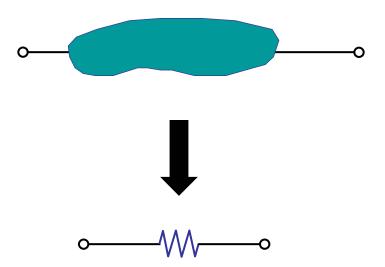


The Digital Abstraction

Review

 Discretize matter by agreeing to observe the lumped matter discipline



Lumped Circuit Abstraction

 Analysis tool kit: KVL/KCL, node method, superposition, Thévenin, Norton (remember superposition, Thévenin, Norton apply only for linear circuits)



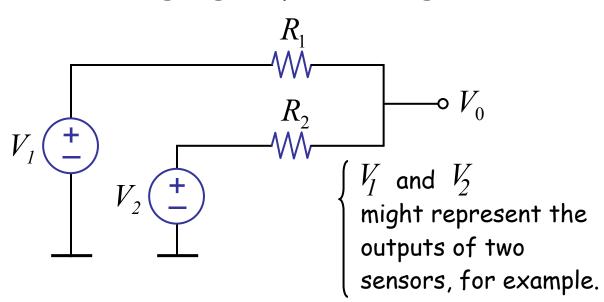
Discretize value \longrightarrow Digital abstraction

Interestingly, we will see shortly that the tools learned in the previous three lectures are sufficient to analyze simple digital circuits

Reading: Chapter 5 of Agarwal & Lang

But first, why digital? In the past ...

Analog signal processing



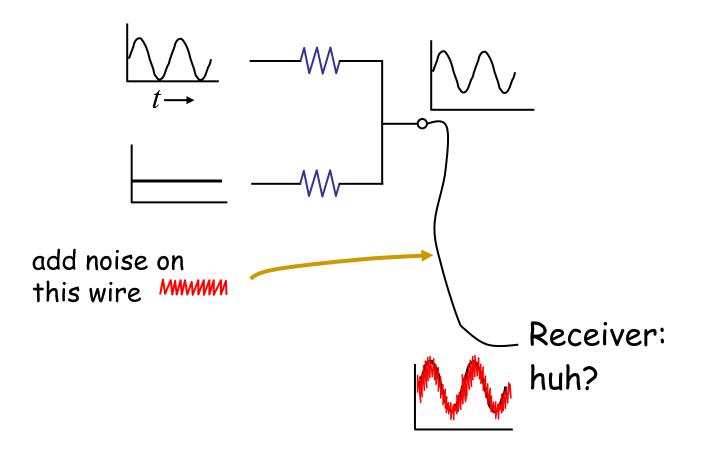
By superposition,

$$V_0 = \frac{R_2}{R_1 + R_2} V_1 + \frac{R_1}{R_1 + R_2} V_2$$

If
$$R_1 = R_2$$
, $V_0 = \frac{V_1 + V_2}{2}$

The above is an "adder" circuit.





... noise hampers our ability to distinguish between small differences in value — e.g. between 3.1V and 3.2V.

Value Discretization

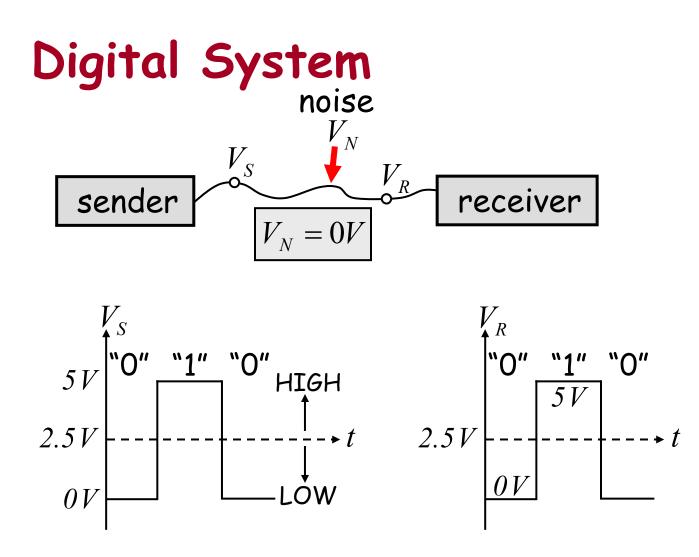
Restrict values to be one of two

HIGH	LOW
5V	OV
TRUE	FALSE
1	0

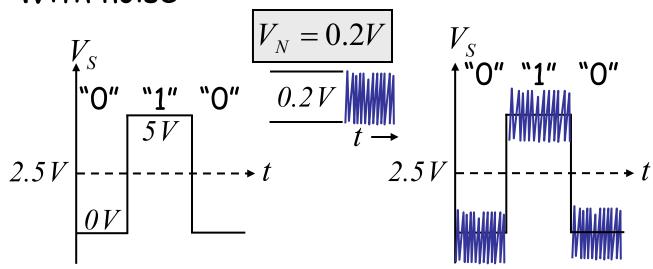
...like two digits 0 and 1

Why is this discretization useful?

