The Design of High Q-factor Silicon Integrated Inductors for up to 4 GHz Applications

by

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Submitted to the Department of Electrical Engineering and Computer Science in Partial Fulfillment of the Requirements for the Degrees of Bachelor of Science in Electrical Science and Engineering and Master of Engineering in Electrical Engineering and Computer Science

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ABSTRACT

High Q-factor inductors on silicon are an essential component, for RF circuit designers to meet increasing consumer desires for low cost, small size, and long battery life in wireless systems. In this thesis we have developed a simple scalable lumped element circuit model for aluminum-copper metallization integrated inductors, that is accurate to within 20% for frequencies up to the self-resonant frequency. Using this model, we have developed a simulator that is suitable for inductor design. Our simulator suggests that inductors with Q-factors of 3 - 10.9 in the frequency range of 1 GHz - 2.4 GHz, for inductances of 2 nH - 12 nH should be feasible using existing RF processing technology. These inductors have self-

resonant frequencies above 10 GHz and areas of at most $1.6 \times 10^5 \mu m^2$.

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Contents

1. Abstract2
2. Acknowledgment3
3. List of symbols5
4. List of tables7
5. List of figures8
6. Chapter 1: Introduction11
7. Chapter 2: The physics of silicon integrated inductors18
8. Chapter 3: Experimental results37
9. Chapter 4: Detailed modeling58
10. Chapter 5: Optimization74
11. Chapter 6: Conclusion91
12. References96

List of symbols

Symbol	Definition
C _m	Center opening dimension
C _n	Inter-metal capacitance
C _{ox}	Half of the oxide capacitance
D ₁	Outer length of inductor
D_2	Outer width of inductor
D _p	Shortest distance form inductor edge to center of pad
ε_{bs}	Permittivity of p-bulk substrate
ε	Permittivity of free space
ϵ_{ox}	Permittivity of oxide
f	Frequency
f _s	Self-resonant frequency
H	Magnetic field
l _{in}	Input current
l _{out}	Output current
J	Current density
L	Lengui Metal inductance
L _m	Self-inductance
L _S	Mutual inductance magnitude
N _m	Number of turns
ρ _{bs}	Resistivity of p-bulk layer
Q-factor	Quality factor of inductor
R _{ac}	AC resistance of metal
R _{dc}	DC resistance of metal
R _m	Metal resistance
R _s	Twice the substrate resistance
R _{shpb}	Sheet resistance of p-buried layer
R _{shpf}	Sheet resistance of p-field implant
S _m	Metal line spacing
T _{bs}	Thickness of p-bulk layer
T _g	Distance from center of inductor to center of substrate
-	contact
T _m	Metal line thickness
T _{ox}	Oxide thickness (Oxide under lowest metal level)

Symbol	Definition
T _{pb}	Thickness of p-buried layer
T _{pf}	Thickness of p-field implant
Tu	Thickness of underpass
T _x	Inter-level oxide thickness
V _{in}	Input voltage
V _{out}	Output voltage
ω	Angular frequency $(\omega = 2\pi f)$
W _m	Metal line width
Z _{in}	Input impedance

List of tables

Table 3.1: Basic Analog Devices RF processing technology 3	7
Table 3.2: Extraction results 4	0
Table 5.1: Fundamental layout parameter values for inductors in design category I7	8
Table 5.2: Fundamental layout parameter values for inductors in design category II8	0
Table 5.3: Fundamental layout parameter values for inductors in design category III8	2
Table 5.4: Fundamental layout parameter values for inductors in design category IV8	3
Table 5.5: Fundamental layout parameter values for inductors in design category V8	5

List of figures

Figure 1.1: Top view of rectangular integrated inductor14
Figure 1.2: Cross-sectional view of inductor shown in figure 1.114
Figure 1.3: Reported values of maximum Q-factor versus inductance of
integrated inductors16
Figure 2.1: Current flow in a planar integrated inductor
Figure 2.2 (a): Magnetic field and current distribution for a conductor with
no skin effect23
Figure 2.2 (b): Approximate current distribution for a conductor with the skin effect23
Figure 2.3 (a): The proximity effect for large spacing
Figure 2.3 (b): The proximity effect for small spacing
Figure 2.4: Simple equivalent circuit model of the integrated inductor
Figure 2.5: Graph of Q-factor versus frequency depicting the sensitivity of
the Q-factor to changes in L_m
Figure 2.6: Graph of Q-factor versus frequency depicting the sensitivity of
the Q-factor to changes in R _m
Figure 2.7: Graph of Q-factor versus frequency depicting the sensitivity of
the Q-factor to changes in C _{ox}
Figure 2.8: Graph of Q-factor versus frequency depicting the sensitivity of
the Q-factor to changes in C _p
Figure 2.9: Graph of Q-factor versus frequency depicting the sensitivity of
the Q-factor to changes in R _s
Figure 3.1: Graph of resistance versus frequency showing the solutions of
equation 3.3 and the DC resistance for inductor S1 of table 3.2
Figure 3.2: Graph of extracted L_m versus frequency for inductor S1 of table 3.245
Figure 3.3: Graph of extracted R_m versus frequency for inductor S1 of table 3.246
Figure 3.4: Graph of extracted R_s versus frequency for inductor S1 of table 3.246
Figure 3.5: Graph of extracted C_p versus frequency for inductor S1 of table 3.247
Figure 3.6: Graph of extracted C_{ox} versus frequency for inductor S1 of table 3.247

Figure 3.7: Graph of Y11 versus frequency showing a comparison between
extracted Y11 and measured Y11 for inductor S1 of table 3.248
Figure 3.8: Graph of Y21 versus frequency showing a comparison between
extracted Y21 and measured Y21 for inductor S1 of table 3.248
Figure 3.9: Graph of Q-factor versus frequency showing a comparison between
extracted Q-factor and measured Q-factor for inductor S1 of table 3.249
Figure 3.10: Variation of Q-factor with changes in metal line width for
inductors of table 3.250
Figure 3.11: Variation of Q-factor with changes in metal line spacing for
inductors of table 3.251
Figure 3.12: Variation of Q-factor with changes in metal line thickness for
inductors of table 3.2
Figure 3.13: Variation of Q-factor with changes in center opening for
inductors of table 3.252
Figure 3.14: Variation of Q-factor with changes in number of turns for
inductors of table 3.2
Figure 3.15: Graph of Q-factor versus frequency showing a comparison between
inductors S1 and C1 of table 3.255
Figure 3.16: Graph of Q-factor versus frequency comparing inductors S1 and
S2 of table 3.2
Figure 4.1: Scattered diagram showing the ratio of modeled inductance (using
the formula of Greenhouse) to measured inductance for inductors characterized
at Analog Devices Inc61
Figure 4.2: Scattered diagram showing the ratio of modeled inductance (using
the formula of Craninckx et al.) to measured inductance for inductors characterized
at Analog Devices Inc62
Figure 4.3: Scattered diagram showing the ratio of calculated DC resistance
to measured DC resistance for inductors characterized at Analog Devices Inc64
Figure 4.4: Graph of metal resistance versus frequency showing the accuracy
of the metal resistance model for inductors S11 and S1 of table 3.264

Figure 4.5: Scattered diagram showing the ratio of modeled to measured
oxide capacitance for inductors characterized at Analog Devices Inc
Figure 4.6: Resistive network model of the subatrate
Figure 4.7: Scattered diagram showing the ratio of modeled to measured
substrate resistance for inductors characterized at Analog Devices Inc
Figure 4.8: Scattered diagram showing the ratio of modeled to measured inter-
metal capacitance for the inductors of table 3.2
Figure 4.9: Graph of Q-factor versus frequency showing the accuracy of the
inductor model for inductors S1 and S17 of table 3.269
Figure 4.10: Graph of Re[Y11] versus frequency showing the accuracy of the
inductor model for inductors S1 and S17 of table 3.269
Figure 4.11: Graph of Im[Y11] versus frequency showing the accuracy of the
inductor model for inductors S1 and S17 of table 3.270
Figure 4.12: Graph of Re[Y21] versus frequency showing the accuracy of the
inductor model for inductors S1 and S17 of table 3.270
Figure 4.13: Graph of Im[Y21] versus frequency showing the accuracy of the
inductor model for inductors S1 and S17 of table 3.271
Figure 5.1: Graph of optimal Q-factor versus inductance for inductors in design
category I79
Figure 5.2: Graph of optimal Q-factor versus inductance for inductors in design
category II81
Figure 5.3: Graph of optimal Q-factor versus inductance for inductors in design
category III
Figure 5.4: Graph of optimal Q-factor versus inductance for inductors in design
category IV84
Figure 5.5: Graph of optimal Q-factor versus inductance for inductors in design
category V
Figure 5.6: Graph of optimal Q-factor versus inductor-to-pad distance
Figure 5.7: Graph of optimal Q-factor versus bulk layer resistivity
Figure 5.8: Graph of optimal Q-factor versus substrate composition parameter

Chapter 1

Introduction

1.1 The importance of silicon integrated inductors

Consumer desires for low cost, minimal power dissipation, and long battery life, are driving silicon integrated circuits for wireless communication applications to higher levels of integration. It is becoming more difficult to meet such desires with existing silicon technologies which provide only transistors, resistors, and capacitors as the design components. Adding inductors to the list of available components will give the circuit designer considerable flexibility and make it easier for him to meet consumer demands. Indeed, the availability of high Q-factor (the Q-factor is a parameter that measures the quality of an inductor) inductors will enable the designer to use passive filtering, inductive loading, inductive peaking of high-frequency amplifiers, matching networks, etc., on silicon integrated circuits. In particular, whatever the value of the inductance needed, Q-factors in the range 5 - 20 are needed for broadband matching sections, and above 30 for narrowband networks like filters, at the frequencies of operation.

Fabricating inductors on silicon is not an easy task. In the past, the idea of accomplishing this task was dismissed. This was partly because it was impossible to obtain very high Q-factors with the low metal line thickness and the high conductivity silicon substrate available back then. The low metal line thickness led to a high metal DC resistance and the high conductivity substrate led to a high substrate loss. These high losses made the Q-factors extremely low at the frequencies of operation of silicon integrated circuits.

The advent of multi-level metallization techniques, the availability of higher resistivity

silicon, and the possibility of using thicker oxides and lower resistivity metals have made the dream of making high Q-factor inductors on silicon a reachable albeit challenging objective. The thicker and lower resistivity metal decreases the metal DC resistance, while the thicker oxide provides more isolation from the high loss substrate. In addition to this, the higher resistivity silicon reduces the conductive loss in the substrate considerably. It is important to note that using thicker metals, lower resistivity metals and higher resistivity silicon increases the cost of fabricating devices on silicon. However, such changes have already been implemented by IBM, who now have a process with five-levels of metal [1].

High Q-factor inductors can be fabricated on III-V substrates like GaAs. Indeed, III-V technologies currently exist that can serve the RF wireless communication market. If this is the case, why do we need to fabricate inductors on silicon? The problem with the III-V technologies is that they are very expensive, and they might not be able to meet increasing demand in the near future. Silicon technologies on the other hand are much cheaper and much more reliable compared to III-V technologies. There is therefore an increasing need for the integration of RF and microwave components, especially inductors, on silicon.

1.2 Objective of thesis

In this thesis we would like to develop a simulator and use it to design inductors with inductances of 2 nH - 12 nH, and Q-factors ranging from 3 to 11 in the frequency range of 1 GHz - 2.4 GHz. These inductors should have self-resonant frequencies of at least 10 GHz and should not have outer dimensions exceeding 460 microns by 460 microns, i.e each should have an area of at most $2.12 \times 10^5 \mu m^2$. It is important to note that we are not trying to design inductors with the minimum possible areas. Our goal is to design high Q-factor inductors with reasonable areas. We would like to achieve this objective without

changing the current RF processing technology at Analog Devices Inc., considerably. These inductors will be used by circuit designers at Analog Devices Inc., to design matching networks, inductive loading circuits, etc.

We stated above that we intend to design inductors with self-resonant frequencies of at least 10 GHz for use in the 1 GHz - 2.4 GHz frequency regime. This raises the question of how high the self-resonant frequency of an inductor needs to be, for a given frequency of use of the inductor. Indeed, it is true that the inductance of an integrated inductor can be highly frequency dependent at frequencies that are extremely close to the self-resonant frequency, and it is very hard to incorporate this effect into a model [1]. In order to ensure that the inductors that we are designing have inductances that are independent of frequency in the frequency regime of interest, we have chosen the self-resonant frequency to be significantly higher than the frequencies at which our designed inductors are going to be used. We must admit though that choosing a self-resonant frequency of at least 10 GHz for use in the frequency regime of 1 GHz - 2.4 GHz might be an exaggeration of the problem. Indeed, a self-resonant frequency of 8 GHz or even 7 GHz might work just fine.

