Measurement of inclusive neutral current π[superscript 0] production on carbon in a few-GeV neutrino beam

Citation

As Published
http://dx.doi.org/10.1103/PhysRevD.81.033004

Publisher
American Physical Society

Version
Final published version

Citable link
http://hdl.handle.net/1721.1/58943

Terms of Use
Article is made available in accordance with the publisher’s policy and may be subject to US copyright law. Please refer to the publisher’s site for terms of use.
Measurement of inclusive neutral current $\pi^0$ production on carbon in a few-GeV neutrino beam


(The SciBooNE Collaboration)

I. INTRODUCTION

Neutrino-nucleus cross sections have been intensively studied for decades. However, the precision and understanding of the cross sections around 1 GeV are still not satisfactory. The next generation of neutrino oscillation experiments will search for subleading flavor oscillation and charge-parity symmetry violation; the precision needed for these searches drives the need for more accurate independent measurements of neutrino cross sections [1,2]. Although several interaction channels contribute to the total neutrino-nucleus cross section in the neutrino energy range of a few GeV, an understanding of neutral current

1550-7998/2010/81(3)/033004(18) 033004-1 © 2010 The American Physical Society

DOI: 10.1103/PhysRevD.81.033004 PACS numbers: 13.15.+g, 13.60.Le, 25.30.Pt, 95.55.Vj
neutral pion production (NC $\pi^0$) is especially important. NC $\pi^0$ events form the largest $\nu_\mu$-induced background to neutrino experiments measuring $\nu_\mu \rightarrow \nu_e$ oscillations in the neutrino energy range of a few GeV or less, such as the T2K experiment [1]. NC $\pi^0$ events can mimic $\nu_e$ signal events when, for example, one of the two photons associated with $\pi^0 \rightarrow \gamma\gamma$ is not detected.

NC $\pi^0$ production has been measured by several past experiments [3–7]. However, their results have large uncertainty due to low statistics and are not useful expressions for predicting background in $\nu_\mu \rightarrow \nu_e$ oscillation searches, since they are typically given as ratios to the charged current (CC) single pion production cross section, which is also poorly known. T2K [1] uses a neutrino beam whose mean neutrino energy is approximately 0.8 GeV. The experiment requires less than a 10% uncertainty on NC $\pi^0$ production to maintain high sensitivity for the $\nu_\mu \rightarrow \nu_e$ oscillation search. Recently, two experiments published NC $\pi^0$ production results. The K2K collaboration reported NC $\pi^0$ production in water with a 1.3 GeV mean neutrino energy beam [8], finding their measurement consistent with the Monte Carlo (MC) prediction based on the Rein and Sehgal model [9]. MiniBooNE reported the yield and spectral shape of $\pi^0$s as a function of $\pi^0$'s momentum and the observation of NC coherent $\pi^0$ production in mineral oil (C$_8$H$_8$) in neutrino beam of mean neutrino energy 0.7 GeV [10]. The total NC $\pi^0$ cross section below 1 GeV has still not been precisely measured yet.

Pions are produced mainly through two distinct mechanisms by neutrinos with energies around 1 GeV. In the dominant mode, resonant pion production, the neutrino interacts with a nucleon in the nucleus and excites it to a baryonic resonance, such as $\Delta$ (1232), which subsequently decays to a pion and a nucleon. The other mode, coherent pion production occurs when the neutrino interacts with the target nucleus so that no nuclear breakup occurs. Resonance production and decay in a nuclear target differs from the case of the free nucleon target. This is due to nuclear effects such as Fermi motion, Pauli blocking, and the nuclear potential. In addition, produced mesons and baryons interact with nuclear matter until they escape from the target nucleus. Because of this final state interaction, the number, momenta, directions and charge states of produced particles can be changed in nuclear matter. Although there are several theoretical models of these processes, their uncertainties are still large. To understand the production mechanism and the nuclear effects, measurements of emitted $\pi^0$ kinematics are very important.

Recent measurements of coherent pion production have drawn much attention. For CC coherent pion production, the K2K experiment placed a limit on the ratio of the CC coherent pion production to the total CC cross sections at 1.3 GeV [11]. This result was confirmed by the SciBooNE experiment [12], although recent data from the SciBooNE Collaboration suggest CC coherent pion production at a level below the published limit in both neutrinos and antineutrinos [13,14]. Moreover, evidence for NC coherent pion production with neutrino energy less than 2 GeV has been reported by the MiniBooNE Collaboration [10]. Hence, it is interesting to search for NC coherent $\pi^0$ production in the SciBooNE data.

In this paper, we present measurements of the NC $\pi^0$ interaction in polystyrene (C$_8$H$_8$) using the same neutrino beam as MiniBooNE (with mean neutrino energy 0.7 GeV). We measure the ratio of the total inclusive NC $\pi^0$ cross section to the total CC cross section and kinematic distributions of the emitted $\pi^0$s. We also extract the fraction of coherent NC $\pi^0$ events from the inclusive NC $\pi^0$ data sample. In these analyses, we define NC $\pi^0$ events to be NC neutrino interactions with at least one $\pi^0$ emitted in the final state from the target nucleus.

II. EXPERIMENT DESCRIPTION

A. Neutrino beam

The SciBooNE experiment detected neutrinos produced by the Fermilab Booster Neutrino Beam (BNB). The same BNB beam is also serving the MiniBooNE experiment. The BNB uses protons accelerated to 8 GeV kinetic energy by the Fermilab Booster synchrotron. Beam properties are monitored on a spill-by-spill basis, and at various locations along the BNB line. Transverse and directional alignment of the beam, beam width and angular divergence, beam intensity and losses along the BNB, are measured and used to monitor data quality. Protons strike a 71.1 cm long beryllium target, producing a secondary beam of hadrons, mainly pions with a small fraction of kaons. A cylindrical horn electromagnet made of aluminum surrounds the beryllium target to sign-select and focus the secondary beam. The data set used in this measurement, the horn polarity was set to neutrino mode, focusing (defocusing) particles with positive (negative) electric charge. The neutrino beam is mostly produced in the 50 m long decay region, mainly from $\pi^+ \rightarrow \mu^+\nu_\mu$ in-flight decays. See [15] for further details.

B. Neutrino detector

The SciBooNE detector was located 100 m downstream from the beryllium target on the axis of the beam. The detector comprised three subdetectors: a fully active and finely segmented scintillator tracker (SciBar), an electromagnetic calorimeter (EC), and a muon range detector (MRD). SciBar served as the primary neutrino target for this analysis.

