MITNE-167

A METHOD OF SHORT-RANGE SYSTEM ANALYSIS FOR ELECTRIC UTILITIES CONTAINING NUCLEAR PLANTS

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A METHOD OF SHORT-RANGE SYSTEM ANALYSIS FOR ELECTRIC UTILITIES CONTAINING **NUCLEAR PLANTS by** Raymond Eng,

Submitted to the Department of Nuclear Engineering on January **15, 1975,** in partial fulfillment of the requirements for the degree of Doctor **of** Philosophy.

ABSTRACT

An optimization procedure has been formulated and tested that will solve for the optimal generation schedule of several nuclear power reactors in an electric utility system, under short-range resource-limited conditions.

The growing fraction of electricity supplied **by** nuclear energy is presenting conventional utility systems with unique unit commitment problems. Due to the batch nature of the nuclear fuel cycle, a nuclear reactor, once loaded, is limited to utilize a fixed amount of thermal nuclear energy (when limited to full-power reactivity-limited burnup). Thus, due to unforeseen circumstances situations may arise when the nuclear power reactors can not or should not be based loaded at full power until their scheduled refueling
date, Any optimization procedure has been devised to date. An optimization procedure has been
calculate the best generation schedule for calculate the best generation schedule for the nuclear
reactor to follow until refueling is possible. The refueling is possible. optimization is with respect to minimizing system costs over the short-range planning horizon.

The optimization procedure utilitizes a concept called Opportunity Cost of Nuclear Power **(OCNP)** to optimally assign the resource-limited nuclear energy to the different weeks in the short-range planning horizon. **OCNP** is a function of a week's system reserve capacity, its economic loading order, the customer demand function, and the composition of the utility system components. The optimized **OCNP** value of the short-range planning period is the utility's short-range cost of replacement energy. The system simulation program, PROCOST, used to calculate **OCNP** is a deterministic linear programming model capable of simulating five types of electric power plants: nuclear, fossil, peaking, hydro, and
pumped-storage units. PROCOST is a versatile program pumped-storage units. capable of using load-duration curves, chronologic or modified chronogic load models. The survey nature of PROCOST allows it to be adapted to study the great variety of short-range options in the operation of a nuclear power reactor.

Using a model utility system, based on data provided **by** American Electric Power Service Corporation, three system
optimization studies were performed. Case 1 was a optimization studies single-reactor optimization, Case 2 was a two-reactor optimization to demonstrate the optimization procedure for a multi-reactor situation. Case **3** was a modification of Case **1** where the outage schedule was adjusted to yield constant minimum monthly system reserves. Analysis of the results of the simulations lead to the following conclusions:

(1) Short-range nuclear system analysis can yield very large savings in fossil fuel costs, on the order of millions of dollars per reactor per optimization cycle.

(2) **A** logical method has been devised to calculate the short-range price of nuclear power, based on the system's substitutional cost of energy.

(3) The system parameters having the greatest effect on total system operating cost are (a) system reserves, **(b)** economic loading order and (c) the demand shape.

> Thesis Supervisor: Hanson Benedict Title: Institute Professor, emeritus

Thesis Supervisor: Edward **A.** Mason Title: Professor of Nuclear Engineering and Head of Department

Dedication

I dedicate this thesis, the culmination of twenty-one years of schooling to **my** dear parents who have waited patiently these many years, and to **my** loving wife, Mary, for her forbearance and her encouragement during the most difficult last two years.

Acknowledgements

I am most grateful for the assistance and guidance offered **by my** thesis supervisors, Hanson Benedict and Edward **A.** Mason, encouraged **by** their faith and understanding, and propelled **by** their probing insights and standard of excellence.

I wish to acknowledge the substantial financial sapport received from the Atomic Energy Commission fellowship program and the Research Assistantship sponsored **by** American Electric Power Service Corporation. I wish to thank Nicholas Tibberts and Myron Adams of **AEP** for their active interest and constructive suggestions during the course of **my** research.

In preparing this thesis, I also appreciate the assistance from **my** wife Mary, **my** brother Tommy, and typists Bea and Allison.

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TERMINOLOSY

- Capacity factor: The ratio of electrical energy generated divided **by** the rated electrical energy.
- Customer demand: The power distribution over time required to be met **by** the utility.
- Demand shape: The distributional shape of a customer demand function.
- Incremental capacity factor: The ratio of the electrical energy generated divided **by** the rated electrical energy for a given increment of the generating capability of a power plant.
- Interval: **A** basic individual unit of time, as compared to a period which is a group of time intervals.
- Hybrid load model: **A** modified chronologic load model where the three average workdays (excluding the high and low workdays) have been combined into one average workday.
- Load model: The model representation of customer demand function.
- Must-run: That portion of unit capacity representing its minimum level of operation without shutting down.
- Nuclear capacity factor: The ratio of the thermal nuclear energy generated divided **by** the rated thermal nuclear energy of the reactor.
- Opportunity cost: The value **of** a limited resource determined **by** the cost of the next best substitutional resource.

Perio1: **A** group of basic time units, as compared to interval, which is a single unit of time.

Scratch lisk: **A** storage device used **by** computer to stored information temporarily.

- System configuration: The collection of power plants available to generate power on a utility system.
- System reserve capacity: The margin of system capacity above the peak load level.
- Valve points: The location **of** throttles on the steam line of the tubine-generator.

1.1 Introduction

Nuclear power system analysis is concerned with the optimal coordination of nuclear power reactors with the conventional power plants of an electric power supply system. This study is interested in the short-range time frame where the nuclear fuel has been charged to the core and the thermal energy potential available for power generation is fixed **(*)** until the reactor's next refueling. The short-range problem is that of optimizing the scheduling of the generation of the electricity potential available from the fuel over the short-range time horizon. This thesis study is concerned only with the resource-limited situation where the amount of available energy from the reactor is insufficient to operate the reactor at full capacity continuously until scheduled refueling. **A** shortage of energy is possible considering the large number of factors that are related to the original decision on the energy content in the reactor **(i.e.,** long lead times involved in the nuclear fuel cycle, poor forecasting judgement, or forced outages). Examples **of** changes in the original planning assumptions which could. lead to an energy-short situation are:

- **(1) The** fuel is required to be removed from the reactor after burnup reaches 20,000 MWD/T instead of the ---------------------
- (*) **Only** the full-power reactivity-limited burnup case is considered.

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originally planned **30,000** MWD/T.

(2) The plant availability has matured faster than anticipated.

Tn such cases, available energy of the reactor must be rationed until the next scheduled refueling (if the refueling can not be advanced).

The motivation for the study of the resource-limited case is to develop the tools and procedures and provide a reference case to make possible the study of more complex short-range situations. Thus, the objectives **of** this thesis are to:

(1) Develop for the resource-limited case, a calculational model to optimize the short-range production schedule **of** the nuclear power plants.

Corollary: Develop **a** calculation model from which more complex short-range problems can be considered.

- (2) Define the parameters that have significant influence on system cost, locating areas of greatest sensitivity.
- **(3)** Develop generalized rules of thumb for utility dispatcher on the optimal use of nuclear power reactors.

corollary: Develop a model that will present the dispatcher with a budget of nuclear energy to be expended over the short-range time horizon.

To make this complex problem tractable **,** a number of assumptions are made to simplify the problem. The major financial assumptions are: **(1)** the nuclear fuel cycle costs are fixel and independent of' the reactor generation schedule; and (2) the time value of money is ignored over time horizons shorter than one year.

The major nuclear assumptions are **(1)** that there is no constraint on the rate of change in the power level of the reactors' operation, and (2) that in the full-power reactivity-limited situation, the total amount of thermal energy obtained from a given reactor before refueling is constant, independent of the power history of the reactor. The corollary resulting from these assumptions is that the nuclear energy in the short-range sense is cost-free. Thus, to maximize its utility to the system, the nuclear energy should be scheduled for generation in times of its greatest value to the system.

1.2 Method of Solution

The resource-limited case is viewed as an economic problem, a resource allocation problem, in deciding how to allocate a resource (nuclear energy) among many consumers (individual time intervals). The classical economic method of solution is to let the free market place decide which coasumers receive the resource and the amount each receives. The free market determines allocation **by** the forces of supply and demand. For the short-range nuclear allocation problem, where the "actual" market price of nuclear power is ambiguous, the economist uses "shadow prices". In the resource-limited case, the supply is limited, Figure **1.1** shows **the** supply and demand curves for the short-range nuclear allocation problem.' The market demand curve for nuclear energy is a summation of the energy demanded from all the individual time intervals. The intersection of the supply and demand curves determines an equilibrium trading price for nuclear energy that balances supply with demand. The equilibrium trading price is a mechanism that determines the allocation of the nuclear energy among all the time intervals. Each interval is allocated that amount which satisfies its own demand curve at the equilibrium price.

The determination of an interval's demand curve for nuclear energy is the key to solving the original short-range nuclear allocation problem. The shadow price an

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interval will pay **for** nuclear power is set **by** the competition (*), the cost of the next best substitional source of energy. This is called the opportunity Cost of Nuclear Power **(OCNP).** It is obvious that **0CNP** will depend on the system environment in which the time interval is, i. e., the customer demand, the system reserves, the economic loading orler, the amount of nuclear energy available, etc.

(*) This economic analysis assumes perfect competition and perfect communication of prices. The commodity of interest is electricity, where many sources of energy may compete with nuclear to supply this commodity.

Figure **1.1 SUPPLY AND DEMAND CURVES** FOR **NUCLEAR** ENERGY

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1.3 Implementation

The basic cyclic nature of the problem makes it convenient to choose one week as the basic time interval within whiCh to derive OCNP (demand) curves. The physical interpretation of **QCNP** is the cost of the displaced energy when optimally distributed nuclear energy is marginally inzreasei. **A** linear programming model of a utility system that solves for the minimum system production cost with a limited amount **of** nuclear energy (via peak-shaving techniques) will calculated an **OCNP.**

A weekly **DCNP** curve is obtained from explicity calculating the OCNP for a number of values of nuzlear energy. The optimization procedure requires a weekly **OCNP** curve for each week in the planning horizon to derive the gross demand curve for nuclear energy. The latter is compared with the **supply** of nuclear energy to establish a global **OCNP** for the planning period. Where the global **OCNP** intersects each weekly **OCNP** curve determines the guantity of nuclear energy allocated to each week.

1.4 Computer Programs'

PROCOST and **ALLOCAT** are the two principal programs developed to implement the optimization procedures. **PROCOST** takes a series of assumed nuclear energy allotments for a particular week and determines the minimal system cost in each allotment of nuclear power via peak shaving techniques and from this **OCNP. ALLOCAT** takes a set of weekly **OCNP** values over a larger period of time and determines how much nuclear energy to allocate to each week **by** using the criterion that the **OCNP** for all weeks shall be the same.

PROCOST, the system simulation program, is a deterministic L.P. model capable of simulating five types of power plants (nuclear, fossil, peaking, hydro, and pumped-storage units) and three types of load models (chronologic, load-duration, and modified chronologic). PROCOST is composed of three parts: **(1) NUC_3PT,** the L.P. formulating program; (2) MPSX, the L.P. package (IBM program product); **(3) PUMPST,** the pumped-storage simulator. In the NUC OPT section, the peaking and hydro units are explicitly simulated, and the fossil economic loading order is calculated. **NUCOPT** also formats the L.P. formulation of the fossil-nuclear optimization problem for MPSX to solve. MPSX in turn writes the solution on a scratch disk for PUMP ST to read. PUMP ST analytically calculates the optimal pumped-storage scheduling solution. The pumped-storage unit can either operate in an economic mode to minimize system cost or in a security mode to maximize

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system reserve generation capability. The L.P. formulation of the nuclear scheduling problem is:

objective function: minimize

$$
\sum_{j} \sum_{i} (c_{i}) {H_{i}} {L_{j}} {H_{i}} \times {i} \tag{1.1}
$$

subject to the following constraints:

(customer demand constraint)

$$
\left\{\sum_{i} x_{i} x_{i}^{i} + \sum_{n}^{N} \sum_{i}^{I_{n}} x_{i}^{i} = D^{j} \right\}_{i=1,...,J}^{(1.2)}
$$

(limited thermal nuclear resource constraint)

$$
\left\{\sum_{j} \sum_{i} (x_{i}^{j})(_{n} H_{i}) (T_{j}) = K_{n} \right\}_{n=1,...,N}
$$
 (1.3)

(bounds, separable programming constraint)

$$
\begin{cases}\n\hat{i}f \text{ and only if } \n\begin{aligned}\n\overrightarrow{f}_n X_{i-1}^j &= \n\overrightarrow{f}_n B_{i-1} \\
\overrightarrow{f}_n \text{ then } \n\end{aligned}\n\end{cases}
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where:

$$
{F}X{i}
$$

- **=** fossil pawer level of the i-th increment and the **j-th** time period (MW)
- *n* Xj **=** power level of the i-th increment and the **j-th** time interval of the n-th nuclear reactor (MW)

- **31** - F_n X_i' = either F_i' or **⁼**incremental fossil heat rate of the i-th *FlHI* -increment **of** the loading order (million BTU/MWHt) incremental nuclear heat rate of the i-th *H*_I = incremental nuclear heat rate of the i-th
nuclear increment of the n-th nuclear reactor (million BTU/MWHt) C. **=** fossil fuel cost (\$/million **BTU)** of the i-th **I** increment ^P**=** modified customer demand of the **j-th** time interval (MW) full-power reactivity-limited thermal energy available from the n-th reactor (million **BTU) ⁼**upper bound of the i-th increment **(MW)** F_n \overline{U}_i = total number of time intervals **^N=** total number of nuclear reactors **=** total number of increments in a nuclear reactor T **=** duration of **j-th** time interval (hours)

The objective function, **Eq. (1.1),** to be minimized is a summation **of** the incremental production cost over all the increments in the economic fossil loading order (index i) and over all the time intervals in the one-week time horizon (index j). The incremental production cost is a product of the fuel cost (\$/million **BTU),** the incremental heat rate (million BTU/MWH) and the energy production (MWH) for each time interval. The constraints to be met are: **(1)** the summation **of** the power levels of the individual nuclear and fossil units in each time period must satisfy the modified customer demand, **Eg.** (1.2), while (2) limiting the total nuclear production to the available resources, **Eq. (1.3).**

In addition, each variable is bounded, **Eg.** (1.4). This is where the "separable programming" aspect is featured. **All** increments are fixed at the lower bound of zero until all the preceding increments have been set .to their upper bound. For example, the third increment **of** the loading order can't be started until the second (and the first) increments are fully loaded. Without this feature, variable heat rates could not be modelled.

1.5 The Utility System

To test the optimization procedures discussed earlier, three system optimization problems were solved. The first was a single-reactor optimization problem, and the second was a multi-reactor optimization problem. The multi-reactor optimization was performed under conditions more severe than "typical" operating conditions. The third optimization problem was a modification of the first in which the monthly configurations were adjusted to yield constant system reserves over the planning horizon.

American Electric Power Service Corp. **(AEP)** provided the basic data from which the utility system configuration **(16)** was constructed. The system, composed of **52** units of five power plant types, was simulated for a short-range planning period of six months, April through September. The system included two nuclear plants (of **1100** MWe each), one hydro plant (with limited pondage and 200 MWe peak generating capacity), one pumped-storage unit (of **300** MWe generating capacity), seven peaking units and 41 fossil units for a total generating capacity of **19250** MWe.

The maintenance schedule (scheduled outage) of the individual fossil and peaking units proposed **by AEP** is displayed in Table **1.1.** Most of the scheduled outage was placed in the spring and fall months. Since the model is deterministic, forced outage effects are simulated, treating them as scheduled outages also. rable **1.1** also displays the systematic treatment of forced outages. Peaking units are

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TABLE 1.1

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Note: An "X" represents a simulated outage for the entire month. The total time of scheduled outage for each plant corresponds to the actual observed outage rate for similar sized units. The specific forced outage schedule for each unit was chosen randomly. The maintenance schedule was chosen to lie mainly in the spring and fall months.

> The **X"** represents a simulated outage for Cases **1,** 2, **3.** The "Y" represents a simulated outage for Cases **1** and 2. The "Z" represents a simulated outage for Case **3.**

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scheduling to peak-shave until their input capacity factors are fulfilled. **All** the peakers had estimated capacity factors of **10%** and start-up and shut-down cost **of** \$100/start-up, except for two gas-turbine units (of **51** and 4 MWe) which has zero start-up and shut-down costs.

The individual plant parameters were supplied **by AEP** in **1973.** The rated capacity, fuel costs and average heat-rate at rated capacity for the 41 fossil units and seven peaking units are tabulated in Table 1.2. The fuel costs do not reflect the sharp rise in fuel costs during 1974. The hydro unit with limited pondage was scheduled to generate 200 MWe for nine peak demand hours during each worklay and 50 MWe at all other times. The pumped-storage unit's operating parameters were: **300** MWe capacity generator, **160** MWe capacity pump, 70% cycle efficiency, **9300** MWH reservoir capacity and **2300** MWH/week free water inflow into the reservoir.

The system treated also contained two nuclear units of **1100** MWe each. Nuclear Unit **1** was scheduled for refueling on October **1.** In the six months prior to refueling which make up the planning period, Unit **.1** was assumed to have **70%** of the thermal energy reguired to operate base loaded at full rated power. In the first simulation, Unit 2 was treated as a new unit just being introduced to service under a gradual programmed start-up: 20% of full rated power throughout April, 40% of full rated power throughout May, **60%** during June, **80%** during July, and **100%** iuring August and

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Table **1.2**

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PLANT PARAMETERS OF **PEAKING** *AND* FOSSIL UNITS

September.

The forecasted weekly energy consumption during the six-month **(26** week) planning period is tabulated in Table 1.3. The six-month planning period spanned three seasons, spring (April and May), summer (June, July, and August) and fall (September). The weekly energy consumption was input to a seasonal load model, MODEL, to generate the detailed hourly customer demand numbers.

In the six-month period prior to refueling, a reactor with insufficient energy to run at full power until scheduled refueling can be considered a candidate for short-range resource-limited optimization. The second reactor, Nuclear Unit 2, coming on-line with **a** fully fueled core had an abundant supply of energy and an undetermined forced outage rate and would be undergoing a planned start-up program, so that the reactor's operation was determinate over the short range. Only reactors with limited resource and a fairly certain availability **(*)** over the short-range time horizon are amenable to short-range system analysis using PROZOST. Availability, at best, can only be fairly certain over a short-range time horizon.

The first system optimization (Case **1)** was then to find

(*) The leterministic approach (used in the PRDCOST program) assumes the availability of the reactor is known with
certainty. Hence, this assumption imposes certain certainty. Hence, this assumption imposes certain
restrictions on the use of this short-range restrictions on the use **of** this short-range optimization technigue. This restriction can possibly be eliminated **by** the utilization of the Booth-Balerieux probabilistic technique, ref. (18), for modeling forced outages in PROCOST.

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TABLE 1.3

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WEEKLY BNERGY FORECAST FOR PIANNING PERIOD

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the optimal distribution of weekly nuclear capacity factors of Nuclear Unit **1,** whose overall thermal energy availability is **70%** of rated capacity for the six-month planning period prior to refueling. The second power reactor was operated at programmed steps in power levels.

Thus, although the system contained two reactors, the first system simulation (Case **1)** was a single-reactor optimization. The second system simulation (Case 2) was a complex two-reactor optimization. Case 2 used exactly the same system configuration as in Case **1,** except for additional constraints on Nuclear Unit 2, which was limited to **80%** of the energy used in the corresponding periods of Case **1,** see Table 1.4. The goal of Case 2 was to find the optimal weekly nuclear capacity factor distribution of both nuclear reactors. Case 2 was admittedly a contrived case to illustrate: **(1)** a multi reactor optimization, and (2) the feasibility of the procedures to handle a complex and involved. situation. Case 2 is not an ordinary straight-forward two-reactor optimization. Nuclear Unit 2 had five smaller separate planning periods, reguiring a separate optimization in each period. (Nuclear Unit 2 was analogous to a collection of five reactors, with each reactor operating for only one period and shut down for the other periods.)

Case **3** is a single reactor optimization similar to Case **1.** The only difference (between Case **1** and **3)** is that the monthly fossil configurations were adjusted in Case **3** to

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TABLE **.4**

OPERATIONAL CONSTRAINTS **ON NUCLEAR** UNIT 2 DUING THE 'IWO-REACTOR OPTIMIZATION, **CASE** 2

levelize the minimum monthly *system* reserves over the six-month planning horizon (see Table **1.1). All** other system parameters of Case **3** are identical to Case **1.**

Before discussing the optimization results, some fundamental characteristics of **OCNP** will be reviewed. Examining Figure 1.2 these distinguishing characteristics of weekly **OCNP** functions are discernable: **(1)** The **OCNP** functions are monotonically decreasing functions with respect to an increasing nuclear capacity factor. (2) The weekly **OCNP** function of different weeks (but the same monthly configurations) never cross. **(3)** For weeks of increasing weekly energy consumption, the **OCNP** function likewise increases. (4) The larger the weekly energy consumption, the larger the slope of the **OCNP** function. **(5)** The weekly **OCNP** functions assume a shape characteristic of their respective economic loading order. **(6)** The amplitude of the OCNP function varies inversely with the weekly system reserve. **(7)** The amplitude of the **OCNP** function is proportional to the average fossil fuel cost of the monthly system configuration.

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Figure **1.2**

Note: Circled numbers refer to the week numbers from the Case **1** simulation

1.6 Case **1**

The results of Case **1,** the optimized weekly nuclear capacity factor distribution, Table **1.5,** reflects many of the **OCNP** principles stated above. The overall nuclear capacity factor for the six-month planning period was **70%.** The high weekly nuclear capacity factor for September reflects the unusually high fossil fuel cost for that month. **All** the other months have about the same fossil fuel cost, as shown in Table **1.6.** Hence September due to its significantly more expensive fossil fuel cost configuration is scheduled to generate at near full capacity to displace as much of the expensive fossil fuel as possible. August and July have the lowest average weekly nuclear capacity factor, in fact, the lowest allowed, because of their large reserve capacity, Table **1.7.** April has the lowest system reserve, hence the second largest set of weekly nuclear capacity factors. Thus, May is the second tightest month system reserve-wise, and also has the second highest fossil fuel configuration. May also has an above average monthly nuclear capacity factor. Within each monthly schedule, the weekly allotments of nuclear energy are proportional to the weekly energy consumption forecast, see Table **1.3.**

The overall impression from the results of this optimization 'study for the system simulated is that the maintenance schedulei was too unbalanced in excluding summer maintenance. Gross generating capacity is large enough to handle the summer peaks while still scheduling more

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OPTIMAL WEEKLY **NUCLEAR** CAPACITY FACTOR FOR THE SINGLE REACTOR OPTIMIZATION DISTRIBUTION **(CASE 1)**

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TABLE 1.6

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September 7.149

Table **1.7**

WEEKLY SYSTEM RESERVE FOR **CASES 1** AID 2

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*Program startup limitation for Nuclear Unit 2.

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maintenance during August and July, and less during April and May. Also, a better mix of fossil plants should be scheduled for September to give lower fossil fuel costs. Such considerations led to the calculation of Case **3,** to be discussed below.

A total system cost calculation from the optimization results of Case **1** showed a very large dollar savings, see Table **1.8.** Comparing the situation of no nuclear optimization, Case **1.A** (uniform hourly nuclear. power generation for the entire six months), with the situation of constant weekly nuclear capacity factor, Case 1.B (optimized hourly generation), the saving was \$4.1 million in fossil fuel costs. By further optimizing the weekly nuclear capacity factor distribution over the six month time horizon, Case **1.C,** the saving increased **by** another \$340,000. The total fossil fuel savings is eguivalent to **66%** of the nuclear fuel cost of Nuclear Unit **1,** at 2.0 mills/KWHe. The order of magnitude of the savings for Case **1** indicates that even for a single-reactor utility system, short-range optimization is worth-while in the resource-limited situations.

		Case 1.A Case 1.B		Case 1.C	
Month	Week	No Nuclear Optimization (\$)	Hourly Optimization $(*)$	Hourly and Weekly Optimization (\$)	
April	ı $\overline{\mathbf{c}}$ $\frac{3}{4}$	10,897,641 11,310,309 10,401,792 9,496,691	10,703,601 11,002,306 10,220,996 9,326,228	10,524,562 10,708,211 10,056,930 9,373,436	
May	5 6 $\overline{6}$ 9	10,585,981 10,078,719 10,316,433 10,660,648 9,762,971	10,406,225 9,886,612 10,126,110 10,482,397 9,611,780	10,227,973 9,830,631 10,063,502 10,300,385 9,660,533	
June	10 11 12 13	9,899,898 10,210,651 9,725,349 9,369,029	9,755,839 10,063,304 9,586,475 9,242,724	9,802,719 10,013,456 9,632,938 9,387,855	
July	14 15 16 17 18	8,847,012 9,950,572 9, 670, 594 10,037,142 9,883,377	8,746,190 9,816,608 9,555,670 9,858,900 9,753,496	8,873,310 9,959,853 9,692,954 10,004,974 9,894,948	
August	19 20 21 22	9,623,066 10,378,333 10,002,896 10,101,697	9,517,456 10,230,513 9,877,511 9,968,648	9,652,246 10,380,137 10,016,482 10,109,134	
September	23 24 25 26	11,538,985 10,879,069 10,908,873 11,551,409	11,379,984 10,716,938 10,745,769 11,390,192	11,101,378 10,559,049 10,586,767 11,216,616	
Total		266,089,137	261,988,509	261,648,975	
Comparison with Case 1.A			(4,100,629)	(4,440,162)	

SYSTEM FOSSIL **FUEL COSTS AND** SAVINGS FOR **CASE 1**

Case **1.A:** Unit **1** is run at constant power **(725** Mw), and Unit 2 is run at programmed power levels (Table 1.8B.) for all three cases.

Case 1.B: The weekly energy output of Unit **1** is the same as in Case **1.A,** but the hourly power level within each week is optimized.

Case **l.C:** Unit l's power levels for each hour of each week are optimized for the entire six-month planning period.

Total energy output of Unit **1** is the same in **all** three cases.

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1.7 Case 2

Case 2 is a two-reactor optimization, which must be solved iteratively. A summary of the optimal capacity factor distribution and system costs with each iteration for Case 2 are given in Table **1.9** and **1.10,** respectively. The complete two-reactor optimization, Case 2.C, results in a total savings of \$6.48 million compared with the situation of no nuclear optimization, Case **2.A. of** this, **\$600,000** represents the improvement from the situation of optimal hourly generation, Case 2.B, compared with the total optimization results, Case 2.Z. Table **1.10** indicates that most of the savings are realizel after only one complete cycle of iterations in this two-reactor system. Other simulations have confirmed the hypothesis that the multi-reactor iteration process is a rapidly convergent one.

The major conclusions of this multi-reactor all simulation are that: **(1)** the short-range resource-limited optimization process described in this thesis has been shown adaptable to a two-reactor situation; (2) convergence takes only a few complete cycles of iterations; **(3)** most of the cost savings are realized after one or two complete cycles of iterations; (4) substantial savings in fossil fuel cost are possible with short-range optimization; **(5)** potential cost savings increase as the amount of nuclear capacity and energy that are optimized is increased.