Our approach to solving the design problem involves the following steps:

1. Characterizing all the existing inductors at Analog Devices Inc.

2. Use the information from step 1 above, and our understanding of the physics of integrated inductors to develop a simple scalable equivalent circuit model for integrated inductors (even though so many researchers are working on designing high Q-factor inductors on silicon, there is no available scalable model for the inductor in a coplanar setting). This model should work over a broad range of frequencies (up to the self-resonant frequency).



Figure 1.1: Top view of rectangular integrated inductor.







P-field implant P-buried layer

P-bulk layer

Metal lines





Metal pads Underpass

Field oxide

3. Use the model to develop a simulator that we can use to design optimal inductors. This involves coming up with a simple optimization program, which when given an inductance value, a frequency of interest, and the details of the technology, produces the values of the fundamental layout parameters - C_m , W_m , S_m and N_m - that give the maximum Q-factor at the specified frequency, subject to the constraints on the area and self-resonant frequency.

1.3 Planar integrated inductor geometries

Planar integrated inductors can have different geometries. They can be square, rectangular, circular, etc. It is worth checking whether the geometry makes a difference in terms of Q-factor and area. In this thesis we have characterized both circular and rectangular inductors. However, the model that we present is for rectangular and square geometries only. Figure 1.1 and 1.2 show the top and cross-sectional views respectively, of a typical rectangular integrated inductor fabricated at Analog Devices Inc.

1.4 State of the art

Several companies and universities are currently working on the problem of designing high Q-factor inductors on silicon. Figure 1.3 shows the maximum Q-factors that have been achieved by researchers at the following institutions:

- 1. University of Califonia at Berkeley: They used a silicon substrate with a resistivity
- of 14 ohm-cm and aluminum metallization with a thickness of 1.8 microns [2].
- 2. AT&T: They used a silicon substrate with a resistivity of 200 ohm-cm and gold metallization with a thickness of 4 microns [3].

3. IBM: They have reported the highest Q-factors up to date. However, their use of one port measurements and a floating substrate raises several questions. They used four

levels and five levels aluminum metallizations and a silicon substrate of resistivity 12 ohm-cm. They also used a considerably thick oxide to provide enough isolation from the silicon substrate [1]



Figure 1.3: Reported values of maximum Q-factor versus inductance of integrated inductors.

It is evident from figure 1.3 that the higher the inductance, the lower the maximum Q-factor attained. This is because higher inductance inductors have disproportionately higher losses compared to lower inductance inductors (or more appropriately, the higher inductance inductors have a higher loss to inductance ratio than the lower inductance inductors). As the losses increase, the maximum Q-factor attained decreases, and it also occurs at a lower frequency. In addition to this, we also see that the thicker the metal line, the higher the maximum Q-factor attained. Indeed, as stated in section 1.1, the thicker the metal, the lower the DC resistance. This accounts for the increase in the Q-factor.

Most researches are focusing mainly on designing inductors with the highest possible

peak Q-factor. This is evident from the extensive literature on integrated inductor design. What circuit designers care about is not the peak Q-factor, but rather the Q-factor at the frequency at which they want to use the inductor in question. Hence, researches should be concentrating on trying to maximize the Q-factor at certain frequencies, say 1 GHz for instance where these inductors are mostly used. This has been the focus of this work.

It is important to note that several research groups are looking into the possibility of fabricating inductors on other substrates like sapphire, glass etc. This thesis does not deal with such substrates. For more information on the progress of such research efforts, see reference [1].

1.5 Organization of thesis

We stated in section 1.2 that our approach to solving the problem of interest involves characterization, modeling, and optimization. The organization of this thesis reflects this approach.

Chapter 2 discusses the physics of integrated inductors. Based on the physics, we propose an equivalent circuit model for the inductor. Chapter 3 discusses the method of extracting the values of the equivalent circuit's elements, and also presents the results of the characterization. Chapter 4 states the closed form expressions for the equivalent circuit elements, derived from the results of the characterization and our understanding of the physics of integrated inductors, while chapter 5 presents the results of the optimization. The optimization program uses the closed form expressions of chapter 4. To end the thesis, in chapter 6 we give a summary of what we have achieved in the thesis, and make several recommendations for the design of inductors with Q-factors higher than those that we have achieved.

Chapter 2

The physics of silicon integrated inductors

In this chapter, we discuss the physics of silicon integrated inductors. We begin by describing an ideal integrated inductor and indicate why it is impossible to design such an inductor. We then give a detailed account of the inductance and the loss mechanisms of an integrated inductor. Based on this discussion, we propose a simple lumped element equivalent circuit model for the inductor and use it to study the sensitivity of the Q-factor to changes in the values of the inductance and the losses of the inductor.

2.1 An ideal integrated inductor

An ideal inductor is an element whose impedance is given by:

$$Z_{in} = j\omega L_m \tag{2.1}$$

Such an inductor has a Q-factor of infinity for any given inductance, and at all frequencies, because it has no loss. It cannot be designed because it is impossible to get rid of all the losses of an integrated inductor completely. These losses include the resistive loss in the metal conductors, the capacitive losses between the metal lines (the inter-metal capacitance) and in the metal-oxide-substrate structure (the oxide capacitance), and the conductive loss in the substrate.

The resistive loss in the metal conductors is the most dominant loss mechanism at low frequencies, i.e. such a loss limits the performance of the inductor at low frequencies. As we go to higher frequencies, the capacitive and substrate losses begin to play a role until ultimately they dominate the behavior of the inductor.

2.2 Inductance

The inductance of a spiral inductor has two components: self-inductance of the individual conductor segments making up the spiral, and mutual inductance resulting from the magnetic interaction or magnetic coupling among these segments.



Figure 2.1: Current flow in a planar integrated inductor

Figure 2.1 shows the flow of current in a planar integrated inductor. In this figure, each of the metal segments (numbered 1 - 5) has a self-inductance, and there is a mutual inductance between each pair of parallel conductors. The mutual inductance between two parallel conductors can be positive or negative depending on the direction of current flow in the conductors. If current flows in the same direction in both conductors, then the mutual inductance is positive and vice-versa. In figure 2.1, the mutual inductance between conductors 1 and 5 is positive, whereas that between conductors 1 and 3, 3 and 5, and conductors 2 and 4, is negative.

The self-inductance of a single straight conductor of rectangular cross-section depends on the length of the conductor, as well as on its width and thickness. The longer the conductor, the higher its self-inductance. This can be seen from the fact that if we have a current flowing uniformly along this conductor, the total magnetic field strength will be greater, the longer the conductor. This greater magnetic field is a manifestation of a higher selfinductance. Also, the wider and thicker a conductor is, the higher its self-inductance will be.

The mutual inductance between two parallel conductors depends on the lengths of the conductors and the distance between the track centers of the conductors (the distance between the track centers depends on the widths of the conductors and the spacing between them). The higher the distance between the track centers, the lesser the magnetic interaction between the two conductors, and the lower the mutual inductance between the conductors. In addition to this, the higher the lengths of the conductors, the higher the mutual inductance since there will be more magnetic interaction between them.

The net inductance per unit length of the spiral inductor depends on the metal line width, the metal line spacing, the number of turns, the center opening dimension, the metal line thickness, and the conductivity of the substrate. The inductance per unit length increases as the metal line spacing decreases all other things being equal. This is because decreasing the spacing decreases the distances between the track centers of the conductors, and this leads to an increase in the net mutual inductance per unit length.

An increase in the center opening dimension, leads to an increase in the separation between conductors having negative mutual inductances between them, assuming all other variables are held constant. Consequently, the negative mutual inductance per unit length decreases, and the net inductance per unit length increases. In addition to this, the higher the number of turns, the higher the net mutual inductance per unit length, since more turns means more magnetic interaction among the increased number of conductors, all other things remaining constant. We noted above that increasing the width of the metal line, leads to an increase in the net self-inductance. On the other hand, it causes an increase in the distances between the track centers of the conductors assuming all other variables are constant. It therefore leads to a lower net mutual inductance per unit length. If all other variables are constant, the effect of the increase in the width can either be an increase or decrease in the net inductance per unit length depending on the changes in the magnitudes of the self and mutual inductances per unit length.

An important question that we should ask is whether or not the inductance is frequency dependent. Indeed, mechanisms like the skin effect, the proximity effect (both are discussed in section 2.4), and the effect of eddy current in the substrate (discussed in section 2.3), might lead us to expect the inductance to be frequency dependent. However, with a substrate resistivity of 20 ohm-cm and a minimum oxide thickness of 1.15 microns, we did not notice any frequency dependence in the inductance of any of our inductors at Analog Devices Inc., except at frequencies extremely close to and beyond the self-resonant frequency. The existing literature on this subject support this finding [1], [4].

2.3 Substrate conductivity and its effect on the total inductance

A time changing current flowing in the conductors creates a time changing magnetic field. This magnetic field induces eddy current in the substrate. The higher the conductivity of the substrate, the more induced eddy current there will be in the substrate. According to Lenz's law, this eddy current creates a magnetic field whose action opposes that of the original magnetic field. The net effect is a decrease in the net magnetic field and consequently, a decrease in the total inductance. This effect is expected to get worse as the frequency increases because the amount of eddy current induced increases with the rate of change of the magnetic field (increasing the frequency of the input current into the metal lines, increases the rate of change of the resulting magnetic field).

Simulations carried out at Analog Devices Inc., by Tom Clark show that for a substrate resistivity of 20 ohm-cm and a minimum oxide thickness of 1.15 microns, the effect of eddy current is negligible for frequencies up to 20 GHz. Indeed, the measurements that we carried out support the simulation results. Other people working on this subject [1], have observed that even for a silicon substrate with a resistivity as low as 12 ohm-cm, the effect of eddy current is negligible.

2.4 Metal resistive loss

In general, the metal resistance is observed to be frequency dependent. It comprises of an AC component and a DC component. At very low frequencies, it is equal to the DC resistance. The DC resistance is a function of the total conductor length, the metal line width, the metal line thickness, and the metal conductivity. The higher the metal conductivity, the metal line width and the metal line thickness, the lower the DC resistance. The physical mechanisms that explain the occurrence of an AC resistance are the skin effect and the proximity effect.

(i) The skin effect [5]

Suppose we have a conductor of finite width and thickness. If the width and thickness are less than the skin depth at all frequencies, the resistance of this conductor is simply its DC resistance. The reason for this is that the current that flows through this conductor flows uniformly over its cross sectional area at all frequencies. In this case, we say that there is no skin effect in the conductor and that the AC resistance due to the skin effect is zero.

If on the other hand, the width or thickness (or both the width and the thickness) of the conductor is greater than the skin depth, current will not flow uniformly over the cross-sectional area of the conductor. Instead, most of the current will flow on the outer part of the conductor thereby reducing its effective cross-sectional area. Figure 2.2 illustrates this phenomenon. A decrease in the effective cross-sectional area leads to an increase in the resistance.



Figure 2.2 (a): Magnetic field and current distribution for a conductor with no skin effect.



Figure 2.2 (b): Approximate current distribution for a conductor with the skin effect.

The skin effect gets worse at higher frequencies. The reason for this is that as the frequency increases, the skin depth decreases leading to an increase in both the metal line width to skin depth ratio and the metal line thickness to skin depth ratio. Consequently, we expect the effective cross-sectional area to decrease, thereby leading to an increase in the resistance.

(ii) The proximity effect [5]

As its name implies, the proximity effect has to do with how close the metal conductors are to each other. Let us consider two parallel conductors of similar width and thickness, and let there be a finite spacing between them. Let us further assume that current of the same magnitude is flowing in the same direction in both conductors.

The magnetic fields cancel out in the region between the conductors. Figure 2.3 illustrates this phenomenon. Since equilibrium has to be maintained for the system of conductors to satisfy Ampere's Law, the current distributions in the conductors will redistribute themselves to account for the loss of magnetic field in the region between the conductors. The redistribution of current leads to a decrease in the effective cross-sectional area over which the current flows. Consequently, the resistance increases. It is important to note that this is not a DC phenomenon.

