Design and Vibration Testing of a Flexible Seal Whisker Model

by

Christopher D. Gerber

Submitted to the
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ABSTRACT

Harbor seal whiskers have a unique surface structure that dramatically reduces vortex induced vibrations as they move through the water. Concurrently with rigid whisker experiments, this project focuses on the design and testing of a flexible model. The rubber model was cast with integrated Kevlar strings, for tensioning purposes, and accelerometers to measure vibration data. The whisker model was mounted to the carriage in the MIT tow tank where it could be towed at a variety of speeds and tension settings. Accelerometer data clarity was a significant problem, but gradual improvements to the whisker mounting design allowed higher quality data to be gathered at a larger range of towing speeds. Using this data we observed correlations between towing speed, vibration frequency, g forces, and displacement in the whisker's vertical axis of motion. Further work could be done to examine whisker motion in multiple axes, as well as with different angles of attack.

Thesis Supervisor: Michael S. Triantafyllou
Title: Professor of Mechanical and Ocean Engineering
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1. Introduction

Harbor seals use their mystacial vibrissae (whiskers) not only to sense through direct contact, but also to detect disturbances in the water. It is believed that based on the whisker vibrations, they can perform hydrodynamic trail following in addition to aiding orientation. This would allow them to catch prey. Actual seals have been shown to be able to follow objects underwater while blindfolded and wearing earmuffs. It is hypothesized that the harbor seal is particularly adept at this because their whiskers experience very little interference due to their own shape moving through the water. When the whiskers do encounter a flow disturbance, the resulting vibrations are then more noticeable.

Close-up pictures reveal that seal whiskers are not actually cylindrical as one might think. The whiskers have an undulated elliptical structure (Figure 1-1). Current experiments in the MIT Towing Tank suggest that this shape is specialized to reduce vibrations caused by vortex shedding, or Vortex Induced Vibrations (VIV), as the whisker moves through the water. Experiments to date have only employed rigid whisker models to attempt to understand their behavior. The problem with this, of course, is that whiskers are not rigid, so a rigid apparatus will not comprehensively model the behavior.

This portion of the research focuses on a flexible whisker model. The fabrication was carried out by casting rubber in a 6’ mold made from machinable wax. The flexible whisker has integrated accelerometers, and it can be tensioned using Kevlar strings. The vibrational response has been measured over different tension and speed settings. These findings provide more accurate biological understanding of how such a structure responds on the real seals. It also has applications in the advancement of underwater sensors. Finally, this work will help designers of marine risers determine the usability of the whisker geometry as a VIV reduction mechanism.
1.1 Seal whisker morphology

The University of Rostock group first proposed the whisker geometry's vibration suppression in their paper [1]. This article talks in detail about seal behavior, training, their methodology, and our main point of interest: the whisker's structure. Using head mounted cameras, the researchers filmed vibrissa behavior during hydrodynamic trail following tests and took whisker samples for examination under a microscope.

Figure 1-1: Close up views of harbor seal (A,B) and sea lion (C,D) whiskers. [1]

Images A and B show the frontal and dorsal views of a harbor seal whisker respectively. Images C and D show the frontal and dorsal views of a California sea lion whisker, which does not have the undulating surface structure of interest. The Rostock group used their observations to generate the geometric description of the whisker in Figure (1-2).
From the article: “Parameters of the idealized vibrissa surface model. M, the half-period of the undulation, equals 0.91mm. a and b, the radii of the vibrissal cross-section in the laterally wide location, equal 0.595mm and 0.24mm, respectively. K and l, the radii of the vibrissal cross-section in the laterally narrow location, equal 0.475mm and 0.29mm, respectively. The connecting lines between the minima and maxima of the undulation on the rostral and caudal edges of the vibrissa, and thus the directions in which a and k were measured, were found not to be perpendicular to the vibrissal axis but oriented at angles α(15.27deg) and β(17.60deg), as indicated.” [1]

Heather Beem used these numbers to create a Solidworks model of the whisker. All future whisker models are based on the dimensions specified by the Rostock group and are simply scaled in size based on the application.
1.2 Previous work

There has been a significant amount of research done in past years in the area of Vortex Induced Vibrations. Researchers have worked with cylinders in flexible and rigid forms. M. Zdravkovich experimented with various shapes in an effort to reduce VIV and drag including helical strakes shown in the image below (a). Unfortunately, while this feature suppressed VIV, it increased drag.

![Image of various additions to cylinders](image)

Figure 1-3: Various different additions to cylinders to try to reduce VIV [6]

Other experiments have been done with cylinders featuring surface bumps. These have been able to reduce vortex shedding by up to 20%, but like the helical strakes, these increased drag.

