Tentative evidence for excess GeV-scale gamma rays from the Galactic Center has been corroborated by several groups, including the Fermi collaboration, on whose data the observation is based. Dark matter annihilation into standard model particles has been shown to give a good fit to the signal for a variety of final state particles, but models with heavy mediators are typically inconsistent with constraints from direct detection or monojets. Models where the dark matter annihilates to mediators that subsequently decay are less constrained. We perform global fits of such models to recent data, allowing branching fractions to all possible fermionic final states to vary. The best fit models, including constraints from the AMS-02 experiment (and also antiproton ratio), require branching primarily to muons, with a $\sim 10\%$ admixture of $b$ quarks, and no other species. This suggests models in which there are two scalar mediators that mix with the Higgs, and have masses consistent with such a decay pattern. The scalar that decays to $\mu^+\mu^-$ must therefore be lighter than $2m_\tau \cong 3.6$ GeV. Such a small mass can cause Sommerfeld enhancement, which is useful to explain why the best-fit annihilation cross section is larger than the value needed for a thermal relic density. For light mediator masses (0.2–2) GeV, it can also naturally lead to elastic dark matter self-interactions at the right level for addressing discrepancies in small structure formation as predicted by collisionless cold dark matter.

I. INTRODUCTION

Indirect detection may offer the best hope of discovering the nature of dark matter beyond its generic gravitational effects. Currently there is a strong hint from Fermi Large Area Telescope data of dark matter annihilation in the Galactic Center (GC), giving rise to an excess of gamma rays peaking at energies of several GeV [1–6]. The morphology is consistent with that expected from dark matter annihilations, and the required cross section is of the right order of magnitude for yielding the correct thermal relic density. Millisecond pulsars are the main conventional astrophysical explanation that has been proposed [7–11] (see however Refs. [12,13] for alternative explanations). Arguments against the pulsar explanation have been given in Refs. [14–16]. While the debate continues, the dark matter explanation remains a possibility that is still being widely explored [17–65].

The simplest models have heavy $s$-channel mediators leading to annihilations $\chi\chi \rightarrow f\bar{f}$ where $f$ represents standard model particles that lead to gamma rays through their decays (or possibly inverse Compton scattering). However even if the mediator does not couple directly to light quarks, its coupling to any charged particle induces mixing with the photon at one loop, leading to dark matter scattering on nucleons. For heavy mediators in which an effective operator analysis of the GC excess is appropriate, the induced coupling typically exceeds that allowed by direct detection or monojet searches, when the annihilation cross section for $\chi\chi \rightarrow f\bar{f}$ is large enough to explain the GC gamma-ray excess (see [66] and references therein). Cosmic ray antiproton data also put pressure on direct annihilation to $bb$ [67,68] (see however [69]).

To escape direct detection and antiproton constraints, one can consider the possibility of light mediators $\phi$ that are produced on shell in the annihilations $\chi\chi \rightarrow \phi\phi$, and subsequently decay. Even relatively slow decays due to very small couplings of $\phi$ to standard model particles can be consistent with the morphology of the GC signal, while making the models compatible with direct searches [66,70–82].

In the present study we reconsider light mediator models, motivated by new data sets for the GC excess, one from Ref. [6] [hereafter Calore-Cholis-Weniger (CCW)] and the other presented by the Fermi collaboration itself [83]. These results allow for heavier dark matter producing gamma rays up to higher energies $\sim 100$ GeV than the earlier determinations of [3,4] which preferred lighter $\sim 30$ GeV dark matter, though the error bars are large.
enough for overlap of the allowed parameters. In addition we take into account constraints on annihilations producing electrons, from the AMS-02 experiment [84,85]. These turn out to strongly disfavor direct annihilations into electrons that would produce a bump-like feature in the electron spectrum.

We find that the CCW and Fermi data show a strong preference for annihilation into mediators that decay with branching fractions \( \sim 80-90\% \) to muons and \( \sim 10-20\% \) to \( b \)-quarks. From a theoretical model building perspective this at first looks peculiar; for a single mediator to have such couplings is not suggested by any symmetry principle. On the other hand, singlet scalars that mix with the Higgs boson will decay preferentially into the heaviest possible standard model particle, since the couplings are just proportional to those of the Higgs. Therefore a more natural explanation is to have two mediators, one whose mass is between \( 2m_\nu \) and \( 2m_e \), and the other with mass between \( 2m_b \) and \( 2m_t \). (For a mediator with mass greater than \( 2m_b \) one must also consider decays into Higgs bosons.) By this combination of fitting to data and theoretical motivations, we are led to consider models with two scalar mediators with a hierarchy of masses. Remarkably, the best fit to the data puts the mediator masses in the ranges described above, which need not to have been the case. This provides further experimental motivation for building models with several mediators, which at first might have seemed like a large theoretical leap.

We begin our analysis with an agnostic view concerning theoretical models, assuming only a single mediator for simplicity, and allowing for arbitrary branching ratios into different lepton and quark flavors, whose spectra are provided by Ref. [86] (hereafter PPPC). We describe the construction of the \( \chi^2 \) functions for fitting to the CCW and Fermi data, respectively, combined with those of AMS-02. The preference for final states consisting of an admixture of muons and \( b \) quarks is thereby established. We then focus on these final states, adding a separate mediator coupled to each one, and refit to the data. In the following section, a simple model of two scalars mixing with the Higgs is presented. We subsequently check whether the preferred models are consistent with complementary constraints from direct detection, thermal relic density, cosmic microwave background, dwarf satellite observations, the antiproton flux ratio, and dark matter self-interactions. A simple two-mediator model is constructed that can fit the observations without excessive fine-tuning; Sommerfeld enhancement of the annihilation in the galaxy plays an important role. The model is shown to be consistent with LHC constraints on extra scalars mixing with the Higgs boson.

## II. PREDICTED SIGNAL

The photon flux (GeV/cm²/s/str) from annihilation \( \chi\chi \to \phi\phi \) of Majorana dark matter (DM) particles into two light mediators, in a given region around the GC, can be expressed as

\[
E_\gamma^2 \frac{dN_{\gamma}^{\text{th}}}{dE_\gamma} = \frac{1}{2} \frac{\langle \sigma v \rangle}{4\pi m_\gamma^2} \sum_f \text{BR}_{\phi \to f} \frac{dN_f^\gamma}{dE_\gamma}
\]

where \( \langle \sigma v \rangle \) is the averaged cross section for DM annihilation into two mediators, \( \text{BR}_{\phi \to f} \) is the branching ratio for decays of the mediator \( \phi \) into \( f \bar{f} \) final states, and \( J \) is the averaged \( J \) factor for the region of interest (ROI),

\[
J = \int_{\text{ROI}} d\Omega I(l, b) = \int_{\text{ROI}} \cos(b) d\Omega dE \int_0^\infty dx \left( \sqrt{x^2 + R_\odot^2 - 2 x R_\odot \cos(\ell)} \cos(b) \right) dx^2
\]

\[
\int_{\text{ROI}} \cos(b) d\Omega dE
\]

and \( dN_f^\gamma/dE_\gamma \) is the photon spectrum from a single DM annihilation into \( f \bar{f} \) final states, described below. For Dirac DM, one should replace the prefactor \( 1/2 \to 1/4 \) in Eq. (1), resulting in a cross section that is twice as large as that for Majorana DM, for a fixed observed flux.\(^1\) Unless otherwise stated we will assume Majorana DM in the following. The \( J \) factor depends upon the assumed shape of the DM density profile, which is commonly taken to be of the generalized Navarro-Frenk-White (NFW) type,

\[
\rho(r) = \rho_s \left( \frac{r}{r_s} \right)^{-\gamma} \left( 1 + \frac{r}{r_s} \right)^{3-\gamma}
\]

