**Lecture #31: Electronic Spectra of Polyatomic Molecules**

Electronic spectra are more complex than vibration-rotation spectra. Polyatomic molecule spectra are more complex than diatomic molecule spectra.

* Many vibrational properties (such as Franck-Condon factors) can’t be calculated because we know too little about $V'(Q')$ and $V''(Q'')$.

QUALITATIVE IDEAS LIKE NODE COUNT STILL WORK!

* Inter-surface interactions are more subtle in $3N-6$ dimensions than in 1 dimension (avoided crossings along high symmetry directions).


This subject is so complex that only a case-by-case approach seems feasible.

Some crucial background information:

1. **Electronic States** ← electronic configurations ← MO’s.
   - symmetry labels
   - effect of each orbital on favored molecular shape (i.e. $R_{AB}$’s and $k_{AB}$’s and $\theta_{ABC}$’s)
   - Qualitative MO Theory e.g. Walsh diagrams
   - localization of orbitals onto “chromophores”

   concept of chromophores is an enormous simplification because:
   * its orbitals and electronic properties are known from other molecules
   **** large changes in molecular shape are confined to the region of the chromophore.

2. **Electronic Transitions**
   - A single orbital promotion, e.g. $\pi^* \leftrightarrow n$, gives direction of transition moment relative to body fixed $\hat{a}$, $\hat{b}$, $\hat{c}$ axes ← **rotational selection rules**
   - direct product $\Gamma_i \otimes \Gamma_f$

   Often **mixed transition type** when chromophore does not lie $||$ on $\perp$ to a principal axis.
   E.g. HCO $\tilde{B}^2 A'-\tilde{X}^2 A'$ ($\bar{u}_{AB}$ in plane of molecule)

   Often **axis-switching effects** when $\hat{a}$, $\hat{b}$, $\hat{c}$ are not oriented the same way in both electronic states because of a large change in geometry

   e.g. $\tilde{A}^1 A_g$ $\tilde{X}^1 \Sigma^+_g$ $\pi^* \leftrightarrow \pi$ in HCCH
3. **Vibrational Structure**

**Symmetry** selection rules for vibrational bands in an allowed electronic transition

\[ \Gamma_{v'} \otimes \Gamma_{v''} \subseteq \Gamma_{\text{totally symmetric}} \]

allowed to see: all \( v \) of totally symmetric mode

alternate (even) \( v \)'s of non totally symmetric modes except in combination with other non-totally symmetric modes

**FRANCK-CONDON** propensity rules

\( \Delta v = 0 \) for all normal modes that are unchanged by \( \phi' \leftarrow \phi'' \) electronic transition.

Long progressions in modes exhibiting large change in \( \omega \) and \( Q_e \) - just as for diatomic molecules.

Only modes localized on the chromophore are expected to exhibit Franck-Condon activity.

Massive Simplification! Crucial diagnostic!

**Symmetry Forbidden Electronic Transitions**

\[ \left( \Gamma_{v'} \otimes \Gamma_{v''} \right) \subseteq \Gamma_{\text{totally symmetric}} \]

a non-totally symmetric normal mode distorts the molecular framework and causes to be mixed in some character of another electronic state that would give rise to a symmetry allowed electronic transition in the lower symmetry point group. In this case the vibrational intensity depends strongly on the number of quanta in the non-totally symmetric “promoting mode”.

See Vibronic coupling handout and the \( \text{H}_2\text{CO} \ A^1 \sim A_2 - X^1 \ A_1 \) transition.

4. **Rotational Structure**

a, b, or c-type selection rules determined by

\[ \Gamma_{v'} \otimes \Gamma_{v''} \quad \text{or} \quad \Gamma_{ev'} \otimes \Gamma_{ev''} \]

electronically allowed vibronically allowed

crucial clue to symmetry assignment.