To date, no geometry has been found to both reduce VIV and drag. Hopefully the whisker geometry's will be able to do so. [6]
1.2.1 Rigid Whisker Experiments

Prior to and simultaneously with this work, are experiments with rigid whisker models [2,3]. The current model is connected to strain gauges which show the whisker vibrations caused by vortex induced vibrations. Experiments have also been conducted to see how the rigid whisker is affected by the wake from another object. This was done by mounting the rigid whisker at various locations behind another structure. Unlike the flexible whisker, whose mounting scheme will be discussed in detail later, the rigid whisker apparatus extends vertically into the water. This helps keep vital electronics dry and ensure the strain gauges are not affected by the weight of the whisker body.

1.2.2 Flexible Structures

The area of flexible structures has also been explored before, and past research has shown that flexible and rigid structures behave very differently. Long underwater pipes or cylindrical structures often behave like flexible structures despite being made out of metal. This is because their length-to-hydraulic diameter ratio is usually very large, so the vortex induced vibrations these structures experience can cause them to flex enormously. Previous experiments have looked at ways to mitigate these vibrations through the addition of various elements on the surface of the cylinder such as helical strakes, streamlined covers, spoiler plates, splitters, etc...

1.3 Flexible Whisker Introduction

The purpose of the flexible whisker is to model the flexible characteristics to eventually combine with the rigid whisker model. The flexible whisker is an incomplete model because it is
attached at both ends rather than cantilevered like a real seal whisker. The cantilevered aspect will be modeled with a much smaller scale rigid whisker.

1.4 Design Requirements

There were a large number of design criteria for the flexible whisker. It needed to be placed in the Tow Tank horizontally so that the boundary conditions at both ends were the same. The whisker should be tested under various tensions, which changes the natural frequency. The model should contain sensors, which are embedded to avoid external devices, which would disturb the flow. The purpose of these is to measure the vibrations at different points along the whisker. Ideally, the accelerometers need to be small enough to fit inside the whisker and not greatly affect the local flexibility. Based on the smallest available size of accelerometers, the diameter of the model was chosen 1.89” crossflow direction and 4.59” in the in line direction. Based on the length of the existing mount used to hold flexible cylinders, previously tested in our lab [4,5], the corresponding length of the whisker model was chosen to be 6’.

The boundary conditions at each end of the whisker were also the subject of concern. A simply supported boundary condition would be the most ideal for modeling purposes, but rigid supports would be easier to build and implement. Extensive discussion and design iterations relating to whisker mounting will be addressed later.
2. Mold Design Process

The rigid whiskers were manufactured using stereolithography, which is an additive manufacturing process similar to 3D printing. This manufacturing method is very fast, but it expensive and most resins for stereo-lithography are expensive to buy in large amounts. Additionally, stereolithography has a very limited ability to manufacture with flexible materials like rubber, and the available machines were not remotely close to the size chosen based on the above design constraints. Most machines are capable of a 24” range at the most, and machines with the range to manufacture 6’ parts are exceedingly rare and expensive.

Creating the molds using a CNC mill posed a similar problem. Most mills have a range of 48” at most and paying a company to machine two 6’ molds would be far too expensive. The only machine available with the adequate range to create these molds was the CNC router in the MIT Hobby Shop. The router has a 4’ by 8’ range, but it can only machine soft materials. Machinable wax was chosen for its consistency (as opposed to wood which has knots and other inconsistencies), resistance to temperature (for the casting process) and machinability. The largest continuous block of machinable wax available was 4’, and buying in that size was extremely expensive. Instead, buying 12” blocks was the best option. To make one side of the mold, 6 of the blocks could simply be lined up and machined as if they were a single 6’ block.

When the 12” long blocks arrived, they were all inconsistently sized so they had to be individually hand machined to be identical. After this the blocks were ready to be aligned and machined. In order to align and secure the blocks during machining, I created a jig out of plywood by routing a 6 inch wide groove into a ½ x 8 x 74 inch plank of plywood. The blocks were slid into place in the groove and screwed into place from the underside of the jig using 4
wood screws per block. This would ensure that the blocks would not become dislodged during machining. After the jig was assembled, it was screwed into the particle board that covers the surface of the CNC router table to keep the entire assembly from moving during machining.

Figure 2-1: Half of the whisker mold (post machining) attached to the router table and plywood alignment jig
2.1 Mastercam Toolpaths:

The toolpaths for the molds were generated using the Mastercam MX5 program. The procedure to generate the toolpaths started with importing the solid parts from Solidworks in the form of .DXF files. The next step was to delete all of the extraneous lines in the part, which includes every line that was not part of the surface loft or the top surface of the mold. In this part of the process it was also extremely important to delete all of the lines that separated each of the 6 machinable wax blocks so Mastercam would consider all of them one continuous block. This was important so that the toolpaths would not be interrupted as the transitioned from one block to the next.