\(^1\)This assumes that the dark matter is symmetric (equal parts of matter and antimatter) even though it could in principle have an asymmetry in this case.

\[
\frac{dN_f^\gamma}{dE_\gamma} = \frac{2}{(x_+ - x_-)} \int_{x_-}^{E_{x+}} E_\gamma' dE_\gamma' dN_0^f
\]

where \( dN_0^f/dE_\gamma \) is the photon spectrum from \( \phi \to f \bar{f} \) in the rest frame of \( \phi \) and \( x_\pm = m_\gamma/m_\phi \pm \sqrt{(m_\gamma/m_\phi)^2 - 1} \). For most final states, a Monte Carlo generator is needed to
predict the distribution of photons from hadronization and decays. We take the spectra \( dN_0/dE \) from PPCP (Ref. [86]), which is valid for mediator masses down to 10 GeV. For lighter mediators, extrapolation of the PPCP results would be required, introducing inaccuracies into the predictions. However our subsequent fits will dictate the need only for lighter mediators decaying into muons, for which we use an analytic expression for \( dN_0/dE \), [87], given in Appendix B. The factor of 2 in (4) accounts for the two mediators produced in the annihilation.

We ignore the contribution \( \chi\chi \rightarrow f\bar{f} \) from s-channel exchange of a single off-shell mediator, whose cross section is approximately

\[
\langle\sigma v\rangle \cong \frac{y_f^2 \theta^2 g^2}{32\pi m_f^2}
\]

Here \( y_f \) is the Yukawa coupling of the fermion, \( m_f/v \) (with \( v = 246 \) GeV), \( \theta \) is the mixing angle of the mediator to the Higgs, and \( g \) is the dark matter-mediator coupling. Later we will note that \( g\theta \lesssim 2 \times 10^{-3} \) from direct detection constraints, while \( m_f \sim 100 \) GeV and \( m_f \sim 5 \) GeV for the heaviest quark of interest in our study, leading to \( \langle\sigma v\rangle \sim 10^{-3}\) cm\(^3\)/s, some nine orders of magnitude below the relevant values for the relic density or the Galactic Center excess.

### III. DATA SETS

We consider three data sets for the GC excess: those of CCW [6], Fermi [83], and Daylan et al. [4]. Detailed descriptions follow; the data are summarized in Fig. 1. We further include the AMS-02 measurement of the spectrum of cosmic ray electrons/positrons, and antiproton ratio data from the BESS, CAPRICE and PAMELA experiments. The antiproton data is not included in our overall \( \chi^2 \) function; rather we will verify after fitting the data that our models are compatible with the antiproton constraints.

#### A. CCW spectrum

The CCW spectrum (Ref. [6]) is downloadable from [88], where a covariance matrix \( \Sigma \) for computing the \( \chi^2 \) for fits to the data is also provided. Then

\[
\chi^2 = \sum_{ij}^{24} \left( E_i \frac{dN^{th}}{dE}(E_i) - E_i \frac{dN^{exp}}{dE}(E_i) \right) (\Sigma^{-1})_{ij} \left( E_j \frac{dN^{th}}{dE}(E_j) - E_j \frac{dN^{exp}}{dE}(E_j) \right)
\]

where the sum is over 24 energy bins, and \((\Sigma^{-1})_{ij}\) are the matrix elements of the inverse of the covariance matrix, obtained from columns 29-52 of the data file from [88]. This accounts for the correlations between the different energy bins.

The ROI for CCW is a \( \pm 20^\circ \) square around the GC; in galactic coordinates, where \( \ell \) is the longitude and \( b \) is the latitude, the region is

\[
|\ell| < 20^\circ \quad \text{and} \quad 2^\circ < |b| < 20^\circ
\]

where the \( \pm 2^\circ \) region in latitude is masked out to remove the galactic disk.

With these inputs and \( \gamma = 1.2 \) for the generalized NFW distribution, the \( J \) factor in (1) is \( J = 2.062 \times 10^{23} \) GeV\(^{-2}\) cm\(^{-5}\) for the CCW data. (This number agrees with [52].)

#### B. Fermi spectrum

The Fermi collaboration has not officially released its data, but we have digitized it from the presentation in Ref. [83], and list the results in Table III, Appendix A. Fluxes are given in 20 energy bins, equally spaced in \( \log_{10}(E) \) between 1 MeV and 89 GeV. We estimate the statistical errors from taking \( \sqrt{N} \) for the number of total events in each bin and applying this to the part of the signal interpreted as the excess. Reference [83] gives two characterizations of the spectrum of excess events, one which is presumed to be a power law in energy with an exponential cutoff, and the other being a separate fit to the excess in each bin. We adopt the latter for our analysis.

In addition to the statistical errors, there is systematic uncertainty associated with assumptions about the templates for background photons from pulsars and OB stars. We define the signal as the median between the upper and lower envelopes found from varying these templates, and the systematic error as the difference. This is added in quadrature with the statistical error to estimate the total uncertainty. The result is plotted in Fig. 2, showing that

![Fig. 1](color online). The three data sets for the GC gamma ray excess. The Fermi flux presented is the total flux from the \( 15^\circ \times 15^\circ \) square around the GC; the other two fluxes are normalized accordingly with the same DM profile. Error bars for CCW are taken from the diagonal components of their covariance matrix. Solid curves are the predictions of the best-fit models described in Sec. IV.
errors are systematics-dominated at low energy, but mostly statistical at high energy. The $\chi^2$ function is then defined in the usual way.

The ROI for the Fermi data is a $15^\circ \times 15^\circ$ square around the GC. Numerically integrating (2) we obtain $J = 1.07 \times 10^{23}$ GeV$^2$/cm$^5$, again assuming generalized NFW parameter $\gamma = 1.2$ and $\rho_\odot = 0.4$ GeV/cm$^3$. Here we do not average over the solid angle (giving $J$ instead of $\bar{J}$) because the Fermi data are reported as a total flux rather than an intensity flux.

**C. Daylan et al. spectrum**

Although our primary purpose is to explore the implications of the first two data sets which are more recent, for completeness we also apply our methodology to the GC excess spectrum determined in Ref. [4]. It can be read from Fig. 5 of that paper, from which it is straightforward to define $\chi^2$ for a given predicted flux. The spectrum shown there has been normalized to correspond to an $J$ factor that is not averaged over any solid angle, but instead is defined along a line of sight $5^\circ$ away from the GC. For $\gamma = 1.2$, we thus find $J = 9.09 \times 10^{23}$ GeV$^2$/cm$^5$ (again using $\rho_\odot = 0.4$ GeV/cm$^3$).

