ELECTRICAL CONDUCTIVITY IN THE
FeO·Fe₂O₃·Al₂O₃·SiO₂ SYSTEM.

by

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ABSTRACT

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FeO·Fe2O3·Al2O3·SiO2 SYSTEM

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Submitted to the Department of Materials Science and Engineering on January 13, 1977, in partial fulfillment of the requirements for the degree of Doctor of Philosophy.

The electrical conductivity of the FeO·Fe2O3·Al2O3·SiO2 system has been studied in the temperature range of 1000° to 1600°C and oxygen partial pressure of $10^{-9} < P_{O2} < 10^9$ atm and as a function of composition.

The compositions studied are of 7 or 17 w/o SiO2 with varying Fe3O4 and Al2O3 contents. The dc-data and the ac-conductivity up to 10 KHz for compositions with more than 33 w/o Fe3O4 are essentially equal, suggesting that the electrical conduction is predominantly electronic.

Several types of conductivity-temperature dependence are observed in air and are directly correlated with the phase chemistry of the system, particularly the crystallization sequences. The compositions studied crystallize to form multiphase composites of spinel, corundum, mullite and/or iron aluminosilicate glasses. The electrical conductivity in the crystallized composites must therefore be interpreted with a multiphase conduction model.

In the first type of conductivity-temperature behavior in air, the electrical conductivity increases with decreasing temperature with no distinct discontinuity upon solidification. The dependence of electrical conduction on temperature is of three stages in all other cases. A sharp discontinuity is observed upon solidification. The activation energies for conduction in these crystallized composites of spinel, mullite and corundum vary from 0.39 to 2.97eV, depending as to whether iron-mullite or corundum is the matrix.

The electrical conductivity of iron aluminosilicate melts at 1550° and 1600°C are also measured as a function of oxygen partial pressure and are found to depend on the total iron concentration and the Fe3+/Fe_{total} ratio. The conductivity decreases with increasing $P_{O2}$ at $P_{O2} > 10^{-1}$ atm. Over a wide intermediate range of $P_{O2}$ ($10^{-5} < P_{O2} < 10^{-1}$ atm), the conductivity remains practically constant. Upon subsequent reduction at still lower $P_{O2}$, the electrical conductivity decreases. The electrical conductivity of all the iron aluminosilicate melts studied is of the order of 0.1-0.2 ohm^{-1}.cm^{-1} over the whole oxygen partial pressure range.

The results are analyzed according to the conduction band
model and a thermally activated mechanism. Using the latter model, the fraction of Fe$^{3+}$ ions in octahedral coordination can be calculated.

Thesis supervisor: H. Kent Bowen
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Chapter I. Introduction

The present study on the electrical conductivity of the FeO$\cdot$Fe$_2$O$_3$-Al$_2$O$_3$-SiO$_2$ system is motivated by two underlying factors. First, it is undertaken because of its indirect association with the development of electrode material for coal-fired MHD power generators. Also, very little is known about the conduction mechanisms in the system. Any contribution to the understanding and modelling of the electrical conduction process is important.

The MHD electrodes must be resistive to corrosion and be compatible with the operating conditions in the channel. Hence, critical requirements are imposed on the electrode material in view of the extremely adverse channel environment. It must be of high electronic conductivity with a low temperature dependence and of good electron emissivity. For materials with appreciable ionic conductivity, a redox reaction occurs at the metal current lead-out, reducing the lifetime of the electrode module.

Iron aluminum spinel has been proposed as a candidate material for the electrode. A graded type electrode, with the hot end richer in hercynite (FeAl$_2$O$_4$) and the cooled electrode/metal interface magnetite (Fe$_3$O$_4$) rich, was proposed.\(^{(1)}\) Because of its apparently advantageous features like a high electronic conductivity and low temperature dependence and the absence of a resistive reaction layer, there has been active
research of the chemical and electrical properties of the Fe-Al-O system.

However, it must also be realized that in the MHD channel, there may be a thin layer of slag of the order of 1 mm thick deposited on the electrode surface. The slag is carried over from the combustor and becomes an integral part of the electrode assemblage. Its properties and chemical compatibility with the electrode material are therefore important factors in the overall performance of the electrode. The slag composition and thickness vary according to the type of coal used, the plasma temperature, the temperature at the electrode/slag interface and the viscous drag forces of the moving gas boundary layer. The slag compositions vary: 40-50 w/o SiO$_2$, 15-30w/o Al$_2$O$_3$, 5-15w/o (FeO+Fe$_2$O$_3$), 5-15w/o CaO, 1-5w/o MgO and different amounts of Na, K and Ti.

As a result of the large percentage of the oxides FeO, Fe$_2$O$_3$, Al$_2$O$_3$ and SiO$_2$ in the slag, it is natural that the FeO·Fe$_2$O$_3$-Al$_2$O$_3$-SiO$_2$ system is chosen as a model for the slag system interacting with the spinel electrode. Besides the engineering applications, an equally important initiative for this work is the study of conduction mechanisms in molten, glassy and crystalline silicates.

The FeO·Fe$_2$O$_3$-Al$_2$O$_3$-SiO$_2$ system is complicated. The compositions studied are those of low silica content. The electrical conductivity has been measured as a function of composition, temperature and oxygen partial pressure. It is
primarily electronic in nature. The results can be interpreted with a detailed understanding of the phase chemistry. In the next chapter, the phase equilibria of the system is reviewed together with the possible conduction models and literature related to the present work.

The thermodynamic activities of the species FeO, Fe$_2$O$_3$ and Al$_2$O$_3$ are then discussed with the emphasis that alumina behaves as a neutral oxide in the iron aluminosilicate melt and its addition has negligible effect on the Fe$^{3+}$/Fe$^{2+}$ equilibrium. Interesting insights can be obtained by using a very simple thermodynamic approach to model the system.

Above the solvus, the iron aluminosilicate melt is in equilibrium with a suspension of spinel, corundum and/or mullite particles. Below the solvus, the solid aggregates are composed of mixtures of varying amounts of spinel, corundum, mullite or glassy silicates. Here the data are interpreted in terms of conduction models for multiphase composites. The results are also discussed with respect to two possible conduction mechanisms: the classical conduction band model and the thermally activated hopping model which has been suggested for glasses and melts containing transition metal ions.
Chapter II. Theory and Literature Review

The high temperature electrical conductivity data for iron-containing silicate systems are very limited. Studies of the conductivity of silicate melts and slags have been made by metallurgists and more recently by Russian researchers. Nevertheless, little is known about the conduction mechanism in iron-containing silicate melts. Meanwhile low temperature conductivity results of semiconducting oxide glasses containing transition metal ions (TMI) are readily available and polaron hopping mechanism has been accepted as that responsible for the electronic conduction in these systems. There is only one publication on conduction in crystalline iron ortho-silicate.

This chapter is divided into three main sections. The first one is a brief examination of two models, the band theory and the polaron hopping model, which are possible mechanisms for conduction in the FeO·Fe₂O₃-Al₂O₃-SiO₂ system. This theoretical treatise is necessary because it provides the basis for the identification of the conduction mechanism in the system. The same section also includes a short review on multiphase conduction models. Since the crystallization products of the compositions studied are mixtures of spinel, corundum, mullite or glass, the net effect of these phases on the total conductivity of the composite has to be interpreted by these models.

The section following is a review of the phase equilibria in the FeO·Fe₂O₃-Al₂O₃-SiO₂ system, in air and as a function of
oxygen partial pressure. Special emphasis is placed on the structure and electrical conductivity of iron aluminum spinel, corundum and mullite.

The last section of the chapter contains a summary of the literature of the conductivity of semiconducting oxide glasses with TMI, of iron and vanadium phosphate glasses and of silicate melts.

II.1. Theory

II.1.1 Conduction Models

The electrical conductivity of a material is defined by the expression,

$$\sigma = \sum_{i} n_i z_i e \mu_i$$

where \(\ell\) is the number of different kinds of electronic and ionic charge carriers contributing to the conduction, \(n_i\) is the concentration of each carrier, \(z_i e\) is the charge on each and \(\mu_i\) its mobility. For an ionic species, the mobility is related to its diffusion coefficient by the Nernst-Einstein equation. As the conductivity in the FeO·Fe₂O₃·Al₂O₃·SiO₂ system is predominantly electronic, this section will only be a summary of the electronic conduction models pertaining to the present system.

Electronic conductivity in materials is commonly described in terms of the classical energy band model. However, for systems containing transition metal ions, the possibility of
conduction by polaron hopping cannot be neglected. Both models have been reviewed extensively in the literature\(^{2-9}\); the purpose of this section is to point out and contrast the fundamental conceptual differences between the two, particularly on the temperature dependence of the terms \(n_i\) and \(\mu_i\).

For the band theory, a normally filled valence band of a semiconductor or insulator is separated from the empty conduction band by an energy gap, \(E_g\). In the intrinsic region, electronic conduction is possible by the thermal excitation of electrons and holes* across this energy gap. The concentration of the carriers is,

\[
n_e = \frac{2\pi m_e^* kT}{\hbar^2} \frac{3/2}{e} - \left(\frac{E_g}{2kT}\right)
\]

where \(m_e^*\) is the effective mass of the electron and \(\hbar\) is Planck's constant.

If a relatively electronegative impurity center of concentration \(N_I\) is present, localized states are extended at an energy level \(E_I\) into the band gap. At a certain temperature, part of these donor states are ionized. Here, the concentration of electrons excited into the conduction band is

\[
n_e = N_I \exp\left(-\frac{E_I}{kT}\right)
\]

In the conduction band, the mobility of the electron is limited by scattering due to lattice imperfections. In highly

*For simplicity sake, only n-type conduction is considered in this section.
disordered systems, this scattering by phonons and impurities is significant. Impurity scattering dominates at low temperatures, with $\mu_i \propto T^{3/2}$. At higher temperatures, the major scattering is due to phonons, giving $\mu_i \propto T^{-3/2}$.

As the temperature dependence of the mobility is algebraic rather than exponential, the thermal activation energy obtained from the slope of a log $\sigma$ versus reciprocal temperature plot reflects the energy required for the excitation of the carriers.

When strong electron-phonon coupling exists, an electron can be trapped in a potential well generated by the lattice distortion due to its coulombic force. The electron in this bound state and the local lattice deformation associated with it is a polaron. Once localized, the polaron can hop to a neighboring unoccupied site, carrying with it the lattice distortion. At temperatures above half the Debye temperature, this motion of the polaron is regarded as a diffusive one and is thermally activated. Holstein$^3$ showed that the thermally activated mobility of the polaron is,

$$\mu = \frac{v e a^2}{kT} \exp(-2a) \exp(-W/kT)$$

(4)

where $v$ is the jump frequency, $\exp(-2a)$ is a tunneling probability for the non-adiabatic case and $a$ is the distance between centers. The thermal activation energy is made up of two terms,

$$W = W_H + \frac{1}{2} W_D$$

(5)
is half the polaron energy and \( W_D \) is the energy difference between neighboring sites.

Mott\(^{(5,10,11)}\) has extended this polaron model to the conduction in glasses and melts containing transition metal ions. The conduction mechanism is one of electron transfer between donor (Fe\(^{2+}, V^{4+}\)) and acceptor (Fe\(^{3+}, V^{5+}\)) centers and is similar to impurity band conduction in doped and compensated semiconductors. The electrical conductivity is expressed as,

\[
\sigma = N_c (1-c) \frac{\nu e^2 a^2}{kT} \exp(-2\alpha a) \exp(-W/kT)
\]

where \( c \) is the fraction of ions with the higher valency, the \( c(1-c) \) term accounts for the probability that neighboring sites are of different oxidation states, \( N \) is the concentration of the transitional metal ions and \( \nu \) is the jump frequency. The \( \exp(-2\alpha a) \) term is a tunnelling probability for the non-adiabatic case. Sayer and Mansingh\(^{(12)}\) could not observe this term for phosphate glasses with different TMIs. They concluded that small polaron hopping in the adiabatic approximation was appropriate for glasses of different compositions within the same system.

In summary, the principal difference between the band model and the polaron hopping model is in the temperature dependence of the carrier concentration and mobility. In the band model, the charge carriers are tunnelled from site to site with the temperature dependence of the conductivity determined by the change in the carrier concentration. However, for the
polaron hopping model, the number of carriers is considered constant and the mobility is thermally activated. In his model, Mott assumed that all the TMIs participate in the conduction process and that all Fe\(^{2+}\) and Fe\(^{3+}\) sites are equivalent. This may not be true.

Boon\(^{(13)}\) has studied the coordination number of ferrous ions in a wide variety of silicate glasses and found that less than 0.5% of all ferrous ions occupy tetrahedral sites. Kurkjian\(^{(14)}\) measured the Mossbauer, optical and electron paramagnetic spectra of ferric ion in phosphate and silicate glasses. The isomer shifts and ligand field parameters indicated that the Fe\(^{3+}\) was predominantly tetrahedrally coordinated in silicates and octahedrally coordinated in phosphates. This was in disagreement with Edward's\(^{(15)}\) finding that the position and intensity of the Fe\(^{3+}\) d-d absorption bands in MO\(\cdot\)P\(_2\)O\(_5\) glasses were consistent with an octahedral environment.

Taragin\(^{(16)}\) also suggested that both ferrous and ferric ions were in octahedral coordination in aluminophosphate glass from room temperature to 450°C. But Loveridge\(^{(17)}\) proposed models for the four-fold and six-fold coordination of Fe\(^{3+}\) ion in Na\(_2\)O\(\cdot\)B\(_2\)O\(_3\), Na\(_2\)O\(\cdot\)SiO\(_2\), and K\(_2\)O\(\cdot\)SiO\(_2\) glasses.

Pargamin et al.\(^{(18)}\) equilibrated CaO-Fe\(_2\)O\(_3\)-SiO\(_2\) and Na\(_2\)O-Fe\(_2\)O\(_3\)-SiO\(_2\) melts at 1550°C in air and then rapidly quenched them as glasses. They used Mossbauer spectroscopy to study the repartition of iron between Fe\(^{2+}\) and Fe\(^{3+}\) and the
distribution of Fe$^{3+}$ ions among octahedral and tetrahedral coordinations. The ferric ions were found to be tetrahedrally coordinated in the alkaline silicate glasses. 45-70% of the Fe$^{3+}$ were octahedrally coordinated in the Fe$_2$O$_3$-CaO-SiO$_2$ glasses. The effect of alumina addition was found to be dependent on composition. Their results for the Fe$_2$O$_3$-Al$_2$O$_3$-CaO-SiO$_2$ system are summarized in Figure 1.

Should the Fe$^{3+}$ ion prefer tetrahedral coordination in the glass or the melt, it is part of the network former and is covalently bounded to the silicate anion. It would not participate in the conduction process. To account for the fraction of Fe$^{3+}$ ions not in octahedral coordination, the appropriate equation for the hopping model is presently defined as

$$
\sigma = N R_{Fe} c (1-c) \frac{v e^2 a^2}{kT} \exp(-2\alpha a) \exp(-\frac{W}{kT})
$$

with

$$
R_{Fe} = \frac{Fe^{3+}_{oct}}{Fe^{3+}_{total}}
$$

II.1.2. Electrical Conductivity in Composite Systems

The crystallization products of the FeO·Fe$_2$O$_3$-Al$_2$O$_3$-SiO$_2$ system in air are mixtures of a number of phases. Thus the measured electrical conductivity would be an effective value and must be analyzed using multiphase conduction models. Numerous theoretical and empirical correlations are found in the literature and have been applied to properties such as electrical and thermal conductivity, dielectric...
Figure 1. The distribution of Fe$^{3+}$ ions among octahedral and tetrahedral coordinations in the Fe$_2$O$_3$-CaO-Al$_2$O$_3$-SiO$_2$ system as a function of composition.
constant, magnetic permeability and so forth, of a composite medium. The models are derived for random and ordered arrangements of the dispersed phases. Geometric factors are introduced to account for the shape of the particles and also their orientation and type of packing. The models are tested experimentally with composites made up of materials (conductors and insulators) of known conductivities. The tests indicated that no one model can accurately predict the conductivity of all types of composite. Review papers have been written by Meredith and Tobias,\(^{(19)}\) Ondracek\(^{(20)}\) and Progelhof et al.\(^{(21)}\). Because of the sheer number of models documented, only the more relevant ones are reviewed here.

Maxwell\(^{(22)}\) first considered the effective conductivity of equivalent, spherical particles of conductivity \(\sigma_d\) imbedded in a matrix of conductivity \(\sigma_c\). The effective conductivity \(\sigma_{\text{eff}}\) of the composite is,

\[
\sigma_{\text{eff}} = \frac{2\sigma_d + \sigma_c + f(\sigma_d - \sigma_c)}{2\sigma_d + \sigma_c - 2f(\sigma_d - \sigma_c) \cdot \sigma_c}
\]

where \(f\) is the volume fraction of the dispersed phase. His equation was derived by solving the Laplace equation for the potential inside and around the particles. This expression is for the conductivity of randomly distributed non-interacting spheres in a homogeneous continuous medium. It can be applied for \(f\) up to 0.1.

For a dispersion of more than 2 phases, the equation was
modified to

\[
\frac{\sigma_{\text{eff}} - \sigma_c}{\sigma_c} = \frac{1}{2} \sum_{i=1}^{n} \frac{\sigma_i}{\sigma_c} - 1 + f_i \frac{\sigma_i}{\sigma_c} - 1
\]  

(9)

Grekiela and Tien(23) used a tetrakaidekahedral model to fit the conductivity data of the ZrO$_2$-CaO system with 0.22-0.50 mole fraction of CaO. It was a geometric model of conducting and insulating phases with the microstructure ranging from either or both phases being the continuum. Their model predicted the discontinuity in conductivity at 39 mole % CaO.

Bruggeman(24) realized that for concentrated mixtures, the conductivity of the aggregate should be used in the derivation instead of the conductivity of the continuum. He derived the empirical formula,

\[
\frac{\sigma_{\text{eff}} - \sigma_i}{\sigma_c} = 1 - f.
\]  

(10)

This expression holds well for a large range of particle sizes in the matrix.

11.2. The FeO·Fe$_2$O$_3$-Al$_2$O$_3$-SiO$_2$ System.

The phase equilibria in this system have been studied by Muan.(25,26) The four component system can be described by a tetrahedron with FeO, Fe$_2$O$_3$, Al$_2$O$_3$ and SiO$_2$ at the corners.
In Figure 2 the plane FeO·Fe$_2$O$_3$·Al$_2$O$_3$·SiO$_2$ is outlined inside the tetrahedron. Also shown is the 0.21 atmosphere oxygen (air) isobaric liquidus surface represented by the dotted and dashed grid to illustrate its position relative to the FeO·Fe$_2$O$_3$·Al$_2$O$_3$·SiO$_2$ plane. The dotted and dashed lines such as CB and AD are parallel to the FeO·Fe$_2$O$_3$·Al$_2$O$_3$ basal plane and are lines of isosilica content. AB is the locus of points where the surface intersects the FeO·Fe$_2$O$_3$·Al$_2$O$_3$·SiO$_2$ plane. The dotted lines indicate that the liquidus surface is to the left and Fe$_2$O$_3$ side of the plane as the wt%Fe$_2$O$_3$/wt%FeO ratio is greater than 2.22. At higher silica and alumina contents the surface is on the right and FeO side of the plane (dashed lines).