![Figure 2-2: The Mastercam mesh of the mold surface is shown above. The neon blue represents the roughing and finishing toolpaths.](image)
2.1.1 Toolpath Details

The first toolpath was a facing toolpath done with a 1/2'' diameter flat end mill router bit. The purpose of this was to make sure the top faces of all 6 machinable wax blocks were level for the subsequent toolpaths. Although each block was hand machined to be identical, there were some irregularities in the plywood jig mentioned earlier. Because of this, some of the blocks sat at an angle in the jig and this called for the use of a facing toolpath. In general, it is good practice to do a facing toolpath before milling complex toolpaths so the router can be accurately zeroed.

The second toolpath was a roughing toolpath done with the same 1/2'' diameter flat end mill router bit. The purpose of the roughing toolpath was to remove the vast majority of the material but use a large enough step over in order to not take up too much time. Roughing toolpaths do not, however, mill down to the final level of the surface. They leave some material for the finishing toolpath.

The finishing toolpath was done with a 1/2'' diameter round end mill router bit. This toolpath removed the excess material left over from the roughing toolpath and left the surface mostly smooth. Finishing toolpaths typically use a very small step over to make sure the surface finish is smooth.

Before running these toolpaths for the first time on hundreds of dollars of machinable wax and many hours of jig assembly, I decided to conduct some test runs on pieces of wood. The results of a single roughing toolpath can be seen in the image below.
Figure 2-3: (Left) Ripples in the surface are still clearly visible in the mold because only the roughing toolpath was used. (Right) Both roughing and finishing toolpaths were used. There is a visible difference in surface smoothness from the finishing toolpath.

2.1.2 Toolpath Mirror Imaging

The second half of the mold needed to be a mirror image of the first side, so this provided an opportunity to save some time. Instead of importing the second solid part and re-programming the toolpaths from scratch, I used the mirror toolpath feature in Mastercam, which created the complimentary mold with one click. This obscure and seldom used command is very useful for expedited mold machining.

2.1.3 Toolpath Optimization

After creating the first mold there were some clear areas for improvement. The machining process took an extremely long time, and left a somewhat rough surface finish that would require extensive sanding. To decrease the machining time, I changed the end mill used in the facing and roughing toolpaths to a 1” flat end mill router bit. Using a much larger bit allowed me to increase the step over and significantly decrease the time of the facing and
roughing passes. To fix the surface finish problem, I increased the tracking speed of the router head, and decreased the step over. This ensured a smooth surface finish without an excessive time increase.

2.2 Mold Flexibility Problems

Due to the immense weight of the machinable wax blocks and the mold length, the plywood jig had severe deformation problems when it was removed from the router table after machining. The problem with this deformation is that it opened up the gaps between each machinable wax block. This would cause severe leaking problems during the casting. In order to remedy this, I installed metal L brackets connecting the jig to the blocks to increase the mold’s rigidity. The use of metal brackets, however, caused a thread stripping problem when the screws were driven into the machinable wax blocks. On the second half of the mold, 2x4’s were used with wood screws instead of metal brackets to alleviate the thread stripping problem. After the molds were machined, extensive sanding was needed to ensure a smooth surface finish. Even the refined finishing toolpath left a ripple effect from the rounded router bit.

2.3 End-bracket design

At each end of the mold there are end brackets that serve several purposes. They are machined out of ½ inch thick aluminum stock and measure 3” tall and 6” wide. The main purpose of the brackets is to hold the two sides of the mold together at the ends. Each bracket has 4 ¼ inch holes that match up with ¼ - 20 threaded holes in the machinable wax molds. The holes are also countersunk to accommodate the ¼ - 20 socket head screws. Each bracket has a 1” diameter center hole to accommodate T shaped cylindrical mounts. (these were not used in
Both brackets have 1/8 inch guide holes for the Kevlar strings that are positioned 1/16 inch to the right and left of the center holes. The top bracket has two more 1” holes to accommodate the pouring of rubber during the casting process. On the bottom bracket, there are two more 1/8 inch holes to allow airflow during casting.

Figure 2-5: The end bracket for the pouring side of the whisker mold
Figure 2-6: Solidworks image showing how the mold, jig, and end brackets connect
3. Whisker Features

3.1 Accelerometers

There were a number of factors that came into play when we chose accelerometers to put inside the whisker. We anticipated that the "g" forces experienced by the whisker would be relatively low, so an accelerometer with a large range would not be necessary. It would be far more ideal to buy an accelerometer with a small range but high precision. It would also be important to measure vertical, horizontal, and lengthwise vibrations in the whisker so the accelerometers would need to measure 3 axes simultaneously.

By far the most pressing concern, however, was size and weight. If the accelerometer was too big or too heavy, it would impact the behavior of the whisker and skew the data. Another concern with size was the structural integrity of the whisker. Based on the density of the rubber, we knew that a 6' whisker would be around 25-30 lbs and large accelerometers inside the whisker could pose a tearing problem within the rubber.