**D. AMS positron/electron spectrum**

AMS-02 published their recent results on the measurement of the $e^+/e^-$ ratio and the separate electron and positron fluxes in [84,85], confirming a positron excess above the expectations from standard cosmic ray propagation scenarios that was previously seen by PAMELA and Fermi. The more precise measurements of AMS-02 do not tell us whether the excess of the positron flux originates from dark matter or pulsars, but the smooth spectrum up to $O(100)$ GeV already puts strong constraints on dark matter models [79,89–92]. If light dark matter annihilates directly into $e^+e^-$, even though the spectrum is initially a delta function of energy, after propagation it leads to bump-like feature in the observed spectra. The feature is more spread out in models with decays into mediators, $\chi\chi \rightarrow \phi\phi \rightarrow 4e$, where the initial spectrum is box-like; nevertheless the final shape is still localized in energy and can be strongly constrained. The differences in shape of the electron spectra for relevant final states are illustrated in Fig. 3.

To simplify our analysis and to make the results more model-independent, we assume that only dark matter annihilating into $e^+e^-$ or $2e^+2e^-$ can be constrained by current AMS-02 data, since these have harder and more localized spectra compared to other channels. The latter also generate positrons and electrons, but they come from three- or four-body final states, which make the spectrum much softer and more broad. It would be easy to absorb such nondistinctive contributions into the smooth background. Following [79], we use polynomial functions to fit the logarithm of AMS spectra as the background. To obtain the electron/positron flux from light dark matter, a cosmic ray propagation model is chosen with a relatively large magnetic field, in order to achieve conservative bounds, since the energy loss is essentially due to the magnetic field and will soften the spectra.

Before including the light dark matter contribution, the absolute $\chi^2$ of the background to fit against the AMS positron ratio data is $\chi^2 = 35.06$. This value does not depend on assumptions about the propagation model or solar modulations since we use fitting functions, rather than considering specific propagation models. However for the dark matter signal, the propagation and solar modulation uncertainties have to be considered. We marginalize over the range of the effective potential of solar modulation, $[0, 1 \text{ GV}]$ and a relatively large magnetic field is chosen to propagate

---

2The background may include contributions from primary and secondary electrons, secondary positrons, pulsars, or heavy dark matter annihilation/decay. All of them could contribute to the smooth spectra observed by AMS-02.
the cross section for dark matter annihilation to hadronic final states, modulo the uncertainties from cosmic ray propagation. Following [93], we use antiproton ratio data from the BESS [94,95], CAPRICE [96] and PAMELA [97] experiments. In order to minimize the systematic uncertainties from different experiments, the antiproton ratio data are employed here, rather than the antiproton flux data. Parameters governing cosmic ray propagation are constrained by fitting to the observed ratio of boron to carbon, but this still leaves some freedom to vary parameters, as well as the solar modulation; this leads to a range of estimates for the astrophysical background of proton and antiproton fluxes, that are consistent with the observed fluxes from the above data sets. Once the propagation model, the solar modulation and the astrophysical background are fixed, we can perform a χ² fit of the ¯p/p data by adding the contribution from the dark matter annihilation.

Two benchmark propagation models are used here to cover the systematic uncertainties of the cosmic ray propagation: KRA and THN, in the notation of Ref. [98], where the main difference of the two models is the halo height, with z₀ = 4 kpc for KRA, and z₀ = 0.5 kpc for THN. The other parameters are the slope of the diffusion coefficient ν = 0.5, nuclei spectral index γ = 2.35, the normalization of the diffusion coefficient D₀ = 2.68 × 10²⁸ cm² s⁻¹, and the solar modulation potential Φ = 0.95 GV for the KRA model. For THN these take the same values except for D₀ = 0.32 × 10²⁸ cm² s⁻¹. Neither of these models consider convection. Further details can be found in [93].

The resulting antiproton constraints on DM annihilating to bbbb with two different ratios of mediator mass to DM mass are shown in Fig. 5. The dependence on propagation model is the largest uncertainty, with THN (dashed lines) giving a factor of 10 weaker constraints than KRA (solid lines), while the dependence on the mediator mass is relatively weak (red versus blue curves). We adopt the more conservative bounds from the THN model in our analysis. It will turn out that in our preferred models with a subdominant branching fraction to b quarks, the antiproton limit is not significantly constraining (see Fig. 9 below).

Better measurements of heavy nuclei abundances from AMS-02, in particular the boron/carbon ratio, may improve our understanding of cosmic ray propagation models, hopefully leading to a decrease in the systematic uncertainty from the propagation models. Moreover a much more precise measurement of antiproton data itself is expected to improve this limit by a factor of two or three. Considering both effects, we anticipate that coming AMS-02 data may shed further light on which DM models can consistently explain the GC excess.

IV. FITS WITH A SINGLE MEDIATOR

Our initial motivation was to reexamine the viability of kinetically mixed Z' models for the GC excess in light of...
the new data sets from CCW and Fermi. Although a good fit to the GC excess can be obtained, these models necessarily have a significant branching fraction into electrons. We found that the combined fit to the GC excess and AMS electron data was quite poor. This suggests doing a model-blind search for different combinations of final state fermions that could give a good fit to all data. We performed this in the 8-parameter space of models characterized by the DM and mediator masses $m_\chi$, $m_\phi$, and branching fractions $f_i$ for annihilation into final states $i = e, \mu, \tau, q, c, b$, where $q$ denotes light quarks, whose spectra are all provided by PPPC [86]. These fractions are subject to the constraint $\sum f_i = 1$, where we ignore invisible channels since this degree of freedom would be degenerate with the overall cross section $\langle \sigma v \rangle$, which makes the 8th parameter.

The result of this search is that $f_e$ must be negligible as a result of the AMS constraint. Therefore for more refined searches we set $f_e = 0$ and remove the AMS contribution from the total $\chi^2$. We find that the CCW and Fermi GC spectra further disfavor any significant contribution from $\tau$, $q$ or $c$, preferring an admixture of muons and $b$ quarks. We sample models with $\chi^2$ near the minimum value using a Markov Chain Monte Carlo (MCMC) search as well as Multinest [99]; this prevents getting stuck in spurious local minima of the $\chi^2$ function. In this way we find a large spread in allowed masses $m_\chi$ and $m_\phi$ as shown in Fig. 6. The best fit values of parameters for the three data sets are listed in Table I.

However the nominal best-fit values should not be given too much importance, because there are quasi-degeneracies in the $\chi^2$ functions that allow for good fits to the data over a
range of parameters for the Fermi and CCW data sets. These are illustrated in Fig. 7. We see that $m_\chi$ can vary in the range $40–100$ GeV keeping $\Delta \chi^2 \lesssim 2$ for the CCW fits. Similarly the Fermi data are compatible with $m_\chi$ in the range $80–180$ GeV. Both data sets are compatible with annihilations into $\mu\bar{\mu}$ and $b\bar{b}$, with the former being dominant. The corresponding results for the Daylan et al. spectrum are qualitatively different, both for the lower range of $m_\chi$ and the final states, which prefer $\mu$, $q$ or $b$ depending upon $m_\chi$. A range of larger masses $m_\chi \sim 55–70$ GeV is however still reasonable with $\Delta \chi^2 \sim 6$. This provides overlap with the preferred regions of the other data sets.