Because of the close proximity of the liquidus surface to the FeO·Fe$_2$O$_3$·Al$_2$O$_3$·SiO$_2$ plane, Muan has projected it onto the plane and treated it as if it were a true ternary system of FeO·Fe$_2$O$_3$·Al$_2$O$_3$·SiO$_2$ (Figure 3). Parts of the 1400°, 1500° and 1600°C isotherms are included. The light dashed lines are lines passing through points of equal wt% Fe$_2$O$_3$/wt% FeO ratios along the liquidus surface.

There are four primary phase fields in which a crystalline phase coexists with the melt. They are spinel, corundum, mullite and cristobalite (tridymite at lower temperatures). P is a piercing point at 1460°C where spinel(ss), corundum(ss), mullite(ss), melt (17 w/o FeO, 38w/o Fe$_2$O$_3$, 25w/o Al$_2$O$_3$ and 20w/o SiO$_2$) and a gas phase ($P_{O_2}=0.21$ atm) are in equilibrium.
Figure 2. The FeO·Fe₂O₃-Al₂O₃-SiO₂ system with the 0.21 atmosphere oxygen isobaric liquidus surface included.
Figure 3. Projection of the 0.21 atmosphere oxygen isobaric liquidus surface onto the FeO-Fe$_2$O$_3$-Al$_2$O$_3$-SiO$_2$ plane. (After Muan, Ref. 25)
Another piercing point is E. It is the lowest temperature (1380°C) where the melt can exist in air. Here the phases in equilibrium are spinel(ss), tridymite, mullite(ss), melt (16w/o FeO, 25w/o Fe₂O₃, 19w/o Al₂O₃ and 40w/o SiO₂) and the gas phase.

In sharp distinction to the phase equilibria in air, six piercing points are present on the 1 atm oxygen liquidus surface. Two new primary phase fields are added, hematite (ss) and Fe₂O₃·Al₂O₃. The highest piercing point is at 1495°C where spinel (ss), corundum (ss), Fe₂O₃·Al₂O₃, melt and oxygen are in equilibrium. The lowest one is at 1390°C, where tridymite, hematite(ss), mullite(ss), melt and the gas phase coexist.

Fewer data are available pertaining to phase relationships at lower P₀₂. However, the qualitative effect of lower oxygen partial pressure is to enhance the spinel and corundum phase fields. The temperature of the liquidus surface is also lowered. A wustite phase field appears at about 10⁻¹⁰ P₀₂ atmosphere.

The spinel, corundum and mullite phases all exhibit varying degrees of solid solution behavior with temperature and P₀₂. The iron aluminum spinel is a complete solid solution of the end members magnetite (Fe₃O₄) and hercynite (FeAl₂O₄). The corundum has some Fe₂O₃ in solid solution. Mullite (3Al₂O₃·2SiO₂) is even more complicated. It not only can have variations in the Fe/(Fe+Al) ratio but also in the Si/(Al+Fe)
ratio. All these factors lead to very complicated crystallization sequences, as will be shown in a later chapter.

As the compositions of major concern in this study lie in the spinel and corundum phase fields, the structure, defects and conductivity of iron aluminum spinel, corundum and mullite will be reviewed.

II.2.1. Iron Aluminum Spinel.

The spinel structure has oxygen ions arranged in a face-centered close packed lattice. The cations distribute themselves among the octahedral and tetrahedral sites. Magnetite is an inverse spinel with half of its Fe$^{3+}$ ions in the tetrahedral sites. The rest of the Fe$^{3+}$ and the Fe$^{2+}$ fill half of the existing octahedral sites. Hercynite has a normal spinel structure which means that the Al$^{3+}$ ions prefer the octahedral interstices while the Fe$^{2+}$ ions fill one-eighth of the tetrahedral sites. The thermodynamics of cation distribution in binary spinels has been studied by Navrotsky.\(^{(27)}\) The molar enthalpy of interchange of cations on the octahedral and tetrahedral sites was calculated with configurational entropy considered as the only consequence of the disordering. Empirical tetrahedral and octahedral site preference energies were obtained for a series of divalent and trivalent cations in spinel.

The conductivity of magnetite has been studied by Miles\(^{(28)}\) and also by Tannhauser.\(^{(29)}\) The conductivity at high temperatures was only slightly temperature dependent and was of n-type.
The results were explained by an electron-transfer model between ferrous and ferric ions on octahedral sites. Hence the conductivity was proportional to the product of the concentration of each species. Tannhauser concluded that the normal free electron in a band model was inappropriate for interpreting the conductivity data.

The conductivity of hercynite and iron aluminum spinels of different compositions have been studied recently by Mason (30). Some of the results are included in Figure 4 together with Miles's for magnetite. Addition of 70 mole% FeAl₂O₄ still did not affect the contour of the conductivity plot to any large extent.

II.2.2. Corundum

The corundum structure has a hexagonal close-packed oxygen sublattice with two-thirds of the octahedral voids filled by aluminum ions. All the tetrahedral sites are empty. The cations are arranged along the c-axis such that each pair of aluminum ions is separated by an unoccupied octahedral site.

Because Al₂O₃ is such a wide band gap material, the electrical properties are usually controlled by the aliovalent impurities present. This is reflected in the activation enthalpy for conduction in the extrinsic range at low temperature. Due to the enormous number of publications on the subject, only the more significant work on the electrical conductivity is reviewed.

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Figure 4. Electrical conductivities of Iron Aluminum Spinels and Magnetite (After T.O. Mason\textsuperscript{30}).
Pappis and Kingery\textsuperscript{(31)} reported that single crystal alumina was an n-type conductor at low oxygen partial pressure, changing to p type conduction at high partial pressures. The activation energy for conduction was 2.97eV.

Brook et al.\textsuperscript{(32)} identified aluminum interstitials as the principal ionic carriers at high $P_\text{O}_2$, with a calculated mobility of about $6 \times 10^{-4}$ cm$^2$/v·sec at 1600°C. The dc-conductivity below 1600°C has an activation energy of 2.9eV for both doped (Ti, Mg, Co, and Si) and undoped crystals.

Kitazawa\textsuperscript{(33)} observed a thermal activation energy of 3.47eV above 1400°C and attributed it to the electronic conductivity in the intrinsic region. Below 1400°C, the activation energy became 2.47eV and was due to extrinsic conduction (total impurity content, 100 ppm, mainly Si). The observed oxygen partial pressure dependence was similar to Pappis and Kingery's. However, below 1400°C there existed a wide intermediate $P_\text{O}_2$ range where the conductivity showed no dependence on the oxygen pressure. Emf measurements showed predominantly ionic conduction in this non-$P_\text{O}_2$ dependent region. Undoped, hot-pressed and MgO-doped polycrystalline samples exhibited conductivities of about two orders of magnitude larger. This was attributed to enhanced electronic conduction in the grain boundaries.

All the above works have suggested that electrical conduction is dominated by extrinsic (impurity) effects at low temperatures, that is, the presence of impurities control the
concentrations of point defects. Pollak\textsuperscript{(34)} has systematically doped alumina with Fe(0.08, 0.5 and 4.4 mole\%). For low iron-dopant level, the conductivity was p-type at high $P_{O_2}$ and n-type at low $P_{O_2}$, similar to earlier findings. However, for high iron concentration, the effect of $P_{O_2}$ was reversed. This peculiar response to the change in oxygen partial pressure was linked to the precipitation of a spinel phase at low $P_{O_2}$ for the 4.4 mole\% Fe-Al$_2$O$_3$ sample. The solubility limit of iron in Al$_2$O$_3$ decreased with decreasing $P_{O_2}$. The appearance of the spinel second phase was equivalent to reducing the Fe dopant level in the corundum matrix.

The magnitude of the conductivity measured varied from $10^{-2}$ to $10^{-5}\text{(ohm}\cdot\text{cm})^{-1}$ between 1600$^\circ$ and 1400$^\circ$C as compared to $10^{-5}$ to $10^{-7}\text{(ohm}\cdot\text{cm})^{-1}$ for nominally "pure" samples. The activation energy obtained was 3.9eV of which 3.5eV was assigned to energy for defect formation. Figure 5 summarizes the results of these workers.

Dutt and Kroger\textsuperscript{(35)} speculated that most Fe ions were present in corundum in the trivalent state. They derived a defect model with Fe$^{\text{III}}_{\text{Al}}$ compensating for Al$^{\text{V}}$, suggesting that the conduction would be p-type at high $P_{O_2}$. They also obtained equilibrium constants for the defect reactions. However, the accuracy of their enthalpies for defect reactions remains questionable.
Figure 5. Electrical conductivities of doped and undoped single and polycrystalline Al$_2$O$_3$. 
II.2.3. Mullite

Mullite, $3\text{Al}_2\text{O}_3 \cdot 2\text{SiO}_2$, is a crystalline silicate which belongs to the orthorhombic system.\(^{(36,37)}\) The unit cell dimensions are: $a_0 = 7.583 \pm 0.002\AA$, $b_0 = 7.681 \pm 0.002\AA$ and $c_0 = 2.8854 \pm 0.0005\AA$. Mullite shows a wide variation in composition and is regarded as an intermediate disordered phase between sillimanite ($\text{Al}_2\text{O}_3 \cdot \text{SiO}_2$) and andalusite ($2\text{Al}_2\text{O}_3 \cdot \text{SiO}_2$).

Mullite has an open structure. It consists of chains of Al octahedra running parallel to the $c$-axis at the center and the four corners of the unit cell. These octahedra are cross-linked by tetrahedra containing both Al and Si ions. The Si and Al in the tetrahedra in mullite are randomly mixed, thereby making it a disordered structure. To arrive at the formula unit of 60 mole% $\text{Al}_2\text{O}_3$, some of the tetrahedrally coordinated Si ions in sillimanite are replaced by Al, accompanied by a shift of some tetrahedral cations into new positions. Oxygen must also be removed to maintain electrical neutrality.

Other cations have appreciable solubility in mullite.\(^{(36)}\) The most notable examples are Fe and Ti. Natural iron-mullites can contain up to 6% $\text{Fe}_2\text{O}_3$. The Fe cation is present mostly in the trivalent state, replacing the Al ions.

Two publications\(^{(38,39)}\) discussed the coordination of the $\text{Fe}^{3+}$ ion in mullite. Iron-doped kaolinite glasses were re-crystallized to form a mullite phase with the Mossbauer spectra indicating that the $\text{Fe}^{3+}$ ions were in octahedral coordination. An earlier study on the change in Mossbauer spectrum during
the phase transformation from kaolinite to mullite suggested that Fe$^{3+}$ was distributed between the tetrahedral and octahedral sites. However, other workers have indicated that the same spectrum resembled a quadrupole doublet for Fe$^{3+}$ ions in octahedral coordination alone.

Electrical conductivity and gravimetric measurements were carried out by Sockel in iron orthosilicate, $2\text{Fe}_{1-y}\text{O} \cdot \text{SiO}_2$ in CO/CO$_2$ atmospheres between 1000°C and 1150°C. The electrical conductivity was of the order of $10^{-2}$ - $10^{-3}$ ohm$^{-1}$·cm$^{-1}$. The possible defects were discussed on the basis of the crystal structure. The dependence of both sets of measurements on $\text{Po}_2^{1/6}$ was consistent with a defect model with doubly ionized iron vacancies and an equal concentration of electron holes. The difference between the enthalpies in conductivity and gravimetric results was 0.252eV and was assumed to be the activation enthalpy for motion of electron holes. The calculated mobility for electron holes was $6 \times 10^{-3} \text{cm}^2/\text{v} \cdot \text{sec}$. All these strongly indicate a small polaron conduction mechanism.

II.3. Electrical Conductivity of Glasses and Silicate Melts

II.3.1. Semiconducting oxide glasses containing transition metal ions (TMI).

In the early 60's, a lot of enthusiasm was centered around the then "newly" discovered semi-conducting oxide glasses containing TMI (such as V, Fe, Co, Cu and Mn).
Verwey\(^{(41)}\) had earlier recognized the importance of the oxidation states of the TMI to the overall conductivity of semiconducting glasses. He introduced the notion of a controlled valence scheme, by adding TMI in different valence states, to fix the conductivity of semiconductors. Mackenzie\(^{(42)}\) suggested that the electrical conductivity would also be governed by the concentration and the interatomic separation of the TMI centers.

The fact that these glasses exhibited electronic conduction was supported by the time independent dc-conductivities, by the absence of any induced emf due to ionic conduction, by the low thermal activation energies for conduction and also by the high magnitudes of the conductivities.

The activation energies for the electrical conductivity of 20BaO-60GeO\(_2\)-20V\(_2\)O\(_5\), 31CaO-61B\(_2\)O\(_3\)-8Fe\(_3\)O\(_4\) and 30CaO-60B\(_2\)O\(_3\)-10CoO glasses were about half those when the TMI were absent.\(^{(43)}\) The addition of 30 mole\% CoO to a CaO-B\(_2\)O\(_3\) glass lowered the resistivity at 350°C by five orders of magnitude, to about 10\(^7\) ohm·cm. Also, with glass compositions of 50.8-87.5 mole\% V\(_2\)O\(_5\), 10-30 mole\% P\(_2\)O\(_5\), 2.3-20 mole\% BaO and 6.5-10.8 mole\% Na\(_2\)O in the V\(_2\)O\(_5\)-P\(_2\)O\(_5\)-BaO and V\(_2\)O\(_5\)-P\(_2\)O\(_5\)-BaO-Na\(_2\)O systems,\(^{(44)}\) the activation energies were as low as between 0.34-0.39eV.

Trap and Stevels\(^{(45)}\) successfully prepared semiconducting glasses from Na\(_2\)O-CaO-SrO-Al\(_2\)O\(_3\)-SiO\(_2\) and Na\(_2\)O-MnO-MgO-Al\(_2\)O\(_3\)-Co\(_3\)O\(_4\)-SiO\(_2\) systems with various amounts of Fe\(_3\)O\(_4\). The conductivity below 500°C could be as high as 10\(^{-2}\)-10\(^{-3}\) ohm\(^{-1}\)·cm\(^{-1}\).
with about 15 mole% of Fe$_3$O$_4$ added. The activation energies had a distinct dependence on the Fe$^{3+}$/Fe$^{2+}$ ratios.

Ferric oxide is a nucleating agent to glasses in the CaO-MgO-Al$_2$O$_3$-SiO$_2$ system. (46-48) O'Horo (49) heat treated an alumino-borosilicate glass with 12 mole% Fe$_2$O$_3$ at 650°C to 800°C resulting in the precipitation of a spinel phase. Upon progressive treatment at higher temperature and for longer time periods, the conductivity underwent dramatic changes. For anneals between 650°C and 800°C the conductivity dropped with increasing annealing temperature, caused by the removal of Fe ions from the glass matrix. At the same time the activation energy increased from 0.68eV to 1.2eV. However, on further anneal at 800°C or higher, the conductivity suddenly increased by several orders of magnitude and the activation energy dropped to 0.02eV. This was attributed to the formation of a continuous spinel network in the glassy matrix.

GeO$_2$-P$_4$O$_{10}$-V$_2$O$_5$ glasses (50,51) have conductivities ranging from $2 \times 10^{-3}$ to $10^{-9}$ ohm$^{-1}$·cm$^{-1}$ at 25°C. Measurements up to 200°C revealed that the conductivity depended on the V$_2$O$_5$ content, and it decreased with increasing concentrations of V$^{4+}$ ions ($V^{5+}$/V$^{4+}$ = 0.5-23.5). For the compositions less than 10 mole% V$_2$O$_5$, the glasses no longer exhibited any electronic conduction, probably because the VO$_6$ octahedra were isolated and this prohibited charge transfer between adjacent sites.
V$_2$O$_5$-CaO-B$_2$O$_3$ and V$_2$O$_5$-CaO-P$_2$O$_5$ glasses$^{(52)}$ have activation energies from 0.47 to 1.11eV. Both the enthalpy and the magnitude of the conductivity were functions of composition, V$^{5+}$/V$^{4+}$ and also the network former. With the same V$^{5+}$/V$^{4+}$ ratio and composition, the conductivity for the B$_2$O$_3$ glass was lower than that for the P$_2$O$_5$ system.

II.3.2. Iron and Vanadium Phosphate Glasses

Hansen$^{(53)}$ reported the only instance where a conductivity maximum occurred at $c=0.5$ as predicted by Mott's model (Eq. 5) for 55(FeO+Fe$_2$O$_3$):45P$_2$O$_5$ glass (in mole%) at 200°C. A resistivity versus $c$ plot went through a broad minimum between $c=0.4$ and 0.6. Unfortunately the variation in resistivity was 10 times higher than if it were to be controlled by the factor $c(1-c)$ alone. This suggested variations in other factors in the model. The thermal activation energies obtained from 300°-700°K ranged from 0.7eV for 55(FeO+Fe$_2$O$_3$):45P$_2$O$_5$ to 1.6eV for 55MgO-45P$_2$O$_5$ composition.

The thermoelectric power for 55(FeO+Fe$_2$O$_3$):45P$_2$O$_5$ glass was virtually temperature independent but very sensitive to $c$. The conductivity changed from p-type to n-type at $c=0.38$, in contradiction to the conductivity maximum occurring at $c=0.5$.

The difficulty encountered in fitting the data with Mott's model was well demonstrated by Vaughan and Kinser.$^{(54)}$ The conductivity maxima for $x$(FeO+Fe$_2$O$_3$):(100-$x$)P$_2$O$_5$ samples of $x$ up to 75 mole% did not in general occur at $c=0.5$. 
except for the special case where \( x = 55 \). The maximum shifted to higher \( c \) with increasing iron content. Phase separation was discovered for glasses containing more than 60 mole\% (FeO+Fe\(_2\)O\(_3\)). Magnetic coupling between Fe\(^{2+}\) ions and the segregation of Fe\(^{2+}\) in the second phase were suggested as possible causes for the difficulty in the data analysis.

The mechanical loss,\(^{(55)}\) modulus relaxation and the ac dispersion\(^{(56)}\) between \( 10^2 \) and \( 10^5 \) cps for the 55(FeO+Fe\(_2\)O\(_3\))·45P\(_2\)O\(_5\) glass were attributed to the induced resonance of electron hopping between the Fe\(^{2+}\) and Fe\(^{3+}\) sites because the temperature dependence of these processes was equivalent to the activation enthalpy for the dc conduction process. However, Kinser\(^{(57)}\) disagreed and noted a change in conductivity upon thermal treatment and the concomitant appearances of dielectric losses with observed devitrification under electron microscopy. He suggested that the dispersions were of the Maxwell-Wagner type from a highly conducting dispersed phase.

Dozier et al.\(^{(58)}\) saw similar changes of conductivity on annealing. Whether the conductivity increased or decreased depended on both the original Fe\(^{3+}/\text{Fe}_{\text{tot}}\) value and the time of anneal. This reflected the effect of the removal of Fe\(^{3+}\) and Fe\(^{2+}\) ions from the matrix, due to devitrification, on conductivity.
Schmid(59) extended Holstein's(3) treatment of small polarons and discussed the validity of small polarons as the carriers in TMI glasses. In particular, he chose to study phosphate glasses containing various amounts of V₂O₅. The activation energies ranged from 0.4-1.0eV for high temperature (below 300°K) and 0-0.2eV for below 100°K. The conductivity did not show a clear-cut dependence on the amount of V₂O₅, but on the importance of the V⁵⁺/V⁴⁺ ratio.