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TABLE **1.9**

OPTIMAL WEEKLY NUCLEAR CAPACITY FACTOR DISTRIBUTION FOR THE TWO REACTOR OPTIMIZATION **(CASE** 2)

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TABLE 1.9 (CONT'D)

		Unit 1				Unit 2			
٠ Month	Week	Capacity Factor	Weekly Energy (105 MWH)	Monthly Total Energy $(103$ MWH)	Monthly Average (10^3 MW)	Capacity Factor	Weekly Energy (10^3 MWE)	Monthly Total Energy (103) MWH)	Monthly Average (10^3 MWE)
At gust	19 20 21 22	0.55 0.55 0.55 0.55	101.64 101.64 101.64 101.64	406.56	101.64	0.70 0.80 0.80 0.70	129.36 147.84 147.84 129.36	554.40	138.60
S eptember	23 24 25 26	0.95 0.95 0.95 0.95	175.56 175.56 175.56 175.56	702.24	175.56	0.90 0.80 0.80 0.90	166.32 147.84 147.84 166.32	628.32	157.08
Total			3,363.36		129.36		2,542.848		97.80

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SUMMARY OF TWO-REACTOR OPTIMIZATION **COST** SAVINGS **AS A** FUNCTION **OF NUMBER** OF ITERATIONS

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1.8 Case **³**

The purpose of Case **3** was to examine the effect of system reserves on **DCNP** and on the optimal weekly nuclear capacity factor distribution. Case **3** is a modification of Case **1** where the fossil outage schedule has been adjusted to obtain a (nearly) constant minimum monthly system reserve. **A** comparison of the minimum monthly system reserves for Cases **1** and **3** is listed in Table **1.11.** The average fossil generation-costs of the monthly fossil configurations are listed in Table 1.12. The optimal weekly nuclear capacity factor distribution is listed in Table **1.13.**

A comparison of the optimal nuclear capacity factor distribution for Case **1** and Case **3** shows a decrease of allocated energy for April and May, and an increase for July, August, and September. The June allotment is the same for both cases. The change in monthly allocation of nuclear energy is consistent with the change in the monthly minimum system reserve, both in direction and magnitude. April and May had large increases in reserves, thus, resulting in significant decreases in nuclear energy allotments. July and August **had** large decreases in system reserve, thus, resulting in significant increases in nuclear energy allotments. June had the smallest monthly change in system reserves (210 MW), not enough to change its nuclear energy allocation. September had a slight decrease in system reserves **(225** MW), resulting in a slight increase the nuclear energy allotment. The comparison of the solution of

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TABLE **1.11**

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TABLE 1.12

MONTHLY AVERAGE FOSSIL **GENERATION COSTS** OF **THE FOSSIL** CONFIGURATION FOR **CASE 3**

OPTIMAL WEEKLY NUCLEAR CAPACITY FACTOR DISTRIBUTION FOR THE SINGLE REACTOR OPTIMIZATION (CASE 3) Monthly
Average Worthly Average Monthly Average Energy Energy Energy Energy (103 MWH) (103 MWH) Capacity Energy Energy Energy Month Week Factor (103 WH) **(103** MWH1) (103 MWH) April **1 0.85 157.08** 554.40 **138.60** 2 0.85 **157.08**
3 0.75 138.60
4 0.55 101.64 **0.75** 138.60
0.55 101.64 4 **0.55** 101.64 **May 5** o.85 **157.08 674.52** 134.90 **5**
 6
 6
 7
 0.75
 138.60
 8
 0.75
 138.60 0.75 138.60
0.75 138.60 **8 0.75** 138.60 **9 0.55** 101.64 June **10 0.65** 120.12 480.48 120.12 **11 0.75 138.60** 12 **0.65** 120.12 **13 0.55** 101.64 **July** 14 **0.55** 101.64 **545.16 109.03 15** o.65 120.12 **16 0.55 101.64**
 17 0.65 120.12
 18 0.55 101.64 0.65 **120.12**
0.55 **101.64 18 0.55** 101.64 August **19** 0.55 101.64 443.51 110.88 19 0.55 101.64
20 0.65 120.12
21 0.55 101.64 21 0.55 101.64
22 0.65 120.12 120.12 **September 23** 0.95 175.56 665.28 166.32

24 0.85 157.08

25 0.85 157.08

26 0.95 175.56 0**.85 157.08**
0**.85 157.08 257.08**
 257.56
 275.56 26 0.95 175.56

^{*}

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Total 3,363.36 **129.36**

Case **1** with Case **3** shows conclusively the significant effect an unequal system reserve has on the optimal distribution of nuclear energy.

In terms of total system costs, Case **3** showed an improvement of about \$2.2 million compared with Case **1,** see Table 1.14. The comparison of case **3.A** with Case **3.C,** no nuclear optimization to weekly nuclear optimization, showed a savings of \$4.7 million, eguivalent to **70%** of Unit **1** fuel cost at \$2.0 mills/KWHe. This is about the same as Case **1.**

Comparing Cases B to Cases **C,** hourly optimization to weekly optimization, the savings are **\$160,000** for Case **3** and \$340,000 for Case **1.** It is to be expected that as the system reserves becomes equalized, the optimal distribution **of** capacity factors becomes narrower and hence the difference in savings between hourly optimization and weekly optimization diminishes. Also, the lower capacity factors of the summer months are partially due to a seasonal influence on the shape of their customer demand function. Both spring and summer have about the same average weekly energy consumption. However summer has much higher demand peaks than the spring, hence summer also has lower demand minimums than spring. Since the lower part of the load-duration curve plays an active role in determining **OCNP,** it is no surprise that summer months should have lower average nuclear capacity factors (with all other parameters egual).

Because of changing economic conditions, fossil fuel

TABLE 1.14

SYSTEM FOSSIL FUEL COSTS AND SAVINGS FOR CASE 3

Case 3.B: The weekly energy output of Unit **1** is the same **as** in Case **3.A,** but the hourly power level within each week is optimized.

Case **3.C:** Unit **l's** power levels for each hour of each week are optimized for the entire six-month planning period.

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Total energy output of Unit **.** is the same in **all** three cases.

costs show a great amount **of** variance from station to station. Hence, the monthly economic loading order will show different patterns for different maintenance schedules. The main conclusion from the system simulations performed is that equal consideration must be given to fossil fuel arrangements as well as system reserves when determining the monthly maintenance schedule.

The sample optimization problems showed that peak-shaving the nuclear energy first resulted in savings on the order **of** millions **of** dollars (per reactor per optimization cycle) and optimally distributing the weekly energy next resulted in saving on the order of hundreds of thousands of dollars (per reactor per optimization cycle). These two optimization steps were reversed to find if the order of optimization had any significant effect on their savings. The result showed that the (order of magnitude of) savings from each optimization steps is independent of their order of application.

A sample of the type of optimal load-following pattern rezommended **by** PROCOST is shown in Figure **1.3.** As shown, the reactor is essentially operated in an on-off mode. The reactor is turned off (to its minimum operating levels) during low demand intervals and turned on to full capacity during high demand intervals.

NUCLEAR DISPATCHING **SCHEDULE**

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1.9 Conclusions

(1) The system simulation performed showed the short-range optimization procedure developed to be flexible and reliable in handling a wide range of system conditions including an adaptability to multi-reactor problems as well as to single reactor optimization problems.

(2) The system simulations showed that very large savings in fossil fuel costs, on the order of millions of dollars per reactor per optimization cycle, are possible from short-range nuclear system analysis. Thus adoption of these short-range system optimization technique **by** the utility industry would be a worth-while undertaking.

(3) Procedural guidelines for optimal dispatching of nuclear generation (under resource-limited conditions) are to (a) peak-shave the dispatching of nuclear energy **by** operating at full rated power during peak demand time intervals and shutting down (or operating at minimum power) during low demand intervals, **(b)** follow a weekly budget of nuclear energy rationing until the next scheduled refueling date. The system simulations show that independent of the order of optimization most of short-range optimization savings (millions of dollars per reactor per optimization cycle) comes from peak-shaving the nuclear energy within each week. Hence, peak-shaving should receive the primary attention. The savings from the weekly redistribution of energy were lower, on the order of hundreds of thousands of dollars per reactor per optimization cycle.

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(4) The system parameters having greatest effect on total system operating costs are (a) system reserves, **(b)** seasonal customer demand- shape, and (c) the economic loading order (in turn comprised of the system configuration and its basic parameters such as heat rates, and fuel costs). These are the system parameters that must be considered **by** the system planner in devising the allocation budget of nuclear energy over the short-range planning horizon.

(5) Using the optimization technigues discused in this thesis, an unambiguous and logical method has been developed to calculate the short-range substitutional cost of nuclear power, the **OCNP.** OCNP is the trade price that should be used when transferring nuclear power **by** utilities.

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2.0 INTRODUCTION TO SHORT-RANGE SYSTEM ANALYSIS 2.1 Introduction

In electric utility *system* planning, there are three principal time periods, the long-range **(10-30** years), the mid-range **(1-10** years), and the short-range (less than **1** year). The major task in long-range system analysis is the planning required to meet system expansion. The major considerations are the power plant type, its size, its location, and its date of introduction to the system. The over-all economics of nuclear power has been so favorable that over half of all new capacity planned in the **U.S.** is nuclear **(1).**

The unconventional batch nature of the nuclear power process and the long lead times in its fuel cycle reguires careful planning; this aspect of system analysis is handled in mid-range planning. The major variables are the reactor's refuel batch size and enrichment. The eight-year lead time necessary for contracting enrichment services and one-year lead time in fabrication requires close coordination of the expected nuclear energy production with the rest of the system components.

In the short-range time frame, in which the nuclear reactor has been charged with its fuel, the system problem becomes that of scheduling generation of the electrical potential available from the fuel. The operating environment is known much more precisely in the short-range taan in the other time frames. Moreover, all the nuclear

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parameters are frozen in the short-range due to its batch nature. Thus the system analysis problem is that of optimizing scheduling of the generation **of** the nuclear plant's limited energy potential over the short-range time horizon in a fairly known environment.

Previous studies in the long-range and mid-range system analysis have been more extensive than in the short-range analysis. The TVA Brown's Ferry study (2) comparing the economics of nuclear power plants to a fossil power plant showed conclusively the advantage of nuclear power. The mid-range system analysis problem studied at MIT (3) and Oak Rilge (4) have led to automated procedures for calculating a power reactor's batch size and enrichment over the mid-range time horizon.

In the short-range operations time frame, the published studies have been mainly limited to **case** studies illustrating advantages of coast-down under certain circumstances (5) . This thesis study investigates the optimization in the short-range of the nuclear reactor generation schedule such to minimize system cost. The resource-limited case is studied in particular since this is where the principal planning problem lies. In the non-limited resource case, the answer is trivial, schedule the reactor at its full capacity and/or revise the refueling date. In the resource-limited case, the scheduling of when .and at what capacity the nuclear plant should be operated is not so obvious.

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2.2 Motivation for Resource-Limited Case

The resource-limited case, 'the one studied in this thesis, is the situation where the nuclear reactor doesn't have enough reactivity to run at full power continuously until its scheduled refueling date and for any of a number of reasons, early refueling is not possible. The amount of thermal nuclear energy to be extracted from the reactor is assumed fixed, limited to full-power reactivity limited burnup. The date of refueling is fixed, and the customer demand function can be forecast. Hence, the resource limited case is a straight-foward optimization problem. Much of the theoretical foundation for the resource-limited case was presented in Hans Widmer's thesis(6). Widmer noted that in short-range system analysis, "the value to the system of the given nuclear energy potential should be used (the system opportunity cost)" in finding the optimal distribution of nuclear energy.

The optimization technique used is a version of Dantzig and Wolfe's Decomposition Principle(7). Once the resource-limited case is solved, it can be extended to include the more complex features of short-range system analysis situations. The operational benefits of moving the refueling date can be guantitatively weighted against the inventory charges and other penalties. The importance of refueling during low seasonal demands can be more accurately calculated; and the significance of stretch-out and the timing of its use can also be studied in more detail. Thus,

the study **of** the resource-limited case in this thesis will develop the tools and procedures and provide a reference case to make possible the study of the more complex short-range situations.

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2.3 Goals of Thesis

The objectives of this thesis are to:

(1) Develop a calculational model for the resource-limited case to optimize the short-range production schedule of the nuclear power plants.

Corollary: Develop a calculation model from which more complex short-range problems can be considered.

- (2) Define the parameters that have significant influence on system cost and the Opportunity Cost of Nuclear Power, locating areas of greatest sensitivity.
- **(3)** Develop generalized rules of thumb for the utility dispatcher on the optimal use of nuclear power reactors.

Corollary: Develop a model that will present the dispatcher with a budget of nuclear energy to be expended over the short-range time horizon.

2.4 Perspective on Short-Range Nuclear Power System **Analysis**

In the early days of nuclear power, the economic justification for nuclear power plants was the main topic of study among system planners (whether to'buy nuclear or to buy fossil?). Some consider the publication of TVA's Brown's Ferry Study (2) the turning point in the utility industry's acceptance of nuclear power. Long-range system analysis deals with the question of how best to meet the future growth in customer demand. The parameters are the types of plants, size of plants, and location of plants. **All** these parameters are closely related to the forecasted composition of the utility's future customer demand. **If** the demand is industrial rather than residential, then base load plants will be preferred over cycling plants. Further, to keep transmission losses to a minimum, future plants should be located as close to future load centers as possible. Hence the utility must anticipate movement of load centers, and/or creation of new ones. The sizes of new plants must be in proportion to service demanded, otherwise either capital is wasted or service requested can not be met. The economics of power production is a consideration in chosing the type of power plant (but **by** no means the only one). The TVA study showed that nuclear was the economically preferred choice for the Brown's Ferry site. TVA's (a system located near the Appalachian-coal mines) move toward nuclear was convincing to the rest of the utility industry in overcoming the industry reluctance to try a new technology. The time

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scale in long-range system planning is from **10-30** years.

Once the decision to build a nuclear plant is made, the long lead times in the nuclear fuel cycle require mid-range planning to provide for the fuel services when needed. The mining industry practice is to open new mines only when demand is assured for the life of the mine (in the form of a long term contract). In most instances, money is advanced **by** the customer to the mining company to provide initial capital to start up the mine. The **AEC** presently requires a ten year notice on enrichment services. Fabrication of fuel takes about a year's time. The financial consequences of long lead times is considerable. The core of a **1000** MWe power reactor is valued at **\$30,000,000.** Thus, the inventory carrying charges would be in the millions of dollars. This places a premium on careful planning and scheduling of fuel services (and in turn, cash flow). The optimization of the nuclear fuel cycle in this time scale is called the mid-range system analysis problem. It deals with optimizing the power production from nuclear power reactors so as to minimize system cost over the mid-range time horizon. Studies in this field at MIT and Oak Ridge (4) have developed procedures for calculating a power reactor's enrichment and batch size over a **3** to **5** year time horizon. At MIT, Paul Deaton (3) developed a System Integration Model (SIM) and a System optimization Model **(SOM).** The SIM generates an optimal production schedule for a particular utility system configuration (using the Booth Baleriaux

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probabilistic simulation technique). The **SOM** searches for the optimal schedule of nuclear reactor's enrichment and batch size to meet the nuclear production schedule set **by SIM.**

The **SOM** relies on a reactor core physics model to provide the intermediate nuclear incremental cost values to perform its optimization analysis. At MIT, core simulation and optimization models (CORSOM) which simulate core physics calculations to find a minimum cost assignment of refuel enrichments and batch size for a given reactor production schedule were developed by J. Kearney (8) and H.Y. Watt (9).

Once the nuclear reactor has been charged with fuel, the system problem becomes one of scheduling the generation of the electricity potentially available from the fuel. This is the basic short-range (less than one year) nuclear power system analysis problem, which is the field of this thesis.

Short-range power system analysis is concerned with the operational aspect of producing and delivering the demanded power for the least cost (under certain rigid constraints). Given the existing network of power plants, the dispatcher must figure out which of his units to make available for the immediate future and the economical distributional dispatch of power generation from each unit.

The demand for electricity fluctuates greatly with geographical location, season and the time of day. For example, the minimum weekly demand at nights and weekends on a system may be only **35%** of the corresponding weekly

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maximum, while the annual minimum demand may represent only 20% of the demand peak. Thus, for the system as a whole, the annual load factor may be only **50%.**

To meet this type of demand requirement, the utilities have at their disposal a wide assortment of different types of power plants with different operating characteristics. The basic operating strategy of nuclear power plants coming on line today is that of base loading them because of their low fuel cost. But as nuclear plants continue to make up an increasing share of the power system capacity, there will be times when demand will be less than a system's nuclear power capacity. Therefore, the optimization of day-to-day operations of nuclear power plants and their interaction with the rest of the power pool is **a** problem worth investigating.

Economic dispatch is concerned with meeting the hour-by-hour load requirements from the units on the line, at least cost. The guiding optimality rule is the "egual incremental production cost criterion". The main operating cost variables are fuel costs, the transmission line losses and the operating efficiencies of generators. To a first-orier approximation, the incremental operating cost is that of the fuel. Since fossil-fuel power plants are continuous processors, the cost of an extra unit of power is equal to cost of an extra unit of fuel. For a nuclear power plant, the calculations of incremental cost of power is not so simple. Nuclear fueling is a batch process whose cost is

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fixed in the short-range time frame.

There are a number of short-range nuclear options at the disposal of the utility to handle short-range deviations just before the scheduled refueling of a nuclear power reactor, for a variety of situations:

- **(1)** Coast-Down: The nuclear reactor has a negative power reactivity coefficient, thus **by** reducing the power level of the reactor, it can be kept critical.
- (2) Lower Feed Water Temperature: The nuclear reactor has a negative temperature reactivity coefficient, thus **by** reducing the water temperature, the reactor can be kept critical, though at lower thermal efficiency.
- **(3)** Alter Refuel Batch Size: If availability was below that expected, one can compensate **by** refueling a smaller batch. However, if availability was higher than expected and one of above methods was used to extend the burnup of the fuel, increasing the refuel batch size at the last minute is not a simple task, because of the long lead times involved in fuel preparation. But if the utility has a number of reactors using the same fuel design and enrichment or belongs to a nuclear fuel swapping pool, larger refuel batch size may be feasible.
- (4) Alter Enrichment: Because of the long lead times in enrichment and fabrication of fuel, this alternative is not usually possible except in cases where the utility could borrow the fuel from another reactor of its

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utility system, with the same fuel design, or from a swapping pool.

- **(5)** Move Refueling Date: With advance notice, refueling may be rescheduled for the revised date when the desired burnup is expected to be reached.
- **(6)** Optimize Production Schedule: To refuel on schedule, optimize the fixed amount of energy available in the fuel until the scheduled refueling date.

Not all of the above options may be feasible, depending upon circumstances. Each option will involve an economic penalty of different size. Lower feed water temperatures will lower the thermodynamic efficiency of the plant. Extending burnup during the present cycle will shorten the next cycle's life time and increase its fuel cost. Refueling before desired burnup is achieved will increase fuel cost of the present cycle. Reducing batch size incurs carrying inventory charges **on** the unused batch. Swapping arrangements are presently unknown but can be expected to entail some service surcharge. Rationing involves the substitution of additional fossil energy to meet customer demand. Obviously, the short-range situation is a very complex and involved problem. Besides the nuclear economic considerations, system reliability considerations(*) are

(*) The major system reliability constraints are: **1** system reserve 2 system security **3** voltage stability 4 current stability

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also involved to pose additional constraints. The refueling date may be difficult to change because (1) system reserve would **be** dangerously low at some other time, or (2) refueling personnel may not be available, having been scheduled elsewhere.

And finally, most short-range options would affect later fuel cycles, which may make necessary a redevelopment of the mid-range plan. Generally, mid-range plans are best adhered to, despite short-range deviations as long as their underlying assumptions are still true. This would imply, that in the case of a nuclear reactor being resource limited, rationing might be the most appropriate option to use. Rationing would have the least disturbing effect on later fuel cycles, and the utility would be able to stay on schedule. As the first step at MIT toward the study of the complex short-range problem, this thesis study concentrated on optimizing the production schedule for a fixed amount of nuclear energy, option **(6),** to be called the Resource-Limited Case.

3.1 Introduction

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The average production cost of nuclear generated electricity has been found to **be** significantly lower than that of electricity generated from fossil fuels $(10, 11)$, such that electric utilities would desire to operate the nuclear units at capacity at all times. This is not feasible when the amount of available energy from the reactor is insufficient to operate the reactor at full capacity continuously until scheduled refueling. **A** shortage of energy is possible considering the large number of factors that are related to the original decision on the energy content in the reactor (i.e., long lead times involved in the nuclear fuel cycle, poor forecasting judgement, or forced outages). Examples of changes in the original planning assumptions which could lead to an energy-short situation are:

- **(1)** The fuel is required to be removed from the reactor after burnup reaches 20,000 MWD/T instead of the originally planned **30,000** MWD/T.
- (2) The plant availability has matured faster than anticipated.

In such cases, available energy of the reactor must be rationed until the next scheduled refueling (if the refueling can not be advanced).

This batch-energy-limited generation characteristic of nuclear units requires modification of the techniques of

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dispatching and unit commitment conventionally used ("Equal Incremental Cost Rule") **by** the electric utility industry to handle the above case. The conventional concept of incremental cost of energy is not applicable to nuclear power plants on the time scale used **by** the electric utility dispatcher (i.e. one hour), because all the major costs associated the nuclear fuel cycle costs are contracted for in advance and fixed before the time of power generation. In the short-range time frame, nuclear energy has no unambiguously definable incremental cost. In fact, nuclear fuel is capitalized and depreciated in service whereas fossil fuel is expensed. The purpose of this research is to develop methods of specifying the optimum dispatching of nuclear generating units in the short-range when each nuclear unit has a fixed refueling date and a fixed amount of thermal energy potential for production by that date.

3.1.1 Method of Solution

The formulation of this problem as a single Linear Programming(L.P.) problem would- involve too many variables to solve in a reasonable amount of time. The deterministic problem of solving the detailed hourly generation schedule for minimum system cost of a utility system composed of **50** units, each of four valve points, and over a one-year time horizon is of an order of magnitude **of 1.6** million variables. Hence, to solve the short-range system analysis -problem efficiently, the method of solution must take advantage of the special structure of the problem.

The resource-limited case is viewed **by** the economist as a "Resource Allocation Problem", deciding how to allocate a resource (nuclear energy) among many consumers (individual time intervals). The "economic optimal" solution is found **by** using the "free enterprise" method, letting the open market place decide which consumer receive a portion of the resource and the amount each receives. The free matket determines allocation **by** the forces of supply and demand. Figure **3.1** shows a typical set of supply and demand curves. The supply curve is monotonically decreasing, as the price increases, the quantity demanded decreases. The intersection of these two curves determines an equilbrium trading price, that balances the supply with the demand for the resource. The equilibrium trading price is a mechanism that determines the allocation of the resource among many potential consumers. Each consumer is allocated just the amount that it is willing to pay for.

In the short-range nuclear allocation problem, where the "actual" market price of nuclear power is ambiguous, the economist uses "shadow prices" **(26)** in the analysis. In the resource-limited case, the supply is "inelastic"; the quantity of resource is fixed. Figure **3.2** shows the supply and demand curves for the short-range nuclear allocation problem. The gross resource demand curve is the summation of the resource demanded from all the possible individual consumers. The gross nuclear energy demand curve is the summation **of** the nuclear energy demanded from all the time

Figure **3.1** TYPICAL **SUPPLY AND DEMAND CURVES**

Figure **3.2 SUPPLY AND DEMAND CURVES** FOR **NUCLEAR** ENERGY

intervals in the short-range time horizon, see Figure **3.3.** Matching the gross supply curve with the gross demand curve determines an equilibrium price. Where this price intersects the individual demand curve of each time interval determines how much nuclear energy each time interval will receive, as illustrated in Figure **3.4.**

A time interval's individual demand curve for nuclear energy is proportional to the "benefit" (to the system) derived from various quantities of nuclear energy. The "benefit" of nuclear energy (to the system) can be measured in terms of savings in operating costs of the other alternative source of energy. This "benefit" is termed the Opportunity Cost of Nuclear Energy **(OCNP).** The individual demand curve in question >i.s a measure of **OCNP** for an individual time interval as a function of nuclear energy.

An individual demand curve can be calculated as **follows: (1)** In a single time interval, calculate the optimal system generation cost for a number of values of nuclear energy, as in Figure **3.5;** (2) find an analytic fit of optimal system as a function of nuclear energy; **(3)** the negative derivative of that function is the **OCNP** curve in question, see Figure **3.6. OCNP** is the incremental savings in system operating cost for an incremental change in nuclear energy.

In summary, the method of solution is as follows: **(1)** calculate a **OCNP** curve for each individual time interval in the planning horizon; (2) determine the eguilibrium **OCNP** for

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the planning horizon **by** matching the gross demand curve for nuclear energy with the **supply; (3)** the inividual allotments of nuclear energy are those quantities read off the individual **OCNP** curves at the equilibrium **OCNP** price.

3.1.2 Implementation

The solution of the one-year time horizon problem has been shown to be a combination of the solutions of many weekly problems. Though the exact combination is not known beforehand, it is distinguish **by** the fact that each week in the time horizon has the same **OCNP.** It can **be** easily shown that this is a stable optimal condition.

The weekly **OZNP** is calculated from the viewpoint that **OCNP** is the cost of the displaced energy when optimally distributed nuclear. energy is marginally increased. In economics, the price of the next best substitutional commodity is also called the opportunity price.

Figure **3.7** shows a simple graphical illustration of determining **OCNP.** Suppose a hypothetical system of two components, one nuclear unit and one fossil, and a two-hour customer demand function, **1900 MW** for the first hour and **900** MW for the second hour, as shown in Figure 3.7a. The fossil unit has **1300** MWe generating capacity and the nuclear unit has **600** MWe generating capacity but only **900** MWHe of energy. The fossil unit has a typically monotonically increasing incremental generation cost curve, a portion of which is shown in Figure **3.7b.** What is the **OCNP** for this set of system parameters? The **OCNP** is that cost of the alternative

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EXAMPLE OF DETERMINATION OF **OCNP** Figure **3. 7**

energy displaced ***by** a marginal increase in the optimally assigned nuclear energy. If the nuclear unit **had 1** MWHe more energy, what would be the cost of the **1** MWHe of displaced fossil energy? The optimal distribution of nuclear energy is displayed in Figure 3.7c; **600** MWH in the first hour and **300** MWH in the second **(*).** Since the nuclear unit is already operating at its full capacity **(600** MW) in the first hour, the marginal unit of nuclear energy would be assigned to the second hour. Hence, the fossil generation scheduled for the second hour would decrease marginally from **600** MWH to **599** MWH. What is the generation cost of that one unit of fossil energy? The fossil incremental heat rate curve, Figure **3.1b** indicates 4.6 mills/KWH. Hence, the **OCNP** of the system is 4.6 mills/KWH. The important condition prior to measuring the displaced energy cost is first to optimally assign all the nuclear energy.

The **OCNP** is that cost of alternative energy above which the nuclear reactor would seek to displace all other energy sources (limited **by** its own generating capacity) in expending all its fixed amount of energy. In this way, the nuclear energy has been distributed to minimize system generation cost, **by** replacing the most expensive energy alternatives. The **OCNP** calculated is associated with the

(*) In this simple example, the optimal distribution of nuclear energy is the condition where the fossil unit's production in the two time intervals is as equal to each other as possible, within the capacity limitations of the units.

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particular amount of weekly nuclear energy distributed, the customer demand function and the system configuration used. But weekly **OCNP** functions are reguired to describe system cost sensitivity over a range of nuclear energy values. The weekly **ONP** function is found **by** calculating explicitly **OCNP** values for a number of values of nuclear energy.

The condition for optimal inter-weekly dispatching of nuclear energy is that the weekly **OCNP** functions for all weeks be equal, subject to the constraint that the total amount of nuclear energy used egual the amount available(*).

The **OCNP** optimization results in the assignment of a specific portion of total nuclear energy to be used each week so to minimize system cost over the short-range time horizon. The dispatcher would be free to utilize that and only that amount of nuclear energy budgeted to meet the weekly system demand. The dispatcher should be cautioned that any sales of nuclear energy across the connected interchange be sold at the optimized **OCNP** price for the planning period because the OCNP represents the short-range system substitutional cost for the nuclear energy.

The implementdtion of the above optimization scheme defines the time interval used for comparison of system costs and defining customer demand as one week. The

^(*) This optimization problem is analogous to the classical dispatching problem of minimizing system cost of a system of all fossil units. That solution is when **all** units operate at equal incremental production cost, while constrained to satisfy the total system demand.

production cost program, PROCOST, solves for the minimal system cost(\$/wk) for specific values of:

- **(1)** the system configuration and its 'operating parameters, such as fuel costs and heat rates;
- (2) customer demand; and

(3) a set **of** nuclear energies for the nuclear reactors.

The minimal cost solution is obtained from the optimal weekly nuclear assignment, which in turn, leads to a determination of **OCNP.** The minimum production cost is obtained **by** running the must-run (base load) units first, and then the hydro(*) and peaking units(**) are dispatched. Next, the optimal distribution of nuclear energy for the week is determined **by** the LP. model. As the last step, the pumped storage and fossil units interactions are calculated analytically.

The PROCOST program is run repeatedly (in the load-duration mode) for a variety of system parameters to generate the large number of data points necessary to define **OCNP** behavior as a function of weekly nuclear capacity factors(***) for each week in the planning horizon. For

- (**) Because of the deterministic nature of this study, usage of peaking units must be assigned, details in Section 4.2.1. Input parameters for peakers includes simulated capacity factors, fuel costs and start-up and shut-down costs.
- (***) For convenience, the normalized parameter, weekly nuclear capacity factor is used in place of nuclear energy.

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^(*) The hydro generation schelule is calculated externally of PR3COST. PROCOST reads in the hydro schedule and subtracts it from the demand function to be fulfilled.

example, the weekly **OCNP** function may be sufficiently characterized by calculating OCNP values at five values of the weekly nuclear capacity factor (i.e., 0.55, **0.65, 0.75, 0.85, 0.95).** Thus, for a **26** week planning horizon, **130 OCNP** values neel be calculated (for a single reactor optimization study). The weekly **OCNP** values are input to a sorting program, **ALLOCAT,** which determines for an overall planning period nuclear capacity factor, the optimal weekly nuclear capacity factor distribution. These optimal capacity factors are re-entered in PROCOST (in chronologic load model mode) to determine the optimal detailed hourly generation schedule for all the units being simulated in the entire short-range time horizon.