The required values of the annihilation cross section $\langle \sigma v \rangle$ needed to fit the magnitude of the excess are illustrated in Fig. 7 (bottom right). The 1-2σ favored regions in the $m_\chi$-$\langle \sigma v \rangle$ plane are somewhat disjoint between the three data sets. We show for comparison estimated limits on annihilation to $80\% \mu\mu + 20\% bb$ from Fermi observations of satellite galaxies of the Milky Way [100], with an interpolation to the case of interest for us of $f_\mu \sim 0.8$, $f_b \sim 0.2$ using $\langle \sigma v \rangle^{-1} \cong f_\mu \langle \sigma_{\mu\mu} v \rangle^{-1} + f_b \langle \sigma_{bb} v \rangle^{-1}$. Here the $\sigma$’s refer to the limiting values. This is a rough estimate of the expected limit on our best-fit models to the CCW and Fermi GC excess data, which is seen to be still consistent with most of the preferred parameter space. Also plotted is our estimate of the limit on $\langle \sigma v \rangle$ from Fermi’s Pass 8 data [101], which is lower than that of Ref. [100] by a factor of 5. These results indicate some tension between the dwarf limits and the GC excess signal. This can be relieved somewhat, still consistently with our fits, by reducing the fraction $f_b$ so that the signal is more $\mu$-like. Figure 7 (bottom right) shows that the constraints into pure $\mu$ final states are significantly weaker.

Since the allowed ranges for $m_\chi$ include values greater than $m_W$ and $m_Z$, we have also performed Monte Carlo

<table>
<thead>
<tr>
<th>Data set</th>
<th>$m_\chi$ (GeV)</th>
<th>$m_\phi$ (GeV)</th>
<th>$f_\mu$</th>
<th>$f_b$</th>
<th>$f_\tau$</th>
<th>$f_q$</th>
<th>$\langle \sigma v \rangle$ (cm$^3$/s)</th>
<th>$\chi^2_{\min}$</th>
<th>DOF</th>
</tr>
</thead>
<tbody>
<tr>
<td>CCW</td>
<td>12.3</td>
<td>46</td>
<td>0.82</td>
<td>0</td>
<td>0.02</td>
<td>0.16</td>
<td>118.8</td>
<td>24</td>
<td></td>
</tr>
<tr>
<td>Fermi</td>
<td>130</td>
<td>114.5</td>
<td>0.80</td>
<td>0</td>
<td>0</td>
<td>0.20</td>
<td>6.4</td>
<td>20</td>
<td></td>
</tr>
<tr>
<td>Ref. [4]</td>
<td>14.6</td>
<td>4.0</td>
<td>0.49</td>
<td>0.01</td>
<td>0.06</td>
<td>0.44</td>
<td>72.9</td>
<td>25</td>
<td></td>
</tr>
</tbody>
</table>
TABLE II. Best fit parameters for single-mediator model fits to the three data sets, allowing for 100% branching to \( \mu \) final states (left) or \( b \) (right). Masses are in GeV units, \( \langle \sigma v \rangle \) in units of \( 10^{-25} \text{ cm}^3/\text{s} \).

<table>
<thead>
<tr>
<th>Data set</th>
<th>( m_\chi )</th>
<th>( m_\phi )</th>
<th>( \chi^2_{\text{min}} )</th>
<th>Data set</th>
<th>( m_\chi )</th>
<th>( m_\phi )</th>
<th>( \langle \sigma v \rangle )</th>
<th>( \chi^2_{\text{min}} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>CCW (( \mu ))</td>
<td>8.5</td>
<td>1</td>
<td>37</td>
<td>CCW (( b ))</td>
<td>75</td>
<td>37</td>
<td>0.6</td>
<td>23.6</td>
</tr>
<tr>
<td>Fermi (( \mu ))</td>
<td>14</td>
<td>1</td>
<td>42</td>
<td>Fermi (( b ))</td>
<td>153</td>
<td>102</td>
<td>1.5</td>
<td>20.5</td>
</tr>
<tr>
<td>Ref. [4] (( \mu ))</td>
<td>7.5</td>
<td>1</td>
<td>51</td>
<td>Ref. [4] (( b ))</td>
<td>51</td>
<td>25</td>
<td>0.4</td>
<td>27.5</td>
</tr>
</tbody>
</table>

One may wonder whether the preference for an admixture of \( \mu \) and \( b \) final states is statistically significant compared to 100% branching to either \( \mu \) or \( b \). We have scanned over \( m_\chi \) and \( m_\phi \) for these cases to compare with the previous results for admixtures of final states. The best-fit parameters and minimum values of \( \chi^2 \) are given in Table II, to be compared to the results of Table I. Annihilations to \( \mu \) only give poor fits to all data sets, while those to \( b \) do better. Nevertheless, the improvement from allowing an admixture of \( \mu \) and \( b \) is statistically significant.

Physically, the preference for two final states arises because the spectrum from any one of them falls with energy as a power law times an exponential cutoff. Especially for the Fermi data (see Fig. 1), the observed spectrum does not have this form but instead remains high to large energies, just before abruptly cutting off. The superposition of final state spectra from \( \mu \) and \( b \) is able to reproduce this shape much better than that from \( b \) alone.

FIG. 8 (color online). Left: best fits as a function of \( m_\chi \) to the CCW data, as in Fig. 7, but for two-mediator model. Masses \( m_\phi \) are in GeV units. Solid lines have \( m_\phi \) freely varying, while dotted ones restrict \( m_\phi = 3 \) GeV. Right: same for Fermi data.

V. FITS WITH TWO MEDIATORS; SOMMERFELD ENHANCEMENT

The previous analysis shows that annihilation to a mixture of \( b \) and \( \mu \) final states gives the best fits to Fermi and CCW data. From a model-building point of view, it may seem ad-hoc to couple the mediator to the standard model fermions in this way. If the mediator is a singlet that mixes with the Higgs, the couplings are proportional to the masses of the fermions. With two such mediators however, the desired mixture of final states could be a natural consequence of the masses \( m_\phi \) and \( m_\phi' \), only requiring that \( m_\phi < 2m_\tau \) and \( 2m_\mu < m_\phi < m_\tau \), so that decays into disfavored channels are kinematically forbidden, or suppressed by small Yukawa couplings. Motivated by this theoretical consideration and the previous results, we thus reconsider the data in the model with five parameters

\[
\{m_\chi, m_\phi, m_\phi', f_\mu/f_\mu, \langle \sigma v \rangle\}
\]

This is one fewer parameter than in the single-mediator models, where we had two additional final states.