Contrary to the iron phosphate glasses, the Seebeck coefficient in V₂O₅-P₂O₅, V₂O₅-CaO-P₂O₅ and V₂O₅-CaO-B₂O₃ glasses(60) changed sign at c = 0.5. On the other hand, Linsley's(61) work on a series of V₂O₅-P₂O₅ glasses indicated that the conductivity maxima occurred at c values of 0.8-0.9. Munakata(62) also reported similar results for 60V₂O₅-5BaO-35P₂O₅ and 60V₂O₅-20BaO-20P₂O₅ glasses where the conductivity maxima occurred between c values of 0.8-0.85. Linsley also observed a linear relationship between the (1-c) term at the conductivity maximum and the P₂O₅ content. The results of these studies are presented in Figure 6. Also included are Hansen and Vaughan et al's data for iron phosphate glass.

So, in vanadium phosphate glasses the conductivity results are inconsistent with Mott's model. While Linsley was unable to rationalize the conductivity results with the hopping model, he attributed this to the complexity in the glass structure. A fraction, θ, of the V⁵⁺ sites were assumed to be rendered inactive such that the c(1-c) term became
Figure 6. Normalized conductivity for phosphate glasses as a function of the oxidation state of the TMI.
(c-θ)(1-c). This was unreasonable for the values of θ calculated (0.63-0.78) because the conductivity would become negative at sufficiently low values of c. Another plausible explanation was the active participation of a fraction of V$^{5+}$ ions in the formation of polymeric network and thus, were screened from any V$^{4+}$ ions.

II.3.3. Silicate Melts.

Very few experimental data have been compiled for silicate melts containing FeO, Fe$_2$O$_3$ or Al$_2$O$_3$. Most of the early work has been concentrated on the conductivities of binary systems. These were ionic in nature. It was later observed that the electrolysis of melts containing iron oxide provided evidence of electronic contribution to the conductivity. Recently research on the conductivity of ferrous slags has been related to MHD activities.

Bockris(63,64) measured the conductivity of silicate melts containing CaO, MnO or Al$_2$O$_3$ over the temperature range of 1000°C-1800°C. The Arrhenius relationship, $\sigma = A \exp(-E/kT)$, was obeyed for all three oxides. In the Al$_2$O$_3$-SiO$_2$ system with 0.03-0.12 mole fraction alumina, the conductivity was of the order $10^{-3}$-$10^{-4}$ ohm$^{-1}$·cm$^{-1}$ at 1600°C-1700°C (as compared to $10^{-1}$ohm$^{-1}$·cm$^{-1}$ for CaO-SiO$_2$ and MnO-SiO$_2$ systems) and was independent of the oxygen partial pressure. Under isothermal conditions, a conductivity maximum occurred at 0.05 mole fraction Al$_2$O$_3$. The terms E and A were dependent
on the composition and varied from 0.559-1.07eV and 0.1-0.2 respectively. The low conductivity of the Al$_2$O$_3$-SiO$_2$ system and the increased viscosity of the melt were evidence that the aluminum and silicon ions were associated with network tetrahedra.

In a 38 w/o CaO 20w/o Al$_2$O$_3$ 42w/o SiO$_2$ melt, the Al tracer diffusivity was 1.6 x 10^-6 cm$^2$/sec at 1450°C. Those for Ca and Si were 4 x 10^-6 cm$^2$/sec and 2 x 10^-6 cm$^2$/sec respectively. Since the density of a slag of composition 10.04w/o CaO 15.06w/o Al$_2$O$_3$ 1.2w/o CrO$_2$ 4.8w/o Nb$_2$O$_5$ 9.7w/o V$_2$O$_5$ 13.5w/o TiO$_2$ 20.7w/o CaF$_2$ 25w/o SiO$_2$ is 2.88 gm/cm$^3$ at 1650°C, the density of the above CaO-Al$_2$O$_3$-SiO$_2$ melt is assumed to be 3.0 gm/cm$^3$. Using the Nernst-Einstein equation, the ionic conductivities calculated for the Ca, Al, and Si ions are 2.11 x 10^{-1} ohm^{-1}.cm^{-1}, 1.01 x 10^{-1} ohm^{-1}.cm^{-1} and 4.35 x 10^{-1} ohm^{-1}.cm^{-1} respectively. Comparing the calculated value for Ca ions with the measured conductivity of 1 x 10^{-1} ohm^{-1}.cm^{-1} for the CaO-SiO$_2$ system shows that most of Ca ions contribute to the conduction process. However, the low conductivity (10^{-3} - 10^{-4} ohm^{-1}.cm^{-1}) of the Al$_2$O$_3$-SiO$_2$ system suggests that a large fraction of Al ions are covalently bonded to anion complexes in the melt and are not available as free charge carriers.

The ternary system CaO-Al$_2$O$_3$-SiO$_2$ was studied by Martin and Derge. The conductivity was measured under a nitrogen atmosphere for compositions 35.1-50.1%SiO$_2$, 35.1-50.05%CaO
and 5.0-19.7% Al$_2$O$_3$ between 1400-1620°C. The conductivity at 1600°C was of the order of 0.25-0.8 ohm$^{-1}$cm$^{-1}$, close to the values for CaO-SiO$_2$.

In a short note, Tomlinson and Inouye$^{(68)}$ asserted that the conductivity of liquid iron oxide contained in an iron crucible was above 150 ohm$^{-1}$cm$^{-1}$ above 1400°C. In later work$^{(69)}$ they measured the p-type conduction in wustite melts with iron electrodes in a nitrogen atmosphere. Addition of 5 mole% of Al$_2$O$_3$ reduced the conductivity from 324 ohm$^{-1}$cm$^{-1}$ to 227 ohm$^{-1}$cm$^{-1}$ at 1500°C. SiO$_2$ had a still larger effect, dropping the conductivity to 164 ohm$^{-1}$cm$^{-1}$ with a 5.4 mole% addition. Their data on iron oxide melts were over an order of magnitude higher than those of Fisher and Vom Ende$^{(70)}$. The conductivities of FeO-SiO$_2$ are plotted in Figure 7 together with those of Al$_2$O$_3$-SiO$_2$ and CaO-SiO$_2$.

The weight loss by an iron anode during the electrolysis of iron-silicate melt gave a measurement of the anode current efficiency, $C_+$(%), based on a two-electron charge in the oxidation of metallic iron anode.

$$C_+ = \frac{100\Delta W}{27.93n}$$

(11)

where $\Delta W$ is the loss in anode mass, $n$ is the number of Faradays passed and 27.93 is the gram-equivalent of iron. Simnad et al$^{(71)}$ reported that the current efficiency stayed between 8-12% for compositions below 10wt% SiO$_2$, then it increased
Conductivities of Binary Silicate melts

FeO-SiO₂

mol % SiO₂

CaO-SiO₂

mol % CaO

Al₂O₃-SiO₂

mol % Al₂O₃

Figure 7. Electrical conductivity of binary silicate systems: FeO-SiO₂, CaO-SiO₂ and Al₂O₃-SiO₂.
linearly with the addition of SiO₂ to about 90% for 34wt% SiO₂. The temperature effect was negligible from 1200°-1400°C. Gaseous oxygen was evolved at the anode, an indication that the anodic oxidation of silicate ions occurred. Otherwise the bulk of the ionic current was carried by ferrous ions.

P-type conduction was observed for the FeO-MnO-SiO₂ system(72) in argon. The behavior was more complex; the addition of MnO might or might not affect the current efficiency, depending on the amount of SiO₂. On the other hand, addition of SiO₂ naturally increased it. The interpretation was further obscured by the fact that not only charge transfer between Fe²⁺ and Fe³⁺ but also between Mn²⁺ and Mn³⁺ contributed to electronic conductivity.

Both calcium and iron ions were ionic carriers in FeO-CaO-SiO₂ melts(73,74) under argon. The transference number calculated for calcium ion showed that an unusually high fraction of the ionic current was carried by this ion. This supported the prevailing view that the ferrous ions were associated with the silicate anion complexes, giving low activities of FeO in iron silicate melts. The anode current efficiencies of FeO-SiO₂, FeO-CaO-SiO₂ and FeO-MnO-SiO₂ are included in Figure 8 for comparison.

Recently there have been numerous publications in the Russian literature on the electrical conductivity of silicate melts as a function of oxygen partial pressure. Both FeO-Fe₂O₃-SiO₂(75) and FeO-Fe₂O₃-CaO-Al₂O₃-SiO₂(76) exhibited
Figure 8. Anode current efficiency measured in the electrolysis of iron oxide-containing silicate melts.
limited dependence of conductivity on the oxygen partial pressure. For the FeO-Fe$_2$O$_3$-SiO$_2$ melts with greater than 34% SiO$_2$, the conductivities were virtually independent of oxygen pressure ($10^{-1}$-$10^{-12}$ atm). For compositions with above 66% (FeO+Fe$_2$O$_3$), the conductivities decreased with decreasing P$_{O_2}$ at $10^{-8}$-$10^{-11}$ atmospheres. For CaO-Al$_2$O$_3$ containing melts, the conductivity was 1-2 orders of magnitude lower. In all cases, the conductivity was independent of frequency ($10^2$-$10^4$ Hz).

Their data interpretation was based on the erroneous assumption that only the electronic conductivity was a function of P$_{O_2}$. This could not be true in the iron-silicates. The oxygen partial pressure controls the Fe$^{3+}$/Fe$^{2+}$ ratio and affected their respective contribution to ionic conduction.

Engell and Vygen(77) studied the conductivity of FeO-Fe$_2$O$_3$-CaO-SiO$_2$ melts. They chose compositions with a $n_{CaO}/n_{SiO_2}$ ratio of 0.79 because the Fe$^{3+}$/Fe$^{2+}$ was a function only of P$_{O_2}$ and not the overall composition. Ac-conductivity was measured at 30KHz. The conductivity results were modelled for contributions from ionic and electronic carriers.

$$\sigma_{total} = \sigma_0 - a'c + b'c(l-c) \quad (12)$$

$$c = \frac{Fe^{3+}}{Fe_{total}}$$

where $\sigma_0$ was the ionic conductivity due to Ca$^{2+}$ and Fe$^{2+}$ ions in a FeO-CaO-SiO$_2$ melts when c = 0. The term a'c was the ionic part that was subtracted from the conductivity to account for...
the difference in the mobilities of Fe$^{2+}$ and Fe$^{3+}$ and the increased concentration of Fe$^{3+}$ ions.

The $b'c(l-c)$ term was discussed in two limiting cases. The first was electron hopping by Mott's model. Engell and Vygen also considered a collision-dependent, bimolecular reaction which allowed for diffusional relaxation after charge transfer. In this context, an activated complex of Fe$^{2+}$ and Fe$^{3+}$ ions was necessary for charge transfer.

Figure 9 shows the dependence of the electrical conductivity on the oxygen partial pressure for a number of silicate melts. $N_{Fe}$ is defined as

$$N_{Fe} = \frac{n_{FeO} + 2n_{Fe_2O_3}}{N_{FeO} + 2n_{Fe_2O_3} + n_{CaO} + n_{SiO_2}}$$

(13)

All of the melts exhibit only very limited response to the change in the oxygen partial pressure.
Figure 9. Electrical conductivity of iron-oxide-containing melts as a function of oxygen partial pressure.
Chapter III. Ionic Activities in Silicate Melts—A Thermodynamic Approach to the FeO·Fe₂O₃·Al₂O₃·SiO₂ System.

The ionic constitution of liquid silicates has been the subject of recent research studies. To the metallurgist, an understanding of the silicate systems is crucial and provides important data for controlling slag reactions. This is, in itself, of obvious value in industrial applications. To others, the complex silicate melts pose an attractive yet puzzling class of systems that demands theoretical modelling.

There are very few experiments that can provide direct confirmation about the structure of silicate melts. It used to be common practice to study the density, viscosity, diffusivity and thermodynamic activities so that inference could be made on the ionic arrangement. But these only give indirect information about ionic distributions and interactions. Only recently (78-80) have experimental techniques been developed, for example, the trimethylsilyl derivatives of the silicate anions have been isolated, identified and their ionic distributions determined.

Parallel to these developments, there have also been significant advances in the modelling of these complex systems. Common basic oxides in slags such as FeO, MnO, CaO, MgO and PbO are expected to ionize and give free cations and oxygen anions which may or may not be bonded to the silicon ion. Silicate anions exist as the monomer SiO₄⁻, the dimer
Si\textsubscript{2}O\textsuperscript{6}-, the trimer Si\textsubscript{3}O\textsuperscript{8}-, and so on.

Flood\textsuperscript{(81)} and Richardson\textsuperscript{(82)} were the first ones to describe the silicate melt by an equilibrium distribution of silicate ions. Toop and Samis\textsuperscript{(83,84)} chose to represent the polymerization in slags by a simple equilibrium reaction (equilibrium constant \(K\)) between oxygen ions doubly bonded (O\textsuperscript{2-}), singly bonded (O\textsuperscript{-}) to silicon ions and other free oxygen ions, (O\textsuperscript{2-})

\[
2O^{2-} \rightleftharpoons O^2 + O^{2-} \quad K \quad (14)
\]

Masson\textsuperscript{(85-87)} decided that it was inadequate to consider the equilibrium reaction without considering the silicate anions. Hence he selected polycondensation reactions of the following type,

\[
\text{SiO}_4^{2-} + \text{Si}_xO_{2(x+1)}^{2-} \rightleftharpoons \text{Si}_{x+1}O_{3x+4}^{2(x+2)-} + O^{2-} \quad K_x \quad (15)
\]

He assumed that ring structures were non-existent in the melt so that all silicate anions were in linear chain configuration with \(K_x\) being the same for all \(x\). This was because, in the polymerization reaction, the free energy of breaking a double oxygen bond in a linear chain would be the same no matter how large the anion was. The value of \(K_x\) would be characteristic of each MO-SiO\textsubscript{2} system. \(K_x\) for FeO-SiO\textsubscript{2} was 1.0 at 1600°C and 0.7 at 1300°C. These were computed by fitting the measured thermodynamic activities with the
model, which also predicted that the $\text{SiO}_4^{4-}$ monomer was the most abundant species in FeO-SiO$_2$ melts at all compositions.

Unfortunately this model has only been successfully applied to binary systems of the type MO-SiO$_2$. So it should be noted that while the FeO-SiO$_2$ system has been well documented, little is known about the ionic structure in FeO-Fe$_2$O$_3$-SiO$_2$, let alone that in the FeO-Fe$_2$O$_3$-Al$_2$O$_3$-SiO$_2$ system.

The sections following present a simple thermodynamic approach in calculating the activities of the FeO-Fe$_2$O$_3$-Al$_2$O$_3$-SiO$_2$ system, leading to the justification of the choice of the alumina crucible as the conductivity cell.

III.1. Thermodynamic Activities in the FeO-Fe$_2$O$_3$-Al$_2$O$_3$-SiO$_2$ System.

The thermodynamic activities of FeO, Fe$_2$O$_3$ and SiO$_2$ in the FeO-Fe$_2$O$_3$-SiO$_2$ system have been experimentally determined by Schuhmann and Ensio$^{(88)}$ and Schuhmann and Michal.$^{(89)}$ A premixed CO/CO$_2$ gas was bubbled through the melt contained in either a silica or $\gamma$-iron crucible. When equilibrium was reached between the gas and the melt, the melt was chemically analyzed.

The Gibbs-Duhem integration of the activity terms was simplified as the activity of one component was fixed (SiO$_2$ or Fe). The activity of another component could be expressed in terms of the oxygen potential. For a silica saturated melt, the Gibbs-Duhem integration became

56
\[
\log a_{\text{FeO}} = -\frac{1}{2} \int \frac{N_{\text{Fe}^{3+}}}{N_{\text{Fe total}}} \, d \log \left( \frac{P_{\text{CO}_2}}{P_{\text{CO}}} \right) \quad (16)
\]

Similar equations were obtained for melts under different equilibrium conditions. Turkdogan (90) gathered the data available and calculated the iso-activity curves for FeO, \( \text{Fe}_2\text{O}_3 \) and \( \text{SiO}_2 \) in the melt at 1550°C.

Lumsden (91) claimed that the activities of the system could be represented with a simple regular solution model. The ionic species he chose were \( \text{FeO} \), \( \text{FeO}_{1.5} \) and \( \text{SiO}_2 \).

The following is a simple regular solution approach to see if it can successfully fit the experimentally measured activities of the \( \text{FeO}-\text{Fe}_2\text{O}_3-\text{SiO}_2 \) system.

For the reaction,

\[
2\text{FeO} + \frac{1}{2}\text{O}_2 \rightarrow \text{Fe}_2\text{O}_3
\]

\[
K = \frac{\gamma_3 N_3}{\gamma_2^2 N_2^2 P_{\text{O}_2}^{1/2}}
\]

\( N_2, N_3 \) are mole fractions for \( \text{FeO} \) and \( \text{Fe}_2\text{O}_3 \), \( \gamma_2, \gamma_3 \) are activity coefficients. For a regular solution model with interaction parameter, \( \alpha \),

\[
RT \ln \gamma_2 = \alpha N_3^2 \quad (18a)
\]

\[
RT \ln \gamma_3 = \alpha N_2^2 \quad (18b)
\]

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substituting

\[
\ln K = \ln \frac{N_3}{N_2^2 P_{O_2}^{1/2}} - \frac{\alpha}{RT} (2N_3^2 - N_2^2)
\]  

(19)

A plot of \( \ln \left( \frac{N_3}{N_2^2 P_{O_2}^{1/2}} \right) \) versus \( (2N_3^2 - N_2^2) \) at constant temperature should give \( \ln K \) as the intercept and \( \alpha/RT \) as the slope. The data of Darken and Gurry\(^{(92)} \) for liquid iron oxide at different partial pressure oxygen at 1600°C were used. Figure 10 shows that the regular solution model is indeed applicable over the range for \( (2N_3^2 - N_2^2) \) below -0.5. Above this range, the increased concentration of Fe\(^{3+} \) ions causes a deviation from linearity. The failure at high Fe\(^{3+} \) concentration is understandable because Fe\(^{3+} \) can have either octahedral or tetrahedral coordination. Fe\(^{2+} \) ions have octahedral coordination only. This contradicts the basic assumption in the regular solution model that the coordination number be the same. The interaction parameter calculated from the slope is -1082 as compared to -4460 for FeO-Fe\(_{1.5} \).

Application of the regular solution model to a ternary system gives,

\[
RT \ln \gamma_1 = -\alpha_3 N_2 N_3 + (N_2 + N_3) (\alpha_1 N_2 + \alpha_2 N_3)
\]  

(20)

where the \( \alpha \)'s are the interaction parameters for the binaries.

So for the FeO-Fe\(_2O_3\)-SiO\(_2\) system,

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Figure 10. Application of the regular solution model to liquid iron oxide melt at 1600°C.
\[ RT(\ln \gamma_3 - 2\ln \gamma_2) = RT \ln K + 2RT \ln N_2 + \frac{1}{2} RT \ln P_{O_2} - RT \ln N_3 \]
\[ = -\alpha_2 (N_2^2 N_{SiO_2}^2 + 2N_{SiO_2} N_3 + 2N_{SiO_2}^2) + \alpha_3 (N_2 N_{SiO_2} + 2N_{SiO_2} N_3 + N_{SiO_2}^2) + \alpha_1 (N_2^2 + N_{SiO_2} N_2 - 2N_{SiO_2} N_3 - 2N_3^2) \] (21)

Using Turkdogan and Bills's\(^{(93,94)}\) equilibrium compositions, the unknowns in the above equation, \(K, \alpha_2\) and \(\alpha_3\) (with \(\alpha_1\) being -1082), can be calculated by taking sets of equilibrium composition data and solving three simultaneous linear equations. The compositions chosen were those at low \(P_{O_2}\), with low \(Fe^{3+}\) concentration. Still \(\alpha_2\) and \(\alpha_3\) do not converge to any reasonable and consistent values.

