

Problem 9.2

A small channel is $h = 5$ cm deep and $b = 10$ cm wide. It carries flow at $U = 10$ cm s^{-1} . The stream-wise coordinate is x . The vertical coordinate is z , with $z = 0$ at the bed and positive upward. A continuous source of dye is injected at a rate of $\dot{m} = 1$ g s^{-1} at mid-depth and mid-width, and at $x = 0$. Assume that the channel has no dye upstream of the injection point. The bed of the channel is a perfect absorber for the dye, such that the concentration of dye in equilibrium with the bed is zero, and thus $C(z=0) = 0$. The molecular diffusivity for the dye is $D = 10^{-5}$ $\text{cm}^2 \text{s}^{-1}$. What is the maximum concentration in the channel 20 m downstream of the source?