Interestingly, the fits to Fermi and CCW data, in which \( m_\phi' \) is free to vary, are consistent with values that are not far from the theoretical threshold \( 2m_\tau \). In Fig. 8 we plot best-fit parameters that are at least local minima of \( \chi^2 \), demonstrating this assertion. \( \chi^2 \) is sufficiently flat as a function of \( m_\phi \), that the models remain good fits even when \( m_\phi \) is restricted to stay below \( 2m_\tau \), as is also shown in the figure. Monte Carlo searches of the parameter space reveal slightly better fits (\( \delta\chi^2 \sim 0.1-0.2 \)) with higher \( m_\phi \), but these do not contradict the goodness of fit of the models with \( m_\phi < 2m_\tau \).

Using MCMC to explore parameters in the model with \( m_\phi \) fixed at 3 GeV, we find that the branching fraction to muons, \( f_\mu \), is concentrated near 0.9 for fits to Fermi, while having a broader distribution in CCW. This is shown in Fig. 9 (left). The best-fit values of the annihilation cross
section $\langle \sigma v \rangle$ are shifted upwards by a factor of a few in these models relative to the single-mediator model, as can be seen from Fig. 9 (right) in comparison to Fig. 7 (bottom right). Here we also show constraints on annihilations from Fermi dwarf observations (see discussion of Fig. 7), and from our analysis of antiproton constraints, for the representative case of 20% branching fraction to $b$ quarks, except for the latest Pass 8 constraint, where we use 10% to $b$ quarks. There is strong tension between this limit and the preferred region for the GC excess of the Fermi data, while some compatibility with the CCW data remains. The antiproton limit on the cross section is relaxed by a factor of 5 compared to the limit for annihilations purely into $b\bar{b}$ shown in Fig. 5. The cross sections needed for the GeV excess are still comfortably below this limit (and more so in the single-mediator model where the target value of the cross section is lower).

A. Sommerfeld enhanced annihilation

The fact that these cross sections are significantly higher than the nominal value $\langle \sigma v \rangle_0 \equiv 3 \times 10^{-26} \text{ cm}^3/\text{s}$, needed for approximately the right relic density, is potentially a cause for concern. Such large cross sections would significantly suppress the density of $\chi$, in contradiction to our assumptions. However the presence of the light mediator $\phi_1$ provides a possibility for resolving this problem, due to the low velocities of DM in the galaxy relative to the early universe, and the resulting nonperturbative Sommerfeld enhancement of the cross section by multiple exchanges of $\phi_1$.

Let us suppose that $\phi_1$ couples to $\chi$ with strength $g_1$ and define $\alpha_1 \equiv g_1^2/4\pi$. (Later we will see that both scalar $g_1$ and pseudoscalar $g_{1,5}$ couplings are needed to get $s$-wave annihilation, but that $g_{1,5} \ll g_1$.) The Sommerfeld enhancement $S$ is controlled by the two small parameters [102]

$$e_\phi = \frac{m_{\phi_1}}{\alpha_1 m_\chi}, \quad e_v = \frac{v}{\alpha_1};$$

A good approximation to $S$ is given by the expression [103,104]

FIG. 9 (color online). Left: distribution of branching fraction to muons for two-mediator model, with $m_{\phi_1}$ fixed at 3 GeV. Right: corresponding distributions of $\langle \sigma v \rangle$ versus $m_\chi$, with Fermi dwarf galaxy constraints overlaid, as well as our constraint from antiprotons and that from the CMB.

FIG. 10 (color online). Left: example of Sommerfeld enhancement factor as a function of coupling $\alpha_1 = g_1^2/4\pi$ of light mediator $\phi_1$ to dark matter, with $m_\chi = 100$ GeV and $m_{\phi_1} = 3$ GeV. Typical required value of $S = 30$ is shown by the horizontal line, for reference. Right: scatter plot of required values of $S$ versus minimum value of $\alpha_1$ corresponding to sample of models in Fig. 9.
\[
S = \frac{\sinh X}{\cosh X - \cos \left(\frac{2\pi}{\xi_\phi} - X^2\right)},
\]

where \(\xi_\phi = (\pi/12)e_\phi\) and \(X = e_\phi/\xi_\phi\). (The cosine becomes cosh if the square root becomes imaginary.)

To quantify the magnitude of Sommerfeld enhancement needed, and the corresponding coupling strengths \(\alpha_1\), for each model in our MCMC chains we estimate the needed value of \(S\) as the actual cross section \(\langle \sigma v \rangle\) divided by the nominal relic density value \(\langle \sigma v \rangle_0\), assuming that \(v = 10^3\). Typically there are several coupling strengths that can yield the required value of \(S\) due to resonances, illustrated in Fig. 10 (left). Scanning over \(\alpha_1\), we find the minimum value of the coupling needed to get the required enhancement. The distributions of \(S\) versus \(\alpha_1\) for fitting the Fermi and CCW data are shown in Fig. 10 (right). It is noteworthy that we can get the right amount of enhancement by invoking reasonably small values of the couplings, with \(0.01 \lesssim \alpha_1 \lesssim 0.06\).

VI. PARTICLE PHYSICS MODELS

To further explore the implications of dark matter with two scalar mediators, such as from the thermal relic density requirement and direct detection constraints, we need to more fully specify the interactions. We will allow for parity-breaking in the dark sector, with both scalar and pseudo-scalar couplings

\[
\mathcal{L}_{\text{int}} = \sum_{i=1}^2 \lambda_i \phi_i (g_i + i g_i S y_j) \chi. \tag{10}
\]

This choice is meaningful if the DM mass \(m_\chi\) is restricted to be real; otherwise \(g_i, S\) can be rotated away by a chiral redefinition \(\chi \rightarrow e^{iy_j S} \chi\). The ansatz (10) is motivated by the fact that the cross section for \(\chi \chi \rightarrow \phi_i \phi_j\) is \(p\)-wave suppressed unless both types of couplings are present. For simplicity we take both mediators to be real fields.

However, both scalars are required to get vacuum expectation values (VEVs) in order to mix with the SM Higgs and hence couple to SM fermions, so in fact Eq. (10) would lead to a complex \(m_\chi\) once the VEVs are taken into account, and we would have to redefine the fields to make it real. Instead we will regard (10) as describing the low-energy effective theory where this has already been carried out.

The other important parameters of the model are the mixing angles \(\theta_i\) between the mediators and the SM Higgs.

These are determined by cross-couplings \(\frac{1}{2} \lambda_i \phi_i^2 |H|^2\) and VEVs,

\[
2\theta_i \approx \frac{\lambda_i \langle \phi_i \rangle v}{m_h - m_{\phi_i}^2}. \tag{11}
\]

Taking \(m_{\phi_i} \sim m_\chi \sim 100\) GeV, the second term is of order \(-1\) GeV\(^2\), similar in size to \(m_\chi^2\) (we have assumed \(m_1 = 3\) GeV for our benchmark models). Therefore no extraordinary fine tuning seems to be required in our model to keep \(m_{\phi_i}\) small (of course we ignored here the Planck-scale hierarchy problem and took the heaviest threshold in the hidden sector for the estimate of the loop contribution). An accidental cancellation between the terms in (13) could even help to explain the smallness of \(m_1\).