Figure 1 shows an event display of a typical NC $\pi^0$ production event candidate. SciBooNE uses a right-handed Cartesian coordinate system in which the z axis is the beam direction and the $y$ axis is the vertical upward direction. The origin is located on the most upstream surface of
SciBar in the z dimension, and at the center of the SciBar scintillator plane in the x and y dimensions. Since each subdetector is read out both vertically and horizontally, two views are defined: top (x vs z projection) and side (y vs z projection).

The SciBar detector [16] was positioned upstream of the other subdetectors. It consists of 14,336 extruded plastic scintillator strips which serve as the target for the neutrino beam as well as the active detection medium. Each strip has a dimension of $1.3 \times 2.5 \times 300 \text{ cm}^3$. The scintillators are arranged vertically and horizontally to construct a $3 \times 3 \times 1.7 \text{ m}^3$ volume with a total mass of 15 tons. SciBar has about four radiation lengths of material along the beam direction. Each strip was read out by a wavelength shifting fiber attached to a 64-channel multianode photomultiplier tube (PMT). Charge information was recorded for each channel, while timing information was recorded in groups of 32 channels by taking the logical or with multihit time-channel, while timing information was recorded in groups of 32 modules of dimensions $262 \times 8 \times 4 \text{ cm}^3$. The fibers are bundled in two independent groups of $4 \times 4 \text{ cm}^2$ transverse cross section, read at both ends by Hamamatsu PMTs. The EC comprises one vertical and one horizontal plane (32 modules each), covering an active area of $2.65 \times 2.65 \text{ m}^2$. The EC has a thickness of 11 radiation lengths along the beam direction. The charge information from each PMT was recorded. A minimum-ionizing particle with a minimal path length deposits approximately 91 MeV in the EC. The energy resolution for electrons was measured to be $14\% / \sqrt{E \text{ (GeV)}}$ using a test beam [18]. The detection efficiency for cosmic muons is 96%; the inefficiency stems from gaps between the modules.

The MRD was installed downstream of the EC and is designed to measure the momentum of muons produced by CC neutrino interactions. It had 12 iron plates with thickness 5 cm sandwiched between planes of 6 mm thick scintillation counters; there were 13 alternating horizontal and vertical planes read out via 362 individual 2 in. PMTs. Each iron plate measured $274 \times 305 \text{ cm}^2$. The MRD measured the momentum of muons up to 1.2 GeV/c using the observed muon range. Charge and timing information from each PMT were recorded. Hit finding efficiency was continuously monitored using cosmic-ray data taken between beam spills; the average hit finding efficiency is 99%.

C. Data summary

The SciBooNE experiment took data from June 2007 until August 2008. After applying data quality cuts to all beam events [12], $2.52 \times 10^{20}$ protons on target are usable for physics analysis, with $0.99 \times 10^{20}$ protons on target collected in neutrino mode. The analysis presented herein uses only neutrino mode data.

III. EXPERIMENT SIMULATIONS

A. Neutrino flux prediction

Predictions for the BNB neutrino flux illuminating the SciBooNE detector are obtained via a GEANT4 simulation of the beamline. The simulation accounts for all relevant
beamline geometry and materials, the measured BNB beam optics properties, and the horn magnetic field. Hadronic interactions are carefully modeled. Cross sections for elastic, quasielastic, and other inelastic interactions of charged pions and nucleons with beryllium and aluminum are simulated according to a custom model validated with external data, and covering the most relevant momentum range (down to 0.5 GeV/c for pions, 2 GeV/c for nucleons). Furthermore, the multiplicity and kinematics of all relevant particle types produced in the inelastic interactions of primary (8.4–8.9 GeV/c) protons with beryllium are also described by a custom model based on external data. For $\pi^+$ production, a parameterization based on HARP [19] and BNL E910 [20] data is used. Other hadronic and all electromagnetic processes of importance to neutrino production are described instead by standard GEANT4 models. The modeling of neutrino-producing weak decays incorporates accurate knowledge of meson decay branching fractions and form factors, and includes muon polarization effects. For a detailed description of the BNB simulation code, see [15]. According to the simulation, the neutrino flux at the SciBooNE detector is dominated by muon neutrinos ($93\%$), while the neutrino energy spectrum peaks at $\sim 0.6$ GeV, has a mean neutrino energy of $\sim 0.7$ GeV, and extends up to 2–3 GeV [12].

B. Neutrino interaction simulation

In the SciBooNE experiment, neutrino interactions with nuclear targets are simulated by the NEUT program library [21,22] that is used in the Kamiokande, Super-Kamiokande, K2K, and T2K experiments. The nuclear targets handled in NEUT are protons, carbon, oxygen, and iron. The energy of neutrons handled by the simulation ranges from 100 MeV to 100 TeV. The types of neutrino interactions simulated in both NC and CC are elastic and quasielastic scattering ($\nu N \rightarrow \ell N^\prime$), single meson production ($\nu N \rightarrow \ell N^\prime m$), single gamma production ($\nu N \rightarrow \ell N^\prime \gamma$), coherent $\pi^0$ production ($\nu^0\mu^+\mu^-\pi^0 \rightarrow \ell \pi^0\mu^+\mu^-\pi^0$), and deep inelastic scattering ($\nu N \rightarrow \ell N^\prime$ hadrons), where $N$ and $N^\prime$ are the nucleons (proton or neutron), $\ell$ is the lepton (electron, muon or neutrino), and $m$ is the meson. In nuclei, interactions of the mesons and hadrons with the nuclear medium are simulated following the neutrino interactions.

1. Single meson production via baryon resonances

The main signal in this analysis is NC single $\pi^0$ production via baryon resonances. The resonant single meson production is simulated based on the model of Rein and Sehgal [9]. The cross section of the NC single $\pi^0$ production per nucleon on a polystyrene target ($C_8H_8$) in NEUT is shown in Fig. 2. The per nucleon cross section of a polystyrene molecule is calculated by summing the contributions from the six protons and six neutrons bound in the carbon nucleus as well as the free proton, and dividing that by 13. Following production, the intranuclear interactions of the meson and nucleons are simulated using a cascade model in which the particles are traced until escaping from the nucleus. According to this model, approximately 40% of $\pi^0$s interact in the target nucleus, averaged over our neutrino flux. For scattering of nucleons in the nucleus by a neutrino, the relativistic Fermi gas model of Smith and Moniz [23] is implemented. The nucleons are treated as quasifree particles and the Fermi motion of nucleons along with the Pauli exclusion principle is taken into account. The Fermi surface momentum is set to 217 MeV/c and the nuclear potential is set to 27 MeV for carbon. The vector and axial-vector form factors are formalized to be dipole with $M_\nu^\pi = 0.84$ GeV/c$^2$ and $M_\nu^\pi = 1.21$ GeV/c$^2$. The same Fermi momentum distribution, nuclear potential and $Q^2$ dependence of form factors are used in all other neutrino-nucleus interactions except for coherent $\pi^0$ production.