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3.2 Assumptions and Idealizations

3.2.1 Deterministic Production Cost Model

The economic dispatch optimization model is a simple power flow problem where the basic time interval is one hour. Electrical circuit stability constraints and transmission loss are not considered. More detailed models concerned with load frequency control and transformer taps are described in Ref. (12,13). PROCOST, the production cost optimization model, calculates only the power distribution from several generators.

A deterministic approach was used to treat both load forecasts and forced outages in the system production cost model, PROCOST. The forecasted customer demand is assumed known with certainty as well as the time horizon (fixed fueling date). To include the effect of the probabilistic distribution of the customer demand would require the use of Stochastic Programming **(27)** and be guite involved. Alternatively using Risk Decision Analysis, Ref. (33), would involve less computations than Stochastic Programming but still more than the deterministic approach. Rees and Larson (23) developed a short-range optimal scheduling program using dynamic programming, but without the capability of simulating nuclear plants. The deterministic method seems to be the quickest and simplest method available.

The deterministic approach also assumes that the system configuration of available power plants is known and fixed throughout each of the week(s) simulated. This implies 10OX

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availability. An alternative to the deterministic approach would be to use the Booth-Balerieux probabilistic utility model (17,18,19). The probabilistic utility model incorporates individual forced outage rates in the system calculation of economically satisfying the system load. This latter model would provide a more realistic set of plant capacity factors and system production costs. The deterministic approach favors the base load units and ignores the peaking units, because of the assumed perfect availability of the thermal units. Therefore, to compensate for this bias, peaking units and hydro units are simulated explicitly to peak shave the demand curve and to meet estimated (input) capacity factors for these units. The fossil units are optimized **by** determining the purely economic loading order and always loading the lowest cost increments first. The nuclear and pumped-storage generation schedules are optimized to peak-shave the resulting demand function.

The peak-shaving operations of the nuclear and pumped-storage are done in series (separately) to reduce the calculational costs involved in a single larger model. The fossil fuel costs of both the two-step and single step methods are identical. The explanation is that the amount of pumped-storage energy is the same in both cases. Since the amount of nuclear is fixed, the resulting fossil generating schedule is the same. Hence, the fossil fuel costs should be the same.

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In short, the deterministic approach was chosen because it was the simplest case that could be studied while retaining most of the factors significant in the short-range optimization problem.

3.2.2 Load Models

^Achronological load model was used to approximate the **168** hour per week customer demand function. The chronologic nature is required to include the effects of fossil plant start-up and shut-down, and also to simulate peaking units and their start-up and shut-down costs. And the modelling of pumped-storage and hydro units (with ponlage) reguired the chronologic model so that it was possible to check that the reservoir level remained within permitted limits. Eventually, the large size of the L.P. optimization model precluded the modelling of the fossil start-up and shut-down costs, which would have required Integer Programming (a very expensive option). The consequence of this omission was believed small, since the system configurations used in the system simulations (modelling the **AEP** system) had little overnight shutdown.

^Achronologic load model sensitivity study concluded that a 40-interval load model was sufficiently accurate in reproducing the fossil incremental capacity factors of a 168-interval model so that the former may be used in optimization studies in place **of** the latter to save computation costs; the details of this study is discussed in Appendix **A** along with the computer programs associated with the load models.

In reproducing **OCNP,** load-duration load models of six intervals were fairly accurate in comparison with the more detailed models. The sensitivity study with load-duration

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load models are discussed in Section **5.2** and Appendix **A.6** The exact number of intervals to use in few-interval models is dependent on the utility's customer demand function, its system configuration, and the accuracy desired in reproducing the results of detailed load models. The principle proven **by** the sensitivity studies is that a large reduction in the number of intervals will substantially reduce computation costs, without impairing accuracy.

The maximum reduction possible in the number of time intervals will depend on the feature of the model to be reproduced with accuracy. Each feature will have a different sensitivity to the number of time intervals in the load model. As discussed above, a greater reduction in intervals is possible when the feature of model of interest is **OZNP** rather than the fossil incremental capacity factors.

As a matter of convenience, holidays were omitted in developing the load models for the simulation studies. **A** low forecasted energy consumption for a week (due to a holiday) would result in a poor prediction of the week's demand function because the effect of the decreased energy consumption is spread over the entire week. The immediate effect would be a poor prediction of the weekly peaks. It has been assumed that utilities would have their own load models that would correct for this deficiency. Since writing sophisticated load models was beyond the range of this thesis, simple load models were used in the simulations, just to generate customer demand numbers. The

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nuclear reactor optimization procedures presented in this thesis are independent of the load models used. **A** summary of current industrial methods in forecasting demand is given in $Ref. (20).$

3.2.3 Nuclear

There are a number of nuclear assumptions in the derivation of the production cost code, PROCOST. This code places no constraints on the rate of change of the nuclear power production from one time interval to the next. Physically, the reactor is adaptable to large and quick load changes, but the fuel presently used in reactors may be constrained in its ability to meet large or rapid changes (21).

Large changes in power are also difficult late in the core life due to the Xenon-135 (Xe) problem. After a prolonged operation at full power, a large power decrease or shut down will result in a substantial build up of Xe. Late in core life, there is not enough excess reactivity to override the Xe. Thus, if allowed to build up before resuming full power operation, a power reactor must wait until the Xe decays away (40-60 hours). Schultz **(14)** has a very good discussion on this Xe control problem. The Xe problem rules out rapid changes in the electrical production of a reactor during its coast-down phase since its excess reactivity is then practically nil. Weekend shutdown would still be possible, however.

Furthermore the codes, as written, allow for no constraint on the minimum power level of the nuclear reactors luring load-following maneuvers.

The L.P. thermal energy model is based upon the assumption that the total amount of thermal energy obtainable from a given reactor before refueling is constant, when limited to full-power reactivity-limited burnup.

3.2.4 Financial

The financial assumptions are very crucial in understanding how the system production cost is derived and applied in the optimization process. The basic financial assumption (under the short-range resource-limited condition) is that the production schedule (power history) of a power reactor has no effect on the cost of the nuclear fuel cycle. Head-end services can not be affected since they have been completed before energy is generated. Since the same end state, the full-power reactivity-limited burnup state, is reached **in** all cases, the tail-end services also will be unchanged. Thus the total cash outlay of the nuclear fuel cycle is undistarbed **by** the generation schedule.

However, more subtle effects result from the time value of money. The timing of (nuclear fuel) depreciation credits (or lease payments), and the timing of fossil fuel cost expenses do have a real financial impact on a utility earnings report, especially in times of high interest rates; see Appendix **E.** This effect favors use of nuclear fuel as early as possible, and defers buying fossil fuel as late as possible. In the mid-range time scale, the time value of woney plays an important role in the decision process, but in the short-range time scale of interest in this thesis, the system reliability considerations outweigh the small economic benefit of distorting the system reserve capabilities. Thus, interest rates have been left out of the system cost calculations for this thesis. Even if the fuel is rented on a heat-delivered basis, the total charge is assumed paid in one lump sum so that the time element can be ignored. Hence, the basic assumption is that there is no variable cost component in the nuclear fuel cycle. The system production cost will **be** exclusively the fossil fuel cost (plus start-up and shut-down costs of simulated peaking. units), expensed as consumed. Operation and maintenance costs are disregarded, as these are assumed to be independent of the mode of operation of the system.

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4.0 OPTIMIZATION **MODELS**

4.1 Introduction

The optimization procedure presented here is a series of separate programs that perform separate tasks. This method insures maximum flexibility and minimum duplication **of** calculational efforts when performing sensitivity studies, such as changing (i) the number of weeks optimized, (ii) a week's system configuration, (iii) the planning horizon resource, or (iv) a week's demand level. The study of a system's nuclear resource is not finished with the completion of a single optimization run, but is a continuing" process. The result of one run provides management insight which suggests study of new parameters for another closer examination of where the greatest sensitivities lie.

The optimization programs are as follows:

- **(1)** PROCOST, the major program which calculates the minimal weekly system cost and the **OCNP** for a given set of parameters;
- (2) **ALLOZAT,** a program which finds the optimal distribution between weeks for nuclear energy from sets of OCNP values.
- **(3)** FOSSIL, a program that calculates the weekly system cost and **OCNP** for a nuclear-fossil system where the power level of the nuclear unit is held constant throughout the week.

PROCOST takes a series of assumed nuclear energy allotments for a particular week and assigns its generation to various times in the week to determine the minimal system cost for each allotment of nuclear power and from this **OCNP. ALLOCAT** takes a set of weekly **OCNP** values over a longer period of time and determines how much nuclear energy to allocate to each week **by** using the criterion that the **OCNP** for all weeks shall be the same.

PROCOST is the system production cost program that calculates the optimal generation schedule from the following input data (i) fossil plant parameters, (ii) peaking unit parameters, (iii) hydro generation schedule, (iv) nuclear unit parameters, **(v)** pumped-storage parameters, and (vi) customer demand function. The user has a choice of specifying whether the nuclear optimization L.P. model use a load-duration model or a true chronologic or modified chronologic load model, the choice depending on the application of the result. rhe pumped-storage generation schedule can be either optimized for economic operation (least operating cost) or for security operation (maximum pumpel-storage reserve capacity).

ALLOCAT is a sorting program that receives as input the collection of weekly **OCNP** functions, with an overall nuclear capacity factor. **ALLOCAT** finds the optimal distribution of weekly nuclear capacity factors **by** using the equal opportunity cost rule.

PROZOST is usually run many times in load-duration mode to generate **OCNP** numbers. When the optimal inter-weekly nuclear capacity factor distribution has been solved **by** **ALLOCAT,** the values are fed back to PROCOST (in chronologic mode) to generate the detailed hourly generation schedule of all the units. The algorithm of **PROCOST** is discussed in Section 4.2 and of **ALLOCAT** in Section 4.3.

FOSSIL is used to calculate system cost for the reference situation when there is no nuclear optimization (constant power level through the week). This simpler program can be used in place of PROCOST in generating **OCNP** values for the case of constant weekly nuclear power level. FOSSIL also is used to calculate **OCNP** values for an alternate and more direct, but approximate, optimization procedure discussed in detail in Section 4.4.

4.2 PROCOST Algorithm

The PROCOST algorithm presented here consists principally of two parts, the optimal generation schedule of nuclear units and the optimal generation schedule of pumped-storage unit. The original reason for dividing the computation was to reduce the computational costs of a single large L.P. model that included both the nuclear and pumped-storage units. Later, a number **of** other constraints(*) on the pumped-storage unit precluded its inclusion in an L.P. model. Figure 4.1 shows the general **flow** chart of the PROCOST algorithm. The nuclear

^(*) These constraints included keeping the reservoir level within bounds, the formulation of a security mode schedule, and difficulty in modelling a pumped-storage unit adequately in a load-duration environment.

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optimization is composed of two parts, and MPSX. The L.P. formulation program, NUC_OPT, writes the L.P. formulation of the nuclear optimization problem. MPSX, an IBM program product, reads the formulation and performs a variety of L.P. optimization and parametric studies. The L.P. solution is read **by** the pumped-storage scheduling program, called PUMPST, which performs either economic or security mode scheduling.

Before NUC_OPT formulates the nuclear optimization, it also performs a simulation of the hydro and peaking units. These subprograms are described in detail in the following sections.

4.2.1 Nuclear L.P. Formulation

The nuclear scheduling problem is solved **by** linear programming (L.P.). To include the important feature **of** variable nuclear heat rates, a special version of L.P. called "separable programming" is used. IBM provides a program product called MPSI (Mathematical Programming Systems Extended) that solves separable programming problems. Thus a preprocessor is required to reformulate the utility system input parameters into the input format required for MPSX , the L.P. formulation of the nuclear scheduling problem. The input to the preprocessor, NUC_OPT , consist of a customer demand function (output from a load model program, MODEL), nuclear, fossil, and peaking units plant data and the hydro.generation schedule. The hydro generation schedule may vary a great deal depending on

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seasonal, geographic, and climatic factors. Thus, the operation of such hydro units are calculated externally and input to the preprocessor. The preprocessor deducts the hydro schedule from the input customer demand function, resulting in a new modified customer demand function which the rest of the system units must satisfy.

The deterministic approach to a demand problem would normally under-utilize higher cost fossil and peaking units (due to the exclusion of forced outages). To partially compensate for this effect, the operation of the system peakers are simulated and forced outages of all fossil units are programmed (scheduled) into the monthly system configurations. Each peaking unit is scheduled to peak-shave the customer demand until its input capacity factor is achieved. Peaking units are called successively, the largest units first, to maximize their effect in flattening the demand function. The rationale for this method of scheduling peaking units is that peakers are observed to be utilized only during peak periods when system reserve is at its lowest point and operated at their full rated capacity. Thus peakers are modelled as single step functions, either on, or off. When needed, peaking units are turned on regardless of cost.

After the peaking unit generation schedule has been determined, the number of start-up and shut-downs for each unit is counted and total operating costs for the peakers calculated. The peaking units' schedule is then deducted from the customer demand function, resulting in a lower modified demand function which the rest of the system units must satisfy. The peaking unit simulator, PEAKERS, operates on each Jifferent weekly customer demand function. The reguired parameters of a peaking unit are: rated capacity(MW), estimated capacity factor, average heat rate, fuel cost, and cost of each start-up and shut-down.

The fossil plant parameters are sorted **by** subroutine PECK_OR that determines the economic incremental fossil loading order and also the fossil must-run level of operation. The latter is then deducted from the customer demand function, resulting in a lower modified demand function which the rest of the system facilities must satisfy. This modified demand function is the one passed to the nuclear scheduling program, **MPSX.** The L.P. formulation of the nuclear scheduling problem is presented as follows:

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Objective function: minimize

 $\sum_{i} \sum_{i} (c_i) (f_* H_i) (f_* X_i^j) (T_i)$ (4.1)

subject to the following constraints:

(customer demand constraint)

$$
\left\{\sum_{i} x_i x_i^j + \sum_{i} \sum_{i} \frac{I_n}{n} x_i^j = D^j \right\} \qquad (4.2)
$$

(limited thermal nuclear resource constraint)

$$
\left\{\sum_{i} \sum_{i} \left(\sum_{n} x_{i}^{j} \right) \left(\sum_{n} H_{i} \right) \left(\sum_{i} \right) = K_{n} \right\} \qquad \qquad \left\{ \sum_{n=1, \ldots, N} \left(\sum_{n=1, \ldots, N} x_{i}^{(n)} \right) \left(\sum_{n=1, \ldots, N} x_{i}^{(n)} \right) \right\}
$$

(bounds, separable programming constraint)

$$
\left\{\begin{array}{l}\n\text{if and only if }\\
\text{then }\\
\begin{array}{c}\n\zeta_{F,n}\times i\rightarrow\\
\zeta_{F,n}\times i\leq\\
\zeta_{F,n}\times i\leq\\
\zeta_{F,n}\times i\neq0\n\end{array}\right\}\n\right\}\n\quad (4.4)
$$
\n
$$
\text{else}\n\left\{\n\begin{array}{c}\n\zeta_{F,n}\times i\leq\\
\zeta_{F,n}\in\mathcal{B}_{i}\n\end{array}\n\right\}\n\quad\n\left\{\n\begin{array}{c}\n\zeta_{F,n}\otimes i\leq\\
\zeta_{F,n}\otimes i\leq\\
\zeta_{F,n}\ot
$$

where:

 $\frac{3}{1}$ = fossil power level of the i-th *F* **i** the **j-th** time period (mw)

increment and
X = power level of the i-th increment and the **j-th** time period of the n-th nuclear reactor- (MW) **J=** -either **XI** or incremental fossil heat rate of the i-th
increment of the loading order (million of the loading order (million BTU/MWHt) *H* = incremental nuclear heat rate of the i-th
 h¹ **i** auclear increment of the n-th nuclear reactor (million BTU/MWHt) ⁼fossil fuel cost (\$/million **BTU)** of the i-th С: increment **DJ=** modified customer demand of the **j-th** period(MW) full-power reactivity-limited thermal energy Kn available in the n-th reactor (million **BTU)** upper bound of the i-th increment (MW) $\mathbf{F} \cdot \mathbf{n}$ = total number of time periods $=$ total number of nuclear reactors = total number of increments in a nuclear reactor duration of j-th time interval (Hours) $T_{\rm i}$

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The objective function, **Eq. (4.1),** to be minimized is a summation of the incremental production cost over all the increments in the fossil loading order (index i) and over the one-week time horizon (index **j).** The incremental production cost is a product of the fuel cost (\$/million **BTU),** the incremental heat rate (million BTU/MWH) and the energy production (MWH) of that time period. The constraints to be met are: **(1)** the summation of the power levels of the individual nuclear and fossil units in each time period must satisfy the modified customer demand, **Eq.** (4.2), while (2) limiting the total nuclear production to the available resources, **Eg.** (4.3). In addition, each variable is bounded, **Eq.** (4.4). This is where the separable programming aspect is featured. **All** increments are fixed at the lower bound of zero until all the preceding increments have been set to their upper bound. For example, the third increment of the loading order can not be started until the second (and the first) increments are fully loaded. Without this feature, variable heat rates could not be modelled.

To examine this problem more closely, notice that many of the fossil increments will always be loaded independently of the amount of nuclear energy to be distributed. For example, assume a fossil imcremental loading order of **100** increments of **100** MWe each. The nuclear unit has a capacity rating of **1000** MWe. In a single time interval, suppose that the customer demand function specifies **8050** MWe to be met **by** the system. Then, irrespective of the optimal amount of nuclear energy assigned to this time interval a priori the first seventy fossil increments must always be fully loaded. Unfortunately, MPSX does not known this a priori. Starting from scratch, MPSX will laborously load each of the fossil increments one **by** one. **A** significant amount of computer time and storage cost is saved **by** having MPSX solve the following equivalent problem instead. For the time interval in question, the fossil incremental loading order is of only thirty increments of **100** MWe each. The nuclear unit is still **of 1000** MWe, but the demand to be met is only **50** MWe. **7000** MWe has been subtracted from both the load demand and

the fossil generating capacity. Hence (in this example), the number of variables has been reduced **by** two-thirds, and the solution computation time cut **by** an order of magnitude, just **by** formulating the same problem from another viewpoint. This improvement of calculating minimum fossil operating levels and subtracting them from the system problem before nuclear optimization has significantly reduced MPSX computer **CPU** time **by** almost an order of magnitude. Specific programming details of NUC OPT are given in Appendix C.

The preprocessor, **NUCOPT**, formats (writes) this information **(L.P.** formulation) to meet **MPSX** input specifications on a transfer medium (such as a scratch disk) as its final product. Execution is transferred to MPSX to solve the nuclear scheduling problem **(by** the revised simplex method) and write the solution on a scratch disk. Execution is then turned over to the pumped-storage program. The programming aspects of MPSX are discussed in Appendix **C.3.**

4.2.2 Pumped-Storage Scheduling Program

The pumped-storage scheduling program, **PUMP_ST,** has three modes of operation: **(1)** security mode to maximize pumped reserve capacity; (2) economic mode to minimize operating costs, **(3)** pumped-storage by-passed completely(*).

^(*) If a pumped-storage unit does not exist, or is an insignificant portion of the system, or is not
important in the OCNP calculational phase, then the important in the **OCNP** calculational phase, then the pumped-storage scheduling routine can
altogether. PUMP ST would then be u altogether. **PUMPST** would then be used just to interpret (and print) the nuclear L.P. solution. See Appendix **C** for details on this option.

The latter choice will be ignored for the remainder of this section. The pumped-storage program first reads and interprets the nuclear L.P. solution. Then control is passed to the economic subroutine, **ECO,** to determine the economic pumped-storage generation schedule. If- the desired mode of pumping is 'security', then the security subroutine, SECURIT is called to calculated the pumping schedule that would keep the reservoir filled as much as possible. Otherwise, the economic pumping schedule is calculated. The reservoir is then checked **for** water overflowing or running dry. Any necessary corrections are then made and control is returned to the main program, PUMPST. **PUMPST** then calculates and prints the capacity factors of both the various fossil increments in the economic loading order, and of all the fossil units themselves. It also calculates total system production cost, and the **OCNP.** Detailed programming specifics are given in Appendix **C.**

This section is further divided in four subsections:

- **(1)** Economic Pumped-Storage Theory
- (2) Economic Pumped-Storage Scheduling Algorithm
- **(3)** Pumped-Storage Security Theory
- (4) Pumped-Storage Security Scheduling Algorithm

4.2.2.1 Economic Pumped-Storage Theory

The economic pumped-storage scheduling problem is an amply documented case **(22).** Originally, 'an L.P. formulation for the pumped-storage problem was devised. But since the solution is well known, this section of the program was rewritten to solve for the solution analytically. With a pumped-storage facility, a utility would pump into the storage facility at times of low customer demand and low incremental cost of power. Stored energy would be discharged at times of peak customer demand and high incremental cost of power. Thus the utility would have lowered production costs **by** the difference between the cost of pumping the water, and the displaced cost of generation at peak demand. If the pumped-storage facility were **100%** efficient and the pump, generator and reservoir were of limitless size, the solution of the scheduling problem would be described (see Figure 4.3) **by** that power level, K, where: **(1)** if the customer demand was above K, the pumped-storage facility would generate that amount equal to difference between K and the customer demand, (2) if the customer demand was below K, the pumped-storage facility would pump that amount equal to the difference between K and the customer demand, and **(3)** the amount pumped and the amount generated were equal over a cycle of the demand function. This is illustrated graphically as follows: Figure 4.2 is a simple load-duration curve representing the customer demand curve for a one-week time period. Power level K is that level where area **Al** equals area **A2** (Figures 4.3 and 4.4) so that the fossil power production is such

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that the fossil power production is levelized (Figure 4.5) and thus, fossil fuel cost is minimized (*).

The fact is that the cycle efficiency is not **100%.** Then the solution is graphically illustrated in Figure 4.6. Returning to the load duration curve, the pumped-storage facility generates power whenever the customer demand is above the power level K1 and pumps whenever the customer demand is below K2 , such that:(1) the incremental cost at K1 equals the incremental cost at K2 divided **by** the cycle efficiency, and (2) the energy generated **Al** eguals the energy stored, **A2** times the cycle efficiency. The first condition is the economic minimal cost criterion and the second condition is the energy conservation principle.

The physical limitations **of** the generator and the pump also make the solution even more complex, as shown in Figure 4.9. **G** and *P* represent the capacity ratings of the generator and the pump, respectively, see Figure 4.10. When the customer demand is above the power level K3, the pumped-storage generator is turned on until its capacity is reached or fossil generation is reduced to K3. When the customer demand is below power level K4, then the pump of the pumped-storage facility is turned on until its capacity is reached or fossil generation has increased to K4. The economic cost criterion dictates that the incremental cost

(*) **A** major assumption used here is that the fossil loading order is strictly economical, the lowest cost increments loaded first, and without regard to start-up and shut-down cost.

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Figure **4.10 PUMPED-STORAGE** DURATION **CURVE** OF FIGURE 4.9

 \bullet

FOSSIL DURATION **CURVE** OF FIGURE 4.9

at K3 eguals the incremental cost at K4 divided **by** the cycle efficiency. The energy conservation principle dictates that the generation energy, area **'A3** equal the pumping energy, area $A4$ times the cycle efficiency (E) .

The physical limitation of the reservoir size reguires that the chronologic water level behavior be checked for overflowing and running dry. The chronologic water level behavior will be a function of generator and pump capacity and the customer demand function. Hence, for a properly designed pumped-storage facility where a utility knows its customer demand, it looks for a site for the pumped-storage facility of compatible reservoir size which in turn dictates generator and pumping capacity in the proper proportions. So in theory, for normal operations, reservoir size should not be expected to be an active constraint. Hence, the pumped-storage scheduling algorithm searches for the solution along the only two active constraints: cost criterion and energy conservation. The algorithm checks the water level after an optimal economic schedule has been calculated. After initially using only the cost criterion as a guide to find feasible pos of cost tradeoffs, the conservation principle is used to move toward maximum energy production **by** the pumped-storage unit. After an optimal schedule has been calculated, the water level is examined for overflows or running dry. If such a case is found, local correction measures are taken at times of violation. Greater details on the correction measures are

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given in the next section. The pumped-storage facility is based on **a** weekly cycle, returning the water level at the end of the week to the level at the beginning of the week (an input specification). Free water inflow into the reservoir is allowed and is assumed to be uniform throughout the week.

4.2.2.2 Economic Pumped-Storage Scheduling Algorithm

In the previous section, the distinguishing characteristics of the economic pumped-storage solution were discussed. In this section, the algorithm to reach the solution is discussed, but **by** a slightly different path than in the previous section. In brief, the algorithm systematically examines a limited number of points that satisfies both the energy conservation principle and the economic cost criterion until the optimal solution is reached. The algorithm locates the loci of points where the energy constraint is active and then proceeds systematically to where the cost constraint is active.

The **flow** chart of the pumped-storage economic algorithm is shown in Figure 4.12. The main program, **PUMP_ST,** passes control to **ECO,** with all the pumped-storage operating parameters including the modified demand function that must be satisfied **by** the fossil increments and the pumped-storage facility. With the additional information of system variables passed from the preprocessor, the data base is formed from which the search for the solution is based. Graphically (see Figure 4.9), the solution is located where

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Figure 4.12 **ECO** FLOW-CHART

the maximum area **A3** (stored energy) satisfies both the cost criterion and energy conservation principle. The maximum area (stored energy) represents the largest utilization and hence the largest cost savings. An enumerative search is made since the number of points satisfying both constraints is small (less than the number of fossil increments), and a computer can search these points very quickly. The search is started **by** determining the lowest feasible value of K3 (Figure 4.12), and in turn, its associated feasible value of **A3** (stored energy) is calculated(*). The value of K3 is increased stepwise until the feasible value of **A3** (stored energy) can no longer increase(**). At this point the optimal solution has been reached.

The starting point of the search is K' (see Figure 4.13), the lowest feasible value of K3. K' is that power level which divides the load-duration curve so that the pumped-storage facility is always pumping or generating without regard for cost, see Figures 4.14 and 4.15. This is the case where the cost criterion is not active. From this starting point, the cost criterion is then introduced. Setting K3 to K' produces a value for K4 (see Figure 4.16). The associated value of A4 is calculated which is compared with **A3.** As illustrated in Figures 4.17 and 4.18, where

^(*) K4 **by** the cost criterion is calculated from K3, which determines area A4 (pumping energy), which in turn, determines the feasible value of **A3** (stored energy).

^(**) Increasing K3, increases K4 which increases A4, (pumping energy),which in turn, increases the feasible value of A4 (stored energy).

PUMPED-STORAGE DURATION **CURVE** OF FIGURE 4.13

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Figure 4.17 **PUMPED-STORAGE** DURATION **CURVE** OF FIGURE 4.16

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energy A3 is out of balance with energy A4 because A3/EA4, the value of K3 is increased to the next higher incremental loading order point. K4 is reset, **A3** and 6A4 are recalculated and compared. This is repeated until they are equal or the balance shifts to the other direction. If the shift occurs, **A3** and A4 are interpolated to the point at which A3=EA4, which determines the maximum feasible pumping. The next step is to re-sort the load duration curve of the pumped-storage facility back to a chronological load curve to check the water level. If the reservoir runs dry, generation is cut back to zero for the required number of intervals (and pumping is likewise adjusted) ; or if the reservoir overflows, pumping is cut back to zero for the required number of intervals (and generation is likewise adjusted). These corrective measures are not performed optimally (in a least-cost sense), but rather to correct the situation as immediately as possible (in as few time intervals as possible).

Finally, the pumped-storage schedule is complete and feasible and the incremental fossil production schedule **by** default is the residual load demand schedule. The detailed pumped-storage schedule is then printed (if desired), and control returned to the main program. The incremental fossil fuel costs are then calculated, and in turn, the total system production cost and the **DCNP** also. **PUMPST** also prints the incremental and each fossil unit's average capacity factors.

As an option, the pumping schedule may be calculated **by** the Pumped-Storage Security Model described in the next section, instead of the economic model discussed in this section.

4.2.2.3 Pumped-Storage Security Theory

Pumped-storage units have proven to be reliable and versatile in helping the utility lispatcher to cope with the statistical fluctuations in meeting customer demand. The pumped-storage facility is guick to adapt to changing load demands with a minimum of strain (24). In fact, utility practice is to assign a large portion of its pumped-storage generating capacity to spinning reserve. For example, AEP's Ludington pumped-storage facility has 460 MWe generating capacity but only **300** MWe is normally scheduled on a planned basis. The remaining **160** MWe capacity is set aside as spinning reserve to take care of equipment forced outages and unexpected load changes.

For the pumped-storage facility to meet this responsibility and to be capable of handling the severest problem, the reservoir must **be** kept as full as possible at all times. This means that whenever the pumped-storage facility is not generating power, it will be pumping water into the reservoir until it is filled. These operational procelures are probably not the least expensive mode of operation. To provide the system with maximum security, the pumped-storage facility has pumping scheduled until the reservoir is full, even though the generation schedule

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Figure **4.19**

doesn't require it and economically, it would be cheaper to wait until the weekend to **do** the pumping. As an illustration, Figure 4.19 is an example of an economic pumped-storage schedule. The figure shows that there is large amounts of pumping on weekends and only a small amount of sub-capacity pumping during the week nights. The security model proposed would do the reverse, pump at rated capacity on week nights until the reservoir is filled, leaving little pumping to be done on weekends.