The amount of magnetic field cancellation that occurs in the region between the conductors depends on the spacing between the conductors. The smaller the spacing, the stronger the individual magnetic field strengths in the region between the conductors and the greater the cancellation that occurs. Hence the smaller the spacing, the greater the extent of the current redistribution and the greater the increase in the resistance.

The number of conductors on each side of the center opening of an integrated inductor is proportional to the number of turns. For conductors on the same side of the center opening, the current is flowing in the same direction. Hence we expect the proximity effect to be present. To the first order, the proximity effect is only noticeable for nearest neighbors. Since the number of nearest neighbors is directly proportional to the number of turns, the AC resistance is proportional to the number of turns. Hence, as a result of the proximity effect, the AC resistance is a function of both the metal line spacing and the number of turns.

2.5 Oxide capacitive loss

The structure comprising of the metal layer, the oxide, and the top surface of the substrate (see figure 1.2) is basically a linear capacitor. This capacitor has a parallel plate component and a fringing component. The parallel plate component depends on the total area of the metal conductors, the thickness of the oxide, and the permittivity of the oxide, while the fringing component depends on the total conductor length, the metal line width, the metal line spacing, the metal line thickness, the thickness of the oxide, and the permittivity of the oxide.

The higher the value of this capacitor, the higher the current (displacement current) that will be flowing through it and the lower the current that will be flowing in the metal lines. This leads to a decrease in the Q-factor.

2.6 Inter-metal capacitive loss

There is a capacitance associated with the interaction or coupling among the metal lines. We can separate this capacitance into two components: the capacitance between parallel metal conductors in the same plane, and the underpass capacitance. The underpass capacitance is the capacitance between the underpass and the metal lines above it (see figure 1.1).

This capacitance can be modeled by a linear capacitor. It depends on the spacing between the conductors, the thickness of the conductors, the number of turns, the conductors' lengths and their widths. The higher the inter-metal capacitance, the lower the



Figure 2.3 (a): The proximity effect for large spacing (little magnetic field cancellaoccurs and the resistance is unchanged).



Figure 2.3 (b): The proximity effect for small spacing (high field cancellation and increased resistance).

Q-factor (especially at very high frequencies).

The smaller the spacing between the metal lines, the greater the interaction among them, and the greater the inter-metal capacitance. Furthermore, the wider the metal lines, the greater the underpass capacitance since this leads to an increase in the overlap area between the underpass and the conductors above it. The higher the number of turns, the greater the net interaction among the metal lines and the greater the overlap area of the underpass and the conductors above it. This leads to an increase in the inter-metal capacitance. Also, the thicker the metal lines, the greater the interaction among the metal lines and the higher the inter-metal capacitance.

2.7 Substrate loss

By substrate loss, we mean the loss resulting from the conductive nature of the substrate. The higher the conductivity of the substrate, the higher the amount of displacement current that will flow into the substrate through the oxide capacitor. As this current increases, the current that flows along the metal lines decreases. This leads to a decrease in the Q-factor, especially at high frequencies.

The amount of displacement current that can flow into the substrate also depends on the area of the inductor. The larger the inductor area, the higher the amount of displacement current that can flow into the substrate. The substrate can therefore be modeled with a simple frequency independent resistor whose value depends on the substrate conductivity, the inductor area, and the distance to the ground contact.

The oxide in the inductor structure isolates the metal lines from the substrate. The thicker the oxide, the more isolation there is between the metal lines and the substrate. This reduces the effects of the substrate loss on the Q-factor.

2.8 Layout Issues: Series versus parallel connection

The optimal integrated inductor is one with maximum Q-factor, high self-resonant frequency, and minimum outer area. To obtain a high Q-factor, we need a thicker metal line among other things. To get a thicker metal line, one can connect several levels of metal with vias. This gives a spiral inductor with the different metal levels connected in parallel. However, to obtain high inductance values with this design approach, one needs to increase the inductor area (by increasing the number of turns, center opening, etc.).

To reduce the area, one could use a series connection instead. Here, the metal levels are not shunted together with vias. Instead, they are connected in series to simulate a higher number of turns. The total number of turns in this case is the number of levels multiplied by the number of turns per level. The disadvantage of this scheme is that we cannot make any of the metal levels too thick. Hence, we cannot get a very high Q-factor. In addition to this, the inter-metal capacitance for this scheme is extremely high. This lowers the selfresonant frequency considerably thereby reducing the useful frequency range of the inductor in question. For high inductance values in a compact design, it is better to use the series connection. Since such inductances are used at low frequencies, the issue of large useful frequency range does not come into play. For low inductance values on the other hand, it is better to use the parallel connection. This gives a higher Q-factor, a higher self-resonant frequency, and a smaller area for such inductance values. Since we are concerned with low inductance values (2 nH -12 nH), we will only focus on the parallel design approach in this thesis.

2.9 An equivalent circuit model of the integrated inductor

From the discussion on inductance and inductor losses, it is clear that we can model the inductance and the inductor losses with passive, linear and non-linear circuit elements. In particular, the inductance can be modeled with an ideal inductor, the metal resistance with a frequency dependent resistor, the oxide and inter-metal capacitances with linear capacitors, and the substrate with a frequency independent resistor.

With this in mind, figure 2.4 shows the equivalent circuit model of the integrated induc-

tor used in this work. Notice that the model is a lumped element equivalent circuit model as opposed to a distributive model. The reason for this is that for the range of inductance values that we are interested in, the total conductor length is less than the wavelength of light in vacuum at all the frequencies of interest. Furthermore, the circuit is symmetrical. Even though the integrated inductor structure is asymmetrical (see figure 1.1), modeling it with a symmetrical circuit is a very good approximation [1-3].

2.10 The Q-factor and the self-resonant frequency defined

Now that we have an equivalent circuit model, we would like to give a rigorous definition of the Q-factor and the self-resonant frequency in terms of the circuit parameters. The input impedance is defined as:

$$Z_{in} = \left. \frac{V_{in}}{I_{in}} \right|_{V_{out}} = 0$$
(2.2)

The circuit shown in figure 2.4 is a two-port network. For a two-port network the relationship between the input and output currents and voltages is given by:

$$\begin{bmatrix} I_{in} \\ I_{out} \end{bmatrix} = \begin{bmatrix} Y11 & Y12 \\ Y21 & Y22 \end{bmatrix} \begin{bmatrix} V_{in} \\ V_{out} \end{bmatrix}$$
(2.3)

We can therefore express the input impedance in terms of the two-port parameters as follows:

$$Z_{in} = \frac{Re[Y11] - jIm[Y11]}{(Re[Y11])^2 + (Im[Y11])^2}$$
(2.4)



Figure 2.4: Simple equivalent circuit model of the integrated inductor.

where Re[Y11] and Im[Y11] are the real and imaginary parts of the parameter Y11. The Q-factor is defined as the imaginary part of the input impedance divided by the real part. From equation 2.4 above, the Q-factor is therefore given by:

$$Q - factor = \frac{-Im[Y11]}{Re[Y11]}$$
(2.5)

At low frequencies, this simplifies to:

$$Q - factor = \frac{\omega L_m}{R_m}$$
(2.6)

for the circuit shown in figure 2.4. At such frequencies the metal resistance and the inductance dominate the behavior of the inductor. The self-resonant frequency is the frequency beyond which the inductor behaves like a capacitor, i.e. it is the frequency beyond which the capacitive elements in figure 2.4 dominate the behavior of the inductor. By definition, this is the frequency at which the input impedance defined in equation 2.4 reaches its maximum. Indeed, this frequency is approximately equal to the frequency at which the Q-factor equals zero (i.e. the frequency at which Im[Y11] equals zero). In this thesis, we will calculate the self-resonant frequency as the frequency at which the Q-factor equals zero.

2.11 Sensitivity analysis

Now that we have an equivalent circuit model and have defined the Q-factor, we would like to study how changes in the values of the equivalent circuit elements affect the Q-factor, i.e. we would like to know how sensitive the Q-factor is to changes in the elements' values. The result of this analysis will give us an idea of how accurately we need to model each of the elements of the equivalent circuit in order to predict the Q-factor at each frequency of interest as accurately as possible.

For this study, let us consider an hypothetical inductor whose equivalent circuit elements have the following values: $L_m=2.3$ nH, $R_m=1.8$ ohm, $C_{ox}=600$ fF, $C_p=30$ fF, and $R_s=360$ ohm. These values are typical for the equivalent circuit elements of a 2.3 nH inductor designed with a thick metal (since the DC resistance is small). We will halve and double each element's values, while holding all the others constant, and see how the Q-factor is affected. Since the equivalent circuit model is very simple, such an analysis can be carried out in matlab. Figures 2.5 - 2.9 show the results of this analysis.

In figure 2.5 we see that the higher the inductance, the higher the Q-factor at low frequencies, the higher the peak Q-factor, and the lower the frequency at which the peak Q- factor occurs. The fact that the peak Q-factor increases as the inductance increases does not contradict the statement in chapter one that the higher the inductance, the lower the peak Q-factor typically attained in practice. In the case of figure 2.5, the inductor losses are held constant. In figure 2.6, we see that the higher the resistance, the lower the Q-factor. Indeed, the Q-factor is very sensitive to changes in the inductance and the resistance. Hence, we need to model these elements very accurately in order to be able to predict the Q-factor accurately.

Furthermore, figure 2.9 shows that the Q-factor is very sensitive to R_s at high frequencies. In interpreting this, we must note that the sensitivity of the Q-factor to changes in R_s depends on the value of C_{ox} . In the extreme case where C_{ox} is very small (effectively an open circuit), the Q-factor is not sensitive to changes in R_s because the substrate is effectively an open circuit when the oxide capacitance is an open circuit.

Figures 2.7 and 2.8 show that the Q-factor is not very sensitive to the capacitive elements in comparison to the other elements, especially at low frequencies. This does not mean that these elements are irrelevant in the model. It simply means that we can model them to within 30% and still predict the Q-factor very accurately, especially at low frequencies. We have to be careful in interpreting the sensitivity of the Q-factor to changes in C_{ox} . If R_s is extremely high, the sensitivity of the Q-factor to changes in C_{ox} will be negligible and vice-versa. To see why this is true, let us consider the extreme case where the substrate is perfectly insulating. In this case, the substrate is an open circuit and consequently, C_{ox} is ineffective no matter how high it is.



Figure 2.5: Graph of Q-factor versus frequency depicting the sensitivity of the Q-factor to changes in L_m .



Figure 2.6: Graph of Q-factor versus frequency depicting the sensitivity of the Q-factor to changes in R_m.



Figure 2.7: Graph of Q-factor versus frequency depicting the sensitivity of the Q-factor to changes in C_{ox} .



Figure 2.8: Graph of Q-factor versus frequency depicting the sensitivity of the Q-factor to changes in C_p.



Figure 2.9: Graph of Q-factor versus frequency depicting the sensitivity of the Q-factor to changes in R_s.

2.12 Summary

The following points summarize the main results of this chapter.

1. The losses of an integrated inductor include the resistive loss in the metal, the oxide capacitive loss, the inter-metal capacitive loss, and the conductive loss in the substrate.

2. An integrated inductor can be modeled with a simple symmetrical lumped element equivalent circuit. In this circuit, an ideal inductor is used to model the metal inductance, a frequency dependent resistor is used to model the metal resistance, linear capacitors are used to model the oxide capacitance and the inter-metal capacitance, while a simple frequency independent resistor is used to model the substrate resistance.

3. For a 20 ohm-cm silicon substrate and a minimum oxide thickness of 1.15 microns, the induced eddy current in the substrate is negligible. Hence the inductance of an inductor fabricated on such a substrate is almost the same as the inductance of a similar inductor

fabricated on an air bridge. This is generally the case for inductors fabricated on lowly doped substrates.

4. Sensitivity analysis shows that the Q-factor is sensitive to the different equivalent circuit elements to varying degrees. It is very sensitive to the metal inductance and the metal resistance, and to the substrate resistance at higher frequencies. It is also sensitive to the oxide capacitance and the inter-metal capacitance at higher frequencies although to a lesser extent. One has to be very careful in interpreting the sensitivity of the Q-factor to the oxide capacitance. Indeed, this depends on the value of the substrate resistance. The higher the substrate resistance, the lower the sensitivity of the Q-factor to changes in the oxide capacitance. Also, the sensitivity of the Q-factor to the substrate resistance depends on the value of the oxide capacitance. The main result of the sensitivity analysis, is that we can model the different components of the equivalent circuit with different degrees of accuracy and still predict the Q-factor very accurately. In particular, the elements that the Q-factor is mostly sensitive to must be modeled as accurately as possible.
Chapter 3

Experimental results

In this chapter we present the experimental results. We start by briefly describing the measurement technique and the processing technology. We then describe the extraction mechanism and demonstrate its effectiveness, after which we present the experimental results for several of the inductors that we characterized at Analog Devices Inc.

