**Talus: A simple way to remove cliffs in cache performance**

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We prove that Talus removes performance cliffs, and evaluate MPKI which plots misses per kilo-instruction (where performance suddenly changes as data fits in the cache. This causes confusing performance bugs that are difficult to reproduce. SPEC CPU2006 The MB lines before they hit. But with 32 MB of these partitions, Talus ensures that as an application is given partitions among competing applications. By controlling the sizes of these partitions, Talus ensures that as an application is given more cache space, its miss rate decreases in a convex fashion. We prove that Talus removes performance cliffs, and evaluate it through extensive simulation. Talus adds negligible overheads, improves single-application performance, simplifies partitioning algorithms, and makes cache partitioning more effective and fair.

Abstract—Caches often suffer from performance cliffs: minor changes in program behavior or available cache space cause large changes in miss rate. Cliffs hurt performance and complicate cache management. We present Talus, a simple scheme that removes these cliffs. Talus works by dividing a single application’s access stream into two partitions, unlike prior work that partitions among competing applications. By controlling the sizes of these partitions, Talus ensures that as an application is given more cache space, its miss rate decreases in a convex fashion. We prove that Talus removes performance cliffs, and evaluate it through extensive simulation. Talus adds negligible overheads, improves single-application performance, simplifies partitioning algorithms, and makes cache partitioning more effective and fair.

Talus: A Simple Way to Remove Cliffs in Cache Performance

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I. INTRODUCTION

Caches are crucial to cope with the long latency, high energy, and limited bandwidth of main memory accesses. However, caches can be a major headache for architects and programmers. Unlike most system components (e.g., frequency or memory bandwidth), caches often do not yield smooth, diminishing returns with additional resources (i.e., capacity). Instead, they frequently cause performance cliffs: thresholds where performance suddenly changes as data fits in the cache.

Cliffs occur, for example, with sequential accesses under LRU. Imagine an application that repeatedly scans a 32 MB array. With less than 32 MB of cache, LRU always evicts lines before they hit. But with 32 MB of cache, the array suddenly fits and every access hits. Hence going from 31 MB to 32 MB of cache suddenly increases hit rate from 0% to 100%. The SPEC CPU2006 benchmark libquantum has this behavior. Fig. 1 shows libquantum’s miss curve under LRU (solid line), which plots misses per kilo-instruction (MPKI, y-axis) against cache size (MB, x-axis). libquantum’s miss curve under LRU is constant until 32 MB, when it suddenly drops to near zero. Cliffs also occur with other access patterns and policies.

Performance cliffs produce three serious problems. First, cliffs waste resources and degrade performance. Cache space consumed in a plateau does not help performance, but wastes energy and deprives other applications of that space. Second, cliffs cause unstable and unpredictable performance, since small fluctuations in effective cache capacity (e.g., due to differences in data layout) result in large swings in performance. This causes confusing performance bugs that are difficult to reproduce [9, 15, 33], and makes it hard to guarantee quality of service (QoS) [16, 21]. Third, cliffs greatly complicate cache management, because optimal allocation is an NP-complete problem without convex miss curves [36, 45].

Talus is the gentle slope of debris formed by erosion of a cliff.

Fig. 1: Performance of libquantum over cache sizes. LRU causes a performance cliff at 32 MB. Talus eliminates this cliff.

Two areas of prior work address performance cliffs in caches: high-performance replacement policies and cache partitioning. High-performance replacement policies have addressed many of the common pathologies of LRU [12, 19, 37, 49]. These policies achieve good performance and often avoid cliffs, but due to their empirical design they are difficult to predict and sometimes perform worse than LRU. The loss of predictability is especially unfortunate, since performance predictions are needed for efficient cache partitioning.

Cache partitioning allows software to control cache capacity to achieve system-level objectives. Cache partitioning explicitly divides cache space among cores or types of data to maximize performance [2, 4, 36], improve fairness [32, 36], or ensure QoS [16, 21]. Partitioning handles cliffs by avoiding operating on plateaus. For example, faced with the miss curve in Fig. 1, efficient partitioning algorithms will allocate either 32 MB or 0 MB, and nowhere in between. This ensures cache space is either used effectively (at 32 MB) or is freed for use by other applications (at 0 MB). Partitioning thus copes with cliffs, but still suffers from two problems: First, cliffs force “all-or-nothing” allocations that degrade fairness. Second, since optimal partitioning is NP-complete, partitioning algorithms are forced to use expensive or complex approximations [2, 32, 36].