4.2.2.4 Pumped-Storage Security Algorithm

The peak-shaving pumped-storage generation schedule for this security model is the same as in the economic model. It is characterized **by** the pumped-storage generation level (power level K3 in Figure 4.9), where if demand load is above that level, then the pumped-storage generators produced enough power to make up the difference or until its nominal capcity(*) is reached.

The pumped-storage generation schedule is first calculated in **ECO,** next subroutine **SECURIT** is called to calculate the security mode pumping schedule. **SECURIT** first determines the allowable time periods to schedule pumping, which takes into account a transition interval before and after generation. For each allowable time period, pumping is scheduled for each time interval starting with the time

(*) Nominal capcity is not the rated capacity of the generators, but that capacity intended for scheduled usage, the remainder is for emergency usage.

interval of lowest demand until either the reservoir is filled, or all available intervals have been scheduled. The detailed'algorithm is presented in Appendix **C.** When pumping for the last time period is scheduled **,** the final water level is set to return to the beginning-of-week level. Program control is then returned to **ECO.**

Three simplifying assumptions used in this model are: (i) a weekly water cycle is assumed, returning the end-of-week water level to beginning-of-week starting level; (ii) the cycle inefficiency is assumed to be all in the pumps. For example, for a **50%** cycle efficient unit, the model reguires a 2 MWH pumping reguirement to produce **1** MWH generation resource, but produces a water level change of only **1** MWH. (iii) The (economic) scheduling method used was assumed sufficient. The pumping schedule could be further flattened **by** iterating over the lowest fossil increments, instead of the lowest demand levels. This would greatly increase the bookkeeping and complexity of the algorithm for a slightly smaller cost determination, hence it was not done.

The first two assumptions are also applicable to the economic pumped-storage model. These two assumptions are not fundamental to the successful execution of the program. These assumptions can be easily modified to fit the requirements of the user.

Appendix **C** contains the program listing of the security model and the I/0 specification of the program.

4.3 **ALLOCAT** Algorithm

The optimal allocation of the nuclear energy between weeks is performed **by** the **ALLOCAT** program. Each week is represented **by** a list of **OCNP** values. Maximum utilization of a limited resource dictates that the first nuclear energy increment go to the week having the highest value for nuclear power, **OCNP.** The first increment utilized, the second increment goes to the week having the second highest **OCNP** value. This process is analogous to selling to the highest bidders. Each week has a list of successive lower bids (as **OCNP** values). The central decision maker (the algorithm), one-by-one allocates increments of nuclear energy to the highest bidder first. After each allocation, the going price moves down, until all available nuclear energy has been allocated. In this condition some weeks may have a full supply of nuclear energy (all bids taken) while other weeks may have only the minimum supply (no bids taken). This describes the algorithm used **by ALLOCAT.** The program is told how much nuclear energy is available and **by** increments, allocates the energy to the individual weeks. It keeps track of the energy allocated each week to the unit being optimized, and when all the nuclear energy is allocated, the program lists the final capacity factor distribution. Appendix **D** lists the program along with the input and output from Case **4** (see Section **5.6).**

4.4 FOSSIL

FOSSIL is a program that calculates weekly system cost and **OCNP** for the case of no nuclear optimization. Thus, FOSSIL is principally used as a basis of comparison to measure the savings of the optimized nuclear dispatching schedule. Figuring the optimal fossil dispatching schedule for the case of base-loaded nuclear power (at constant power level throughout the week) is a trivial problem, since there is no nuclear optimization. The fossil algorithm is as **follows:** The constant nuclear power level is subtracted from the modified demand function, leaving the revised demand requirement that is to be fulfilled **by** the fossil units. The fossil units are represented **by** an economic loading order (output from NUC_OPr), hence, it is a simple table look-up operation to figure the optimal fossil dispatching schedule and operating cost. The **OCNP** is the incremental fossil fuel cost of the weekly average fossil demand requirement.

The simplicity of FOSSIL (and its very quick method of calculating **OCNP)** also makes it convenient to use FOSSIL for developing initial guesses for multi-reactor problems. This alternate solution technique inverts the order **of** optimization steps discussed in Section **3.1.** The exact optimization procedure (discussed in Section **3.1)** is to first optimally peak-shave the nuclear energy within each week in the planning horizon (using PROCOST) and secondly calculate the optimal distribution of nuclear energy between

the weeks (using **ALLOCAT).** This procedure is referred to as the "Peak-Shave First" method. The alternate solution technique is to first calculate the optimal distribution of nuclear energy among all the weeks in the planning horizon, assuming a constant nuclear power level in each week, using FOSSIL and **ALLOCAT.** Secondly the optimal nuclear peak-shaved distribution is calculated (using PR3COST) for the optimized energies in the first step. This approach is referred to as the "Peak-Shave Second" method. a comparison of the two methodologies shows the "Peak-Shave Second" method to be a more direct (but approximate) method involving less computations. This method is especially useful in defining the neighborhood of the optimal solution of a multi-reactor problem where the calculation savings would be very large. Section **5.6** presents a numerical example of using the two solution techniques on the same system example.

5.0 System Qetimization Studies

5.1 The sygtem

To test the optimization procedures discussed earlier, three sample system optimization problems were solved. The first was a single-reactor optimization problem, and the second was a multi-reactor optimization problem. The multi-reactor optimization was performed under conditions more severe than "typical" operating conditions. The third optimization problem was a modification of the first in which the monthly configurations were adjusted to yield constant system reserves over the planning horizon.

American Electric Power Service Corporation **(AEP)** proviaed the basic data from which the utility system configuration **(16)** was constructed. The system, composed of **52** units of five power plant types, was simulated for a short-range planning period of six months, April through September. The system includel two nuclear plants **(of 1100** MWe each), one hydro plant (with limited pondage and 200 MWe peak generating capacity), one pumped-storage unit (of **300** MWe generating capacity), seven peaking units and 41 fossil units for a total generating capacity of **19,250** MWe. The fossil units were of three classes, large (1300-400MWe), medium (400-160 MWe) and small (below **160** MWe). The distinction between fossil classes was the shape of their average heat-rate curves. In PROCOST all fossil units are identified with one of three general shapes (or classes), with the amplitude of their average heat-rate curve being an

individual scalar multiple of one of the three standardized shapes. The 41 fossil units were composed of **15** large-sized fossil units, **15** medium-sized fossil units, and **11** small-sized fossil units. The three standardized fossil average heat-rate curves are presented in Appendix B. The standardized heat-rate curve **of** the large fossil class is flat between **0.7** and **1.0** of rated power and steeply rising below **0.7** of rated power. The medium fossil heat-rate curve is similar to the large fossil curve except that its slope is not so steep below **0.7** of rated power. The standardized heat-rate curve of the small fossil class is very different from the other two. The small fossil curve begins at 14,000 BTU/KWH at 0.4 rated power, slopes down to **12,500** BTU/KWH at **0.'7** rated power and slopes up to **13,000** BTU/KWH at rated power.

The maintenance schedule (scheduled outage) of the individual fossil and peaking units proposed **by AEP** is displayed in Table **5.1.** Most of the scheduled outage is placed in the spring and fall months. Since the model is deterministic, forced outage effects are simulated, treating them as scheduled outages also. Table **5.1** also displays the systematic treatment of forced outages. Essentially the same forced outage rate is displayed for each **of** the months. As mentioned earlier, peaking units are scheduled to peak-shave until their input estimated capacity factors are fulfilled. **All** the peakers had estimated capacity factors of **10%** and start-up and shut-down cost of \$100/start-up, except for two

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TABLE **5.1** (CONT'D)

Note: An "X" represents a simulated outage for the entire month. The total time of scheduled outage for each plant corresponds to the actual observed outage rate for similar sized units. The specific forced outage schedule for each unit was chosen randomly. The maintenance schedule was chosen to lie mainly in the spring and fall months.

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gas-turbine units (of **51** and 4 MWe) which had zero start-up and shut-down costs.

The individual plant parameters were supplied **by** AEP in **1973.** The rated capacity, fuel costs and average heat-rate at rated capacity for the 41 fossil units and seven peaking units are tabulated in Table **5.2.** The fuel costs do not reflect the sharp rise in fuel costs during 1974. The hydro unit with limited pondage was scheduled to generate 200 MWe for nine peak demand hours during each workday and 50 MWe at all other times. The pumped-storage unit's operating parameters were: **300** MWe capacity generator, **160** MWe capacity pump, **70%** cycle efficiency, **9300** MWH reservoir capacity and **2300** MWH/week free water inflow into the reservoir. The operation of pumped-storage unit has been discussed in Section 4.3.

The system treated also had two nuclear units of **1100** MWe each. Nuclear Unit **1** was scheduled for refueling on October **1.** In the six months prior to refueling which make up the planning period, Unit **1** was assumed to have **70%** of the energy required to operate base loaded at full rated power. In the first simulation, Unit 2 was treated as a new unit just being introduced to service under a gradual programmed start-up: 20% of full rated power throughout April, 40% of full rated power throughout May, **60%** during June, **80%** during July, and **100%** during August and September.

The forecasted weekly energy consumption during the six months **(26** week) planning period is tabulated in Table **5.3.**

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TABLE **5.2 PLANT** PARAMETERS OF **PEAKING AND** FOSSIL UNITS

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Table **5.3**

WEEKLY ENERGY FORECAST FOR PLANNING PERIOD

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These energy consumption numbers were supplied **by AEP** for simulation purposes. The six-month planning period spanned three seasons, Spring (April and May), Summer (June, July, and August) and Fall (September). The weekly energy consumption was input to a seasonal load model, MODEL, to generate the detailed hourly customer demand numbers. The weekly energy consumption was used as the independent variable of a seasonal customer demand correlation that determined the customer demand function for a week of a particular energy consumption and season. The load model is discussed in Appendix **A** and the detailed weekly customer demand functions generated from the energy forecasted are presented in Appendix A.4.3. The weekly peak demand of each week and the average power level inferred from the energy consumption are also tabulated in Table **5.3.** The calculated peaks were obtained from MODEL; see Appendix **A** for details.

In the six-month period prior to refueling, a reactor with insufficient energy to run at full power until scheduled refueling can be considered a candidate for short-range resource-limited optimization. The second reactor, Nuclear Unit 2, coming on-line with a fully fueled core had an abundant supply of energy and an undetermined forced outage rate and would be undergoing a planned start-up program, so that the reactor's operation was determinate over the short range. Only reactors with limited resource and a fairly certain availability (*) over the short-range time horizon are amenable to short-range system analysis using PROCOST. Availability, at best, can only be fairly certain over a short-range time horizon.

The objective of the first system optimization (Case **1)** was then to find the optimal distribution of weekly nuclear capacity factor of Nuclear Unit **1,** whose overall thermal energy availability is **70%** of rated capacity for the six months planning period prior to refueling. The second power reactor was operated at programmed steps in power levels.

Although the system contained two reactors, the first system simulation (Case **1)** was a single-reactor optimization. The second system simulation (Case 2) was a complex two-reactor optimization. Case 2 used exactly the same system configuration as in Case **1,** except for additional constraints on Nuclear Unit 2, which was limited to **80%** of the energy used in the corresponding periods of Case **1,** see Table 5.4. Nuclear Unit 2 was limited to **16%** capacity factor on energy and 20% of power for April, **32%** capacity factor on energy and 40% of power for May, 48% capacity factor on energy and **60%** of power for June, 64%

(*) The deterministic approach (used in the PROCOST program) assumes the availability of the reactor is known with
certainty. Hence, this assumption imposes certain Hence, this assumption imposes certain
on the use of this short-range $restricctions$ optimization technique. This restriction can possibly be eliminated **by** the utilization of the Booth-Balerieux probabilistic technique, Ref. (16), for modelling forced outages in PROCOST.

TABLE 5.4

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OPERATIONAL **CONSTRAINTS ON NUCLEAR** UNIT 2 DURING THE TWO-REACTOR OPTIMIZATION, **CASE** 2

capacity factor on energy and **80%** of power for **July,** and **80%** capacity.factor and **100%** of power for August and September. The goal of Case 2 was find the optimal weekly nuclear capacity factor distribution of both nuclear reactors. Case 2 was admittedly a contrived case to illustrate: **(1)** a multi reactor optimization, and (2) the feasibility of the procedures to handle a complex and involved situation. Case 2 is not an ordinary straight-forward two-reactor optimization. Nuclear Unit 2 had five smaller separate planning periods, reguiring a separate optimization in each period. Nuclear Unit 2 was analogous to a collection of five reactors, with each reactor operating for only one period and shut down for the other periods.

Case **3** is a single reactor optimization similar to Case **1.** The only difference between Case 1 and **3** is that the monthly fossil configurations were adjusted in Case **3** to levelize the minimum monthly system reserves over the six-month planning horizon. The adjusted fossil monthly maintenance and forced outage schedule for Case **3** is tabulated in Table **5.5. All** other system parameters of Case **3** are identical to Case **1.**

This completes the description **of** the system environment and the three optimization problems. **A** complete listing **of** all the parameters used in Case **3** is tabulated in Appendix **C.7.** The solving of the optimization problem reguired a very fast method to calculate **OCNP** values. The next section describes the load model sensitivity studies

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Table **5.5**

MAINTENANCE AND FORCED **OUTAGE SCHEDULE** OF **PEAKING AND** FOSSIL UNITS FOR **CASE 3**

	MAINTENANCE SCHEDULE												ASSUMED FORCED OUTAGE SCHEDULE											
Month:		J F M			A M J J A						S O N D			$J \tF$	M		A M J J			A S		\mathbf{o}	N	D
FOSSIL																								
$\overline{31}$	x																			X X				
32				x																		x		
33	\mathbf{x}	\mathbf{x}	$\mathbf x$	\mathbf{x}	\mathbf{x}	\mathbf{x}	\mathbf{x}		X X X															
34												$\mathbf x$										$\mathbf x$	$\mathbf x$	
35									x														$\mathbf x$	\mathbf{x}
36												x									x			
37			$\bf x$																					\mathbf{x}
38 39							$\bf x$										X X							
								٠			$\mathbf x$							$\mathbf x$						
40					x									\mathbf{x}	\mathbf{x}									
41										x									$\mathbf x$	x				

Table **5.5 (CONT'D)**

Note: An "x" represents a simulated outage for the entire month. The total time of scheduled outage for each plant corresponds to the actual observed outage rate for similar sized units.
undertaken to meet this goal. The subsequent sections discuss the results and the conclusions **of** the three system optimization problems.

5.2 Load Model Sensitivity **Study**

The primary intent of this thesis study was to develop a calculational procedure to analyze short-range options of a nuclear utility system that is quick, efficient and accurate. The practical usefulness of such a survey program requires that execution to be low in cost. Developing such a program **by** necessity involves making some sacrifices in accuracy when analyzing a large complex problem. Hence a sensitivity study was undertaken to find the optimal cost-effective load models appropriate to use in the short-range optimization procedures. As discussed in section **3.1.1,** a detailed L.P. model to determine the optimal generation schedule'for a large utility system would involve a problem with a million variables. This problem can be solved piecemeal **by** solving many smaller problems to lead to the solution of the original large problem.

DCNP is the concept used to relate smaller weekly optimization problems to the original optimal nuclear generation schedule problem. **A** detailed (hourly) weekly generation problem is an L.P. problem of 10,000-variables, which while manageable, is still too large a problem to solve **500** times to generate **500 OCNP** values. The first phase of the optimal nuclear generation schedule problem is to find the optimal weekly nuclear capacity factor distribution, for which only the **OCNP** values of the weekly

optimization problem is required. Other information about the optimized solution such as system production cost, fossil incremental capacity factors, and the detailed generation scheduled are superfluous (at this stage of the optimization process).

Since only a single feature **(OCNP)** of the weekly optimization problem was deemed important (in the first phase), reproduction of that single feature in a much simpler calculational model was sought. For this purpose, load-duration load models were tested for their ability to reproduce **OCNP** values obtained from more detailed chronologic load models.

In parallel with this load-duration **OCNP** study, there were efforts to find a simpler chronologic load model to reduce computational costs where the chronologic demand pattern was important. The simple chronologic load model would retain the ability to reproduce the system production cost, **OCNP,** and fossil incremental capacity factors of a more detailed load model.

The simpler chronologic load model also provided a standard of comparison with which to judge the various load-duration load models.

The chronologic load model sensitivity study investigated a great many variations of the **168** hour weekly load model. The initial set of load models included 84 2-hour intervals, 54 3-hour intervals, and 42 4-hour intervals. **Of** the three, only the 84 2-hour interval load model yielded satisfactory reproduction results. Further reduction of time intervals involved the use of non-uniform time intervals and combining the three average workdays together, aside from the peak workday and low workday. Thus, a modified chronologic 40-interval load model was developed, composed of a 10-interval peak workday, a 10-interval average workday, a 10-interval low workday, and a 10-interval weekend. This 40-interval modified chronologic model reproduced with sufficient accuracy the details of the 168-hour representation. Thus, it was chosen as the standard to judge the load-duration models. Further details of the chronologic sensitivity study are presented in Appendix **A.5.**

Preliminary work on the load-duration sensitivity studies showed that models of very few time intervals (between six to ten) were in surprisingly good agreement compared with the very detailed load-duration models in reproducing **OCNP.** The details of these preliminary studies are discussed in Appendix **A.6.**

Before choosing a six-interval load-duration load model for generating OCNP values (required for the three system optimization studies), a number of comparisons were made with more detailed load models. The study included the comparison of the weekly **OCNP** function of a typical summer week obtained from six load models: a 120-interval modified chronologic model **(A),** two 50-interval load-duration models (B and **C),** a 40-interval modified chronologic model **(D),** and

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COMPARISON OF **A** TYPICAL SUMMER WEEKLY **OCNP** *FUNCTION* FROM SIX **LOAD MODELS**

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two six-interval load-duration models **(E** and F). The *six* models and their **OCNP** values are described in Table **5.6.** The system environment for this comparison was the same as those conditions representing the first week in August of the first system simulation, Case **1,** discussed in the previous section. The agreement in results of Model **E** compared with the more detailed models is very good. The difference in the weekly **OCNP** functions for Model **E** compared with the weekly **OCNP** function of Model **A** is **by** only one increment (at **0.55** nuclear capacity factor). Similarly, the deviation of Model **E** from the weekly **OCNP** function obtained from Model **C** is **by** only one increment at one nuclear capacity factor, and from Model B at a single increment each at two nuclear capacity factors. Model **E** agrees perfectly with the standard, Model **D.** The results of Model F (also listed in Table **5.6)** are in poor agreement with the other models. Model F agrees at only two out of five points compared with Model **A,** and at only three out of five points compared with Model **D,** the standard **of** comparison. The fossil economic incremental loading order (derived from the August system configuration) used in this study is presented in Table **5.7.**

The subtleties in calculating the correct **OCNP** value are illustrated from observing the differences between Model E, with a constant heat-rate and Model F, with a variable heat-rate. One model yields very accurate answers and the other contradictory values even though both models have the same number of time intervals. Since a variable nuclear

AUGUST ECONOMIC FOSSTL LOADING ORDER

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TABLE **5.7 (CoNT'D)**

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heat-rate is the more realistic representation, it seems peculiar that the constant nuclear heat-rate model, **E,** gives more accurate results than the variable nuclear heat-rate model, F. The explanation lies in fact that a detailed represenatation of the nuclear heat-rate is incompatible in a coarse load model representation. In a six-interval model, each time interval represents about 20-40 hours. The nature of the L.P. model is such that the power level of each unit is constant for the duration of each time interval. This distortion effect is serious when the six-interval model schedules a reactor to generate power at a partial power level for only two time intervals, which in reality may represent **20-60** hours. In comparison, the detailed models would have scheduled the same reactor (under the same conditions) to a partial power level for only **10-30** hours. (The exact number depending on the customer demand function and the other system parameters.)

The principal reason for the smaller number of hours (in the detailed model) is that a variable nuclear heat-rate representation places a premium on operating at the most efficient power level as much as possible. Thus, a detailed model would schedule a reactor to operate at full rated power most of the time and operate at partial power as little as possible, i.e., about 20 hours a week. **A** six-interval model is handicapped in that each of its time interval represents 23-40 hours so. that if it scheduled a reactor to be at a partial power level for only two time

intervals, that may represent as much as **60** hours. The overall effect of the differences in hours at partial power is that the overall average effective nuclear heat-rate is lower for the detailed load model than the six-interval model. This implies more nuclear electricity generated (from the same amount of thermal nuclear energy) for the detailed model than the six interval model, and in turn, a lower **OCNP** value. Therefore, the differences in **OCNP** values of a six interval model, with variable nuclear heat-rate (compared to a detailed load model) are inherent.

This difference in nuclear electricity also explains why using a constant nuclear heat-rate is necessary in a six-interval model. The nuclear heat-rate value in the constant heat-rate model egualed the **100%** rated power value. **A** six-interval model that utililizes the same amount of nuclear electricity (that a detailed model would), is more likely to calculate the same **OCNP** value. This argument is illustrated **by** examining the optimal nuclear and fossil generation schedules calculated from three load models (F, **D, E** as described in Table **5.6)** for the same sample problem, presented in Table **5.8.**

Table **5.8** deals with a typical summer week, with Nuclear Unit **1** limited to **75%** average capacity factor. The solution for Model F, Table 5.8a, shows that there are two time intervals equivalent to **60** hours when Nuclear Unit **1** is at partial power. **By** contrast, the solution for Model **D,** Table **5.8b,** shows that its Nuclear Unit **1** is at partial

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NUCLEAR-FOSSIL GENERATION **SCHEDULE** OF THREE **LOAD** MODELS FOR **A** TYPICAL SU1MER WEEK **AT 0.75 NUCLEAR** CAPACITY FACTOR

Table **5.8a**

Table *5.8e*

Table **5.8b**

40-Interval Modified Chronologic with Variable Heat Rate

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Only intervals when Nuclear Unit **1** is at partial power are listed

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power for nine intervals for an equivalent of **37** hours. The solution of Model E, Table 5.8c, shows its Nuclear Unit 1 is scheduled for only one time interval at partial power for an equivalent of **36** hours, almost the same as Model **D.** Therefore, it is not surprising that Model **E** will yield a more consistent set of **OCNP** values than Model F.

A further verification for using Model **E** (for generating **OCNP** values) is the results of a study comparing the weekly **OCNP** funztions of Model **E** with Model **D** under different system operating conditions. The four system operating conditions, taken from the first system optimization problem, included: **(1)** a typical spring week, the third week of April, (2) a typical summer week, the first week of August, **(3)** the peak summer week, the second week of August and (4) a typical fall week, the fourth week of September. The weekly **OCNP** functions are tabulated in Table **5.9.**

The farty intervals in Model **D** were obtained from a reduction of-the 120 interval modified chronologic load model **(*).** This reduction is further explained in Appendix **A.** The six intervals in Model **E** were obtained from a

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COMPARISON OF WEEKIY **OCNP FJNCTIONS** BETWEEI **A** SIX INTERVAL LOAD DURATTON (E) MMDEL **AND A** 40 INTERVAL HYBRID **MODEL (D)**

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reduction of the same forty intervals used in Model **D** (**). **A** comparsion of the 20 **OCNP** values from each load model (of Table **5.9)** shows differences in only six **OCNP** values. **Of** the six **OCNP** aff-values, four out of six show differences **by** only one fossil increment level. Hence, only two **OCNP** values (from Model **E)** out of twenty values deviate more than one fossil increment from the the reference values (from Model **D).** Three of the **OCNP** off-values, including the two severely off-values are located at the **0.95** nuclear capacity factor where there is inherent difficulty for a six interval model to reproduce **3CNP** values accurately. Excluding the **0.95** nuclear capacity factor region, the agreement between the Model **D** and Model **E** is almost perfect except for three points where the difference at each point is off by only one fossil increment.

The inherent difficulty at **0.95** nuclear capacity factor (and any nuclear capacity factor near unity) lies in the fact that a few-interval load-duration model does its poorest task of approximation at the extremities of the load-duration curve. The lower end of the load-duration curve is where the **OCNP** of **1.0** weekly nuclear capacity factor is determinel. Hence, all **OCNP** values for weekly

^(**) Notice that the typical summer weekly **OCNP** function of the model of Table **5.9** is slightly different from the model of Table 5.6. The reason is that the six-interval model of Table **5.6** was obtained from a direct reduction of the 120-interval model whereas the six-interval model of Table **5.9** was obtained from a reduction of the forty-interval load model. Hence the two six-interval models were slightly different.

nuclear capacity factor near unity, obtained from a few-interval load-duration model, are of low-accuracy. This is not a serious drawback for the few-interval load-duration model since, in the resource-limited situation, the region of interest is far below unity. Only **in** the non-resource-limited situation is the region of interest near unity. In such a case, the optimization procedures discussed here would not be applicable.

There is an inherent reason why four out of six **OCNP** off-values are positive deviations. In a variable nuclear heat-rate model, there is a bias toward scheduling nuclear generation at high (more efficient) power levels over low power levels (*). This bias effectively lowers the calculated **OCNP** value, because **OCNP** is calculated only from those intervals for which the nuclear unit is partially loaded. The average partial loading (of the nuclear power level) is higher in the many-interval model with variable heat-rate, and in turn, the critical fossil incremental power level(**) is lower, and hence **OCNP** is lower.

This effect is amply illustrated **by** re-examining Table **5.8b** and Table **5.8c,** an optimal solution from Model **D,** with variable heat-rate compared with Model **E,** with constant

- (*) For reasons of economy, the variable nuclear heat-rate model tends to shut down generation during some intervals which otherwise would be lightly loaded, to raise the power levels of other partially loaded intervals to more efficient operating power levels. (**) Critical fossil incremental power level is the power
	- level used to determine the **OCNP** value. Refer to Section **3.1.1** for the determination of the **OCNP** value.

heat-rate. Model **E** had a partial nuclear power setting at **275** MWe and Model **D** had an average nuclear partial power setting of 832 MWe. Similarly, the critical fossil incremental power level for Model **E** was **2057** MWe; while for Model **D,** the (weighted average) critical incremental power level was **2031** MWe.. It is expected for two models with the same average nuclear heat-rate that the critical fossil incremental power level will be lower for a variable heat-rate model than for a constant heat-rate model. Therefore, most **OCNP** deviations of Model **E** compared with Model **D** would be positive, which is comfirmed **by** the experimental results.

It is possible to compensate for this effect **by** assuming a lower effective nuclear heat-rate for the constant nuclear heat-rate model than used in a detailed load model simulation. This is the justification for using an average nuclear heat-rate value equivalent to **100%** rated capacity in the six-interval model for system optimization studies.

In conclusion, the satisfactory results of the six-interval load-duration model with constant nuclear heat-rate was used in obtaining the weekly **OCNP** functions for three system simulations. As mentioned earlier, further details on the load-duration sensitivity studies are supplied in Appendix **A.6.**

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5.3 Single Reactor Optimization Study **-** Cagse **¹**

The single reactor optimization study involved finding the optimal weekly nuclear capacity factor distribution over a 26-week time horizon for a 1100 MWe nuclear reactor in the system described in Section **5.1.** First, the optimization procedure is to calculate a weekly **OCNP** function for each week in the time horizon using PROCOST. The **26** weekly **OCNP** functions are tabulated in Table **5.10** and plotted in Figure **5.1 by** their respective months. The OCNP values have been calculated for values of weekly nuclear capacity factor between **0.55** and **0.95** at intervals of **0.10.** The values for the weekly nuclear capacity factors were chosen arbitrarily. The density and spacing of data points is at the user's discretion. The criterion depends on which of the system conditions are being modeled. Secondly, the **26** weekly **OCNP** functions were fed to **ALLOCAT** to calculate the optimal weekly nuclear capacity factor distribution. The results are tabulated in Table **5.11.** The weekly nuclear capacity factors were allowed to have a maximum value of **0.95,** a minimum value of **0.55** and intermediate values at intervals of **0.10.** Before discussing the optimization results further, some fundamental principles of **OCNP** must be stated first.

Examining Figure **5.1** or Table **5.10,** these distinguishing characteristics of weekly **OCNP** functions are discernable: **(1)** The **OCNP** functions are monotonically decreasing functions with respect to an increasing nuclear capacity factor. (2) The weekly **OCNP** functions of different

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TABLE 5.io

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WEEKLY **OCNP FUNCTIONS** FROM THE SINGLE REACTOR OPTIMIZATION **(CASE 1)**

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OPTIMAL WEEKILY **NUCLEAR** CAPACITY FACTOR FOR THE SINGLE REACTOR OPTIMIZATION DISTRIBUTION (CASE 1

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weeks (but the same monthly fossil configurations) never cross. **(3)** For weeks **of** increasing weekly energy consumption, the **OCNP** function likewise increases. (4) The larger the weekly energy consumption (with the same fossil configuration), the larger the slope of the **OCNP** function. **(5)** The weekly **OCNP** functions assumes a shape characteristic of their respective economic loading order. **(6)** The amplitude of the **OCNP** function varies inversely with the weekly system reserve. **(7)** The higher the average fossil fuel cost of the monthly system configuration, the higher the **OCNP** value.