Large changes in A, B, C rotational constants:

* spectra look much more complex than a vibration-rotation band because Q branches are not line-like and do not fall into regular patterns of sub-bands;

* crucial key to configurational assignment because the A, B, and C rotational constants tell us about gross changes in equilibrium geometry.
Two classic examples:

1. The trans-bent $\pi^* \leftarrow \pi$ excited state of HCCH

2. The non-planar $\pi^* \leftarrow n$ excited state of H$_2$CO

Acetylene has a linear ground state

```
I \Sigma^+_g \quad 14 \text{ total } e^- \quad \text{HOMO} \quad \text{LUMO}
```

C 1s

H1s, C2s

C–C

σ-bond

C 2p

π-bonds

π*

Some sp polarization

Numbering within symmetry type is in order of energy and number of nodal surfaces. Listed in increasing energy order.

What are the plausibilities for the upper state of a $\pi^* \leftarrow \pi$ transition?

| Linear Upper State | \( \pi^* \leftarrow \pi \) Transition | Symmetry
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
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</thead>
<tbody>
<tr>
<td><strong>cis-bent</strong></td>
<td><img src="image1.png" alt="Diagram" /></td>
<td>( C_{2v} )</td>
</tr>
<tr>
<td>Four Possibilities</td>
<td><img src="image2.png" alt="Diagram" /></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Hole in ( \pi ) (( \pi^- )) in plane ( \perp ) to plane</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Single ( e^- ) in plane ( \perp ) to plane in ( \pi^* ) (( \pi^+ ))</td>
<td></td>
</tr>
<tr>
<td><strong>trans-bent</strong></td>
<td><img src="image3.png" alt="Diagram" /></td>
<td>( C_{2h} )</td>
</tr>
</tbody>
</table>

Again, 4 possibilities for $\pi^- \text{ and } \pi^*$ orientations.
<table>
<thead>
<tr>
<th>Structure</th>
<th>Symmetry</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>Vinylidene</td>
<td>$C_{2v}$</td>
<td>$\pi^* \leftarrow \pi$ gives $^1\Delta_u$, $^3\Delta_u$, $^1\Sigma_u^+$, $^3\Sigma_u^+$, $^1\Sigma_u^-$, $^3\Sigma_u^-$ states, all of which except $^1\Sigma_u^+$ are forbidden from $^1\Sigma_g^+$.</td>
</tr>
<tr>
<td>Diborane bridged structure</td>
<td>$D_{2h}$</td>
<td>Refer to Bogey <em>Phys. Rev. Lett.</em> <strong>66</strong> 413 (1991) for non-planar structure.</td>
</tr>
<tr>
<td>Non-planar (like HOOH)</td>
<td>$C_2$</td>
<td>Near trans or cis.</td>
</tr>
<tr>
<td>Unequal CH bond lengths</td>
<td>$C_s$</td>
<td>Planar or non-planar.</td>
</tr>
</tbody>
</table>

Linear possibility unlikely because $\pi^* \leftarrow \pi$ gives $^1\Delta_u$, $^3\Delta_u$, $^1\Sigma_u^+$, $^3\Sigma_u^+$, $^1\Sigma_u^-$, $^3\Sigma_u^-$ states, all of which except $^1\Sigma_u^+$ are forbidden from $^1\Sigma_g^+$. In CO and N$_2$ the analogous $^1\Sigma_u^+$ state is very high lying and above the first dissociation limit.

$^1\Sigma_u^+ \leftarrow ^1\Sigma_g^+$ is expected to have $\parallel$ type rotational selection rules (strong R, P, weak Q) and the observed bands obviously contain strong Q lines.

In addition, we do not expect the $\pi^* \leftarrow \pi$ states to be linear because a *trans*-bend distortion mixes the C–H bonding $2\sigma_u$ MO into the $\pi^*$ MO, thereby strengthening the two CH bonds AND DIMINISHING the anti-bonding interaction between the C’s

OR

a *cis*-bend distortion mixes the CH bonding $2\sigma_g$ MO into the $\pi^*$ MO, thereby strengthening the two CH bonds.

So we expect the $\pi^*$ and $\pi$ possibilities to be most likely.
Electronic Spectra of Polyatomic Molecules

Last time: Survey of relevant factors

* symmetry selection rules
* electronic
* vibrational
* rotational

* propensity rules
localization onto chromophores
Franck-Condon factors
* expected shapes of molecules
predictions based on qualitative MO theory
proof of one vs. other structure based mostly on group theory

The $S_1 \leftarrow S_0$ transition in HCCH (first to be rotationally analyzed) rules out linear excited state.