The Rein and Sehgal model assumes an intermediate baryon resonance, $N^*$, in the reaction of $\nu N \rightarrow \ell N^*$. All intermediate baryon resonances with mass less than 2 GeV/c$^2$ are included. Baryon resonances with mass greater than 2 GeV/c$^2$ are simulated as deep inelastic scattering. Pion-less $\Delta$ decays—which produce no pion in the final state and account for 20% of $\Delta$ events [24]—are also simulated. To determine the angular distribution of final state pions, Rein’s method [25] is used for the $P_{33}(1232)$ resonance. For other resonances, the directional distribution of the generated pion is chosen to be isotropic in the resonance rest frame.

The inelastic scattering, charge exchange, and absorption of pions in nuclei are simulated. The interaction cross sections of pions in the nuclei are based on the model by Salcedo et al. [26]. For inelastic scattering and charge exchange interactions, the direction and momentum of pions are affected. In the scattering amplitude, Pauli blocking is also taken into account.

2. Coherent $\pi^0$ production

The $\pi^0$ signal events contain a contribution from NC coherent $\pi^0$ production. Because of the small momentum...
3. Quasielastic scattering and deep inelastic scattering

The dominant interaction in the SciBooNE neutrino energy is CC quasielastic scattering, which is implemented using the Smith and Moniz model [23]. $M_V^{QE}$ and $M_A^{QE}$ are set to be 0.84 GeV/c^2 and 1.21 GeV/c^2, respectively.

The deep inelastic scattering (DIS) cross section is calculated using the GRV98 parton distribution functions [29]. As well as quasielastic scattering and deep inelastic scattering, other neutrino interactions in NEUT are described in [12] in detail.

With the SciBooNE neutrino beam exposure of 0.99 × 10^{20} protons on target, the expected number of events in the SciBooNE detector in each neutrino interaction is listed in Table I. For the purpose of systematic studies of neutrino interaction simulations, we also use the NUANCE event generator [30] that is used in the MiniBooNE experiment. The types and models of neutrino interactions in NUANCE are similar to those of NEUT but with different treatment of interactions of mesons and hadrons with the nuclear medium.

C. Neutrino detector simulation

The GEANT4 framework is used for the detector simulation. The Bertini cascade model within GEANT4 [31] is used to simulate the interactions of hadronic particles with detector materials. The detector simulation includes a detailed geometric model of the detector, including the detector frame and experimental hall and soil, based on survey measurements taken during detector construction. A description of the detector simulation is given in [12].

In addition to neutrino interactions inside the detector, we also simulate interactions in the surrounding material (the walls of the detector hall and soil). The density of material is assumed to be 2.15 g/cm^3 for the calculation of the interaction rate, and concrete of that density is used as the material for propagation of product particles. We generate events in a volume of ±5 m in x, y, and z direction in the SciBooNE coordinates.

IV. DATA ANALYSIS

The present analysis has two main goals. The first is to measure the ratio of NCπ^0 production cross section to the total CC cross section. We measure the ratio of cross sections in order to minimize systematic uncertainty due to the neutrino flux prediction. The second goal is to measure the π^0 momentum and angular spectra. In addition to the two main goals, we also extract the coherent π^0 fraction in the context of the Rein and Sehgal model.

We reconstruct gamma rays converting in SciBar and select events with two reconstructed gamma rays and no muons, which is the characteristic topology of NCπ^0 events. We do not include NCπ^0 events in which one or both gamma rays convert in the EC.

A. Signal definition

We define an NCπ^0 interaction as an NC neutrino interaction in which at least one π^0 is emitted in the final state from the target nucleus, $\nu_\mu C \rightarrow \nu_\mu \pi^0 X$ where X represents the nuclear remnant and any combination of

<table>
<thead>
<tr>
<th>Interaction Type</th>
<th># Events</th>
<th>Fraction(%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>CC quasielastic</td>
<td>53,363</td>
<td>41.4</td>
</tr>
<tr>
<td>CC single $\pi^0$ via resonances</td>
<td>29,688</td>
<td>23.1</td>
</tr>
<tr>
<td>CC coherent $\pi^0$</td>
<td>1,771</td>
<td>1.4</td>
</tr>
<tr>
<td>CC single meson except $\pi^0$</td>
<td>839</td>
<td>0.7</td>
</tr>
<tr>
<td>CC DIS</td>
<td>6,074</td>
<td>4.7</td>
</tr>
<tr>
<td>NC elastic</td>
<td>22,521</td>
<td>17.5</td>
</tr>
<tr>
<td>NC single $\pi^0$ via resonances</td>
<td>6,939</td>
<td>5.4</td>
</tr>
<tr>
<td>NC coherent $\pi^0$</td>
<td>1,109</td>
<td>0.9</td>
</tr>
<tr>
<td>NC single meson except $\pi^0$</td>
<td>4,716</td>
<td>3.7</td>
</tr>
<tr>
<td>NC DIS</td>
<td>1,768</td>
<td>1.4</td>
</tr>
</tbody>
</table>

TABLE I. The expected number and fraction of events in each neutrino interaction estimated by NEUT at the SciBooNE detector location with the neutrino beam exposure of 0.99 × 10^{20} protons on target. The 10.6 ton fiducial volume of the SciBar detector is assumed. CC and NC interactions are abbreviated as CC and NC, respectively.
nucleons and mesons. According to our MC simulation, 96% of NCπ0 events without any selection cuts have a single π0 (85% from a single π0 without any other mesons and 11% from a single π0 with charged mesons) and 4% have two π0’s. Any π0 emitted from the initial target nucleus constitutes a signal event whether it is created from the neutrino vertex or final state interactions. Events with a π0 produced in the neutrino interaction but absorbed in the target nucleus are not included in the signal sample, nor are events in which π0’s are produced by secondary particles interacting with the detector scintillator outside the target nucleus.

B. Gamma ray reconstruction

1. Gamma conversion probability

Since the length of SciBar in the beam direction corresponds to four radiation lengths, a significant fraction of gamma rays escape from SciBar without conversion. In 30% of events with a π0 emitted within SciBar’s fiducial volume, both gamma rays convert in SciBar; in 38%, only one gamma ray converts in SciBar; in 32%, neither gamma ray converts in SciBar. Since we aim to reconstruct two gamma rays to identify NCπ0 events, the maximum detection efficiency attainable is 30%.

2. Track reconstruction

The first step of the event reconstruction is to search for two-dimensional tracks in each view of SciBar using a cellular automaton algorithm [32]. For tracking, the hit threshold is set to 2.5 photo-electrons, corresponding to roughly 0.25 MeV. Three-dimensional tracks are reconstructed by matching the timing and z edges of the two-dimensional projections. In order to match track projections in a three-dimensional track, the timing difference between two two-dimensional projections is required to be less than 50 ns, and the z-edge difference must be less than 6.6 cm for upstream and downstream edges. This method is used for all charged particles and is the first step of gamma ray reconstruction.

