I. INTRODUCTION AND OVERVIEW

Quantum chromodynamics (QCD) [1,2] predicts the cross sections for the production of objects with large transverse momentum ($p_T$) [3] in hadronic collisions. Such calculations are performed by factorizing the interaction into a hard scattering process that can be calculated perturbatively and a set of soft processes that must be described phenomenologically. The high-$p_T$ jet production cross section is calculated [4] by convolving the matrix elements for the scattering of two initial-state partons (quarks and gluons), with the corresponding parton distribution functions (PDF), to produce a partonic final state. To predict the momentum spectrum of the final particles, additional effects must be considered. The outgoing partons fragment into jets of hadrons. The beam remnants also hadronize and the spectator partons in the proton can also interact, leading to multiple parton interactions (MPI). QCD radiation from the initial- and final-state partons occurs, leading to additional jets and to an increase in the ambient energy. These effects vary with the momentum transfer of the hard parton scattering. Some of these processes take place at an energy scale where the QCD coupling constant is large and perturbation theory cannot be used. They must therefore be described using QCD-motivated phenomenological models, implemented in Monte Carlo (MC) event generators. In general, these models contain a number of free parameters with values that must be obtained by fitting to experimental data.

For a single proton-proton ($pp$) collision, the underlying event (UE) is defined to be any hadronic activity not associated with the jets or leptons produced in the hard scattering process. In practice, because color fields connect all the strongly interacting partons in the proton-proton event, no unambiguous assignment of particles to the hard scattering partons or UE is possible. Instead, distributions that are sensitive to UE modeling are constructed from the tracks that are far from the direction of the products of the hard scatter. This direction is approximated by the direction of the highest-$p_T$ (leading) object in the event.

Measurements of observables sensitive to the UE characteristics in $p\bar{p}$ collisions were performed at the Tevatron by CDF using jet events at center-of-mass energies $\sqrt{s} = 630$ GeV and $\sqrt{s} = 1.8$ TeV [5], and using Drell-Yan and jet events at $\sqrt{s} = 1.96$ TeV [6]. Underlying event observables have been measured in $pp$ collisions with $\sqrt{s} = 900$ GeV and $\sqrt{s} = 7$ TeV from the distribution of charged particles in the region transverse to leading charged particles and leading charged-particle jets by CMS [7,8] and in the regions transverse to and away from leading charged particles by ATLAS [9] and ALICE [10]. A complementary analysis by ATLAS studied UE properties using both neutral and charged particles [11].
This paper extends previous studies of the UE by measuring the charged-particle multiplicity and transverse momentum density in the transverse and away regions with respect to leading charged-particle jets reconstructed using the anti-$k_T$ [12] algorithm and varying the radius parameter, $R$, of that algorithm between 0.2 and 1.0. We can regard the leading charged particle as a charged-particle jet with $R \approx 0$. As long as $R$ remains below a characteristic value determined by the momentum transfer ($q^2$) of the hard scatter, the $p_T$ of charged-particle jets formed with larger $R$ are better indicators of the hard scatter energy. Such charged-particle jets are reconstructed with high efficiency at low jet transverse momentum, $p_T^{\text{jet}}$, and can therefore be used to study the behavior of the UE in the transition region between soft-QCD interactions and hard partonic scattering. At larger $p_T^{\text{jet}}$, charged-particle jets provide a complement to calorimeter-based measurements, with results that are independent of calorimeter calibrations, selections, and uncertainties. Variations in the mean values of these UE observables with $R$ provide additional information on the interplay between the perturbative and nonperturbative components of QCD-inspired MC models.

This paper is organized as follows. The ATLAS detector is described briefly in Sec. II. The QCD Monte Carlo models used in this analysis are discussed in Sec. III. The variables sensitive to UE activity are defined in Sec. IV. The event and object selections are presented in Sec. V. Section VI contains a description of the analysis. In Sec. VII, the treatment of systematic uncertainties is discussed. Fully corrected data distributions are presented in Sec. VIII, and the results are compared to the predictions of several Monte Carlo generators. Section IX discusses the dependence of the UE observables on $R$. Conclusions are provided in Sec. X.

II. THE ATLAS DETECTOR

The ATLAS detector is described in detail in Ref. [13]. The subsystems relevant for this analysis are the inner detector (ID) and the trigger system.

The ID is used to measure the trajectories and momenta of charged particles. It consists of three detectors: a pixel detector, a silicon strip tracker (SCT), and a transition radiation straw-tube tracker (TRT). These detectors are located inside a solenoid that provides a 2 T axial magnetic field and have full coverage in the azimuthal angle $\phi$ over the pseudorapidity range $|\eta| < 2.5$. The ID barrel (end cap) typically has $3(2 \times 3)$ pixel layers, $4(2 \times 9)$ layers of double-sided silicon strip modules, and $73(2 \times 160)$ layers of TRT straw tubes. A track traversing the barrel typically has 11 silicon hits (3 pixel clusters and 8 strip clusters), and more than 30 straw-tube hits. Typical position resolutions are 10, 17, and 130 $\mu$m for the $r-$ $\phi$ coordinate of the pixel detector, SCT, and TRT, respectively. The resolution of the second measured coordinate is 115 $\mu$m for the pixel detector and 580 $\mu$m for the SCT.

The ATLAS trigger consists of three levels of event selection: level 1 (L1), level 2 (L2), and event filter. The trigger relevant for this analysis is the single-arm L1 minimum bias trigger [14], which uses information from the beam pickup timing devices (BPTX) and the minimum bias trigger scintillators (MBTS). The BPTX stations are composed of electrostatic button pickup detectors attached to the beam pipe at $\pm 175$ m from the center of the ATLAS detector. The coincidence of the BPTX signal between the two sides of the detector is used to determine when bunches collide in the center of the detector. The MBTS consists of 32 scintillation counters located at pseudorapidities $2.09 < |\eta| < 3.84$. The trigger requires a single hit above threshold in the MBTS together with a BPTX coincidence.

