



NOW EVALUATE EQ 4 FOR THIS CONTROL VOLUME

$$(A) \frac{d}{dt} \int_{CV} C dV = - \int_{CS} C \vec{V} \cdot \vec{n} dA + \int_{CS} D_n \frac{dC}{dn} dA \pm S$$

BECAUSE WE ASSUME STEADY STATE,  $d/dt = 0$ , THE FIRST TERM IS ZERO

NO SOURCE OR SINK IS MENTIONED,  $\therefore$  SET  $S = 0$

WE EVALUATE THE TWO SURFACE INTEGRALS,  $\int_{CS}$ , AT THE THREE INDICATED AREAS OF FLUX

NOTE THAT WE PLACED THE SURFACE 1, 2, 3 FAR ENOUGH INTO THE PIPES THAT  $dC/dn = 0$  AT EACH

SURFACE  $\therefore$  THERE IS NO DIFFUSIVE FLUX, TERM 3 = 0

EVALUATING TERM 2 AT EACH FLUX AREA

$$(B) 0 = + u_1 A_1 C_1 + u_2 A_2 C_2 - u_3 A_3 C_3$$

FROM CONSERVATION OF FLUID MASS (CONTINUITY) WE ALSO HAVE  $u_1 A_1 + u_2 A_2 = u_3 A_3$  FOR INCOMPRESSIBLE FLOW. USING THIS TO REPLACE  $u_3 A_3$  IN (B) AND SOLVING FOR  $C_3$

$$(C) C_3 = \frac{u_1 A_1 C_1 + u_2 A_2 C_2}{(u_1 A_1 + u_2 A_2)}$$

$$\text{OR, } C_3 = \frac{(20 \frac{\text{cm}}{\text{s}})(10 \text{cm}^2)(9 \text{mg/l}) + (10 \frac{\text{cm}}{\text{s}})(10 \text{cm}^2)(0 \text{mg/l})}{(20 \frac{\text{cm}}{\text{s}})(10 \text{cm}^2) + (10 \frac{\text{cm}}{\text{s}})(10 \text{cm}^2)}$$

$$C_3 = \frac{20}{30} * 9 \text{mg/l} = 6 \text{mg/l}$$