Luckily, the Kistler 8688A5 accelerometer met all of these needs. The 8688A5 has a range of +/- 5g's, and a sensitivity of 1000 mV/g. It measures in 3 axes, weighs only 7 grams, and is a ½ inch per side cube. For comparison, the whisker is approximately 2" thick and 4" wide, so the accelerometer would have almost no impact on the structural strength. Additionally, the average density of the accelerometer is 84 lbs/ft^3 while the density of the rubber is approximately 70 lbs/ft^3. Because these densities are relatively comparable, the weight of the accelerometer would have very little impact on the whisker's behavior. This combination of size, weight, and sensitivity made the accelerometer ideal for application in the flexible whisker. Conveniently, these new Kistler accelerometers were compatible with the 4 channel couplers/power supplies already mounted on the tow tank carriage, so this saved a significant
amount of money. These power supplies are the Kistler 5010B and the data sheet is shown in the appendix. The accelerometers are connected to the power supplies with single 4 pin cable that splits to 3 BNC inputs.

3.1.1 Accelerometer Mounting

The 8688A5 accelerometers also have a threaded base that was very useful for mounting. We experimented with a few mounting schemes and conducted a practice run mounting the accelerometers in the middle of a casted piece of rubber. The picture below shows half of a small test mold milled out of machinable wax for the practice accelerometer mounting. To mount the accelerometer, a small segment of Kevlar string was clamped in the threaded base of the accelerometer. The Kevlar string was then pulled tight to and clamped in the mold to provide stability in one axis while the blue BNC connector cable was pulled tight to provide stability in the other direction. The rubber mixture was then poured into the enclosed mold shown in the image below.
Figure 3-1: The resulting block of rubber with the embedded accelerometer (shown above) served as a proof of concept for the Kevlar string mounting scheme which would be used in a modified manner later on the full scale mold.

Based on the signals measured from this setup, it was determined that the mounting scheme needed improvement to ensure more accurate alignment of the axes with the mold axes. Two Kevlar strings were run through the threaded clamp on the bottom of the accelerometers. These were pulled tight and screwed into the sides of the mold to ensure they were held tight for the casting process. This technique reduced the movement significantly from when the accelerometer was mounted on a single Kevlar string, however they still had a tendency to rock forward and backward, twisting both strings. To reduce this problem, brackets were 3D printed (Figure 3-2) to fit around the accelerometer casing and extend to the surface of the whisker mold. This added a third axis of stability for the accelerometer mounts and significantly reduced rotational movement. The red substance in the image below is wax used to waterproof the
connection between the accelerometer and BNC cable. All 3 accelerometers were mounted in the mold in this fashion and the BNC cables were threaded sequentially out one end of the whisker mold.

Figure 3-2: Center accelerometer mounted in preparation for casting
3.2 Kevlar Strings

Kevlar strings were also integrated inside the structure of the whisker. The strings were used to tension the whisker differently, thus changing the natural frequency. Kevlar was chosen because of its low deformation under tension and high strength to size ratio. The size was a very important aspect because we did not want the composition of the whisker to be significantly impacted by the strings running through it. The Kevlar strings chosen were less than 1/16 inch thick and had a breaking strength of 200 lbs—well over the maximum tension we intended to place the whisker under. Two Kevlar strings were placed along the length of the Z axis (the long cross sectional axis) of the whisker, down the middle, and approximately 1 inch apart. This was done to allow for angle of attack changes in addition to providing stability. The Kevlar strings exited the whisker at each end, passed through holes in the mount, and interfaced with the turnbuckle spring tension system which will be explained in detail later.

3.3 Casting Process

Before attempting casting, there were a number of aspects that were important to consider and plan thoroughly. First, we would be mixing and pouring over 3 gallons of rubber, so it was important that the rubber’s setting time was not too fast so the rubber wouldn’t being setting in the buckets rather than in the mold. Second, the molds were very heavy ~100lbs, and would be even heavier with 3 gallons of rubber inside so we needed to think carefully about how to clamp it down. Third, how would the rubber actually be poured into the mold? The mold was 6’ high so there could be immense pressure at the bottom if casting was done vertically. This pressure could cause severe leaking and cause us to run out of rubber and have an unfinished whisker.
Because of this problem, we considered pouring the whisker horizontally using some sort of tube or syringe apparatus, but these seemed more difficult and risky than the vertical method.

In order to mitigate leaking, 16 through holes were drilled to secure each half of the mold to the other. The end brackets also helped with this purpose. Each gap between machinable wax blocks was also covered with duct tape to prevent leaking if the mold flexed. For similar casting projects in the future, it is not recommended to use duct tape to cover the gaps. While the duct tape did keep most of the leaks at bay, the tape’s thickness was enough that it caused irregularities in the whisker’s surface finish. Instead of duct tape, we would recommend using glue of some sort to seal the gaps, or coat the entire inside of the mold in some waterproof material.

