

**1.021, 3.021, 10.333, 22.00 : Introduction to Modeling and Simulation : Spring 2011**

**Part II – Quantum Mechanical Methods : Lecture 8**

# **Applications in Energy: Introduction and Solar PV**

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“The purpose of computing is insight, not numbers.”

— Richard Hamming

*“What are the most important problems in your field? Are you working on one of them? Why not?”*

*“It is better to solve the right problem the wrong way than to solve the wrong problem the right way.”*

*“In research, if you know what you are doing, then you shouldn't be doing it.”*

*“Machines should work. People should think.”*

*...and related: “With great power comes great responsibility.” (Spiderman's Uncle)*

# Part II Outline

## theory & practice

1. It's A Quantum World: The Theory of Quantum Mechanics
2. Quantum Mechanics: Practice Makes Perfect
3. From Many-Body to Single-Particle; Quantum Modeling of Molecules
4. From Atoms to Solids
5. Quantum Modeling of Solids: Basic Properties
6. More on Band Structures and Modeling of Solids

7. Advanced Prop. of Materials: What else can we do?

## example applications

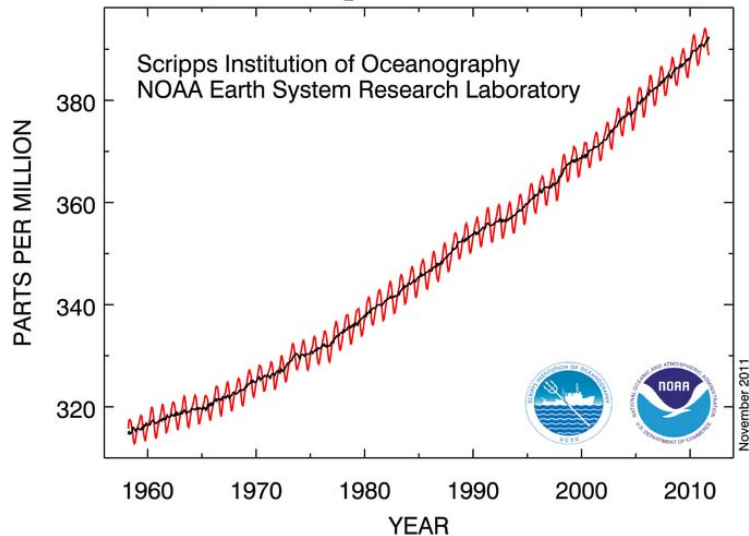
8. Solar Photovoltaics: Converting Photons into Electrons
9. Solar Fuels: Pushing Electrons up a Hill
10. Hydrogen Storage: the Strength of Weak Interactions
11. A bit of review for the quiz
12. Summary, concluding remarks, and free PIZZA!

# Cost of Inaction?

## Grinnell Glacier and Grinnell Lake, Glacier National Park, 1910-1997



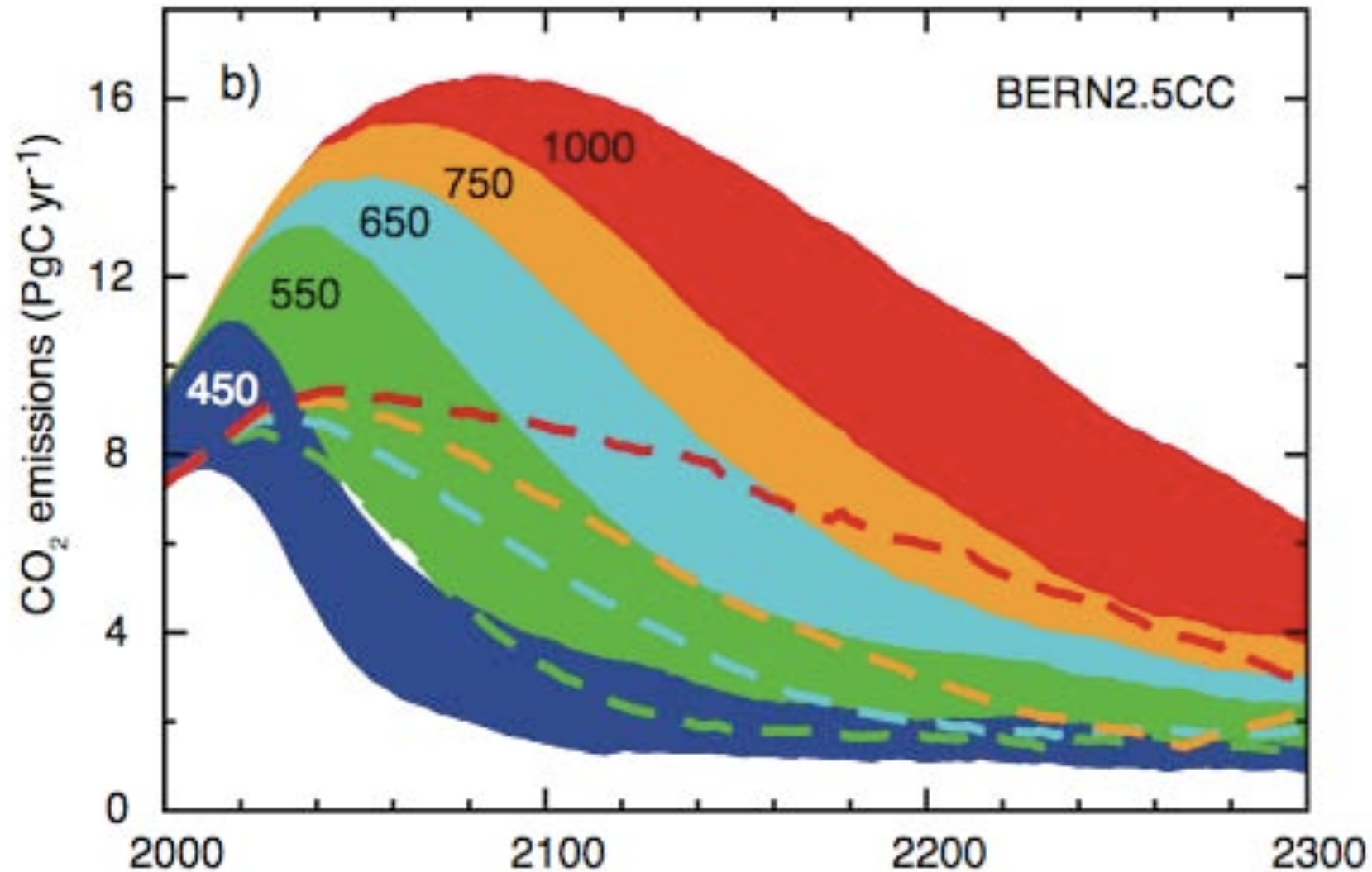
Atmospheric CO<sub>2</sub> at Mauna Loa Observatory



Graph by Dr. Pieter Tans, [NOAA/ESRL](#) and Dr. Ralph Keeling, [Scripps Institute of Oceanography](#).

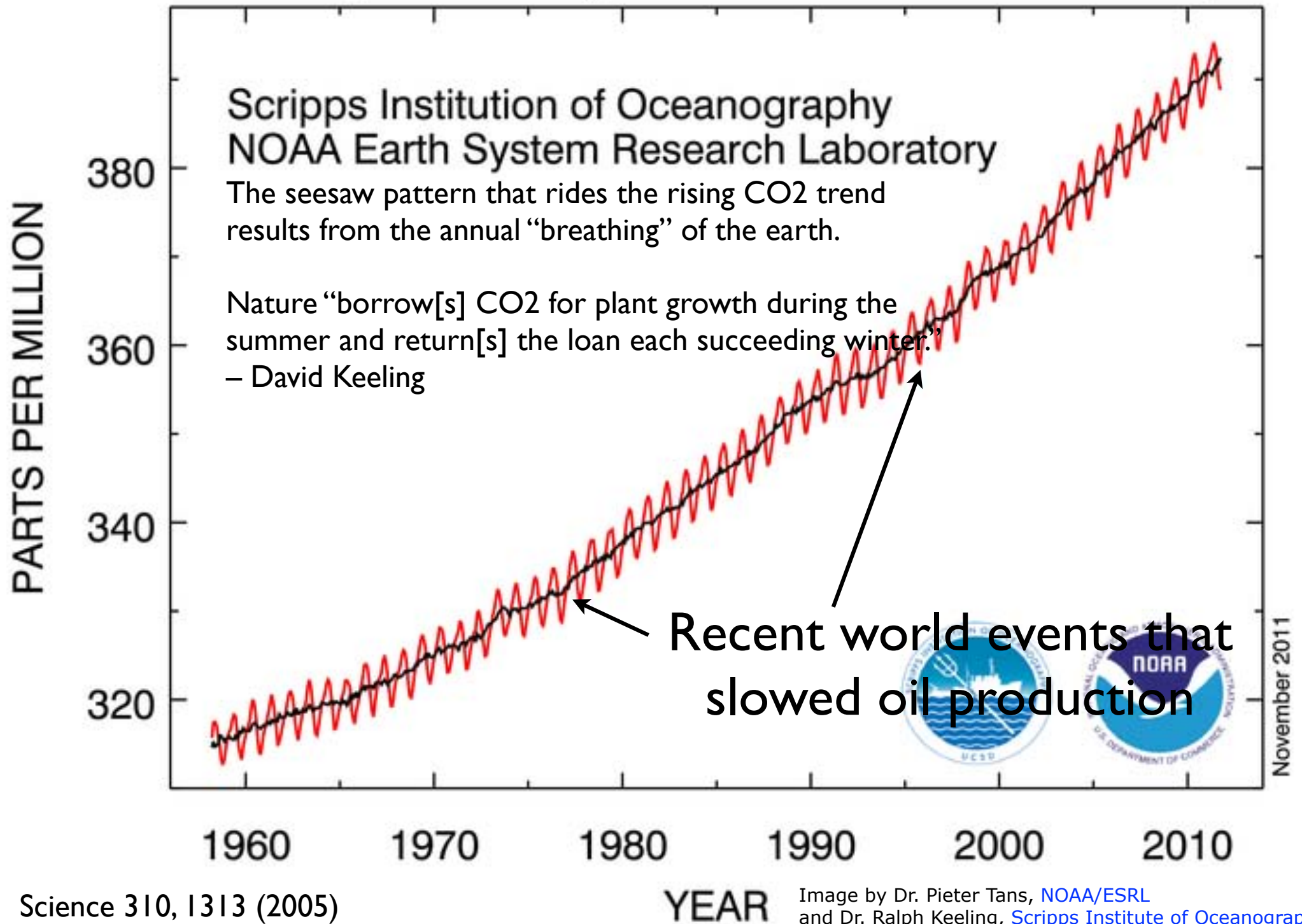
Photos by Fred Kiser, Glacier National Park Archives, and Daniel Fagre, USGS.