III. MONTE CARLO SAMPLES

MC event samples are used to compute detector acceptance and reconstruction efficiencies, determine background contributions, unfold the measurements for detector effects, and estimate systematic uncertainties on the final results. The samples used here are the same as those used in Ref. [15]. The baseline Monte Carlo event generator used to determine acceptance and efficiencies is Pythia 6.4.21 [16] with the ATLAS tune AMBT1, which uses the MRST2007LO* PDF [17]. This tune was derived using the measured properties of minimum bias events [18]. Generated events are simulated using the ATLAS detector simulation [19], which is based on the Geant4 toolkit [20]. The simulated events are processed using the same software as the data. Several other simulated samples are used to assess systematic uncertainties on the detector response: Pythia 6 using the Perugia 2010 tune [16] (CTEQ5L PDF [21]), Pythia 6 with the ATLAS MC09 tune [22] (MRST2007LO* PDF) and Pythia 8.145 with tune 4C [23] (CTEQ6L1 PDF).

In the past year, significant work has been done to improve agreement between the MC generators and LHC data by tuning the parameters of the phenomenological models used to describe soft-QCD processes [24,25]. UE data, after applying corrections for detector effects, are compared to recent tunes of several MC event generators. Samples with high statistics were produced using the Pythia 6.4.21, Pythia 8.145, and Herwig ++ 2.5.1 [26] generators. Several different Pythia 6 samples were generated with different UE tunes. AUET2B [27] is an ATLAS tune that uses the $p_T$-ordered parton shower, interleaved initial-state radiation (ISR) and MPI which has been tuned to UE data from CDF and ATLAS. This employs the MRST2007LO** [17] PDF. The CMS tune Z1 [25] is very similar, but is fitted to CMS UE data and uses CTEQ5L PDF. The Perugia 2011 tune [28] uses similar settings, with the
UE parameters constrained by minimum bias and UE data from CDF and ATLAS. Perugia 2011 NOCR is a tune of the $p_T$-ordered model that does not employ color reconnection. The Pythia 8 generator includes many new features over Pythia 6, such as fully interleaved $p_T$-ordered MPI + ISR + FSR evolution and a different model of hard diffraction. The default author tune 4C [29] with CTEQ6L1 PDF [30] is used. The recently released Herwig $^+$ $^+$ version with tune UE7-2 used here has angle-ordered parton showers, employs MRST2007/LO* PDF, and has an improved model of color reconnection.

IV. DEFINITION OF VARIABLES

After reconstructing jets from charged tracks in the event, $p_T^{\text{jet}}$ refers to the transverse momentum ($p_T$) of the jet with the highest $p_T$. The variation of the UE properties with $p_T^{\text{jet}}$ is measured in this analysis. In addition, the dependence of these properties on $R$ is studied.

Particles are defined to be in the transverse region if their azimuthal angle differs from that of the leading jet ($|\Delta \phi| = |\phi_{\text{particle}} - \phi_{\text{jet}}|$) by between $\pi/3$ and $2\pi/3$ radians, as shown in Fig. 1. This region is most sensitive to the UE. Particles with $|\Delta \phi| > 2\pi/3$ are defined to be in the away region. This region is likely to contain the fragmentation products of the subleading parton produced in the hard scattering.

Three observables sensitive to UE activity are studied in the transverse and away regions:

(i) $N_{\text{ch}}$: the number of tracks in the region;
(ii) $\sum p_T$: the scalar sum of the transverse momentum of the tracks in the region;
(iii) $\bar{p}_T$: the average $p_T$ of the tracks in the region ($\bar{p}_T = \sum p_T / N_{\text{ch}}$).

![Diagram of transverse and away regions](diagram)

FIG. 1 (color online). Definition of the transverse and away regions with respect to the leading jet.

V. EVENT SELECTION AND RECONSTRUCTION

The events used in this analysis were collected with the ATLAS detector at a center-of-mass energy $\sqrt{s} = 7$ TeV during early 2010. The data sample, event selection, and reconstruction are almost identical to those used to measure the cross section and fragmentation functions of jets reconstructed from tracks [15]. The minimum track $p_T$ selection criteria in the current analysis differs from those in [15] and are discussed in this section. Events are required to have passed the L1 minimum bias trigger that was highly prescaled. The sample represents an integrated luminosity of 800 $\mu$b$^{-1}$ after the trigger prescale. The average number of collisions per bunch crossing, $\mu$, varied throughout the data-taking period but never exceeded a value of $\mu = 0.14$. Over half the data were taken with $\mu \leq 0.01$. Thus, effects due to the presence of more than one collision in the same bunch crossing (“pileup”) are minimal. Primary vertex reconstruction [31] is performed using tracks with $p_T > 0.4$ GeV and $|\eta| < 2.5$. A minimum of two tracks is required to form a vertex. To further reduce the contributions of pileup, events are rejected if more than one primary vertex is reconstructed.

Tracks used in the reconstruction of jets and UE observables are required to have $p_T > 0.4$ GeV, $|\eta| < 2.5$, transverse impact parameter with respect to the primary vertex $|d_0| < 1.5$ mm and longitudinal impact parameter with respect to the primary vertex $|z_0 \sin\theta| < 1.5$ mm. Only tracks with at least one pixel hit and six SCT hits are considered. To minimize the contribution of particles produced by secondary interactions in the ID, tracks are required to have a hit in the innermost pixel layer if the extrapolated track passes through an active portion of that layer.

For each event, jet collections are constructed, corresponding to the output obtained when the anti-$k_t$ algorithm is applied to the tracks for five separate values of $R$: 0.2, 0.4, 0.6, 0.8, and 1.0. For each jet collection, the leading jet is defined to be the jet with the largest $p_T^{\text{jet}}$ satisfying the requirements $p_T^{\text{jet}} > 4$ GeV and $|\eta^{\text{jet}}| < 1.5$. This maximum $|\eta^{\text{jet}}|$ cut ensures that all tracks associated with jets in the fiducial region are within the fully efficient tracking volume.

VI. ANALYSIS PROCEDURE

The analysis is performed in parallel on each of the five jet collections using the following procedure. First, the leading jet is selected and events are rejected if there is no jet that satisfies the requirements described in the previous section. Next, the $\Delta \phi$ of each track with respect to the leading jet is calculated and the tracks in the transverse and away regions are identified. In addition to satisfying the selection criteria discussed in Sec. V, tracks used for the UE measurements are required to pass the same pseudorapidity cut as the jets, $|\eta| < 1.5$. This
requirement minimizes the contamination in the UE calculation, from constituent tracks of a leading jet with $|\eta^{\text{jet}}| > 1.5$.