(Remember, numbers larger than 1 can be represented using multiple binary digits and coding, much like using multiple decimal digits to represent numbers greater than 9. E.g., the binary number 101 has decimal value 5.)



With noise

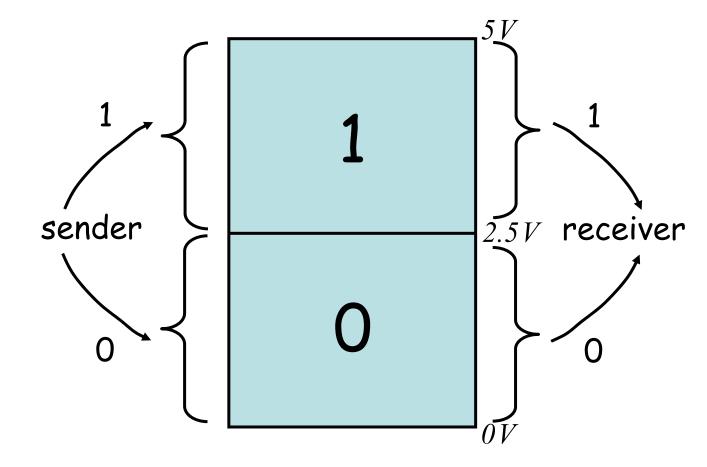


Digital System

Better noise immunity Lots of "noise margin"

For "1": noise margin 5V to 2.5V = 2.5VFor "0": noise margin 0V to 2.5V = 2.5V

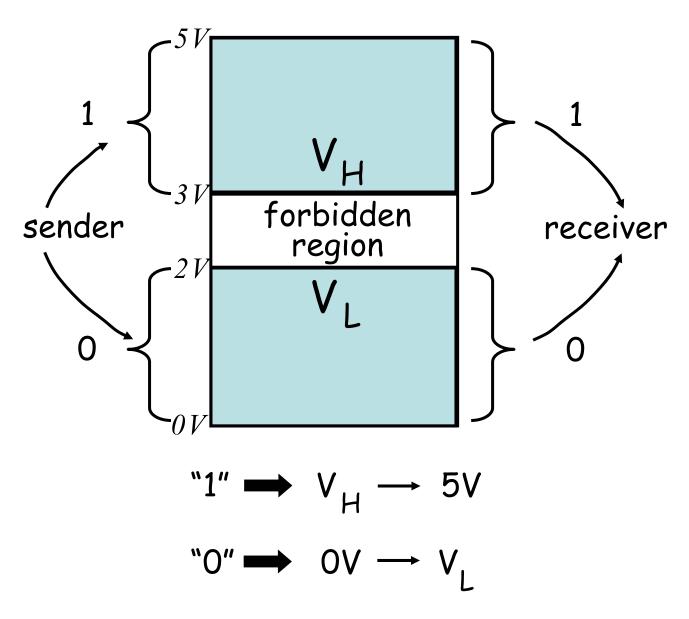
Voltage Thresholds and Logic Values



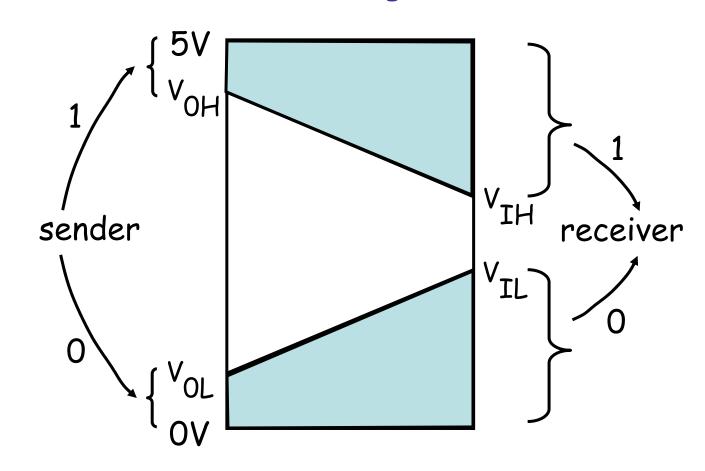
But, but, but ... What about 2.5V?