Cliffs are not a necessary evil: optimal cache replacement (MIN [3]) does not suffer them. Rather, cliffs are evidence of the difficulty in using cache space effectively. Eliminating cliffs would be highly desirable, since it would put resources to good use, improve performance and fairness, increase stability, and—perhaps most importantly in the long term—make caches easier to reason about and simpler to manage.

We observe that performance cliffs are synonymous with non-convex miss curves. A convex miss curve has slope that shrinks with increasing capacity. By contrast, non-convex miss
curves have regions of small slope (plateaus) followed by regions of larger slope (cliffs). Convexity means that additional capacity gives smooth and diminishing hit rate improvements.

We present Talus, a simple partitioning technique that ensures convex miss curves and thus eliminates performance cliffs in caches. Talus achieves convexity by partitioning within a single access stream, as opposed to prior work that partitions among competing access streams. Talus divides accesses between two shadow partitions, invisible to software, that emulate caches of a larger and smaller size. By choosing these sizes judiciously, Talus ensures convexity and improves performance. Our key insight is that only the miss curve is needed to do this. We make the following contributions:

- We present Talus, a simple method to remove performance cliffs in caches. Talus operates on miss curves, and works with any replacement policy whose miss curve is available.
- We prove Talus’s convexity and generality under broad assumptions that are satisfied in practice.
- We design Talus to be predictable: its miss curve is trivially derived from the underlying policy’s miss curve, making Talus easy to use in cache partitioning.
- We contrast Talus with bypassing, a common replacement technique. We derive the optimal bypassing scheme and show that Talus is superior, and discuss the implications of this result on the design of replacement policies.
- We develop a practical, low-overhead implementation of Talus that works with existing partitioning schemes and requires negligible hardware and software overheads.
- We evaluate Talus under simulation. Talus transforms LRU into a policy free of cliffs and competitive with state-of-the-art replacement policies [12, 19, 37]. More importantly, Talus’s convexity simplifies cache partitioning algorithms, and automatically improves their performance and fairness. In short, Talus is the first approach to offer both the benefits of high-performance cache replacement and the versatility of software control through cache partitioning.

II. BACKGROUND AND INSIGHTS

We first review relevant work in cache replacement and partitioning, and develop the insights behind Talus.

A. Replacement policies

The optimal replacement policy, Belady’s MIN [3, 30], relies on a perfect oracle to replace the line that will be reused furthest in the future. Prior work has proposed many mechanisms and heuristics that attempt to emulate optimal replacement. We observe that, details aside, they use three broad techniques:

- Recency: Recency prioritizes recently used lines over old ones. LRU uses recency alone, which has obvious pathologies (e.g., thrashing and scanning [10, 37]). Most high-performance policies combine recency with other techniques.
- Classification: Some policies divide lines into separate classes, and treat lines of each class differently. For example, several policies classify lines as reused or non-reused [19, 24]. Classification works well when classes have markedly different access patterns.
- Protection: When the working set does not fit in the cache, some policies choose to protect a portion of the working set against eviction from other lines to avoid thrashing. Protection is equivalent to thrash-resistance [19, 37].

High-performance policies implement these techniques in different ways. DIP [37] enhances LRU by dynamically detecting thrashing using set dueling, and protects lines in the cache by inserting most lines at low priority in the LRU chain. DIP inserts a fixed fraction of lines (ε = 1/32) at high priority to avoid stale lines. DRRIP [19] classifies between reused and non-reused lines by inserting lines at medium priority, includes recency by promoting lines on reuse, and protects against thrashing with the same mechanism as DIP. SHiP [49] extends DRRIP with more elaborate classification, based on the memory address, PC, or instruction sequence. PDP [12] decides how long to protect lines based on the reuse distance distribution, but does not do classification. IbdRP [22] uses PC-based classification, but does not do protection.

