

**22.351 Systems Analysis of the Nuclear Fuel Cycle**  
**Spring 2003**  
**Problem #9**

If you review Sections 3.4 and 3.8 of the “Linear Reactivity Model for Nuclear Fuel Management”, you will find that if the reactivity is assumed to follow a linear function of burnup,  $B$ :

$$\rho = \rho_0 - A B, \text{ where } A \text{ is a constant}$$

The equilibrium batch discharge for equal power sharing among assemblies can be approximated by:

$$B = \frac{2n}{n+1} \left[ \frac{\rho_0}{A} \right], \text{ where } n \text{ is the number of batches. (See pp. 73-79 and 88 – 90 in Excerpts from “Linear Reactivity” that is separately posted)}$$

An approximate power sharing ratio (local assembly power to core average power) relation is given by:

$$F_i = 1 + \frac{\rho_i}{\rho_0}$$

Where  $\rho_i$  = average reactivity over cycle  $i$  and  $\rho_0$  is a linearized constant that is dependant on the region size containing assemblies of similar power

For BWRs, with smaller unit assemblies than a PWR,  $\rho_0 = 0.35$

Question: Compare the steady-state cycle burnups of four-batch BWRs operated in the following two modes:

- (1) Uniform power throughout irradiation
- (2) A power sharing sequence of 1.2, 1, 1, 0.8 (freshest to oldest batches) for the remainder.

Assembly reactivity, including leakage, is given by

$$\rho = 0.20 - 10^{-2} B.$$