3.1 Fabrication and characterization

Table 3.1 describes the RF processing technology used at Analog Devices Inc., to fabricate

Parameter	Value			
ε _{bs}	11.7ε _o			
ρ _{bs}	20 ohm-cm			
ρ _m	3.7e-8 ohm-cm			
R _{shpb}	1.2e3 ohms/sq			
R _{shpf}	7.5e3 ohms/sq			
T _{bs}	625 μ <i>m</i>			
T _{m1} (Metal level 1)	0.8 μ <i>m</i>			
T _{m2} (Metal level 2)	1.1 μ <i>m</i>			
T _{m3} (Metal level 3)	3 μ <i>m</i>			
T _{ox}	1.15 μ <i>m</i> / 2.1μ <i>m</i>			
T _x	1 μ <i>m</i>			

Table 3.1: Basic Analog Devices RF processing technology (based on AlCu metallization).

Note: Metal level three was only used in the fabrication of six inductors.

the inductors used in this study. These inductors were integrated with other devices including bipolar transistors, field effect transistors, resistors, capacitors, etc.

The characterization of all the inductors used in this study was done on wafer, with the use of the of the HP 8720C 50 MHz - 20 GHz network analyzer and a pair of ground-signal-ground probes. The following steps were taken during this process:

1. Calibration of equipment.

- 2. Measurement of s-parameters for inductors embedded in pad-structure.
- 3. Measurement of s-parameters for pad structures.

4. De-embed data obtained in step 3 from data obtained in step 2 to get corrected sparameter data.

5. Convert s-parameters to y and z-parameters.

6. Use the data expressed in terms of y and z-parameters to get the Q-factor, self-resonant frequency, and the values of the equivalent circuit elements.

3.2 Extraction

We can extract the values of the equivalent circuit elements from the corrected inductor data obtained in step 5 in section 3.1. Table 3.2 shows the extraction results for some of the inductors that we characterized at Analog Devices Inc. For the circuit shown in figure 2.4, we have the y-parameter equations shown below. These are the equations that we used to derive extraction mechanisms for C_p , L_m and R_m .

$$Re[Y11] = \frac{R_m}{R_m^2 + \omega^2 L_m^2} + \frac{\omega^2 C_{ox}^2 R_s}{1 + \omega^2 C_{ox}^2 R_s^2}$$
(3.1)

$$Im[Y11] = -\frac{\omega L_m}{R_m^2 + \omega^2 L_m^2} + \frac{\omega C_{ox}}{1 + \omega^2 C_{ox}^2 R_s^2} + \omega C_p$$
(3.2)

$$Re[Y21] = \frac{-R_m}{R_m^2 + \omega^2 L_m^2}$$
(3.3)

$$Im[Y21] = \frac{\omega L_m}{R_m^2 + \omega^2 L_m^2} - \omega C_p$$
(3.4)

3.3.1 Extraction of L_m

At very low frequencies, the impact of the capacitor C_p on the behavior of the inductor is negligible. At such frequencies, the term ωC_p can be considered negligible compared to the other terms in equations 3.4 and 3.2, and we see from equations 3.3 and 3.4 that L_m is given by:

$$L_m \approx \frac{Im[Y21]}{\omega[(Re[Y21])^2 + (Im[Y21])^2]}$$
(3.5)

We argued in chapter 2 that the inductance is constant for all frequencies below the self-resonant frequency. This means that the value of L_m obtained from equation 3.5 at very low frequencies is strictly speaking equal to the inductance at all frequencies below the self-resonant frequency. In this thesis, we use this value of L_m as the inductance at all frequencies.

3.3.2 Extraction of R_m

Let us consider equation 3.3. If we substitute for L_m , Re[Y21], and ω , the equation becomes a quadratic equation in R_m . The two solutions to this equation are as follows:

Label	W _m μ <i>m</i>	Τ _m μ <i>m</i>	S _m μm	N _m	C _m μm	Τ _{ox} μm	L _m (nH)	R _{dc} (Ω)	C _{ox} (fF)	C _p (fF)	R _s (Ω)
S1	20	1.9	3	3.5	60	1.15	2.13	2.49	745	30	320
S2	20	1.9	3	3.5	60	1.15	2.13	2.49	690	30	400
S 3	15	1.9	3	3.5	60	1.15	1.99	2.53	435	19	560
S4	40	1.9	3	3.5	60	1.15	3.15	2.1	1930	47	230
S5	5	1.9	3	3.5	60	1.15	1.92	5.49	130	8	1300
S6	10	1.9	3	3.5	60	1.15	1.94	3.42	280	15	800
S7	10	1.9	2	3.5	60	1.15	1.93	3.04	266	12	850
S8	10	1.9	5	3.5	60	1.15	1.97	3.17	306	15	740
S9	10	1.9	10	3.5	60	1.15	2.07	3.93	347	15	680
S10	10	1.9	3	3.5	30	1.15	1.3	2.57	208	5.1	1000
S11	10	1.9	3	5.5	30	1.15	3.23	4.61	410	30	690
S12	10	1.9	3	4.5	30	1.15	2.09	3.42	293	20	800
S13	10	1.9	3	6.5	30	1.15	4.81	6.33	550	40	560
S14	10	1.9	3	3.5	40	1.15	1.51	2.84	234	5	930
S15	20.2	1.9	1.4	3.5	60	1.15	2.09	2.27	748	28.9	320
S16	5	4	2	8.5	50	2.1	9.14	7.12	255	13	1456
S17	10	4	2	6.5	25	2.1	4.45	2.62	350	16	1220
S18	5	0.8	2	8.5	50	1.15	9.31	24	220	12	600
S19	5	1.9	2	8.5	50	1.15	8.96	15.3	382	12	562
C1	20	1.9	3	3.5	60	1.15	2.17	2.28	670	30	350
C2	20	1.9	3	3.5	40	1.15	1.82	2.04	582	29	383
C3	20	1.9	3	3.5	20	1.15	1.47	1.96	501	25	421

Table 3.2: Extraction results

Note:

(1). Inductors S1 and S15 have substrate contacts.

- (2). Inductors S16 and S17 have no p-buried layer and no p-field implant.
- (3). Inductors C1, C2, and C3 are circular. The rest have rectangular geometry.

$$R_{1} = \frac{\left(-Re[Y21]\right)^{-1} + \sqrt{\left(Re[Y21]\right)^{-2} - 4\omega^{2}L_{m}^{2}}}{2}$$
(3.7)

$$R_{2} = \frac{(-Re[Y21])^{-1} - \sqrt{(Re[Y21])^{-2} - 4\omega^{2}L_{m}^{2}}}{2}$$
(3.8)

From equation 3.3 it is easy to see that as ω tends to zero, R₁ is the valid solution (R₁ gives the DC resistance in this regime). Also, as ω becomes very large, we see that R₂ and R₁ could be valid solutions. By solving for R₁ and R₂ for 70 different inductors characterized at Analog Devices Inc., and by using the fact that at sufficiently low frequencies R_m is equal to the DC resistance, we empirically found the following: (i) R₁ is the valid solution in the frequency range from zero to about 100 MHz. Indeed, R₁ is equal to or very close to the DC resistance in this frequency regime. Beyond this frequency regime, R₁ increases rapidly with frequency and takes values that are higher than the expected values of the resistance. For instance, at frequencies beyond this regime where we expect the resistance to be equal to the DC resistance, R₁ can be as high as six (or more) times the DC resistance; (ii) R₂ is the valid solution from about 250 MHz at which point it is approximately equal to the DC resistance, up to very high frequencies. With these observations we developed the following empirical rule to extract R_m:

$$R_m = Max(R_{dc}, R_2) \tag{3.9}$$

Figure 3.1 shows a graph of R_1 , R_2 and R_{dc} versus frequency, for inductor S1 of table 3.2. By comparing the metal line width and the metal line thickness of inductor S1 to the

skin depth of AlCu metallization, we expect the skin effect to be negligible for frequencies up to 1 GHz. Also, since the metal line spacing for S1 is 3 μm and the number of turns is only 3.5 we expect the proximity effect to be negligible for frequencies up to 1 GHz [5]. Consequently, we expect R_m for inductor S1 to be the DC resistance or at least very close to the DC resistance for frequencies up to 1 GHz.



Figure 3.1: Graph of resistance versus frequency showing the solutions of equation 3.3 and the DC resistance for inductor S1 of table 3.2.

From figure 3.1, we see that R_1 is equal to the DC resistance for frequencies up to about 100 MHz. However, between 100 MHz and 620 MHz where we expect R_m to be equal to or very close to the DC resistance, R_1 increases to more than 10 times the DC resistance. Hence, R_1 is the valid solution only in the frequency range from zero to about 100 MHz. R_2 on the other hand is equal to the DC resistance from about 250 MHz to about 600 MHz and it is very close to the DC resistance from 600 MHz to 1 GHz. In addition to this, the

rate at which R_2 increases with frequency is typically the observed rate of increase of the metal resistance with frequency [4]. This suggests that R_2 is the valid solution from about 250 MHz up to very high frequencies.

3.3.3 Extraction of C_p

By substituting for L_m , R_m , Im[Y21], and ω in equation 3.4, we can solve for C_p as follows:

$$C_{p} = \frac{1}{\omega} \left(\frac{\omega L_{m}}{R_{m}^{2} + \omega^{2} L_{m}^{2}} - Im[Y21] \right)$$
(3.11)

It is important to note that the practical extraction of C_p is only possible at high frequencies where its impact on the behavior of the inductor is not negligible (i.e. at frequencies where the term ωC_p is either comparable to or greater than the other terms in equations 3.2 and 3.4). By solving equation 3.11 for C_p at high frequencies, we do not typically get a constant value. Since C_p is supposed to be constant, we therefore take the average of all the values at high frequencies.

3.3.5 Extraction of C_{ox} and R_s

Let us consider the circuit in figure 2.4. At sufficiently low frequencies, the impedance of the C_p branch is extremely high compared to the impedance of the L_m - R_m branch. Since these branches are in parallel, we can consider the C_p branch to be an open circuit at such frequencies. Also, at such frequencies, the impedance of the C_{ox} - R_s branch is considerably higher than that of the L_m - R_m branch. Since these two branches are in series, we can consider the L_m - R_m branch as essentially a short circuit. With these assumptions at sufficiently low frequencies, we can approximate Re[Z12] and Im[Z12] for the circuit in figure 2.4 as follows:

$$Im[Z12] \approx \frac{-1}{2\omega C_{ox}} \tag{3.12}$$

$$Re[Z12] \approx \frac{R_s}{2} \tag{3.12}$$

We can solve for C_{ox} and R_s from equations 3.11 and 3.12 respectively.

3.4 Illustration of extraction method

To check the accuracy of the above extraction method for any inductor, the following steps must be taken:

- 1. Substitute the extracted values into the y-parameter equations (eqs. 3.1 3.4) to generate extracted y-parameters.
- 2. Use the generated extracted y-parameters to compute the extracted Q-factor.
- 3. Compare the extracted y-parameters and the extracted Q-factor with the experimen-
- tal y-parameters and the experimental Q-factor.

To illustrate this, let us consider inductor S1 of table 3.2. As shown in that table, the extracted values for this inductor are: $L_m=2.13$ nH, $R_{dc}=2.49$ ohms, $C_{ox}=745$ fF, $C_p=30$ fF, and $R_s = 320$ ohms. Figure 3.2 shows the result of using equation 3.5 to extract L_m for frequencies up to 4 GHz. It is clear form the figure that L_m is constant to within 5% on average for the frequencies shown. We used the constant value of 2.13 nH for L_m at all frequencies, to extract C_p and R_m . Figure 3.3 shows a graph of the extracted metal resistance versus frequency. Indeed, the metal resistance is an increasing function of frequency as expected. It is equal to the DC resistance at low frequencies, and it increases rapidly at hi-



Figure 3.2: Graph of extracted L_m versus frequency for inductor S1 of table 3.2 ($L_m = 2.13 \text{ nH}$).

gher frequencies (due to the skin effect and the proximity effect).