The selected tracks are used to calculate the three event observables $N_{\text{ch}}$, $\Sigma p_T$, and $p_T$, denoted generically as $O$, in the transverse and away regions. The final results presented here are the distributions and mean values of these observables for specific ranges (bins) of $p_T^{\text{jet}}$. To allow comparisons with MC generators, the data distributions are corrected for detector acceptance, reconstruction efficiency, and for bin migration due to track and jet momentum-resolution effects. The corrections used in this unfolding procedure are obtained by matching the jets reconstructed in simulated MC samples with those obtained when the anti-$k_t$ algorithm is applied to the primary charged particles produced by the generator. Primary charged particles are defined as charged particles with a mean lifetime $\tau > 0.3 \times 10^{-10}$ s, which are produced in the primary collision or from subsequent decays of particles with a shorter lifetime. Thus, the charged decay products of $K^0_S$ and $\Lambda$ particles are not included. A reconstructed jet is considered to be matched to a particle-level jet if their centers are separated by $\sqrt{(\Delta \eta)^2 + (\Delta \phi)^2} < R/2$.

Jets below the minimum $p_T^{\text{jet}}$ cut or outside the maximum $|\eta^{\text{jet}}|$ cut are used in the procedure that corrects for the effects of resolution smearing. Thus, looser requirements of $p_T^{\text{jet}} \geq 1$ GeV and $|\eta^{\text{jet}}| \leq 2.5$ are imposed during the reconstruction. In addition, since corrections for migration of jets into the fiducial volume require knowledge of the population outside that volume, the transverse momentum of the leading jet outside the fiducial volume ($\bar{p}_T^{\text{ext}}$) is also determined in each reconstructed jet collection for each event and, in MC samples, for each collection of particle-level charged-particle jets.

The events satisfying these requirements are corrected back to the primary charged-particle spectra satisfying the event-level requirement of at least one anti-$k_t$ jet with $p_T^{\text{jet}} \geq 4$ GeV and $|\eta^{\text{jet}}| < 1.5$ reconstructed from charged primary particles with $p_T > 0.5$ GeV and $|\eta| < 2.5$. Data distributions are unfolded using an iterative method [32] based on Bayes’ theorem, implemented in the RooUnfold [33] software package. The procedure requires three inputs: a measured input distribution (stored as a multidimensional histogram), a response matrix (obtained from simulated data) that provides a mapping between reconstructed objects and those obtained directly from the event generator, and an initial choice for the prior probability distribution, or prior for short. Each observable $O$ is stored in a three-dimensional histogram (one histogram for each observable and separate histograms for the transverse and away regions) where the binning variables are $p_T^{\text{jet}}$, $\bar{p}_T^{\text{ext}}$, and $O$. To accommodate the decreasing statistics in the data with $p_T^{\text{jet}}$ and the variation of the $p_T^{\text{jet}}$ and $\bar{p}_T^{\text{ext}}$ resolution with transverse momentum, these histograms have variable bin width. The response matrix is stored as a six-dimensional histogram that specifies the probability that observed values of $p_T^{\text{jet}}$, $p_T^{\text{ext}}$, and $O$ are measured for given true values of $p_T^{\text{jet}}$, $p_T^{\text{ext}}$, and $O$. This response matrix is not unitary because in mapping from generator to reconstruction some events and jets are lost due to inefficiencies and some are gained due to misreconstruction or migration of true objects from outside the fiducial acceptance into the reconstructed observables.

Unfolding the experimental distribution to obtain the corrected distribution is done as follows. The response matrix, measured data, and initial prior are used as inputs to the unfolding algorithm to produce an updated distribution, the posterior. This posterior is used as the input prior for another iteration of the algorithm, and this process is repeated. The inputs to each iteration of the unfolding algorithm are the baseline response matrix, measured data and the posterior of the previous iteration. The number of iterations is determined from Monte Carlo by examining the difference in $\chi^2$ between successive iterations, and the difference between the unfolded and true distributions. In this analysis, a total of four iterations are performed for each measured distribution. The associated uncertainties are discussed in Sec. VII. The initial prior is taken to be the prediction of the baseline Monte Carlo generator. Systematic uncertainties associated with this choice and with the modeling of the response matrix are discussed in Sec. VIII.

Once the corrected distributions have been obtained in bins of $p_T^{\text{jet}}$, the mean value of $O$ for each $p_T^{\text{jet}}$ bin is determined from these distributions. Some care must be taken to avoid bias when the mean is calculated since the output of the unfolding procedure is a histogram and the distribution of the population varies across the bin. For $\Sigma p_T$ and $N_{\text{ch}}$, the cumulative distribution function of the unfolded distribution is calculated and fit to a cubic spline and the mean is determined from the results of the spline fit. This step reduces the bias between the binned and unbinned calculation of the mean from a few percent to less than 0.5%. The $\bar{p}_T$ distributions have sufficiently fine binning that the bias is below 0.5% without this step.

VII. SYSTEMATIC UNCERTAINTIES

A summary of the systematic uncertainties and how they affect the measurements is presented in Table I. The following sources of systematic uncertainty have been considered:

1. The track reconstruction efficiency and momentum reconstruction uncertainty, due to potential discrepancies between the actual detector performance and the simulation model.
2. Potential bias arising from the unfolding procedure.