# CO<sub>2</sub> Projections



Source: Climate Change 2007: The Physical Science Basis. Contribution of Working Group I to the Fourth Assessment Report of the Intergovernmental Panel on Climate Change

# Atmospheric CO<sub>2</sub> at Mauna Loa Observatory



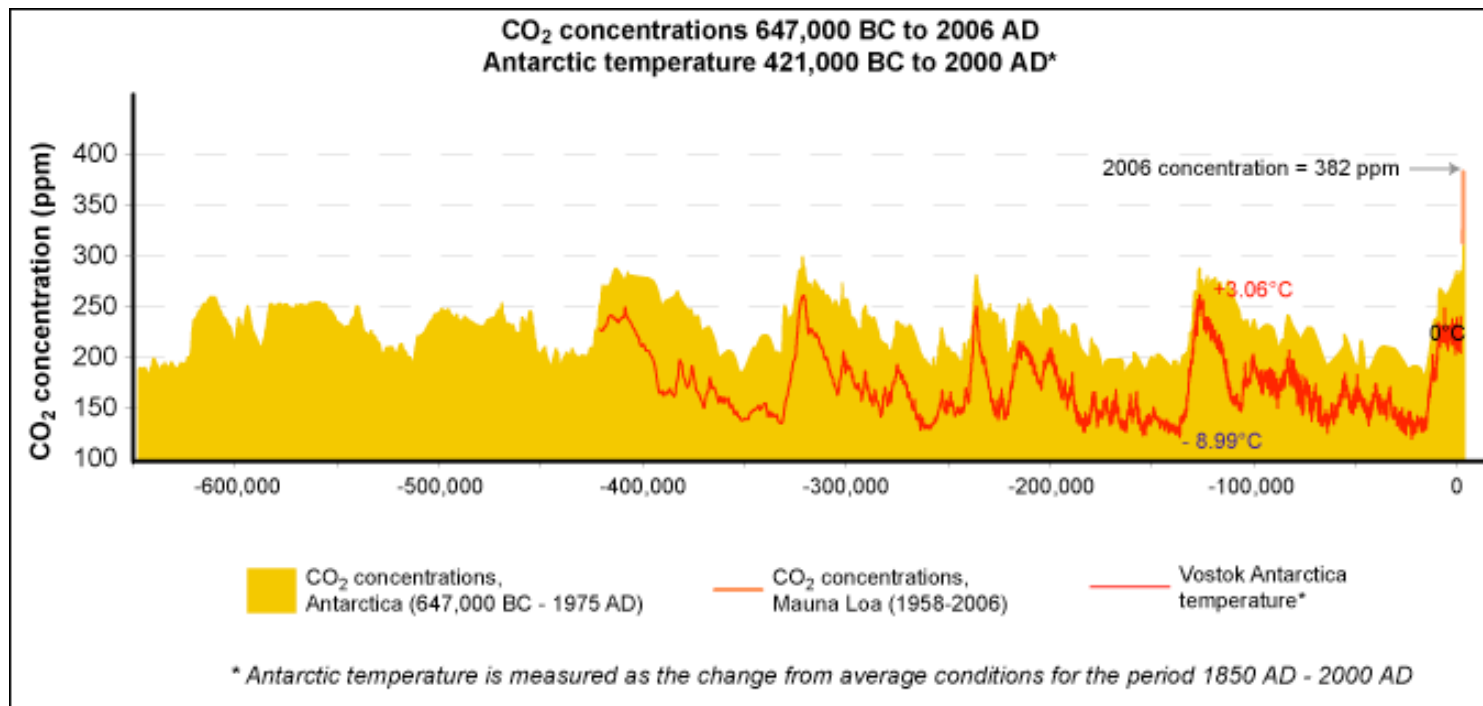
Science 310, 1313 (2005)

Image by Dr. Pieter Tans, [NOAA/ESRL](#)  
and Dr. Ralph Keeling, [Scripps Institute of Oceanography](#).

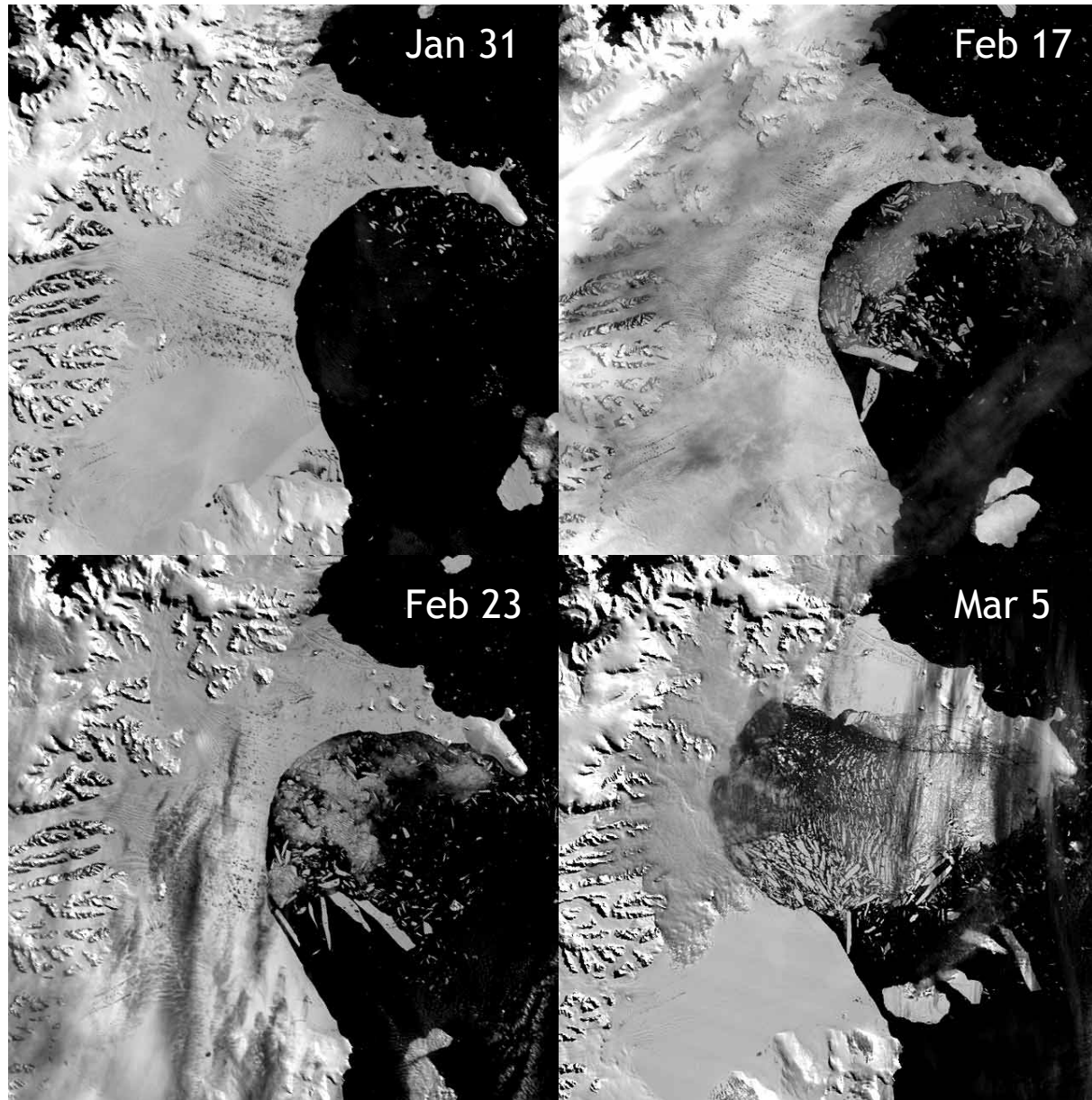


Temperature inferred from isotope ratios in the Vostok ice core

Carbon dioxide levels measured in the trapped air bubbles in the same core



# Warming is Real and Has Real Effects



Between Jan 31, 2002 and March 5, 2002 a chunk of the Larsen B ice shelf the size of Rhode Island disintegrated.

Images from NASA's Terra satellite, National Snow and Ice Data Center, University of Colorado, Boulder.



Surveys show the mountain pine beetle has infested 21 million acres and killed 411 million cubic feet of trees -- double the annual take by all the loggers in Canada. In seven years or sooner, the Forest Service predicts, that kill will nearly triple and 80 percent of the pines in the central British Columbia forest will be dead.

*The Washington Post, March 1, 2006*

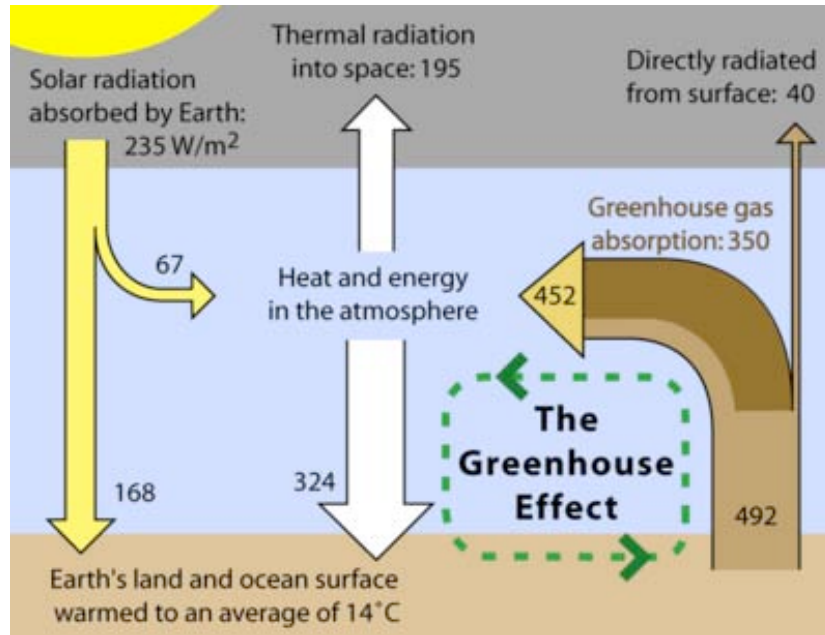


Image created by Robert A. Rohde / [Global Warming Art](http://ocw.mit.edu/fairuse). License: CC-BY-SA. This content is excluded from our Creative Commons license. For more information, see <http://ocw.mit.edu/fairuse>.

## Global Warming Projections

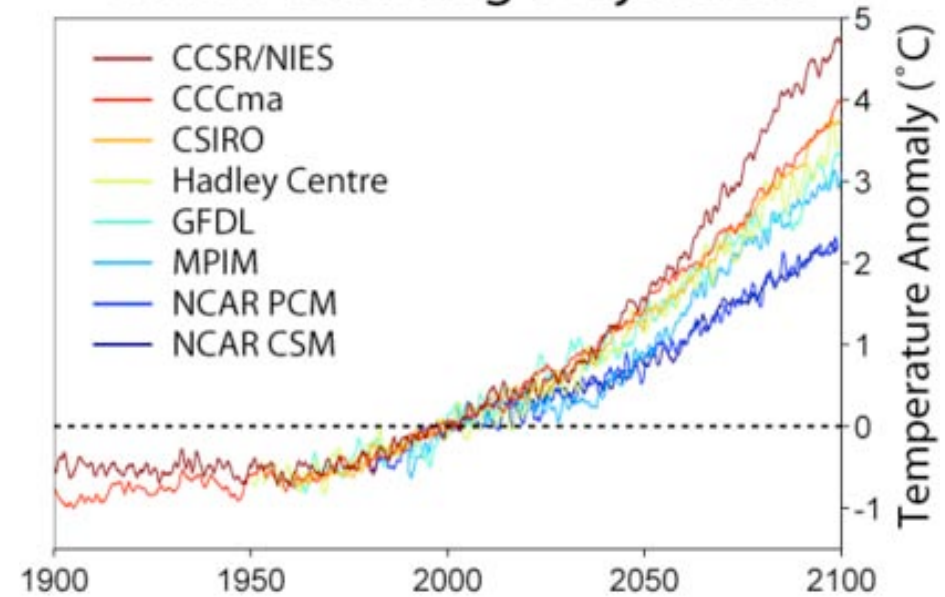
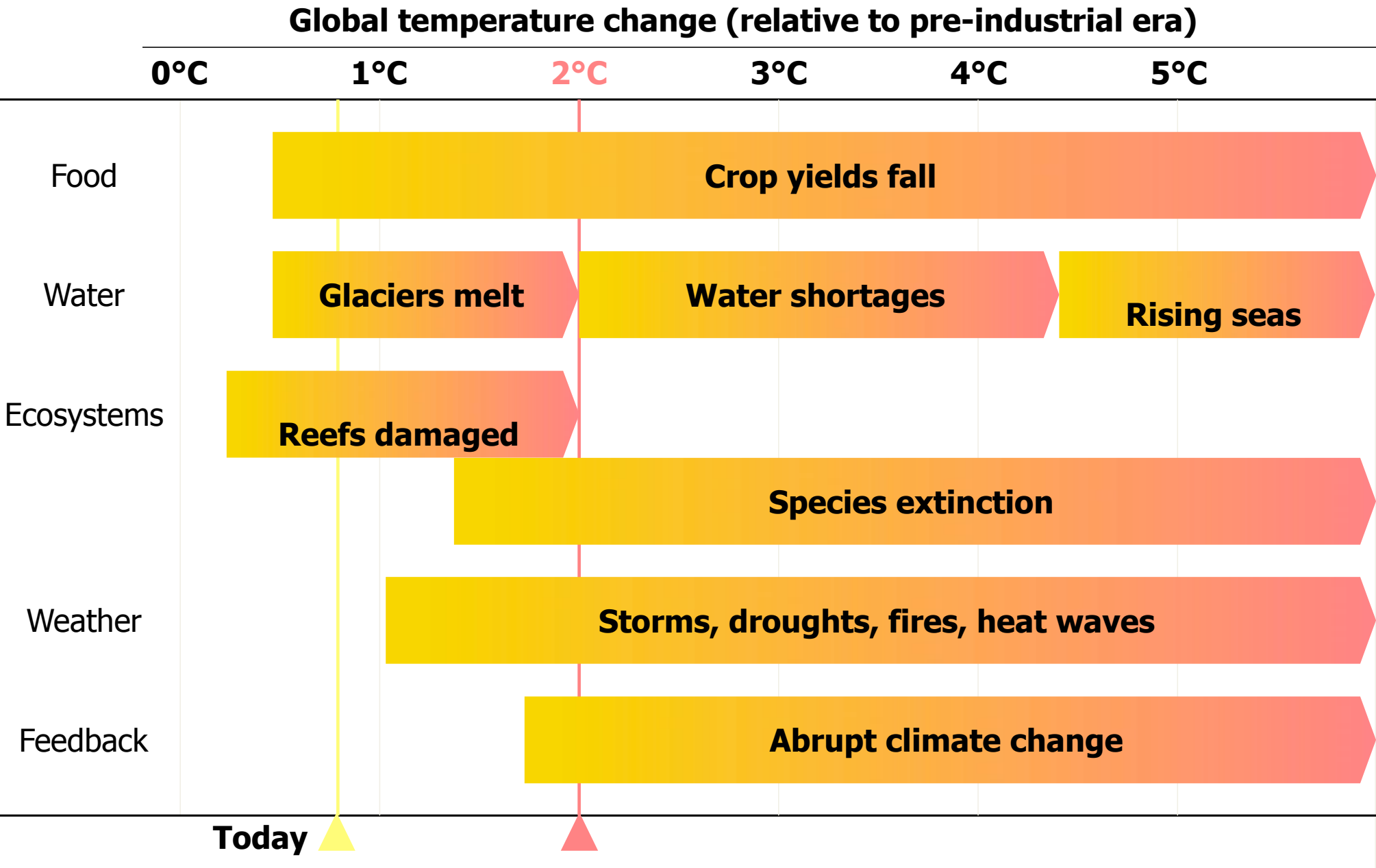


