MIT OpenCourseWare http://ocw.mit.edu

18.440 Probability and Random Variables Spring 2009

For information about citing these materials or our Terms of Use, visit: http://ocw.mit.edu/terms.

18.440 problem set 4

Problems 1-3 from Ross are from the 7th or 8th Ed.

- 1. Chap. 4, Problem 36 (or 4.36).
- 2. Chap. 4, Problem 54 (or 4.54).
- 3. Chap. 4, Problem 79 (or 4.79). Also find EX.

4. State whether the following probabilities can be reasonably approximated by Poisson probabilities. If so, give a formula for the approximation and evaluate the binomial probabilities and Poisson probabilities numerically. Recall that b(k, n, p) is the probability of exactly k successes in n independent trials with probability p of success on each trial.

- (a) b(3, 30, 0.01)
- (b) b(39, 40, 0.99)
- (c) b(25, 40, 0.5).

5. (a) Show that as n becomes large, b(n, 6n, 1/6) is asymptotic to CA^n/n^b for some constants C, A, and b and evaluate the constants.

(b) Do the same for b(2n, 6n, 1/6).

(c) Asymptotically, are the two probabilities of about the same order of magnitude, or is one much smaller than the other?