The basis for the above characteristics of **OCNP** is the fact that the particular **OCNP** values are obtained indirectly from the economic loading order. It is the interactions of the system reserve and the demand function that determines the exact location on the economic loading order that an **OCNP** is read off. To clarify the latter two points **(6** and **7),** reference may be made to Table **5.12,** a tabulation of the average fossil fuel cost of all the fossil components of the monthly system configurations, and Table **5.13,** a tabulation of the system's weekly reserve.

The results of Case **1,** the optimized weekly nuclear capacity factor distribution tabulated in rable **5.1** reflects many of the **OCNP** principles stated above. The overall nuclear capacity factor for the six-month planning period was **70%.** The high weekly nuclear capacity factor for September reflects the unusually high fossil fuel cost for

MONTHLY **AVERAGE** FOSSIL **FUEL COSTS** OF THE FOSSIL CONFIGURATION FOR **CASES 1 AND** 2

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MonthWeek

Total gross generating capacity, MW Fossil maintenance outage, W Nuclear scheduled outage,* **^m** Fossil forced outage, **Ad** Net generating capacity MW Weekly peak load, NW Net reserve, **1.**

MonthWeek

Total gross generating capacity, M Fossil maintenance outagj, **MW** Nuclear scheduled outage, MW Fossil forced outage, NW Net generating capacity, **M** Weekly peak load, MW Net reserve, **NY**

MonthWeek

Total gross generating capacity, MW

Fossil maintenance outage, MW Nuclear maintenance outage⁷ MW Fossil forced outage, MW Net generating capacity, W Weekly peak load, MW Net reserve, MW

440 440 440 440**2,555 2,555 2,555 2,555** 15,415 15,415 15,415 15,415 **13,951** 14,227 **13,793 13,456 1,464 1,188 1,632 1,959** August₁ 2202,045 2,045 **16,600** 16,600 **16,600** 16,600 **16,600** 12,954 14,143 **13,869 14,226** 14,o79 **3,646** 220 2,457 **2,731** 220 2,045 220 2,045 2,374 2,045 *2,521* Seotember

*Program startup limitation for Nuclear Unit 2.

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that month. **All** the other months have about the same fossil fuel cost, as shown in Table **5.12.** September, due to its significantly more expensive fossil fuel cost configuration is scheduled to generate at near full capacity, to displace as much of the expensive fossil fuel as possible. August and July have the lowest average weekly nuclear capacity factor, in fact, the lowest allowed, because of their large reserve capacity, rable **5.13.** April has the lowest system reserve, hence the second largest set of weekly nuclear capacity factors. May is the second tightest month system reserve-wise, and also has the second highest fossil fuel configuration. May also has an above average monthly nuclear capacity factor. June has the lowest fossil fuel cost configuration and sufficient reserve such that its monthly nuclear capacity factor is below the average for the whole planning period. Within each monthly schedule, the weekly allotments of nuclear energy are proportional to the weekly energy consumption forecast, see Table **5.3.** The low summer. (June, July, and August) weekly nuclear capacity factors also reflect a seasonal influence. Demand peaks fluctuate a great deal more during the summer than during other seasons. Hence, the average capacity factor for the summer would be lower than during any other season with the same system reserve.

The overall impression from the results of this optimization study for the system. simulated is that the maintenance scheduled was too unbalanced in excluding summer maintenance. Gross generating capacity is large enough to handle the summer peaks while still scheduling more maintenance during August and July, and less during April and May. Also, a better mix of fossil plants should be scheduled for September to give a lower fossil fuel cost rate.

A total system cost calculation from the optimization results of Case **1** showed a very large dollar savings; see Table 5.14. Comparing the situation of no nuclear optimization, Case **1.A,** (uniform hourly nuclear power generation for the entire six months), with the situation of constant weekly nuclear capacity factor, Case 1.B (optimized hourly generation), the saving was \$4.4 million in fossil fuel costs. **By** further optimizing the weekly nuclear capacity factor distribution over the six-month time horizon, Case **1.C,** the saving increased **by** another \$340,000. For comparison, the total fossil fuel savings are eguivalent to **66%** of the nuclear fuel cost of Nuclear Unit **1,** at 2.0 mills/KWH. The order of magnitude of the savings for Case **1** indicates that even for a single-reactor utility system, short-range optimization is worth-while in the resource-limited situations.

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		Case 1.A	Case 1.B	Case 1.C
Month	Week	No Nuclear Optimization (\$)	Hourly Optimization (\$)	Hourly and Weekly Optimization (\$)
April	ı 2 $\frac{3}{4}$	10,897,641 11,310,309 10,401,792 9,496,691	10,703,601 11,002,306 10,220,996 9,326,228	10,524,562 10,708,211 10,056,930 9,373,436
May	5	10,585,981	10,406,225	10,227,973
	$\overline{6}$	10,078,719	9,886,612	9,830,631
	7	10,316,433	10,126,110	10,063,502
	$\dot{\mathbf{8}}$	10,660,648	10,482,397	10,300,385
	9	9,762,971	9,611,780	9,660,533
June	10	9,899,898	9,755,839	9,802,719
	11	10,210,651	10,063,304	10,013,456
	12	9,725,349	9,586,475	9,632,938
	13	9,369,029	9,242,724	9,387,855
July	14	8,847,012	8,746,190	8,873,310
	15	9,950,572	9,816,608	9,959,853
	16	9,670,594	9,555,670	9,692,954
	17	10,037,142	9,858,900	10,004,974
	18	9,883,377	9,753,496	9,894,948
August	19	9,623,066	9,517,456	9,652,246
	20	10,378,333	10,230,513	10,380,137
	21	10,002,896	9,877,511	10,016,482
	22	10,101,697	9,968,648	10,109,134
September	23	11,538,985	11,379,984	11,101,378
	5ŗ	10,879,069	10,716,938	10,559,049
	25	10,908,873	10,745,769	10,586,767
	26	11,551,409	11,390,192	11,216,616
Total		266,089,137	261,988,509	261,648,975
Comparison with Case 1.A			(4,100,629)	(4,440,162)

Table 5.14 SYSTEM FOSSIL FULM **COSTS AND SAVINGS** FOR **CASE 1**

Case **1.A:** Unit **1** is run at constant power **(725** Mw), and Unit 2 is run at programmed power levels (Table **-5)** for **all** three cases.

Case 1.B: The weekly energy output of Unit **1** is the same as in Case **1.A,** but the hourly power level within each week is optimized.

Case **1.C:** Unit **l's** power levels for each hour of each week are optimized for the entire six-month planning period.

Total energy output of Unit **1** is the same in all three cases.

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PROGRAMMED **CONSTANT** POWER LEVELS OF **NUCLEAR** UNIT 2 FOR **CASES** 1 **AND 3**

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5.4 Multi-Reactor Optimization Study **-** Case 2

In a multi-reactor resource-limited optimization, the optimal solution is- approached iteratively. In 'the first iteration a weekly nuclear capacity factor distribution is assumed for all the reactors in the system except one, the first reactor to be optimized. The resulting weekly **OCNP** functions for that reactor (for the entire planning period) are input to **ALLOZAT** to calculate its optimal distribution. In the second iteration, the first reactor is assigned the capacity factor distribution obtained in the first iteration, and the second reactor is optimized (via **ALLOCAT),** with all the other reactors having the same weekly nuclear capacity factor distribution used in the first iteration. This process is repeated for each reactor in the system successively. The first cycle of optimization is complete when each reactor has been optimized once. **A** second cycle of optimization is initiated to improve on the first cycle siace more complete information is then known about the operation of the system nuclear reactors. The cycles of optimization are repeated until there is a convergence of all the reactors' weekly capacity factors, or until improvement in system costs savings becomes insignificant. These optimization procedures are illustrated below.

The multi-reactor optimization problem considered in this thesis, Case 2, is an extension of the first simulation, with the added complication that Nuclear Unit 2 is also assumed to be limited in its production capacity.

The operating constraints of Unit 2 are given in Table 5.4. Nuclear Unit **1** has a **70%** overall nuclear capacity factor for the same six month planning period. The remainder of the system is the same as Case **1,** described in Section **5.1.** The first step in finding the optimal weekly nuclear capacity factor distribution of both reactors was to calculate the weekly OCNP functions (using PROCOST). The weekly **OCNP** functions for Nuclear Unit 1 were calculated for weekly nuclear capacity factors from **0.55** to **0.95** at intervals of **0.10.** The weekly **OCNP** function of Nuclear Unit 2 were calculated at four nuclear capacity factor values for April **(8,** 12, **16,** 20%), four for May **(16,** 24, **32,** 40%), five for June **(36,** 42, 48, 54, **60%),** five for July (48, **56,** 64, **72, 80%)** and five for August and September **(60, 70, 80, 90, 100%).** The weekly **OCNP** functions for Case 2 are tabulated in Appendix B.3.

OCNP values are required for all the possible permutations of the weekly nuclear capacity factors of the two reactors to be pre-calculated because:(1) it is not known before hand which **OCNP** values are needed; (2) there is an economy of scale in computational efforts (and costs) in calculating all **OCNP** values at once, instead of **by** a piecemeal process. This procedure calculates many more **OCNP** than needed. However, **OCNP** calculations via six-interval load-duration models are fast enough that it is not a serious drawback. As experience (and insight) on the utility system responds is gained the system planner will be able to specify a much narrower range in nuclear capacity factors (and hence need few **OCNP** data points calculated). This will greatly reduce computational costs **by** eliminating the calculation of most of the unnecessary OCNP values and will be especially desirable as the number of reactors increases.

In deciding which reactor (Unit **1** or 2) to optimize in the first iteration, Nuclear Unit **-1** was noted to be relatively 'more' resource-limited, and that Unit 2 has strict limitations on shifting its energy from week to week. Thus, it seems that starting the optimization process with Unit **1** would lead to more rapid convergence. Hence, Nuclear Unit **¹**was optimized in the first iteration. where Nuclear Unit 2 is assumed to have a constant weekly nuclear capacity factor distribution. Table **5.16** tabulates the nuclear capacity factor distribution of each reactor at the end of each iteration. Under Column I of Table **5.16** are listed the results **of** the first multi-reactor iteration. The only difference in system conditions between the first iteration of the multi-reactor optimization and the the single reactor optimization problem is that Unit 2 has 20% less energy, across the entire **26** weeks. The difference in results comparing the solution of the first iteration (of the multi reactor case) with the solution of the single reactor optimization (Table **5.11)** is a shift in energy from April and June to September. To a first approximation, all months should be equally affected. As stated earlier, the

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OPTIMAL WEEKLY NUCLEAR CAPACITY FACTOR DISTRIBUTION FOR THE MULTIREACTOR SIMULATION **(CASE** 2)

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reason for September's larger use of nuclear energy is its higher fossil fuel cost alternative. Hence, September has a relatively greater need for nuclear energy.

Nuclear Unit 2 has five separate planning periods in the six month planning horizon under consideration. In each of the smaller planning periods is associated a different operating capacity level and a different capacity factor objective. Hence, Unit 2 is **bE** treated as, if it is a collection of five separate reactors where only one reactor is on-line at a time.

In the second iteration, Unit 2 is optimized five times, in each **of** its separate planning periods. Nuclear Unit **1** is assumed to have the distribution calculated **by** the first iteration. The weekly **DCNP** functions of Unit 2 used in its optimization must be carefully matched to the proper weekly nuclear capacity factor of Nuclear Unit **1.** The results **of** the second iteration are listed in Table **5.16** under Column II. The weekly distribution of Unit 2 (in each month) shows a correlation of nuclear capacity factors to the energy consumption pattern in each month.

For weeks of higher energy consumption, the weekly nuclear capacity factor is higher. The exception is May where most of correlation effect was already displayed in Unit 1's May weekly nuclear capacity factors. The step sizes in may's value of weekly nuclear capacity factors were large enough not to require any further changes in Unit 2's May weekly nuclear capacity factors. Optimizing each

reactor of the system once completes the first cycle of the optimization process. The second cycle starts (iteration III) with Unit **1** being optimized again, from the weekly nuclear capacity factor distribution for Unit 2 solved in iteration II. The results of iteration III compared with iteration I show that only the weekly nuclear capacity factors of April have been changed, indicating that absolute convergence is near. Iteration IV of Unit 2 shows identical results to iteration II indicating convergence has been reached. Technically, Unit **1** should be optimized again to compare iteration V with iteration III, to show Unit **1** also has reached convergence. But in a two-reactor system, this step is not necessary since iteration V is based on iteration IV, and iteration III is based on iteration II. It was shown that iteration II and IV are identical, hence, iteration III and V must also be identical. Thus only two complete cycles of iteration were necessary to find complete convergence in this multi reactor simulation.

The optimal nuclear energy distribution for Case 2 is given in Table **5.17. A** detailed tabulation of the weekly system costs before and after optimization is given in Table **5.18A. A** summary of changes in system cost with each iteration is given in Table **5.19.** The complete two-reactor optimization, Case **2.C,** results in a total savings of \$6.48 million compared with the situation **of** no nuclear optimization, Case **2.A. Of** this,.\$600,000 represents the improvement from the situation of optimal hourly generation,

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OPTIMAL WEEKLY **NUCLEAR** CAPACITI FACTOR DISTRIBUTION FOR THE TWO REACTOR OPTIMIZATION **(CASE** 2)

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TABLE 5.18A

*In Case **A,** Unit **1** is run at constant power **of 725** Mw. Unit 2 is run at predetermined power level shown in Table 5.18B.

In Case B, the weekly energy output of both units is the same as in Case **A,** but the hourly power level within each week is optimized. In Case **C,** power levels for each hour of each week are optimized within the constraints shown in Table 5.4. Total energy output from each reactor is the same in **all** cases.

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TABLE 5.18B

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 $\label{eq:2.1} \frac{1}{\sqrt{2\pi}}\sum_{i=1}^N\frac{1}{\sqrt{2\pi}}\sum_{i=1}^N\frac{1}{\sqrt{2\pi}}\sum_{i=1}^N\frac{1}{\sqrt{2\pi}}\sum_{i=1}^N\frac{1}{\sqrt{2\pi}}\sum_{i=1}^N\frac{1}{\sqrt{2\pi}}\sum_{i=1}^N\frac{1}{\sqrt{2\pi}}\sum_{i=1}^N\frac{1}{\sqrt{2\pi}}\sum_{i=1}^N\frac{1}{\sqrt{2\pi}}\sum_{i=1}^N\frac{1}{\sqrt{2\pi}}\sum_{i=1}^N\$

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TABLE 5.19

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SUMMARY OF TWO-REACTOR OPTIMIZATION **COST** SAVINGS **AS A FUNCTION** OF **NUMBER** OF ITERATIONS

Case 2.B, compared with the total optimization results, Case 2. C.

Table **5.19** indicates that most of the savings were realiz'ed after only one complete cycle of iterations in this two-reactor system. Other simulations have confirmed the hypothesis that the multi-reactor iteration process is a rapidly convergent one.

The major conclusions of this multi reactor simulation are that: **(1)** the short-range resource-limited optimization process lescribed in this thesis has been shown adaptable to a two-reactor situation, (2) convergence takes only a few complete cycles of iterations, **(3)** most of the cost savings is realized after one or two complete cycles of iterations, **(4)** substantial savings in fossil fuel cost are possible with short-range optimization, and **(5)** potential cost savings increase as the amount of nuclear capacity and energy that are optimized are increased.

5.5 Single Reactor O2timization Study-Case **³**

The purpose of Case **3** was to examine the effect of system reserves on **OCNP,** and on the optimal weekly nuclear capacity factor distribution. Case **3** is a modification of Case **1** where the fossil outage schedule (Table **5.1)** has been adjusted to obtain a (nearly) constant minimum monthly system reserve, see Table **5.5.** The original outage schedule (Table **5.1)** was altered **by** moving the outage of as few units as possible within the six-month planning horizon. Most of the alteration occurred in the maintenance outage schedule. The few changes made in the forced outage schedule were aimed at achieving a better balance in the monthly forced outage total compared with the monthly net generating capacity.

The 26-week **OCNP** values for Case **3** are listed in Table **5.20.** The weekly system reserves are listed in Table **5.21.** The average fossil generation costs of the monthly fossil configurations are listed in Table **5.22.** The optimal weekly nuclear capacity factor distribution is listed in Table **5.23.**

A comparison of the optimal nuclear capacity factor distribution for Case **1** and Case **3** (Tables **5.11** and **5.23)** shows a decrease **of** allocated energy for April and May, and an increase for July, August, and September. The June allotment is the same for both cases. The change in monthly allocation of nuclear energy is consistent with the change in the monthly minimum system reserve, both in direction and

WELY **OCNP** FUNCTIONS FROM **THE** SIGLE REACTOR OPTIMIZATION (Case **3)**

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TABLE **5.21**

WEEKLY SYSTEM RESERVE FOR **CASE 3**

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TABLE 5.22

MONTHLY **AVERAGE** FOSSIL GENERATION **COSTS** OF THE FOSSIL CONFIGURATION FOR **CASE 3**

 $\label{eq:2.1} \frac{1}{\sqrt{2\pi}}\int_{0}^{\infty}\frac{1}{\sqrt{2\pi}}\left(\frac{1}{\sqrt{2\pi}}\right)^{2\alpha}e^{-\frac{1}{2\alpha}}\left(\frac{1}{\sqrt{2\pi}}\right)^{\alpha}e^{-\frac{1}{2\alpha}}\left(\frac{1}{\sqrt{2\pi}}\right)^{\alpha}e^{-\frac{1}{2\alpha}}\left(\frac{1}{\sqrt{2\pi}}\right)^{\alpha}e^{-\frac{1}{2\alpha}}\left(\frac{1}{\sqrt{2\pi}}\right)^{\alpha}e^{-\frac{1}{2\alpha}}\left(\frac{1}{\sqrt{2\pi}}\right)^{\alpha}e$

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 $\mathbf{v} = \left\{ \begin{array}{ll} 0 & \text{if} & \text{if} \\ 0 & \text{if} & \text{if} \end{array} \right.$

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TABLE **5.23**

OPTIMAL WEEILY **NUCLEAR** CAPACITY FACTOR DISTRIBUTION FOR THE SINGLE REACTOR OPTIMIZATION (CASE 3)

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magnitude. April and May had large increases in reserves, hence significant decreases in naclear energy allotments. July and August had large decreases in system reserve, hence significant increases in nuclear energy allotments. June had the smallest monthly change in system reserves (210 MW), not enough to change its nuclear energy allocation. Sepember had a slight decrease in system reserves **(225** MW), hence a slight increase the nuclear energy allotment. The comparison of the solution of Case **1** with Case **3** shows conclusively the significant effect an unequal system reserve has on the optimal distribution of nuclear energy.

Table 5.24 shows the cost savings in Case **3** made possible **by** successively optimizing the hourly use of nuclear energy while holding weekly allocation fixed (Case 3.B) and then optimizing both hourly and weekly use of nuclear energy (Case **3.C).** Hourly optimization saves \$4.4 million and both hourly and weekly save \$4.7 million, about **70%** of Nuclear Unit l's fuel cycle cost at 2.0 mills/KWHe.

Comparison of Table 5.24 for Case **3** with Table 5.14 for Case **1** show that the total system fossil fuel costs for the changed maintenance and forcei-outage schedule of Case **3** was a little more than \$2 million lower than Case **1.** Comparing Cases B to Cases **C,** hourly optimization to weekly optimization, the savings are **\$160,000** for Case **3** and \$340,000 for Case **1.** It is to be expected that as the system reserves becomes equalized, .the optimal distribution **of** capacity factors becomes narrower and hence the

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TABLE 5.24

		SYSTEM FOSSIL FUEL COSTS AND SAVINGS FOR CASE 3		
Month	Week	Case 3.A	Case 3. B	Case 3.C
April	ı	10,629,018	10,452,025	10,309,019
	2	10,886,122	10,707,502	10,557,379
	3	10,204,452	10,039,148	9,993,321
	4	9,421,808	9,303,841	9,435,075
May	5	10,084,300	9,898,125	9,762,328
	6	9,624,926	9,454,683	9,411,099
	$\overline{\mathbf{z}}$	9,839,201	9,659,938	9,614,924
	8	10,151,039	9,964,469	9,915,509
	9	9,377,179	9,212,606	9,347,943
June	10	9,632,264	9,466,427	9,613,347
	11	9,963,262	9,781,430	9,734,177
	12	9,451,599	9,295,217	9,338,910
	13	9,081,760	8,945,116	9,079.552
July	14	8,848,790	8,715,163	9,837,240
	15	10,131,453	9,943,949	9,987,474
	16	9,811,395	9,632,603	9,766,925
	17	10,229,689	10,039,813	9,996,213
	18	10,055,654	9,870,064	10,009,600
August	19	11,455,317	9,641,892	9,773,228
	20	10,770,796	10,491,448	10,535,539
	21	10,803,244	10,075,964	10,216,792
	22	11,468,438	10,185,716	10,229,252
September	23	10,011,848	11,468,807	11,199,903
	24	10,884,673	10,795,505	10,640,491
	25	10,461,200	10,825,555	10,669,462
	26	10,572,132	11,481,658	11,212,542
Total System Costs (\$)		263,857,559	259,348,663	259,187,244
Comparison with Case 3.A			(4, 508, 896)	(4, 670, 315)
Case 3.A:				
Unit 1 is run at constant power (725 Mw), and Unit 2 is run at programmed power levels (Table 5.15) for all three cases.				

Case 3.B: The weekly energy output of Unit **1** is the same as in Case **3.A,** but the hourly power level within each week is optimized.

Case **3.C:** Unit l's power levels for each hour of each week are optimized for the entire six-month planning period.

Total energy output of Unit 1 is the same in all three cases.

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difference in savings between hourly optimization and weekly optimization diminishes. As mentioned earlier, the low capacity factor of the summer months is partially due to a seasonal influence on the shape of their customer demand function. Both spring and summer have about the same average weekly energy consumption. However summer has much higher demand peaks than the spring, hence summer also has lower demand minimums than spring. Since the lower part of the load-duration curve plays an active role in determining **OCNP,** it is no surprise that summer months should have lower average nuclear capacity factors (with all other parameters equal).

^Amajor determining system parameter for **OCNP** is the economic loading order. The economic loading order is made up of several system parameters such as fuel cost, maintenance schedule, heat-rate, etc. The slope of the **OCNP** curve is a reflection of the slope of the economic loading order from which **OCNP** is derived. **A** utility in the short-range has very few system parameters to manipulate. The customer demand is beyond real short term control. **A** large portion of fuel costs may be fixed **by** long-term contracts. Heat-rates are built into the physical equipment. The maintenance schedule is the only tool left which the system planner can use to manipulate system reserves and the economic loading order, and in turn **OCNP.** Because **of** changing economic conditions, fossil fuel costs show a great amount of variance from station to station.

Hence, the monthly economic loading order will show different patterns for different maintenance schedules. The main conclusion from the system simulations performed is that equal consideration must be given to fossil fuel arrangements as to system reserves when determining the monthly maintenance schedule.

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5.6 Applicability

The optimization procedure used in the previous system simulations (Cases **1,** 2, **3)** has been to optimally peak-shave the nuclear energy within the week, and then find the optimal distribution of nuclear energy among the weeks. This procedure is referred to as the "Peak-Shave First" method. Another optimization procedure would be to optimally distribute the nuclear energy among **all** the weeks in the planning horizon first, then optimally peak-shave each week's energy within the week. This approach is referred to as the "Peak-Shave Second" method. As an illustration, the single-reactor optimization problem, Case **3,** is repeated using the "Peak-Shave Second" method, which is referred to as Case 4.

In Case 4, the optimal weekly distribution of nuclear. capacity factors was found **by** using FOSSIL (instead of PROCOST) to calculate the weekly **OCNP** functions. FOSSIL modeled the nuclear units operating at fixed power level throughout the entire week. The **OCNP** values were then fed to **ALLOCAT** to calculate the optimal weekly nuclear capacity factor distribution. This case is labelled 4.D to signify the difference in optimization procedures as compared to the previous cases. Table **5.25** tabulates the resulting optimal distribution of capacity factors and energies for Case 4.D. Notice that there is some similarity between the optimal distribution for Case 4 and the optimal distribution for Case **3.** The peak-shaving of each week's nuclear energy was

OPTIMAL WEEKLY **NUCLEAR CAPACITY** FACTOR DISTRIBUTION FOR **CASE** 4

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performed **by** PROCOST, Case 4.E. Table **5.26** tabulates the weekly system cost and savings (compared to Case **3.A)** for Case 4. The system problem for Case **3** and 4 was exactly the same, only the optimization procedures applied were different. **A** comparison of the final results of Case **3.C** with 4.E shows that the "Peak-Shave First" method is a better procedure, **by \$60,000.** The cost comparison of Case 4.D with Case **3.A** shows a savings of \$200,000, about the same savings as the in Case **3** derived from optimally distributing the nuclear energy between the weeks. Comparing Case 4.E with Case 4.D shows that the savings from peak-shaving is \$4.4 million, about the same as in Case **3.** This comparison shows that the order of magnitude of the savings derived from optimally peak-shaving within the week, and optimally distributing the energy among all the weeks in the planning horizon is roughly independent of the order in which these steps are performed.

The results for Case 4 further document the conclusions of the previous cases that most of the potential savings (millions of dollars per reactor) of short-range nuclear system analysis lies in peak-shaving the operation of the nuclear reactors within a week. Lesser savings (approximately \$200,000) are derived from optimally distributing the limited amount of nuclear energy among the weeks. The main reason is that the energy consumption in different weeks throughout a year are more similar to each other than the energy consumption levels for the different

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TABLE **5.26**

SYSTEM FOSSIL **FUEL COSTS AND SAVINGS** FOR **CASE** 4

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(4,612,840)

(*) Case 4.D: The power level of Unit **1** (constant throughout each week) is optimally assigned for each week in the planning period.

(*) Case $4.E$: The weekly energy is the same as in Case $4.D$, but the hourly power level within each week is optimized (peak shaved).

The total energy output from Unit **1** is the same as in Case **3.**

hours of a week. The maximum difference in weekly energy consumption is about 20% whereas the maximum difference in hourly energy consumption is about **250%.**

Consideration of the two optimization procedures indicates that the "Peak-Shave First" method is the more logical optimization method. However since peak-shaving calculation are time consuming, the "Peak-Shave Second" method, which solves for the weekly distribution of energy prior to peak-shaving each week, saves computer time (with some loss in precision of the final result). This saving would be of particular importance in multi-reactor optimizations where several iterative calculational cycles are required for each reactor. The "Peak-Shaving Second" method is a more direct but approximate method of calculating the optimal dispatching schedule and hence is useful in narrowing the range in which the more accurate method may be applied, thus conserving calculational effort.

For convenience, the resource-limited case assumed a fixed refueling date in the framework of the problem. However, the date chosen is an independent variable. The study of a variable refueling date problem can be viewed as a study of a series of (related) fixed refueling date problems. There is a potential for computational savings since the utility system configuration is the same for the entire series of fixed refueling date problems. The results of many of the system calculations once performed, can be used repeatedly in each of separate fixed refueling date

problems.

The "stretch-out" case can also be viewed as another version of the resource-limited problem. During the coast-down period, the power level of the nuclear power reactor is already programmed; but for the time period before coast-down has started, the problem is a resource-limited problem.

^Asample of the weekly nuclear optimization recommended **by** PROCOST is given in Figure **5.2.** As shown, the nuclear unit should be operated essentially in an on-off mode. It is turned on at full rated power during high demand time periods, and turned off (to the minimum power level) during low demand time periods, thus the optimal peak-shaving of nuclear reactor is a simple daily cycling (high-low) of the power level. **A** complex detailed following of the customer demand pattern is not necessary. Nuclear reactors under construction are projected to be capable of some degree of load-following cycling such as recommended **by** PR3COST. In the event that an on-off mode is not physically feasible for the reactors, **PROCOST** should be modified so as to include a minimum, or must-run, power level for each nuclear reactor involved in the optimization. See Appendix **C.1** for details of suggested changes to accomplish this.

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NUCLEAR DISPATCHING **SCHEDULE**

6.0 Conclusions and Recommendations **6.1** Conclusions

(1) rhe system simulations performed showed the short-range optimization procedure developed to be flexible and reliable in handling a wide range of system conditions including an adaptability to multi-reactor problems as well as to single reactor optimizations.

(2) The system simulations showed that very large savings in fossil fuel costs, on the order of millions of dollars per reactor per optimization cycle, are possible from short-range nuclear system analysis. Thus use of these short-range system optimization technique **by** the utility industry would be a worthwhile undertaking.