Image created by Robert A. Rohde / [Global Warming Art](http://ocw.mit.edu/fairuse). License: CC-BY-SA. This content is excluded from our Creative Commons license. For more information, see <http://ocw.mit.edu/fairuse>.

“I can get eight professors from MIT on both sides of this issue and no one in this room will walk away understanding what they said about climate change.”

— Charlie Baker, Candidate for  
Massachusetts Governor

# If warming exceeds 2°C, negative effects increase and catastrophic changes become more likely



Courtesy of Hal Harvey. Used with permission.

# It's Not *Only* About Warming: Abundance of Affordable Energy Resources Can Uplift the World

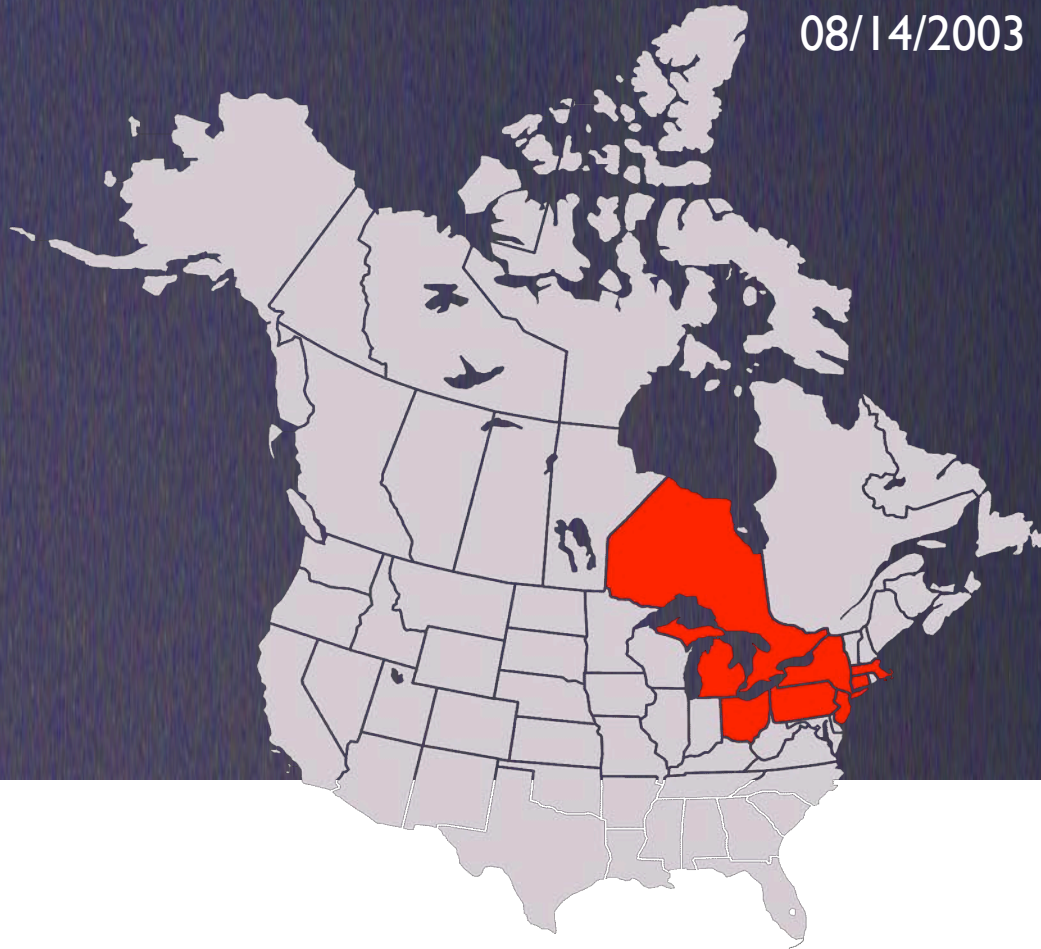
Image removed due to copyright restrictions. Please see Benka, Stephen G. "[The Energy Challenge](#)." *Physics Today* 55 (April 2002): 38-9.

**HUMAN WELL-BEING INCREASES WITH INCREASED PER-CAPITA ENERGY USE**

# It's Not *Only* About Warming: Abundance of Affordable Energy Resources Can Uplift the World

## North American Electrical Blackout

08/14/2003



... August 15 ...  
just 24 hours into blackout  
Air Pollution was Reduced

SO<sub>2</sub> >90%

O<sub>3</sub> ~50%

Light Scattering  
Particles ~70%

“This clean air benefit was realized  
over much of eastern U.S.”

Marufu et al., Geophysical Research  
Letters 2004



by 4:13 pm 256 power plants were off-line

Courtesy: Vladimir Bulovic

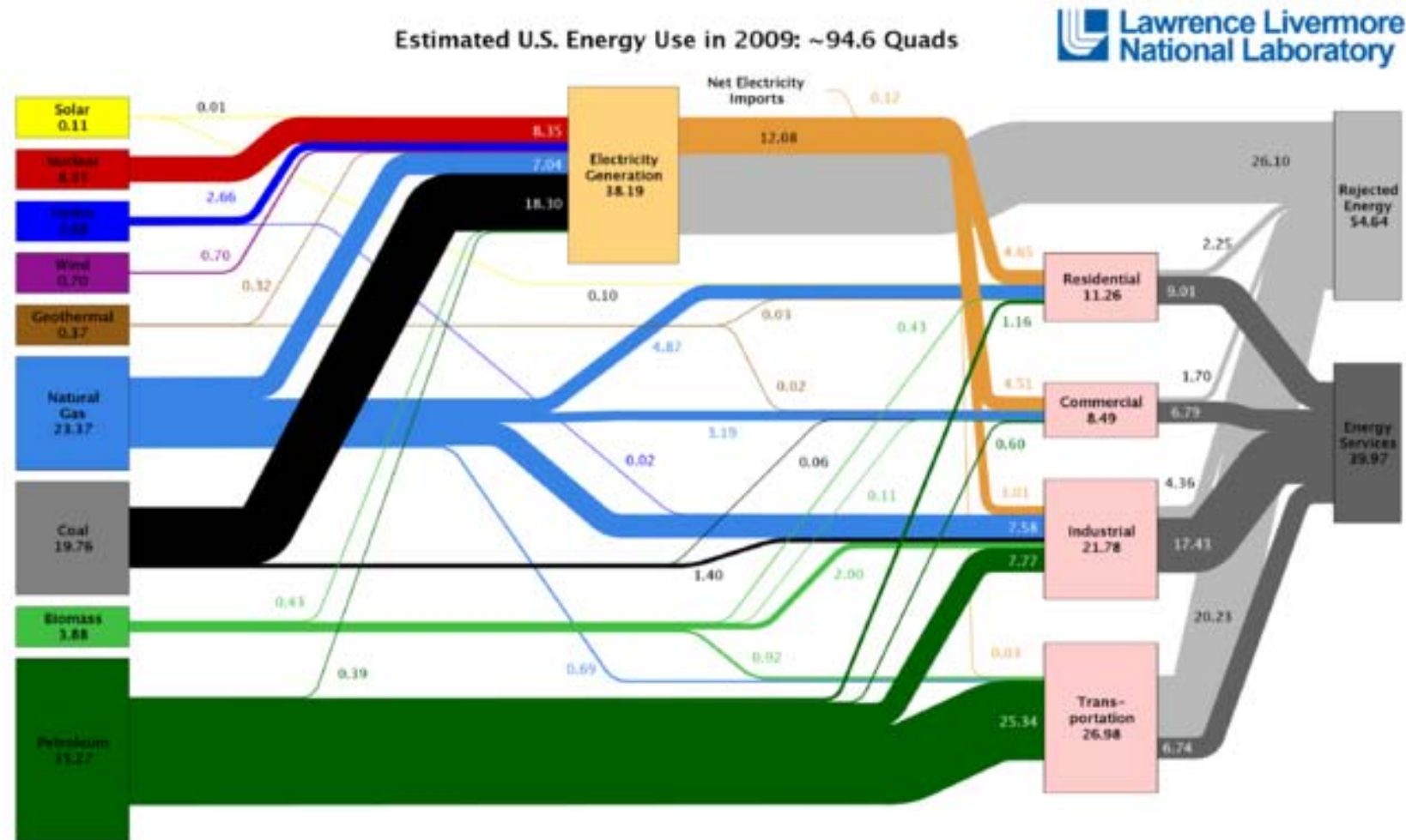
# Map of the World Scaled to Energy Consumption by Country



- In 2002 the world burned energy at a rate of 13.5 TW
- How fast will we burn energy in 2050?
- (assume 9 billion people)
- If we use energy like in U.S. we will need **102 TW**
- Conservative estimate: 28~35 TW