These policies improve over LRU on average, but have two main drawbacks. First, these policies use empirically tuned heuristics that may not match application behavior, so they sometimes perform worse than LRU (Sec. VII-C). Second, and more importantly, the miss curve for these policies cannot be easily estimated in general, which makes them hard to use with partitioning, as we discuss next.

B. Cache partitioning

Cache partitioning allows software to divide space among cores, threads, or types of data [2, 7, 40], enabling system-wide management of shared caches. There are several ways to implement partitioning schemes. Way partitioning [1, 7] is simple and commonly used, but it allows only few coarse partitions and degrades associativity. Fine-grained partitioning techniques like Vantage [40] and Futility Scaling [48] support hundreds of inexpensive partitions sized in cache lines, and strictly enforce these sizes. Finally, set partitioning can be implemented in hardware through reconfigurable or molecular caches [38, 47], or in software by using page coloring [29].

Replacement policies vs. partitioning: Cache partitioning is often used to improve performance in systems with shared caches [32, 36, 44], and is sometimes compared to thread-aware extensions of several replacement policies [12, 17, 19]. However, cache partitioning has many other uses beyond performance, and is better thought of as an enabling technology for software control of the cache. Partitioning strikes a nice balance between scratchpad memories, which yield control to software but are hard to use, and conventional hardware-only caches, which are easy to use but opaque to software. For instance, partitioning has been used to improve fairness [32, 35], implement priorities and guarantee QoS [8, 13, 21], improve NUCA designs [2, 28], and eliminate side-channel attacks [34]. Talus adds another capability to partitioning: eliminating cache performance cliffs.

Partitioning is therefore a general tool to help achieve system-level objectives. After all, caches consume over half of chip area in modern processors [27]; surely, software should have a say in how they are used. Hardware-only replacement policies simply do not support this—they use policies fixed at design time and cannot know what to optimize for.

C. Predictability

We say that a replacement policy is predictable if the miss curve, i.e. its miss rate on a given access stream at different
partition sizes, can be estimated efficiently. Miss curves allow partitioning policies to reason about the effect of different partition sizes without actually running and measuring performance at each size. Using miss curves, dynamic partitioning algorithms can find and set the appropriate sizes without trial and error. Because resizing partitions is slow and the space of choices is very large, predictability is highly desirable.

The need for predictability has confined partitioning to LRU in practice. LRU’s miss curve can be cheaply sampled in hardware using utility monitors (UMOns) [36], or in software using address-based sampling [11, 42]. However, high-performance replacement policies lack this predictability. Since they are designed empirically and do not obey the stack property [30], there is no simple known monitoring scheme that can sample their miss curve cheaply. Likewise, much work has gone into modeling LRU’s performance for general access patterns, but little for high-performance policies. For example, DIP was analyzed on cyclic, scanning access patterns [37] (e.g., lbquantum in Fig. 1). While insightful, this analysis does not extend to general access patterns that do not exhibit cyclic behavior (e.g., Fig. 3 in Sec. III; see also Sec. V-C).

Alternatively, non-predictable policies can adapt through slow trial and error [8, 14]. However, these schemes can get stuck in local optima, scale poorly beyond few cores, and are unresponsive to changes in application behavior since partitions take tens of milliseconds to be resized.

Convexity is thus not a substitute for predictability. Some high-performance policies are mostly convex in practice (e.g., DRRIP [19], Fig. 10), but without some way of predicting their performance, such policies cannot be effectively controlled by software to achieve system-level objectives.

High-performance cache replacement and partitioning are consequently at loggerheads: techniques that improve single-thread performance are incompatible with those used to manage shared caches. This is unfortunate, since in principle they should be complementary. A key contribution of Talus is to eliminate this conflict by capturing much of the benefit of high-performance policies without sacrificing LRU’s predictability.

