An Algorithm for Computing the Symmetry Point of a Polytope

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Abstract—Given a closed convex set $C$ and a point $x$ in $C$, let $\text{sym}(x, C)$ denote the symmetry value of $x$ in $C$, which essentially measures how symmetric $C$ is about the point $x$. Denote by $\text{sym}(C)$ the largest value of $\text{sym}(x, C)$ among all $x$ in $C$, and let $x^*$ denote the most symmetric point in $C$. These symmetry measures are all invariant under linear transformation, change in inner product, etc., and so are of interest in the study of the geometry of convex sets and arise naturally in the evaluation of the complexity of interior-point methods in particular. Herein we show that when $C$ is given by the intersection of halfspaces, i.e., $C = \{x \mid Ax \leq b\}$, then $x^*$ as well as the symmetry value of $C$ can be computed by using linear programming. Furthermore, given an approximate analytic center of $C$, there is a strongly polynomial-time algorithm for approximating $\text{sym}(C)$ to any given relative tolerance.

[Full Text Not Available]