Turkdogan and Bills\(^{(93,94)}\) had also compiled the equilibrium compositions of the \(FeO-Fe_2O_3-SiO_2\) system at 1550°C at different \(P_{O_2}\). Their data are recalculated and presented as the \(Fe^{3+}/Fe^{2+}\) ratio as a function of \(P_{O_2}\) at constant silica content (Figures 11, 12 and 13).

Figure 14 gives the approximate location in air of the fractionation curves in the spinel and corundum phase fields of the \(FeO \cdot Fe_2O_3-Al_2O_3-SiO_2\) system, as given by Muan.\(^{(25)}\)

These curves were constructed from the conjugation lines.*

* A conjugation line joins the composition of the melt with the equilibrium composition of the coexisting crystalline phase. It is a tangent to the fractionation curve.
Figure 11. The $\text{Fe}^{3+}/\text{Fe}^{2+}$ ratio in iron silicate melt (at 1550$^\circ$C, $x_{\text{SiO}_2} = 0.1$) as a function of oxygen partial pressure.
Figure 12. The $\frac{Fe^{3+}}{Fe^{2+}}$ ratio in iron silicate melt (at 1550°C, $X'_{SiO_2} = 0.2$) as a function of oxygen partial pressure.
Figure 13. The $\frac{Fe^{3+}}{Fe^{2+}}$ ratio in iron silicate melt (at 1550°C, $x'_{SiO_2} = 0.3$) as a function of oxygen partial pressure.
Figure 14. Fractionation curves in the FeO-Fe₂O₃-Al₂O₃-SiO₂ system, after Muan. (25)
They are instrumental in the calculation of the thermodynamic activities of the system. It is acknowledged that it is difficult to specify the ionic species in the melt. But certain assumptions must be made to express the melt constitution in some convenient form. As short range order is expected to be retained in the melt, the activities of the system are expressed in terms of the FeO, Fe$_2$O$_3$, Al$_2$O$_3$ and SiO$_2$ species.

The standard states referenced are the forms which are stable at the equilibrium temperature and P$_{O_2}$ conditions. They are liquid wustite, hematite(s), magnetite(s), alumina(s) and silica(s) for the calculations here.

The activities of the end members Fe$_3$O$_4$ and FeAl$_2$O$_4$ in iron aluminum spinel have been calculated from the solvus at 700°C. Alcock's experimental results suggest an ideal behavior of the end members at 1300°C. Mason has used the generalized Clausius-Clapeyron equation to develop a cation (Fe$^{2+}$, Fe$^{3+}$ and Al$^{3+}$) mixing scheme on octahedral and tetrahedral sites for an iron aluminum spinel $xFe_3O_4$·(1-$x$)FeAl$_2$O$_4$. He showed that the Fe$_3$O$_4$ and FeAl$_2$O$_4$ activities were complicated, yet very close to composition linearity ($a = x$). Thus the activities FeO, Fe$_2$O$_3$ and Al$_2$O$_3$ in a $xFe_3O_4$·(1-$x$)FeAl$_2$O$_4$ spinel can be calculated as follows.

From the reactions,
\(3\text{FeO(\ell) + 1/2O}_2(g) \rightleftharpoons \text{Fe}_3\text{O}_4(s)\) \hspace{1cm} \(\Delta G^o_1 = -102,550 + 46.9T\ \text{cal}^{(98)}\)

\[K_1 = \frac{a_{\text{Fe}_3\text{O}_4}}{a_{\text{FeO}} a_{\text{Po}_2}^{1/2}}\] (22)

\(3\text{Fe}_2\text{O}_3(s) \rightleftharpoons 2\text{Fe}_3\text{O}_4(s) + 1/2\text{O}_2\) \hspace{1cm} \(\Delta G^o_2 = 59,800 - 33.55T\ \text{cal}^{(98)}\)

\[K_2 = \frac{a_{\text{Fe}_3\text{O}_4}^2 a_{\text{Po}_2}^{1/2}}{a_{\text{Fe}_2\text{O}_3}^2}\] (23)

\(\text{FeO(\ell) + Al}_2\text{O}_3(s) \rightleftharpoons \text{FeAl}_2\text{O}_4(s)\) \hspace{1cm} \(\Delta G^o_3 = -14855 + 2.14T^{(99)} + 0.5T\ln T\ \text{cal}\)

\[K_3 = \frac{a_{\text{FeAl}_2\text{O}_4}}{a_{\text{FeO}} a_{\text{Al}_2\text{O}_3}}\] (24)

one obtains,

\[a_{\text{FeO}} = 3 \sqrt{\frac{K_1 a_{\text{Po}_2}^{-1/2}}{x_{\text{Fe}_3\text{O}_4}}}\]

\[a_{\text{Fe}_2\text{O}_3} = 3 \sqrt{\frac{a_{\text{Po}_2}^{1/2} K_2^{-1} x_{\text{Fe}_3\text{O}_4}^2}{}}\]

\[a_{\text{Al}_2\text{O}_3} = \frac{(1 - x_{\text{Fe}_3\text{O}_4})}{K_3 a_{\text{FeO}}}\]

In the spinel primary phase field where the iron aluminum spinel is in equilibrium with the melt,

\(\mu_{\text{FeO}}^{\text{melt}} = \mu_{\text{FeO}}^{\text{spinel}}\)

\(\mu_{\text{Fe}_2\text{O}_3}^{\text{melt}} = \mu_{\text{Fe}_2\text{O}_3}^{\text{spinel}}\)

\(\mu_{\text{Al}_2\text{O}_3}^{\text{melt}} = \mu_{\text{Al}_2\text{O}_3}^{\text{spinel}}\)
Figures 15, 16 and 17 are the isothermal activities versus mole fraction plots for Fe$_2$O$_3$, FeO and Al$_2$O$_3$. Several observations can be made. FeO deviates negatively whereas Fe$_2$O$_3$ positively from Raoultian behavior, just as in the case of FeO-Fe$_2$O$_3$-SiO$_2$. They both tend towards ideal behavior at higher temperatures according to the sign of the partial molar heat of solution. The silica content also decreases towards higher temperature, $x_{\text{SiO}_2}$ varies from 0.245 to 0.261 at 1500°C and from 0.09 to 0.162 at 1575°C. Also included in Figures 15 and 16 are the curves A and B. Curve A corresponds to the activities in iron silicates at 1550°C and $x_{\text{SiO}_2} = 0.4$. Curve B is for the FeO-Fe$_2$O$_3$-CaO system also at 1550°C and $x_{\text{CaO}} = 0.4$. The FeO activities suggest that the interactions of divalent iron cations and silicate anions are less in the iron aluminosilicates than in the iron silicates.

Along each isothermal activity curve, the amount of Al$_2$O$_3$ in the melt varies from $x_{\text{Al}_2\text{O}_3} = 0.05$ to as high as 0.3. The silica content decreases only slightly towards higher $x_{\text{FeO}}$ and $x_{\text{Fe}_2\text{O}_3}$. The large variations of Al$_2$O$_3$ content seem to have minimal effect on the activities of FeO and Fe$_2$O$_3$. It is interesting to note that, as illustrated in Figure 17, Al$_2$O$_3$ obeys Henry's law for dilute solutions. The isothermal activity coefficients are 3.048 (at 1600°C), 3.431 (at 1550°C) and 4.109 (at 1500°C). In the following section, the effect of additions of Al$_2$O$_3$ on the Fe$^{3+}$/Fe$^{2+}$
Figure 15. Isothermal activities of \( \text{Fe}_2\text{O}_3 \) in iron aluminosilicate melt.
Figure 16. Isothermal activities of FeO in iron aluminosilicate melt.
Figure 17. Isothermal activities of Al$_2$O$_3$ in iron aluminosilicate melt.
equilibrium in iron aluminosilicate is discussed.

III.2. Justification for Using an Alumina Crucible as the Conductivity Cell.

At first glance the use of an alumina container for the silica melt at high temperatures seem to be a poor choice, especially for compositions with high iron content. In the spinel primary phase field, the melt is unsaturated with $\text{Al}_2\text{O}_3$ leading to the dissolution of the crucible and changing the overall composition of the melt. However, the following facts help affirm that the choice is legitimate.

$\text{Al}_2\text{O}_3$ acts as an amphoteric oxide and can be ionized as either

$$\text{Al}_2\text{O}_3 \rightleftharpoons 2\text{Al}^{3+} + 3\text{O}^{2-} \quad (25)$$

or

$$\text{Al}_2\text{O}_3 + 3\text{O}^{2-} \rightleftharpoons 2\text{AlO}_3^3- \quad (26)$$

Larson and Chipman\textsuperscript{(100)} discovered that $\text{Al}_2\text{O}_3$ was neutral to an iron oxide melt and addition of up to 8 mole% $\text{Al}_2\text{O}_3$ at 1550°C and $P_{\text{O}_2} = 9.968 \times 10^{-6}$ atm did not affect the $\text{Fe}^{3+}/\text{Fe}^{2+}$ ratio in the melt. Muan\textsuperscript{(25)} in his phase equilibria study also noted that $\text{Al}_2\text{O}_3$ has very little effect on the $\text{Fe}^{3+}/\text{Fe}^{2+}$ ratio in $\text{Fe}_2\text{O}_3$-$\text{Al}_2\text{O}_3$-$\text{SiO}_2$ melts. In addition a number of workers\textsuperscript{(101,102)} have studied the oxidation state of iron in $\text{Na}_2\text{O}$-$\text{SiO}_2$ melts with very low iron content. Johnston\textsuperscript{(101)} used an alumina crucible to hold the glassy
melt. He reported the excessive dissolution of the crucible induced a contamination of 30 wt% Al$_2$O$_3$ in the melt composition at 1450°C. Even this, he said, did not affect the nature of the Fe$^{3+}$/Fe$^{2+}$ oxidation-reduction equilibrium. The slope of log (Fe$^{3+}$/Fe$^{2+}$) versus log $P_{O_2}$ remained constant.

Because of the Henrian behavior of Al$_2$O$_3$ in the melt and the interesting phenomena stated above, the Fe$^{3+}$/Fe$^{2+}$ ratios in iron aluminosilicates obtained by Muan(25) are reanalyzed. A new parameter $x'_{SiO_2}$ is defined,

$$x'_{SiO_2} = \frac{x_{SiO_2}}{x_{FeO} + x_{Fe_2O_3} + x_{SiO_2}} \quad (27)$$

For iron silicates,

$$x'_{SiO_2} = x_{SiO_2}$$

Figure 18 is a plot of Fe$^{3+}$/Fe$^{2+}$ as a function of $x'_{SiO_2}$ for both iron aluminosilicate and iron silicate at different temperatures and $P_{O_2}$. The solid symbols represent the independent data for iron silicates from White(103), Turkdogan and Bills(93) and Larson and Chipman(100). The open symbols are the reanalyzed data in the spinel primary phase field of FeO·Fe$_2$O$_3$-Al$_2$O$_3$-SiO$_2$.

From the agreement between the different sets of data, the Fe$^{3+}$/Fe$^{2+}$ ratio in FeO·Fe$_2$O$_3$-Al$_2$O$_3$-SiO$_2$ melt can be represented by that in iron silicate under the same equilibrium.
Figure 18. Comparison of Fe$^{3+}$/Fe$^{2+}$ ratios in FeO-Fe$_2$O$_3$-SiO$_2$ and FeO·Fe$_2$O$_3$-Al$_2$O$_3$-SiO$_2$ systems.

The graph shows the variation of Fe$^{3+}$/Fe$^{2+}$ ratios with $X'_\text{SiO}_2$ at different temperatures and oxygen pressures. The expression for $X'_\text{SiO}_2$ is given as:

$$X'_{\text{SiO}_2} = \frac{X_{\text{SiO}_2}}{X_{\text{FeO}^+} + X_{\text{Fe}_2\text{O}_3} + X_{\text{SiO}_2}}$$

The data points are marked with different symbols for different oxygen pressures and temperatures. The Fe-Al-O melt (up to 8 m/o Al$_2$O$_3$) is also indicated on the graph.
conditions. The typical $\text{Fe}^{3+}/\text{Fe}^{2+}$ versus $P_\text{O}_2$ at constant $x_\text{SiO}_2$ curves (Figures 11-13) are useful in predicting the $\text{Fe}^{3+}/\text{Fe}^{2+}$ equilibrium.

Unfortunately, the $\text{Al}_2\text{O}_3$ behavior is fortuitous, it is yet to be associated with its solution thermodynamics in the melt. Nevertheless, despite the complexity of the system, it is shown that the thermodynamic activities of the oxide species can be determined from the phase equilibria data.

To make sure that the dissolution of the alumina crucible did not affect the overall composition of the melt drastically, a sample composition of $73\text{Fe}_3\text{O}_4-20\text{Al}_2\text{O}_3-7\text{SiO}_2$ (a sample with the highest iron content in this study) was melted and held at 1600°C for 15 hours. Chemical analysis* showed that the $\text{Fe}/(\text{Fe} + \text{Al})$ ratio changed from 0.689 to 0.640, an increase in about 5.2 wt% $\text{Al}_2\text{O}_3$ in the composition.

*Analysis done by Arnold Greene Testing Lab., Inc. Natick, Mass. 01760.
Chapter IV. Research Objectives

The aim of this study was to determine the electrical conductivities in the FeO·Fe₂O₃·Al₂O₃·SiO₂ system, with low silica content, in the solid and molten states. To achieve this goal, the following tasks were proposed:

1. To characterize the electrical conductivity in air as a function of composition and of temperature.
2. To measure the ac- and dc-conductivities to identify the electronic and ionic contribution to total conductivity.
3. To measure the dependence of electrical conductivity on oxygen partial pressure and compare the results with those of other silicate systems.
4. To determine the correlation between the conductivity and the phase equilibria of the system.
5. To identify the conduction mechanism in iron alumino-silicate melt and to interpret the conductivity results in the solid state in terms of multiphase conduction.
Chapter V. Experimental Procedures

This chapter deals with the different facets involved in the collection of experimental data. First, the method of sample preparation is discussed. Following is the description of the conductivity cell design and the actual experimental setup for measurement. A precise control of the oxygen partial pressure is also crucial to the accuracy of the work. Towards the end of this chapter, the techniques used to gather supportive evidence for the interpretation of the results is documented.

V.1.1. Sample Preparation

The objective was to prepare homogeneous batches of powder compositions in a convenient way without introducing excessive contamination. Originally, homogeneity was achieved by melting and remelting weighed portions of FeO·Fe$_2$O$_3$, Al$_2$O$_3$ and SiO$_2$ powders in a platinum crucible. Unfortunately, this method was tedious and expensive. The following method proved to be much superior.

150-200 gm batches of powder mixtures were processed at one time. The starting materials used were FeO·Fe$_2$O$_3$ (Fisher Scientific Company, purified grade), Al$_2$O$_3$ (Alcoa XA-139, super ground, 99.95% purity, Table I) and SiO$_2$ (Research Organic/Inorganic Chemical Corp, 0325 mesh, 99.89% purity). Exact proportions of these powders were weighed out
XA-139 high purity $\text{Al}_2\text{O}_3$ is a fine crystalline (less than 1 $\mu$m) $\text{Al}_2\text{O}_3$. The following are typical values for lots that have been analyzed.

<table>
<thead>
<tr>
<th></th>
<th>wt%</th>
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</thead>
<tbody>
<tr>
<td>$\text{SiO}_2$</td>
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</tr>
<tr>
<td>$\text{Fe}_2\text{O}_3$</td>
<td>.007–.011</td>
</tr>
<tr>
<td>$\text{TiO}_2$</td>
<td>.001</td>
</tr>
<tr>
<td>$\text{Na}_2\text{O}$</td>
<td>.005–.01</td>
</tr>
<tr>
<td>$\text{CaO}$</td>
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<td>$\text{Ga}_2\text{O}_3$</td>
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</tr>
<tr>
<td>$\text{B}_2\text{O}_3$</td>
<td>.001</td>
</tr>
<tr>
<td>$\text{MnO}$</td>
<td>.0006</td>
</tr>
<tr>
<td>$\text{Cr}_2\text{O}_3$</td>
<td>.0002</td>
</tr>
<tr>
<td>$\text{MgO}$</td>
<td>.002</td>
</tr>
<tr>
<td>$\text{ZnO}$</td>
<td>.0005</td>
</tr>
<tr>
<td>$\text{CuO}$</td>
<td>.0005</td>
</tr>
<tr>
<td>$\text{V}_2\text{O}_5$</td>
<td>.0001</td>
</tr>
<tr>
<td>$\text{Al}_2\text{O}_3$</td>
<td>99.95+</td>
</tr>
</tbody>
</table>
on a Mettler balance, put into a 32 oz. plastic bottle and tumbled overnight. The powder mixture was then pressed into pellets 1-1\(\frac{1}{2}\)" long using a 7\(\frac{7}{8}\)" diameter steel die. They were sintered in a bottom loading type furnace with silicon carbide heating elements, built specifically for this purpose. The sintering temperature was usually 1200°C. The sintered pellets were then pulverized on a steel plate and ball-milled with \(\frac{3}{4}\)-5/16" diameter steel balls. The resulting fine powder was sieved and repressed into pellets. The above process was repeated two to three times to assure homogeneity.

Eight of the mixtures were analyzed wet chemically. The chemical analysis results were in wt% Fe, Al and Si. The corresponding wt% Fe\(_3\)O\(_4\), Al\(_2\)O\(_3\) and SiO\(_2\) were calculated and compared with the original composition in Table II. The generally lower silica content in the final powder was because, in the tumbling of the original mixture, the silica powder tends to adhere to the bottle. The pick up of iron during the ball-milling seemed to be negligible. These results showed that the method could produce fine homogenized powders with final compositions close to the original, as-mixed values.

V.1.2. Conductivity Cell: Design and Calibration

The conductivity cell consisted of a 5 c.c. alumina crucible, a tube, a crucible cover and two platinum electrodes. A typical sample cell design is shown in Figure 19. A platinum crucible could not be used because the melt was
Figure 19. Schematic of the conductivity cell design.
drawn over its sides. Also, in a reducing atmosphere, iron alloyed with platinum.

In Figure 19, A is the alumina crucible cover with its center cored so that the 1" long alumina tube B (1/4" I.D., 3/8" O.D.) can fit through. The particular shape of A is to facilitate filling the cell with powder and to allow for ample gaseous exchange between the melt and the furnace atmosphere. Two 40 mil clearance holes were machined on A and B for the positioning of the platinum electrodes, (27 mil diameter wire), C. The cover, tube and the electrodes were secured using high temperature curing alundum cement with polyvinyl acetate binder. The electrodes were maintained at a distance of ~3mm apart. As a result, the conductivity chamber was limited to the enclosure of the Al$_2$O$_3$ tube. This two-point probe arrangement was used instead of the four-point technique in view of the relatively high conductivity of the system (0.1 ohm$^{-1}$cm$^{-1}$). Preliminary results also indicated that the difference between the two methods was insignificant.