D. Convexity

Convexity means that the miss curve’s slope shrinks as cache space grows [45]. Convexity implies that the cache yields diminishing returns on performance with increasing cache space, and thus implies the absence of cliffs. It has two other important benefits: it makes simple allocation algorithms (e.g., hill climbing) optimal, and it avoids all-or-nothing behavior, improving fairness. Although the benefits of convexity may not be obvious, prior work shows that there is latent demand for convex cache behavior in order to simplify cache management.

Simple resource allocation: Without convexity, partitioning cache capacity to maximize performance is an NP-complete problem [45]. Existing algorithms yield approximate and often good solutions, but they are either inefficient [36] or complex [2, 32]. This makes them hard to apply to large-scale systems or multi-resource management [4]. Alternatively, prior work consciously ignores non-convexity and applies convex optimization [4, 8], sacrificing performance for simplicity and reduced overheads. As we will see in Sec. VII, applying convex optimization to LRU wipes out most of the benefits of partitioning. Thus, it is not surprising that prior techniques that use hill climbing or local optimization methods to partition LRU find little benefit [4, 8], and those that use more sophisticated methods, such as Lookahead or dynamic programming, report significant gains [2, 21, 32, 36, 40, 50].

Convexity eliminates this tradeoff, as cheap convex optimization (e.g., hill climbing) finds the optimal sizes [5, 45]. By ensuring convexity, Talus simplifies cache management.

Fairness: Even if optimization complexity is not a concern, eliminating cliffs also avoids all-or-nothing behavior in allocations and improves fairness. For example, imagine a system with a 32 MB cache running two instances of libquantum (with miss curve shown in Fig. 1, solid line). If the cache is unpartitioned, both applications will evict each other’s lines, getting no hits (both will have effective capacity below the 32 MB cliff). Partitioning can help one of the applications by giving it the whole 32 MB cache, but this is unfair. Any other choice of partition sizes will yield no benefit. Imbalanced partitioning [35] finds that this is common in parallel applications, and proposes to allocate most cache space to a single thread of a homogeneous parallel application to improve performance. Convex miss curves make this unnecessary: with Talus’ miss curve (Fig. 1, dashed line), giving 16 MB to each instance of lbquantum accelerates both instances equally and maximizes the cache’s hit rate. In general, with homogeneous threads and convex miss curves, the maximum-utility point is equal allocations, which is also the most fair.

In summary, convexity not only provides smooth, stable behavior, but makes optimal resource allocation cheap, improves fairness, and leads to better allocation outcomes.

III. TALUS EXAMPLE

This section illustrates how Talus works with a simple example. Talus uses partitioning to eliminate cache performance cliffs. Unlike prior work that partitions capacity among different cores, Talus partitions within a single access stream. It does so by splitting the cache (or, in partitioned caches, each software-visible partition) into two hidden shadow partitions. It then controls the size of these partitions and how accesses are distributed between them to achieve the desired performance.

Talus computes the appropriate shadow partition configuration using miss curves; in this example we use the miss curve in Fig. 3. Fig. 3 is the miss curve of LRU on an application that accesses 2 MB of data at random, and an additional 3 MB sequentially. This results in a performance cliff around 5 MB, when MPKI suddenly drops from 12 to 3 once the application’s data fits in the cache. Since the cache gets 12 MPKI at 2 MB, there is no benefit from additional capacity from 2 until 5 MB. Hence at 4 MB, half of the cache is essentially wasted since it could be left unused with no loss in performance.

Talus can eliminate this cliff and improve performance. Specifically, in this example Talus achieves 6 MPKI at 4 MB. The key insight is that LRU is inefficient at 4 MB, but LRU is efficient at 2 MB and 5 MB. Talus thus makes part of the cache behave like a 2 MB cache, and the rest behave like a 5 MB cache. As a result, the 4 MB cache behaves like a combination of efficient caches, and is itself efficient. Significantly, Talus requires only the miss curve to ensure convexity. Talus is totally blind to the behavior of individual lines, and does not
(a) Original cache at 2 MB.

(b) Original cache at 5 MB.

(c) Talus cache at 4 MB.