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TABLE I. The systematic uncertainties associated with measurement of the mean values of \( \Sigma p_T, N_{\text{ch}}, \) and \( \bar{p}_T. \)

<table>
<thead>
<tr>
<th>Source</th>
<th>( \Sigma p_T ) (%)</th>
<th>( N_{\text{ch}} ) (%)</th>
<th>( \bar{p}_T ) (%)</th>
<th>( \Sigma p_T ) (%)</th>
<th>( N_{\text{ch}} ) (%)</th>
<th>( \bar{p}_T ) (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Tracking reconstruction</td>
<td>2.1–2.5</td>
<td>2.0–2.3</td>
<td>0.2–0.3</td>
<td>2.1–2.6</td>
<td>2.0–2.3</td>
<td>0.1–0.2</td>
</tr>
<tr>
<td>Unfolding procedure</td>
<td>1.5–6.0</td>
<td>1.5–4.0</td>
<td>1.0–4.0</td>
<td>1.5–5.0</td>
<td>1.5–4.0</td>
<td>1.0–4.0</td>
</tr>
<tr>
<td>Leading jet misidentification</td>
<td>( \leq 1.0 )</td>
<td>( \leq 1.0 )</td>
<td>( \leq 0.5 )</td>
<td>( \leq 1.0 )</td>
<td>( \leq 1.0 )</td>
<td>( \leq 0.5 )</td>
</tr>
<tr>
<td>Response matrix</td>
<td>0.5–2.1</td>
<td>0.5–1.6</td>
<td>0.5–1.6</td>
<td>0.5–2.2</td>
<td>0.5–1.6</td>
<td>0.5–1.2</td>
</tr>
<tr>
<td>Discretization matrix</td>
<td>( \leq 0.5 )</td>
<td>( \leq 0.5 )</td>
<td>( \leq 0.5 )</td>
<td>( \leq 0.5 )</td>
<td>( \leq 0.5 )</td>
<td>( \leq 0.5 )</td>
</tr>
<tr>
<td>Total</td>
<td>2.7–6.6</td>
<td>2.6–4.7</td>
<td>1.3–4.1</td>
<td>2.7–5.7</td>
<td>2.6–4.7</td>
<td>1.3–4.1</td>
</tr>
</tbody>
</table>

(3) Misidentification of the leading jet due to cases where the leading reconstructed jet does not correspond to the true leading jet.

(4) The uncertainty in the response matrix, which is derived using a particular MC sample and thus depends on the details of the event generator.

(5) Uncertainty in the calculation of the means from the distributions of observables due to discretization effects arising from the finite bin width of the unfolded distributions.

Uncertainties on the tracking efficiency are \( \eta \) dependent and vary between 2% (for \( |\eta^{\text{track}}| \leq 1.3 \)) and 7% (for \( 2.3 < |\eta^{\text{track}}| \leq 2.5 \)) [34]. The dominant source of this uncertainty comes from possible inaccuracies in the description of the detector material in the simulation. The effect of this uncertainty on the measured observables is assessed by randomly removing from the data a fraction of the tracks consistent with the uncertainty on the tracking efficiency and recalculating the observable. The resulting uncertainty is then assumed to be symmetric. Uncertainties on the track momentum resolution are parametrized as an additional \( \eta \)-dependent broadening of the resolution in track curvature with values that vary from 0.4 TeV\(^{-1}\) to 0.9 TeV\(^{-1}\) [35]. Systematic uncertainties on the tracking performance lead to relative uncertainties on the mean values of \( \Sigma p_T \) and \( N_{\text{ch}} \) that vary with \( R \) from 2.1% (\( R = 0.2 \)) to 2.6% (\( R = 1.0 \)). Uncertainties on \( \bar{p}_T \) are below the percent level for all values of \( R \) and \( p_T^{\text{jet}} \).

The performance of the unfolding procedure is studied by unfolding the distributions measured in simulated MC control samples and comparing them to the known generator-level distributions. These closure tests have been performed using all the simulated samples described in Sec. III. In each case, before the test is performed, the input MC sample is reweighted so that the truth distributions of \( p_T^{\text{jet}} \) and of the observable \( O \) reproduce the unfolded distributions in the data. The maximum deviations on the mean value of \( O \) are lowest (1%–1.5%) at low \( p_T^{\text{jet}} \) and increase to 4%–6% at large \( p_T^{\text{jet}} \) for all three observables.

At least three effects can result in differences between the leading reconstructed jet and the true leading jet. One possibility is that a jet with \( p_T^{\text{jet}} < 4 \) GeV or with \( |\eta^{\text{jet}}| > 1.5 \) is reconstructed to be inside the acceptance (“feed-in” jets). Another effect is that due to differences in the distributions of true and reconstructed particles the anti-\( k_t \) algorithm, when applied to the reconstructed data, produces jets that do not match any jets obtained when the algorithm is applied to true particles (“accidental jets”). A third possibility is that a nonleading jet is identified as a leading jet due to resolution smearing and inefficiencies in the track reconstruction. The unfolding procedure intrinsically corrects for migration into the fiducial region. Residual uncertainties on the contribution from misidentification of the leading jet have been assessed by reweighting the simulation to reproduce the observed distributions of the subleading \( p_T^{\text{jet}} \) and the azimuthal angle between the leading and subleading jet, and applying the unfolding procedure to the reweighted sample. Changes in the resulting output from the unfolding differ from the default by \(< 1\%\). Studies with simulated data indicate that the rate for accidental jets is below 0.1% for all values of \( R \) and \( p_T^{\text{jet}} \). Therefore, the systematic uncertainty due to accidental jets is judged to be negligible. The systematic uncertainty on the fraction of nonleading jets that are misidentified as the leading jet due to uncertainties in the tracking efficiency is already included in the tracking systematic uncertainty described above.

Systematic uncertainties due to discretization effects (finite bin size) have been studied using simulated data by comparing the mean calculated from the binned data to the mean calculated from unbinned data. The differences are below 0.5% for all observables and all values of \( R \).

The sensitivity to the number of iterations used for unfolding is determined by comparing the baseline results to those obtained when the number of iterations is varied. Changes in the unfolded results are below 0.5% for all the observables.

The response matrix is derived using a particular MC sample; therefore, it depends on the topology of the event and track \( p_T \) spectrum of the event generator and tune. The sensitivity of the result to differences between the baseline MC sample and the data have been studied by comparing the baseline results to those obtained when the data are...
unfolded using an alternative response matrix constructed after the MC sample has been reweighted to reproduce the unfolded \( p_T^{\text{jet}} \) and UE observables. Relative differences between the baseline measurements and those obtained with the reweighted response matrix are below 0.25% for all three observables. The effects of statistical uncertainties in the response matrix are evaluated using the bootstrap method [36] to create 50 statistically independent samples of the reweighted MC simulation and repeating the unfolding procedure on the data for each sample. The RMS (relative to the baseline) of the resulting ensemble of unfolded results is less than 0.1%.