The cell constant of each conductivity cell was obtained by calibrating with two KCl solutions of different normality (0.04922N, 0.0216N, 0.0108N or 0.024N). Chiu$^{104}$ has reported the ac-conductivity of KCl in the range of .005-1.0N. The ac-conductance C(d) of the cell with KCl solution filled to a distance, d, from the top was measured at 95KHz at room
TABLE II

Wet Chemical Analysis of FeO·Fe₂O₃·Al₂O₃·SiO₂ Samples.

<table>
<thead>
<tr>
<th>Original Composition (wt%)</th>
<th>Analyzed Composition (wt%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fe₃O₄</td>
<td>Al₂O₃</td>
</tr>
<tr>
<td>1</td>
<td>23.0</td>
</tr>
<tr>
<td>2</td>
<td>33.0</td>
</tr>
<tr>
<td>3</td>
<td>43.0</td>
</tr>
<tr>
<td>4</td>
<td>63.0</td>
</tr>
<tr>
<td>5</td>
<td>73.0</td>
</tr>
<tr>
<td>6</td>
<td>33.0</td>
</tr>
<tr>
<td>7</td>
<td>43.0</td>
</tr>
<tr>
<td>8</td>
<td>53.0</td>
</tr>
</tbody>
</table>
The cell constant $K'(d)$ was calculated with the equation,

$$K'(d) = \sigma/C(d) \quad \text{(27)}$$

The distance, $d$, was measured by studying the water mark left on the alumina tube by the KCl solution. A typical plot of the cell constant as a function of $d$ is shown in Figure 20. It shows excellent agreement in the cell constant values obtained by using two different solutions. The cell constants obtained for all the conductivity cells were consistently in the same range of values.

The conductivity cell was filled with the powder composition and the whole assemblage cemented to the end of a cell holder consisting of two 30" long four-bore alumina thermocouple rods fixed to a brass end-cap. 14 mil platinum wires were used as leads. A platinum-platinum-10% Rodium thermocouple was positioned right next to the cell for temperature measurements.

In some instances, specimens in the form of rectangular bars (typically 2x 2 x 15 mm) were cut out of melted samples. The conductivity of these specimens was measured using 8 mil platinum wires as electrodes in a four-point method. Platinum paste was added to ensure good contact. The cross-sectional area, $A$, of the specimen was measured by a micrometer and the distance, $\Delta l$, between the voltage probes was measured with a cathetometer. The conductivity was,

$$\sigma = \frac{A}{\Delta l} \cdot \frac{1}{R} \quad \text{(28)}$$
Figure 20. Cell constant as a function of liquid level in the conductivity cell.
V.2.1. Electrical Conductivity Measurement

In the dc-conductivity measurements, a 1 1/2 volt battery was used to apply the current through the conductivity cell. The current was measured by a Keithley model 160 multimeter in series. The voltage drop between the electrodes was recorded by a Keithley model 160B multimeter with input impedance of 10 mega ohm. A variable resistor was inserted to increase the total load.

The ohmic I-V characteristic of the conductivity cell is shown in Figure 21.

A Princeton Applied Science model 124A Lock-in-amplifier (LIA) was used for the ac measurement. The frequency range studied was from 1 to 10KHz. A constant current source was generated from the reference signal from the LIA (Figure 22) and passed through the sample. The voltage drop between the electrodes was first attenuated and measured by the LIA.

To alleviate the noise and interference from the furnace current and the other electrical instruments, the power to the LIA was supplied through a Sola type CVS constant voltage transformer.

An instrument panel was constructed with the capability to measure four samples simultaneously. This switching panel was designed such that while the conductivity was taken of one sample, the other three were isolated from the circuit.

The conductivity cell was placed in a molybdenum wire wound hydrogen furnace with an alumina muffle. The conduct-
Figure 21. I-V characteristic of the conductivity circuit at 1347°C.
Figure 22. Circuit of the voltage controlled current source.
ivity was measured after the sample was equilibrated at different temperatures. The time of equilibration depended on the temperature. It varied from a minimum of three hours for samples with high iron content to over 10 hours for those with less iron.

The temperature range for this conductivity study was between 1000° and 1600°C. The sample was either a melt, melt plus solid or multiphase solid.

The conductivity dependence of samples with compositions in the spinel primary region as a function of furnace oxygen partial pressure was studied at 1550°C and 1600°C. The atmosphere control of the furnace is described in the following section.

V.2.2. Oxygen Partial Pressure Control

The variation of equilibrium oxygen partial pressure in the furnace atmosphere was achieved via pre-determined flow ratios of Ar/O₂ and CO/CO₂ gaseous mixtures. Ar/O₂ mixtures were used for the oxygen partial pressure range of 1-10⁻³ atmosphere. The highest oxygen partial pressure attained with the CO/CO₂ mixture in the flow system was on the order of 10⁻⁵ atmosphere. The lowest partial pressure used was of the order of 10⁻⁹ atmosphere.

Before they entered the furnace, the gases were scrubbed of their water content by passing through columns of drierite and anhydrole. Ascarite was installed in the CO gas train
to absorb any trace of CO$_2$. Copper wire screens maintained at 450°C served as oxygen scrubbers for the Ar, CO and CO$_2$ gases. The flow volume of each gas was controlled by calibrated flowmeters to achieve a linear flow rate of about 1 cm/sec in the furnace.

The oxygen partial pressure in the furnace was determined by a calcia-stabilized zirconia cell located at the outlet of the furnace. The cell was maintained at 832°C. For the Ar/O$_2$ mixture, the induced emf of the cell gave the precise oxygen partial pressure. For CO/CO$_2$ mixtures the equilibrium oxygen partial pressure was controlled by the reaction,

$$2\text{CO}(g) + \text{O}_2(g) \rightarrow 2\text{CO}_2(g) \quad \Delta G^\circ = -135,000 + 41.5T \text{ Kcal}$$

The induced emf then gave the precise CO/CO$_2$ ratio from which the oxygen partial pressure at the furnace temperature could be calculated using the thermodynamic data for the above equation.

V.2.3. Experimental Error

The maximum error limit obtained in the conductivity results was less than 10%. The confidence in the accuracy of the measurement in the present study was established on the following grounds.

Repetitive measurement on different samples with the same batch composition produced conductivity data that were consistently within 10% of each other. Secondly, the ac-
conductivity which was measured in a different circuit was equivalent to the dc value. Also, the repeated melting, solidification, remelting and resolidification of the same sample gave reproducible results in both the solid and molten state. Finally, the reproducibility of the results was demonstrated by the agreement in the results obtained from a solid conductivity cell sample and a rectangular specimen.

While no error bars were drawn together with the presentation of results in Chapter VI, this error limit should be noted.

V.2.4. Identification and Characterization of Phases

This is a very important part of the present study. As the iron aluminosilicate melt solidified to form a multi-phased agglomerate of either spinel, corundum, mullite and/or glass, the ability to identify the phases, and to characterize their compositions and volume fractions aided the analysis of the conductivity results.

Powders of each composition were melted and equilibrated in air at a specific temperature. The sample was then quenched in liquid nitrogen. Identification of the phases present in the quenched samples was done by the Debye-Scherrer x-ray diffraction method with an iron target. However, the lack of sufficient high angle peaks for the spinel structure led to the conclusion that this technique alone was unsuitable for a precision lattice parameter determination.
A powder x-ray diffraction pattern was obtained on a Norelco diffractometer with a Cu tube and a LiF monochromator. The precise 2θ values of the (333) and (440) diffractions of iron aluminum spinel were determined, using the internal standard silicon (311) peak (2θ = 56.122°) as a reference. The 2θ values for the same diffraction peaks of the end members, magnetite and hercynite, and of the iron aluminum spinel were determined experimentally.

A linear relationship was assumed to exist between the 2θ values and the spinel composition. To calculate the wt% of FeAl₂O₄ in the spinel, the following expressions were used.

\[
\text{wt}\% \text{ FeAl}_2 \text{O}_4 = \frac{2\theta - 56.84}{0.0206} \quad \text{for (333) peaks (29a)}
\]

\[
\text{wt}\% \text{ FeAl}_2 \text{O}_4 = \frac{2\theta - 62.42}{0.0232} \quad \text{for (440) peaks (29b)}
\]

The compositions of the corundum, mullite, spinel and glassy regions were also measured by an electron probe microanalyzer. The results on the spinel phase provided a good check for the above x-ray diffraction method. The compositions of the standards used were listed in Table III.

Volume fractions of different phases were obtained by point-counting on micrographs taken of representative areas. The different phases were readily recognizable without any etchant.
TABLE III
Standards Used for Composition Analysis in the M.I.T. Earth and Planetary Electron Microscopy Facility.*

Cossyrite - standard for Si

<table>
<thead>
<tr>
<th>Element</th>
<th>Standard Oxide Composition (wt%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Na</td>
<td>6.928</td>
</tr>
<tr>
<td>Si</td>
<td>40.922</td>
</tr>
<tr>
<td>Ti</td>
<td>8.706</td>
</tr>
<tr>
<td>Fe</td>
<td>40.971</td>
</tr>
</tbody>
</table>

Mn Ilmenite - standard for Fe

<table>
<thead>
<tr>
<th>Element</th>
<th>Standard Oxide Composition (wt%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mg</td>
<td>0.2486</td>
</tr>
<tr>
<td>Ti</td>
<td>51.611</td>
</tr>
<tr>
<td>Mn</td>
<td>1.496</td>
</tr>
<tr>
<td>Fe</td>
<td>45.413</td>
</tr>
</tbody>
</table>

Enstatite Al 2O - standard for Al

<table>
<thead>
<tr>
<th>Element</th>
<th>Standard Oxide Composition (wt%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mg</td>
<td>32.12</td>
</tr>
<tr>
<td>Al</td>
<td>19.98</td>
</tr>
<tr>
<td>Si</td>
<td>47.87</td>
</tr>
</tbody>
</table>

* Materials Analysis Corporation Model 5 Automated electron microprobe.
Chapter VI. Experimental Results

VI.1. Introduction

The results of the present study are presented in two main sections. The first part consists of the dc- and ac-conductivities in air as a function of temperature for different compositions (with 7 or 17 w/o SiO₂). The second half of this chapter deals with the isothermal dc-conductivity of silicate melts at 1550°C and 1600°C as a function of oxygen partial pressure.

The results in air are again divided into categories according to the original sample composition and the phase chemistry. Figure 23 shows the locations of the compositions that are investigated. The compatibility triangle s₁c₁m₁ corresponds to the compositions of the spinel, corundum and mullite phases in equilibrium with a silicate melt of composition P at 1460°C. A second compatibility triangle is SiO₂-s₂-m₂. It is composed of spinel, mullite and tridymite compositions co-existing with the melt of composition E at 1380°C.

Then the data in the first section is organized into the following four categories. The first includes samples which form crystallization products with a glassy matrix. They are the compositions within the compatibility triangle SiO₂-s₂-m₂. The second group consists of samples which have mullite as the matrix of the final crystalline composite. The majority of the compositions studied fit this description.
Figure 23. Location of the compositions investigated (with 7 and 17 wt% SiO₂) with respect to the FeO·Fe₂O₃-Al₂O₃-SiO₂ system.
They are further separated into two sub-divisions; those that are within the quadrilateral \( s_1 s_2 m_2 m_1 \) and the ones inside the compatible triangle \( s_1 c_1 m_1 \). One other composition inside \( s_1 c_1 m_1 \) produced a solid assemblage with a corundum matrix. Its conductivity-temperature relationship is recorded individually. The last category of the results in air is the conductivity of iron aluminosilicate melts. The graphical presentation is then by means of a plot of 

\[
\sigma T/c(l-c) \text{ versus reciprocal temperature, where } c \text{ is the } Fe^{3+}/Fe_{\text{total}} \text{ ratio.}
\]

Any results available from electron microanalysis and x-ray diffraction studies are also introduced in conjunction with the conductivity data. The ac-conductivity for compositions containing more than 33 wt% \( Fe_3O_4 \) is essentially equivalent to the dc values, indicating the predominantly electronic nature of the conduction process.

The chapter ends with the consideration of the isothermal dc-conductivity of silicate melts as a function of oxygen partial pressure and of \( Fe^{3+}/Fe_{\text{total}} \).

VI.2. Conductivities in Air as a Function of Temperature


Three compositions that were studied fell into this category. They were 73\( Fe_3O_4 \)-20\( Al_2O_3 \)-7\( SiO_2 \), 63\( Fe_3O_4 \)-20\( Al_2O_3 \)-17\( SiO_2 \), and 33\( Fe_3O_4 \)-30\( Al_2O_3 \)-17\( SiO_2 \) (in wt%). Their iso-
silica-alumina lines intersect the \( \text{FeO} \cdot \text{Fe}_2\text{O}_3 \cdot \text{Al}_2\text{O}_3 \cdot \text{SiO}_2 \) plane within the composition triangle \( \text{SiO}_2-s_2-m_2 \) (Figure 23). Of these three, the main research effort was concentrated on the composition 73F-20A-7S.*

Figure 24 gives the conductivity data in air versus reciprocal temperature for a sample of 73F-20A-7S. The temperature ranged from 1550°C to 1024°C. The conductivity value at 1550°C was 0.237 ohm\(^{-1}\) cm\(^{-1}\) which was obtained by averaging the results of four different runs. Figure 24 shows that the conductivity, while being somewhat insensitive to temperature, increased with decreasing temperature. It also did not show any discontinuity upon complete solidification of the sample. From such a plot, no simple relationship between conductivity and temperature could be derived. The equilibration time permitted between data points was 5-6 hours. At \( o_1 \) and \( o_2 \), the sample was held overnight (16 hours). \( o_1 \) was at 1365°C. For the phase diagram, it was apparent that the last liquid of this sample composition disappeared near 1390°C.

Similar behavior was exhibited by samples of 63F-20A-17S and 53F-30A-17S (Figures 25 and 26). Likewise, the curves could not be fitted by a simple linear relationship versus reciprocal temperature.

* The following abbreviations are used: \( F = \text{Fe}_3\text{O}_4 \), \( A = \text{Al}_2\text{O}_3 \), and \( S = \text{SiO}_2 \). Numbers are expressed in weight %.
Temperature dependence of the electrical conductivity of composition $73\text{Fe}_3\text{O}_4-20\text{Al}_2\text{O}_3-7\text{SiO}_2$.

Figure 24.
Figure 25. Temperature dependence of the electrical conductivity of composition $53\text{Fe}_3\text{O}_4-30\text{Al}_2\text{O}_3-17\text{SiO}_2$. 

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Figure 26. Temperature dependence of the electrical conductivity of composition $63\text{Fe}_3\text{O}_4-20\text{Al}_2\text{O}_3-17\text{SiO}_2$. 
The same data are, in Figure 24, plotted as the product (conductivity x temperature) versus reciprocal temperature. The data below 1390°C were fitted with a linear relationship and an apparent activation energy of 0.0584eV was obtained.

The following experiments were carried out to affirm that this behavior which was observed for all the samples of this composition was not spurious. One sample was held at 1360°C for over 80 hours. The conductivity remained constant throughout the whole period. In another case, a sample was first quenched from 1540°C to 1200°C in 15 minutes. It was then re-annealed at 1355°C for 20 hours and then cooled. The data were reproduced.

The conductivity remained between 0.2-0.3 ohm\(^{-1}\)cm\(^{-1}\) over a wide temperature range. To look at the effect of temperature on the conductivity, a sample was melted and the data taken from 1550°C down to 210°C. The results are plotted in Figure 27. The difference in conductivity between 270°C and 1550°C, where the sample was a melt with one-third volume fraction of spinel \(\text{Fe}_3\text{O}_4-3\text{FeAl}_2\text{O}_4\), was merely a factor of 3.42. Above 600°C, the conductivity increased with decreasing temperature. The opposite effect was observed for temperatures below 600°C. Also superimposed on the same plot, but on a different scale, was the product of (conductivity x temperature). A bend occurred near 600°C resulting in a higher activation energy for the low temperature region.
Figure 27. Electrical conductivity as a function of temperature for composition \(73\text{Fe}_3\text{O}_4-20\text{Al}_2\text{O}_3-7\text{SiO}_2\).
Figure 28 is a micrograph of a sample quenched from 1526°C. It illustrates that the equilibrium phases at 1526°C in air are spinel and melt. The spinel composition was determined as 55.97Fe$_2$O$_4$-43.76FeAl$_2$O$_4$ (in wt%). The dendritic structure was the spinel crystallites formed during quenching.

It was predicted that such a composition would give a crystalline mixture of spinel, tridymite and mullite as it solidified. However, a careful study of a sample melted at 1550°C, slowly cooled until 1250°C where it was held for 24 hours showed that the situation was not that unambiguous.

Figure 29 shows the final microstructure. Grain growth has occurred for the spinel phase during the annealing at 1250°C. The optical micrograph indicated that the large spinel grains were separated by interconnecting regions. X-ray fluorescence study confirmed that these areas were rich in silica. The electron microanalysis results were 58.74Fe$_2$O$_4$-39.92FeAl$_2$O$_4$ for spinel and 7.05FeO 21.56Al$_2$O$_3$ 69.13SiO$_2$ for the matrix with the SiO$_2$ content ranging from 53.54 to 76.27 wt%. The huge variation in the analysis of the silica-rich region reflected its homogeneity.

The volume fraction occupied by this silica-rich region was 26.1%, calculated by point counting. The Debye-Scherrer diffraction pattern failed to show any trace of mullite and silica (Table IV). The only diffraction peaks obtained were those from spinel. Electron microprobe data gave 58.74Fe$_2$O$_4$-39.92FeAl$_2$O$_4$ as the only spinel composition. However, x-ray diffraction results provided additional information. At least three
Figure 28. Microstructure of a sample of composition $73 \text{Fe}_3\text{O}_4 - 20\text{Al}_2\text{O}_3 - 7\text{SiO}_2$ quenched from $1526^\circ\text{C}$. (Magnification 200X)
Figure 29. The microstructure of a sample of composition $73\text{Fe}_3\text{O}_4-20\text{Al}_2\text{O}_3-7\text{SiO}_2$ annealed in air at 1250°C for 24 hours. (Magnification 50x)
TABLE IV

X-ray diffraction pattern for $73\text{Fe}_3\text{O}_4 -20\text{Al}_2\text{O}_3 -7\text{SiO}_2$
melted and held at $1250^\circ\text{C}$ for 24 hours, with Fe x-ray, 
MnO filter.