VII. RELIC DENSITY

The relic density of \(\chi\) is determined by \(\chi \chi \rightarrow \phi_i \phi_j\) summed over all possible final states. At kinematic threshold we find that

\[
\sigma v_{\text{th}} \approx \sum_{i=1,2} \frac{g_i^2 g_j^2 |m_\chi| \sqrt{m_{\phi_i}^2 - m_\chi^2}}{8\pi (m_{\phi_i}^2 - m_\chi^2/2)^2} + \frac{f^2}{16\pi (m_{\phi_i}^2 - m_\chi^2/4)} \tag{14}
\]
The magnitude of sufficient Sommerfeld enhancement gives a third, fixing we get two constraints on the couplings. The requirement gives the required ratio of achieving the observed relic density, and also that

$$g_1 = \frac{m_2^2}{4m^2}.$$  \hspace{1cm} (15)

The couplings are constrained by the fits to the GC excess indicating that the number of muons to $b$ quarks produced in the annihilations is given by

$$\frac{N(\mu)}{N(b)} = \frac{N(\phi_1)}{N(\phi_2)} \sim \frac{(g_1g_1 \pm F^2/4)}{(g_2g_2 \pm F^2/4)}.$$  \hspace{1cm} (16)

For simplicity we here omitted the dependence upon $m_2^2/m^2$ implied by Eq. (14), but the more exact expression is given in Appendix C [Eq. (C2)].

By demanding that $\langle \sigma v \rangle$ matches the canonical cross section $\langle \sigma v \rangle_0 = 3 \times 10^{-26}$ cm$^3$/s for approximately achieving the observed relic density, and also that (C2) gives the required ratio of $\mu/b$ for a given model realization, we get two constraints on the couplings. The requirement of sufficient Sommerfeld enhancement gives a third, fixing the magnitude of $g_1$. We can take the value of $F$ in (15) as a free parameter that can be varied to explore the range of possible solutions for $g_1, g_{1.5}$ characterizing viable models. Details of the algebraic solution for the couplings are given in Appendix C.

We have carried out the above procedure for the models in our Monte Carlo searches that give good fits to the GC GeV excess, to find the ranges of allowed values for the couplings. Scatter plots of $g_{1.5}, g_2, g_{2.5}$ versus $g_1$ are shown in Fig. 11 for fits to the Fermi and CCW data sets, within the $2\sigma$-allowed regions. Here we have assumed solutions for $g_1$ that give the smallest values of the couplings (since a quadratic equation must be solved leading to a second branch of solutions with larger values). Interestingly, the parity-conserving couplings turn out to be the largest, with $g_1 \sim g_2 \sim (0.5–0.8)$, while the parity-violating couplings are suppressed, with $g_{1.5} \sim (0.02–0.1)$ and $g_{2.5}$ being smaller. The exact range of $g_{2.5}$ (which we take to be negative, see Appendix C) is the least constrained of all the couplings, with $g_{2.5} = 0$ always being a possibility (corresponding to $F = F_{\text{max}}$), since we have freedom to impose this as an extra condition while satisfying the remaining physical constraints. But in no case can $|g_{2.5}|$ be large while maintaining that $\mu$ final states dominate over $b$ for the GeV excess spectral shape.

**VIII. DIRECT DETECTION**

The cross section for scattering on nucleons (with mass $m_p$) is dominated by exchange of the light $\phi_1$ mediator,

$$\sigma_p \approx \frac{(g_2^2 + g_{1.5}^2)(\theta_1 y m_p)^2}{\pi m_{\phi_1}^4}$$  \hspace{1cm} (17)

in the limit that $m_p \gg m_\chi$. Defining $\tilde{g}_1 = (g_2^2 + g_{1.5}^2)^{1/2}$, direct detection limits put an upper bound on $\theta_1 \tilde{g}_1$ that

![FIG. 11 (color online). 2$\sigma$-allowed values of mediator couplings to DM for fits to CCW (left) and Fermi (right) data sets. Regions differ depending upon the choice a one free combination of couplings which we take to be $F$ [Eq. (15)], which we illustrate for $F = 0$ and $F = 0.9F_{\text{max}}$ [see Eq. (C4)].](image1)

![FIG. 12 (color online). Upper limit on DM coupling times mixing angle of the light mediator $\phi_1$ from LUX [106] direct search.](image2)
depends upon $m_\chi$ as shown in Fig. 12 for fixed $m_{\phi_1} = 3$ GeV. Here $y$ is the Higgs-nucleon coupling, which we take to be $y = 1.3 \times 10^{-5}$ (see Ref. [105] for a recent review). For $m_\chi \sim 100$ GeV as suggested by our fits to the GC excess, this gives $\tilde{g}_1 \theta_1 < 2 \times 10^{-5}$. On the other hand the Sommerfeld enhancement determined in Sec. VA demands that $\tilde{g}_1 \sim 0.6$, so $\theta_1 \lesssim 3 \times 10^{-5}$. Equation (11) then implies $\lambda_1 (\phi_1) < 4 \times 10^{-3}$ GeV. We can eliminate the singlet VEV using its relation to the $\phi_1$ mass and self-coupling $\lambda_1$ by $m_{\phi_1} = \sqrt{2} \lambda_1 (\phi_1)$. Taking $m_{\phi_1} = 3$ GeV, we see that the direct detection constraint implies a hierarchy between the scalar quartic couplings,

$$\frac{\lambda_1}{\lambda_1^{1/2}} < 2 \times 10^{-3}. \quad (18)$$

This is not technically unnatural since the coupling $\lambda_1$ only receives multiplicative renormalizations.

**IX. COSMOLOGICAL CONSTRAINTS**

We consider here the impact of cosmic microwave background constraints, and those coming from scattering of dark matter on itself in this section. We will show that the models treated in this work are compatible with current data, but are close to the limits, with interesting potential to address puzzles in the small scale structure of galaxies predicted by noninteracting cold dark matter.

**A. Cosmic microwave background**

Dark matter annihilations into charged particles during the epoch of reionization can impact the temperature and polarization fluctuations of the cosmic microwave background (CMB) [107–112], leading to constraints on the annihilation cross section that are particularly strong for low DM masses, scaling linearly with $m_\chi$. At this late era, the DM velocity is already sufficiently low that the magnitude of Sommerfeld enhancement occurring in collisions at the Galactic Center will be operative also for the CMB. Therefore we can directly compare the cross sections needed for the GC excess to the CMB limits.

The CMB limits are dependent upon the efficiency $f_{\text{eff}}$ for given final state particles to deposit electromagnetic energy in the plasma. The latest upper limit on the annihilation cross section using Planck temperature and polarization data can be expressed as

$$f_{\text{eff}} (\sigma v) < 4 \times 10^{-26} \left( \frac{m_\chi}{100 \text{ GeV}} \right) \text{cm}^3/\text{s} \quad (19)$$

which we infer from Fig. 41 of Ref. [113]. Reference [110] gives $f_{\text{eff}} = 0.25 (0.33)$ for $\mu (b)$ final states at $m_\chi = 100$ GeV, which we average to $f_{\text{eff}} = 0.27$ for our benchmark two-mediator model with 80% $\mu + 20% b$ final states, to give $\langle \sigma v \rangle < 1.5 \times 10^{-25} (m_\chi/100 \text{ GeV})$ cm$^3$/s.