When comparing the mean values of UE observables for different values of \( R \), the correlations among the systematic uncertainties must be properly treated. Uncertainties due to track reconstruction efficiency and due to discretization effects are fully correlated among the measurements and thus do not contribute to the systematic uncertainty on the ratio of the mean responses measured for different \( R \). Uncertainties due to unfolding are partially correlated. The systematic uncertainties on the ratios of UE observables for different values of \( R \) are determined from the deviations from the baseline ratios, of the ratios obtained from MC samples where the input spectra are varied concurrently for all jet collections. The uncertainties on the ratios are typically below 1.5% except for the highest bin in \( p_T^{\text{jet}} \), where the uncertainty on the ratio of \( R = 0.2 \) to \( R = 0.6 \) rises to 6% for \( \Sigma p_T \) in the transverse region.

The same events are used to reconstruct all the jet collections; therefore, the statistical uncertainties are also correlated among the measurements. The statistical uncertainties on the ratio of the observables measured with one value of \( R \) to those measured with a different \( R \) are obtained by applying a bootstrap method to the data.

**VIII. MEASUREMENTS OF UE DISTRIBUTIONS**

The dependence on \( p_T^{\text{jet}} \) of the mean values of the unfolded \( \Sigma p_T \), \( N_{\text{ch}} \), and \( \bar{p}_T \) distributions is shown in Figs. 2–4, respectively. The dependence is shown for all five values of \( R \) for the transverse region. To facilitate comparisons with previous measurements, these mean values are reported as densities per unit \( \eta \)-\( \phi \). Therefore, the mean values of \( \Sigma p_T \) and \( N_{\text{ch}} \) are divided by \( 2\pi = \Delta \phi \times \Delta \eta \), where \( \Delta \phi = 2\pi/3 \) (\( \pi/3 \leq |\Delta \phi| \leq 2\pi/3 \)) and \( \Delta \eta = 3 \) (\( -1.5 \leq \eta \leq 1.5 \) contributes \( \Delta \eta = 3 \)).

The qualitative behavior of the distributions is the same for all five \( R \) values. The mean values of \( \Sigma p_T \) rise rapidly with \( p_T^{\text{jet}} \) for low \( p_T^{\text{jet}} \) and continue to rise slowly for high \( p_T^{\text{jet}} \). The mean values of \( \bar{p}_T \) exhibit qualitatively similar behavior as those of \( \Sigma p_T \). The mean value of \( N_{\text{ch}} \) rises rapidly with \( p_T^{\text{jet}} \) for low \( p_T^{\text{jet}} \) and approaches a plateau for high \( p_T^{\text{jet}} \). The systematic differences in the measurements as \( R \) is varied are discussed in Sec. IX.

The unfolded data are compared to several MC generators and tunes. In general, the level of agreement between the data and MC samples is reasonable, with differences below 20% for all observables and all \( p_T^{\text{jet}} \) bins. The Pythia 6 Z1 sample reproduces the mean values of \( \Sigma p_T \) within uncertainties for all \( p_T^{\text{jet}} \) bins. This MC sample tends to slightly overestimate \( N_{\text{ch}} \) for \( p_T^{\text{jet}} \geq 15 \text{ GeV} \), and this manifests itself as a slight underestimation of \( \bar{p}_T \) in the same \( p_T^{\text{jet}} \) range. The Pythia 6 AUET2B sample tends to slightly underestimate \( \Sigma p_T \) for \( p_T^{\text{jet}} \approx 20 \text{ GeV} \), and overestimate \( \Sigma p_T \) at higher \( p_T^{\text{jet}} \). Pythia 6 AUET2B reproduces \( N_{\text{ch}} \) for \( p_T^{\text{jet}} \approx 15 \text{ GeV} \), and overestimates \( N_{\text{ch}} \) for \( p_T^{\text{jet}} \approx 15 \text{ GeV} \). This MC sample slightly underestimates the mean values of \( \bar{p}_T \) in all \( p_T^{\text{jet}} \) bins. Pythia 6 Perugia2011 exhibits reasonable agreement with the data for \( \Sigma p_T \) distributions, having tendencies to underestimate the data at low \( p_T^{\text{jet}} \) and overestimate it for \( p_T^{\text{jet}} \approx 15 \text{ GeV} \). This MC sample tends to overestimate \( N_{\text{ch}} \) and slightly underestimate \( \bar{p}_T \). The other tunes show somewhat worse agreement for all distributions. Pythia 8 tune 4C underestimates all three observables, although the agreement is better for \( \bar{p}_T \). Herwig ++ tune UE7-2 underestimates the \( \Sigma p_T \) and \( N_{\text{ch}} \). The Pythia 6 Perugia 2011 NOCR tune is disfavored by the \( \bar{p}_T \) data.

Figs. 5–7 show the unfolded distributions \( (1/N_{\text{ev}})dN_{\text{ev}}/d\Sigma p_T \), \( (1/N_{\text{ev}})dN_{\text{ev}}/dN_{\text{ch}} \), and \( (1/N_{\text{ev}})\times dN_{\text{ev}}/d\bar{p}_T \) in the transverse region for three representative values of \( R \) and for low (5–6 GeV) and high (31–50 GeV) bins of \( p_T^{\text{jet}} \). Here \( N_{\text{ev}} \) is the number of events in the sample with \( p_T^{\text{jet}} > 4 \text{ GeV} \) and \( |\eta^{\text{jet}}| < 1.5 \). The Pythia 6 Z1 tune shows differences with respect to the data of less than 20%–30% for most distributions and \( p_T^{\text{jet}} \) bins. The Pythia 6 AUET2B shows discrepancies of up to a factor of 2 for the \( \Sigma p_T \) and \( N_{\text{ch}} \) distributions at large values of \( p_T^{\text{jet}} \). For \( p_T^{\text{jet}} = 5 \text{ GeV} \), the Perugia 2011 tune undershoots the data for \( R = 0.2 \) by 30%–75% for \( N_{\text{ch}} \geq 20 \) and by 20%–80% for \( \Sigma p_T \geq 20 \text{ GeV} \). The differences are smaller for \( p_T^{\text{jet}} = 30 \text{ GeV} \) and for large \( R \) values Herwig ++ show an excess of events at low \( \Sigma p_T \) and low \( N_{\text{ch}} \) for small \( p_T^{\text{jet}} \); at high \( p_T^{\text{jet}} \) it does a reasonable job of predicting the shape of the distributions but underestimates the normalization of \( \Sigma p_T \) and \( N_{\text{ch}} \) distributions by about 50%.

