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Silvio Micali

# A Useful Homomorphic Encryption Method

Silvio Micali  
CSAIL, MIT  
silvio@csail.mit.edu

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In its full generality, homomorphic encryption (HE) is a form of encryption enabling the evaluation of a given function  $F$  on a plaintext by running another function  $F'$  on the ciphertext. The existence of such a general scheme was proved by Gentry at STOC 2009 based on lattice assumptions.

We consider HE as a way for a party  $A$  to run a secret program  $P$  of another party  $B$  on data of party  $A$  (and  $B$ ). In essence this is so because  $F$  could be taken to be the universal Turing machine (or a suitable circuit version of it), the plaintext to be  $B$ 's secret program  $P$ .

We now consider the useful choice of  $P$ : namely, the program that, on input  $x$ , outputs both  $h(x)$  and the GMR signature of  $h(x)$ . Here  $h$  could be a collision-resistant function —e.g., one randomly chosen by  $B$  in a given family. By GMR signature we mean a non-existentially forgeable digital signature scheme under a chosen message attack. In essence  $P$  has embedded the secret signing key of the GMR scheme. The corresponding public key may or may not be made public. The same is true about function  $h$ .

We'll elaborate on the merits of this method later on.