Figures 3.4 and 3.6 show graphs of the extracted C_{ox} and R_s versus frequency respectively. From these figures we see that the oxide capacitance and the substrate resistance are constant to within small percentages. Finally, from figure 3.5 which shows a graph of the extracted C_p versus frequency at high frequencies, we see that we typically do not get a constant when we use our extraction method to extract C_p . However, it is clear from the figure that the average value of C_p is 30 fF, and that is what we consider as the extracted value of C_p for inductor S1 of table 3.2.

Using these extracted values, we generated the extracted y-parameters and the extracted Q-factor for the inductor S1 of table 3.2. Figure 3.7 and 3.8 show a comparison between the extracted y-parameters and the measured y-parameters, while figure 3.9 shows a com-

parison between the extracted Q-factor and the measured Q-factor. From these figures, it is



Figure 3.3: Graph of extracted R_m versus frequency for inductor S1 of table 3.2.



Figure 3.4: Graph of extracted R_s versus frequency for inductor S1 of table 3.2 ($R_s = 320$ ohms).

clear that the extraction mechanism is very accurate for inductor S1 of table 3.2.



Figure 3.5: Graph of extracted C_p versus frequency for inductor S1 of table 3.2 ($C_p = 30$ fF).



Figure 3.6: Graph of extracted C_{ox} versus frequency for inductor S1 of table 3.2 ($C_{ox} = 745$ fF).



Figure 3.7: Graph of Y11 versus frequency showing a comparison between extracted Y11 and measured Y11 for inductor S1 of table 3.2.



Figure 3.8: Graph of Y21 versus frequency showing a comparison between extracted Y21 and measured Y21 for inductor S1 of table 3.2.



Figure 3.9: Graph of Q-factor versus frequency showing a comparison between extracted Q-factor and measured Q-factor for inductor S1 of table 3.2.

3.5 Experimental data

In this section we present and explain the measured data for some of the inductors of

table 3.2.

3.5.1 Q-factor versus several layout and processing parameters

We would like to study experimentally the relationship between the Q-factor and several layout and processing parameters including the metal line thickness, the metal line width, the metal line spacing, the center opening dimension, and the number of turns.

Figure 3.10 shows the impact of changing the metal line width on the Q-factor. Indeed, if we increase the metal line width while holding all other parameters constant, we expect the total conductor length to increase. This in turn increases the inductance. In addition to this, the inter-metal capacitance and the oxide capacitance increase while the substrate resistance decreases. As a result of this, the frequency at which the Q-factor reaches its

peak decreases, and the peak Q-factor also decreases. Furthermore, the self-resonant frequency decreases and the Q-factor at high frequencies decreases. It is important to note that increasing the metal line width decreases the metal DC resistance per unit length. Consequently, the Q-factor at lower frequencies increases. This tells us that increasing the metal line width is an effective way of getting high Q-factors at lower frequencies.

Figure 3.11 shows the impact of changing the metal line spacing with all other variables remaining constant. When we change the metal line spacing, the total length changes and the amount of interaction among the metal lines also changes. This means that the inductance and the losses change. Hence we expect the Q-factor to change. However, from our experimental results, we observe that when the metal line spacing changes from 2 microns to 10 microns, the Q-factor is hardly affected. This might mean that such a change brings about negligible changes in a mechanism like the proximity effect, and thus leaves the



Figure 3.10: Variation of Q-factor with changes in metal line width for inductors of table 3.2.



of table 3.2.



table 3.2.



Figure 3.13: Variation of Q-factor with changes in center opening for inductors of table 3.2



Figure 3.14: Variation of Q-factor with changes in number of turns for inductors of table 3.2.

metal line resistance unchanged. It might also mean that there are negligible changes in the inductance and the other inductor losses. Indeed, the extracted data show that both scenarios explain the negligible change in the Q-factor.

Figure 3.12 shows the effects of changes in the metal line thickness on the Q-factor. If we change the metal line thickness, we expect the Q-factor to change significantly. In particular, if we increase the metal line thickness, the DC resistance decreases and this increases the Q-factor at all frequencies as we saw in section 2.11. It is important to note that increasing the metal line thickness causes the ratio of the thickness to the skin depth to increase. Hence, the skin effect should become more apparent at higher frequencies. For the range of metal line thickness that we are dealing with, this effect is outweighed by the decrease in the metal DC resistance.

Figure 3.13 depicts the impact of changes in the center opening on the Q-factor. As stated in chapter two, changing the center opening dimension while holding all other variables constant, changes the inductance and the inductor losses because such a change changes the total conductor length, the outer area of the inductor, and the amount of interaction among the conductors on opposite sides of the center opening. For example, if we increase the center opening, we expect the inductance to increase and we also expect a higher increase in the losses. Hence, the peak Q-factor should decrease, and the frequency at which it occurs should generally decrease also. In general, for a given inductance, it is best to design an inductor with a large center opening and a small number of turns. This is because having lesser turns reduces the influence of the proximity effect, and this gives a higher Q-factor. In particular, we want to have a single turn, but this means that we must have a very large center opening in order to get the given inductance. The reason why this

design is never used in practice is that such an inductor uses up a large area of the chip.

Following closely the discussion in the above paragraph, we expect an increase in the number of turns (with all other things remaining constant) to increase the effectiveness of the proximity effect and thereby increase the metal AC resistance. It also leads to an increase in the other inductor losses and to an increase in inductance. The increase in the inductor losses is much higher than the increase in the inductance (especially at high frequencies). Thus, increasing the number of turns effectively reduces the Q-factor at high frequencies, reduces the peak Q-factor and reduces the frequency at which the peak Q-factor occurs. This scenario is shown in figure 3.14.

3.5.2 Rectangular/square versus circular inductor geometry

Several researchers working on the problem of designing high Q-factor inductors on silicon have claimed that inductors with circular geometry are better than those with rectangular or square geometry [7 - 9]. Some of the reasons given for this are the following:

For a given inductance, the DC resistance of a circular inductor is less than that of a square inductor because the total conductor length of the circular inductor is smaller.
For a given inductance, a circular inductor has a smaller area than a square/rectangular inductor. This means that a circular inductors uses less space on a chip.

While reason number one is true, the difference in the DC resistance is only about 10%. Hence, we only see about a 10% or less difference in the Q-factor. This is illustrated in figure 3.15 which compares a circular inductor to a rectangular inductor with similar layout and processing parameters. Reason number two is misleading. The area that should be considered is the effective area on the chip that is used up by the inductor structure. For a square or rectangular inductor this area is the physical area of the inductor. For a circular inductor on the other hand, this area is the area of the square that surrounds the circular



Figure 3.15: Graph of Q-factor versus frequency showing a comparison between inductors S1 (rectangular geometry) and C1 (circular geometry) of table 3.2.



Figure 3.16: Graph of Q-factor versus frequency comparing inductors S1 (with substrate contacts) and S2 (without substrate contacts) of table 3.2.

structure, i.e. it is the area of a square whose width is equal to the outer diameter of the circular structure. When we consider this effective area, we see that the circular inductor geometry is not better than the square/rectangular geometry, in terms of chip area used.

3.5.3 Substrate contact versus no substrate contact

Circuit designers usually argue that it is unwise to put a substrate contact near an inductor structure [1]. This claim has not yet been substantiated. For all the inductors that we characterized at Analog Devices Inc., there seems to be no substantial difference between inductors with substrate contacts and those without, in terms of the Q-factor. This is illustrated in figure 3.16.

It is important to mention that for inductors with no substrate contact, it is rather difficult to extract R_s using our extraction technique. The problem is not the extraction technique. Our equivalent circuit model does not account for the fact that for inductors with no substrate contact, there is a distributive capacitance between the substrate and the grounded metal pads. Indeed, it is very difficult to understand the nature of this distributive capacitance. The model is mainly for inductors with a substrate contact, in which case the substrate is directly connected to the grounded metal pads, i.e. the substrate is grounded while measurements are being done. What this translates to is that for inductors without a substrate contact, the value of R_s extracted using our extraction scheme is not a constant. Hence, we take an average over the frequency range where extraction is done.

3.6 Summary

The following points summarize the main results of this chapter.

1. Using the y-parameter equations of the equivalent circuit model, we have developed a procedure to extract L_m , R_m and C_p . The assumption made is that L_m is constant at all fre-

quencies.

2. We use Z12 at sufficiently low frequencies to extract C_{ox} and R_s .

3. An increase in the metal line width while holding all other variables constant, leads to an increase in the Q-factor at lower frequencies. It also leads to a decrease in the peak Qfactor, and to a lowering of the frequency at which the peak Q-factor occurs.

4. Changes in the metal line spacing from 2 microns to 10 microns hardly affect the Q-factor.

5. An increase in the metal line thickness (with all other variables remaining unchanged) leads to an increase in the Q-factor at all frequencies. Such a change leaves the frequency at which the Q-factor reaches its peak unchanged. One of the implications of this is that changing the metal line thickness leaves the inductance unchanged. Hence, the inductance is approximately independent of the metal line thickness.

6. An increase in the center opening (with all the other parameters remaining unchanged) reduces the peak Q-factor and the frequency at which this peak occurs.

7. An increase in the number of turns (with all other variables remaining unchanged) leads to a decrease in both the peak Q-factor and the frequency at which this peak occurs.

8. Generally, it is better to design inductors with a large center opening and a small number of turns. The issue here is the reduction of the proximity effect. The only problem is that this leads to a higher inductor outer area.

9. There is not much of a difference between circular and rectangular planar inductors, in terms of the Q-factor and the effective area they consume on a chip.

10. There is not much of a difference between inductors with and those without substrate contacts in terms of the Q-factor.

Chapter 4

Detailed modeling

Based on our understanding of the physics of integrated inductors, and the results of the extraction, we would like to come up with closed form expressions for the dependencies of the equivalent circuit elements on the layout and processing parameters of the inductor. These expressions should accurately predict the values of these elements given the necessary layout and processing parameter values (the level of accuracy desired is dictated by the sensitivity of the Q-factor to changes in the different equivalent circuit elements' values - see section 2.11). In this chapter, we present such expressions, demonstrate their accuracy, and discuss their limitations.

4.1 Modeling the metal inductance

Greenhouse [6] and Craninckx [4] have developed different formulae for computing the inductance of a planar inductor. The latter is particularly useful for quick back-of-the-envelope calculations. In this thesis, we will only use the former to model the metal inductance because it is more accurate than the latter.

4.1.1 The Greenhouse formula

1. Self-Inductance

The Greenhouse formula for the self-inductance of a non-magnetic metal conductor of rectangular cross-section is given by [6]:

$$L_m = 0.0002L \left\{ \ln \left(\frac{2L}{W_m + T_m} \right) + 0.50049 + \frac{W_m + T_m}{3L} \right\}$$
(4.1)

where all dimensions are in cm and the inductance is in nH.

2. Mutual Inductance

According to Greenhouse [6], the magnitude of the mutual inductance between two parallel conductors x and y of common length L is given by:

$$M_{x, y} = 2LV \tag{4.2}$$

where $M_{x,y}$ is the mutual inductance magnitude in nH, L is length in cm and V is a dimensionless parameter defined as follows:

$$V = \ln\left(\frac{L}{GMD} + \sqrt{1 + \frac{L^2}{GMD^2}}\right) - \sqrt{1 + \frac{GMD^2}{L^2}} + \frac{GMD}{L}$$
(4.3)

The variable GMD in equation 4.2 is the geometric mean distance between the two conductors. It is given by [6]:

$$GMD = \exp\left\{ \left(\frac{1}{12\left(\frac{d}{W_m}\right)^2} + \frac{1}{60\left(\frac{d}{W_m}\right)^4} + \frac{1}{168\left(\frac{d}{W_m}\right)^6} \right) \ln(d) \right\}$$
(4.4)

where d, the distance between the track centers of the conductors is simply $W_m + S_m$. The GMD is in cm when all dimensions are in cm. Notice that the mutual inductance can be positive or negative depending on the direction of current flow in the conductors. If current is flowing in the same direction in both conductors, then the mutual inductance is positive, and vice-versa.