# U.S. Energy Consumption

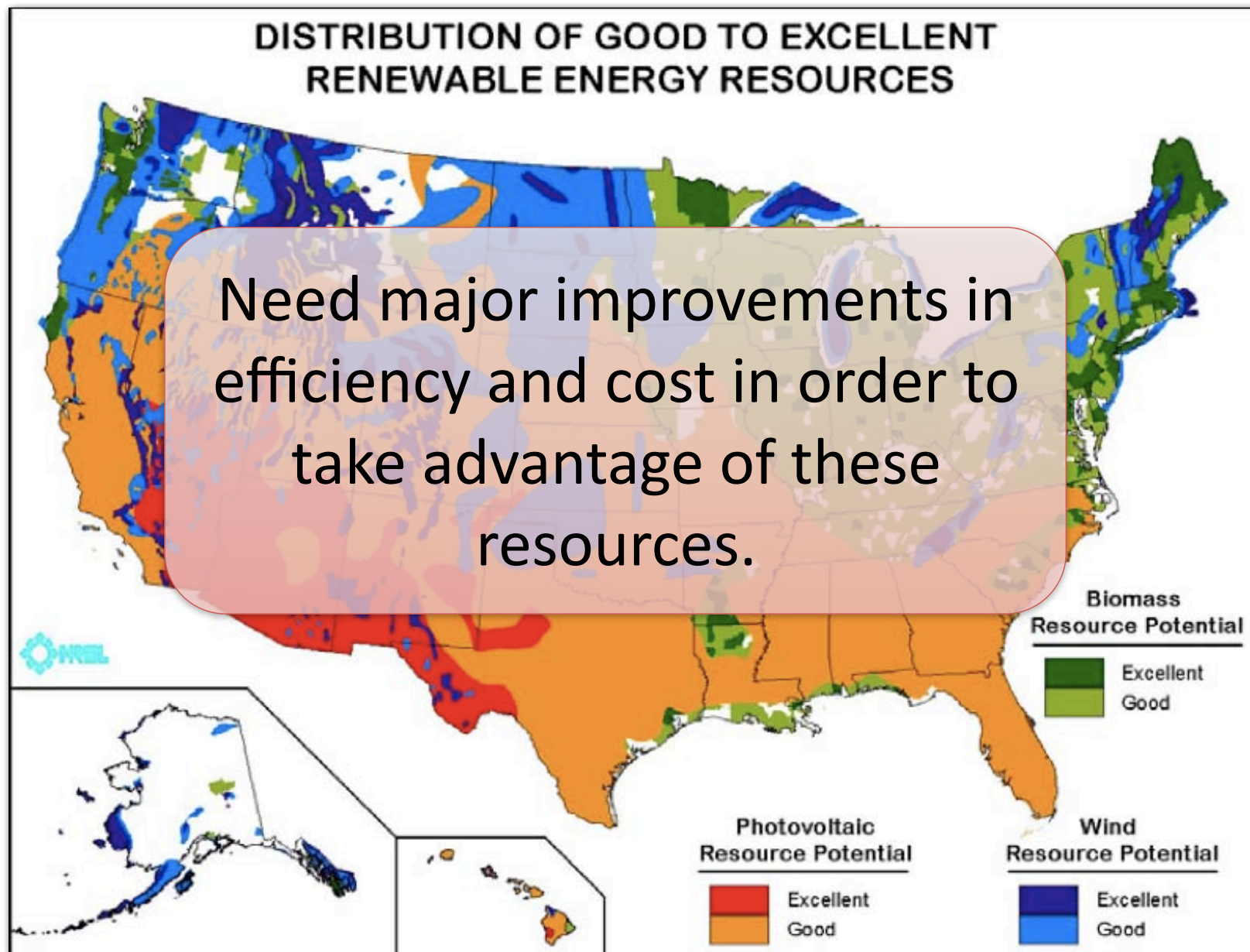
Goal: consume half of our electricity through renewable sources by the year 2050.



Source: LLNL, 2010. Data is based on DOE/EIA-0384(2009), August 2010. If this information or a reproduction of it is used, credit must be given to the Lawrence Livermore National Laboratory and the Department of Energy, under whose auspices the work was performed. Distributed electricity represents only retail electricity sales and does not include self-generation. EIA reports flows for non-thermal resources (i.e., hydro, wind and solar) in BTU-equivalent values by assuming a typical fossil fuel plant "heat rate." The efficiency of electricity production is calculated as the total retail electricity delivered divided by the primary energy input into electricity generation. End use efficiency is estimated as 80% for the residential, commercial and industrial sectors, and as 25% for the transportation sector. Totals may not equal sums of components due to independent rounding. LLNL-MI-410527



# U.S. Resources



# Energy from the Sun

- Energy released by an earthquake of magnitude 8 ( $10^{17}$  J):
  - the sun delivers this in one second
- Energy humans use annually ( $10^{20}$  J):
  - sun delivers this in one hour
- Earth's total resources of oil (3 trillion barrels,  $10^{22}$  J):
  - the sun delivers this in two days

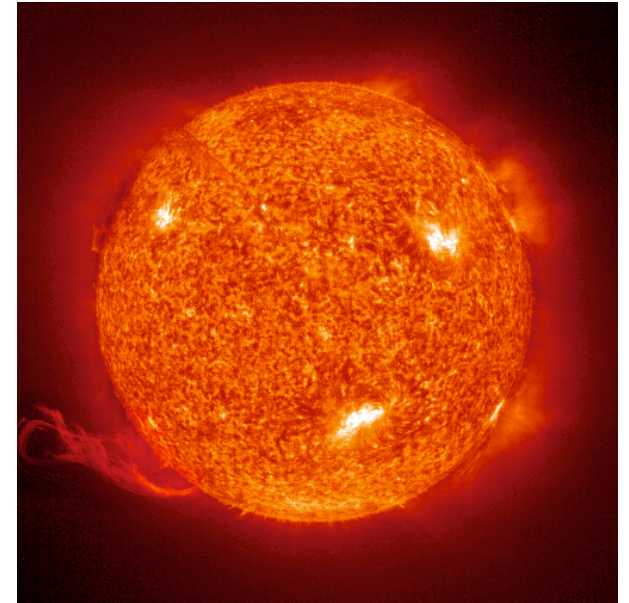


Image by NASA/Goddard Space Flight Center.

# Solar Across Scales

Moscone Center: 675,000 W



Residential home: 2400 W



Photos by [Mark H. Anbinder](#) on Flickr, [Pujanak](#) on Wikimedia Commons.

Kenyan PV market:  
Average system: 18W

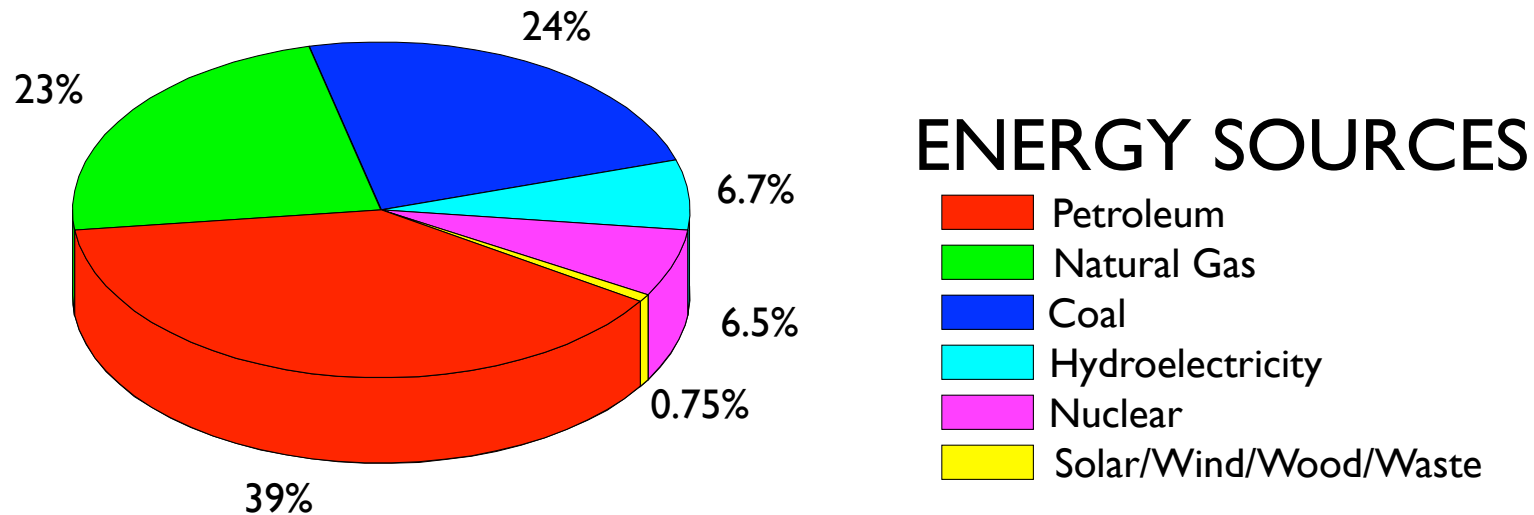


# Abundance of Solar Energy

Average solar power incident on Earth ~ 130,000 TW

Global energy consumption (2001) ~ 13.5 TW

Source: DOE



If ~2% of the continental United States is covered with PV systems with a net efficiency of 10% we would be able to supply all the US energy needs (0.3% land coverage to meet just electricity needs)

(Land area requirement is comparable to area occupied by interstate highways)

**Note: 40% of our land is allocated to producing food**

Nuclear power equivalent is 3,300 x 1 GW nuclear power plants.

(1 for every 10 miles of coastline or major waterway)

# Solar Land Area Requirements

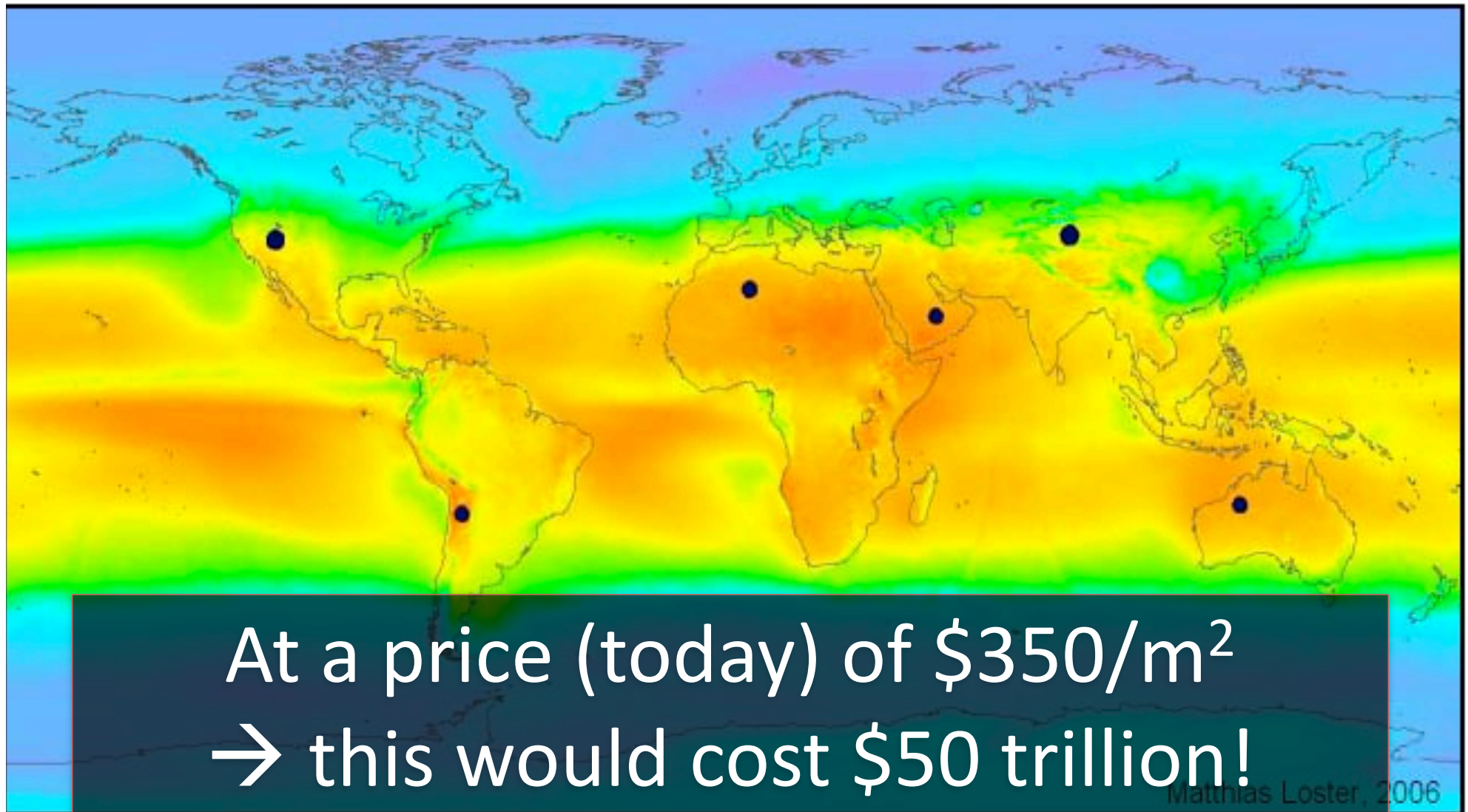
150 Km<sup>2</sup> solar panels in Nevada would power the U.S. (15% efficient)

J.A. Turner, *Science* 285  
1999, p. 687.



