

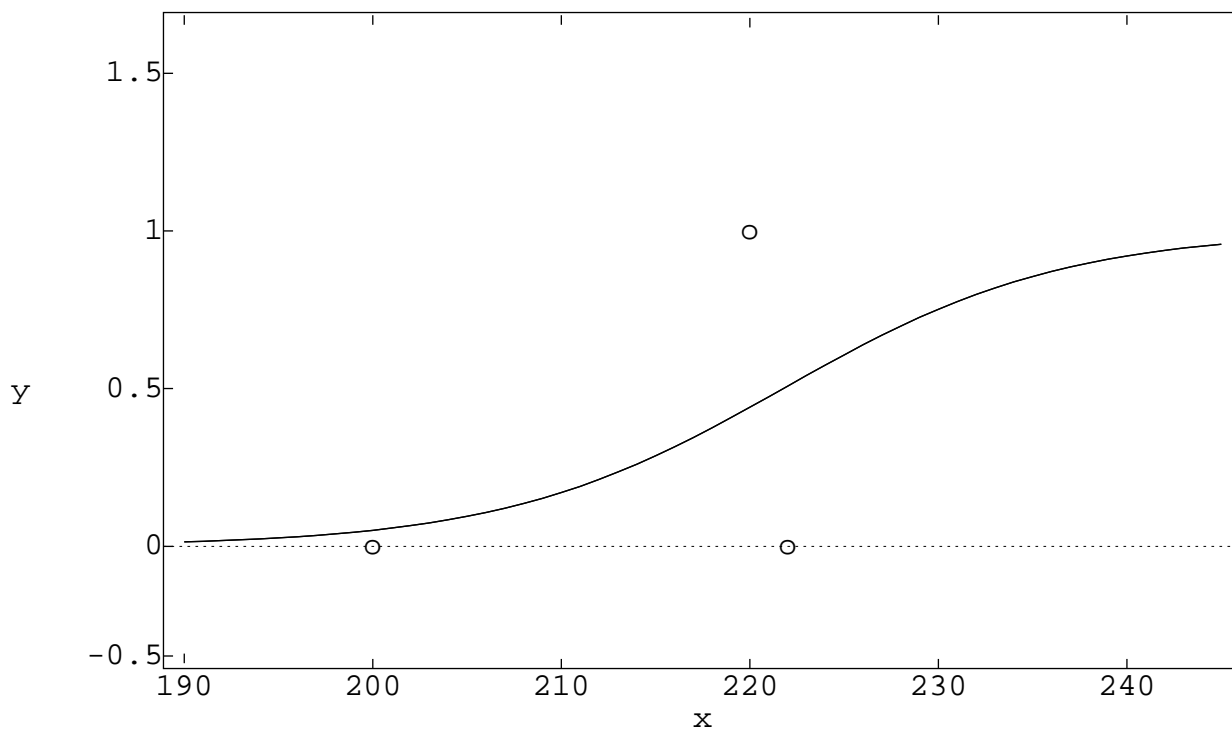


## 18.441 : Statistical Inference

### Spring 2002



In regard to #5 on the 11th problem set, see the graph.



The logistic curve must either approach 1 as  $x$  goes to infinity and approach 0 as  $x$  goes to minus infinity, or vice versa, or remain constant.

The best-fitting such curve has a  $y$ -value near  $1/2$  when  $x$  is 221, because half of the observed  $y$ -values in that vicinity are 1 (and the other half are zero). It has a  $y$ -value near 0 when  $x$  is 200, since the one  $y$ -value in that vicinity is 0. One could achieve a better fit near 200 that makes the  $y$ -value there even closer to 0, but only at the expense of making the curve much steeper near 221, so that it would be closer to 1 at 222 (making the fit worse at that point) and closer to 0 at 220 (also making the fit worse at that point).

Alpha is positive since the  $y$ -value of  $1/2$  near  $x=221$  is bigger than the  $y$ -value of 0 near  $x=200$ , so  $y$  increases as  $x$  increases.