The measured distributions in the away region, together with MC comparisons, are shown in the Appendix. The \( \Sigma p_T \), \( N_{\text{ch}} \), and \( \bar{p}_T \) all continue to rise with \( p_T^{\text{jet}} \), as expected. This behavior indicates the presence of a second jet recoiling against the leading jet.

**IX. DEPENDENCE OF THE UE ON \( R \)**

The distributions of the UE observables change with the value of \( R \) used in the jet reconstruction. The variations are
FIG. 2 (color online). The mean value, per unit $\eta \cdot \phi$, of $\Sigma p_T$ in the transverse region, as a function of $p_T$ for (a) $R = 0.2$, (b) $R = 0.4$, (c) $R = 0.6$, (d) $R = 0.8$, and (e) $R = 1.0$. The shaded band shows the combined statistical and systematic uncertainty on the data. The data are compared to the predictions obtained with Pythia 6 using the AUET2B and Z1 tunes. The bottom insert shows the ratio of MC predictions to data for several recent MC tunes.
FIG. 3 (color online). The mean value, per unit $\eta\phi$, of $N_{ch}$ in the transverse region, as a function of $p_T^{jet}$ for (a) $R = 0.2$, (b) $R = 0.4$, (c) $R = 0.6$, (d) $R = 0.8$, and (e) $R = 1.0$. The shaded band shows the combined statistical and systematic uncertainty on the data. The data are compared to the predictions obtained with Pythia 6 using the AUET2B and Z1 tunes. The bottom insert shows the ratio of MC predictions to data for several recent MC tunes.
FIG. 4 (color online). The mean value of $\bar{p}_T$ in the transverse region, as a function of $p_T^{jet}$ for (a) $R = 0.2$, (b) $R = 0.4$, (c) $R = 0.6$, (d) $R = 0.8$, and (e) $R = 1.0$. The shaded band shows the combined statistical and systematic uncertainty on the data. The data are compared to the predictions obtained with Pythia 6 using the AUET2B and Z1 tunes. The bottom insert shows the ratio of MC predictions to data for several recent MC tunes.
FIG. 5 (color online). Distributions of $\Sigma p_T$ in the transverse region for (a) $R = 0.2$ and $5 \text{GeV} \leq p_T^{\text{jet}} < 6 \text{GeV}$, (b) $R = 0.2$ and $31 \text{GeV} \leq p_T^{\text{jet}} < 50 \text{GeV}$, (c) $R = 0.6$ and $5 \text{GeV} \leq p_T^{\text{jet}} < 6 \text{GeV}$, (d) $R = 0.6$ and $31 \text{GeV} \leq p_T^{\text{jet}} < 50 \text{GeV}$, (e) $R = 1.0$ and $5 \text{GeV} \leq p_T^{\text{jet}} < 6 \text{GeV}$, and (f) $R = 1.0$ and $31 \text{GeV} \leq p_T^{\text{jet}} < 50 \text{GeV}$. The shaded band shows the combined statistical and systematic uncertainty on the data. The histograms show the predictions of several MC models with the same legend as in (a) and also Figs. 2–4.
FIG. 6 (color online). Distributions of $N_{\text{ch}}$ in the transverse region for (a) $R = 0.2$ and $5 \text{ GeV} \leq p_{\text{T}}^{\text{jet}} < 6 \text{ GeV}$, (b) $R = 0.2$ and $31 \text{ GeV} \leq p_{\text{T}}^{\text{jet}} < 50 \text{ GeV}$, (c) $R = 0.6$ and $5 \text{ GeV} \leq p_{\text{T}}^{\text{jet}} < 6 \text{ GeV}$, (d) $R = 0.6$ and $31 \text{ GeV} \leq p_{\text{T}}^{\text{jet}} < 50 \text{ GeV}$, (e) $R = 1.0$ and $5 \text{ GeV} \leq p_{\text{T}}^{\text{jet}} < 6 \text{ GeV}$, and (f) $R = 1.0$ and $31 \text{ GeV} \leq p_{\text{T}}^{\text{jet}} < 50 \text{ GeV}$. The shaded band shows the combined statistical and systematic uncertainty on the data. The histograms show the predictions of several MC models with the same legend as in (a) and also Figs. 2–4.
FIG. 7 (color online). Distributions of $p_T$ in the transverse region for (a) $R = 0.2$ and $5 \text{ GeV} \leq p_T^{\text{jet}} < 6 \text{ GeV}$, (b) $R = 0.2$ and $31 \text{ GeV} \leq p_T^{\text{jet}} < 50 \text{ GeV}$, (c) $R = 0.6$ and $5 \text{ GeV} \leq p_T^{\text{jet}} < 6 \text{ GeV}$, (d) $R = 0.6$ and $31 \text{ GeV} \leq p_T^{\text{jet}} < 50 \text{ GeV}$, (e) $R = 1.0$ and $5 \text{ GeV} \leq p_T^{\text{jet}} < 6 \text{ GeV}$, and (f) $R = 1.0$ and $31 \text{ GeV} \leq p_T^{\text{jet}} < 50 \text{ GeV}$. The shaded band shows the combined statistical and systematic uncertainty on the data. The histograms show the predictions of several MC models with the same legend as in (a) and also Figs. 2–4.
summarized in Fig. 8, which compares the results obtained for the observables in the transverse region for $R = 0.2$, 0.6, and 1.0. For low $p_T$, the mean values of the $\sum p_T$ and $N_{ch}$ densities are largest for the smallest value of $R$, while they are largest for the highest value of $R$ at high $p_T$. In contrast, the mean value of $\bar{p}_T$ in the transverse region shows little variation with $R$.