To use the Greenhouse formula in the computation of the inductance, we have to view

the spiral inductor as a group of conductors. We can then compute the self inductance of each of the conductors, and compute the mutual inductance between parallel conductors. The total inductance is the sum of the self-inductances and the net mutual inductance, where the net mutual inductance is the sum of the positive mutual inductances minus the negative mutual inductances. To illustrate this, let us consider the inductor in figure 2.1. For that inductor, the total metal inductance is given by:

$$L_m = \sum_{i=1}^{5} L_{s_i} - M_{1,3} - M_{3,5} - M_{2,4} + M_{1,5}$$
(4.5)

Note that the Greenhouse formula is for suspended inductors, i.e. inductors with no substrate underneath. Since we argued in chapter two that the effect of our substrate on the inductance is negligible, we can use the Greenhouse formula to model the metal inductance. Figure 4.1 shows the ratio of the modeled metal inductance (using the Greenhouse formula) to the measured metal inductance for several inductors characterized at Analog Devices Inc. From this figure, we see that the Greenhouse formula is accurate to within 10%.

4.1.2 The formula of Craninckx et al.

Craninckx et al., [4] recently developed a formula for computing the inductance of a square/rectangular planar inductor from the results of electromagnetic simulations. This formula tends to give higher values of inductance compared to the Greenhouse method. It is for inductors fabricated on lowly doped substrates, i.e. it assumes that the effect of eddy current is negligible. Using our notation, we can express this formula as follows:

$$L_m = 1.3 \times 10^{-4} \left(\frac{(D_1 \times D_2)^{1.5}}{W_m^2} \right) \left(\frac{L \times W_m}{D_1 \times D_2} \right)^{1.67} \left(\frac{W_m}{W_m + S_m} \right)^{0.25}$$
(4.6)

where all the dimensions are in microns and the inductance is in nanohenries. Figure 4.2 shows the ratio of modeled inductance (using the Craninckx formula) to measured inductance for several inductors characterized at Analog Devices Inc. By comparing figures 4.1 and 4.2, we see that this formula is less accurate than the Greenhouse formula.



Figure 4.1: Scattered diagram showing the ratio of modeled inductance (using the formula of Greenhouse) to measured inductance for inductors characterized at Analog Devices Inc.

4.2 Modeling the metal resistance

As stated in chapter 2, the metal resistance comprises of an AC component and a DC component, i.e.

$$R_m = R_{ac} + R_{dc} \tag{4.7}$$

Let us rewrite this as follows:

$$R_m = R_{dc} \left(1 + \frac{R_{ac}}{R_{dc}} \right) \tag{4.8}$$



Figure 4.2: Scattered diagram showing the ratio of modeled inductance (using the formula of Craninckx et al.) to measured inductance for inductors characterized at Analog Devices Inc.

where

$$R_{dc} = \frac{\rho_m L}{W_m T_m} \tag{4.9}$$

Using curve fitting techniques, we find that the term $\frac{R_{ac}}{R_{dc}}$ takes the form Cf^k [3], where

C and k are constants depending on the inductor layout and structural parameters. Using curve fitting techniques, we find that the constant k is approximately equal to 2 for all the inductors that we characterized.

The variable C is a function of W_m , S_m , N_m and T_m due to the skin effect and the proximity effect. By using extensive curve fitting techniques, we find that C is given by:

$$C = \frac{N_m (W_m^{1.2} + T_m^{1.2})}{726.8S_m^{0.25}}$$
(4.10)

with all dimensions in microns.

It is important to note that this formula was derived for AlCu metallization with a resistivity of 3.7×10^{-8} ohm-cm. For the metal resistance model to be accurate, the DC resistance must be accurate to within 20% or better. From figure 4.3 which shows the ratio of the calculated DC resistance to the measured DC resistance we see that this is the case. Figure 4.4 shows a comparison between our metal resistance model and the measured metal resistance. From it we see that our metal resistance model is very accurate (to within 20%) for frequencies up to 10 GHz for inductors S1 and S11 (see table 3.2 for the description of these inductors). In general, our metal resistance model is accurate to within 20% on average for frequencies up to the self-resonant frequency of the inductor.

4.3 Modeling the oxide capacitance

The oxide capacitance comprises of a parallel plate component and a fringing component. To model both components, we use an effective width that is the sum of the actual metal line width and the metal line thickness. Indeed, this models the oxide capacitance to the first order. The element C_{ox} in the equivalent circuit model is given by:

$$C_{ox} = \frac{\varepsilon_{ox} L(W_m + T_m)}{2T_{ox}}$$
(4.10)



DC resistance for inductors characterized at Analog Devices Inc.



Figure 4.4: Graph of metal resistance versus frequency showing the accuracy of the metal resistance model for inductors S11 and S1 of table 3.2.

Figure 4.5 shows the ratio of the modeled oxide capacitance to the measured oxide capac--itance. From this figure, we see that this model is accurate to within 10% on average. This accuracy is enough since the Q-factor is not sensitive to 10% variations in C_{ox} .

4.4 Modeling the substrate resistance

The substrate resistance is the parallel combination of the following resistors:

- 1. Two resistors associated with the p-field implant.
- 2. Two resistors associated with the p-buried layer.
- 3. Two resistors associated with the p-bulk layer.

This is shown in figure 4.6 which shows the complete model of the substrate. These six resistors are all lateral resistors because we have co-planar structures, and the back of the wafer in our case is not a good ground. During the measurement stage, we found that the back of the wafer did not serve as a good ground contact because there was a buried oxide underneath the bulk material, and the distance from the metal lines to the back of the wafer sitting on the chuck was much larger than that to the co-planar substrate contacts.

In figure 4.6, R1 is associated with the p-field implant. It is the resistance of a resistor of length T_g , width D_2 , and sheet resistance R_{shpf} . Using our notation, we can express R1 as follows:

$$R1 = \frac{R_{shpf}T_g}{D_2} \tag{4.11}$$

R2 is associated with the p-buried layer. It is the resistance of a resistor of length T_g , width D_2 and sheet resistance R_{shpb} . In terms of our notation, R2 is given by:



Figure 4.5: Scattered diagram showing the ratio of modeled to calculated oxide capacitance for inductors characterized at Analog Devices Inc.



Figure 4.6: Resistive network model of the substrate (the substrate contacts are grounded).

$$R2 = \frac{R_{shpb}T_g}{D_2} \tag{4.12}$$

R3 is associated with the p-bulk layer. Intuitively, we expect it to be the resistance of a resistor of length T_g , width D_2 and thickness T_g . However, this does not seem to fit the

measured data very well. We find that by using a thickness of D_2 instead of T_g we get a better agreement with the measured data. We therefore model R3 as follows:

$$R3 = \frac{\rho_{bs}T_g}{D_2^2}$$
(4.13)

Since the resistive network used in modeling the substrate resistance is symmetric and R_s is twice the substrate resistance, R_s is therefore simply the parallel combination of R1, R2, and R3. The scattered diagram in figure 4.7 shows the ratio of the modeled substrate resistance to the measured substrate resistance for several inductors characterized at Analog Devices Inc. From the figure, we see that the substrate resistance model is accurate to within 25% on average. Indeed, this is good enough because the Q-factor is not very sensitive to such errors in the substrate resistance.

4.5 Modeling the inter-metal capacitance

The inter-metal capacitance comprises of the underpass capacitance and the capacitance between parallel conductors in the same plane. The underpass capacitance dominates for the parallel layout structures, and it is therefore the only one that we will concentrate on in this thesis. The underpass capacitance comprises of a parallel plate component and a fringing component. Once again to model both the fringing capacitance and the parallel plate capacitance, we define an effective metal width that equals the actual metal width plus the thickness of the underpass. The underpass capacitance is therefore given by:

$$C_p = \frac{N\varepsilon_{ox}W_m(W_m + T_m)}{T_x}$$
(4.14)



Figure 4.7: Scattered diagram showing the ratio of modeled to measured substrate resistance for inductors characterized at Analog Devices Inc.



Figure 4.8: Scattered diagram showing the ratio of modeled to measured inter-metal capacitance for the inductors of table 3.2.



Figure 4.9: Graph of Q-factor versus frequency showing the accuracy of the inductor model for inductors S1 and S17 of table 3.2.



Figure 4.10: Graph of Re[Y11] versus frequency showing the accuracy of the inductor model for inductors S1 and S17 of table 3.2.



Figure 4.11: Graph of Im[Y11] versus frequency showing the accuracy of the inductor model for inductors S1 and S17 of table 3.2.



Figure 4.12: Graph of Re[Y21] versus frequency depicting the accuracy of the inductor model for inductors S1 and S17 of table 3.2.



Figure 4.13: Graph of Im[Y21] versus frequency showing the accuracy of the inductor model for inductors S1 and S17 of table 3.2.

where the variable N represents the number of overlap regions between the underpass and the metal conductors above it. When N_m takes values like 1.5, 2.5, etc., $N = N_m - 0.5$. On the other hand, when N_m takes the values 1, 2, 3, 4, etc., $N = N_m - 1$. Figure 4.8 shows the ratio of the modeled inter-metal capacitance to the measured inter-metal capacitance for the inductors in table 3.2. The figure shows that our inter-metal capacitance model is accurate to within 40% on average. Indeed, this is not a large error if we are dealing with frequencies that are well below the self-resonant frequency of the inductor. This is because the Q-factor is not too sensitive to such errors in C_p at frequencies that are well below the self-resonant frequency. However, the error might become significant when we are dealing with frequencies that are extremely close to the self-resonant frequency.

4.6 Accuracy of the entire model

We would like to determine the accuracy of the overall model. This is accomplished by comparing Q-factors computed using the model to measured Q-factors and by also comparing Y11 and Y21 data computed using the model, to measured data. Figures 4.9 - 4.13 show a comparison between the model and the measured data for inductors S1 and S17 of table 3.2. These figures show that the model is very accurate (to within 20%) for frequencies up to 10 GHz for the two inductors. In general, the model is accurate to within 20% on average for frequencies up to the self-resonant frequency of the inductor. The accuracy is more pronounced at frequencies that are well below the self-resonant frequency.

4.7 Limitations of the model

The scalable integrated inductor model that we have developed, is specifically for AlCu metallization. This is because the metal resistance model is an empirical model derived specifically for this type of metallization. If we have a different metallization, we will have to re-model the metal resistance to properly account for the skin effect and the proximity effect in that particular metal. The equations for all the other elements are independent of the type of metallization (as long as the metallization is non-magnetic).

4.8 Summary

The following points summarize the main results of this chapter:

1. The Greenhouse formula [6] for calculating the metal inductance is accurate to within 10% on average. It is more accurate than the formula of Craninckx et al [4].

2. The scalable inductor model that we have developed for AlCu metallization predicts the Q-factor accurately to within 20% on average for frequencies up to the self-resonant frequency of the inductor. The accuracy is more pronounced at frequencies that are well
below the self-resonant frequency.

Chapter 5

Optimization

Now that we have developed an accurate model for the integrated inductor, we would like to use the model to develop a simulator which we would then use to design optimized inductor structures. In this chapter we state the optimization problem, discuss our approach to solving it, and then present the optimization results.

5.1 Optimization problem

The optimization problem can be stated as follows: given an inductance value, the details of the processing technology, and a frequency of interest, we want to know what values of the fundamental layout parameters - metal line width, metal line spacing, center opening dimension, and number of turns - give the maximum Q-factor, subject to the following constraints:

- 1. Self-resonant frequency must be at least 10 GHz.
- 2. The area of the inductor must be no greater than $2.12 \times 10^5 \mu m^2$.

In this thesis, the frequencies of interest are 1 GHz, 1.8 GHz, and 2.4 GHz, and the inductances are in the range 2 nH - 12 nH. It is important to note that we are not trying to design inductors with the minimum possible areas. Our focus in this thesis is on maximizing the Q-factor at certain frequencies for inductor structures with reasonable areas.

5.2 Approach to solving optimization problem

To solve the optimization problem we developed a simple simulator that uses the matlab constrained optimization routine 'constr' [10]. The simulator incorporates the yparameter equations (equations 3.1 and 3.2), the Q-factor equation (equation 2.5), and all the model equations of chapter 4 expressed as functions of the fundamental parameters and frequency, with the processing parameters in these equations set to the values dictated by the given processing technology. It takes the given frequency, the given inductance, the minimum allowed self-resonant frequency, any necessary bounds on the fundamental parameters, and a starting iteration point as its inputs. It then maximizes the Q-factor at the specified frequency with respect to the fundamental parameters, subject to all the constraints. The values of the fundamental parameters that give the maximum Q-factor at the frequency of interest, and the maximum Q-factor value are its outputs.