3. Particle identification parameter

The SciBar detector has the capability to distinguish protons from other particles using dE/dx since recoil protons at SciBooNE energies interact well above minimum-ionizing energy deposit. We define a muon confidence level (MuCL) using the observed energy deposit per layer for all reconstructed tracks [12]. The MuCL of the proton tracks tends to be close to 0 while the MuCL of other tracks tends to be close to 1. Proton-like tracks are defined to have MuCL less than 0.03.

4. Extended track

Single reconstructed tracks are extended in two ways to improve the energy reconstruction of gamma rays within SciBar. The first step is merging two or more tracks if they are nearly colinear, because electromagnetic showers can form separate hit clusters in SciBar resulting in two or more tracks. The second step is collecting lone hits around merged tracks. Electromagnetic showers sometimes deposit energy around the main track and these hits are missed by the track reconstruction algorithm. Hits not assigned to any track within 20 cm from two-dimensional projections of the merged track (i.e., after the first step) for each view are added to the extended track. The methods described above are applied only to non-proton-like tracks. For the energy reconstruction, we use charge information of hits associated with original tracks as well as newly assigned hits. For reconstructing the directions of gamma rays, we fit positions of hits in all original tracks in the extended track with a straight line and do not use hits newly collected in the second step.

5. SciBar-EC matching

Gamma rays can escape SciBar to deposit energy in the EC. After event reconstruction in SciBar, we search for EC clusters aligned with tracks from SciBar. One EC cluster is defined as a collection of neighboring EC hits. For an EC hit, the pulse heights of both side PMTs are required to be above threshold, which is set to 3 times the width of each pedestal—about 7 MeV. The energy of an EC hit is the geometric average of the two PMTs. The center of an EC cluster is defined as the energy-weighted average of hits in the cluster. To match an EC cluster to an SciBar track, the EC cluster is required to be within 10 cm of the extrapolated two-dimensional projections of the SciBar track in each EC plane. The energy of matched EC clusters is added to the corresponding extended tracks.

6. Gamma ray reconstruction performance

We study the performance of the gamma ray reconstruction algorithms using the MC simulation. The angular resolution of gamma rays passing all selection cuts (see Sec. IV D) is estimated to be approximately 6°. For the energy reconstruction, energy of matched EC clusters is added to corresponding extended tracks. About 7% of selected extended tracks are made by two or more tracks. The average gamma ray energy deposit of SciBar is estimated to be 116 MeV and the energy resolution is estimated to be 6%. About 17% of selected extended tracks have matched EC clusters. The average gamma ray energy deposit in such matched EC clusters is estimated to be 72 MeV and the energy resolution is estimated to be 32%.

Not all gamma ray energy is deposited in, nor recorded by, the detector. Such lost energy is called leakage. The actual leakage, defined as

\[ L_{\text{act}} = 1 - \frac{\text{gamma energy in extended track}}{\text{true gamma energy}} \]  

is estimated to be 24%; 11% comes from energy loss in
passive regions and gamma rays escaping from the detectors and 13% comes from energy deposit in active regions but not assigned to the extended track. The reconstructed energy can include energy deposited by other particles. On average, 15% of the total energy in an extended track comes from other particles. Because of this contamination, the effective leakage, defined as

\[ L_{\text{eff}} = 1 - \frac{\text{reconstructed energy of extended track}}{\text{true gamma energy}} \]  

(2)

is 15%, which is smaller than \( L_{\text{act}} \) averaged over all NC\( \pi^0 \) events.

**C. CC event selection**

To identify CC events, we search for events in which at least one reconstructed track in SciBar, when projected out of SciBar, is matched with a track or hits in the MRD. We reject events with hits associated with the muon track on the most upstream layer of SciBar to eliminate neutrino-induced incoming particles from the upstream wall or soil. The neutrino interaction vertex for CC events is reconstructed as the upstream edge of the muon track. We select events whose vertices are in the SciBar fiducial volume, defined to be \( \pm 130 \) cm in both the x and y dimensions, and \( 2.62 \) cm \( < z < 157.2 \) cm, a fiducial mass of 10.6 tons. The time of the muon track is required to be within a 2 \( \mu s \) window around the beam pulse. Finally, we require the muon track to stop in the MRD. The MRD-stopped event sample [12] serves as the normalization sample in the cross-section ratio measurement. Unless otherwise indicated, the MC distributions in this paper are normalized using the MRD-stopped data sample.

**D. NC\( \pi^0 \) event selection**

The clearest feature of NC\( \pi^0 \) production is two gamma rays, coming from the decay of the \( \pi^0 \), converted into two \( e^+ e^- \) pairs. Background events stem from sources both internal and external to SciBar. Internal backgrounds are neutrino interactions other than NC\( \pi^0 \) (mainly CC) within SciBar; external backgrounds come from neutrino interactions in the material outside of the detector volume (support structure, walls and soil—so-called dirt events) as well as from cosmic rays. In dirt events, neutrinos interact with materials such as the walls of the experimental hall or soil and produce secondary particles which deposit energy within SciBar’s fiducial volume and cause recorded hits. The contribution of accidental cosmic rays in any event sample is small and accurately estimated by data taken with off-beam timing; the fraction of accidental cosmic-ray events is 1.8% after all event selection cuts. Data distributions shown hereafter have been cosmic-ray subtracted from them. The event selection cuts for NC\( \pi^0 \) production are developed to select events with two gamma rays while rejecting these backgrounds.

**1. Preselection cuts**

We select events with at least two three-dimensional tracks. The timing of tracks are required to be within 50 ns of each other and the closest endpoints of any two tracks are required to be in the fiducial volume defined in Sec. IV D. The closest endpoints are chosen as the edge combination for two given tracks that gives the minimum distance among the four possible combinations. The times of the two tracks are required to be within the 2 \( \mu s \) beam window. In addition, we reject events with hits in the first layer of SciBar within 100 ns from the times of tracks, to remove dirt background events.

**2. Muon track rejection cuts**

Events with muons are predominantly CC events. To avoid muons which escape SciBar but do not penetrate the MRD, we reject events with tracks escaping from the side of SciBar; both edges of tracks must be in \( \pm 130 \) cm in both the x and y dimensions.