Fig. 2: Performance of various caches for the miss curve in Fig. 3. Fig. 2a and Fig. 2b show the original cache (i.e., without Talus), conceptually dividing each cache by sets, and dividing accesses evenly across sets. Fig. 2c shows how Talus eliminates the performance cliff with a 4 MB cache by dividing the cache into partitions that behave like the original 2 MB (top) and 5 MB (bottom) caches. Talus achieves this by dividing accesses in dis-proportion to partition size.

Fig. 2 is similar, but for a 5 MB cache. This cache is also split by sets at a 1 : 2 ratio. It achieves 3 MPKI, coming from the top sets at 1 MPKI and the bottom sets at 2 MPKI.

Finally, Fig. 2c shows how Talus manages the 4 MB cache using set partitioning. The top sets behave like the top sets of the 2 MB cache (Fig. 2a), and the bottom sets behave like the bottom sets of the 5 MB cache (Fig. 2b). This is possible because Talus does not hash addresses evenly across sets. Instead, Talus distributes them in the same proportion as the original caches, at a 1 : 2 ratio between top : bottom. Hence the top sets in Fig. 2c operate identically to the top sets in Fig. 2a. (They receive the same accesses, have the same number of sets and lines, etc.) In particular, the top sets in Fig. 2c and Fig. 2a have the same miss rate of 4 MPKI. Similarly, the bottom sets between Fig. 2c and Fig. 2b behave identically and have the same miss rate of 2 MPKI. Hence the total miss rate in Fig. 2c is 4 + 2 = 6 MPKI (instead of the original 12 MPKI). This value lies on the convex hull of the miss curve, as shown in Fig. 3.

In this example, Talus partitions by set. However, with sufficient associativity, capacity is the dominant factor in cache performance, and cache organization or partitioning scheme are less important. So while this example uses set partitioning, Talus works with other schemes, e.g. way partitioning.

The only remaining question is how Talus chooses the partition sizes and sampling rates. 4 MB lies at a ratio of 2 : 1 between the end points 2 MB and 5 MB. Although not obvious, the partitioning ratio should be the inverse, 1 : 2. We derive and explain this in detail in the next section.

IV. TALUS: CONVEXITY BY DESIGN

Fig. 4 summarizes the parameters Talus controls. It shows a single application accessing a cache of size \( s \), employing some replacement policy that yields a miss curve \( m(s) \). For example, \( m(1 \text{ MB}) \) gives the miss rate of a 1 MB cache. Talus divides the cache into two shadow partitions of sizes \( s_1 \) and \( s_2 \), where \( s = s_1 + s_2 \). Each shadow partition has its own miss curve, \( m_1(s_1) \) and \( m_2(s_2) \) respectively. Furthermore, Talus inserts a fraction \( \rho \) of the access stream into the first shadow partition, and the remaining \( 1 - \rho \) into the second.

We now show how, for any given size \( s \), we can choose \( s_1 \), \( s_2 \), and \( \rho \) to achieve performance on the convex hull of the
original miss curve. We develop the solution in three steps. First, we show how miss curves change when the access stream is divided among shadow partitions. Second, we show how to choose partition sizes to linearly interpolate cache performance between any two points of the original miss curve. Third, we show that by choosing these points appropriately, Talus traces the original miss curve’s convex hull. Because these claims are broad, independent of particular applications or replacement policies, we present rigorous proofs.

A. General assumptions

Before we get started, we need to make some basic assumptions about cache performance and application behavior. These assumptions are often implicit in prior work, and as we shall see, are well-supported by experiments (Sec. VII).

Assumption 1. Miss curves are stable over time, and change slowly relative to the reconfiguration interval.

Talus uses the miss curve sampled in a given interval (e.g., 10 ms) to adjust its configuration for the next interval. If the access stream drastically changes across intervals, Talus’s decisions may be incorrect. In practice, most applications have stable miss curves. Dynamic partitioning techniques and PDP [12] also make this assumption.

Assumption 2. For a given access stream, a partition’s miss rate is a function of its size alone; other factors (e.g., associativity) are of secondary importance.

With reasonable associativity, size is the main factor that affects performance. Assumption 2 is inaccurate in some cases, e.g., way partitioning with few ways. Our implementation (Sec. VI) describes a simple way to satisfy this in practice, justified in our evaluation (Sec. VII). This assumption is made in prior partitioning work [2, 40] that uses UMONs to generate miss curves without using way partitioning.