(3) All short-range options can be viewed as expending a certain amount of nuclear energy in a certain time period. Thus a basis has been established for comparisons of other complex and involved short-range options.

(4) Procedural guidelines for optimal dispatching of nuclear generation (under resource-limited conditions) are to (a) peak shave the dispatching of nuclear energy **by** operating at peak power during peak demand time intervals and shutting down (or operating at minimum power) during low demand intervals, **(b)** follow a weekly budget of nuclear energy rationing until the next scheduled refueling date. The system simulations show that independent of the order of optimization most of short-range optimization savings (millions of dollars per reactor per optimization cycle)

comes from peak-shaving the nuclear energy within each week. Hence, peak-shaving should receive the primary attention. The savings from the weekly redistribution of energy were lower, on the order of hundreds of thousands of dollars per reactor per optimization cycle.

(5) The system parameters having greatest effect on total system operating costs are (a) system reserves, **(b)** seasonal customer demand shape, and (c) the economic loading order (in turn comprised of the system configuration and its basic parameters such as heat rates, and fuel costs). These are the system parameters that must be considered **by** the system planner in devising the allocation budget of nuclear energy over the short-range planning horizon.

(6) The sample system simulations have shown that the economic loading order is principally determined **by** the station's fuel cost (under today's economic conditions). Hence, the utility's determination of the maintenance schedule should aim at achieving a balanced fuel cost configuration in addition to a balanced system reserve configuration.

(7) Using the optimization techniques discused in this thesis, an unambiguous and logical method has been developed to calculate the short-range substitutional cost of nuclear power, the **OCNP.** This is the trading price that should be used when transferring nuclear power **by** utilities.

(8) The system simulation studies have shown the optimal solution to be sensitive to the accuracy of the

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input variables (i.e. fossil fuel costs and maintenance schedule). Hence, great care is necessary in determination of system parameters. Because of the introduction of new technology (i.e. nuclear power) in the utility industry coupled with a changing economic environment, many of the old "rules of thumb" and intution may no longer valid. The new operating environment requires a reassessment of old operating practices.

(9) The scope and complexity of the system interactions illustrated in the sample system simulation demonstrate the usefulness and need for the computer as a tool in system dispatching.

6.2 Recommendations

The sample system simulations studied in this thesis showed that potential operating savings derived from short-range nuclear system analysis to be in the millions of dollars. Relatively simple models were used in the computer programs to pattern the operations of a modern utility system. The models identified the system parameters of greatest sensitivity on system cost and provided an upper limit on the potential savings that may be achievable through short-range nuclear system analysis. How much of this potential savings that can **be** realized depends on the operating constraints not included in the programs and validity of the assumptions used. The following is a list of recommendations to improve and define the accuracy of the

computer programs and calculational technique used.

(1) The range of applicability of the deterministic approach used in PROCOST should be assessed. This may be accomplished using risk-decision analysis, Ref. **(33),** to measure the severity for assuming **100%** availability of the nuclear reactors, see Sections **3.2.1** and **5.1.** The usefulness of the Booth-Balerieux probabilistic utility model in determining OCNP should be investigated in overcoming the difficulty mentioned above. Probability theory is most accurate in dealing with a large sample or large time periods. Thus, the applicability of the probabilistic model for a one-week time period should be considered.

(2) Future load models should include the modeling of holidays in the week to study the optimal generation schedule for these periods, see Sections **3.2.2** and **A.1.**

(3) Minimum operating load levels should be included in the nuclear unit representation in PROCOST. The procedure for implementing this feature is discussed in Appendix **C.1.**

(4) Start-up and shut-down costs should be included in future simulations studies. This may reguire use of (a) Integer Programming or **(b)** multi load-duration curves in PROCOST, see Appendix **C.1.**

(5) PROCOST, in its present form is a general program offering a number of options. Specialized users of PROCOST should modify the program to fit their own individual requirements and achieve improved computational efficiency

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and lower execution time and storage reguirements. The performance of the pumped storage subroutine, **ECO,** especially can be improved upon. Separate chronologic and load-duration versions of PROCOST should also improve computational efficiency. Details on these changes are given in Appendix **C.1.**

(6) From the sample system simulation studied in Section **5.6,** it was found that the "Peak-Shave Second" method yielded within 2 **%,** the same system cost savings as the "Peak-Shave First" method. Since the "Peak-Shave Second" method is more calculationally efficient, it is recommended that further tests should be made comparing the two solution techniques under several different system environments. If the two methods continue to show nearly the same system cost savings, then the simpler and quicker "Peak-Shave Second" method can be used in place of the "Peak-Shave First" method.

Appendix **A: LOAD MODELS**

A.1 Introduction

The weeky customer demand function is a necessary system input parameter for PROZOST, the production cost program. This demand function may be a set of actual demand numbers or it may be derived from a set of coefficients describing a seasonal demand function as dependent on one or two (or more) independent variables. For the case of performing sensitivity analysis, changing a single independent variable is more convenient than changing,168 numbers individually. The basic hypothesis for such a load model was that the customer demand for each hour of the week was linearly dependent on the weekly average power level. **A** least squares fit correlation was made for each hour of the week to the weekly average power level for each season. General utility practice has been to use the weekly peak power level as the independent variable. **A** comparison of the two methods (using **1971** Commonwealth Edison's customer demand) revealed that during the summer and a part of the fall seasons, the weekly peak is a better independent variable (in terms of a higher.correlation coefficient) than the weekly average power level. However, the latter was used as the independent variable in the simulations discussed in this thesis, because **of** its overall higher correlation coefficient during the entire one year sample. Statistically, the peak fluctuates more than the mean, thus, the mean (weekly average power level) provides the higher

correlation coefficient. The form of the regression is: customer demand **=** coeff(1)+coeff(2)*independent variable, where coeff is a two element array containing the regression coefficients.

A 168-interval load model was found to be computationally burdensome. Several studies were performed to find simplified load models that would yield the same system results as the 168-interval load model. Appendix **A.5** reports on a chronologic load model study that found a forty-interval model that duplicated most system results very well. Appendix **A.6** reports on a load-duration study that found a six-interval model that duplicated OCNP values very well. The forty-interval model is a modified chronologic load model. The three average weekdays (excluding the peak weekday and the low weekday) were found to be very similar to each other. Table **A.1** shows the distribution of daily energy consumption in a work week. Thus, the three average workdays were combined to form one day in the load model. The forty-interval model consisted of a 10-interval peak weekday, a 10-interval average weekday, a 10-interval low weekday, and a 10-interval weekend. Zombining weekdays together rather than combining consecutive hours together retains a greater amount of accuracy in the load model. This can be illustrated **by** Figure **A.1.** Choosing the customer demand at **3** o'clock on Monday, Tuesday and Friday (three average weekdays, excluding the high and the low), the range in values is **398**

TABLE **A.1**

REIATIVE DAILY (WEEKDAY) ENERGY **CONSUMPTION***

Note: Each number shown is the ratio of the day's energy consumption divided **by 1/7** of the week's energy consumption.

The data are from the winter season of AEP's **1971** Customer Demand.

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MWH, whereas the smallest range in values on the same weekdays for 2,3,4 o'clock is **688** MWH.

The logical extension of combining weekdays together is toward load-duration curves. **A** six-interval load-duration model with constant nuclear heat-rate was found to yield accurate **OCNP** values. six-intervals were chosen to be approximately equidistant from each other. curve was divided into six equal intervals. Within each interval, the average demand level was calculated, yielding six demand levels. The demand levels **of** the The range in demand in the load-duration

Use of several computer programs aided formulating the different load models.

(1) PROFILE, listed in Appendix **A.2** is a program that plots the contour of the average weekly demand function for a season.

(2) REGRESS, listed in Appendix **A.3** is a program that calculates the weekly regression coefficients for particular combination of time intervals.

(3) MODEL, listed in Appendix A.4 is a program that calculates the individual demand function values from the forecasted weekly energy consumption and the regression coefficients.

PROFILE is a visual aid to help the system planner in deciding which of the hours of the week to combine to form the simplified load model. When a particular combination has been chosen REGRESS will calculate the regression

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coefficients. MODEL will use the regression coefficients to calculate the projected demand function.

The interesting feature about REGRESS is that it performs a sorting of the weekday **by** energy consumption. For example, the disadvantage of grouping all Mondays (or any weekday) together (to form a correlation of Monday's hours with the weekly average power) is that some Mondays are the week's lowest demand day and other times, Monday is the highest damand day. The same is true for all the weekdays. **A** comparison of the ratio of the daily energy comsumption to the weekly average for an entire season is tabulated in Table **A.1.** Interestingly, it shows that the weekly low weekday deviates more from the weekly norm than the weekly high weekday. There is a random distribution of which days are the high and low weekdays. But it shows that the other three weekdays usually show very similar energy consumption. Thus, higher correlation coefficients are obtained for developing correlation parameters for high weekdays, low days, average weekdays, and weekends rather than Mondays, Tuesdays, Wednesdays, etc. The former load model would be more representative than a week composed of **5** average weekdays.

MODEL is a computer program that calculates customer demand functions for energy consumption levels beyond the validity of the correlation the parameters were based on. Using only **1971** customer demand numbers, four seasonal sets of demand parameters were developed, However, to simulate a

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1977 system demand function (for the system simulations) , required a a **50%** jump'in power level which was as beyond the validity of the correlation. Thus, the independent variable was normalized **by** the average **1977** seasonal power level.

It is recommended that more accurate load models be used in the future which would include **(1)** provisions for holiday, and (2) stochastic demand levels.

A.2 PROFILE

A.2.1 Input Specifications

The File Structure:

COPY: file on which **DEMAND** resides

Input Variable Name:

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DEMAND(168): the array which contains the chronologic weekly customer demand numbers. Thirteen weeks of data are required for each season.

Note: PROFILE uses the Fortran subroutine, PRTPLT (34) , to do the printing of the average demand function. It is important that the **JCL** is in the correct order to establish the proper linkage.

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APPENDIX A.2.3 SAMPLE OUTPUT FROM PROFILE

A.3 REGRESS

A.3.1 Input Specifications

The File Structure:

COPY: file on which **DEMAND** resides (as in PROFILE, Appendix **A.2.1)**

SYSIN: file on which the load model parameters are inputted.

Input Variable Names **by** order of input on file SYSIN:

- I: number of weekly **DEMAND** values to skip before processing.
- X: number of time intervals used in representing a weekday in the load model.
- Y: number of time intervals used in representing a weekend in the load model.

P: number of weeks to a season.

- **LEN(X):** array containing the number of hours represented **by** each time interval in the weekday portion of the load model. If X=24, then omit **LEN.**
- **END(Y):** array containing the number of hours represented **by** each time interval in the weekend portion of the load model. If Y=48, then omit **END.**

Note: REGRESS calls the Fortran subroutine, LSFIT(25) to do the least squares fit analysis. It is important that the **JCL** is in the correct order to establish proper linkage.
```
//TEST EXEC PLIXCGO,LIBRARY='U.C7920.10712.PLIX21.PLIBASE'
//C.SYSIN DD *,DCB=BLKSIZE=2000
 REGRESS: PROC OPTIONS(MAIN);
 DCL (X,Y,I,P,QS) FIXED BIN;
 GET LIST(I);
 READ FILE(COPY) IGNORE(I );
 CN ENDFILE(SYSIN) GO TO BOTTCM;
 ON ENDFILE(COPY) CLOSE FILE(COPY);
 TOP:GET LIST (X,
YP);
 PUT DATA (X,Y,P)
 S=3*X+Y:
Q=S+i;
 BEGIN;
 DCL WEEK( P,
Q) FLOAT DEC;
 DCL ( END(Y)
LEN( X),HIGH( 2) ,LOW( 2))
FIXED BIN,
   STRING BIT(
5) VARYING, DEMAND(168)
FIXED DEC,
 (B, KI,E,F
G,J) FIXED BIN,
 A(5) FIXED B
IN(31);
WEEK=9;
 ON ERROR PUT CATA(E,K,KK,
I,WEEK(KKI),DEMAND(E+K));
 IF X=24 THEN LEN=1;ELSE
GET LIST(LEN);
 IF Y=48 THEN END=1;ELSE
GET LIST(END);
 DO 1=2 TO X;LEN(I)=LEN(I)+LEN(I-1);
 END;
 DO 1=2 TO Y;
 END(I)=END(I)+END(I-I);END;
 PUT DATA(LEN, END);
 PUT PAGE LIST(' HIGH, LO
W, E,
F, G, AND THEIR RELATIVE SIZES');
 DO KK=l TO P;READ FILE(COPY) INTJ (OEM
AND);
 A=0;
 DO J=1 TO 5;
```
REGROO01> **REGRU002'0** REGROOO3 : REGROO04 REGR0005 **,** REGROOO6| REGR0007F REGR0008 倍 REGROOO9. **,** REGROO10i-REGROOll $REGROO12$ REGR0013版 REGROO14₁p REGROO15E REGROO16 REGROO17 REGROO18 REGROO19F REGR0020 REGR0021 **gH** REGR0022¹ REGR0023] 5 REGR0024REGRU025REGR0026REGR0027REGR0028REGR0029REGR0030REGR0031REGR0032REGROO33REGROU34REGR0035REGR0036

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APPENDIXA. ÷, 3.3 SAMPLE OUTFUT FROM RECEIPSE $\omega_{\rm{eff}}$

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118 -1727.1 1.15612 ϵ $\frac{1}{\sqrt{2}}$ 1.15768 \cdot $\Delta\phi = \Delta\phi/\Delta\phi$ $119 - 1417.3 - 1.27354$ ϵ $120 - 2075.2$ 1.12652 $\bar{\mathcal{A}}$ $\pmb{\sigma}$ ϵ \sim e ø \mathcal{C} ϵ^2 \sim \mathcal{S} \bullet^+ \mathbf{I} $\boldsymbol{\mathcal{I}}$ \sim $\frac{2}{3}$ $\tilde{\omega}$ \mathcal{C} \bar{z} \mathbf{I} $\mathcal{L}_{\mathcal{A}}$ \mathbf{r}^{\star} $\bar{\mathbf{z}}$ م ω $\ddot{}$ v $\overline{}$ \ddotsc ◢ \bullet ر \sim ø $\overline{}$ \bullet ں \bullet \bullet

- **A.** 4 MODEL
	- A.4.1 Input Reguirements

The File Structure:

- LDMDL: File where the customer demand function is to be printed.
- **COEF:** File name of dataset where the seasonal regression coefficients **A** and B reside.
- SYSIN: File where the load model input parameters are located.

Variable Names by Order of Input in File SYSIN:

- **I:** The number of seasons sets of **A** and B to be skipped on file **COEF** before beginning processing.
- **SEASON:** The number of sets of seasonal parameters **(A** and B) to **be** processed in calculating all the demand function desired.
- **PTS:** The number of time intervals used in the load model to represent a weekly customer demand function.
- TIME: Array containing the number of hours represented **by** each time interval in the load model.
- WEEKS: The number of weeks a set of seasonal parameters is used.
- MEAN_POWER: The mean power level of the season for which a seasonal set of regression parameters is valid.
- **MEANENERGY:** The average weekly energy consumption value for the season being simulated.
- ENERGY: The weekly energy consumption of the week for which the demand function is desired.

The last four variables are repeated for each season output desired.

Example Problem Number One:

The weekly demand function for two summer weeks and one winter week are desired. The summer weekly energy consumption values are **1,000,001** and **1,000,002** and the winter weekly energy consumption value is **1,000,100.** The seasonal average summer energy is **1,000,500** and the seasonal average winter energy is **1,000,050.** The seasonal power level for which the regression coefficents are valid are **6,000** and **5,000** for winter and summer, respectively.

The seasonal regression coefficients lie in the order of spring, summer, fall, and winter on file **COEF.** The load model is represented **by** four time intervals. The time duration of each interval is 41, 42, 43, 42 hours respectively.

The resulting input SYSIN file would read as follows: **1 3** 120

- 41 42 43 42
- 2 **5000 1,000,500 1,000,001** 1,000,002
- **0 0 0**

1 6000 1,000,050 1,000,100

Example Problem Number Two:

The input required for the weekly demand functions used in the system simulations (in Section **5.0)** is listed below the program listing, in Appendix A.4.2. Appendix A.4.3 is the resulting computer output.

// 'PAY ENG',CLASS=A,REGICN=128K / **EXEC** PLIXCGO, //CoSYSIN **DD** *,DCB=BLKSIZE=2000 MODFL: PROC OPTIONS(MAIN); DCL **(I,SEASONS, PTS, WEEKS, K) FIXED BIN; GET LIST(I,SEASONSPTS);** PUT **DATA(I,SEASONS,PTS**)SKIP; REAO FILE(COFF) **IGNURE(PTS*I);** BLOCK: **BEGIN; DCL** (A(PTS),8(PTS), C(PTS),COEFF(2)) FLOAT **DECTIME(PTS)** FIXED **BIN,** (POWER, ENERGY, MEAN_POWER, MEAN_ENERGY, TOTAL) FLOAT DEC(16): **GFT** LIST(TIME)COPY; LOOP: **DO** K=1 TO **SEASONS; DIU** I=1 TO **PTS;** READ FILE(COEF) **INTO(COEFF); A(I)=COPFF(i); 13(I)=COEFF(2); E** ND:**A(99)=A(100);** $B(99) = B(100);$ **GET** LIST(WEEKS, MEANPOWER, **MEANENERGY);** PUT CATA(WEEKS, MEAN_POWER, MEAN_ENERGY)SKIP Df **1=1** TO WEEKS;**GFT** LIST(ENERGY); PUT CATA(ENERGY)SKIP(2); POWER=MEAN_POWER*ENERGY/MEAN_ENERGY; $C = A + B * P$ CWER: **TKTAL=SUM(C*TIME); C=CV*ENEQGY/TJTAL ;** PUT FILE(LDMDL) EDIT(C)(168 F(8)); PUT EDIT(C)(8 F(10), SKIP) SKIP; **FMD:** END LOCP;**END** BLOCK;

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A.5 Chronologic Load Model Sensitivity Study

The survey nature of the production cost program reguired a reduction of variables to improve its cost performance. **A** sensitivity study of load models was undertaken to find a configuration that would retain system accuracy for a minimum number of time intervals simulated. The criterion used for judging system accuracy was incremental capacity factors. Initially, simple averaging techniques were considered. The 168-hour-per-week representation (Figure **A.2)** were reduced to 84 2-hour intervals (Figure **A.3)** and **56** 3-hour intervals (Figure A.4). Such arbitrary methods proved lacking in sufficient detail. The use **of** non-uniform time intervals proved more satisfactory. Starting with the 168-hour representation (Figure **A.1)** the investigation's depth reached the extreme of a four-interval-per-week load model (Figure **A.5)** which represented the high and the low of the weekdays, and the high and the low of the weekend. For these two models, a comparison of the system cost of the four-interval load model was calculated very close to the reference 168-interval model, see Table **A.2.** This effect was due to a cancellation of errors. The closeness in system costs between the '4' and **'168'** is due to the very coarse time intervals used in the '4' load model. Averaging time intervals generally lowers system production cost due to the fact that peakers operate at higher cost then the base load increments, thus averaging substitutes lower cost energy for

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FIGURE **A.3** 84 INTERVAL REPRESENTATION OF THE **CUSTOMER** DEMAND FOR THE WEEK OF **JAN.** 4, **1971**

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Figure **A.4**

56-Interval Representation of the Customer Demand

for the Week of Jan. 4, 1971

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Optimal System Cost Comparison of **6** Load Models (on Winter Load Data and Cost Plan 1)

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high cost energy. Table **A.2** shows the trend in lower production cost with the decrease in the number of time intervals being simulated. However, the coarseness of the **'14'** model causes large amounts of nuclear energy to be used at inefficient (low) power levels, forcing the greater use of fossil fuel, thus offsetting the averaging effect. **Of** course, the capacity factors criterion for the four-interval model was not satisfied as shown in Figure **A.6 -**

As with the simple averaging technique, the next set of models preserved the seven-day representation explicitly. There was a 42-interval load model,(Figure **A.7)** consisting of **7** days/week and **6** intervals/day. Also an 84-interval load model (Figure **A.8)** consisting of **7** days/week and 12 intervals/day. Figures **A.6** and **A.9** shows how these models compare with the reference case. As expected the 84-interval load model did best in reproducing the incremental capacity factors. The next modeling simplification step was to combine the average weekdays together because of their strong similarity. **A** 19-interval load moiel (Figure **A.10)** representing one peak day of **6** intervals, and average day (composite of the four other week days) of **6** intervals and a weekend of **7** intervals was compared with the previous results. Figure **A.11** shows that the 19-interval load model very closely reproduced the results **of** the 42-interval load model. Both models represented **6** time intervals per day. Thus the similarity in weekdays could be used effectively to reduce the number

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FIGURE **A.9** COMPARISON OF INCREMENTAL FOSSIL CAPACITY FACTORS **ON** WINTER **LOAD DATA AND COST PLAN 1**

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FIGURE A.11 COMPARISON OF INCREMENTAL FOSSIL CAPACITY FACTORS ON WINTER LOAD DATA AND COST PLAN 1

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of time intervals that had to be simulated. Table **A.2** compares the weekly system production costs of the various load models using the same input parameters.

Accordingly, a 40-interval load model (Figure **A.12)** was formed, representing a peak weekday **(10** intervals), a low weekday **(10** intervals), an average weekday (composite of the three other weekdays, **10** intervals) and a weekend **(10** intervals). The comparison of incremental capacity factors is shown in Figure **A.13** . To demonstrate that the good comparison was not coincidental, a comparison of the 40-interval load model with the 168-interval load model was made for summer load model data, instead of winter, see Figure A.14. The comparison of incremental capacity factors with the reference (168-hours) case was again favorable, shown in Figure **A.15** . The small aberrations at the high increments seem to be due to the pumped storage model.

As a further test, fossil fuel costs were changed from "Cost Plan **1"** to "Cost Plan 2", Table **A.3,** so that the loading order of the fossil units was different. Figure **A.16** shows that the incremental capacity factor distributions for the 40-interval load model and the 168-interval load model were very similar for "Cost Plan 2",also (see Figure **A.13** for Cost Plan **1).** The results justify using the 40-interval load model for future simulation studies in place of a 168-interval representation. Table A.4 compares the weekly system production cost of the 40-interval load model and the reference load model for the various tests referred to

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FIGURE **A.13** COMPARISON OF INCREMENTAL **FOSSIL** CAPACITY FACTOR *ON WINTER* **LOAD DATA AND COST PLAN 1**

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TABLE **A. 3**

FOSSIL PIANT **DATA USED IN** SENSITIVITY **STUDY**

1. Standardized Average Heat Data:

3. Information on each class of plants:

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Table **1.** 4

"Optimal System Cost Comparison of 40 Int/wk Load Model with **168** Int/wk Load Model (Units: $$10^3/\text{wk}$$)"

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above. The agreement is favorable. Table **A.3** also lists the plant parameters used in this study.

A.6 Load-Duration Sensitivity Study

The explicit simulation of **168** hours of the week is a costly calculation. It has been shown in the chronologic load model sensitivity study that little accuracy is lost in the prudent combination of time intervals to reduce the explicit number of intervals simulated. Depending on the particular feature of system the simulation model is trying to reproduce, the minimum number of time intervals will vary accordingly. In the previous section, the system feature to be reproduced was the incremental capacity factors, which allowed only a moderate reductions in the number of time intervals. In the reproduction of the **OCNP,** much less detail of the system need **by** reproduced. The chronologic pattern of the load model is not essential. The detailed simulation of high peaking demand intervals and low demand intervals is not so important. To find the correct value of **OCNP,** the model must locate the correct alternative cost to nuclear energy only at the time the nuclear energy is being exhausted. The difficulty **of** finding the correct alternative cost depends on the fine structure of the incremental fossil loading order. Table **A.5** shows a typical fossil incremental loading order derived from a large **15,000** MWe capacity utility system. In the area of interest, the middle section of the loading order, the interval width vary from **100** MWe to **300** MWe. Some contiguous intervals have the same energy cost or only slight differences. Thus, it seems a great amount of latitude is available in reproducing the

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TYPICAL ECONOMIC LOADING ORDER

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correct **OCNP,** as is shown **by** the experimental results.

Two system environments were used in the sensitivity study of load-duration models. An April load model with a non-nuclear system capacity of 12,000 MWe and an August load model with a non-nuclear system capacity of **13,000** MWe. The system parameters for the April and August system environments were the same as those used in the single reactor optimization study (Case **1)** except for the modelin.g of the large fossil units. The large fossil units had a minimum operating level of **60%** instead of 40% as used in the optimization studies.

Studying the situation of varying the capacity factor of a single reactor **(1100** MWe, constant heat-rate), the April simulations were tested for load-duration models of **25,** 12, 8, **6, 5,** 4, **3,** 2 time intervals. The list of resulting **OCNP,** system's cost, and incremental capacity factors are tabulated in Tables **A.6, A.7,** and **A.8,** respectively. As the number of time intervals decreases the **OZNP** values hardly change until the very end. The system cost numbers show only slight deterioration and even then, the changes are proportional for the various nuclear capacity factors (implying incremental system costs are the same for the various models, reinforcing the **OCNP** results).The incremental capacity factors, though, show marked deterioration with the reduction in the number of time intervals.

A similar single reactor case was repeated with the

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TABLE **A.6**

OCNP COMPARISON FOR THE LOAD-DURATION SENSITIVITY **STUDY (oNE** REACTOR, APRIL **LOAD DATA CASE)**

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WEEKLY SYSTEM COST COMPARISON FOR LOAD-DURATION STUDY (ONE REACTOR, APRIL LOAD DATA CASE)

TABLE $A:8$ **INCREMENTAL** CAPACITY FACTOR COMPARISON FOR THE **LOAD** DURATION SENSITIVITY STUDY (Single Reactor, April Load Data Case)

The following tables are a comparison of the capacity factors of the **52** fossil increments in the April economic loading from eight load-duration models. The tables are arranged as follows:

The increments are labeled horizontally and the number of intervals in the load-duration models are labeled vertically. There is a separate table for each of eight values of the weekly nuclear capacity factor, ordered **by** descending **values.**

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TABLE A.84
FOSSIL INCREMENTAL CAPACITY FACTOR CCMPARISON FOR 0.90 WEEKLY NUCLEAR CAPACITY FACTOR

TABLE A.8B

FOSSIL INCREMENTAL CAPACITY FACTOR COMPARISON FCR 0.80 WEEKLY NUCLEAR CAPACITY FACTOR

TABLE **A.8C FOSSIL** INCREMENTAL CAPACITY FACTOR COMPARISON FCR **0.70** WEEKLY **NUCLEAR** CAPACITY FACTOR $\mathcal{L}^{\text{max}}_{\text{max}}$.

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TABLE **A.8D**

FCSSIL INCREMENTAL CAPACITY FACTOR CCMPARISON FCR **0.60** WEEKLY **NUCLEAR** CAPACITY FACTOR

TABLE **A.8E**

FOSSIL INCREMENTAL CAPACIlY FACTCR **CCMPARISON** FCR **NUCLEAR CAPACIlY** FACTOR **0.50** WEEKLY $\sim 10^6$

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TABLE A.8F FOSSIL INCREMENTAL CAPACITN FACTOR **CCMPARISON** FCR 0.40 WEEKLY **NUCLEAR** CAPACITY FACTOR ~ 10

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TABLE **A.8G** FOSSIL **INCREMENTAL** CAPACITY FACTOR **CCMPARISCN** FOR **0.30** WEEKLY **NUCLEAR** CAPACITY FACTOR $\sim 10^7$

TABLE **A.8h** FCSSIL **INCREMENTAL** CAPACITY FACTOR **CCMPARISON** FOR 0.20 WEEKLY **NUCLEAR CAPACITN** FACTOR

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August system environment. Tables **A.9, A.10,** and **A.11** show the resulting comparison of **OCNP,** system costs, and incremental capacity factors for six load-duration models, (20, 12, **10, 8, 6,** and 4 time intervals per week). The August simulations verify the results of the April simulations.

Two-reactor simulations were also tested in the April and August environments. The April system tested two reactors (constant heat-rate) **of 1100** MWe and 220 MWe rated capacity for 12 load-duration models. The resulting **OCNP** and system costs are tabulated in Tables **A.12** and **A.13,** respectively. The **OCNP** results (Table **A.12)** continued to be reproduced faithfully, even at a very small number of time intervals.

In the August environment, two reactors of **1100** MWe each were simulated for **6** load models, but for a wider range of capacity factors. The resulting comparison of **0CNP** and system costs are shown in Tables A.14 and **A.15,** respectively. The results of these comparisons confirm the hypothesis that *OCNP* (and changes in system costs) are reproducible **by** load-duration models of only **6** time intervals. See Section **5.2** for more details on the load-duration study.