Figure 3-3: One half of the mold with end brackets and accelerometers mounted in preparation for casting. Each gap between blocks is covered with duct tape.
Prior to casting, all of the rubber was mixed in large buckets. All of the rubber was poured into the mold vertically, taking special care not to pour a stream of rubber directly onto one of the accelerometers and possibly dislodge it. There was a copious amount of leaking from the bottom area of the mold, most likely due to the high pressure. This was mitigated by pouring extra rubber into the top of the mold. Eventually the rubber began curing and the leaks ceased. The whisker was allowed to cure for over 24 hours and was removed from the molds. Excess rubber attached to the whisker was removed and the whisker was ready for mounting.
4. Mount Design

4.1 Mount structure

The whisker mount is made out of stainless steel and is composed a 76” cylinder which terminates at each end with two vertical hydrofoils that extend down into the water. At the bottom of the hydrofoils, there are square mounting points which is where the Kevlar strings that come out of the ends of the whisker are threaded. The hydrofoils are hollow and have small holes in the bottom of each side to let water fill the hollow compartments. The purpose of this is to minimize the buoyancy force of the mount and the potential interference that this force could pose on the experimentation with the whisker.

Figure 4-1: Whisker mount with whisker attached
The whisker was designed with the length of this mount already in mind. As a result, there are 3” of leeway on each side of the whisker before the Kevlar strings reach the mounting points at the bottom of the hydrofoils.

The mount connects to the carriage using a large bracket system. This bracket is screwed into the ¼ - 20 threaded holes on the carriage, and the mount attaches to the bracket with 4 semicircular clamps around the top cylinder of the mount.

4.2 Initial Mounting Plan

Originally, the whisker was designed to have rigid cylinders embedded at the ends and partially protruding out in order to assist mounting. Aluminum tubes with cross pieces would be integrated with the whisker during casting. The end brackets were designed with center holes to account for these tubes and hold them in place during casting. The tubes were designed to protrude 3” from each end of the whisker and attach to a custom-made clamp system at the bottom of the hydrofoil whisker mount.

Figure 4-2: (Left) The clamping mechanism for one side of the whisker, and (right) the circular slot allowing free rotation of the whisker on the other side.
The benefit of this design was that it would allow for easy angle of attack adjustments during testing. However, the idea was discontinued because it constrained the ends of the whisker rigidly which negatively impacts the flexible behavior modeling. Instead, we opted for a mounting scheme that involving only the Kevlar strings. This meant the whisker was dynamically constrained at each end.

4.3 Revised Mounting Plan

The whisker mount needed to have a variable tensioning system and the capability to let the whisker flex freely due to vibrations. In order to design this mounting system, I consulted the flexible cylinder tow tank projects whose mount systems had similar capabilities [4,5].

The flexible cylinder project used a spring and screw rod mounted to one of the hydrofoils to tension the whisker. The screw rod allowed the cylinder to be set at a base level tension, and the spring allowed the cylinder to lengthen as a result of vibrations. This design could not be used for the flexible whisker because unlike the cylinders, the whisker has two Kevlar strings running through its center. These strings need to be kept horizontal for the whisker to stay level, so attaching them to a screw rod that would twist up the strings was not an option. So, a new tensioning system had to be designed.

The new mount design uses the same spring and screw principle with some alterations. The new system was designed with a spring on both sides of the whisker, so they can both move freely. The tensioning mechanisms were designed to mount to the sides of the hydrofoils in order to save space. A turnbuckle is attached to the top of each hydrofoil, which holds a spring
on each side underneath. The Kevlar strings attach to the bottom of the springs and are threaded through pulleys at the bottom of each hydrofoil.

Figure 4-3: The proof of concept mockup (shown above) is made with a wooden frame, small turnbuckles, and springs. The components are connected by a string, which stands in for the Kevlar strings and whisker.

4.3.1 Spring and turnbuckle selection

For the full scale model, the turnbuckles and springs were chosen carefully. The springs chosen were 6” extension springs with a maximum load of 55lbs. The turnbuckles were chosen for their large adjustment range of 3”. This would allow us to vary the tension significantly between experiments.
4.3.2 Spring Constant

As opposed to the flexible cylinder mount design, the new mounting scheme did not include a force gauge. In order to save costs, we opted not to buy an expensive force gauge and instead find the tension in the Kevlar strings by measuring the deformation of the springs. Before this strategy could be implemented we tested the spring deformation with a series of loads shown in the chart below.