<table>
<thead>
<tr>
<th>$2\theta^\circ$</th>
<th>$d$ (Å)</th>
<th>Intensity</th>
<th>Assignment (spinel) (hk1)</th>
</tr>
</thead>
<tbody>
<tr>
<td>39.22°</td>
<td>2.884</td>
<td>MW</td>
<td>220</td>
</tr>
<tr>
<td>43.56°</td>
<td>2.609</td>
<td>VVW</td>
<td></td>
</tr>
<tr>
<td>46.24°</td>
<td>2.465</td>
<td>S</td>
<td>311</td>
</tr>
<tr>
<td>48.46°</td>
<td>2.359</td>
<td>VVW</td>
<td></td>
</tr>
<tr>
<td>56.58°</td>
<td>2.042</td>
<td>MW</td>
<td>400</td>
</tr>
<tr>
<td>70.67°</td>
<td>1.674</td>
<td>VW</td>
<td>422</td>
</tr>
<tr>
<td>75.46°</td>
<td>1.582</td>
<td>M</td>
<td>511</td>
</tr>
<tr>
<td>82.02°</td>
<td>1.475</td>
<td>S</td>
<td>440</td>
</tr>
<tr>
<td>99.25°</td>
<td>1.271</td>
<td>VW</td>
<td>533, 622</td>
</tr>
<tr>
<td>126.7°</td>
<td>1.083</td>
<td>VW</td>
<td>642</td>
</tr>
<tr>
<td>137.25°</td>
<td>1.039</td>
<td>VW</td>
<td>553, 731</td>
</tr>
</tbody>
</table>
Figure 30. Isothermal ac-conductivity as a function of frequency for composition $73\text{Fe}_3\text{O}_4-20\text{Al}_2\text{O}_3-7\text{SiO}_2$. 
different compositions of spinel were measured: 48.14Fe$_3$O$_4$-51.86FeAl$_2$O$_4$, 63.8Fe$_3$O$_4$-36.2FeAl$_2$O$_4$ and 93.99Fe$_3$O$_4$-5.01FeAl$_2$O$_4$.

The ac-conductivities in the range of 1-10 KHz were equivalent to the dc data, within experimental limits. Figure 30 compares the results at 1528°C, 1421°C, 1258°C and 1229°C of composition 73F-20A-7S. The ac-conductivities for compositions 63F-20A-17S and 53F-30A-17S were also independent of frequency in the above frequency range.

VI.2.2. Compositions with Mullite as the Matrix Phase of the Multi-Phased Crystallization Product.

Most of the compositions studied fell into this category. The compositions were 63Fe$_3$O$_4$-30Al$_2$O$_3$-7SiO$_2$, 58Fe$_3$O$_4$-35Al$_2$O$_3$-7SiO$_2$, 53Fe$_3$O$_4$-40Al$_2$O$_3$-7SiO$_2$, 48Fe$_3$O$_4$-45Al$_2$O$_3$-7SiO$_2$, 46Fe$_3$O$_4$-47Al$_2$O$_3$-7SiO$_2$, 43Fe$_3$O$_4$-50Al$_2$O$_3$-7SiO$_2$, 33Fe$_3$O$_4$-60Al$_2$O$_3$-7SiO$_2$, 43Fe$_3$O$_4$-40Al$_2$O$_3$-17SiO$_2$, and 33Fe$_3$O$_4$-50Al$_2$O$_3$-17SiO$_2$. These can be further split into two groups according to the microstructure of their crystallization products. The first group was those of the compositions inside the quadrilateral $s_1s_2m_2m_1$ in Figure 23. For them, the corundum phase began to be resorbed at 1460°C. The microstructure then showed spinel grains in a mullite matrix together with amounts of the remnant corundum phase. The second consisted of those of the above compositions that lie inside the triangle $s_1m_1c_1$ in Figure 23. Their crystallization product formed from the molten state was
a three phase mixture of spinel and corundum grains in a mullite matrix.

Typically, the conductivity dependence on temperature for these compositions displayed a three-stage behavior. At high temperature (region I) where the equilibrium phases were the melt with a suspension of crystalline phase(s), the conductivity had a slight dependence on temperature. The third region (region III) was the conduction through the mullite matrix at low temperature. The conductivity measured was an effective one which depended on the volume fractions of the spinel, corundum and mullite present. The thermal activation energy varied according to the composition of the mullite phase. An intermediate transition region, where the conductivity underwent a sharp discontinuous change, separated regions I and III.

These two groups will now be treated separately.

a) Compositions within the area $s_1 s_2 m_2 m_1$

The compositions included under this heading were

$63\text{Fe}_3\text{O}_4-30\text{Al}_2\text{O}_3-7\text{SiO}_2$, $58\text{Fe}_3\text{O}_4-35\text{Al}_2\text{O}_3-7\text{SiO}_2$, $53\text{Fe}_3\text{O}_4-40\text{Al}_2\text{O}_3-7\text{SiO}_2$, $48\text{Fe}_3\text{O}_4-45\text{Al}_2\text{O}_3-7\text{SiO}_2$, $43\text{Fe}_3\text{O}_4-40\text{Al}_2\text{O}_3-17\text{SiO}_2$, and $33\text{Fe}_3\text{O}_4-50\text{Al}_2\text{O}_3-17\text{SiO}_2$.

Figure 31 is a conductivity versus reciprocal temperature plot for $63\text{Fe}_3\text{O}_4-30\text{Al}_2\text{O}_3-7\text{SiO}_2$ ($63\text{F}-30\text{A}-7\text{S}$). The sample was first melted, with the initial data point taken at 1560°C. As the temperature was lowered to about 1400°C, region II took over. It should be noted that the apparent activation energy
Figure 31. Electrical conductivity as a function of temperature for composition 63Fe$_3$O$_4$-30Al$_2$O$_3$-7SiO$_2$. 

$0.434 \text{eV}$
of region II has no actual physical significance. Region II was simply a transitory situation between regions I and III. When $1128^\circ C$ was reached, the sample was reheated. The data taken during this upswing in temperature indicated that the conductivity results were reproducible. $o_1(1388^\circ C)$, $o_2(1277^\circ C)$ and $o_3(1128^\circ C)$ were the temperatures at which the sample was held overnight. The conduction in the multiphased solid aggregate had an activation energy of 0.434eV.

In the above, the significance of the slope in region II was alluded to. The conductivity plot of sample 58F-35A-7S helps illustrate this point (Figure 32). A hysteresis loop existed between the data taken with decreasing temperature and those with increasing temperature. The conductivity taken while the sample was solidifying was higher. Again the conductivity increased slightly with decreasing temperature in region I where the sample was a melt saturated with spinel and corundum. The junction between regions I and II was at $1390^\circ C$. At $o_1(1230^\circ C)$ the sample was held overnight. The low temperature range had an activation energy of 0.447eV.

The data for samples of 58F-35A-7S, 48F-45A-7S, 43F-40A-17S and 33F-50A-17S were compared in Figure 33. One important point is that region II became predominant at or just above $1380^\circ C$ for every sample. Also, the conductivities of 43F-40A-17S and 33F-50A-17S decreased with decreasing temperature in region I. This was due in part to the increasing corundum and mullite volume fractions in the melt, which were much less
Figure 32. Electrical conductivity as a function of temperature for composition $58\text{Fe}_3\text{O}_4 - 35\text{Al}_2\text{O}_3 - 7\text{SiO}_2$. 
Figure 33. Electrical conductivities of four compositions within the $s_1s_2m_2m_1$ quadrilateral.
conductive than the melt itself. In addition, the Fe$^{3+}$/Fe$^{2+}$ ratio in the melt was increasing and deviating further away from unity as the temperature dropped. The activation energies for conduction via the mullite matrices varied from $0.393 - 0.623\text{eV}$.

The composition 63F-30A-7S is just off to the spinel side of the spinel-corundum-melt three phase boundary. Table V is the x-ray diffraction data for a sample quenched from 1520$^\circ\text{C}$. Spinel was the only crystalline phase detected. Figure 34 is the microstructure of a 63F-30A-7S sample melted at 1550$^\circ\text{C}$, slowly cooled and annealed at 1250$^\circ\text{C}$ for 24 hours. It showed 75.17Fe$_3$O$_4$-24.68FeAl$_2$O$_4$ spinel grains and remnant corundum particles (20.50mol % Fe-Al$_2$O$_3$) in a mullite matrix (19.37 w/o Fe$_2$O$_3$, 60.6 w/o Al$_2$O$_3$, 25.03 w/o SiO$_2$). The compositions were obtained from electron microprobe analysis.

The ac-conductivities of these samples were also independent of frequency in the range of 1 - 10KHz. This applied for samples both in the molten and the solid state. Figures 35, 36 and 37 are ac-conductivity versus log frequency plots at various temperatures for compositions 63F-30A-7S, 48F-45A-7S and 33F-50A-17S respectively.

b) Compositions Within the Compatible Triangle $s_1m_1c_1$.

Of the four compositions in this triangle that were investigated, three had mullite as the matrix phase in the final crystallization product. They were 47Fe$_3$O$_4$-46Al$_2$O$_3$-
TABLE V

X-ray diffraction pattern for $63\text{Fe}_3\text{O}_4\cdot30\text{Al}_2\text{O}_3\cdot7\text{SiO}_2$
melted and held at 1250°C for 24 hours, without filter.

<table>
<thead>
<tr>
<th>$2\theta^\circ$</th>
<th>d (Å)</th>
<th>Intensity</th>
<th>Assignment (Spinel)</th>
</tr>
</thead>
<tbody>
<tr>
<td>23.824</td>
<td>4.689</td>
<td>6</td>
<td>111</td>
</tr>
<tr>
<td>35.53</td>
<td>3.172</td>
<td>6</td>
<td></td>
</tr>
<tr>
<td>39.487</td>
<td>2.865</td>
<td>2</td>
<td>220</td>
</tr>
<tr>
<td>42.02</td>
<td>2.699</td>
<td>5</td>
<td></td>
</tr>
<tr>
<td>46.61</td>
<td>2.447</td>
<td>1</td>
<td>311</td>
</tr>
<tr>
<td>56.82</td>
<td>2.0344</td>
<td>3</td>
<td>400</td>
</tr>
<tr>
<td>68.28</td>
<td>1.725</td>
<td>5</td>
<td>422</td>
</tr>
<tr>
<td>71.42</td>
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</tr>
<tr>
<td>76.49</td>
<td>1.5637</td>
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</tr>
<tr>
<td>82.78</td>
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<td>440</td>
</tr>
<tr>
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<td>1.308</td>
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<tr>
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<td>1.029</td>
<td>5</td>
<td>800</td>
</tr>
</tbody>
</table>

1 is the strongest, intensity decreases with number.
Figure 34. Microstructure of a sample of $63\text{Fe}_2\text{O}_3-30\text{Al}_2\text{O}_3-7\text{SiO}_2$ annealed in air at $1250^\circ\text{C}$ for 24 hours. (Magnification 200x).
Figure 35. Isothermal ac-conductivity as a function of frequency for composition $63Fe_3O_4 - 30Al_2O_3 - 7SiO_2$. 

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Figure 36. Isothermal ac-conductivity as a function of frequency for composition $48\text{Fe}_3\text{O}_4 - 45\text{Al}_2\text{O}_3 - 7\text{SiO}_2$. 

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Figure 37. Isothermal ac-conductivity as a function of frequency for composition $33\text{Fe}_3\text{O}_4-50\text{Al}_2\text{O}_3-17\text{SiO}_2$. 

$33\text{Fe}_3\text{O}_4 - 50\text{Al}_2\text{O}_3 - 17\text{SiO}_2$
7SiO$_2$, 43Fe$_3$O$_4$-50Al$_2$O$_3$-7SiO$_2$ and 33Fe$_3$O$_4$-60Al$_2$O$_3$-7SiO$_2$. The conductivities still displayed the similar three stage dependence on temperature, but with two major distinctions from that described in the previous section.

Figure 38 shows the conductivities of the three samples as a function of temperature. It should be noted that region II established itself at a higher temperature, near 1460°C. Also the activation energies for conduction in the low temperature range (region III) were higher, about 1.2eV.

Also included in Figure 38 was the conductivity result of a rectangular specimen (43F-50A-7S) by a four-point probe technique with a geometric factor of 8.889 cm$^{-1}$ (dotted line). This was carried out to test the reproducibility of the data from the conductivity cell.

Figure 39 is the microstructure of composition 47F-46A-7S melted and annealed at 1250°C for 24 hours. The morphology is similar to that of composition 63F-30A-7S. It shows spinel grains and corundum platelets in a crystalline mullite matrix. The ac-conductivity of composition 43F-50A-7S at different temperatures was again independent of frequency.

Using Maxwell's model for multiphase conduction, the actual conductivity of the mullite matrix was calculated from each of the compositions and is presented in Figure 40.

VI.2.3. Conduction via a Corundum Matrix in the Crystalline Composite.

One of the compositions in the triangle $s_1m_1c_1$ had a high
Figure 38. Electrical conductivities as a function of temperature for compositions within the compatible triangle $\text{Si}_3\text{MgCl}_4$. 

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Figure 39. Microstructure of a sample of composition 47F - 46A - 7S annealed in air at 1250°C for 24 hours. (Magnification 100x)
Figure 40. The calculated electrical conductivity of mullite of composition 13.09 w/o Fe$_2$O$_3$, 61.4 w/o Al$_2$O$_3$, 25.5 w/o SiO$_2$. 
enough alumina content that the corundum phase became the matrix of the solid aggregate. This difference in the microstructure led to a unique conductivity-temperature dependence.

Figure 4 is the microstructure of a sample of this composition, $23\text{Fe}_3\text{O}_4 - 70\text{Al}_2\text{O}_3 - 7\text{SiO}_2$ partially melted at $1550^\circ\text{C}$ and annealed at $1250^\circ\text{C}$ for a day. The acicular shaped grain was mullite ($11.63\text{ w/o Fe}_3\text{O}_4 62.79\text{w/o Al}_2\text{O}_3 25.57\text{w/o SiO}_2$) in a matrix of corundum containing $7.37\text{w/o Fe}$. Because of the high alumina content, the corundum grains formed an interconnecting network before the last melt solidified. As the sample was only partially melted, empty voids occupied a fair volume fraction.

The dc-conductivity data in Figure 4 revealed a drop of over two orders of magnitude upon solidification. Between $1550^\circ\text{C}$ and $1460^\circ\text{C}$ the conduction was through an iron aluminosilicate melt saturated with corundum and mullite. The conductivity decreased with temperature as corundum and mullite shared a greater portion of the melt. The activation energy for conduction via the corundum phase below $1460^\circ\text{C}$ was $2.97\text{eV}$.

Polarization effects were observed during the dc-conductivity measurements on the solid sample. When the current was first applied to the sample, it sustained a higher instantaneous conductivity. This then levelled off to the steady state dc-value in a time span of 45-60 min.
Figure 41. Microstructure of a sample of composition 23F-70A-7S annealed in air at 1250°C for 24 hours. (Magnification 200x)
Figure 42. Electrical conductivity as a function of temperature for composition $23\text{Fe}_3\text{O}_4 - 70\text{Al}_2\text{O}_3 - 7\text{SiO}_2$. Calculated by multiphase model.
Using the point counting technique, the volume fractions of corundum, mullite and void were obtained. Applying Maxwell's equation for the matrix conductivity, the conductivity of the iron-doped alumina phase (7.37w/o Fe) was

$$\sigma_{\text{corundum}} = 0.541 \sigma_{\text{sample}}$$

The calculated conductivity was included in Figure 42 (dashed line).

It has been documented that for all compositions with a high iron oxide content, the ac-conductivity was equivalent to the dc-value within the temperature range studied. However, such was not the case for 23F-70A-7S (Figure 43). The ac-data at 1544°C, where the conduction was through the melt, only showed slight enhancement with increasing frequency. But the data in the solid state were dependent on the measuring frequency. The increase in total conductivity over the dc-value was attributed to the contribution from ionic species.

VI.2.4. Electrical Conductivity of Iron Aluminosilicate Melts.

The conductivity of the iron aluminosilicate melts (region I) presently studied did not conform to the Arrhenius equation. It has a complicated dependence on temperature.

In region I of the conductivity results, the equilibrium phases present were a melt coexisting with spinel, corundum, and/or mullite. The relative volume fraction and composition of each depended on the temperature and the location of the
Figure 43. Isothermal ac-conductivity as a function of frequency for composition 23Fe$_3$O$_4$-70Al$_2$O$_3$-7SiO$_2$. 

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overall composition in the FeO·Fe$_2$O$_3$·Al$_2$O$_3$·SiO$_2$ system. Figure 44 is a micrograph of a sample of composition 63F-30A-7S quenched from 1495°C where the melt was saturated with spinel and corundum. The sample was sectioned vertically to see if there was any phase segregation. The micrograph showed that the spinel grains formed a layer at the top of the melt. A layer of corundum particles rested underneath it. The melt, of approximate composition 38w/o Fe$_2$O$_3$ 19w/o FeO 27w/o Al$_2$O$_3$ 16w/o SiO$_2$, was at the bottom of the crucible. Again the fine dendritic structure was a result of spinel-formation during quenching.

The conductivity cell was designed such that the platinum electrodes were about 3 mm above the bottom of the alumina crucible. The melt in the crucible was filled to a depth of at least 20 mm. So it would be safe to conclude that at sufficiently high temperatures when the solid phases occupied a small volume fraction, the conductivity measured would be that of the melt itself.

Figure 45 is a plot of the dc-conductivity at 1550°C as a function of the overall sample composition. It should be noted that even though the conductivity increased with the iron content, the change was not large. Points c$_1$, c$_2$, and c$_3$ actually represented the same melt on the spinel-corundum-melt phase boundary. This meant that the conductivities those of melts of the same composition but each with different volume fractions of corundum and spinel. The fact that the
Figure 44. The microstructure of a sample of composition 63Fe₂O₄-30Al₂O₃-7SiO₂ quenched from 1495°C in air, showing the segregation of phases.
Iron Aluminosilicate Melts

7 wt% SiO$_2$, 1550°C in Air

Figure 45. Isothermal electrical conductivity in air at 1550°C as a function of composition.
conductivities were identical within experimental error supports the argument mentioned in the last paragraph.

However, such was not the case for points $c_4$ and $c_5$. Here, the volume fraction of corundum was over 60%. Hence the conductivities measured were an effective value for corundum particles suspended in an iron aluminosilicate melt.

Figure 46 is a plot of $\log \sigma T/(1-c)$ versus reciprocal temperature for five compositions, where $c$ is the $Fe^{3+}/Fe_{\text{total}}$ ratio.


The isothermal conductivity of melts was measured as a function of oxygen partial pressure. For the curves presented in Figure 47 the equilibrium phases in air consisted of spinel or corundum particles in the melt. As the oxygen partial pressure was lowered, the compositions and volume fractions of the solid and molten phases changed according to the phase equilibria of the system. The partial pressure dependence was very similar to that of other silicate melts (Figure 9). The electrical conductivity decreased with decreasing oxygen partial pressure at the low $P_{O_2}$ range while for intermediate $P_{O_2}$, the conductivity was insensitive to any change in $P_{O_2}$.

A study of the isothermal conductivity of melts at a temperature above the liquidus surface could eliminate any problem posed by the presence of the solid phase. The melt
Figure 46. Plot of $\log \frac{\sigma T}{c(1-c)}$ versus reciprocal temperature for iron aluminosilicate melts.
Figure 47. Isothermal dc-conductivity as a function of oxygen partial pressure for iron aluminosilicate melts.
would remain single-phase over a range of oxygen partial pressure. Bringing the melt to equilibrium with oxygen at a given $P_{O_2}$ meant that the $\text{Fe}^{3+}/\text{Fe}^{2+}$ ratio, hence the $c(1-c)$ term, was adjusted without any accompanying change in the total iron, alumina and silica content. Figure 48 presents the isothermal results above the liquidus temperature.