TABLE **A.9**

THE OCNP COMPARISON FOR THE LOAD-DURATION SENSITIVITY **STUDY (oNE** REACTOR, **AUGUST LOAD DATA CASE)**

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TABLE **A.1O**

THE WEEKLY PRODUCTION **COST** COMPARISON FOR THE LOAD-DURATION SENSITIVITY **STUDY (ONE** REACToR, **AUGUST LOAD DATA CASE)**

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TABLE **A.l1** INCREMENTAL CAPACITY FACTOR COMPARISON FOR THE **LOAD** DURATION SENSITIVITY **STUDY** (Single Reactor, August Load Data Case)

The following tables are a comparison of the 'capacity factors of the **60** fossil increments in the August economic loading from six load-duration models. The tables are arranged as follows: The increments are labeled horizontally, and the number of intervals in the load-duration models are labeled vertically. There is a separate table for each of eight values of the weekly nuclear capacity factor, ordered **by** descending values.

FOSSIL **INCREMENTAL** CAPACITY FACTOR CCMPARISON FOR **0.90** WEEKLY **NUCLEAR** CAPACIY FACTOR TABLE **A.11A**

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FOSSIL INCREMENTAL CAPACITY FACTOR **CCMPARISON** FOR **0.70** WEEKLY **NUCLEAR** CAPACITY FACTOR TABLE **A.LIC**

INCRE: T **20: 1.00 1.00 0.98** C.97 0.96 **0.96 0.96 0.93 0.93 0.93 E** *12:* **1.00 1.00 0.98 0.96** 0.96 **0.96** 0.96 **0.93 0.93 0.93** R **10: 1.00 1.00 0.98 C.96 0.96 0.96 0.96 0.96 0.93 V 8: 1.00** 1.00 **1.00 0.95 0.95 0.95** 0.95 *0.95* 0.95 **0.95 A 6: 1.00 1.00 1.00** 0.96 **0.93** 0.93 **0.S3 0.93 0.93 0.93** L 4: **1.00 1.00 1.00 1.00 1.00** 1.00 1.00 **1.00 1.00 1.00** INCRE: T *20:* **0.93 0.93 0.91** C.88 **C. 82** 0.82 **C.78 0.59 0.59 0.59 E** *12:* **0.93 0.93 0.93 0.86 C.82 0.82 0.80 0.62 0.62 0.61** R **10: 0.91 0.91 0.91 0.91 0.88 0.77 0.77 0.71 0.56 0.56 V 8: 0 .95 C.95 0.93 0.82 C.82** 0.82 **0.E2 0.71 0.56 0.56 A 6: 0.93 0.93 0.93 0.93 0.93 0.93 0.68 0.56 C. 56 0.56** L 4: **0.88 0.82** *0.82* **0.E2 0.82** 0.82 **0.82 0.71 0.56 0.56 INCRE:** T *20:* **0.59 0.57 0.56 C. 53** 0.52 **0.52 C .52 0.52** *0.52* **0.52 E** *12: 0.56* **0.56 0.56 0.56 0.56** 0.49 0.49 **0.49** 0.49 0.49 R **10: 0.56 0.56 0.56 0.56 0.56 0.55** C.46 0.46 0.46 0.46 **V 8: 0.56 0.56 0.56 C. 56 0.56 C .56 C .4c** *0.45* 0.45 0.45 **A 6: 0.56 0.56 0.56 0.56 0.56 0.56 C.56** 0.47 0.45 0.45 L 4: **0.56 0.56 0.56 0.56 0.56 C.56 0.56 0.56 0.56).56** I **NCRE:** T *20:* 0.46 0.46 0.46 C. 44 C.42 0.42 0.41 **0.37 0.32 0.30 E** *12:* 0.48 0.45 0.45 0.45 0.41 0.41 0.41 **0.38** *0.32* **0.32** R **10:** C.46 **C.46** 0.46 C.44 0.42 0.42 0.42 **0.39 0.28 0.27 V 8:** 0.45 0.45 0.45 0.45 C.41 0.41 **C.4 1 0.38 0.29 0.29 A 6:** 0.45 0.45 0.45 0.45 0.45 0.45 0.45 **0.35 0.32 0.32** L 4: *0.55* 0.41 0.41 0.41 0.41 0.41 0.41 0.41 0.41 0.41 INCRE: T 20: **0.27 0.27 0.27 0.27** *0.26* 0.04 0.04 0.04 0.03 **0.00 E** *12:* **.0.30 0.23 0.23 0.23 0.23 0.23 0.11 0.00 0.00 0.00** R **10: 0.27 0.27 0.27 0.27 0.27 0.21 0.00 0.00** 0.00 **0.00 V 8:** 0 **.29 0.29 0.29 0.29 C.29** 0.14 **C.0C 0. oc C. C 0.00 A 6: 0.32 0.32 0.32 0.32** 0.24 **0.00 0.00 0.00** 0.00 **0.00** L 4: **C** .41 0.34 **0.0c C.0c 0CC 0.00 C .00 0.00 0. C 0.1)0** INCRE: T **20: 0.00 0.00 0.00 0.00** 0.00 **C.03 C .00 0.00** 0.00 0.0C **E** *12:* **0.00 0.00 0.00 0.00 0.00 0.00 0.00** 0.00 **0.00** R **10: 0.00 0.00 C.00 c.00 0.00 0.00 C.00 0.00 c .00 c .** 00 **V 8: 0.00 0.00 0.00** *C.'n0* **0.00 0.00 C.00** 0.00 **0.C0c 0. C0 A 6: o.00 0.00 0.00 0.0C 0.00 0.00 0.00 0.00 0.00** 0.00 L 4: **0.00 C.00** 0.00 **0.0C 0.00 0.00 C .00 0.00 0.00 ,.-I1 11** *21* **31** 41 **51** *2* 12 *22* **32** 42 **52 3 13 23 33** 43 **53** 4 14 24 34 44 54 *5* **15 25 35** 45 **55 6 16 26 36** 46 **56 7 17 27 37** 47 **57 8 18 28 38** 9 **19** 29 **39 10** 20 **30** 40 48 49 **50 58 59 60**

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FOSSIL INCFEMENTAL CAPACITY FACTOR **CCMPARISON** FOR **0.50** WEEKLY **NUCLEAR** CAPACITY FACTOR **TABLE A.11E**

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TABLE **A.l?**

OCNP COMPARISON FOR THE LOAD-DURATION SENSITIVITY **STUDY** (TWO-REACTOR, APRIL *LDAD* **DATA CASE)**

Weekly Nuclear Capacity Factor **of** Two Reactors **OCNP** (mills/lo,Ooo Btut) Number of Time Intervals in Load-Duration Model **155.13/3.59 4.79/3.35 4.76/3.33 10 5.13/3.594.79/3.35 4.76/3.33 95.59/3.89 4.79/3.35 4.76/3.33 0.70/0.800.80/0.80 8***5.13/3.59* **4.79/3.35 75.13/3.59 4.79/3.35 65.13/3.594.79/3.35 55.56/3.59 4.79/3.35** 4**5/13/3.59 4.79/3.35 35.56/3.59 4.79/3.35 4.76/3.33 4.76/3.33 4.76/3.33 0.70/0.800.80/0.80 0.90/0.80** *50***5.13/3.594.79/3.35 4.76/3.33 30** *5.13/3.59***4.79/3.35 4.76/3.33** 20**5.13/3.594.79/3.35 4.76/3.33** o.90/o.80 **4.76/3.33 4.76/3.35 4.76/3.33**

TABLE **A.13**

SYSTEM **COST** COMPARISON FOR THE LOAD-DURATION SENSITIVITY **STUDY** (IWo REACTOR, APRIL **LOAD DATA CASE)**

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TABLE A.14

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OCNP COMPARISON FOR THE LOAD-DUIATION SENSITIVITY STUDY (TWO-REACTOR, **AUGUST LOAD DATA CASE)**

TABLE **A.15**

SYSTEM **COST** COMPARISON FOR THE LOAD-DURATION SENSITIVITY **STUDY** (TWO-REACTOR, **AUGUST LOAD DATA CASE)**

Appendix B: SYSTEM PARAMETERS

B.1 Nuclear Heat-Rates

The nuclear heat-rate data used throughout this study are obtained from Figure B.1, a result of an analytic fit made **by** Prof. **M.** Benedict from points supplied **by** Commonwealth Edison. Individual data points are not shown to preserve the confidentiality of the material. **Of** particular interest, Figure B.1 shows that operating a nuclear reactor below **70%** rated capacity results in high inefficiencies. Thus, a program to maximize nuclear uttilization would avoid operation below **70%** as much as possible, even to the extent of shutting down.

B.2 Fossil Heat Rates

Fossil heat-rates used in this report are obtained from a number of analytic fits derived **by** the author from plant data supplied **by** Commonwealth Edision. The plant data were measured in the years **1958-1962,** and it seems to be utility practice not to update such data with the age of the plants. As such, a cause of significant deviations from optimal operations of a utility system may possibly lie in the outdated heat-rate statistics used(28). Considering the approximate nature of the statistics to the actual performance levels, standardized heat-rate curves were derived for the three types of fossil plants for which data was available: large fossil **(300 - 600** MWe), medium fossil **(150 - 300** MWe), and small fossil **(150 - 50** MWe). The heat-rate used for individual plant would be obtained **by**

multiplying the appropriate standardized heat-rate **by** an individual plant factor (average heat-rate at rated capacity) to lower or raise the standard curve to fit individual plant characteristics. During **1960,** Commonwealth Edison had no data for the **1000** MWe class of fossil plants because none existed. Thus the heat-rates of plants used in this stuly are derived from the large fossil standardized heat-rate curve whereas if data were available, it would be more appropriate to use a separate standardized heat-rate curve for these extra large fossil units. Figures B.2, B.3, and B.4 show the analytically fitted standardized heat-rate curves derived for large, meiium and small fossil units, respectively. The individual data points are not shown to preserve the confidentiality of the material.

B.3 OCNP Values from Case 2

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TABLE B.3.1

WEEKLY **OCNP FUNCTIONS** OF UNIT **1** FOR APRIL FROM THE MULTI-REACTOR OPTIMIZATION **(CASE** 2)

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WEEKLY **OCNP** FUNCTIONS OF UNIT **1** FOR MAY FROM THE MULTI-REACToR OPTIMIZATION **(CASE** 2)

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WEEKLY **OCNP FUNCTIONS** OF UNIT **1** FOR **JUNE** FROM THE MULTI-REACTOR OPTIMIZATION **(CASE** 2)

WEEKLY **OCNP FUNCTIONS** OF UNIT **1** FOR **JULY** FROM THE MULTI-REACTOR OPTIMIZATION **(CASE** 2)

WEEKLY **OCNP FUNCTIONS** OF UNIT **1** FOR **AUGUST** FROM THE MULTI-RFACTOR OPTIMIZATION **(CASE** 2)

WEEKLY **OCNP FUNCTIONS** OF UNIT **1** FOR SEPTEMBER

WEEKLY **OCNP FUNCTIONS** OF UNIT 2 FOR APRIL FROM THE MULTI-REACTOR OPTIMIZATION **(CASE** 2)

WEEKLY **OCNP FUNCTIONS** OF UNIT 2 FOR MAY FROM THE MULTI-REACTOR OPTIMIZATION **(CASE** 2)

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WEEKLY **OCNP FUNCTIONS** OF UNIT 2 FOR **JUNE** FROM THE MULTI-REACTOR OPTIMIZATION **(CASE** 2)

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WEEKLY **OCNP FUNCTIONS** OF UNIT 2 FOR **JULY** FROM THE MULTI-REACTOR OPTIMIZATION **(CASE** 2)

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WEEKLY **OCNP FUNCTIONS** OF UNIT 2 FOR **AUGUST** FROM THE MULTI-REACTOR OPTIMIZATION **(CASE** 2)

 $\sim 10^{-1}$

WEEKLY **OCNP FUNCTIONS** OF UNIT 2 FOR SEPTEMBER FROM THE MULTI-REACTOR OPTIMIZATION **(CASE** 2)

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Appendix **C:** PROCOST

C.1 Introduction

The organization **of** PROCOST and the algorithm of its main components were *discussed-in* Section 4.0. **A** review of MPSX and the detailed algorithm of SECURIT are covered in later sections of this Appendix. The major topic remaining is the general operating philosophy for using PROCOST. The flowchart of PROCOST is given in Figure **C.1.** The component subprograms of PROCOST are:

- **NUC_OPT:** main program that writes the L.P. nuclear optimization formulation;
- PEAKERS: subroutine that simulates the operation of peaking units;
- PECK OR: subroutine that formulates the fossil economic loading order;
- **DURATN:** subroutine that calculates the load-duration load model

MPSX: the program that solves the L.P. nuclear problem; **PUMPST:** main pumped-storage simulation program that also

reads the L.P. nuclear solution, and calculates **OCNP; ECO:** economic pumped-storage subroutine; SECURIT: security pumped-storage subroutine.

The function of PROCOST is two-fold **(1)** to calculate **ONP** values, and (2) to calculate the optimal dispatching schedule for the system's nuclear reactor(s). The latter step assumes that the modelling assumptions used in the other system components are reasonable in order to derive a

feasible and optimal nuclear dispatching schedule. Use of PROCOST is tied to the (method of) solution of the short-range problem, in as much as PROCOST attempts to supply the information **(OCNP** values and dispatching schedules) specified **by** the theory. Use of any other production cost code in place of PROCOST that supplied the same information would be also serve the purpose.

A great amount of effort **has** been directed toward making PROCOST a fast and efficient program. Compared with the early version, very substantial improvement in computational performance had been made. To calculate **OCNP** values, the current version of **NUC OPT** consumes about 0.2 CPU-Sec./value, MPSX consumes about 0.2 CPU-sec/value, while **PUMPST** consumes about **1.1** ZPU-sec./value. Most of the developmental effort had been toward improving the L.P. calculations, so that it is no longer the constricting **job** step (in terms of **CPU** time).

PUMPST was originally designed for a detailed pumped-storage optimization based on the 168-hour load model. Hence, a great deal of calculational effort is wasted when **PUMPST** is used with **a** six-interval load model. Therefore, it is recommended that: **(1)** the present pumped-storage version of PUMP_ST not be used for the OCNP calculations but reserved for use when the detailed optimization schedule is desired; (2) a simpler model of pumped-storage operation be written for **OCNP** (six-interval models) calculations; **(3) PUMPST** be examined to reduce the large number of calculations it performs.

PROCOST has a core-storage requirement of **230** K. The determining step is in **NUCOPT** which is due to the overhead required to provide the dual capability of formulating L.P. problems with two types **of** load models (chronologic and load-duration) and accepting the original input (customer demand) data in any of three forms of load models. To achieve a large reduction in the storage requirement and improve CPU time, it is recommended that **NUC** OPT should be divided into two versions, one for load-duration models, and other for chronologic models.

In the present version of PROCOST, there is no constraint on the minimum operating level of the reactor. To make this option available, a new input variable, referred to as MINIMUM would be read in with the rated capacity (CAPACITY) of the reactor. MINIMUM would be considered the must-run portion of the nuclear unit, and have its capacity subtracted from the demand function prior to the L.P. formulation. In the L.P. model, the operating range of the reactor would be from zero to ZAPACITY-MINIMUM. The nuclear resource constraint in the L.P. model must also **be** modified, to subtract out the portion of energy already allocated to the must-run portion of the reactor. It is important that the nuclear heat-rate curve be use to calculate the correct value of this must-run energy. In addition, the nuclear heat-rate curve itself must be adjusted for use in the L.P. model due to the revised operating range of the reactor. Finally, MINIMUM should be added back to the nuclear optimized solution before the L.P. solution is to be printed.

The recommendations discussed above are related only to. improving the numerical techniques without changing any of the modelling assumptions involved. Many of the simple assumptions and concepts in PROCOST can be improved upon. Start-up and shut-down effects can be included **by** allowing use of several loading orders and load-duration curves, each appropriate for only certain hours **of** the day. Incorporating error bands on the customer demand function should be easily implemented **by** MPSX parametric procedures. Other possibilities are suggested in Sections **6.2, 5.5,** and **3.2.**

Even through PROCOST is not perfect, it is a very flexible program. The flexibility is derived from the many options available in **NUCOPT** and MPSX especially. **MPSX** is extensively used **by** the oil and gas industry. MPSX was designed as a production code where intermediate results can be saved, old L.P. problems can transferred, and many other useful features intended for users with a permanent interest in L. P. models. MPSX also has a great variety of parametric analysis routines and editting capability for L.P. models. Thus, once the basic L.P. model is formulated, NUC_OPT need mot be used again to alter the model. The editing faci lities of MPSX have be saved, solutions sufficient capability to perform any required adjustments to

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the L.P. model. The potential flexibility of MPSX makes it well suited for the type of analysis desired **by** the system planner, to study a variety of related and complex situations.

To facilitate manipulation of the L.P. model, a detailed description of the L.P. nuclear model is given next, in Appendix **C.2.** Following is a review of the MPSX control language program which dictates the optimization routines to be used on the L.P. model.

Appendix C.4 contains a detailed description of the pumped-storage security algorithm. The remaining sections of Appendix **C** are: description of the input specification to PROCOSr; listing of PROCOST; a complete listing of the PROCOST input file **SYSIN** for Case **3;** and a representative selection **of** computer output from Case **3.**

C.2 L.P. MODEL

Efficient use of PROCOST requires agile manipulation of the L.P. model, in the MPSX control language program. The following is a detailed description of the *L.P.* model (its row and column names), to facilitate its use. The equations governing the L.P. model were given in Section 4.2.1.

The L.P. model is as follows (describing the rows from top to bottom, and the columns from left to right). The first row is the objective function, named **CDST,** which is the summation of the incremental fossil fuel cost for the week, see Eqn. (4.1). Each time interval in the load model is simulated **by** a customer demand constraint equation, see Egn. (4.2). The row name of each of these eguations is of the form DEMANxxx where xxx is a three digit representation of the time interval being simulated. Each nuclear power reactor is represented **by** thermal nuclear resource constraint equation, see Eqn. (4.3). The row name of each of these equations is of the form NUCLRxxx where xxx is a three digit number assigned to each reactor. The constraints on each column variable is expressed **by** a **BOUND** row, see Eqn. (4.4). The **BOUND** row is named **"BOUND1".**

There is a separate column variable for each fossil and nuclear increment in each distinct time interval. The name of the fossil variables is of the form FFxxxyyy and the name of the nuclear variables is of the form Nxxxzzw where xxx is a three digit representation **of** the time interval number, **yyy** is a three digit representation of the fossil increment

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number, zz is a two digit representation of the reactor number, and w is a single digit representation of the nuclear increment number. The RHS column lists the values of the demand function and the nuclear resource constraints. The name of this column is RHS001. There are also RHS change columns which are used to, modify RHS columns to form new (temporary) RHS columns on which RHS parametric analysis is based. The change column named **CHCOO0,** is used to modify the customer demand function. For each nuclear resource row, there are two RHS change columns, one for positive changes, and one for negative changes. The name of these columns are of the form CHCxxx where xxx is a three digit representation of **(2n-1)** for positive changes, and (2n) for negative changes and where n is the reactor number.

The above description is valid for either a load-duration or a chronologic load representation in a one-week L.P. model. To represent several weeks using a load-duration model, one L.P. model is required for each week. To represent several weeks using a chronologic load model, only one L.P. model is reguired for each different fossil configuration. The variation in the time duration of each time interval (for different weeks in the load-duration mode) reguires a new L.P. model for each week. In the chronologic load model situation, the body of L.P. model is the same for different weeks (with the same fossil configuration). The only difference is an extra RHS column for each additional week. The name of this RHS column is of

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the form RHSxxx where xxx is a three digit representation of the week number. This difference in the number of L.P. models generated **by NUCOPT** must not be overlooked when specifying the MPSX control language program or in the **PUMP_ST** input parameters.

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C.3 MPSX

C.3.1 Control Language Program

MPSX (IBM program product) is a general purpose linear programming package. This section is not an introduction to **MPSX,** but rather a technical review of some useful MPSX programming procedures developed for the PROCOST operating environment. The prospective user of MPSX is referred to References (29,30) for introductions to linear programming and MPSX. An explanation of the keywords (commands) used in the **MPSX** control language program is given in Reference **(31).** An explanation of the role of the many subroutines available in MPSX, their abilities and their restrictions is covered in Reference **(32).**

MPSX is composed of two **job** steps: a compilation step and an execution step. The first step is the compiling of the **MPSX** control language program, which is the specification of the optimization procedures and parametric analysis used in solving the L.P. problem. The second step is the solving of the L.P. problem **by** the algorithm dictated in the MPSX control language program. Control is passed to the second step automatically upon completion of the first step. This section is a review **of** two sample MPSX control
language programs. It is assumed that the reader is familiar with **MPSX,** L.P., PL1, and general computer programming terminology.

The procedure for solving a simple L.P. problem is a straight-fDrward one. Sample **1,** listed in Appendix **C.3.2** is a simple example of a basic MPSX control language program solving a single L.P. problem. However, to efficiently solve a large number of related problems (as in calculating **OCNP** values), parametric technigues should be used. Instead of solving each problem from scratch, parametric analysis searches for a solution starting from the solution of a previously solved problem. Since the problems are related, their solutions are also similar. Thus a large amount of computations can be avoided **by** starting the calculations for solutions from an optimal solution of a related problem. Such an algorithm is illustrated in Sample 2. Sample 2, listed in Appendix **C.3.3,** is an example of a MPSX control language problem applicable to a single reactor optimization problem.

Sample **1** illustrate the basic steps in a control language problem: **(1)** identity the input data, "SYSTEB01"; (2) provide (or identify) the problem name, "MINIMIZE"; **(3)** convert the input data (located on file IN) to machine code; (4) ilentify the objective function, **"COST"; (5)** setup the problem with the appropriate bounds for solving; **(6)** identify the RHS, "RHS **001"; (7)** solve the problem; **(8)** write the solution (or a portion thereof). Each of the above functions corresponds with a command in the MPSX control language. The exact sequence of commands depends on the specific problem being solved as does the parameters used with commands. The PROGRAM statement denotes the beginning of the control program and **PEND** denotes the end. An asterisk in column 1 denotes a comment card. **A** TITLE statement provides a title on every page of MPSX output. The INITIALZ command initializes all MPSX variables to default values. The first MOVE statement informs the computer, the name of the input data to be read (important, since several input models may reside in the same device). The **name,** SYSTEBO1, is formed from the concatenation of the character variable, **SYSTE,** with the week number (2 digits) of the problem in NUC_OPT. The second MOVE statement identifies the name to be associated with the L.P. problem when.residing in the computer's storage devices. The name, "MINIMIZE" is arbitrary, but must not duplicate a name already on the PROFILE. The CONVERT instruction reads the data named SYSTEB01 on file IN, and converts the data to machine code. The third MOVE statement identifies the name of the L.P. row to be used as the objective function (several may be available). The **SETUP** command prepares the problem in matrix format ready for solving. **"BOUND1"** is the name of the row of bounds to be used in the present optimization. Minimization is the default mode. The fourth MOVE statement identifies the name of the RHS column to be used in the optimization (several may **be** available). The

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OPTIMIZE instruction performs the actual problem solving. The SOLUTION instruction writes the solution on the user file **SOLN.** Only selected information from the solution is written: columns **² ,** 4, and **8 of** the row variables and columns 2 and 4 of those column variables beginning with the letter **N** (the nuclear variables). The EXIT command terminates execution of the program. The entire solution is not written since the fossil schedule must complement the nuclear schedule to fulfill the demand function (conserving space and computer operations).

Sample **1** solves a single model without performing any parametric anaylsis. Sample **2,** listed in Appendix **D.2** is a more elaborate program that solves a large number of similar problems through repetitive use of subroutine call statements and parametric analysis. The subroutine structure is basically similar to Sample **¹**with the addition of the parametric analysis statements. The parametric analysis solves for the solution of the same basic L.P. problem for different increments of nuclear energy. Sample 2 is a typical example of how to program MPSX to obtain the values of 22 weekly **OCNP** functions.

The following discussion of Sample 2 will cover only those statements not explained above. The function of the MVADR statement is to change the program branch for XDOPRINT from the default procedure to the user procedure labelled **SET.** XDJPRINT is explained below. The XPREQLGD=O and XFREQLA=O statements sets the printing of the iteration log

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to a minimum (which is still guite voluminous). The XPARDELT=2 statement is related to XDOPRINT and will be discussed later. The EXEC(TIP) statement is a subroutine call to TIP. Subroutine TIP is called repeatedly to solve 22 different weekly L.P. molels, and perform parametric analyses. The length of the control language program is limited. Hence, when groups of commands are used repeatedly, subroutines and loops should be incorporated in the program to conserve the number of statements.

Subroutine TIP is established **by** using the name, TIP, as the label to the first command of the subroutine. TIP is the label to a CONVERT command. The end of subroutine is denoted **by** a **STEP** or **CONTINUE** command. The difference between **STEP** and **CONTINUE** is that execution is returned to the calling routine when **CONTINUE** is encountered, whereas **STEP** implies execution should go to the statement following the calling statement. Other entry points may be established in the subroutine **by** placing labels such as PARRR and **S2** on the relevant statements. The XPARAM=O resets -the system increment variable to its inital value.

An initial optimal solution to a L.P. model is required before the program can perform parametric analysis. Parametric RHS analysis also requires knowledge of how the RHS is to be varied and at what increments to write the solution. MOVE(XCHCOL,'CHC002') identifies the column named **'CHCO02'** as the Change Column that' is to **be** combined with the RRS column to form the new RHS. One unit of **'CHCO02'**

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will decrease the nuclear resource constraint **by 5%,** in the present version of **NUC_OPT.** The new parametric RHS is a combination the old RHS plus a multiple of 'CHC002'. XPARAM, the multiplier **of 'CHC002',** is increased continuously. XPARAM=0 sets its initial value to zero and XPARMAX=8, sets the final value of XPARAM to eight. PARARHS is the command which performs the parametric analysis. There is a pause each time XPARAM is a multiple of XPARADELT, which is set **by** the statement XPARDELr=2. When the pause occurs, XDOPRINT is signaled, which has been set to-call subroutine **SET,** which specifies that the current solution is to be written on file **SOLN.**

In other words, **for** each of the 22 L.P. models, the solution of the basic weekly L.P. problem was solved with the inital amount of nuclear resource, along with four other values of the nuclear resource, at **10%** decreasing intervals in nuclear energy. **A** total of **110** L.P. solutions will reside on user file **SOLN.**

A programming note: user files with large BLOCKSIZES will overload the buffers and result in **SCC=80A.** Unlimited increases in the RE3ION parameter on the **JOB** card will not alleviate the problem. The MPSX buffer core size parameter should be changed.

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 $\label{eq:2.1} \frac{1}{\sqrt{2}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\left(\frac{1}{\sqrt{2}}\right)^2\left(\frac{1}{\sqrt{2}}\right)^2\left(\frac{1}{\sqrt{2}}\right)^2\left(\frac{1}{\sqrt{2}}\right)^2.$

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 $\label{eq:2.1} \frac{1}{2} \sum_{i=1}^n \frac{1}{2} \sum_{j=1}^n \frac{$

 $\label{eq:2.1} \begin{split} \mathcal{L}_{\text{max}}(\mathcal{L}_{\text{max}}) = \mathcal{L}_{\text{max}}(\mathcal{L}_{\text{max}}) \,, \end{split}$

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 $\label{eq:2.1} \frac{1}{\sqrt{2}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\left(\frac{1}{\sqrt{2}}\right)^2\left(\frac{1}{\sqrt{2}}\right)^2\left(\frac{1}{\sqrt{2}}\right)^2\left(\frac{1}{\sqrt{2}}\right)^2.$

 $"COMASKS"$, $N*******"$, $"$ **CONTINUE** PEND \mathcal{L}_{max} and \mathcal{L}_{max} . $\label{eq:2.1} \frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac{1}{\sqrt{2}}\sum_{i=1}^n\frac$

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SOLUTION('FILE','SCLN','RSECTION','2/4/8','CSECTION','2/4/', X **SAM20073 SAM20074 'CMASKS','N*******',' ') SAM20075 STEP SAM20076** SOLUTION('FILE','SOLN','RSECTIUN','2/4/8','CSECTION','2/4/', X **SAM20077 SAM20078 SAM20079**

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C. 4 Pumped-Storage Security Algorithm

The peak-shaving pumped-storage generation schedule for this security model is the same as in the economic model. It is characterized **by** the pumped-storage generation level (power level K3 in Figure 4.9), where if demand load is above that level, then the pumped-storage generators produced enough power to make **up** the difference or until its nominal capcity(*) is reached.

The pumping schedule flowchart is shown in Figure C.2. The pump scheduling algorithm is determined as follows:

- **(1)** Define the periods when pumping is allowed and where it is not allowed. **A** bit string representing the -number of time intervals in a week can serve this purpose where a '1' bit means no pumping is allowed and a **''** bit means pumping is allowed. The string is initially all '0's. The generation periods are then denoted **by** '1' bits from an examination of the generation schedule. The bye periods(an input specification) before and after generation periods are also denoted **by** '1' bits. The remaining '0' bit substrings define periods when pumping is allowable.
- (2) Set pointers to the beginning and end of the next allowable pumping period.
- **(3)** Calculate the minimum amount of pumping that can be

(*) Nominal capcity is not the rated capacity of the generators, but that capacity intended for scheduled usage, the remainder is for emergency usage.

