AND 1 ELECTRON IN b OR c  $\rightarrow$  4 WAYS  
 $\Rightarrow 6 \times 4 = 24$  STATES

$$Z = \dots + \underline{\underline{24e^{-4\Delta/RT} + 4e^{-4.5\Delta/RT}}}$$

d)  $k \ln 4$

e)  $k \ln 120$

f)  $C(T) \rightarrow 0$   $T \rightarrow \infty$  SINCE THE TOTAL ENERGY HAS AN UPPER BOUND  
 UPPER BOUND

g-b)  $E = 0$ : ALL 3 BOSONS IN a  $\rightarrow$  1 STATE  
 $E = \Delta$ : 2 BOSONS IN a, 1 IN b OR c  $\rightarrow$  2 STATES

$$\underline{\underline{Z = 1 + 2e^{-\Delta/RT} + \dots}}$$

g-c)  $E = 4.5\Delta$ : 3 BOSONS IN d AND/OR e  $\rightarrow$  4 STATES

$E = 4.0\Delta$ : 2 BOSONS IN d AND/OR e  $\rightarrow$  3 WAYS

AND 1 BOSON IN b OR c  $\rightarrow$  2 WAYS

$\Rightarrow 3 \times 2 = 6$  STATES

$$Z = \dots + \underline{\underline{6e^{-4\Delta/RT} + 4e^{-4.5\Delta/RT}}}$$

g-d)  $S(0) \rightarrow k \ln 1 = 0$

g-f)  $C(T) \rightarrow 0$  SINCE THE TOTAL ENERGY HAS AN  
 $T \rightarrow \infty$  UPPER BOUND

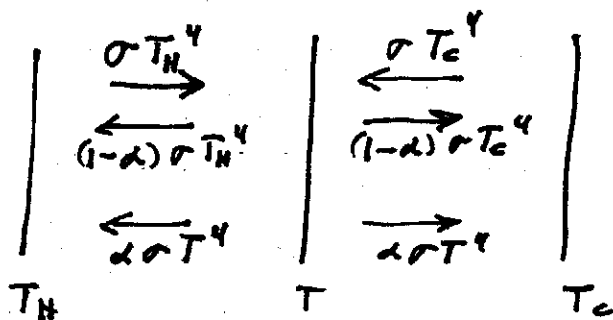
g-a) FOR INFORMATION ONLY!

THE TOTAL NUMBER OF STATES = THE # OF WAYS  
OF PUTTING 3 SPINLESS BOSONS IN 5 SPATIAL  
STATES = # WAYS OF PUTTING 3 BALLS IN  
5 DIFFERENT BOXES WHEN ORDER DOES NOT  
MATTER = # WAYS OF ORDERING 3 BALLS AND  
4 PARTITIONS WHEN THE ORDER OF THE BALLS  
DOES NOT COUNT

$$= \frac{7!}{(7-3)!} \times \frac{1}{3!} = \frac{7 \cdot 6 \cdot 5}{3 \cdot 2 \cdot 1} = \underline{\underline{35}}$$

IN PARTICULAR THERE ARE 5 WAYS OF PUTTING ALL  
3 BOSONS IN THE SAME STATE,  $5 \times 4 = \underline{20}$  WAYS OF  
PUTTING 2 IN 1 STATE AND 1 IN ANOTHER, AND  
 $5 \times 4 / 2! = \underline{10}$  WAYS OF PUTTING EACH IN A SEPARATE STATE.

3 a)



$$\frac{e}{\alpha} = \sigma T^4$$

$$\Rightarrow e = \alpha \sigma T^4$$

$$T_H^4 - (1-\alpha)T_H^4 - \alpha T^4 = -T_C^4 + (1-\alpha)T_C^4 + \alpha T^4$$

$$\alpha T_H^4 + \alpha T_C^4 = 2\alpha T^4$$

$$T^4 = \frac{T_H^4 + T_C^4}{2}$$

b)  $\sigma \alpha T_H^4 - \sigma \alpha T^4 = \alpha \sigma (T_H^4 - T^4) = \frac{\alpha \sigma}{2} (T_H^4 - T_C^4)$

J IN ABSENCE OF SHEET =  $\sigma (T_H^4 - T_C^4) \equiv J_0$

$$J_{\text{SHEET}} = \frac{\alpha}{2} J_0 = \underbrace{\left(\frac{1-\tau}{2}\right)}_{\sigma_f} J_0$$

4

THE ENTROPY OF THE IDEAL PARAMAGNET DEPENDS ON H AND T ONLY THROUGH THE RATIO  $\eta = \frac{\text{LEVEL SPACING}}{kT} \propto H/T$

ADIABATIC  $\Rightarrow$  CONSTANT S  $\Rightarrow$  CONSTANT H/T  $\Rightarrow T \propto H$

$$\frac{H_f}{H_i} = \frac{20}{8,000} = \frac{1}{400} \Rightarrow T_f = \frac{1}{400} T_i = \frac{1}{400} K = \underline{\underline{2.5 \text{ mK}}}$$

NOTE: SINCE THE SPIN SYSTEM IS USUALLY SATURATED AT THE BEGINNING OF SUCH AN EXPERIMENT, ARGUMENTS BASED ON THE CURIE LAW ARE NOT SUFFICIENT.