<table>
<thead>
<tr>
<th>Weight (lbs)</th>
<th>Force (N)</th>
<th>Inches</th>
<th>X (m)</th>
<th>Deformation</th>
<th>Spring Constant</th>
</tr>
</thead>
<tbody>
<tr>
<td>10</td>
<td>44.5</td>
<td>4.5625</td>
<td>0.1159</td>
<td>0.0079</td>
<td>5632.911392</td>
</tr>
<tr>
<td>15</td>
<td>66.75</td>
<td>4.9375</td>
<td>0.1254</td>
<td>0.0174</td>
<td>3836.206897</td>
</tr>
<tr>
<td>20</td>
<td>89</td>
<td>5.3125</td>
<td>0.1349</td>
<td>0.0269</td>
<td>3308.550186</td>
</tr>
<tr>
<td>25</td>
<td>111.25</td>
<td>5.75</td>
<td>0.1461</td>
<td>0.0381</td>
<td>2919.947507</td>
</tr>
<tr>
<td>30</td>
<td>133.5</td>
<td>6.3125</td>
<td>0.1603</td>
<td>0.0523</td>
<td>2552.581262</td>
</tr>
<tr>
<td>35</td>
<td>155.75</td>
<td>6.5625</td>
<td>0.1667</td>
<td>0.0587</td>
<td>2653.321976</td>
</tr>
<tr>
<td>40</td>
<td>178</td>
<td>7.0625</td>
<td>0.1794</td>
<td>0.0714</td>
<td>2492.997199</td>
</tr>
<tr>
<td>55</td>
<td>244.75</td>
<td>8.1875</td>
<td>0.208</td>
<td>0.1</td>
<td>2447.5</td>
</tr>
</tbody>
</table>

Table 4-1: Plotting deformation with spring constant gave the equation needed to find the force based on any deformation.

\[ y = 1014.8x^{-0.338} \]

Figure 4-4: Graph of spring constant versus deformation
4.3.3 Implementation on the mount

To mount the tensioning system to each hydrofoil on the mount, I drilled through-holes and attached a bolt on each side. Each bolt extends an inch from the side of the hydrofoils, and they are the points where the entire tensioning system and whisker hang from. High strength lines are looped through the springs and tied to the bolts. The turnbuckles hang under the springs. The Kevlar strings, which extend from the ends of the whisker, are threaded into through-holes in the bottom of each hydrofoil. The Kevlar strings turn vertically after the through-holes and are tied to the bottom loop of the turnbuckle on each side.

![Figure 4-5: The proof of concept tensioning design (left) has the turnbuckle above the spring. For the full-scale rig (right) the spring and turnbuckle were switched because the Kevlar string could be attached to the turnbuckle more effectively.](image-url)
4.4 Troubleshooting Mount Problems

There were extensive problems with the Kevlar strings snapping caused from abrasion with the sharp metal edges of the mount. The first instance was caused by the small holes in the bottom of the mount where the Kevlar string pass through. This was fixed by enlarging the holes so the strings did not come in contact with the sides. The next instance was caused by the bottom edge of the hydrofoil, which rubbed the strings as the tension mechanism flexed. To remedy this, a small PVC pipe was used to alter the angle at which the strings exited the holes in the mount.

Figure 4-6: PVC Pipe attached to the bottom of the hydrofoils to prevent Kevlar strings from snapping.

The PVC material also allowed the strings to slide freely. Another mount problem was caused by springs rubbing on the sides of the hydrofoils, which impeded their motion when the whisker
needed to flex. This was remedied by the addition of pulleys, which served as spacers to move the variable tensioning system away from the hydrofoils.

![Image](image_url)

**Figure 4-7:** Pulleys mounted 6” from top of hydrofoils to prevent springs and turnbuckles from rubbing

While all previous snapping incidents occurred either out of the tank or during mounting, the strings experienced catastrophic failure during a 0.7 m/sec test run in the tank. The whisker had not yet been tested at this speed, and the Kevlar strings alone did not constrain the whisker enough for such a fast test. The whisker oscillated violently and turned so the broad side faced forward. This increased the drag immensely and snapped three of the four connections during the test. We learned two important lessons learned from this failure: increase testing speed gradually, and leave plenty of slack in the accelerometer cables. The second point is extremely important because the whisker could have pulled directly on the accelerometer BNC cables as it separated from the mount if there hadn’t been enough slack. Also, during high speed runs in
uncharted territory, it is a good idea to be ready to hit the stop button at any time if something goes wrong. This accident prompted a redesign of the whisker mounting components.

4.5 Final Mount Design

The central problem with the previous mounting strategies was that the whisker was only supported by the Kevlar strings. The whisker was mounted this way in order to have a simply supported boundary condition, but it was clear that the strings were not enough to keep the whisker stable while moving at high speeds. The solution was to create some sort of clamping mechanism on each end of the whisker that would support the weight of the whisker, while the Kevlar strings only purpose was to maintain tension. The first idea was to 3D print the clamps based on the Solidworks part shown below. The clamp would have the whisker surface geometry integrated so that it would be able to clamp very securely.