To reject muons stopping in SciBar, we tag the electrons from muon decay. No charge information is recorded for any scintillator strip after its first hit in an event, but the times of hits above threshold continue to be recorded. Thus most decay electrons are not reconstructed as tracks but can be identified as delayed time hits near the end of a muon track. We examine the maximum timing difference (\( \Delta t_{\text{max}} \)) between the track times and late hits times at the

![FIG. 4 (color online). \( \Delta t_{\text{max}} \) distribution (IV D 2) after rejection of side escaping tracks. The contributions from events with decay electrons, events without decay electrons and the dirt events are shown separately for the MC simulation.](033004-7)
ends of tracks. Events with decay electrons yield high values of $\Delta t_{\text{max}}$ because of the long muon lifetime ($\tau_{\mu} = 2.2 \mu \text{sec}$). Figure 4 shows the $\Delta t_{\text{max}}$ distribution. We select events with $\Delta t_{\text{max}}$ less than 100 ns.

3. Track disconnection cut

CC events often have two or more tracks with a common vertex while two gamma rays from $\pi^0$s are typically isolated from each other. Hence, the distance between two tracks is used to separate two gamma rays from CC events. If there are two particles with a common vertex, the minimum distance is close to zero. Figure 5 shows the distribution of the minimum distance. Events with a minimum distance greater than 6 cm are selected.

4. Electron catcher cut

Matched EC Clusters are used to reject muons penetrating the EC. Two quantities are used: the energy deposit in matched EC clusters in the upstream layer, $E_1$ ($E_2$ is energy in the downstream layer), and the ratio of energy deposits in the downstream EC cluster over the upstream EC cluster, $R_{\text{EC}} = E_2/E_1$. Figures 6–8 shows the distributions of the number of tracks with matched EC clusters, $E_1$ and $R_{\text{EC}}$, respectively. Events satisfying one of the three following condition are selected, (i) No matched EC clusters or (ii) $E_1 > 150$ MeV or (iii) $R_{\text{EC}} < 0.2$. For events without matched EC clusters, both $E_1$ and $R_{\text{EC}}$ are left undefined (not included in Fig. 7 and 8). For events with only up-
stream matched EC clusters, the minimum $E_1$ is chosen and $R_{EC}$ is set to 0. For events with both upstream and downstream matched EC clusters, the maximum $R_{EC}$ is chosen and the corresponding $E_1$ is chosen.

5. Number of photon tracks

We use the extended track information instead of the track information hereafter. As described in Sec. IV B 4, we only use non-proton-like tracks to obtain extended tracks. Figure 9 shows the MuCL distribution after the EC cut. The dashed line ($\text{MuCL} = 0.03$) separates into particles to protonlike or non-proton-like tracks. The gamma ray efficiency for the non-proton-like sample is 87% and the contamination of gamma rays in the non-proton-like sample is 81%.

Figure 10 shows the distribution of the number of extended tracks after the EC cut. To reconstruct $\pi^0$s, events with more than one extended track are selected. As shown in Fig. 10, 58% of the NC$\pi^0$ events have only one extended track and are rejected by this cut. However, 39% are events with one reconstructed gamma ray, due to misreconstruction or gamma rays not converting in SciBar. Such events can not be used for $\pi^0$ reconstruction; 12% are events where the two gamma rays are reconstructed as two tracks but then merged, resulting in one extended track.

This cut is also effective at rejecting dirt backgrounds since many dirt background events have only one extended track, as shown in Fig. 10.

6. Reconstructed $\pi^0$ vertex position cut

The reconstructed vertex position of a $\pi^0$ is calculated as the intersection of two two-dimensional extended tracks.
First, we calculate the intersection point for all combinations of extended tracks in each view—two \( z \) positions (\( z_{\text{top}} \) and \( z_{\text{side}} \)) for each combination. We choose the combination giving the minimum \( \frac{z_{\text{top}}}{C_{0}} \frac{1}{\cos \theta_{\text{rec}}} \) as the candidate. The reconstructed \( z \) vertices are obtained by taking the error weighted average of \( z_{\text{top}} \) and \( z_{\text{side}} \):

\[
z = \frac{z_{\text{top}}}{\delta z_{\text{top}}} + \frac{z_{\text{side}}}{\delta z_{\text{side}}}
\]

where \( \delta z_{\text{top(side)}} \) is the error on \( z_{\text{top(side)}} \) returned by the track reconstruction algorithm. Figure 11 shows the reconstructed \( z \)-vertices of \( \pi^0 \)s. The vertex resolution is approximately 12 cm for all three dimensions. Most events with a \( \pi^0 \) produced in SciBar yield a vertex within SciBar—but many dirt events yield a vertex position upstream of SciBar—so we select events with reconstructed \( \pi^0 \) \( z \) vertex greater than 0 cm.

### 7. Reconstructed \( \pi^0 \) mass

Figure 12 shows the reconstructed mass of the \( \pi^0 \) calculated as \( \sqrt{2E_{\gamma 1}E_{\gamma 2}(1 - \cos \theta_{\text{rec}})} \), where \( E_{\gamma 1} \) and \( E_{\gamma 2} \) are the reconstructed energies of the extended tracks (\( E_{\gamma 1} > E_{\gamma 2} \)) and \( \theta_{\text{rec}} \) is the reconstructed angle between the extended tracks. The MC simulation describes well the tail of the distribution, which is background-dominated. We select events with 50 MeV/c\(^2 \) < \( M_{\pi^0} \) < 200 MeV/c\(^2 \). The peak value is smaller than the actual \( \pi^0 \) mass (135 MeV) due to energy leakage of \( \gamma \)s.

### 8. Event selection summary

Table II shows the number of events in data and the MC at each event selection stage. The numbers for the MC simulation are normalized to the number of MRD-stopped events. We select 657 events after all cuts. Subtracting the estimated background of 240 events (202 internal and 38 external) yields 417 signal events. The MC expectation is 368 events. The purity of NC\( \pi^0 \) production after all event selection cuts is estimated to be 61\% (40\% from single \( \pi \) production via resonance decay, 15\% from coherent \( \pi \) production and 5\% from neutrino deep inelastic scattering). According to our MC simulation, 96\% of selected NC\( \pi^0 \) events have one \( \pi^0 \) (91\% from a single \( \pi^0 \) without any other mesons and 5\% from a single \( \pi^0 \) with charged mesons) and 4\% have two \( \pi^0 \)s. The efficiency for NC\( \pi^0 \) production, defined as

\[
\epsilon_{\text{NC}\pi^0} = \frac{\text{the number of selected NC}\pi^0 \text{ events}}{\text{the number of generated NC}\pi^0 \text{ events}}
\]

is estimated to be 5.3\%. The internal background, which accounts for 33\% of this sample, contains CC\( \pi^0 \) production including secondary \( \pi^0 \)s (18\%), NC secondary \( \pi^0 \) production in detector materials (9\%) and non-\( \pi^0 \) background (6\%). According to our MC simulation, the average energy of neutrinos producing NC\( \pi^0 \) events in the SciBar fiducial volume is 1.3 GeV and the average energy of neutrinos producing NC\( \pi^0 \) events that pass all selection cuts is 1.1 GeV. The average energy of neutrinos producing NC\( \pi^0 \)s coherently is 1.1 GeV, while the average energy that pass the selection cuts is 1.0 GeV.
V. RESULTS

A. $\sigma(\text{NC}\pi^0)/\sigma(\text{CC})$ cross-section ratio

We measure the ratio of the NC\pi^0 production to the total CC interaction cross sections.