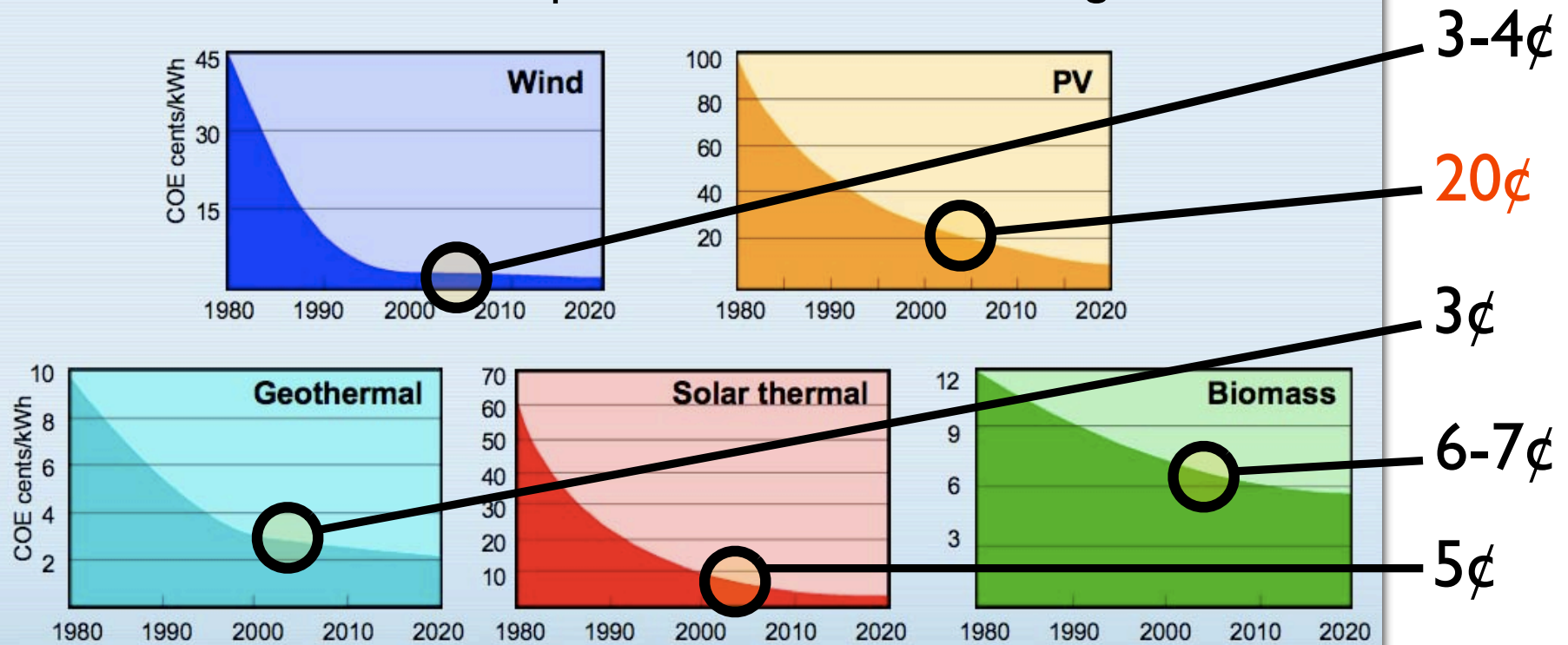
Image from [National Atlas of the United States](#),  
U.S. Geological Survey/Department of the Interior.

# Solar Land Area Requirements for ~20TW



# A Challenge with Solar PV

All but solar PV are comparable to cost of coal/oil/gas



Source: NREL Energy Analysis Office

<sup>1</sup>These graphs are reflections of historical cost trends NOT precise annual historical data.

Updated: June 2002

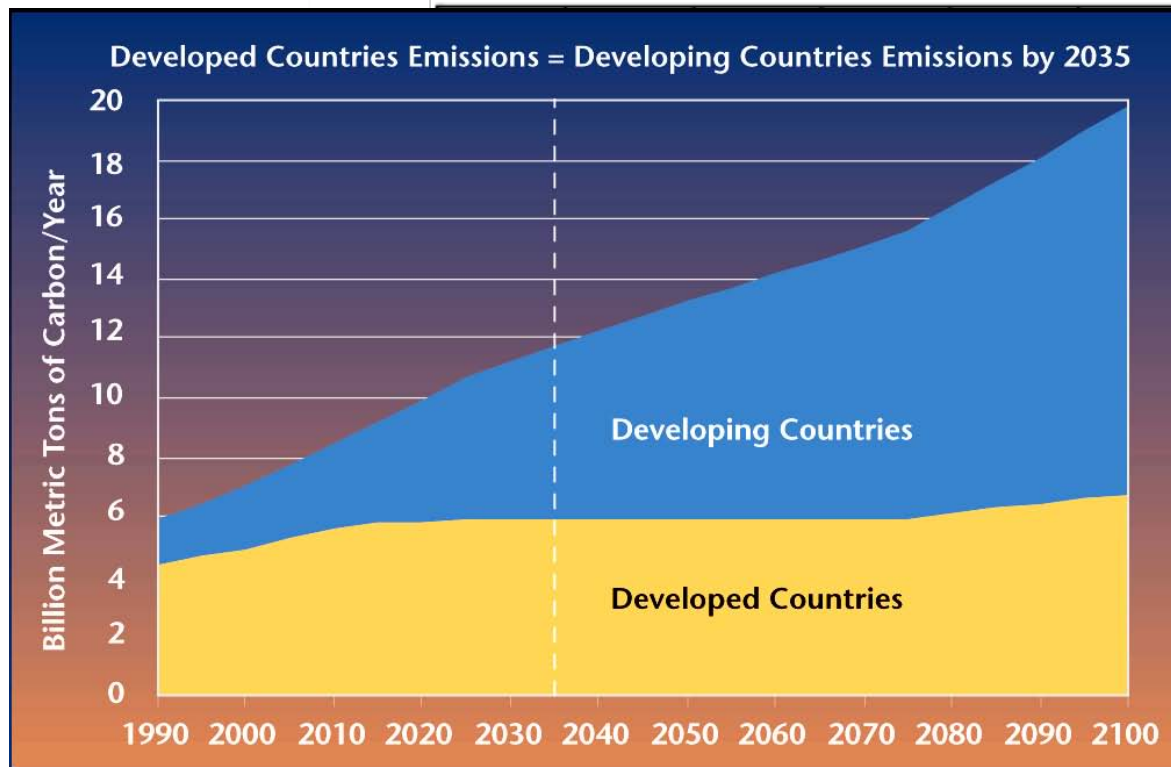
# Solar PV: Grid Parity

Please see Exhibit 1 from Lorenz, P., D. Pinner, and T. Seitz. "[The Economics of Solar Power](#)." *Energy, Resources, Materials*: McKinsey & Company, June 2008.

*Source: Mckinsey*



# Aim: capture 10% of electrical generation with PV



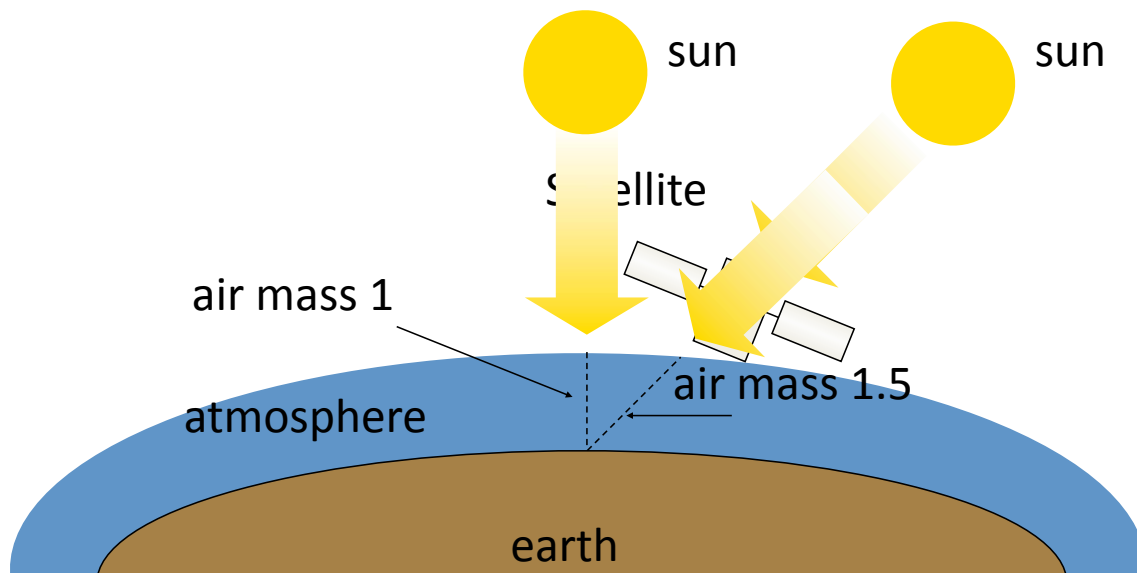
Side note: replacing fossil fuels in the developing world will become much more important in the near future.

At **14¢ per  $kW_e h$** , PV could cost-effectively replace 10% of electrical energy used in U.S.

No storage needed.

Could be deployed by 2022, with 0.04% land use.

# SOLAR INTENSITY: HOW MUCH AREA IS REQUIRED TO GENERATE POWER?



Solar spectrum outside atmosphere:  
air mass 0 (AM0) 1353 W/m<sup>2</sup>

At earth's surface:

**sun at zenith:**

air mass 1 (AM1) 925 W/m<sup>2</sup>

**sun at 45°:**

air mass 1.5 (AM1.5) 844 W/m<sup>2</sup>

**AM1.5 is terrestrial solar cell standard**

# Solar PV technology landscape (2015)

- Cost/efficiency tradeoff:
- high efficiency modules have lower installation costs
- low efficiency modules have lower module costs