This is plotted on Fig. 9 (short dash-dotted curve). It is a somewhat weaker constraint that the latest (Pass 8) limit from Fermi dwarf galaxy observations, but still excludes the preferred regions for the GeV excess fits to Fermi data with two-mediator models, while remaining marginally compatible with the fits to the CCW data.

**B. Dark matter elastic self-interactions**

Self-interactions of dark matter can be significant in our two-mediator model, from $t$- and $u$-channel exchange of the lighter mediator. The viscosity cross section, relevant for effects of DM self-scattering on structure formation, is

$$\sigma_v = \int d\Omega (1 - \cos^2 \theta) \frac{da}{d\Omega} = \frac{2 \alpha_1^2 m_\chi^2}{3 \pi m_\phi^4}. \quad (20)$$

Taking the typical values $g_1 \sim 0.6$, $m_{\phi_1} = 3$ GeV, $m_\chi = 100$ GeV, indicated by our fits, this leads to a cross section per DM mass of order $\sigma_v / m_\chi \sim 10^{-5}$ b/GeV, far below the bound $\sim 0.5$ b/GeV from simulations of structure formation including DM self-interactions [114]. However, there is freedom in our model to take $m_{\phi_1}$ as small as 2 $m_\chi = 0.2$ GeV, if we adjust $\alpha_1$ to somewhat smaller values $\sim 0.01$ to compensate for the increased boost from Sommerfeld enhancement in the Galactic Center.

The self-interaction cross section in such models can have nonperturbative enhancements in analogy to the Sommerfeld effect, which have been studied in detail in Refs. [115,116]. For $\alpha_1 = 0.01$, the latter reference finds that $\sigma_v / m_\chi$ is at the right level to address problems of collisionless cold dark matter for predicting the observed galactic small scale structure, if $m_\chi \sim 165 m_{\phi_1}$ in the region $m_{\phi_1} = 0.2$–2 GeV, which overlaps with values needed for explaining the GC excess. These problems include the difficulty for collisionless cold dark matter to correctly predict abundances and maximum masses of dwarf satellite galaxies, as well as the cusp versus core issue for dwarf galaxy DM density profiles; see Ref. [117] for a review.

**X. COLLIDER CONSTRAINTS**

We also consider the collider limits on the particle physics model described in Sec. VI. In a model having additional scalars, which mix with the SM Higgs, one would expect possible limits resulting from the recent observation and measured signals of the Higgs boson at the LHC. Although we find the limits posed by direct detection and relic density results to be more constraining, we include here the collider considerations for completeness.

For the following analysis, we do not initially assume a small mixing angle approximation. We supplement the SM

---

For scattering of identical particles, this is more appropriate than weighting by $(1 - \cos \theta)$ since it treats scattering by $180^\circ$ as equivalent to forward scattering.
Higgs potential with two real, scalar, singlet fields. Both fields acquire vevs, thereby inducing mixing with the Higgs. The relevant parameters are then the masses of the three scalars, \( m_h, m_{\phi_1}, m_{\phi_2} \), and the two mixing angles, \( \theta_{1h}, \theta_{2h} \). Mixing between the field and mass eigenstates is given according to

\[
\begin{pmatrix}
\tilde{h} \\
\tilde{\phi}_1 \\
\tilde{\phi}_2
\end{pmatrix} =
\begin{pmatrix}
c_{\theta_{1h}} c_{\theta_{2h}} & s_{\theta_{1h}} & c_{\theta_{1h}} s_{\theta_{2h}} \\
-s_{\theta_{1h}} c_{\theta_{2h}} & c_{\theta_{1h}} & -s_{\theta_{1h}} s_{\theta_{2h}} \\
-s_{\theta_{2h}} & 0 & c_{\theta_{2h}}
\end{pmatrix}
\begin{pmatrix}
h \\
\phi_1 \\
\phi_2
\end{pmatrix} \tag{21}
\]

where \((c, s)\) denote \((\cos, \sin)\), respectively.

The scalar couplings to standard model particles are then simply the SM Higgs couplings, scaled by \( c_{\theta_{1h}}, c_{\theta_{2h}}, s_{\theta_{1h}}, c_{\theta_{1h}} s_{\theta_{2h}}, \) for \( h, \phi_1, \) and \( \phi_2 \), respectively. We take \( h \) to be the recently discovered Higgs boson, setting \( m_h = 125.6 \text{ GeV} \), and take \( \phi_1 \) to be the lighter scalar, such that \( m_{\phi_1} < m_{\phi_2} \). We determine the allowed values of the two mixing angles, using the publicly available code HIGGSBOUNDS 4.2.0

\[ m_{\phi_1} = 3 \text{ GeV}, m_{\phi_2} = 115 \text{ GeV} \]

where \( \theta_{1h} \) and \( \theta_{2h} \) are the two mixing angles, taking \( \theta_{1h} = 15^\circ \) and \( \theta_{2h} = 18^\circ \).

\[ m_h = 125.6 \text{ GeV} \]

The result is shown in Fig. 13. The upper figure shows the regions excluded by LEP and hadronic (Tevatron and LHC) exclusion Higgs searches, obtained by HIGGSBOUNDS, while the lower one shows the regions preferred by compatibility with the observed Higgs signal strengths. The set of experimental results and specific Higgs channels that we use for the Higgs signal limit, can be found in Refs. [121] and references therein.

\[ \Delta \chi^2(m) = \frac{4m^2_{\phi}}{32\pi m_h} \left( 1 - \frac{4m^2_{\phi_2}}{m^2_h} \right)^{1/2} \]

A recent CMS analysis [134] presents an upper limit on the Higgs total width, obtained from the ratio of measurements of off-shell and on-shell Higgs production and decay in the \( H \rightarrow ZZ \) channel. CMS finds \( \Gamma_h < 4.2\Gamma_h^\text{SM} \) with \( \Gamma_h^\text{SM} = 4.15 \text{ MeV} \). We find the upper limit on the cross coupling shown in Fig. 14.
XI. CONCLUSIONS

In this study we compared two new data sets, characterizing the excess gamma rays from the Galactic Center, to predictions from models where dark matter annihilates into light mediators that subsequently decay into standard model particles. In contrast to models with direct annihilation into heavy quarks, these are more easily compatible with direct detection and cosmic ray antiproton constraints, as we have demonstrated. In a first approach, general admixtures of final state particles yielded good fits, revealing a preference for the data to be described by decays mostly to muons (electrons being excluded by AMS-02 data) and $b$ quarks, with dark matter masses in the range 40–140 GeV. Either Majorana or Dirac dark matter are viable possibilities.