As noted in Sec. I, the phenomenological description of jet production and the UE is complex. This is especially true in the low $p_T$ region where the distinction between the hard scattering process and the soft physics associated with the beam remnants is an artifact of the model used to parametrize this physics. Nevertheless, several general features of jet production are useful for interpreting the observed $R$ dependence of the UE observables. For example, the inclusive jet cross section depends on $R$. Also, leading jets obtained with different $R$ parameters will not in general have the same reconstructed centroid position, resulting in differences in the definitions of the transverse and away regions. Furthermore, the amount of transverse momentum collected in a jet increases with the value of $R$ used for the reconstruction.

Measurements of the inclusive cross section for jets reconstructed from tracks show that this cross section increases significantly as the radius parameter $R$ is increased [15]. Both the Z1 and AUET2B tunes of Pythia 6 do a remarkably good job of reproducing the measurements therein. The number of jets reconstructed in the

![Graphs and diagrams showing the mean values of observables as a function of $p_T^\text{jet}$ for different $R$ values.](image)

**FIG. 8 (color online)**. The mean value of (a) $\sum p_T$ (per unit $\eta - \phi$), (c) $N_{ch}$ (per unit $\eta - \phi$), and (e) $\bar{p}_T$ in the transverse region as a function of $p_T^\text{jet}$ for $R = 0.2$, $R = 0.6$, and $R = 1.0$; because the systematic uncertainties are correlated among the different $R$ values, only statistical uncertainties are shown, and the ratio of the mean value of (b) $\sum p_T$, (d) $N_{ch}$, and (f) $\bar{p}_T$ in the transverse region measured for $R = 0.2$ and $R = 1.0$ to that measured for $R = 0.6$. The shaded bands show the total uncertainty. The lines show the predictions of Pythia 6 with the Z1 tune; predictions for AUET2B show comparable agreement.
The difference in azimuthal angle between the leading jet reconstructed with $R = 0.2$ and the leading jet reconstructed with $R = 1.0$ has been studied as a function of $p_T^{\text{jet}}$. These studies demonstrate that event reorientation effects due to changes in the reconstructed position of the leading jet for different values of $R$ are small. For $p_T^{\text{jet}} \approx 4$ GeV, 7% of events are reoriented by $\pi/3 \leq |\Delta \phi| \leq 2 \pi/3$. For $p_T^{\text{jet}} \geq 15$ GeV the effect is much smaller; less than 1% of events are reoriented.

For cases where jets reconstructed with different $R$ parameters are matched, the $p_T$ of the jet reconstructed with larger $R$ will exceed that of the jet reconstructed with smaller $R$, leading to migration of events to bins with higher $p_T^{\text{jet}}$. Many physical processes influence the amount of migration as the radius parameter increases. These effects include the collection of additional fragmentation particles, the inclusion of additional hadrons produced via soft gluon radiation from the final-state parton, and the sweeping of particles from the UE into the jet cone. Attempts to compensate for the observed $R$ dependence by correcting $p_T^{\text{jet}}$ using the average UE energy deposited within the jet cone were unsuccessful. This might be due to the fact that there is a correlation between the amount of $p_T$ migration and the level of UE activity in the event because UE activity exhibits long-range correlations in $|\eta\phi|$. Events with higher UE activity will exhibit larger $p_T$ migration as $R$ is increased. Thus, the ability of the MC generators to model the variation of the UE with $R$ depends not only on how well the generator reproduces the mean UE response, but also on how well it models the fluctuations in the UE and how correlated these fluctuations are spatially.

X. CONCLUSION

Observables sensitive to UE activity in events containing one or more charged-particle jets produced in $pp$ collisions at $\sqrt{s} = 7$ TeV have been measured. The properties of the UE activity have been studied both in the transverse and away regions. The jets are reconstructed with the anti-$k_T$ algorithm, with a radius parameter $R$ varying between 0.2 and 1.0. Measurements of the evolution of the UE activity with $R$ are also presented. Predictions from several MC tunes have been compared to the data. The predictions from Pythia 6 based on tunes that have been determined using LHC data, namely, Z1, AUET2B, and Perugia 2011, show reasonable agreement with the data, not only for the mean event activity but also for fluctuations in UE activity within events. Other tunes, such as Perugia 2011 NOCR, are disfavored by the data. The comparison of the predictions from Pythia 8.145 tune 4C and the Herwig $+$ $+2.5.1$ UE7-2 tune to the data indicates that additional tuning of UE parameters is necessary in these cases. The measurements presented here provide a testing ground for further development of the Monte Carlo models.

APPENDIX: UE DISTRIBUTIONS IN THE AWAY REGION

The dependence on $p_T^{\text{jet}}$ of the mean value of $\Sigma p_T^{\text{jet}}$, $N_{\text{ch}}$, and $p_T^{\text{jet}}$ for all five values of $R$ is shown in Figs. 9–11 for the away region. The $\Sigma p_T^{\text{jet}}$, $N_{\text{ch}}$, and $p_T^{\text{jet}}$ values all continue to rise with $p_T^{\text{jet}}$. The away region is expected to have smaller