Running the optimization simulations to get valid inductor designs involves the following steps:

1. Specify the inductance, frequency of interest, and the minimum self-resonant frequency.

2. Set the necessary bounds on the fundamental parameters to ensure that the area constraint is met.

3. Specify a starting iteration point, i.e. the values of the fundamental parameters that serve as the starting iteration values. Obviously, these values should lie within the bounds specified in step 2 above.

4. Run the simulation to obtain the optimal fundamental parameters and the optimal Q-factor.

5. Choose several other starting iteration points and run the simulation to ensure that the resulting optimal Q-factor is a global as opposed to a local maximum.

75

5.3 Optimization results

We did optimization simulations for five design categories. In each of these categories, we used the basic Analog Devices RF technology with the following changes in metal line thickness and oxide thickness (in the design categories 'a Mx - b My' represents metal level 'x' of thickness 'a' microns via metal level 'y' of thickness 'b' microns).

1. Design Category I: In this category, the metal line thickness is 1.9 microns (metal one via metal two: 0.8 M1-1.1 M2) and the oxide thickness is 1.15 microns. Figures 5.1 and table 5.1 show the features of the inductors in this category.

2. Design Category II: Here, we used a metal line thickness of 2 microns (metal level two only: 2 M2), and an oxide thickness of 2.1 microns. The results are shown in figure 5.2 and table 5.2.

3. Design Category III: In this category, the metal line thickness is 3 microns (metal level two only: 3 M2) and the oxide thickness is 2.1 microns. The results are depicted in figure 5.3 and table 5.3.

4. Design Category IV: In this category, the metal line thickness is 3 microns (metal level three only: 3 M3) and the oxide thickness is 3.1 microns. Figure 5.4 and table 5.4 show the features of the inductors in this category.

5. Design Category V: Here the metal line thickness is 4 microns (metal level two via metal level three: 1 M2-3 M3), and the oxide thickness is 2.1 microns. The results are shown in table 5.5 and figure 5.5.

All the inductors that we have designed need to be fabricated and characterized in order for us to test the accuracy of the optimization scheme.

In all the designs, the shortest distance from the outer edge of the inductor to the center

of the substrate contact (D_p) has been set to 200 microns. The reason for this choice is because this is the optimal distance for all the inductors we characterized. If we make this distance as another unknown in the optimization program, our substrate resistance model will force the simulator to choose D_p to be infinite. This is because this choice makes the substrate resistance infinite and causes the Q-factor to increase considerably. Our model for the substrate resistance is valid for cases where the back of the wafer is not a good AC ground, and the only ground is at the substrate contacts. This occurs when the distance to the back of the wafer is much greater than the horizontal distance to the substrate contacts. If the horizontal distance from the inductor edge to the substrate contacts becomes as large as the wafer thickness, then for back-lapped wafers, the back of the wafer sitting on the chuck during measurement will be an effective AC ground. This will then invalidate our assumption of a coplanar ground only, and will necessitate the inclusion of vertical resistors in our model for the substrate resistance. Since we did not characterize an inductor with such a feature, we do not know exactly when the back of the wafer will start behaving as a good AC ground. Hence, we have simply set the distance in question to the optimal value for all the inductors characterized. It is necessary for Analog Devices Inc., to design inductors with substrate contacts placed at distances from the inductor that are of the order of the substrate thickness. This will enable them to know when the back of the wafer starts to behave as a good AC ground, and to study how the back of the wafer serving as a good AC ground contact affect the Q-factor.

L _m (nH)	f (GHz)	Q-factor	W _m (μ <i>m</i>)	S _m (µm)	N _m	C _m (μ <i>m</i>)
2	1	6.3	47.4	4.3	1.6	300
2	1.8	6.2	29.1	4.6	2.1	190.6
2	2.4	5.9	19.8	3.9	2.3	164.1
4	1	4.9	23.1	2.0	3.2	177.3
4	1.8	4.7	13.6	2.0	4.2	111.2
4	2.4	4.5	9.6	2.0	4.4	99.1
6	1	4.2	15.4	2.0	4.7	128.6
6	1.8	4.0	9.2	2.0	5.9	81.5
6	2.4	3.7	6.6	2.0	6.2	74.8
8	1	3.7	11.6	2.0	6.0	103.1
8	1.8	3.5	7.0	2.0	7.4	66.1
8	2.4	3.2	5.0	2.0	7.7	62
10	1	3.3	9.4	2.0	7.2	87.2
10	1.8	3.1	5.6	2.0	8.7	56.6
10	2.4	2.8	5.0	2.0	8.8	57.1
12	1	3.1	7.9	2.0	8.3	76.3
12	1.8	2.8	5.0	2.0	9.8	50.1
12	2.4	2.4	5.0	2.0	9.7	53.7

<u>Table 5.1: Fundamental layout parameter values for inductors in design category I</u> 0.8 M1-1.1 M2).

It is clear from the optimization results (in tables 5.1 - 5.5 and figures 5.1 - 5.5) that to meet the Q-factor specification of our design problem (Q-factor in the range 3-12), we have to use design category V. This means that we have to use metal levels two and three, with a via connecting the two to simulate a thicker metal. It is also clear that we can improve the existing metal level one via metal level two designs that Analog Devices cur-

rently has, by appropriate choices of the fundamental layout parameters. Q-factors in the range 2.4 - 6.3 can be obtained in the frequency range of 1 GHz - 2.4 GHz, with the current metallization (metal level one via metal level two).

Another interesting observation that is clear from the results is that it is better to have a thicker metal and a thinner oxide (the oxide should be at least 1.15 microns thick), than a higher level thinner metal with a very thick oxide. For instance, it is better to have metal level two via metal level three with a total metal thickness of 4 microns and an oxide thickness of 2.1 microns, than just 3 microns of metal level three and an oxide that is 3.1 microns thick. The reason for this is that the decrease in the DC resistance resulting from using a thicker metal has a more significant effect on the Q-factor than the decrease in the oxide capacitance caused by the thicker oxide.

3



Figure 5.1: Graph of optimal Q-factor versus inductance for inductors in design category I (0.8 M1-1.1 M2)

L _m (nH)	f (GHz)	Q-factor	W _m (μ <i>m</i>)	S_m (μm)	N _m	C _m (μ <i>m</i>)
2	1	6.8	47.1	4.6	1.6	300
2	1.8	6.5	28.0	4.5	2.0	197.8
2	2.4	6.2	18.9	3.8	2.2	169.2
4	1	5.3	23.7	2.2	3.0	199.3
4	1.8	4.9	13.1	2.0	4.0	117.9
4	2.4	4.7	9.2	2.0	4.3	103.4
6	1	4.5	15.7	2.0	4.4	145.8
6	1.8	4.2	8.8	2.0	5.7	87.1
6	2.4	3.9	6.3	2.0	6.0	78.3
8	1	4.0	11.9	2.0	5.7	117.6
8	1.8	3.7	6.7	2.0	7.2	71.0
8	2.4	3.4	5.0	2.0	7.5	65.4
10	1	3.7	9.5	2.0	6.8	100
10	1.8	3.3	5.4	2.0	8.5	60.9
10	2.4	2.9	5.0	2.0	8.6	59.4
12	1	3.3	7.9	2.0	7.9	87.9
12	1.8	2.9	5.0	2.0	9.6	55.1
12	2.4	2.5	5.0	2.0	9.6	55.1

<u>Table 5.2: Fundamental layout parameter values for inductors in design category II</u> (2 M2).

Furthermore, the designs (particularly the lower inductance designs) tend to have large center openings and small number of turns. Indeed, this validates the claim we made in chapter 3. As we stated, the reason why such designs are better is that they reduce the proximity effect considerably (the net proximity effect depends on both the metal line spacing and the number of turns). Also, for low values of inductance, the designs seem to



Figure 5.2: Graph of optimal Q-factor versus inductance for inductors in design category II (2 M2)



Figure 5.3: Graph of optimal Q-factor versus inductance for inductors in design category III (3 M2)

L _m (nH)	f (GHz)	Q-factor	W _m (μ <i>m</i>)	S_m (μm)	N _m	C _m (μ <i>m</i>)
2	1	9.0	44.0	4.1	1.8	249.1
2	1.8	8.5	22.0	3.4	2.4	156.2
2	2.4	8.0	15.3	3.0	2.5	135.5
4	1	7.0	21.5	2.0	3.7	141.1
4	1.8	6.4	10.8	2.0	4.5	94.7
4	2.4	5.9	7.8	2.0	4.7	93.0
6	1	5.9	14.4	2.0	5.2	101.2
6	1.8	5.3	7.4	2.0	6.3	71.4
6	2.4	4.8	5.4	2.0	6.6	65.9
8	1	5.2	10.9	2.0	6.7	80.0
8	1.8	4.5	5.7	2.0	7.8	59.1
8	2.4	4.0	5.0	2.0	7.9	57.1
10	1	4.7	8.8	2.0	7.9	66.8
10	1.8	4.0	5.0	2.0	9.0	52.1
10	2.4	3.4	5.0	2.0	9.0	51.7
12	1	4.2	7.4	2.0	9.1	57.7
12	1.8	3.5	5.0	2.0	9.9	50.0
12	2.4	2.9	5.0	2.0	9.9	50.0

Table 5.3: Fundamental layout parameter values for inductors in design category III (3 M2).

have very wide metal lines. This is particularly true for the 1 GHz designs. The reason for this is that increasing the line width at such a frequency reduces the DC resistance considerably without increasing the skin effect that much.

The designs for the higher inductance values do not use all the available area. In fact they use smaller areas compared to some of the lower inductance inductors. This seems

L _m (nH)	f (GHz)	Q-factor	W _m (µm)	S_m (μm)	N _m	$C_{\rm m}$ (μm)
2	1	9.7	46.9	4.7	1.6	300.0
2	1.8	8.9	22.1	3.6	2.1	185.0
2	2.4	8.3	15.2	3.1	2.3	156.6
4	1	7.5	22.9	2.3	3.2	181.8
4	1.8	6.7	10.9	2.0	4.1	114.0
4	2.4	6.2	7.8	2.0	4.4	98.0
6	1	6.4	15.2	2.0	4.6	133.9
6	1.8	5.6	7.4	2.0	5.8	85.8
6	2.4	5.0	5.4	2.0	6.2	75.3
8	1	5.7	11.4	2.0	5.9	108.1
8	1.8	4.8	5.7	2.0	7.3	70.8
8	2.4	4.2	5.0	2.0	7.6	63.9
10	1	5.1	9.2	2.0	7.1	91.8
10	1.8	4.2	5.0	2.0	8.5	61.6
10	2.4	3.5	5.0	2.0	8.8	56.7
12	1	4.7	7.7	2.0	8.2	80.6
12	1.8	3.7	5.0	2.0	9.6	55.4
12	2.4	3.0	5.0	2.0	9.8	51.7

Table 5.4: Fundamental layout parameter values for inductors in design category IV (3 M3).

puzzling at first sight. However, it tells us that for every inductance value, there exists an optimal area. This is the area for which the losses of the inductor are minimum, subject to the constraints.

The designs at 1 GHz are better than those at 1.8 GHz and 2.4 GHz. This is because the simulator finds it easier to minimize the losses at 1 GHz. Finally, we see that the higher the



Figure 5.4: Graph of optimal Q-factor versus inductance for inductors in design category IV (3 M3)



Figure 5.5: Graph of optimal Q-factor versus inductance for inductors in design category V (1 M2-3 M3)

L _m (nH)	f (GHz)	Q-factor	W_m (μm)	S_m (μm)	N _m	$C_{\rm m}$ (μm)
2	1	10.9	40.6	3.8	2.1	194.4
2	1.8	10.1	19.1	2.9	2.6	133.5
2	2.4	9.5	13.4	2.5	2.7	117.3
4	1	8.4	19.6	2.0	4.1	112.1
4	1.8	7.5	9.6	2.0	4.8	82.2
4	2.4	6.9	7.0	2.0	5.0	75.4
6	1	7.0	13.0	2.0	5.7	81.7
6	1.8	6.1	6.6	2.0	6.6	63.1
6	2.4	5.5	5.0	2.0	6.8	59.8
8	1	6.1	9.8	2.0	7.2	65.9
8	1.8	5.2	5.1	2.0	8.1	53.0
8	2.4	4.5	5.0	2.0	8.2	52.3
10	1	5.4	7.8	2.0	8.4	56.1
10	1.8	4.4	5.0	2.0	9.1	50.0
10	2.4	3.7	5.0	2.0	9.1	50.0
12	1	4.9	6.6	2.0	9.6	50.0
12	1.8	3.8	5.0	2.0	9.9	50.0
12	2.4	3.1	5.0	2.0	9.9	50.0

<u>Table 5.5: Fundamental layout parameters values for inductors in design category V</u> (1 M2-3 M3)

inductance, the lower the optimal Q-factor attained. This is because the higher the inductance, the disproportionately higher the inductor losses.