![Figure 4-8: Half the design for one of the new end clamps. The large hole in the back of the clamp is to accommodate the BNC accelerometer connectors and the Kevlar strings.](image-url)
Unfortunately, 3D printing these parts would have taken over 20 hours, which did not work with our timeframe, so we opted for a much simpler clamp design. The final design involved 2 simple metal brackets. The bottom of each bracket was screwed into the base of the hydrofoils with 2 \( \frac{3}{4}'' \)-20 screws. Four \( \frac{1}{4}'' \) through holes were drilled through the top and bottom pieces of each bracket. 3'' screws were used to tighten the brackets like a sandwich around each end of the whisker shown in the image below.

![Figure 4-9: Clamp mechanism tightened around the left end of the whisker](image)

These brackets have changed the end conditions of the whisker from simply supported to rigidly constrained, however, they have enabled us to tow the whisker at much higher speeds and achieve higher tensions on the whisker—both of which are improvements for the validity of our data. Shown below is the finalized design of the whisker, tensioning system, brackets, and mount.
Figure 4-10: Diagram of the mounted whisker and all components

Figure 4-11: Final whisker design mounted in the tow tank
5. Experiments and Discussion

5.1 Tests without clamps

Data was collected using Kistler accelerometers, which were connected to the Kistler amplifiers on the tow tank carriage. The data was recorded in Labview and analyzed in Matlab.

5.1.1 Varying Tension

The whisker was tested at different tensions and different speeds while it was only supported by the Kevlar strings. During these tests the bulk of the acceleration data is due to a swaying motion the whisker experienced because of the weak constraints. Shown below is a medium speed run.

![Acceleration Chart](image)

Figure 5-1: Whisker test run at 0.3 m/sec and tension of 105 N
This test run starts at around 12 seconds, the whisker is in motion until \(~54\) seconds, and the tapering of the data at the end of the run corresponds to some dissipating vibrations still present after the whisker has stopped. One noticeable aspect of this plot is the gradual taper of the magnitude of the data from beginning to end. This is caused by initial acceleration imparted to the whisker from the carriage. Because of the weak constraints of only the Kevlar strings, this initial acceleration caused a swaying motion in the center of the whisker that dominates the acceleration data. This gradual taper is from the swaying motion dying out over the course of the run. One way to decrease the swaying motion was to increase the tension in the Kevlar strings. The plot below shows a run at the same speed, but with the tension increased to 122 N.

![Figure 5-2: 0.3 m/sec run with 122 N of tension. There is no visible taper in this run because the higher tension has reduced the dominant swaying motion. It is important to note that although the taper is gone, the swaying motion is still present, just not as dominant.](image)
The presence of this swaying motion at lower tensions, along with the repeated snapping of the Kevlar strings is what prompted the redesign with the clamps.

5.1.2 Varying Speed

Testing the whisker vibrations at different speeds was also an area of interest. During testing without clamps there was a distinct trend for acceleration data. As the towing speed increased, the motion became more violent, again due to the loose constraints, so acceleration magnitudes scaled linearly with towing speed. Below is a plot of two runs—one at 0.2 m/sec and one at 0.3 m/sec—superimposed on each other.

![Figure 5-3: 0.3 m/sec run (blue) superimposed on 0.2 m/sec run (red). It is clear that the magnitudes of the accelerations for the 0.3 m/sec run are significantly larger.](image)

This trend holds for all of the runs without clamps because the swaying of the whisker is only exacerbated by the higher speeds. As mentioned earlier in the mount design section, the whisker sway got so violent at a test run of 0.7 m/sec that the whisker turned sideways (with the long axis...
of the elliptical cross section perpendicular to the direction of motion rather than parallel.) This increased the drag enormously and easily snapped the Kevlar strings. Shown below is a plot of the standard deviation of acceleration data at various speeds and tensions which shows the linear increase.

![Plot of Standard Deviation of Acceleration vs. Towing Speed](image)

Figure 5-4: The plot shows a clear linear correlation between Stdev of acceleration and towing speed due to the increasingly violent sway motions that occur as speed increases.

This swaying problem made it clear that in order to obtain reliable data, the whisker would need to be tensioned as much as possible. During all of these runs, there was a visible downward bow along the length of the whisker, however, the implementation of the clamps allowed for a much higher tension and elimination of the bowing problem.
5.2 Tests with clamps

In order to achieve high tension with the clamps, the Kevlar strings were tightened fully while the clamps were still open. After the string was under heavy tension, the screws through the clamps were tightened to take the load off the Kevlar strings. This way, the large load from the tension and the even more significant drag loads during high speed runs, were supported by the clamps. Shown below is the whisker under full tension with very little bow along the length.

![Whisker under high tension exhibits very little bowing](image)

Figure 5-5: Whisker under high tension exhibits very little bowing

5.2.1 Pluck Testing

The first step in testing the clamp-mounted whisker was conducting a pluck test. The purpose of the pluck test was to determine the natural frequency of the whisker with the damping from the water. To perform a pluck test, we simply pulled the whisker up approximately 6” and released. The whisker was allowed to oscillate until the vibrations died out. Shown below is the plot of the pluck test for the highest tension with the clamps.
The natural frequency of 1.196 Hz was found from the pluck test by plotting the power spectra using a Fourier transform shown below.