Figure 49 shows the conductivities plotted against $\text{Fe}^{3+}/\text{Fe}_{\text{total}}$ ratio. For the compositions with 7 wt% SiO$_2$, the conductivities peaked at $c = 0.67$. For the composition 63F-20A-17S the maximum was at $c = 0.55$. 
Figure 48. Isothermal dc-conductivity as a function of oxygen partial pressure for iron aluminosilicate melts above the liquidus temperature.
Figure 49. Isothermal dc-conductivity as a function of Fe\(^{3+}\)/Fe\(_{\text{total}}\) ratio in iron alumino-silicate melts.

\[ N_{Fe} = \frac{n_{FeO} + 2n_{Fe_2O_3}}{n_{FeO} + 2n_{Fe_2O_3} + n_{Al_2O_3} + n_{SiO_2}} \]
Chapter VII. Discussion

The primary thrust of this research effort has been to understand the electrical conductivity in the FeO·Fe₂O₃·Al₂O₃·SiO₂ system as a function of composition, temperature and oxygen partial pressure. In this chapter, the results will first be related to the phase chemistry of the system. The possible conduction mechanisms in the solid and molten states will also be discussed.

The compositions studied showed four basic types of conductivity-temperature dependence in air. These four classes of conductivity behavior can conveniently be differentiated according to where the composition is located in the ternary system. The conductivity of the three compositions inside the compatibility triangle SiO₂·s₂·m₂ of Figure 50 increased with decreasing temperature without any observable discontinuity upon solidification. The rest of the compositions investigated were within the s₁s₂m₂m₁ quadrilateral and the s₁m₁c₁ compatibility triangle. The temperature dependence of their electrical conductivity typically had three stages. At high temperatures, where an iron aluminosilicate melt was in equilibrium with spinel, corundum and/or mullite, the conductivity was rather insensitive to temperature. Upon solidification with further cooling, there was a sharp discontinuity in electrical conductivity. For the composition with 23 w/o Fe₂O₃, the drop in conductivity at 1460°C was over two orders of magnitude. The thermal activation energies for
Figure 50. Illustration of several crystallization sequences in the FeO·Fe₂O₃-Al₂O₃-SiO₂ system.
conduction in the final crystallization products of the compositions within the $s_1s_2m_2m_1$ area varied from 0.393 to 0.623eV. The conductivity of three compositions inside $s_1m_1c_1$ have thermal activation energies of 1.155, 1.212 and 1.248eV while an activation energy of 2.97eV was measured for the composition in the same compatibility area that contained 23w/oFe$_3$O$_4$.

The properties of a multicomponent system such as FeO-Fe$_2$O$_3$-Al$_2$O$_3$-SiO$_2$ are controlled by the phases in equilibrium. Therefore one must revert to a detailed understanding of the phase chemistry in order to comprehend the complicated conductivity-temperature dependence. In the following, the association between the electrical conductivity and crystallization sequence of different compositions is discussed, using Figure 50 as an illustration.

The composition 73Fe$_3$O$_4$-20Al$_2$O$_3$-7SiO$_2$ (point "a" in Figure 50) is representative of compositions in the SiO$_2$-$s_2^-$-$m_2$ compatibility triangle. Below 1600°C, spinel starts to crystallize out of the melt. As the temperature is lowered, the equilibrium spinel composition continues to be enriched in magnetite and the crystallization proceeds along the dotted line $aa'$. The volume fraction of spinel of composition 63Fe$_3$O$_4$-38FeAl$_2$O$_4$ is about one-third at 1550°C. At about 1390°C, the crystallization path reaches $a'$ on the liquid-spinel-tridymite boundary. Here the last liquid disappears.

While phase equilibria predicts that the final crystallization product should be a mixture of spinel, mullite and
tridymite, Debye-Scherrer diffraction patterns failed to reveal any peaks characteristic of mullite or tridymite. Optical micrographs showed that the solid state aggregate was composed of large spinel grains imbedded in a matrix. The large spinel grains were found to be of the same composition. However, further x-ray diffraction studies revealed that at least two more different spinel compositions were present. The electron microprobe analysis also indicated that the matrix was inhomogeneous. The average matrix composition was 70.5\% FeO, 21.5\% Al$_2$O$_3$, 69.13\% SiO$_2$, with the silica content varying from 53.54 to 76.27\%. This was not representative of any stoichiometric composition. Judging from the broadening of the diffraction peaks, there were submicron spinel crystallites present. Given this evidence, it was concluded that the matrix of the 73Fe$_3$O$_4$-20Al$_2$O$_3$-7SiO$_2$ sample was made up of residual iron aluminosilicate glass with fine spinel crystallites.

The conductivity of this composition increased with decreasing temperature between 1380$^\circ$ and 1100$^\circ$C. The magnitude of the conductivity ruled out the possibility that the conduction was through interconnected large spinel grains. If it were so, the electrical conductivity would be of the order of 10-100 ohm$^{-1}$·cm$^{-1}$, i.e., at least two to three orders of magnitude higher. The results were reproducible by different means as described in Chapter VI. The plausible explanation is multiphase conduction in a microstructure with large spinel grains.
imbedded in a matrix of glass with fine crystallites.

The effect of iron oxide content on the conductivity and thermal activation energy of a glass has been reported by others. Trap and Stevels added 15 m/o \( \text{Fe}_3\text{O}_4 \) to a batch of glass with composition 24 m/o \( \text{Na}_2\text{O} \), 12 m/o \( \text{Al}_2\text{O}_3 \), 3 m/o \( \text{CaO} \), 3 m/o \( \text{SrO} \), 40 m/o \( \text{SiO}_2 \). The conductivity of the resulting glass was \( 1.09 \times 10^{-3} \text{ ohm}^{-1}\text{.cm}^{-1} \) with a thermal activation energy of 0.075eV. If 18 m/o \( \text{Fe}_3\text{O}_4 \) was added, the conductivity increased to \( 2.75 \times 10^{-3} \text{ ohm}^{-1}\text{.cm}^{-1} \) and the activation energy became 0.061eV. The conductivity was drastically reduced to \( 6.6 \times 10^{-6} \text{ ohm}^{-1}\text{.cm}^{-1} \) while the activation energy increased slightly, to 0.103eV, if only 12 m/o \( \text{Fe}_3\text{O}_4 \) was added.

Since the conductivity measured in this study for composition \( 73\text{Fe}_3\text{O}_4-20\text{Al}_2\text{O}_3-7\text{SiO}_2 \) remained between 0.2 and 0.3 ohm\(^{-1}\).cm\(^{-1}\) between 1380\(^\circ\) and 1100\(^\circ\)C, using an average value for the iron content in the matrix, the charge carrier mobility could be estimated. Assuming that the free charge carrier is ionized from the iron present in the glass, taking the iron content to be the maximum possible value (5.7 w/o) and using a density of 3.0 gm/cm\(^3\) for the glass, the calculated minimum mobility is of the order of \( 7.5 \times 10^{-4} \text{ cm}^2/\text{v}\cdot\text{sec} \). Such a low carrier mobility suggests that a conduction mechanism other than the band model is in operation. However, this speculation relies on the validity of the assumption that all iron ions are involved in the conduction process.
Even though plots of $\log_{10} \sigma \cdot T$ versus reciprocal temperature are linear for the compositions $73\text{Fe}_2\text{O}_4 - 20\text{Al}_2\text{O}_3 - 7\text{SiO}_2$ and $53\text{Fe}_2\text{O}_4 - 30\text{Al}_2\text{O}_3 - 7\text{SiO}_2$ (Figures 24 and 25), with activation energies of 0.0643 and 0.0547eV, respectively, the exact conduction mechanism cannot be identified unambiguously. Additional information on the precise variation of the free charge carrier concentration with temperature is essential in concluding whether the conduction is best represented by the conduction band model or by a thermally activated hopping process. Because of the small conductivity-temperature dependence, a plot of $\log \sigma T^{3/2}$ versus reciprocal temperature also has a linear relationship.

The composition $43\text{Fe}_2\text{O}_4 - 40\text{Al}_2\text{O}_3 - 17\text{SiO}_2$ (point "c" in Figure 50) is chosen as an illustration for the compositions inside the $s_1s_2m_2m_1$ region. This composition is a liquid above 1675°C. Corundum (ss) is the first crystalline phase to precipitate as the temperature is lowered. The crystallization proceeds along the locus cc'. At about 1500°C, the liquid-mullite-corundum boundary is reached (point c'). The crystallization now follows the boundary to point "1" at 1460°C where the liquid is in equilibrium with spinel, mullite and corundum. At "1", corundum is resorbed and the crystallization continues, progressing along the liquid-spinel-mullite boundary towards point "2". As this occurs the spinel composition in equilibrium with the melt and mullite changes from $s_1$ towards $s_2$. The mullite composition simultaneously alters from $m_1$ towards $m_2$. 141
At about 1400°C, the spinel and mullite compositions in equilibrium with the melt are $s_f$ and $m_f$, respectively. The points $s_f$, $m_f$ and $c$ lie on a straight line. The last liquid disappears at this temperature, leaving behind a crystallization product of spinel and remnant corundum grains in a mullite matrix.

The last liquids disappear in the vicinity of 1390-1400°C for all the compositions studied in the $s_1s_2m_2m_1$ region. This is, in all cases, accompanied by the succession of region II in the conductivity-temperature data.

The measured electrical conductivity for the composite structure was the conductivity through the mullite matrix with small contributions from the spinel grains present. But in as much as the silicate wets the corundum and spinel grains, few of the spinel grains would form enough contact area to allow a major fraction of the current just through spinel (or corundum). As the mullite composition ($m_f$) in the final crystallization composite varies according to each overall composition, the change in the thermal activation energy (0.393 to 0.623eV) is consistent with decreasing iron content. This evidence strongly indicates a direct correlation between the conductivity-temperature dependence and the phase chemistry of the FeO·Fe$_2$O$_3$·Al$_2$O$_3$·SiO$_2$ system.

The composition 43Fe$_3$O$_4$-50Al$_2$O$_3$-7SiO$_2$ (point "b" in Figure 50) inside the $s_1m_1c_1$ compatibility triangle follows the crystallization curve bb'. Spinel of approximate composi-
tion $53 \text{Fe}_3 \text{O}_4 - 47 \text{FeAl}_2 \text{O}_4$ appears at $1500^\circ \text{C}$ (point b'). The liquid-spinel-mullite boundary is followed until point "1" is reached. Unlike the compositions inside the $s_1 s_2 m_2 m_1$ region, the last liquid vanishes here. The crystallized composite contains spinel($s_1$) and corundum($c_1$) grains in a mullite($m_1$) matrix.

The junction between regions I and II of the conductivity-temperature data was at $1460^\circ \text{C}$ for compositions within the $s_1 c_1 m_1$ triangle. This was in contrast to a temperature of about $1390^\circ \text{C}$ observed for the compositions inside $s_1 s_2 m_2 m_1$.

The conductivity in the solid state was again through the mullite matrix of the multiphased aggregate. However, the mullite composition($m_1$) is fixed, regardless of the overall composition. Only the relative volume fraction of each phase was affected. Thus, the observed thermal activation energies do not vary as much and were 1.155, 1.212 and 1.248eV for iron-mullite of composition $m_1$.

Because mullite has a disordered structure intermediate between sillimanite and andalusite, it is difficult to interpret the conductivity results and identify the defects responsible for the conduction mechanism. The problem is further compounded by the variations in the $\text{Fe}/(\text{Fe+Al})$ and $\text{Si}/(\text{Fe+Al})$ ratios. Besides the defects inherent in the mullite structure, the partial replacement of Al by Fe ions create those extrinsic in nature. Iron is present mainly in the trivalent state. Mossbauer spectroscopy\cite{37,38} indicates a preference for
the octahedral coordination.

The mullite compositions in the present study have (Fe+Al)/Si ratios of 3.28 and above, as compared to a normal ratio of 3 for stoichiometric mullite. In view of this excess of Al and Fe ions and the randomness on the Al and Si tetrahedra, point defects such as $\text{Al}^{\text{i,t}}$, $\text{Al}^{\text{i,t'}}$, $\text{V}^{\text{i,t}}$, $\text{Si}^{\text{i,t}}$, $\text{V}^{\text{i,t}}$, $\text{Al}^{\text{i,o'}}$, $\text{V}^{\text{i,o}}$, $\text{Fe}^{\text{Al,o}}$ and $\text{Fe}^{\text{Al,o}}$ can be visualized.* If the mullite structure is regarded as one with a fixed cation to oxygen ratio, any excess in Al at the expense of Si leads to the creation of oxygen vacancies, $V_0^-$, in order to satisfy the charge and mass balance.

$$\text{Al}_2\text{O}_3 + \text{Si}^{\text{i,t}} = 2\text{Al}^{\text{i,t}} + V_-^0 + 0_0 + \text{SiO}_2 \quad (30)$$

For the iron-mullite composition($m_1$): 13.09w/o Fe$_2$O$_3$ 61.37w/o Al$_2$O$_3$ 25.53w/o SiO$_2$, the calculated oxygen vacancy fraction is of the order of $6 \times 10^{-3}$. Since one-third of the Al cations are involved in the tetrahedral network and if one considers that the Fe ions prefer the octahedral coordination, the fraction of Al octahedral sites replaced by Fe is 0.179. This means that almost one out of five octahedral cations is Fe. Obviously this is a limiting case of maxima occupancy for Fe ions in octahedral coordination. However, it demonstrates that the substitution of Al by Fe constitutes the major defect in the mullite lattice. The orthorhombic crystal structure of mullite may also allow conductivity anisotropy. *$i,t$ refers to interstitial tetrahedral site; $Al,O$ refers to octahedral site normally occupied by Al, etc.
Using Maxwell's multiphase conduction model, the electrical conductivity for the iron-mullite composition \( m_1 \) was about \( 2 \times 10^{-2} \ \text{ohm}^{-1} \cdot \text{cm}^{-1} \) at 1200°C (Figure 40). The average activation energy for conduction was 1.205eV. On the other hand, the activation energies for compositions within the area \( s_1 s_2 m_2 m_1 \) are lower and vary from 0.393 to 0.623eV because of the difference in the final mullite composition. These mullite phases have a higher silica content and a lower \((\text{Fe+Al})/\text{Si}\) ratio than \( m_1 \). With a similar \( \text{Fe}_2\text{O}_3 \) content (10.32 - 14.37w/o) a larger fraction of Al cations are replaced by Fe ions.

Unfortunately, the conduction mechanism in mullite cannot be determined without additional information on the temperature dependence of the mobility term and the \( \text{P}_2\text{O}_5 \) dependence of the conductivity.

A different conductivity-temperature dependence was displayed by the composition \( 23\text{Fe}_3\text{O}_4 - 70\text{Al}_2\text{O}_3 - 7\text{SiO}_2 \) (point "d" in Figure 50, within the \( s_1 m_1 c_1 \) compatibility triangle). This composition follows a crystallization path that leads to a product with a corundum(ss) phase as the matrix. The conductivity in air up to 1460°C has an activation energy of 2.97eV. This is comparable to values for \( \text{Al}_2\text{O}_3 \) of 2.97ev\textsuperscript{31} (undoped), 2.90eV\textsuperscript{32} (Co, Mg, Ti, Si-doped and undoped) and 2.47eV\textsuperscript{33} (undoped) from previous works. The impurity levels in the undoped crystals used by the other workers were less than 10 ppm. In a sample of compositions \( 23\text{Fe}_3\text{O}_4 - 70\text{Al}_2\text{O}_3 - 7\text{SiO}_2 \)
annealed at 1250°C in air, 13 m/o of iron was dissolved in the corundum phase. Comparing the results for the doped and undoped crystals, there is a similarity in the activation energies yet an enormous difference in the magnitude of the electrical conductivity. All these measurements probably are extrinsic even for the nominally "pure" crystals.

Of the Schottky and Frenkel type of intrinsic defects in alumina, it has now been suggested that Frenkel defects on the cation sublattice are the predominant type. Fe ions are incorporated substitutionally and the following defect reaction can be written,

\[
3\text{Fe}_{\text{Al}}^X + \text{Al}_{\text{Al}} + \frac{3}{2}\text{O}_2^X \rightarrow 3\text{Fe}^'_{\text{Al}} + \text{Al}_{\text{i}}^{\cdot\cdot} + \frac{3}{4}\text{O}_2 (K_{eq})
\]  

Assuming charge neutrality

\[
[\text{Al}_{\text{i}}^{\cdot\cdot}] = \frac{1}{3} [\text{Fe}_{\text{Al}}^']
\]

Dutt and Kroger have suggested that \( K_{eq} = 8.621 \times 10^3 \exp(-\frac{7.32eV}{RT}) \). However, this enthalpy value of 7.32eV seems unrealistically large. Also, the [Fe_{Al}'] would then be a very strong function of temperature. Pollak used a simple model and calculated the Fe\(^{2+}\)/Fe\(^{3+}\) equilibrium ratio in iron-doped alumina. At 1600°C and \( P_{O_2} = 10^{-2} \) atm, the [Fe_{Al}']/[Fe_{Al}^X] ratio is \( 3 \times 10^{-3} \). Previous work on the color centers in alumina has also indicated that the Fe ion is primarily present in the trivalent state.

In the high \( P_{O_2} \) region (above \( 5 \times 10^{-3} \) atm), Pollak reported that the 4.4 m/o Fe-Al\(_2\)O\(_3\) sample behaved like an
n-type conductor: \( \sigma \propto \text{P}_2^{-0.18} \). Assuming \( \text{Fe}^{+}_{\text{Al}} \) ionizes to give an electron in the conduction band,

\[
\text{Fe}^{+}_{\text{Al}} \rightarrow \text{Fe}_{\text{Al}} + e'
\]  

(32)

he suggested that this ionizing reaction might be responsible for the electronic conduction. Assuming this defect model, the conductivity is,

\[
\sigma \propto [\text{Fe}^{+}_{\text{Al}}]^{3/4} K_{eq}^{3/4} \left[ \text{Fe}_{\text{total}} \right]^{3/4} \text{Po}_{2}^{-3/16} \quad (33)
\]

The predicted conductivity dependence of \( \text{Po}_{2}^{-3/16} \) is very close to Pollak's observed dependence of \( \text{Po}_{2}^{-0.18} \).

This model also predicts that at constant temperature and \( \text{P}_{02} \), the electrical conductivity is dependent on \( \left[ \text{Fe}_{\text{total}} \right]^{3/4} \). Figure 51 is a plot of electrical conductivity at 1250°C in air as a function of \( \left[ \text{Fe}_{\text{total}} \right] \). The slope is 0.535, lower than as predicted by the model. Point A is obtained from this study.

In the preceding paragraphs, the emphasis has been focused on the correlation between the electrical conductivity results and the phase chemistry of the \( \text{FeO} \cdot \text{Fe}_2 \text{O}_3 \cdot \text{Al}_2 \text{O}_3 \cdot \text{SiO}_2 \) system. The conduction mechanism in the solid state was also discussed. Now, in the following, the conduction mechanism in iron aluminosilicate melt is considered in terms of the band conduction and thermally activated hopping models.