We then argued that this might be more naturally accomplished with two scalar mediators $\phi_1$ mixing with the Higgs, such that $\phi_1$ decays primarily to $\mu^+\mu^-$ and $\phi_2 \rightarrow b\bar{b}$, as a consequence of the mediator masses. Encouragingly, fits to the data in this two-mediator model were consistent with masses in the desired ranges $2m_{\chi} < m_{\phi_1} < 2m_{\mu}$, $2m_{\mu} < m_{\phi_2} < m_{\chi}$. Moreover quite reasonable perturbative values of the mediator couplings to $\chi$ give consistent results. To avoid $p$-wave suppression of the annihilation cross section we invoked parity violating couplings, which turn out to be somewhat smaller than the parity-conserving ones.

An interesting feature of these models is that the best-fit cross sections for annihilation in the Galactic Center are several times larger than the value needed for achieving the right thermal relic density. We showed that this can be consistent due to Sommerfeld enhanced annihilation in the galaxy, due to multiple exchanges of the lighter of the two mediators, taking $m_{\phi_1} = 3$ GeV as a benchmark model. It only requires that the scalar coupling of $\phi_1$ to $\chi$ be of order $g_1 \sim 0.5$. If the light mediator mass is somewhat lower, the cross section for elastic DM self-scattering can have the right magnitude for addressing the missing satellite and cusp-core problems from simulations of structure formation. Improved CMB constraints anticipated from Planck data may be in tension with the best-fit regions of parameter space.

LHC constraints on the couplings and mixing angles of the mediators are relatively weak compared to those from direct detection. The latter provides good prospects for independent confirmation of our model, requiring that the cross-coupling between $\phi_1$ and the Higgs boson be $\lesssim 10^{-3}$. No fine tuning in the technical sense is needed to satisfy this constraint, but neither is there any symmetry reason for the coupling to be small.

The allowed parameter space in $(\sigma v)$ versus $m_\chi$ shows some tension with the latest Fermi-LAT constraints on dark matter annihilation in dwarf spheroidals, especially for the fit to the Fermi GeV excess data. Planck constraints on distortions to the CMB are in tension at a similar level. The fit to the CCW excess is also challenged by these results, though to a lesser extent. More optimistically, as we were completing this work, preliminary evidence for a positive signal from the dwarf galaxy Reticulum II appeared [135], at a level consistent with expectations from the GC excess.

ACKNOWLEDGMENTS

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APPENDIX A: FERMI SPECTRUM

We list the Fermi spectrum in Table III.

**TABLE III.** Energy flux derived from Fermi collaboration’s presentation [83] for the Galactic Center gamma ray excess, and statistical along with systematic errors as described in Sec. III B. The flux intensity is obtained by averaging the observed total flux over the $15^\circ \times 15^\circ$ square around the GC. Flux units are GeV$^{-1}$ cm$^{-2}$ s$^{-1}$ sr$^{-1}$.

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MULTIMEDIATOR MODELS FOR THE GALACTIC CENTER ...

APPENDIX B: SPECTRUM FROM DECAY TO MUONS

For completeness, we present the photon spectrum from \( \phi \to \mu^+\mu^- \) in the rest frame of \( \phi \) [79,87]. It includes photons from final state radiation and from radiative decays. Final state radiation gives the contribution

\[
\frac{dN_{\text{FSR}}}{dx} = \frac{\alpha_{\text{em}}}{\pi} \frac{1 + (1-x)^2}{x} \left[ -1 + \ln \left( \frac{m_{\phi}^2(1-x)}{m_{\mu}^2} \right) \right], \tag{B1}
\]

where \( x = 2E_{\gamma}/m_\phi \). The contribution from radiative decay is

\[
\frac{dN_{\text{rad}}}{dx} = \frac{\alpha_{\text{em}}}{3\pi x} \left\{ \frac{17}{2} - \frac{3}{2} x + \frac{191}{12} x^2 - \frac{23}{3} x^3 + \frac{7}{4} x^4 \right. \\
+ \left[ 3 + \frac{2}{3} - 6x^2 + 3\frac{2}{3} x^4 + 5 x \ln x \right] \ln \frac{1}{r} \\
+ \left[ 3 + \frac{2}{3} x - 6x^2 + 3\frac{2}{3} x^4 \right] \ln(1-x) \\
- \frac{28}{3} x \ln x + 5x \ln(1-x) \ln x + 5 x \text{Li}_2(1-x) \right\} \tag{B2}
\]

where \( r = \frac{m_{\mu}^2}{m_\phi^2} \ll 1 \), and the range of \( x \) is \((0, 1)\) which does not depend on \( r \) since \( r \) is negligible. The sum of (B1) and (B2) gives us the total photon spectrum from annihilation to muons.

APPENDIX C: DETERMINATION OF COUPLINGS

Here we show how the couplings of the mediators to dark matter are analytically determined from the various observational constraints. We parametrize the annihilation cross section as

\[
\langle \sigma v \rangle = ax + by + cF^2 \tag{C1}
\]

where \( x = (g_1g_1.5)^2 \), \( y = (g_2g_2.5)^2 \), and \( a, b, c \) are the functions of \( m_{\chi}, m_{\phi_2} \) in (14). The ratio \( R \) of muons to \( b \) quarks resulting from the annihilations is

\[
R = \frac{ax + cF^2/2}{by + cF^2/2}. \tag{C2}
\]

Setting the cross section equal to the relic density value \( \langle \sigma v \rangle_0 \) and using (C2), we can solve for \( x \) and \( y \), for a given value of \( F \):

\[
x = \frac{1}{a} \left( \frac{\langle \sigma v \rangle_0}{1 + R^{-1} - \frac{c}{2} F^2} \right) \\
y = \frac{1}{b} \left( \frac{\langle \sigma v \rangle_0}{1 + R - \frac{c}{2} F^2} \right). \tag{C3}
\]

Since \( x, y \geq 0 \), this constrains

\[
|F| \leq F_{\text{max}} = \left( \frac{2\langle \sigma v \rangle_0}{c} \right)^{1/2} \min \left\{ \frac{1}{\sqrt{1+R}}, \frac{1}{\sqrt{R+1}} \right\}. \tag{C4}
\]

The minimum value of \( a_1 \) needed for sufficient Sommerfeld enhancement determines \( g_1 = \sqrt{4\pi a_1} \); then \( g_{1.5} = \sqrt{x}/g_1 \) and \( g_{2.5} = \sqrt{y}/g_2 \), where we should allow for both possible signs of \( x \) and \( y \). Eliminating \( f_{1.5} \) and \( f_{2.5} \) in Eq. (15) for \( F \) results in a quadratic equation for \( s = g_1/g_2 \):

\[
s = \frac{F \pm \sqrt{F^2 - 4\sqrt{x}\sqrt{y}(1 - q^2)}}{2\sqrt{y}(1 + q)} \tag{C5}
\]

where \( q = m_{\phi_2}^2/4m_\phi^2 \). The smallest value of \(|s| \) is found when the signs of the two terms in the numerator of (C5) are opposite. We can take \( F > 0 \) and the lower sign while keeping \( s > 0 \) if \( \sqrt{y} < 0 \), corresponding to the choice of all couplings except for \( g_{2.5} \) being positive. (Alternatively, we could take all couplings except for \( g_{1.5} \) positive and \( F < 0 \), but there is no physical difference.) One can explore the range of possible couplings by allowing \( F \) to vary between 0 and \( F_{\text{max}} \).


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