1. NC\pi^0 production

The efficiency corrected number of NC\pi^0 events is calculated as

$$N(\text{NC}\pi^0) = \frac{N_{\text{obs}} - N_{\text{BG}}}{\epsilon_{\text{NC}\pi^0}}, \quad (5)$$

where $N_{\text{obs}}$ is the number of observed events, $N_{\text{BG}}$ is the number of background events estimated by the MC simulation, and $\epsilon_{\text{NC}\pi^0}$ is the selection efficiency of NC\pi^0 events calculated by the MC simulation. $N_{\text{obs}}$ and $N_{\text{BG}}$, $\epsilon_{\text{NC}\pi^0}$ are 657, 240.0, and 0.053, respectively. After subtracting background and correcting for the selection efficiency, the number of NC\pi^0 candidates is measured to be $[7.8 \pm 0.5(\text{stat})] \times 10^2$. For the background calculation, we use the MC expectation normalized to the number of MRD-stopped events. The neutrino energy dependence of the selection efficiency for NC\pi^0 events is shown in Fig. 13. The mean neutrino energy for NC\pi^0 events in the sample is estimated to be 1.1 GeV after event selection cuts.

2. Total CC interactions

The total number of CC interactions is estimated using the MRD-stopped sample. The mean neutrino energy of MRD-stopped events is estimated to be 1.2 GeV. The number of CC candidates after correcting for the selection efficiency is calculated as

$$N(\text{CC}) = \frac{N_{\text{obs}}^{\text{CC}} - N_{\text{BG}}^{\text{CC}}}{\epsilon_{\text{CC}}}, \quad (6)$$

where $N_{\text{obs}}^{\text{CC}}$ is the number of observed CC events, $N_{\text{BG}}^{\text{CC}}$ and $\epsilon_{\text{CC}}$ are the number of background events and selection efficiency in the sample, respectively, estimated with the MC simulation. We observed 21702 MRD-stopped events

FIG. 13 (color online). Expected neutrino energy spectra and selection efficiency as a function of neutrino energy for NC\pi^0 events.
The number of background events and the selection efficiency are estimated to be $2348 (N_{BG}^{CC})$ and $19\% (\varepsilon_{CC})$, respectively. The neutrino energy dependence of the selection efficiency for CC events is shown in Fig. 14. After subtracting the background events and correcting for the efficiency, the number of CC events is measured to be $2.02^{+0.5}_{-0.5} \times 10^5$.

**3. Cross-section ratio**

The ratio of the NC$\pi^0$ production to the total CC cross section is measured to be

$$
\frac{\sigma(NC\pi^0)}{\sigma(CC)} = \frac{N(NC\pi^0)}{N(CC)} = (7.7 \pm 0.5(stat) \pm 0.5(sys) \times 10^{-2} \quad (7)
$$

at the mean neutrino energy of 1.14 GeV; systematic uncertainties are described in Sec. VA.4. The MC expectation based on the Rein and Sehgal model is $6.8 \times 10^{-2}$. The total uncertainty, $\pm 0.7 \times 10^{-2}$ is obtained adding statistical and systematic uncertainties in quadrature. Although the value of this measurement is larger than the expectation by 11%, the excess corresponds to 1.3 standard deviations if the total uncertainty is taken into account.

**4. Systematic errors**

The sources of systematic error are divided into four categories, (i) detector response and track reconstruction, (ii) nuclear effects and neutrino interaction models, (iii) neutrino beam, and (iv) dirt background. We vary these sources within their uncertainties and take the resulting change in the cross-section ratio as the systematic uncertainty of the measurement. Table III summarizes the systematic errors in the NC$\pi^0$ cross-section ratio. The total systematic error is $\pm 0.5 \times 10^{-2}$ on the cross-section ratio.

Detector response and track reconstruction.—The cross-talk of the multi-anode photomultiplier (MA-PMT) was measured to be $3.15^{+0.4}_{-0.4}\%$ for adjacent channels and is varied within the measurement error. The single photoelectron resolution of the MA-PMT is set to 50% in the simulation, to reproduce the observed $dE/dx$ distribution of cosmic muons. The absolute error is estimated to be $\pm 20\%$. Hence, we vary the single photoelectron resolution by $\pm 20\%$. Birk’s constant for the SciBar scintillator was measured to be $0.0208 \pm 0.0023$ cm/MeV [33] and is varied within the measurement error. The hit threshold for track reconstruction is varied by $\pm 20\%$. A 10% difference of the total pion-carbon cross section is seen for higher energy pions between the GEANT4 simulation and external measurements. Hence, we vary the cross section by $\pm 10\%$. The uncertainty of the energy scale of gamma rays is estimated to be $\pm 3\%$. We vary the reconstructed energy of extended tracks by $\pm 3\%$. For the uncertainty on reconstruction of the gamma direction, we study how the difference between data and MC distributions changes when we change the gamma direction reconstruction algo-

**TABLE III. Summary of the systematic errors in the NC$\pi^0$ cross-section ratio.**

<table>
<thead>
<tr>
<th>Source</th>
<th>Error ($\times 10^{-2}$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Detector response</td>
<td>$-0.39$</td>
</tr>
<tr>
<td>$\nu$ interaction</td>
<td>$-0.25$</td>
</tr>
<tr>
<td>Dirt background</td>
<td>$-0.10$</td>
</tr>
<tr>
<td>$\nu$ beam</td>
<td>$-0.11$</td>
</tr>
<tr>
<td>Total</td>
<td>$-0.48$</td>
</tr>
</tbody>
</table>

FIG. 14 (color online). Expected neutrino energy spectra and selection efficiency as a function of neutrino energy for all CC events.
algorithm. We compare our standard algorithm with gamma direction reconstruction obtained using extended tracks - resulting in poorer angular resolution. We take this change as the uncertainty. The largest contribution to the uncertainty in the cross-section ratio are the crosstalk of the MA-PMT (−0.00, +0.27) and the hit threshold (−0.25, +0.05).