Today: 1. Why would the HCCH $\pi^* \leftarrow \pi$ excited states want to be bent? QMOT (Qualitative Molecular Orbital Theory)
2. rule out \[assignment]
3. support for \[assignment]

How do various MOs respond to distortion of the molecular shape: e.g. HCCH?

For QMOT, look at books by John Lowe, Gimarc, and papers by Walsh.

The following diagram shows how MOs in acetylene change energy as the molecule is distorted from linear to cis-bent (left side of diagram) or linear to trans-bent (right side of diagram).
Anti-bonding interactions are always slightly more unfavorable energetically than corresponding bonding interactions.

<table>
<thead>
<tr>
<th>$\text{C}_{2v}$</th>
<th>$E$</th>
<th>$\text{C}_2(z)$</th>
<th>$\sigma_v(xz)$</th>
<th>$\sigma_v(yz)$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$A_1$</td>
<td>1</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>$z$</td>
<td></td>
</tr>
<tr>
<td>$A_2$</td>
<td>1</td>
<td>1</td>
<td>$-1$</td>
<td>$-1$</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>$R_z$</td>
<td></td>
</tr>
<tr>
<td>$B_1$</td>
<td>1</td>
<td>$-1$</td>
<td>1</td>
<td>$-1$</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>$T_x, T_y$</td>
<td></td>
</tr>
<tr>
<td>$B_2$</td>
<td>1</td>
<td>$-1$</td>
<td>$-1$</td>
<td>1</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>$T_y, R_x$</td>
<td></td>
</tr>
</tbody>
</table>

$(a, b, c) = (x, z, y)$
\( \pi^* \) in plane \( B_1 \) symmetric with respect to \( \sigma_v(xz) \) anti-symmetric with respect to \( \sigma(yz) \).

\( \perp \) plane \( A_2 \)

\( \pi^{-1} \) in plane \( A_1 \)

\( \perp \) plane \( B_2 \)
favors bent

The only allowed transition is \( B_1 \leftarrow A_1 \) \( = \Sigma_g^+ \) which is a-type \( \Delta K_a = 0 \), weak Q, which does not agree with spectrum. Moreover, the \( B_1 \) excited states are expected to be either linear or only slightly bent.

Note the tilt (exaggerated as drawn)!!!!

\[
\begin{array}{|c|c|c|c|c|}
\hline
C_{2h} & E & C_{2(z)} & \sigma_h(xy) & i \\
\hline
A_g & 1 & 1 & 1 & 1 & R_z \\
A_u & 1 & 1 & -1 & -1 & T_z \\
B_g & 1 & -1 & -1 & 1 & R_x, R_y \\
B_u & 1 & -1 & 1 & -1 & T_x, T_y \\
\hline
\end{array}
\]

\( (a, b, c) = (x, z, y) \)

\( \pi^* \) in plane \( \perp \) plane \( B_g \) \( \leftrightarrow \) favors bent

\( \perp \) plane \( B_g \) \( \leftrightarrow \) neutral

\( \pi^{-1} \) in plane \( \perp \) plane \( A_u \) \( \leftrightarrow \) favors bent

\( \perp \) plane \( A_u \) \( \leftrightarrow \) neutral

excitation favors linear
neutral

favors bent
neutral

excitation favors linear
neutral

\( x, y = a, b \) next to lowest E weakly bent

\( z = c \) highest E linear

\( c \) lowest E strongly bent

\( a, b \) next to highest E linear
expect to find either c-type $^1A_u \leftarrow ^1\Sigma_g^+$ strongly bent
or a,b-type $^1B_u \leftarrow ^1\Sigma_g^+$ weakly bent

c-type $\Delta K_a = \pm 1$, $\Delta K_c = \text{even, strong Q}$
a-type $\Delta K_a = 0$, $\Delta K_c = \text{odd, weak Q}$
b-type $\Delta K_a = \pm 1$, $\Delta K_c = \text{odd, strong Q}$

$X^1\Sigma_g^+$ linear ground state is special because it has only $\ell = 0$ (which acts like $K_a$) in zero-point level.