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10 GeV

The dependence on $p_T^{\text{jet}}$ of the mean value of $\Sigma p_T^{\text{jet}}$, $N_{\text{ch}}$, and $p_T^{\text{jet}}$ for all five values of $R$ is shown in Figs. 9–11 for the away region.
FIG. 9 (color online). The mean value, per unit $\eta \cdot \phi$, of $\Sigma p_T$ in the away region, as a function of $p_T^{\text{jet}}$ (a) for $R = 0.2$, (b) for $R = 0.4$, (c) for $R = 0.6$, (d) for $R = 0.8$, and (e) for $R = 1.0$. The shaded band shows the combined statistical and systematic uncertainty on the data. The data are compared to the predictions obtained with Pythia 6 using the AUET2B and Z1 tunes. The bottom insert shows the ratio of MC predictions to data for several recent MC tunes.
The mean value, per unit $\eta$-$\phi$, of $N_{\text{ch}}$ in the away region, as a function of $p_T^{\text{jet}}$ (a) for $R = 0.2$, (b) for $R = 0.4$, (c) for $R = 0.6$, (d) for $R = 0.8$, and (e) for $R = 1.0$. The shaded band shows the combined statistical and systematic uncertainty on the data. The data are compared to the predictions obtained with Pythia 6 using the AUET2B and Z1 tunes. The bottom insert shows the ratio of MC predictions to data for several recent MC tunes.
FIG. 11 (color online). The mean value of $\bar{p}_T$ in the away region, as a function of $p_T^{\text{jet}}$ (a) for $R = 0.2$, (b) for $R = 0.4$, (c) for $R = 0.6$, (d) for $R = 0.8$, and (e) for $R = 1.0$. The shaded band shows the combined statistical and systematic uncertainty on the data. The data are compared to the predictions obtained with Pythia 6 using the AUET2B and Z1 tunes. The bottom insert shows the ratio of MC predictions to data for several recent MC tunes.
FIG. 12 (color online). Distributions of $\mathcal{S}p_T$ in the away region for (a) $R = 0.2$ and $5 \text{ GeV} \leq p_T^{\text{jet}} < 6 \text{ GeV}$, (b) $R = 0.2$ and $31 \text{ GeV} \leq p_T^{\text{jet}} < 50 \text{ GeV}$, (c) $R = 0.6$ and $5 \text{ GeV} \leq p_T^{\text{jet}} < 6 \text{ GeV}$, (d) $R = 0.6$ and $31 \text{ GeV} \leq p_T^{\text{jet}} < 50 \text{ GeV}$, (e) $R = 1.0$ and $5 \text{ GeV} \leq p_T^{\text{jet}} < 6 \text{ GeV}$, and (f) $R = 1.0$ and $31 \text{ GeV} \leq p_T^{\text{jet}} < 50 \text{ GeV}$. The shaded band shows the combined statistical and systematic uncertainty on the data. The histograms show the predictions of several MC models. The bottom insert shows the ratio of the MC predictions to the data.
FIG. 13 (color online). Distributions of $N_{ch}$ in the away region for (a) $R=0.2$ and $5 \text{ GeV} \leq p_{T}^{\text{jet}} < 6 \text{ GeV}$, (b) $R=0.2$ and $31 \text{ GeV} \leq p_{T}^{\text{jet}} < 50 \text{ GeV}$, (c) $R=0.6$ and $5 \text{ GeV} \leq p_{T}^{\text{jet}} < 6 \text{ GeV}$, (d) $R=0.6$ and $31 \text{ GeV} \leq p_{T}^{\text{jet}} < 50 \text{ GeV}$, (e) $R=1.0$ and $5 \text{ GeV} \leq p_{T}^{\text{jet}} < 6 \text{ GeV}$, and (f) $R=1.0$ and $31 \text{ GeV} \leq p_{T}^{\text{jet}} < 50 \text{ GeV}$. The shaded band shows the combined statistical and systematic uncertainty on the data. The histograms show the predictions of several MC models. The bottom insert shows the ratio of the MC predictions to the data.
FIG. 14 (color online). Distributions of $p_T$ in the away region for (a) $R = 0.2$ and $5 \text{ GeV} \leq p_T^{\text{jet}} < 6 \text{ GeV}$, (b) $R = 0.2$ and $31 \text{ GeV} \leq p_T^{\text{jet}} < 50 \text{ GeV}$, (c) $R = 0.6$ and $5 \text{ GeV} \leq p_T^{\text{jet}} < 6 \text{ GeV}$, (d) $R = 0.6$ and $31 \text{ GeV} \leq p_T^{\text{jet}} < 50 \text{ GeV}$, (e) $R = 1.0$ and $5 \text{ GeV} \leq p_T^{\text{jet}} < 6 \text{ GeV}$, and (f) $R = 1.0$ and $31 \text{ GeV} \leq p_T^{\text{jet}} < 50 \text{ GeV}$. The shaded band shows the combined statistical and systematic uncertainty on the data. The histograms show the predictions of several MC models. The bottom insert shows the ratio of the MC predictions to the data.
\(\Sigma p_T\) than the towards region. This is mainly because the leading jet by definition has the highest summed transverse momentum and the distribution of the fraction of the momentum carried by charged particles is broad. For \(p_T^{\text{jet}} \geq 10\ \text{GeV}\), the mean \(\Sigma p_T\) contained in charged particles in the away region is typically between 60% (large \(p_T^{\text{jet}}\) and large \(R\)) and 100% (small \(p_T^{\text{jet}}\) and small \(R\)) of the leading jet \(p_T\). Herwig ++ overestimates \(p_T\) for \(p_T^{\text{jet}} \geq 10\ \text{GeV}\). Pythia 6 Perugia 2011 (without color reconnection) underestimates \(p_T\) for \(p_T^{\text{jet}} \leq 40\ \text{GeV}\).

Figures 12–14 show the unfolded distributions \((1/N_{ev}) dN_{ev}/dp_T\), \((1/N_{ev}) dN_{ev}/d\eta_{\text{ch}}\), and \((1/N_{ev}) \times dN_{ev}/d\eta_{\text{jet}}\) in the away region for three representative values of \(R\) and for low (5–6 GeV) and high (31–50 GeV) bins of \(p_T^{\text{jet}}\). Here \(N_{ev}\) is the number of events in the sample with \(p_T^{\text{jet}} > 4\ \text{GeV}\) and |\(\eta_{\text{jet}}\)| < 1.5. Most of the MC models reproduce the shapes of the distributions reasonably, with Pythia 6 Z1 and Perugia 2011 providing the best agreement. Pythia 6 AUET2B predicts values of \(\Sigma p_T\) and \(N_{\text{ch}}\) that are higher than the data at large \(p_T^{\text{jet}}\).

[3] ATLAS uses a right-handed coordinate system with its origin at the nominal interaction point in the center of the detector and the z axis along the beam pipe. The x axis points from the interaction point to the center of the LHC ring, and the y axis points upward. Cylindrical coordinates (\(r, \phi\)) are used in the transverse plane, being the azimuthal angle around the beam pipe. The pseudorapidity is defined in terms of the polar angle \(\theta\) as \(\eta = -\ln(\tan(\theta/2))\). The transverse momentum \(p_T\) is defined as \(p_T = \sqrt{E^2 - m^2 \sin^2(\theta)}\), where \(E\) is the total energy and \(m\) is the mass.
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