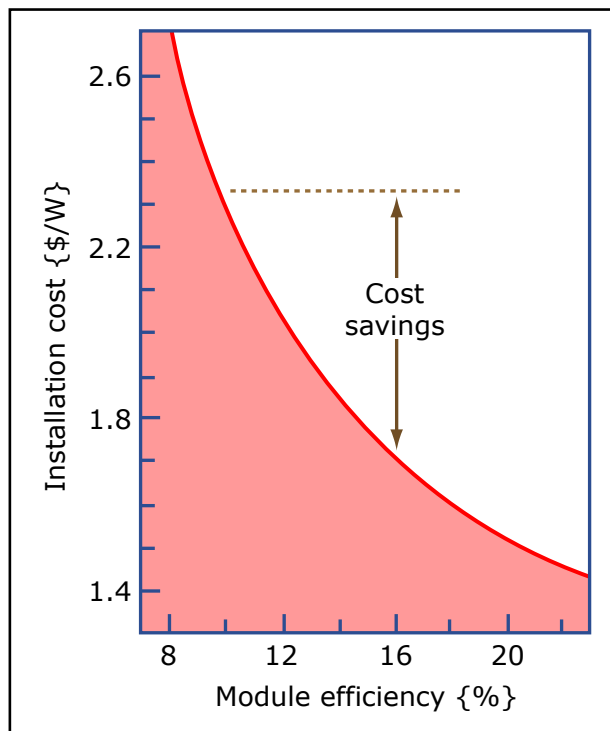
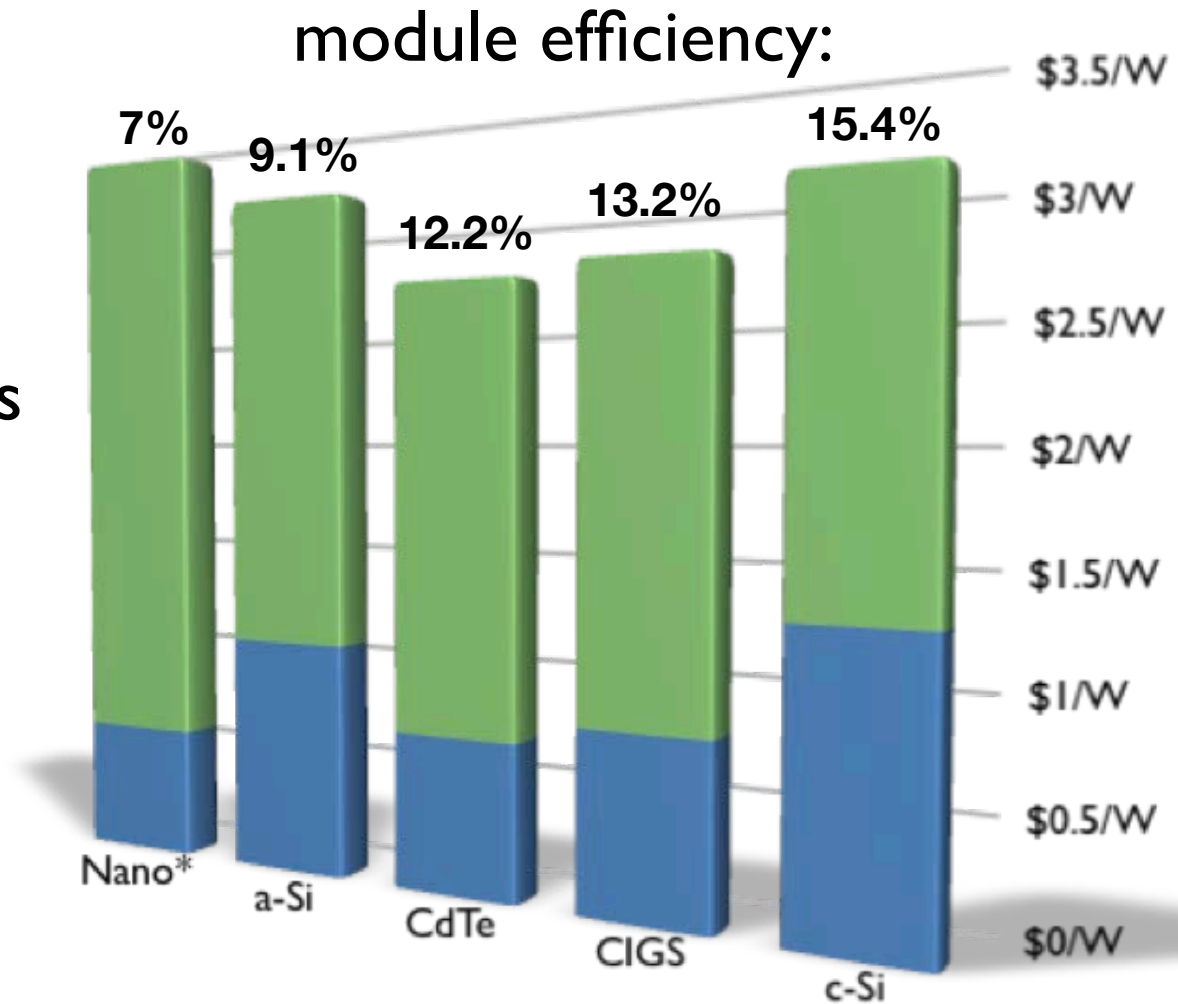


Image by MIT OpenCourseWare.



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# How do we supply 81 kWh/day/person of solar electricity?

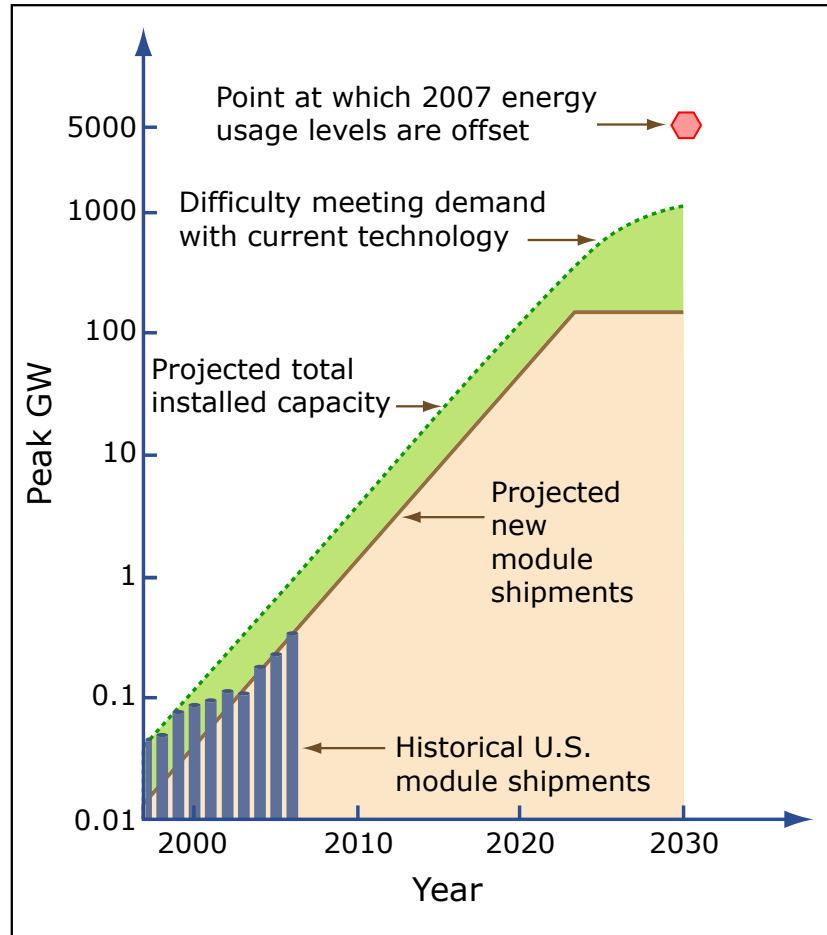


Image by MIT OpenCourseWare.

<i>TECHNOLOGY</i>	<i>BOTTLENECK</i>
<i>nano</i>	<i>low efficiency</i>
<i>a-Si</i>	<i>Si deposition</i>
<i>CdTe</i>	<i>tellurium availability</i>
<i>CIGS</i>	<i>indium availability</i>
<i>c-Si</i>	<i>module assembly</i>

At present manufacturing rates, only 10% of 2007 fuel usage will be eliminated by 2025

# How do we supply 81 kWh/day/person of solar electricity?

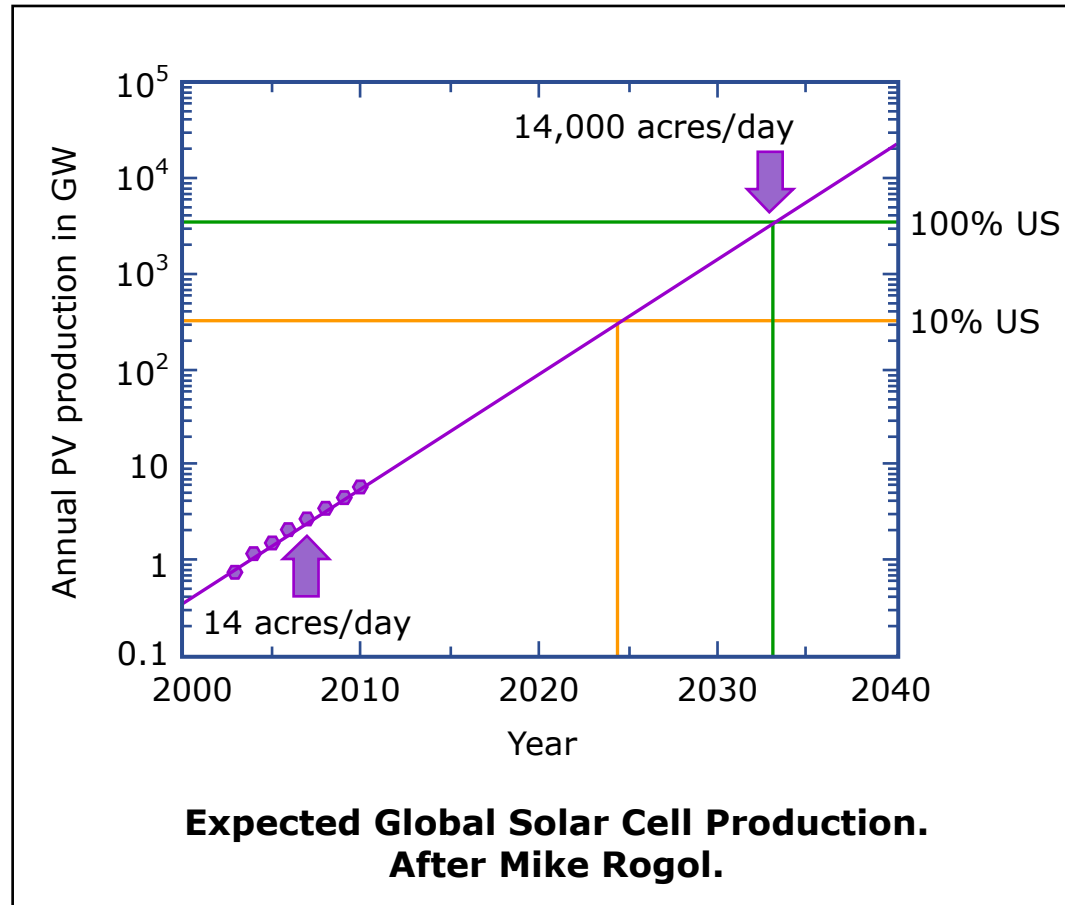


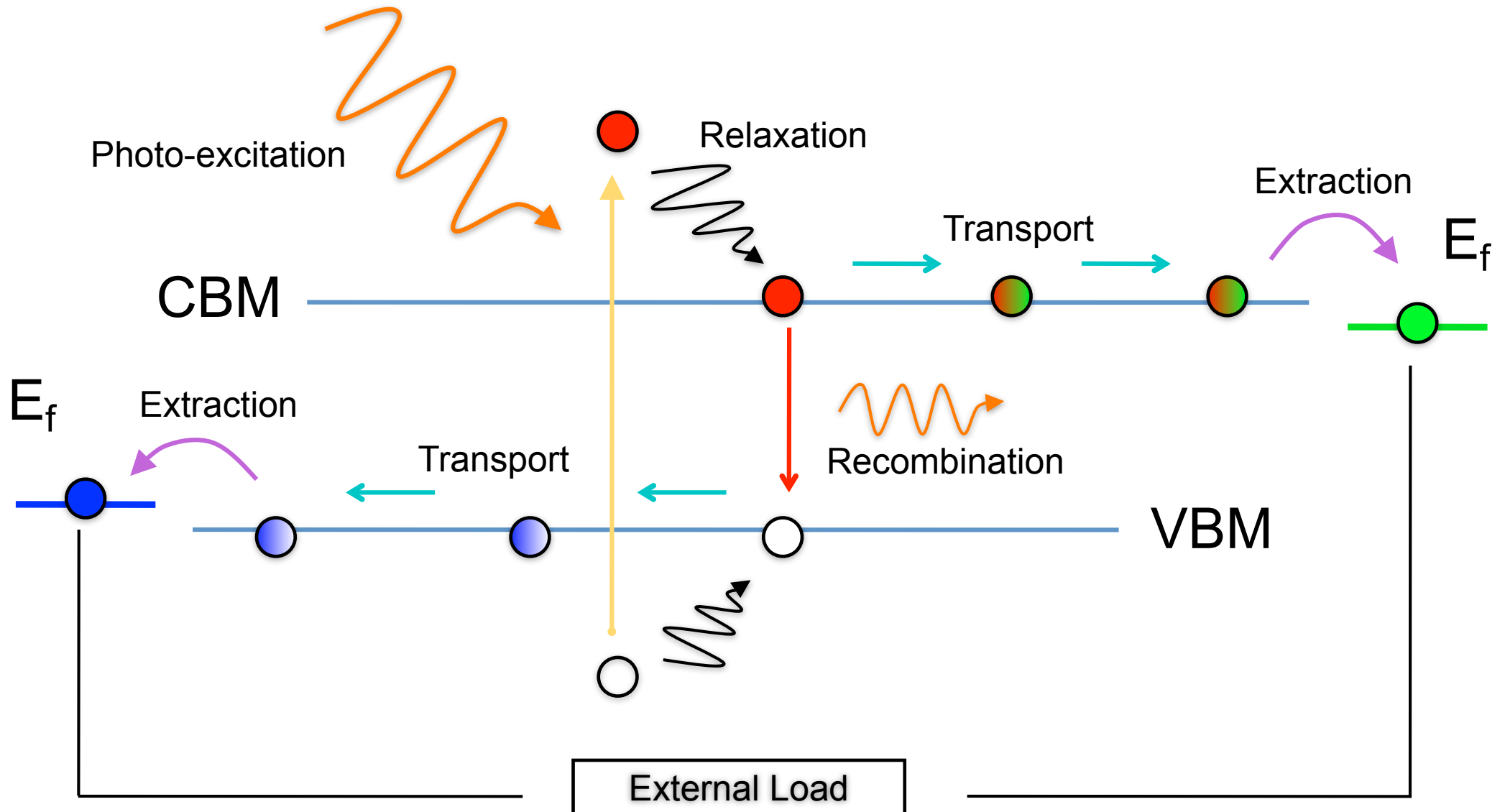
Image by MIT OpenCourseWare.