Figure C.2 SECURIT ALGORITHM

scheduled during this period before overflowing occurs. Hence, water-usage-to-date must be calculated for the present pumping period. The chronologic water level pattern is calculated **by** considering the generation schedule, free inflow (assumed uniform), pumping to late, and the starting water level (an input specification). The water level pattern is needed to determine the requirement of water to fill the reservoir during the present pumping period. That amount is the difference between the reservoir size and the calculated water level at the end of the period in question.

- (4) Search for the lowest demand interval during the pumping period. Scheduling pumping for this interval first is the most economic choice available. The timing of the pumping schedule is determined **by** this step.
- **(5)** The amount of pumping scheduled in an interval is subject to three constraints: (i) when capacity of the pump is reached, (ii) when the reservoir is-filled, and (iii) when fossil load level reaches the turnaround level(*). Whichever constraint becomes active first stops the pumping and hence determines the amount scheduled.

(*) Turnaround level is that load level, above which no pumping is allowed (K4 of Figure 4.9). It would be too expensive to pump. It's determined as a certain amount (an input specification) of MW below the pumped storage generation level (K3 of Figure 4.9).

(6) If constraints (i) or (iii) becomes active repeat step **4,** search for the lowest demand interval. If constraint (ii) becomes active, or time has run out(pumping has been scheduled for all allowable time intervals and reservoir is not full) then repeat step 2, defining the next pumping period. The subroutine returns to **ECO** when the end of the string has been reached.

PROCOST is composed of three program steps: (1) **NUC_OPT,** the preprocessor to MPSX which formulates the L.P. model; (2) **MPSX,** the program that solves the L.P. model; **(3)** PUMP ST, the pumped-storage program. The data input to MPSX are automatically written by NUC_OPT, hence, there are no input parameters directly fed to MPSX. Control of MPSX is derived from the input data to **NUCOPT** (which in turn inputs to **MPSX)** and the MPSX control language program (which was discussed in the previous section). The input specifications to **NUZOPT** and **PUMPST** are given below.

C.5.1 NUC-OPT Input Specifications

The file structure is:

(1) DATA: a transfer medium to MPSX,

(2) HYDRO: contains the hydro generation schedule,

(3) LDMDL: contains the customer demand function,

(4) **PEAKS:** contains peaking unit parameters,

(5) PECK: contains fossil loading order parameters,

(6) SYSIN: contains modelling parameters,

(7) TRANSFR: transfer medium to **PUMPST.**

The DATA file is the one on which NUC_OPT writes the MPSX input L.P. data. The record format should be card image, i.e., DCB=(RECFM=FB, LRECL=80, BLKSIZE=12880).

The HYDRO file contains the values of the array variable HYD, which is the dispatching schedule of the hydro unit (calculated off line).

The LDMDL file contains the values of the array

variable **DEMAND,** the weekly (chronologic) customer demand function.

The **PEAKS** file contains all the variables associated with the peaking units. One set of peaking unit variables is required for each week being simulated. If **52** weeks are being simulated, **52** sets of peaking parameters are required. Thus, there is available a large amount of flexibility in varying the peaking units available each week. **A** complete input set consists of the following parameters: P NUM: the number of peaking units for the week. CFACTOR: the simulated capacity factor for a peaking unit. RATIN3: the rated capacity of the peaking unit, MW.

HEAT: the average heat-rate of the peaking unit at rated capacity, (million BTU/MWH).

F_COST: the fuel cost of the peaking unit, (\$/million BTU). SUSD: the average cost of one start-up and shut-down, (3). **CODE:** if **2ODE=O,** then the detailed peaking unit generation

schedule is printed.

At the very least, the minimum input set consists of a zero value for P_NUM, otherwise PROCOST will ABEND. When P_NUM is not zero, the five peaking unit variables above are read successively (in the order listed above), **P_NUM** number of times. **CODE** is the last variable listed in a single set of peaking unit data.

The PECK file contains all the variables associated with the fossil economic incremental loading order. The input variables (listed in order of input) are:

NI: The number of large fossil units.

- **VP1:** The number of valve points modelled in the large fossil units.
- **N2:** The number of medium fossil units.
- VP2: The number of valve points modelled in the medium fossil units.
- **N3:** The number of small fossil units.
- VP3: The number of valve points modelled in the small fossil units.
- LGE_HEAT(VP1,2): Array containing the average heat-rate data for large fossil units.
- MED_HEAT(VP2,2): Array containing the average heat-rate data for medium fossil units.
- SML_HEAT(VP3,2): Array containing the average heat-rate data for small fossil units.
- **NL3E(N1,4):** Array Containing the station characteristics of large fossil units. The parameters of interest for each station are the number of units, MW capacity of each unit, the heat rate (million BTU/MWH), and the fuel cost (\$/million **BTU).**
- NMED($2, 4$): Array containing the station characteristics of medium fossil units. The parameters of interest for each station are the number of units, MW capacity of each unit, the heat rate (million BrU/MWH), and the fuel cost (\$/million **BTU).**
- **NSML(N3,4):** Array containing the station characteristics of small fossil units. The parameters of interest for each

station are the number of units, MW capacity of each unit, the heat rate (million BTU/MWH), and the fuel cost (\$/million **BTU).**

EMERG: The size (MW) of the last increment added to the economic loading order (as an insurance measure). This may represent emergency purchase capacity.

E COST: The cost (mills/KWH) of the last increment.

The SYSIN file contains the parameters associated with the structure of the L.P. model. The names of the variables (listed in the order of input) are:

- **SYSTE:** The name to be associated with the L.P. model to be written on file **DATA. A** maximum of six characters is allowed in the name.
- **M&DE:** aGDE-'CHR' for chronologic load model mode, and MODE='DUR' for load-duration load model mode.
- TRUE: The actual number of hours represented **by** the load model. **TRUE=168** for a weekly load model.
- **N1:** The number of time intervals in the input load model on file LDMDL.
- **N2:** The number of time intervals desired in the load-duration model. If MODE='CHR', then set **N2=N1.**
- **VP:** The number of valve points in the input nuclear heat rate curve.

NUMBER: the number **of** nuclear reactors in the L.P. model.

K: the number **of** increments in the fossil economic incremental loading order.

- PARAMETER: If no parametric analysis on the modified demand function will be performed **by** MPSX, set PARAMETER=O, else chose **I1'** or '21. When PARAMETER=1, the change column equals **1%** of the modified demand function; if PARAMETER=2, then it equals **100** MW.
- WEEKS: the number of weeks using the same economic loading order and hydro generation schedule.
- PECKING: ='YES' if the fossil economic incremental loading order is desired to be punched out on cards, in a format usable in FOSSIL.

='NO' if punched cards not desired.

- TIME(N1): The array describing the weight (in hours) assigned to each time interval in the input load model. If **TRUE=N1** then all values in TIME are automatically set equal to **1.** In such a case, TIME should be omitted. **CODE(TRUE):** an array containing the correspondence in which the input load model can be expanded to the basic **(168)** hourly load model. If **TRUE=N1,** omit this variable, the program will substitute the correct values.
- **LOAD(NUMBER):** the array containing the average weekly nuclear capacity factors used in calculating the nuclear resource constraint (and included in the RHS column vectors).
- EFFIC(VP,2): the array containing the nuclear incremental heat rate data.

CAPACITY(NUMBER): the array containing the capacities(MW)

of the nuclear reactors.

BTU(NUMBER): the array containing the average heat rate at rated capacity for each of the nuclear reactors.

The TRANSFR file is the medium on which **NUCOPT** writes the values of several system variables to be transferred to the pumped storage routine, PUMP_ST. An adequate DCB for TRANSFE is (RECFM=U,BLKSIZE=13030).

- **C.5.2 PUMPST** Input Specifications The file structure is:
- **(1)** SYSIN: contains pumped-storage modelling parameters;
- (2) TRANSFR: contains system parameters transferred from NUC_OPT;
- **(3) SOLN:** contains the L.P. model solutions written **by MPSX.**

The input parameters (listed **by** order of input) on file SYSIN are:

MODE= **'QUCK'** if only the nuclear L.P. solution is to be printed, no pumped-storage simulation,

'NONE' if more detailed information about system is to be printed but still no pumped-storage simulation, **⁼IECO'** if the economic pumped-storage schedule is to be calculated,

⁼#SEC' if security pumped-storage schedule is to be calculated.

CODE=O if printing the detailed dispatching schedule is desired.

=1 if printing the detailed dispatching schedule is

not desired.

CAPACITY= MW generation capacity of pumped-storage unit. RATIO= cycle efficiency of pumped-storage unit (fraction). CAP_PUMP= MW'pumping capacity of pumped-storage unit. RESERIOR= MWH size of pumped-storage reservoir. FREE= weekly stream inflow into pumped-storage unit (MWH). START= starting water level of reservoir (MWH). BYE= time (Hours) of transition (rest) interval before and

after generation.

- **TOLERANCE=** The buffer **(MW)** below the minimum pumped-storage generation (demand) level at which no pumping is allowed.
- **ALLOT(N)=** array containing the number of L.P. solutions solved for a weekly L.P. model, where **N=1** for a load-duration model and **N=** the number of weeks using the same L.P. model for a chronologic load model.

I= number of descriptive character strings immediately following, that are to printed on the computer output.

TITLE= a descriptive character string with maximum length of **80** characters, entered I times.

In the load-duration mode, the last three parameters are repeated for each week having the same fossil configuration, see sample input.

The whole sequence of parameters above is repeated for each fossil configuration in PROCOST. An example of a sample input is presented in Appendix **C.7,** the complete listing **of** the card input for Case **3.** In Appendix **C.8** is a

Programming Notes: **(1) All** input parameters reguired on file SYSIN are format-free; (2) Caution, the use of a DUMMY file for the MPSX SYSPRINT should be reserved for those with an expert knowledge of MPSX; **(3)** Subroutine **DURATN** calls the Fortran subroutine, ISORT (35) , to sort the elements of an array into ascending order. It is important that the **JCL** is in the correct order to establish the proper linkage.

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PROC0217 DO J=1 TO N2: **PROCO218** PUT FILE(DATA) EDIT $(IRHS^+, I, {}^{\dagger}DEMAN^+, J, DEMAN^-, J)$ PR0C0219 P'999', COL(15), A, P'999', COL(25), PROCO220 $(SKI P, COL (5), A,$ PR0C0221 $p1$ -------V.9999'): **PROCO222** END: **PROCO223** DO J=1 TO NUMBER; PROCO224 PUT FILE(DATA) EDIT **PROC0225** $(IRHS^T, I, INUCLR^T, J, N_RHS(J))$ P1999', COL(15), A, P1999', COL(25), **PROCO226** $(SKIP, COL(5), A,$ $P1$ -------V.9999'): PROCO227 PROCO228 END; **PROCO229** IF MODE='DUR' THEN I=WEEKS; $END:$ **PROC0230 PROC0231** IF PARAMETER=0 THEN GO TO SKIPP; IF PARAMETER=1 THEN DO: PROCO232 **PROC0233** DO J=1 TO N2; PUT FILE(DATA) EDIT('CHC',0,'DEMAN',J,DEMAN(J)/100) PROCO234 P'999', COL(15), A, P'999', COL(25), **PROC0235** $(SKIP, COL(5), A,$ $p1$ -------- V_2 9999! : **PROC0236 PROCO237** END: END: IF PARAMETER=2 THEN DO: **PROC0238 PROC0239** DO J=1 TO N2; PUT FILE(DATA) EDIT('CHC', 0, 'DEMAN', J, 100) **PROCO240** P'999',COI(15),A,P'999',COL(25), **PROC0241** $(SKIP, COL. (5), A,$ $P1------V.9999!)$: **PROCO242 PROCO243** END; END; SKIPP: **PROCO244 PROCO245** $D()$ I=1 TO NUMBER; **PROC0246** PUT FILE(DATA) EDIT('CHC',2*I-1,'NUCLR',I, CHANGE(I)) P'999', COL (15), A, P'999', COL (25), **PROC0247** $(SKIP, COL(5), A,$ P^{\dagger} = = = = = = = - V. 9999' }; **PROC0248** PUT FILE(DATA) EDIT('CHC',2*I ,'NUCLR',I,-CHANGE(I)) **PROC0249** $(SKIP, COL(5), A,$ $P'999'$, $COL(15)$, A , $P'999'$, $COL(25)$, **PROCO250** $P1$ -------V.9999'); PR0C0251 END: **PROCO252**

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 $\label{eq:2.1} \frac{1}{\sqrt{2}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{$

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LIST(
'NUCLEAR UNITDISPATCHING: ');
                                                                         00001910PROC0757PUT FILF(SYSPRINT)
SKIP00001920PROC075800001930PROC0759ED IT(
'INTERVAL WEIGHTING FACTOP')(A);
              PUT FILE(SYSPRINT)
                                                                         00001940 PROC0760
              FDIT(
' DEMAND' , 'FOS
SIL','NUCLEAR l','NUCLEAR
2',
                                                                         00001950PROC0761'NUCLEAR 3',...')
(X-(5), 3( AX(9 )),3(A,X
(9 )));
                                                                         00001960PROC0762PUT SKIP EDIT (
                                                                         00001970PROC0763'(HOURS)', '(MW)'
, (MW)',
'(MW)',
'(MW)',
'(MW)')(
                                                                         00001980PROC0764COL(14),A(7), COL
(33), A(4
), X(11)
,A
                                                                         00001990PROC07653(X(13), A(4)):
                                                                         00002000 PROC0766
              no 1=1 TO NN;
                                                                         00002010PROC0767PUT FILE(SYSPR
INT)
                                                                         00002020PROC0768EDIT( I, TIME(
I), DEMAND(I), FOSSIL(I)-,(
                                                                         00002030PROC0769NUCLEAR(IJ)
DO J=1 TO NUMBER)) (
                                                                         00002040 PROC0770
                                                                         00002050PROCU771F(5),F(12),F(
20), F(15), 4 F(17))SKIP;

00002060PROC0772END;
              PEAD FILE(SOLN) IGNORE(2);
                                                                         00002070PROC0773*<sub>1</sub>/* END OF L.P. READERSECTION00002080 PROCOll4
/* MODE OF OPERATION OF
PUMPED STORAGE UNIT IS CHOSEN: (1) IF "NONE",
                                                                         00002090PROC0775
                                                                         00002100PROC0776THEN NO P.S. UNIT IS SCHEDULED, THE PROGRAM CONTINUES WITH
CALCULATING THE FOSSILINCREMENTAL CAPACITY FACTORS; (2) IF "QUCK",
                                                                         00002110PROC0777THEN NO FURTHER PROCESSING (NO P.S. SCHEDULING, AND NO INCREMENTAL
                                                                         00002120PROC0778FOSSIL CAPACITY FACTOR CALCULATIONS); (3) IF "ECO", THEN THE ECONOMIC
                                                                         00002130PROC0779
PUMPED STORAGE ALGORITHM IS CALLED; (4) IF "SEC",
THEN THE SECURITY
                                                                         00002140 PROC0780
P.S. ALGORITHM IS CALLED. *******************/
                                                                         00002150PROC0781DO I=1 TO NI;
                                                                         00002160PROC0782LOAD(I)= FOSSIL(ORDER(I));
                                                                         00002170'PROC0783END;
                                                                         00002180PROC0784IF MODE='NONE' THEN00002190PROC0785
                 GO TO REPORT;00002200 PROC0786
              IF MODE='QUCK' THEN00002210PROC0787GO TO SHORT CUT;
                                                                         00002220PROC0788PUT SKIP(2) LIST('PUMPED STORAGE
STATISTICS:');
                                                                         00002230PROC0789IF MODE='ECO' I MODE='SEC' THEN00002240 PROC0790
                 CALL00002250PROC0791ECO(N1,CUM, LOAD,CODE, CUM_STEP,FUEL, MODE, CAPACITY, 00002260 PROCO792
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 $\label{eq:2.1} \frac{1}{\sqrt{2}}\int_{\mathbb{R}^3}\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2\frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^2.$

 $\label{eq:2.1} \mathcal{L}(\mathcal{L}^{\mathcal{L}}_{\mathcal{L}}(\mathcal{L}^{\mathcal{L}}_{\mathcal{L}})) = \mathcal{L}(\mathcal{L}^{\mathcal{L}}_{\mathcal{L}}(\mathcal{L}^{\mathcal{L}}_{\mathcal{L}})) = \mathcal{L}(\mathcal{L}^{\mathcal{L}}_{\mathcal{L}}(\mathcal{L}^{\mathcal{L}}_{\mathcal{L}}))$

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 $\label{eq:2.1} \frac{1}{\sqrt{2}}\left(\frac{1}{\sqrt{2}}\right)^{2} \left(\frac{1}{\sqrt{2}}\right)^{2} \left(\$

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IF LOAD(I) > CAPACITY THEN
                                                                                         00001260PROCll 7STORE(I) = CAPACITY;
                                                                                         00001270PROC1118ELSE00001280PROC1119STIRE(I)=LOAD(I);
                                                                                         00001290PROC1l20
      END;
                                                                                         00001300PROC1121F_COST(1)=SUM(STORE);
                                                                                         00001310PROC1122F (1 )=N1;
                                                                                         00001320PROC1123DO KK=CJM TO 2 BY -1 WHILE ( F_COST(IKK)
<= 0);
                                                                                         00001330PROC1124END;
                                                                                         00001340 PROC1125
/* "KK" RECORDS THE INCREMENT LEVEL WHERE PUM
PING COMES
INTO PLAY,
                                                                                         00001350PROC 126WHEREAS, THE FREE WATER INFLOW DID ALL THE PE
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             IF LOAD(J)-CAPACITY > LOAD(I) THEN
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          SUN(I)=TEMP-FR
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IF (AMT **>=** MARGIN} **&** (PUMP **>=** MARGIN) **THEN 00001270**PROC **162100001280**PROC1622DO; $*$ / **00001290**PROC1623 */** RESERVIOR **IS** FILLED **NEW(** LOWEST (2 **))=NEW(LOWEST** (2))+MARGIN; **00001300**PROC1624 **00001310**PROC1625 STOPE(LOWEST(2))=PARGIN; **00001320**PROC1626**GO** TO **NEXTLEVEL; 00001330**PROC1627**END;** 00001340 PROC1628 **ELSE00001350**PROC1629 **DO; 00001360**PROC1630*/** **SCHEDULE PUMPING** CAPACITY OR TIL **TURNAROUND** LEVEL **IS** REACHED ***/ 00001370**PROC1631 IF AMT **> PUMP THEN00001380**PROC1632AMT=PUMP;**00001390**PROC1633MARGIN=MARGIN-AMT;00001400 PROC1634 STORE(LOWEST(2))=AMT; NEW(LOWEST(2))= NEW(LOWEST(2))+AMT; 00001410PROC1635 /* FIND **NEXT** LOWEST **DEMAND** PERIOD ***/** 00001420 PROC1636 00001430 PROC1637 TEMP(LOWEST(2))=90000; 00001440 PROC1638 LOWEST(1)=90000; 00001450 PROC1639 **GO** TO SORT;00001460 PROC1640 **END; */**00001470 PROC1641 */** MOVE POINTER 00001480 PROC1642 **NEXTLEVEL:** IF **LENGTH(STRING)=LENGT THEN** 0**0001490** PROC1643 **00001500**PROC1644RETURN;**00001510**PROC1645**LENGT =LENGT +1; 00001520**PROC1646 STRING=SUBSTR(STRING,LENGT); POINT=POINT+LENGT **-1; 00001530**PROC164T00001540 PROC1648 **LENGT** =INDEX(STRING,'0'BI; **00001550**PROC1649IF **LENGT = 0 THEN 00001560**PROC **1650**RETURN;STRING=SUBSTR(STRING, LENGT); **00001570**PROC1651**POINT=POINT+LENGT -1; 00001580**PROC1652**GO** TO WATERLEVEL; **00001590**PROC1653**00001600**PRiC1654 **END** SECURIT **; .**

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APPENDIX **D: ALLOCAT**

D.1 Input Specifications

Input Variable Names listed **by** order of input on file SYSIN:

NCF: Overall nuclear capacity factor for the planning period.

WEEKS: Number of weeks in the planning period.

LENGTH: Dne more than the maximum number of **OCNP** data $\pmb{\cdot}$ points in a weekly curve.

KEY= **'SAME',** if all weekly sets of **OCNP** values are obtained from a single set of weekly nuclear capacity factors;

else KEY=(any four characters).

N=number of **OCNP** values in weekly representation

INTERVALS(N)=interval spacing of **OCNP** values

OCNP(N)=GCNP data walues

If KEY7'SAME' then the last three variables are repeated WEEKS times. If KEY='SAME' then **N** and INTERVALS need be listed only once.

NOTES: The number of **OCNP** data points for each week need not be the *same.* The algorithm is given in Section 4.3.

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APPENDIX D.3 SAMPLE OUTPUT FROM ALLOCAT

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Appendix **E:** Effect **of** Time Value of Money

An experiment was made in which the result of optimizing a system for minimum discounted production cost *was* compared with result of optimizing the the system for minimum undiscounted production cost. Although the optimum system generation schedules for the two cases were guite different, a comparison of discounted production costs for both schedules showed that they were practically identical. In summary, disregarding the time value of money has very little effect on the financial consequences of the short-range optimization.

A system of four units with a system capacity of 2400 MWe of which 44% was nuclear was -studied over a one-year time horizon with a discount factor of **8%.** Table **E.1** lists the parameters used. The time horizon used in this study was one year, consisting of **26** equal time intervals. The biweekly electric system demand was obtained **by** using **1%** of the total biweekly demand of electricity of the United States, from June **1971** to May **1972** (15). The system under consideration consisted of two **536** MWe nuclear plants, each with the heat-rate vs. **%** power characteristics given in Table **E.1** and two **670** MWe fossil plants with the heat-rate **vs.** % power characteristics given there. These average heat-rate characteristics are those recommended **by** Commonwealth Edison. The cost of heat to each nuclear plant was taken as 0.45 mills/KWHt; to fossil unit No. **1, 1.8** mills/KWHt; and to fossil unit No. 2, 2.0 mills/KWHt.

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TABLE E.1

PARAMETERS OF **THE COST** *OF MONEY* EXPERIMENT

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Thermal energy available in one nuclear unit (No. **3)** was limited to **8.5** million MWHt, prior to scheduled refueling in biweekly period No. 20. After refueling , this unit was assumed available **99%** of the time. The thermal energy available in the second nuclear unit (No. 4) was limited to 4.0 million MWHt prior to refueling in biweekly period No. **10.** After refueling, this unit was assumed to be available **96%** of the time. Refueling downtime was neglected.

The method of optimization used was linear programming, IBM's MPSX program product. The objective function was the variable costs of this system, assumed to be the cost of the fuel for the fossil plants and the income tax depreciation credit for the nuclear heat utilized.

The solution of the optimization studies is displayed as follows: in Figures **E.1** and **E.2,** the solid lines plot the biweekly generation distribution for each of the system's units for the case of no discounting, i.e., zero effective cost **of** money; and, the dashed lines display the case of discounting both the fossil fuel costs and the nuclear fuel tax credits.

From the comparison of the solid and dashed lines, notice that the effect of the discounting is to shift the assignment of the fossil units to operate at lower capacity factors in the earlier time intervals and at higher capacity in the later time intervals. Correspondingly, the nuclear units are operating at higher capacity factors in the earlier time periods. This is not surprising because

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Legend no discounting production schedule **---** production shift due to discounting Objective Function no discounting, **\$29.5** million with discounting, \$29.4 million

I I discounting naturally has the effect of postponing cash outflows as much as possible and taking tax credits as soon as possible.

But what is the magnitude of this effect? Is it of concern where the largest time period in our studies is only one year? The change in the objective function from the comparison **of** the total-discounting case with the no-discounting case was 0.31X. But for a system where the average customer demand is about **10,000** MWe and the nuclear plants supplied about 48% of the power, the use of discounting represents a saving of about half million dollars per year. However, the frequent fluctuations of the market price of fossil fuel and the stochastic nature of the customer demand function introduces error bounds larger than the savings involved. As large as this savings may sound economically, the reliability considerations as mentioned in Section 2.4 subjectively outweight the savings of distorting the production schedule to favor nuclear utilization early in time over later periods of time.

Even though discounting is a very important factor in considering alternatives in the mid-range horizon, its use in the short-range is considered to be swamped **by** reliability concerns caused **by** the random statistical nature of events in the short-run **(11 .** Hence, discounting has not been taken into account in the present short-range studies.

Appendix F: FOSSIL

F.1 Input Soecifications

Input variables listed **by** order of input on file SYSIN: **N=** number of time intervals in weekly load model. **N1=** number of increments in the fossil economic loading order. **NN=** number of weeks using the same loading order. NUMBER= number of nuclear energy values to be read. $DEFiAND(NN, N)$ = array containing the modified customer demand

functions.

TIME(NN, N)= array containing the number of hours each time interval (in the load model) represents.

NUCLEAR(NUMBER)= array containing the nuclear energies(MWe). Economic Loading Order= use card output from PROCOST.

The items of interest on the cards are the cumulative interval sizes(MW), incremental fuel cost (mills/KWHe), and the cumulative generation cost $(\frac{4}{H})$.

For multiple cases, the whole set of variables is repeated for each set of fossil configurations.

The sample input (Appendix $F.2$) is a portion of that used for Case 4. The sample output (Appendix *F.3) is* the entire output of FOSSIL for Case 4. The OCNP values obtained from the FOSSIL output are the same as those used in the sample input to **ALLOCAT,** in Appendix **D.2.**

77 EXEC PLIXCGU **//C. SYSINDD** tDCB=BLKSIZE=2000) **FOSS IL:**PROC OPTIONS(MAIN); **DCL (N,** NINNNUMBER)FIXED **BIN; ON** ENOFI**LE(SYSIN) GO** TO BOTTOM; TOP: **GETLIST(N, Ni, NN, NUNBER)** COPY; BLOCK: BEGIN;**DCL CCNP FLOAT DEC(16)** ; **DCL (DEMAND(NN,N), TIME(NN,N), NTEMP, CSTEP (NI)** , **NUCLEAR (NUMBER)**) FIXED BIN(31), TOTAL FIXED **DEC (15,2); DCL (FUE L(Ni), CFUEL(N1))** FIXED **DEC(15,2); GET LIST (DEMAND,** TIME, **NUCLEAR)** COPY; **DO** I=1 TO **Ni; GET** EDIT(**CSTEP(I), FUEL(I), CFUEL(I)**)(SK IP,X(15), F(1O), F(10,2), **F(15)**); **END; DO J=1** TO **NN; DO** M=l TO NUMBER;**PUT** SKIP **DATA(NUCLEAR(M));** TOTAL=U;**OCNP=O;** DO **1=1** TO **N; NTEMP= DEMAND(J,** I) **-** NUCLEAR(M); OCNP=CCNP+NTEMP*TIME(J, I); **DO K=N1** TO **1** BY **-1** WHILE(NTEMP **<** CSTEP(K)) ;**END;** IF K=O **THEN** TOTAL=TOTAL+NTEMP*FUEL(K+1)*TI **ME(J, I); ELSE** TDTAL=TOTAL+TIME(J, I) **END; CC NP=(CNP/168.;** DO K=i TO **NI** WHILE(OCNP **>**C.STEP(K)); END ; nCNP= FUEL(K); PUT SKIP;***((NTEMP-C_STEP(K))*FUEL (K+1)+C.FUEL(K))** ;

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ERMPLE OUTPUT FROM FOSSIL

APPENDIX F.3

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Biographical Note

Raymond Eng was born on February 2, 1948 in Bronx, New York. He attended elementary school at **P.S.** 200 and junior high school at **P.S. 128,** and high school at Brooklyn Technical High School, all located in Brooklyn, New York. For his undergraduate studies, he attended Massachusetts Institute of Technology from September **1965** to June **1969.** He received a B.S. degree from the Department of Chemistry majoring in Chemical Physics and minoring in Economics. He received a Uniroyal Scholarship during his junior and senior year.

His undergraduate research in Nuclear Chemistry, titled "Isomeric-Yield Ratios of Cd-117 in the (n.X) and (d, p) Reactions", was published in the Journal of Inorganic and Nuclear Chemistry, Volume **35, 1973, pp 371-380,** Pergamon Press, Great Britain.

He was awarded a three-year **AEC** fellowship to continue his graduate work in M.I.T.'s Department of Nuclear Engineering, majoring in Nuclear Fuel Management. His minor was in Management.

He was also extensively involved in a variety of extra-curricular activities. He was elected member of the Graduate Student Council, elected Social Chairman and Treasurer of Ashdown House, and elected President of the MIT Chinese Student Club during his graduate residence years.