Hmmm... create "no man's land" or forbidden region

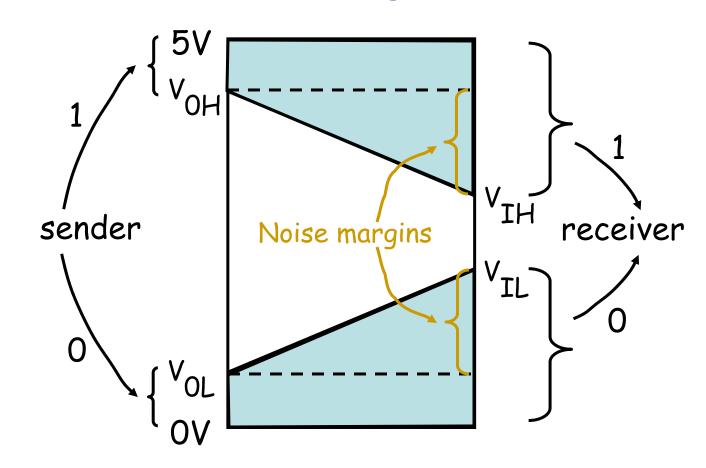
For example,



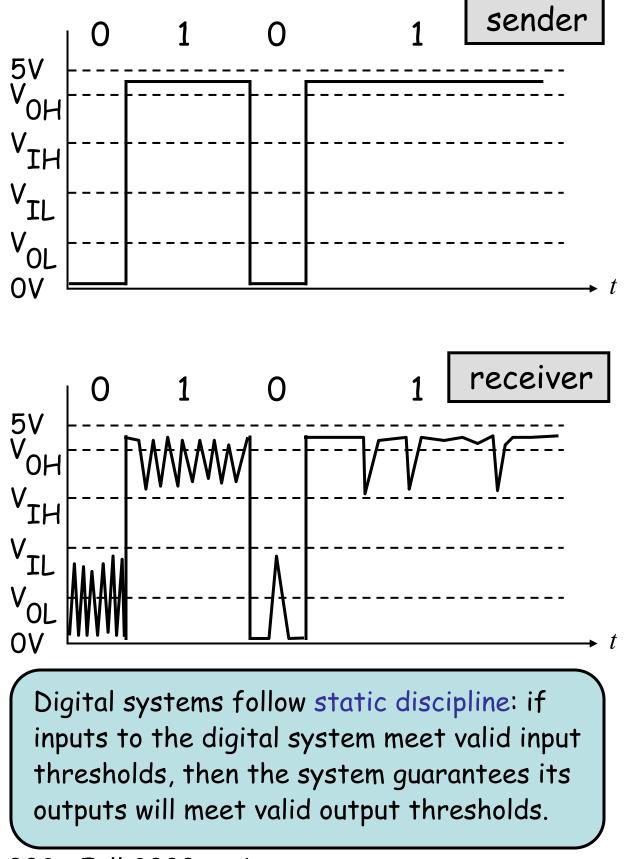
But, but, but ... Where's the noise margin? What if the sender sent 1: V_H ? Hold the sender to tougher standards!



But, but, but ... Where's the noise margin? What if the sender sent 1: V_H ? Hold the sender to tougher standards!



"1" noise margin: V_{IH} - V_{OH} "0" noise margin: V_{IL} - V_{OL}



Processing digital signals

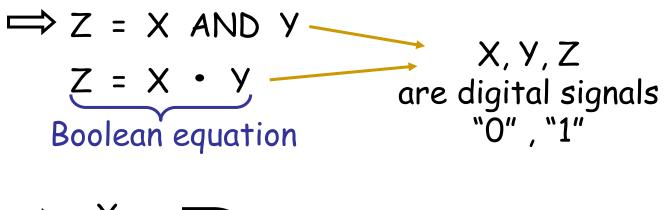
Recall, we have only two values —

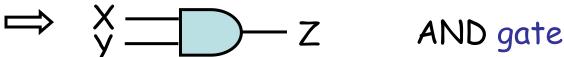
1,**0** \implies Map naturally to logic: T, F \implies Can also represent numbers

Processing digital signals

Boolean Logic

 $\implies \text{If } X \text{ is true and } Y \text{ is true}$ Then Z is true else Z is false.