2035: Required Solar Cell Production Rate: 14,000 acres / day

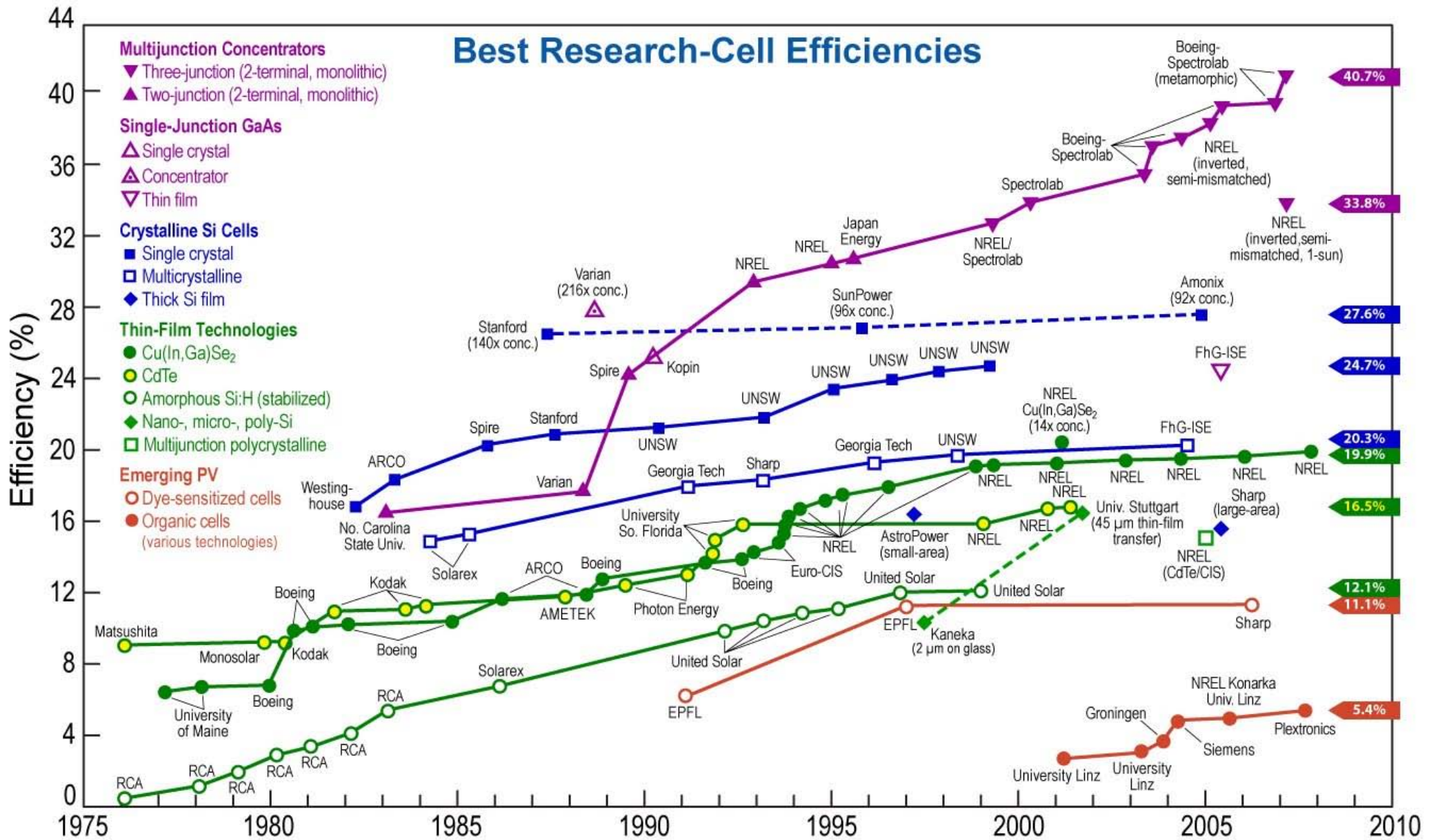
To survive, any new technology needs to:

- ACCELERATE OVER THE Si-PRODUCTION
- REACH HIGHER EFFICIENCIES and/or LOWER INSTALLATION COSTS

# Fundamental Processes Involved in Solar Photovoltaics: Electron's View



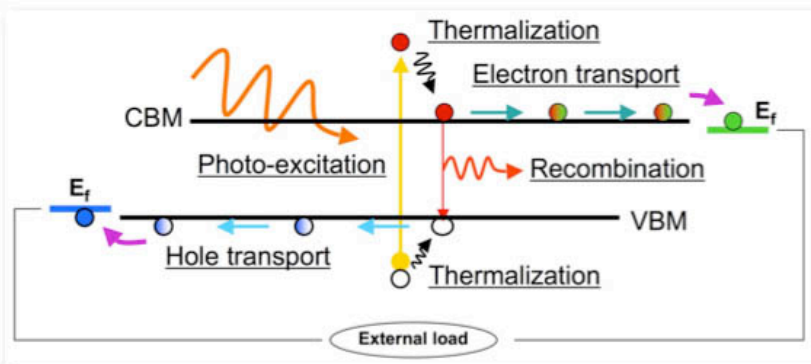
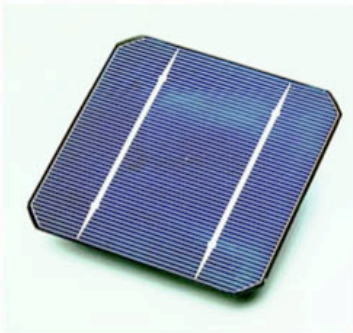
# Many Materials for PV



Rev. 11-07-07

# The Role of Computational Quantum Mechanics

- What do we know how to compute?
- How does it help for solar PV?



?  
electrical  
properties



?  
mechanical  
properties

?  
optical  
properties



# Crystalline Silicon Solar PV (80-90% of current market)

- Light Absorption

- Band Gap

Please see graph at

[http://www.tf.uni-kiel.de/matwis/amat/semi\\_en/kap\\_2/illustr/si\\_banddiagram.gif](http://www.tf.uni-kiel.de/matwis/amat/semi_en/kap_2/illustr/si_banddiagram.gif)

- Band Structure

- Electron/Hole Transport

- Electron/Hole Mobilities

$$\sigma = e^2 \tau \int \frac{d\mathbf{k}}{4\pi^3} \left( -\frac{\partial f}{\partial E} \right) \mathbf{v}(\mathbf{k}) \mathbf{v}(\mathbf{k})$$

# Amorphous Silicon Solar PV (3% of current market)

- Light Absorption (is actually pretty good)
- Electron-Hole Separation (also not a problem)
- Electron/Hole Transport (Holes are Slow!)
  - Hole Mobilities
  - Hole Traps: from total energy differences ( $E_{\text{neutral}} - E_{\text{charged}}$ )

# Organic Solar PV

- Light Absorption (need to capture more of the solar spectrum)

- Band gap

Graph of P3HT absorption removed due to copyright restrictions.

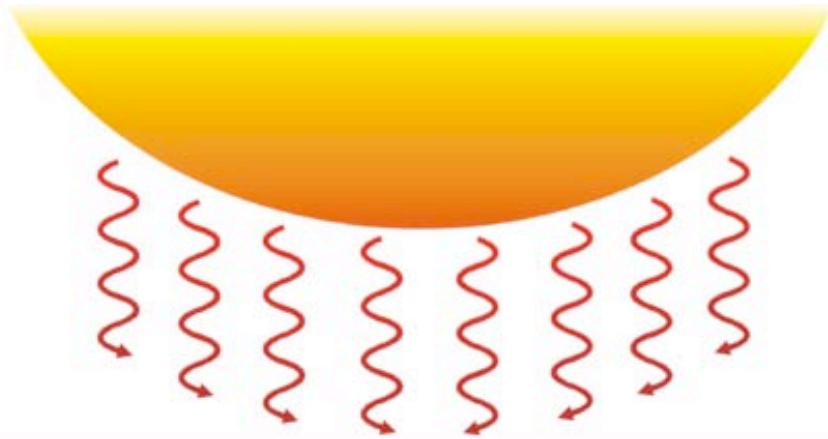
- Electron-Hole Separation

- Orbital energies

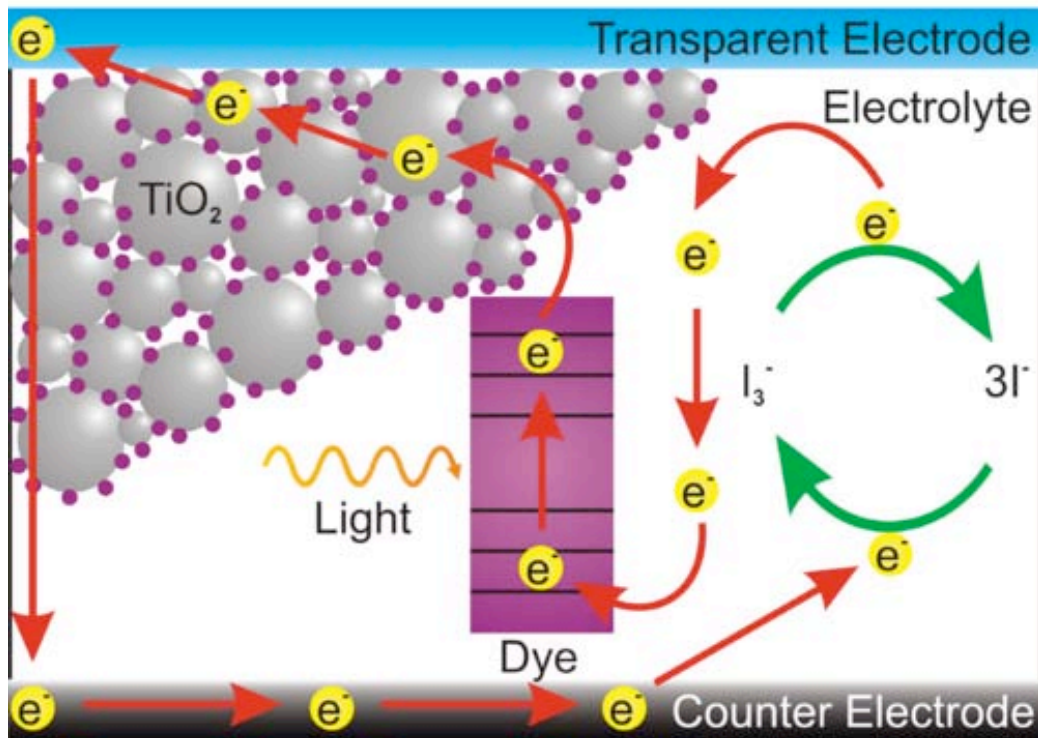
Poly(3-hexylthiophene) (P3HT):  $E_{g,exp} = 2.1$  eV  
Low-energy photons are not absorbed!