Neutrino interaction models and nuclear effects.—The uncertainty in CC resonant pion production is estimated to be approximately ±20% based on the K2K measurement [34]. We vary the cross section of CC resonant pion production by ±20% and take that change as the systematic error. We also vary the NC/CC ratio by ±20% and take that change as a systematic error. The uncertainty in the axial-vector mass for CC quasielastic and NC elastic scattering as well as CC(NC) resonant pion production is estimated to be approximately ±0.1 GeV/c² based on recent measurements [35,36]; results from past experiments are systematically lower than recent measurements [37], and thus we only vary $M_A$ down to 1.11 GeV/c², and take that change as the systematic error. The biggest contribution to the uncertainty of the cross-section ratio is the CC resonant pion production (−0.14, +0.16).

We consider uncertainties in the pion interactions inside the nucleus. For pions produced by neutrino interactions, uncertainties on the cross sections for pion absorption, pion inelastic scattering and pion charge exchange in the nucleus are approximately 30% [38] in the momentum range of pions from Δ decays; we vary these pion interaction cross sections and take the resultant change in the ratio as the uncertainty. The largest contribution to the uncertainty of the cross-section ratio is the pion absorption (−0.17, +0.19).

As a cross check, we measure the cross-section ratio using the NUANCE event generator [30] to predict event rates and calculate efficiencies, and obtain a measured ratio of $7.9 \times 10^{-2}$ (the NUANCE expectation is $7.1 \times 10^{-2}$). The result using NUANCE agrees with the NEUT result ($7.7 \times 10^{-2}$) within the systematic uncertainty, so we do not add the NEUT/NUANCE difference to the systematic uncertainty.

Dirt Backgrounds.—As shown in Fig. 11, the dirt background simulation describes data at $z < -20$ cm where the dirt background is the dominant contamination. However, the statistical uncertainty is large, 15%. We scale the dirt contamination by ±15% in the final sample and take the change as the systematic error due to dirt backgrounds.

Neutrino beam.—The uncertainties in secondary particle production cross sections in proton-beryllium interactions, hadronic interactions in the target or horn, and the horn magnetic field model are varied within their externally estimated error bands. Detailed descriptions of each uncertainty are found elsewhere [15]. Systematic uncertainties in the neutrino flux are reduced by removing the model dependent parameterization in the propagation of errors from the HARP data [15]. Uncertainties associated with the delivery of the primary proton beam to the beryllium target and the primary beam optics, which result in an overall normalization uncertainty, are not considered in this analysis since they cancel in the cross-section ratio.

B. Reconstructed $\pi^0$ kinematics

After all event selection cuts, we studied the reconstructed kinematics of the $\pi^0$s: the $\pi^0$ momentum and
cosine of the $\pi^0$ angle with respect to the beam direction, as shown in Figs. 15 and 16. The NC$\pi^0$ efficiency as functions of $\pi^0$ momentum and angle are shown in Figs. 17 and 18, respectively. The average momentum of reconstructed $\pi^0$s is estimated to be 223 MeV/c while the average momentum of true $\pi^0$s after all event selection cuts is 264 MeV/c according to our MC simulation. This difference comes from energy leakage of gamma rays. The relation between the true and reconstructed $\pi^0$ momentum is shown in Fig. 19. The momentum resolution is estimated to be 23%. The relation between the true and reconstructed $\pi^0$ direction is shown in Fig. 20. The angular resolution of $\pi^0$s is estimated to be 6°. In events with two $\pi^0$s, we choose the $\pi^0$ with the largest momentum when comparing the true and reconstructed kinematic quantities.

In the reconstructed $\pi^0$ momentum and angular distributions, we extract NC$\pi^0$ signal events by subtracting the expected backgrounds; to estimate backgrounds, we use the MC expectation normalized to the number of MRD-stopped events. After the background subtraction, we convert the reconstructed $\pi^0$ momentum (direction) distribution to the true momentum (direction) distribution using a

FIG. 17 (color online). The true $\pi^0$ momentum of generated MC events (solid) and selected MC events (dashed) for all NC$\pi^0$ production processes (top), and the true $\pi^0$ momentum dependence of the efficiency of NC$\pi^0$ production (bottom).

FIG. 18 (color online). The true $\pi^0$ angle with respect to the beam direction for generated MC events (solid) and selected MC events (dashed) for NC$\pi^0$ production (top), and the efficiency for NC$\pi^0$ production as a function of the true $\pi^0$ direction (bottom).
Bayesian unfolding method \[39\] using the MC simulation to define the unfolding matrix. Figure 19 (Fig. 20) shows the true versus reconstructed \(\pi^0\) momentum (angle) distribution; these figures are graphical representations of the smearing matrices used for the unfolding. Finally, we perform the efficiency correction to obtain the true \(\pi^0\) momentum (direction) distribution. Figures 21 and 22 show the \(\pi^0\) momentum and direction distributions, respectively, after background subtractions, conversions to

FIG. 19. The true \(\pi^0\) momentum \((P_{\text{true}})\) versus reconstructed \(\pi^0\) momentum \((P_{\text{rec}})\) from the MC simulation. The solid line shows the identity.

FIG. 20. The true \(\pi^0\) direction \((\cos \theta_{\text{true}})\) versus reconstructed \(\pi^0\) direction \((\cos \theta_{\text{rec}})\) from the MC simulation. The solid line shows the identity.

FIG. 21 (color online). The \(\pi^0\) momentum distribution after all corrections described in the text, with statistical (error bars) and systematic (red boxes) uncertainties. The dashed line shows the Monte Carlo expectation based on the Rein and Sehgal model.

FIG. 22 (color online). The \(\pi^0\) angular distribution after all corrections described in the text, with statistical (error bars) and systematic (red boxes) uncertainties. The dashed line shows the Monte Carlo expectation based on the Rein and Sehgal model.
the true $\pi^0$ kinematics and efficiency corrections. To compare the shapes of the distributions, the total numbers of entries in the distributions are normalized to unity both for the measurement and the MC expectation. The shapes of these two distributions agree with the MC expectation. The systematic errors of Fig. 21 and 22 are expected to arise from the same sources, and are estimated in the same manner, as described in Sec. VA 4.