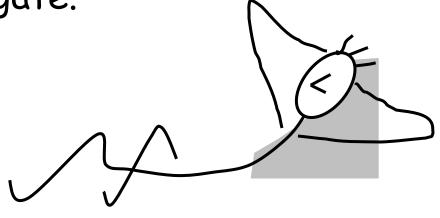
 \implies Truth table representation:

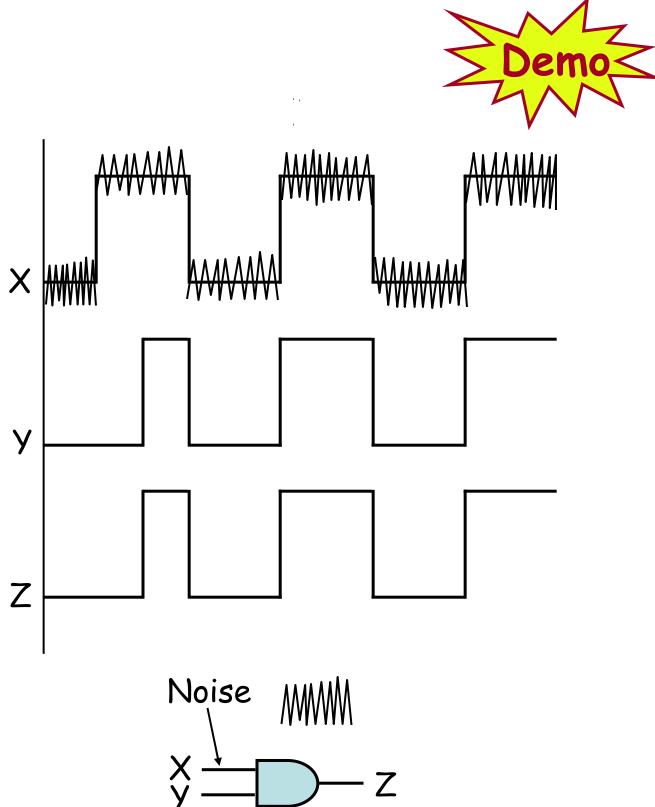
Enumerate all input combinations

Combinational gate abstraction

- Adheres to static discipline
- Outputs are a function of inputs alone.

Digital logic designers do not have to care about what is inside a gate.





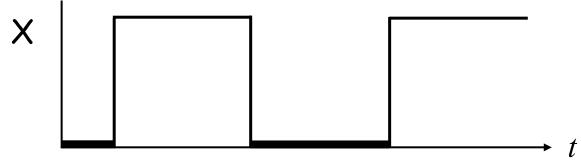


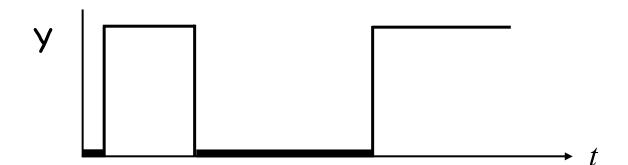
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Examples for recitation





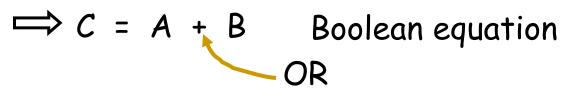


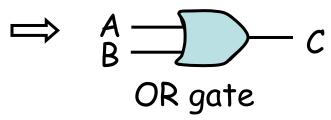


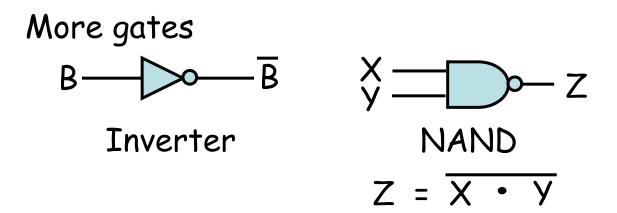
Z = X • Y

In recitation...

Another example of a gate If (A is true) OR (B is true) then C is true else C is false







<u>Boolean Identities</u>

$$X \cdot 1 = X$$

$$X \cdot 0 = X$$

$$X + 1 = 1$$

$$X + 0 = X$$

$$\frac{1}{1} = 0$$

$$\overline{0} = 1$$

$$AB + AC = A \cdot (B + C)$$

Digital Circuits

Implement: output = $A + \overline{B \cdot C}$