$$E_{gap} = E_o \quad E_{gap} = 0.55E_o \quad E_{gap} = 1.1E_o$$

# Dye Sensitized Solar PV

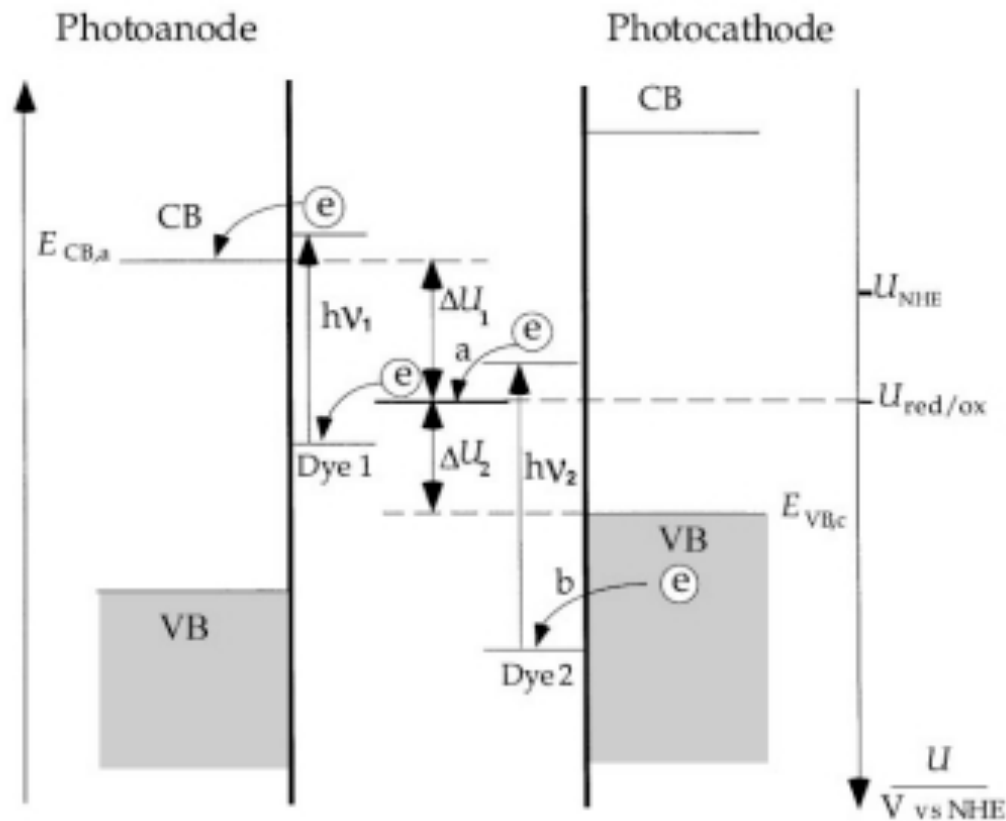


Gratzel and O'Regan  
(Nature, 1991)



- Made up of 3 active materials:
- **Dye** absorbs light.
  - **TiO<sub>2</sub> nanoparticles** with very large surface area take electron.
  - Liquid **electrolyte** delivers new electron from cathode to dye.

# Dye Sensitized Solar PV



Courtesy of Elsevier, Inc., <http://www.sciencedirect.com>. Used with permission.

- Biggest problem is a liquid electrolyte.
- **Relative energy levels** of  $TiO_2$  and dye also key.

# Multi-Junction Solar PV

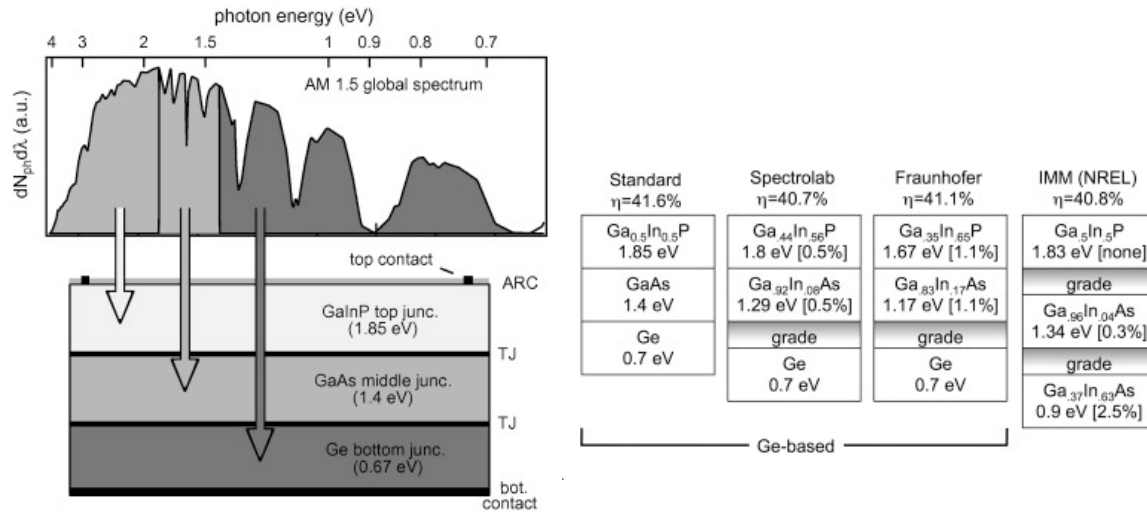
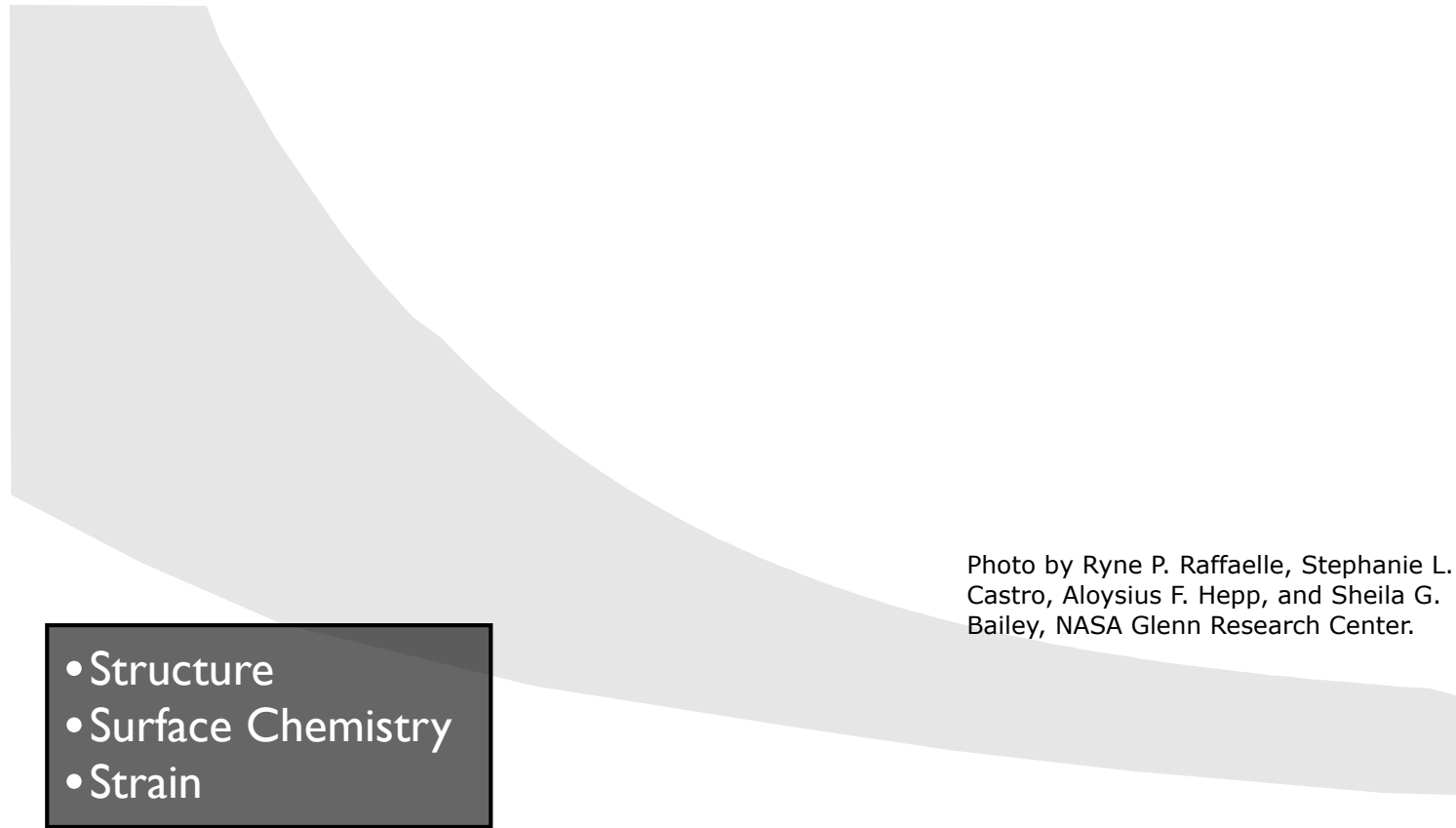


Image removed due to copyright restrictions.  
Please see the schematic of a tandem PV cell in Pentland, William.  
"Solar Energy's Bleeding Edge - Breakthrough PV Research Projects."  
*CleanBeta Blog*, June 22, 2008.

Courtesy of Elsevier, Inc., <http://www.sciencedirect.com>.  
Used with permission.

- Light Absorption
  - Band gaps
  
- Conductivity Across Interfaces
  - Band gaps, Band structures

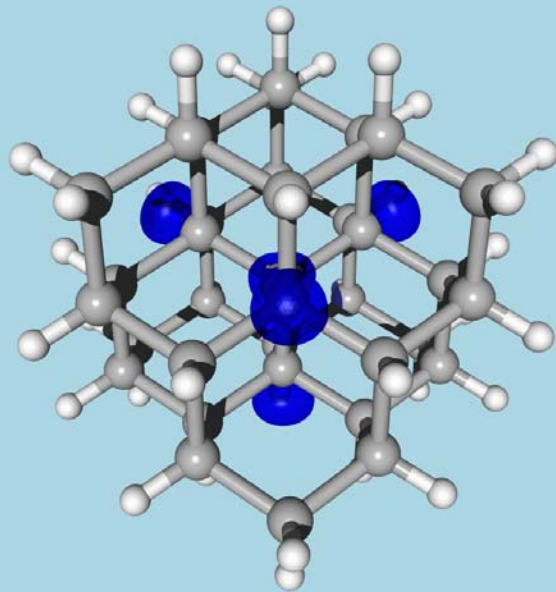
# Needing to Know Structure and Chemistry



J.P. Wilcoxon *et al.* Phys. Rev. B **60** 2704 (1999)

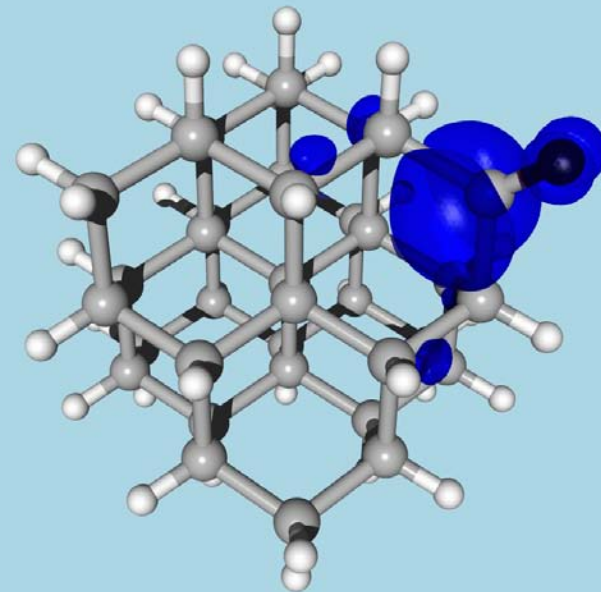
# Needing to Know Structure and Chemistry

Clean Surface



Emits blue light

Oxygenated Cluster



Emits red light

A. Puzder *et al.* Physical Review Letters, **88** 097401 (2002)



# Summary

- Energy is a Major Global Challenge
- The Sun has a Lot of it For Free but it's Too Expensive to Utilize
- Computational Quantum Mechanics can Help us **Understand** and **Predict** PV New Materials

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Spring 2011

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