Systems such as \( \text{FeO-SiO}_2 \), \( \text{FeO-MnO-SiO}_2 \) and \( \text{FeO-CaO-SiO}_2 \) show appreciable non-ionic conductivity. \(^{71-73} \) Electronic conductivity comprises 50% of the total conductivity at 20 w/o
Figure 51. Electrical conductivity of $\text{Al}_2\text{O}_3$ as a function of iron content at 1250°C in air.
SiO$_2$ in FeO-SiO$_2$ and FeO-MnO-SiO$_2$ at 1400°C. For FeO-CaO-SiO$_2$, this happens at a range of iron content (60-80%) depending on the CaO/(CaO+SiO$_2$) ratio. In liquid wustite, the ionic conductivity at 1400°C constitutes only 7-8% of the total conductivity. In measuring the dc-conductivity of iron aluminosilicate melt in this study, no time-dependent polarization was observed, indicating that the electrical conduction is primarily electronic. This is supported by the fact that the ac-conductivity of the melt up to 10 KHz is equivalent to the dc-conductivity.

Since the conductivity of the binary Al$_2$O$_3$-SiO$_2$ system is ionic and is only $6 \times 10^{-4}$ ohm$^{-1}$ cm$^{-1}$ at 1750°C, the value of $0.12 - 0.3$ ohm$^{-1}$ cm$^{-1}$ for iron aluminosilicate melt suggests that the electronic behavior is due to the presence of iron ions.

Engell and Vygen$^{77}$ have considered two limiting models for electronic conduction in FeO-Fe$_2$O$_3$-CaO-SiO$_2$ melts. The conductivity was measured at 50 KHz and therefore had ionic and electronic contributions. The polaron hopping model and a collision dependent bimolecular reaction model were used to interpret the electronic conductivity results. However, their model was based on the time dependent collision of Fe$^{2+}$ and Fe$^{3+}$ ions to form an activated dipole prior to charge transfer. It also required ionic rearrangement after charge transfer was completed. Consequently, the odd feature of their approach lies in the fact that the electronic conduction is
actually dependent on the mobility of the Fe$^{2+}$ ion.

The electrical conductivity data for the liquids in this study have been analyzed to distinguish between the band and polaron hopping model in an effort to identify the conduction mechanism in iron aluminosilicate melt. The most conclusive test in distinguishing between the two models is the temperature dependence of the charge carrier mobility. This temperature dependence is obtained only if the free charge carrier concentration is known at all temperatures.

Calculation of the iron ion concentration, $N$, in iron aluminosilicate requires a knowledge of the density of the melt. Henderson et al.\textsuperscript{107} reported that the positive deviation of the computed "ideal density", for mechanical mixtures of the pure components, FeO and SiO$_2$, from the actual density of FeO-SiO$_2$ melt was less than 2.5% below 10 w/o SiO$_2$. It is assumed that the density of iron aluminosilicate melt can be estimated by the value computed from the densities of the pure components. The densities of pure liquid iron oxide\textsuperscript{108}, alumina\textsuperscript{109} and silica\textsuperscript{110} used are 4.0, 2.97 and 2.22 gm/cm$^3$, respectively. The calculated values of $N$ range from 8.475 x 10$^{21}$/cm$^3$ (for a 36Fe$_3$O$_4$-37Al$_2$O$_3$-27SiO$_2$ melt) to 1.924 x 10$^{22}$/cm$^3$ (for 71Fe$_3$O$_4$-19Al$_2$O$_3$-10SiO$_2$).

To obtain the free carrier mobility using the band model, several assumptions are made. The conductivity increases with decreasing oxygen partial pressure in the P$_{O_2}$ region above 10$^{-1}$ atm, suggesting that the conduction may be n-typed. It
is also assumed that all ferrous ions can be ionized to give electrons in the conduction band. The free carrier concentra-
tion, $n$, at a given melt composition is then approximated by

$$n = (1-c) N$$  \(34\)

where $(1-c)$ is the fraction of iron ions in the divalent state. The carrier mobility is therefore,

$$\mu = \frac{\sigma}{e(1-c)N}$$  \(35\)

For the composition $73\text{Fe}_3\text{O}_4$-$20\text{Al}_2\text{O}_3$-$7\text{SiO}_2$, the term $N$ in Equations 34 and 35 is replaced by $N_0 \exp(-0.216\text{eV}/RT)$ where the activation energy, 0.216eV, is obtained from the slope a plot of $\log(\sigma T^{3/2})$ versus reciprocal temperature and is taken to be the ionization energy for free charge carrier.

The mobility term, $\mu$, is calculated for series of melts formed along the crystallization pathes of five compositions. Log $\mu$ is plotted against log $T$ in Figure 52. A line with a slope of $-3/2$ is also drawn in the figure.

The decrease in mobility with increasing temperature supports the argument in favor of the conduction band model as the mechanism responsible for conduction in iron alumino-
silicate melt. However, the calculated mobilities are of the order of $10^{-4}$ cm$^2$/v·sec, simply too small for the band model to be valid. Since the accuracy of the mobility term depends on the ability to predict the free carrier concentration, any erroneous assumption made in estimating the concentration would easily result in the underestimation of the mobility.
Figure 52. Free carrier mobility as a function of temperature, based on the conduction band model.
A critical assumption is that all ferrous ions are ionized. Despite the large variation in the melt composition: 36-73 w/o Fe$_3$O$_4$, 17-37 w/o Al$_2$O$_3$, 7-30 w/o SiO$_2$, the electrical conductivity of the melt does not change significantly. The conductivity in air at 1550°C for a melt of composition 71Fe$_3$O$_4$-19Al$_2$O$_3$-10SiO$_2$ (N = 1.92 x 10$^{22}$/cm$^3$) is 2.37 x 10$^{-1}$ohm$^{-1}$.cm$^{-1}$ and that for composition 36Fe$_3$O$_4$-37Al$_2$O$_3$-27SiO$_2$ (N = 8.475 x 10$^{21}$/cm$^3$) is 1.138 x 10$^{-1}$ohm$^{-1}$.cm$^{-1}$. One would expect that if all ferrous ions contribute to the free carrier concentration, any variation in the melt composition and change in (1-c)N will affect the conductivity correspondingly. Figure 53 is a plot of electrical conductivity at 1550°C in air plotted as a function of (1-c)N in the melt. The proportionality between the conductivity and (1-c)N lends additional support to the validity of the above assumption.

The low value of the mobility term (10$^{-4}$cm$^2$/v-sec) suggests that the charge carriers are localized and thus the conductivity should be analyzed for dependencies as in the polaron hopping model.

Using Equation 7, a plot of log $\sigma$T/N c(1-c)a$^2$ versus reciprocal temperature should give the activation energy of the mobility, with $v$ and R$_{Fe}$ (the Fe$^{3+}$/Fe$_{total}$ ratio) assumed to be constant. This plot (Figure 54) shows no activation energy for four of the five cases. Even though this seems to suggest that polaron hopping is not the conduction mechanism in the melt, the evidence is by no means conclusive.
Figure 53. Electrical conductivity in iron aluminosilicate melt as a function of ferrous ion concentration
Figure 54. Effective mobility as a function of temperature, based on the polaron hopping model ($R_p$ assumed to be constant).
This apparent disagreement with hopping conduction is based on the premise that \( R_{Fe} \) remains constant even for different melt compositions. For the overall composition 73Fe\(_3\)O\(_4\)-20Al\(_2\)O\(_3\)-7SiO\(_2\), the liquid composition is about 71Fe\(_3\)O\(_4\)-19Al\(_2\)O\(_3\)-10SiO\(_2\) at 1550°C and as the temperature is lowered to 1477°C, the approximate liquid composition becomes 65Fe\(_3\)O\(_4\)-17Al\(_2\)O\(_3\)-18SiO\(_2\). The above analysis assumes \( R_{Fe} \) to be the same for the two melts.

The \( R_{Fe} \) term is actually a function of composition and the Fe\(^{3+}\)/Fe\(^{2+}\) ratio. The conductivity of iron aluminosilicates depends on the oxygen partial pressure in the following manner. At high \( P_{O_2} \), the conductivity increases with decreasing \( P_{O_2} \). In the intermediate range the conductivity is insensitive to any change in \( P_{O_2} \), and finally at very low \( P_{O_2} \), it decreases upon further reduction. Since the \( c(l-c) \) term is sensitive to the oxygen partial pressure over the melt, the following expression holds for a single-phase melt under isothermal conditions:

\[
\sigma = R_{Fe} \cdot c(l-c)
\]

Results show that the conductivity maxima are located at \( c > 0.5 \) (Figure 49), suggesting that some of the Fe\(^{3+}\) ions are in tetrahedral coordination and are not involved in the conduction process as they are covalently bonded to the silicate anions. Figure 55 depicts the Fe\(^{3+}\) distribution factor \( R_{Fe} \) as a function of composition. The distribution is very similar to the results of Pargamin\(^{18}\) for FeO-Fe\(_2\)O\(_3\)-Al\(_2\)O\(_3\)-SiO\(_2\) melts (Figure 1).
Figure 55. $\frac{Fe^{3+}}{Fe}$ distribution factor, $R_{Fe}$, as a function of composition in iron aluminosilicate melts.
The Fe\(^{3+}\) ions allocate themselves in octahedral and tetrahedral sites such that at the particular value of c and melt composition, the free energy of the system is a minimum. In a FeO-SiO\(_2\) melt of low SiO\(_2\) content, Masson\(^8\) suggested that the anions are mostly SiO\(_4^{4-}\) with a small concentration of Si\(_2\)O\(_6^{6-}\). Addition of Al\(_2\)O\(_3\) to the iron silicate increases the fraction of complex anions in the liquid. The Al ions in the liquid can occupy both tetrahedral and octahedral coordinations.\(^{111,112}\) It is therefore probable that some of the Al and Fe\(^{3+}\) ions are part of the network-forming unit in iron aluminosilicate melts. Complex anions such as SiO\(_4^{4-}\), AlO\(_4^{5-}\), Si\(_2\)O\(_6^{6-}\), SiAlO\(_7^{-}\), SiFeO\(_7^{-}\), etc. would be present.

It is also interesting to note the effect of SiO\(_2\) content on R\(_{Fe}\) (Figure 55). Higher SiO\(_2\) content increases R\(_{Fe}\). This suggests that if more network-forming Si ions become available, a greater portion of the Fe\(^{3+}\) ions are relieved from the polymeric anions and go into octahedral coordination. This may be related to the higher activities of Fe\(_2\)O\(_3\) at higher SiO\(_2\) content. Consequently it is very unlikely for R\(_{Fe}\) to be the same for the two melts: (a) 71Fe\(_3\)O\(_4\)-19Al\(_2\)O\(_3\)-10SiO\(_2\) (ΣM/O/ΣM\(_2\)O\(_3\) = 0.638), (b) 65Fe\(_3\)O\(_4\)-17Al\(_2\)O\(_3\)-18SiO\(_2\) (ΣM/O/ΣM\(_2\)O\(_3\) = 0.676), discussed above. The concave upward contour of the log\(_{10}\) cT/N c(1-c)a\(^2\) versus reciprocal temperature plot (Figure 54) can be due to the variation in R\(_{Fe}\). Taking R\(_{Fe}\) to be 0.45 and 0.65 for melts (a) and (b) respectively (obtained from Figure 55), log\(_{10}\) cT/N c(1-c)a\(^2\) R\(_{Fe}\) is 1.666 x 10\(^{-4}\) ohm\(^{-1}\)°K for melt (a) at 158
1552°C and is $1.159 \times 10^{-4}$ ohm$^{-1}$K for melt(b) at 1477°C. Hence, taking the $R_{Fe}$ term into consideration, a lower mobility at lower temperature is likely.

It is then quite possible that the apparent disagreement between Figure 54 and the polaron hopping model is due to the variation in the $R_{Fe}$ term with the liquid composition. For the specific instance that the $R_{Fe}$ term is considered, the mobility shows indication of a thermally activated behavior.

In summation, the electrical conductivity data of the FeO·Fe$_2$O$_3$-Al$_2$O$_3$-SiO$_2$ system have been directly correlated to its phase chemistry and crystallization sequence. The electrical conductivity of the solid composites can be interpreted with a multiphase conduction model. The conduction mechanisms in the composite matrices, iron aluminosilicate glasses, iron-mullite and Fe-Al$_2$O$_3$ have been discussed. As regards iron aluminosilicate melts, basing on the available evidence, one cannot determine unambiguously the conduction mechanism. Analysis of the results according to a band conduction model gives a decreasing mobility with increasing temperature. Yet the mobility ($10^{-4}$ cm$^2$/v·sec between 1450° and 1550°C) is too low for the band model to be valid. Initial analysis of the data based on the polaron hopping model, with $R_{Fe}$ assumed to be constant for all melt compositions, does not lead to a thermally activated mobility term. Further consideration with the variation in $R_{Fe}$ taken into account.
seem to suggest that the conduction process is thermally
activated.

Confirmation of either model as the conduction mechanism
will require exact information on the charge carrier concentra-
tion, the precise dependence of $R_{Fe}$ on melt composition and
the temperature dependence of the mobility term.
Chapter VIII. Conclusions

The dc- and ac-conductivity results of the compositions (7 or 17 w/o SiO$_2$) in the FeO-Fe$_2$O$_3$-Al$_2$O$_3$-SiO$_2$ system, which are investigated, suggest that the conduction is predominantly electronic for compositions with more than 33 w/o Fe$_3$O$_4$.

Four basic types of conductivity-temperature dependence are observed in air and are explained in terms of the phase chemistry of the system. Comparison of the conductivity-temperature dependence with the phase equilibria strongly indicates a direct correlation between the result and the crystallization sequence followed by each composition. The conductivity in the crystallized composites of spinel, mullite, cornudum or iron aluminosilicate glasses has to be interpreted in terms of multiphase conduction. The four types of conductivity-temperature dependence are summarized as follows:

1. The electrical conductivity increases with decreasing temperature with no distinct discontinuity upon solidification in the first kind of behavior. This is the case for all three compositions studied, which are in the compatibility region SiO$_2$-$s_2$-m$_2$ (Figure 23). These compositions crystallize to form an aggregate with iron aluminosilicate glasses as the matrix. Unfortunately, the conduction mechanism in the glass remains unidentified due to the inability in measuring its iron content.

2. The dependence of electrical conductivity on temperature is of three stages in the second type of behavior. A sharp discontinuity is observed at about 1390°C in the conductivity
of compositions in the area $s_1 s_2^m m_1$ (Figure 23). The conduction in the crystallized composites is through the iron-mullite matrices and shows activation energies varying from 0.292 to 0.623eV, depending on the iron content and the (Fe+Al)/Si ratio.

3. The discontinuity occurs at 1460°C for compositions within the compatibility triangle $s_1 m_1 c_1$ (Figure 23). The thermal activation energies for conduction in crystallized composites with an iron-mullite (13.09 w/o $\text{Fe}_2\text{O}_3$, 61.37 w/o $\text{Al}_2\text{O}_3$, 25.53 w/o $\text{SiO}_2$) matrix are 1.155, 1.212 and 1.248eV. The conductivity of this iron-mullite is calculated using Maxwell's multiphase conduction model. Due to its disordered crystal structure and varying composition, the conduction mechanism in iron-mullite is not determined unambiguously.

4. For the composition $23\text{Fe}_3\text{O}_4 - 70\text{Al}_2\text{O}_3 - 7\text{SiO}_2$, the drop in conductivity at 1460°C is over two orders of magnitude. The thermal activation energy is 2.97eV and is attributed to conduction in the crystallized composite through a corundum matrix containing 13 m/o Fe. It is tentatively suggested that the ionization of $\text{Fe}^{1+}$ is responsible for the electrical conduction.

The conductivity of iron aluminosilicate melts at 1550°C and 1600°C decreases with increasing oxygen partial pressure at $P_{O_2} > 10^{-1}$ atm. It remains essentially constant over the intermediate range of $10^{-5} < P_{O_2} < 10^{-1}$ atm. Upon subsequent reduction at still lower $P_{O_2}$, the electrical conductivity
decreases, indicating that it may be p-typed.

Based on the available evidence, the conduction mechanism in iron aluminosilicate melts cannot be determined unambiguously. Analysis of the results according to a band conduction model gives a decreasing mobility with increasing temperature. However, the mobility is $10^{-4}$ cm$^2$/v·sec between 1450$^\circ$ and 1550$^\circ$C and is too low for the band model. Using the polaron hopping model, the fraction of Fe$^{3+}$ ions in octahedral coordination, R$_{Fe}$, is calculated. Analysis of the data with the variation in R$_{Fe}$ taken into account suggests that the conduction process is thermally activated.
Chapter IX. Suggestions for Future Work

Several experiments are suggested which would be helpful in elucidating the areas that are not yet resolved by the present study.

1. A direct measurement of the Hall coefficients of mullite and iron aluminosilicate glasses to determine the charge carrier mobility at different temperatures, this would help identify the conduction mechanisms.

2. A study of the electrical conductivity of a simple system such as iron silicate as a function of temperature, composition and oxygen partial pressure, this would provide valuable information on the conduction mechanism in more complex silicate melts containing iron oxide.

3. Very little is known about mullite, especially the substitution of Al by Fe ions. It should be exciting to carry out equilibrium thermogravimetric and conductivity measurements on mullites with different Al/Si and (Fe+Al)/Si ratios as a function of oxygen partial pressure. This will provide important understanding on the defects in mullite.

4. To study the effect of addition of Al$_2$O$_3$ on the density of iron silicate melt. This can give further information on the structural constitution of the melt.
Appendix: Equivalent Circuit for Ionic and Electronic Conductivity.

An interesting problem has been the capability to discern the electronic and ionic contribution to the total conductivity of a material. The ionic transference number can be obtained by electrochemical cell measurements, while the dc-conductivity at "infinite" time gives the electronic conductivity. Any ionic component would be observed as a time-dependent polarization process in a dc measurement, if blocking electrodes are used.

A simple equivalent circuit can be used to model as the electronic and ionic conductivity. The electronic path is represented by the resistor $R_e$, whereas the ionic path is indicated by the capacitor $C_i$ in series with resistor $R_i$. The impedance of this network is

$$Z_i = \frac{1}{\frac{1}{R_e} + \frac{1}{R_i} - j \omega C_i}$$

$$= \frac{(R_e R_i (R_e + R_i) \omega^2 C_i^2 + R_e)}{(R_e + R_i)^2 \omega^2 C_i^2 + 1} - j \omega C_i R_e^2$$

The measured impedance $|Z_i|$ is

$$|Z_i| = \sqrt{R_e^2 R_i^2 (R_e + R_i)^2 \omega^4 C_i^4 + 2R_e R_i (R_e + R_i) \omega^2 C_i^2 + R_e^2 + \omega^2 C_i^2 R_e^2}$$

$$(R_e + R_i)^2 \omega^2 C_i^2 + 1$$
\[ Z_{ij} = \frac{R_e + R_i}{R_e + R_i} \]

and considering \( \sigma_e \propto \frac{1}{R_e} \) and \( \sigma_i \propto \frac{1}{R_i} \), then at \( \omega \gg \omega_c \)

\[ \sigma(\omega) = \sigma_i + \sigma_e \]

Consequently, at \( \omega = 0 \), the dc conductivity represents the electronic contribution. The conductivity increases with frequency, in the range \( 0 < \omega < \omega_c \), due to the increasing contribution of the ionic component. At a frequency, \( \omega >> \omega_c \), the total conductivity is independent of frequency as the presence of \( C_i \) is insignificant. It is the summation of contributions from ionic and electronic parts. This frequency-independent conductivity together with the dc-value give the ionic and electronic transference numbers.

At much higher frequencies such as \( 10^7 \) Hz and above, electron polarization and other ionic processes become important. The conductivity is no longer a simple function of frequency.
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Biographical Note.

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