5.4 Sensitivity studies

We would like to study the sensitivity of the optimal Q-factor to changes in certain par-

-ameters that were held constant for the inductors in design categories I - V. In particular, we want to study the sensitivity of the optimal Q-factor to changes in D_p (the shortest distance from the outer edge of the inductor to the grounded pads or substrate contacts), the p-bulk substrate resistivity, and the substrate composition. For this study, we will consider an 8 nH inductor, and the frequency of interest is 1 GHz. The area constraint and the self-resonant frequency constraint remain the same as in design categories I - V, while the metal line thickness and the oxide thickness used in this study are 4 microns and 2.1 microns respectively.

5.4.1 Sensitivity of Optimal Q-factor at 1 GHz to changes in D_p

For the inductors in design categories I - V, we set D_p to 200 microns for reasons specified in section 5.3. Now we want to see what happens when D_p takes values in the range 50 microns - 200 microns. Figure 5.6 shows the resulting optimal Q-factor at 1 GHz for an 8 nH inductor. As shown in that figure, the higher D_p is, the higher the optimal Q-factor attained. The reason for this is that the higher the value of D_p , the higher the substrate resitance since the distance to the substrate contact increases. What this tells us, is that if the back of the wafer sitting on the chuck during measurement is always floating (i.e. it is not an AC ground), then we should make D_p as large as possible (ideally we want D_p to be infinite in this case).

5.4.2 Sensitivity of optimal Q-factor at 1 GHz to changes in p-bulk layer resistivity

From our model of the substrate resistance, we see that the higher the resistivity of the p-bulk layer, the higher the substrate resistance, and consequently, the higher the Q-factor. The question though is how high does the p-bulk layer resistivity need to be for us to attain certain improvements in the Q-factor. Figure 5.7 which shows a graph of optimal Q-factor

at 1 GHz versus bulk layer resistivity provides the answer to our question. Looking at the figure closely, we see that the optimal Q-factor seems to saturate at higher resistivity values. The reason for the seeming saturation effect has to do with the composition of the entire substrate. As shown in figure 1.1 in chapter 1, the substrate of the standard Analog Devices RF technology has three layers: the p-buried layer, the p-field implant and the pbulk layer. The model for R_s (twice the substrate resistance) is a parallel combination of three resistors, each representing one of the layers. Increasing the p-bulk layer resistivity only increases the resistance of the p-bulk layer. As we start to increase this resistivity, we see a significant increase in the net substrate resistance because the p-bulk resistance dominates the parallel combination of the resistors (since it is the smallest of the three). When the bulk resistance becomes higher than the resistances of the other layers, the substrate resistance is then dominated by these other resistances (particularly the resistance of the pburied layer since this layer has a lower sheet resistance than the p-field implant layer). At this point an increase in the p-bulk resistance only leads to a very small increase in the net substrate resistance.

5.4.3 Sensitivity of optimal Q-factor at 1 GHz to changes in the composition of the substrate.

We would like to know how the optimal Q-factor changes when we change the composition of the substrate. In particular, we want to know what happens to the optimal Q-factor if we remove both the p-buried layer and the p-field implant, and if we only remove the p-buried layer. Figure 5.8 shows the results of changing the substrate composition. It is clear from this figure that we need not remove the p-field implant. We only need to remove the p-buried layer for the standard Analog Devices RF processing technology. For this technology, the parallel combination of the p-bulk resistance, the p-buried layer resistance and the p-field implant layer resistance is dominated mostly by the first because it is the smallest of the three. The resistance of the p-buried layer is the second dominant resistance in the parallel combination. Because of the presence of this layer, the substrate resistance is less than the resistance of the p-bulk layer. Removing it, greatly increases the dominance of the p-bulk layer and causes the substrate resistance to be approximately equal to the resistance of the p-bulk layer.

The p-field implant has the highest resistance of the three layers and does not affect the net substrate resistance that much. If we remove it, we only get a small increase in the Q-factor. However, if we want to increase the Q-factor by significantly increasing the resistivity of the p-bulk layer, then we have to remove both the p-buried layer and the p-field implant layer as we found in section 5.4.2.



Figure 5.6: Graph of optimal Q-factor versus inductor-to-grounded pad distance (D_p).



Figure 5.7: Graph of optimal Q-factor versus bulk layer resistivity.



Figure 5.8: Graph of optimal Q-factor versus substrate composition parameter. $(L_m = 8 \text{ nH}, f = 1 \text{ GHz})$

5.5 Summary

The following points summarize the main results of this chapter.

1. By appropriately choosing the layout parameter values, we can design inductors with Q-factors in the range 2.4 - 6.3 for frequencies of 1 GHz - 2.4 GHz and inductances of 2 nH - 12 nH, using the standard Analog Devices RF processing technology that provides a 1.9 microns metal thickness (metal level one via metal level two). These inductors have a self-resonant frequency of at least 10 GHz.

2. By using a metal thickness of 4 microns and an oxide thickness of 2.1 microns, we can design inductors with Q-factors in the range 3 - 10.9 for the same inductance and frequency ranges mentioned in point 1 above.

3. To obtain optimal Q-factors greater than 11 in the range 1 GHz - 2.4 GHz for inductors with self-resonant frequencies of at least 10 GHz and inductances of 2 nH - 12 nH, drastic processing technology changes are needed. Some of these changes are discussed in chapter 6.

4. Sensitivity studies show that as long as the back of the wafer is not a good AC ground, D_p must be as large as possible in order to achieve the maximum possible Q-factor.

5. If we want to increase the Q-factor by significantly increasing the resistivity of the bulk, we have to remove both the buried layer and the field implant layer.

6. Removing the buried layer from the substrate leads to an increase in the Q-factor, with all other variables remaining unchanged.

90

Chapter 6

Conclusion

In this chapter we briefly summarize what we have found, and make recommendations for designing inductors that are better than those that we have designed. It is important to note that the inductors that we have designed need to be fabricated and characterized for our claims to be substantiated.

6.1 The findings of this thesis

We have shown that we can model integrated inductors with a simply lumped element equivalent circuit. Using the y and z-parameter equations of this circuit, we have derived an accurate extraction mechanism that enables us to extract the values of the equivalent circuit elements from experimental data. The results of the extraction and our understanding of the physics of silicon integrated inductors enabled us to make the equivalent circuit model scalable. The scalable model is accurate to within 20% on average for frequencies up to the self-resonant frequency of the inductor, and is therefore a useful design tool. It is important to note that this model is specifically for AlCu metallizations, because the metal resistance formula is an empirical formula derived specifically for this type of metallization. If we have a different metal type, we have to re-model the metal resistance to properly account for the skin effect and the proximity effect in the metal in question. The models for the other equivalent circuit elements will remain unchanged (provided the new metal is non-magnetic).

With our model, we have developed a simulator with which we have demonstrated that with the current RF processing technology at Analog Devices Inc., that provides a metal thickness of 1.9 microns (metal level one via metal level two), inductors with Q-factors of 2.4 - 6.3 in the 1 GHz - 2.4 GHz frequency range, can be designed for inductances of 2 nH - 12 nH. Indeed, this is a great improvement when compared to the Q-factors of 1 - 4 that have been achieved with this process in the frequency range of interest. In addition to this, by adding a third level of metal, we have designed inductors with Q-factors of 3 - 10.9 in the frequency range of interest, for inductances of 2 nH - 12 nH. These inductors have self-resonant frequencies of at least 10 GHz, and outer dimensions of at most 400 microns by 400 microns. Hence, we have been able to meet our design objective with only a slight change in the standard Analog Devices RF processing technology.

The high Q-factor inductors that we have designed will enable designers at Analog Devices Inc., to use matching networks, inductive loading techniques, etc., on silicon integrated circuits if they work as we have claimed. Indeed, these inductors will give the circuit designers a lot of flexibility in their effort to design circuits that meet increasing consumer demands for low power dissipation and long battery life, and in their attempt to use silicon technologies in the fast emerging broadband and wireless communications market.

6.2 Recommendations

To design a high Q-factor inductor, the inductor losses must be minimized. There are two ways of achieving this in silicon, namely:

- 1. Choosing the layout/structural parameters appropriately.
- 2. Making changes to the current standard silicon process.

In this thesis, we have combined both methods in coming up with our designs. However, we only made a slight change to the standard RF processing technology at Analog Devices (by basically increasing the metal line thickness), and focused mainly on choosing the values of the layout parameters that yield the optimal Q-factors at the frequencies of interest. With this technique, we only achieved Q-factors in the range 3 - 10.9. To get Q-factors higher than this, we definitely have to make more changes to the processing technology. Some of these changes are discussed below.

6.2.1 Increasing the metal line thickness

Increasing the metal line thickness is by far the most popular modification that has been made to the standard silicon technology in an effort to design high Q-factor inductors. The reason for this is that the most important loss mechanism is the metal resistive loss, and increasing the metal line thickness reduces this loss considerably by decreasing the DC resistance of the metal line. However, it causes the skin effect to be more effective. It is a fact that for the range of thicknesses that we are talking about (up to 5 or 6 microns), the decrease in the DC resistance outweighs the skin effect introduced. Some people have achieved a thicker metal by using more levels of metal [1]. Indeed, it is not necessary for Analog Devices Inc., to introduce metallization up to metal level four in an attempt to make better inductors. All that needs to be done is to introduce a very thick metal level three on top of the existing metal level two.

6.2.2 Changing the metallization type

One way of reducing the metal line resistance is by increasing the conductivity of the metal. The current metallization type for the standard silicon process is aluminum. By changing the metallization type to copper or gold, a higher metal conductivity will be obtained [11], [12].

6.2.3 Increasing the substrate resistivity

The conductive loss in the silicon substrate is one of the reasons why it is difficult to design high Q-factor inductors on silicon. To make this point clearer, let us consider GaAs. Q-factors as high as 120 have been obtained for single loop inductors fabricated on GaAs [13]. The reason for this is that GaAs substrates can be fabricated with very high resistivities. In terms of our model, this means that the substrate resistance for GaAs substrates is infinite [14]. The loss in the silicon substrate causes the substrate resistance to be finite and much smaller compared to that achieved with GaAs. To reduce the loss in the substrate, it is necessary to increase the resistivity of the substrate. This will increase the substrate resistance considerably, and consequently increase the Q-factor and the self-resonant frequency [3], [11].

For the standard Analog Devices RF processing technology, increasing the substrate resistivity does not mean increasing the resistivity of the p-bulk layer only. It can be achieved either by increasing the resistivity of all the layers of the substrate, or by simply increasing the resistivity of the p-bulk layer and removing both the p-buried layer and the p-field implant layer.

6.2.4 Using SOI

In an effort to reduce the influence of the substrate, we can put a layer of SOI between the oxide and the substrate. The insulating nature of the SOI will cause an increase in the Q-factor and the self-resonant frequency. The thicker the SOI layer that is used, the higher the Q-factor and the self-resonant frequency will be.

6.2.5 Increasing the thickness of the oxide

Another way of reducing the effect of the substrate is to increase the thickness of the oxide that isolates the metal lines from the silicon substrate. This will decrease the oxide

94

capacitance, and consequently decrease the amount of current (displacement current) that flows into the silicon substrate. It will therefore increase the Q-factor and the self-resonant frequency.

6.2.6 Making use of trenches in the substrate

By building trenches filled with an insulator in the substrate, we can break the path of current flow in the substrate. Theoretically, this should make the substrate appear as an open circuit thereby eliminating both the substrate loss and the oxide capacitive loss. Consequently, it should increase the Q-factor and the self-resonant frequency.

6.2.7 Etching away the silicon substrate

A more drastic way of minimizing the silicon substrate loss is to etch away the silicon underneath the inductor. Indeed this will make the substrate resistance infinite and also make the oxide capacitance ineffective. This should increase the Q-factor and the self-resonant frequency, something that has been substantiated [15].

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