After approximating the data in Figure 5-6, with a 2nd order differential equation, and using the natural frequency from Figure 5-7, we found the damping ratio of the whisker in water to be...
0.112. This indicates that the whisker is under-damped which is very evident from the vibration data in Figure 5-6 because it is a damping ratio below 1.

Tests were run with the clamped whisker at speeds from 0.2 m/sec to 1.0 m/sec in increasing 0.1 m/sec increments. From that acceleration data, the power spectra was obtained for each run and the dominant frequencies plotted to compare with the whisker's natural frequency.

![Graph showing dominant frequencies](image)

Figure 5-8: The dominant frequencies during towing are all significantly higher than the natural frequency of 1.196 Hz. There is also an interesting drop in frequency at 0.8 m/sec suggesting another mode of vibration beginning at higher speeds.
5.3 Discussion

The Strouhal number is a dimensionless quantity that describes oscillation mechanics due to vortex shedding. It is defined as:

\[ St = \frac{fL}{V} \]

where \( f \) is the frequency of vortex shedding, \( L \) is the characteristic length (hydraulic diameter in this case) and \( V \) is the velocity of the flow (towing speed.) If we assume the vortex shedding frequency is comparable to the dominating frequency of one of the whisker runs, we can approximate the Strouhal number for a run at 0.5 m/sec to be 0.17. This Strouhal number is in the intermediate range, which is characterized by the buildup and rapid shedding of vortices. The desired Strouhal number at which we want to operate is \(-0.2\) so the optimal speed is just under 4.0 m/sec which gives a Strouhal number of 0.21.

The Strouhal number of 0.2 should result in the largest value of non-dimensionalized amplitude vs. reduced velocity. Reduced velocity is defined as:

\[ V_r = \frac{U}{fd} \]

where \( U \) is towing speed, \( f \) is frequency, and \( d \) is hydraulic diameter. When reduced velocity is plotted with \( A/d \), it results in a bell curve shape whose greatest \( A/d \) value occurs at a Strouhal number of 0.2. It was the goal of this project to tow the whisker at a variety of speeds, extract the amplitude from the acceleration data by integrating twice, and then try to recreate this bell curve. Using “cumtrapz” integrating function in Matlab, the acceleration was integrated to get velocity data. The problem with the velocity data was that it had a large time bias in the positive direction. To fix this, we fit a line to the data and subtracted the resulting line from the velocity data to get it centered around zero. The process was repeated again using the “cumptrapz”
function and removal of the time bias to get the displacement data. The Amplitude vs Velocity plot and 3 corresponding acceleration, velocity, and displacement plots are shown below.

Figure 5-9: From top to bottom: acceleration, velocity and displacement plots

Figure 5-10: Dimensionless amplitude vs. reduced velocity. Each data point is averaged from multiple runs at the same speed and there is no discernible bell curve trend.
We tried a variety of filters to clean up the accelerometer data including high pass and low pass filters, and data smoothing by averaging sets of data points. None of these approaches solved the integration error problem or the time bias so the data was integrated without a filter and the time bias was eliminated manually for each integral. In the future, the noise problem could be solved using more advanced filtering techniques, or by reducing the sampling rate of the accelerometers. The Kistler accelerometers sample at 800 points per second, which is much higher than what this project needs, and that makes the data difficult to handle in the analysis phase.

5.4 Conclusion

This project focused very heavily on the manufacturing and design side of the flexible whisker experiment. Even during data collection we learned three important lessons that related back to the design of the whisker and mount. First, the whisker needed to be under enough tension to be as close to horizontal as possible in order for the data to be reliable. Second, the whisker must be tested at a large variety of towing speeds in order to get an idea of the full spectrum of the Strouhal number bell curve. And third, the end conditions, which depend on how the whisker is mounted, play a very large role in the vibration behavior of the whisker. Each of these issues were resolved by mounting the whisker more rigidly and under higher tension. This project presented the unique challenge of mounting a large, heavy object that had to be towed at high speed. Hopefully researchers can learn from these many design iterations when mounting similar large structures in the future.

There is massive room for the expansion of this project. The area of most importance is to find displacement data that supports the dimensionless amplitude vs. reduced velocity bell
Further testing could be done through varying towing speed, tension, and angle of attack of the whisker. Testing different angles of attack, however, would require significant changes to the current mounting design. Additionally, the accelerometers measure vibrations in all 3 axes, but only the vertical axis was considered in this project. In addition to adding the other axes, there are two more accelerometers in the whisker—each at 1.5’ from the ends—which will complement the center accelerometer’s data and help us to gain a better understanding of the whisker’s behavior. There are numerous directions in which the flexible whisker research project could go, and I am excited to have developed a testing platform for extensive research in the future.
Bibliography