### C. Coherent pion production

In the coherent pion production, the neutrino interacts the entire nucleus. In this case, the following relation should be satisfied:

$$|t| < \frac{1}{R},$$

(8)

where $t$ and $R$ are the momentum transfer to the nucleus and the nuclear radius, respectively. Using Eq. (8), we can deduce

$$E_{\pi^0}(1 - \cos\theta_{\pi^0}) < \frac{1}{R} \sim 100 \text{ MeV}$$

(9)

according to Ref. [40]. In this equation, the $E_{\pi^0}$ and $\theta_{\pi^0}$ are the $\pi^0$ energy and direction with respect to the neutrino beam, respectively. Hence, the fraction of coherent $\pi^0$ production is extracted from the $E_{\pi^0}^{\text{rec}}(1 - \cos\theta_{\pi^0})$ distribution shown in Fig. 23, where $E_{\pi^0}^{\text{rec}}$ is the reconstructed $\pi^0$ energy calculated as $E_{\pi^0}^{\text{rec}} = E_{\pi^0}^{\text{rec}} + E_{\pi^0}^{\text{rec}}$. We fit this distribution using three templates made by dividing the final MC sample into NC coherent $\pi^0$, NC resonant $\pi^0$ and background samples. Two parameters, $R_{\text{coh}}$, $R_{\text{res}}$, scale NC coherent $\pi^0$ and NC resonant $\pi^0$ templates independently. The scale of the background sample is fixed to unity. The expected number of events in the $i$-th ($i = 1, 2, \ldots, N(=20)$) bin in the $E_{\pi^0}^{\text{rec}}(1 - \cos\theta_{\pi^0})$ distribution is expressed as

$$N_{i}^{\exp} = R_{\text{coh}} \times N_{i}^{\text{coh}} + R_{\text{res}} \times N_{i}^{\text{res}} + N_{i}^{\text{BG}}.$$  

(10)

The fit minimizes the following $\chi^2$:

$$\chi^2 = -2 \ln \frac{f(N^{\text{obs}}; N^{\text{exp}})}{f(N^{\text{obs}}; N^{\text{exp}})},$$

(11)

where $N^{\text{obs}}(\exp)$ represents the observed (expected) number of events in all bins ($N^{\text{obs}}(\exp), N^{\text{obs}}(\exp), \ldots, N^{\text{obs}}(\exp)$) and $f(N^{\text{obs}}; N^{\text{exp}})$ is the Poisson likelihood to find $N^{\text{obs}}$ events when $N^{\text{exp}}$ events are expected. When the systematic errors for each bin and their correlation expressed using the covariance matrix $V_{jk}$ ($j, k = 1, 2, \ldots, N(=20)$) are given, the likelihood is expressed as

$$f(N^{\text{obs}}; N^{\text{exp}}; V) = A \int \left[ \prod_{i=1}^{N} dx_i \frac{x_i^{\text{obs}}}{N_{i}^{\text{obs}}} e^{-x_i} \right] \times \exp \left[ -\frac{1}{2} \sum_{j=1}^{N} \sum_{k=1}^{N} (x_j - N_j^{\exp}) V_{jk}^{-1} (x_k - N_k^{\exp}) \right].$$

(12)

where $A$ is the normalizing constant. To calculate this integral, we generate 1000 MC expectations with random variations drawn from Gaussian distributions about the expectations for each bin, with correlations, estimated from the MC simulation. Using $x_{i,m}$ for the $m$-th expectation in the $i$-th bin, the likelihood is expressed as

$$f(N^{\text{obs}}; N^{\text{exp}}; V) = \frac{1}{M} \sum_{m=1}^{M} \prod_{i=1}^{N} \frac{x_{i,m}^{\text{obs}}}{N_{i}^{\text{obs}}} e^{-x_{i,m}},$$

(13)

where $M$ is the total number of random samples (1000). The result of the fit is

$$R_{\text{coh}} = 0.56 \pm 0.34,$$

(14)

$$R_{\text{res}} = 1.33 \pm 0.16.$$  

(15)

The $E_{\pi^0}^{\text{rec}}(1 - \cos\theta_{\pi^0})$ distribution after the fitting is shown in Fig. 23. The $\chi^2$ per degree of freedom, before the fit is 17.8/20 = 0.89, and it is 12.9/18 = 0.72 after the fit. The statistical error and all systematic errors described in Sec. VA 4 are included in the errors of $R_{\text{coh}}$ and $R_{\text{res}}$. Without the systematic errors, we obtain $0.79 \pm 0.30(\text{stat})$ and $1.24 \pm 0.13(\text{stat})$ for $R_{\text{coh}}$ and $R_{\text{res}}$, respectively. The dominant systematic source is the detector response.
The ratio of the NC coherent $\pi^0$ production to the total CC cross sections from the MC prediction based on the Rein and Sehgal model is $1.21 \times 10^{-2}$. Hence, the cross-section ratios are measured to be

$$\frac{\sigma(\text{NC coh} \, \pi^0)}{\sigma(\text{CC})} = R_{\text{coh}} \times 1.21 \times 10^{-2},$$

$$= (0.68 \pm 0.41) \times 10^{-2}, \quad (16)$$

where $R_{\text{coh}}$ is 0.56 ± 0.34. The mean neutrino energy for NC coherent $\pi^0$ events in the sample is estimated to be 1.0 GeV. This result is 1.6 standard deviations above the no coherent production assumption and consistent with the MC prediction based on the Rein and Sehgal model.

VI. CONCLUSIONS

In conclusion, we have observed the production of the NC $\pi^0$ events by a muon neutrino beam on a polystyrene target ($C_8H_8$) using the SciBooNE neutrino data set of $0.99 \times 10^{30}$ protons on target. The ratio of the NC $\pi^0$ production to total CC cross sections is measured to be $(7.7 \pm 0.5^{\text{(stat)}} \pm 0.5^{\text{(sys)}}) \times 10^{-2}$ at mean neutrino energy 1.1 GeV. The MC prediction based on the Rein and Sehgal model [9] is $6.8 \times 10^{-2}$. The measured shapes of the $\pi^0$ momentum and angular distributions, as shown in Figs. 21 and 22 agree with the MC prediction within uncertainties. The ratio of NC coherent $\pi^0$ production to the total CC cross section is measured to be $(0.7 \pm 0.4) \times 10^{-2}$ based on the Rein and Sehgal model [27], while the MC prediction is $1.21 \times 10^{-2}$.

ACKNOWLEDGMENTS

We acknowledge the Physics Department at Chonnam National University, Dongsin University, and Seoul National University for the loan of parts used in SciBar and the help in the assembly of SciBar. We wish to thank the Physics Departments at the University of Rochester and Kansas State University for the loan of Hamamatsu PMTs used in the MRD. We gratefully acknowledge support from Fermilab as well as various grants and contracts from the MEXT and JSPS (Japan), the INFN (Italy), the Ministry of Science and Innovation and CSIC (Spain), the STFC (UK), and the DOE and NSF (USA). This work was supported by MEXT and JSPS with the Grant-in-Aid for Scientific Research under Grant No. A 19204026, Young Scientists Grant No. S 20674004, Young Scientists Grant No. B 18740145, Scientific Research on Priority Areas “New Developments of Flavor Physics”, and the global COE program “The Next Generation of Physics, Spun from Universality and Emergence.” The project was supported by the Japan/U.S. Cooperation Program in the field of High Energy Physics and by JSPS and NSF under Contract No. under the Japan-U.S. Cooperative Science Program.