This means that cold bands will sample only limited number of $K'_a$ values (0 and/or 1).

THIS IS WHY HCCH WAS 1ST POLYATOMIC MOLECULE FOR ROTATIONAL ANALYSIS OF AN ELECTRONIC TRANSITION.

Observed bands are probably c-type because they consist of strong $K' - \ell'' = \pm 1$ sub-bands and contain a strong Q branch. This can be checked because, for a near prolate asymmetric top, the prolate-oblate correlation diagram requires that the higher energy member of each asymmetry doublet have the lower $K_c$ value

$$J_{K_a} \quad K_c = J - K_a$$
$$\quad K_c = J - K_a + 1$$

and the magnitude of the asymmetry splitting is controlled mostly by B-C.

So we can figure out which rotational branches are naively\textsuperscript{*} allowed for c vs. a,b-hybrid transitions.

\textsuperscript{*} Neglecting nuclear spin and rovibronic symmetry requirements.
Supplement

\[ J + 1_{1J} \]
\[ J + 1_{1J+1} \]
\[ J_{1J-1} \]
\[ J_{1J} \]
\[ J - 1_{1J-2} \]
\[ J - 1_{1J-1} \]

\( ^2K_a = \) odd
\( ^2K_c = \) even

\( ^2K_a = \) odd
\( ^2K_c = \) odd

\( ^2K_a = \) even
\( ^2K_c = \) even

```
"Combination defects" ← a-type
R(J) - Q(J) = 2(J + 1)B' + 2 \( ^\prime \)
Q(J) - P(J) = 2JB' - 2 \( ^\prime \)
```

```
b-type
R(J) - Q(J) = 2(J + 1)B' - 2 \( ^\prime \)
Q(J) - P(J) = 2JB' + 2 \( ^\prime \)
```

```
no Q
```

What else do we expect?

Activity in the C-C stretch (expect frequency near that of ethylene ground state) because \( \pi^* \leftarrow \pi \) should weaken \( k_{CC} \) and lengthen \( r_{CC} \)

\( \omega_{CC} = 1623 \text{ cm}^{-1} \)

\( v_2 \) in \( \tilde{X} \)-State

Activity in the \textit{trans}-bend because the bend angle decreases from 180° (sp hybridization) and the bend frequency nearly doubles.
Small activity in symmetric CH stretch because CH might get slightly shorter and stronger (expect \(~3100 \text{ cm}^{-1}\)).

No activity in torsion (< 1000 cm\(^{-1}\)), antisymmetric (~3100) CH stretch, and antisymmetric in-plane bend (< 1000 cm\(^{-1}\)).

All Confirmed!

**Inertial defect** \(I_A + I_B - I_C = 0\) is useful criterion for planar molecule. All atoms in xz plane.
\[
\frac{1}{A} + \frac{1}{B} - \frac{1}{C} = -0.0044 \text{ cm}
\]

<table>
<thead>
<tr>
<th></th>
<th>( \tilde{A}_1 A_u )</th>
<th>( \tilde{X}^1 \Sigma_g^+ )</th>
</tr>
</thead>
<tbody>
<tr>
<td>trans-bend</td>
<td>( \nu_3 ) 1047.70 cm(^{-1})</td>
<td>( \nu_4 ) 608.26</td>
</tr>
<tr>
<td>C–C</td>
<td>( \nu_2 ) 1389</td>
<td>( \nu_2 ) 1973.5</td>
</tr>
<tr>
<td>A(_0)</td>
<td>12.94</td>
<td></td>
</tr>
<tr>
<td>B(_0)</td>
<td>1.1243</td>
<td>B 1.1766</td>
</tr>
<tr>
<td>C(_0)</td>
<td>1.0297</td>
<td></td>
</tr>
<tr>
<td>r(_{CH})</td>
<td>1.08Å</td>
<td>1.058</td>
</tr>
<tr>
<td>r(_{CC})</td>
<td>1.388Å</td>
<td>1.208</td>
</tr>
<tr>
<td>( \theta_{CCH} )</td>
<td>120°</td>
<td>180°</td>
</tr>
</tbody>
</table>