This assumption also means that, although we prove results for Talus on an unpartitioned cache, our results also apply to individual partitions in a partitioned cache.

Assumption 3. Sampling an access stream produces a smaller, statistically self-similar access stream.

In large last-level caches, hits and misses are caused by accesses to a large collection of cache lines. No single line dominates accesses, as lower-level caches filter temporal locality. For example, if a program accesses a given line very frequently, that line will be cached in lower levels and will not produce last-level cache accesses. Thus, by pseudo-randomly sampling the access stream (i.e., by hashing addresses), we obtain an access stream with similar statistical properties to the full stream [23]. This holds in practice for large caches and good hash functions [6, 25, 39, 46]. Assumption 3 is extensively used, e.g. to produce miss curves cheaply with UMONs [36], dynamically switch replacement policies using set dueling [37], or accelerate trace-driven simulation [23]. Talus uses this property to reason about the behavior of the shadow partitions.

B. Miss curves of shadow partitions

Using the previous assumptions, we can easily derive the relationship between the partition’s full miss curve, \( m(s) \), and the miss curves of an individual shadow partition, \( m'(s') \). Intuitively, a shadow partitioned cache with accesses split pseudo-randomly in proportion to partition size behaves the same as an unpartitioned cache (see Fig. 2a and Fig. 2b). In particular, misses are also split proportionally between shadow partitions. So if the partition gets a fraction \( \rho = s'/s \) of accesses, its miss curve is \( m'(s') = s'/s \ m(s) = \rho \ m(s'/\rho) \). This relation holds when accesses are distributed disproportionately as well:

**Theorem 4.** Given an application and replacement policy yielding miss curve \( m(s) \), pseudo-randomly sampling a fraction \( \rho \) of accesses yields miss curve \( m'(s') \):

\[
m'(s') = \rho \ m\left(\frac{s'}{\rho}\right)
\]

Proof. Since a sampled access stream is statistically indistinguishable from the full access stream (Assumption 3) and capacity determines miss rate (Assumption 2), it follows that misses are distributed evenly across capacity. (If it were otherwise, then equal-size partitions would exist with different miss rates, exposing either statistical non-uniformity in the access stream or sensitivity of miss rate to factors other than capacity.) Thus, following the discussion above, Eq. 1 holds for proportionally-sampled caches.

Eq. 1 holds in general because, by assumption, two partitions of the same size \( s' \) and sampling rate \( \rho \) must have the same miss rate. Hence a disproportionally-sampled partition’s miss rate is equal to that of a partition of a larger, proportionally-sampled cache. This cache’s size is \( s'/\rho \), yielding Eq. 1.

C. Convexity

To produce convex cache performance, we trace the miss curve’s convex hull (e.g., the dotted lines in Fig. 3). Talus achieves this by linearly interpolating between points on the miss curve’s convex hull, e.g. by interpolating between \( \alpha = 2 \) MB and \( \beta = 5 \) MB in Fig. 3.

We interpolate cache performance using Theorem 4 by splitting the cache into two partitions, termed the \( \alpha \) and \( \beta \) shadow partitions (Fig. 4), since Talus configures them to behave like caches of size \( \alpha \) and \( \beta \). We then control the sizes of the shadow partitions, \( s_1 \) and \( s_2 \), and the sampling rate, \( \rho \) (into the \( \alpha \) partition), to achieve the desired miss rate. First note from Theorem 4 that the miss rate of this system is:

\[
m_{\text{shadow}}(s) = m_1(s_1) + m_2(s_2)
\]

\[
= \rho \ m(s_1) + (1 - \rho) \ m(s - s_1)
\]

(2)
Lemma 5. Given an application and replacement policy yielding miss curve \( m(\cdot) \), one can achieve miss rate at size \( s \) that linearly interpolates between any two points on the curve, \( m(\alpha) \) and \( m(\beta) \), where \( \alpha \leq s < \beta \).

Proof. To interpolate, we must anchor terms in \( m_{\text{shadow}} \) at \( m(\alpha) \) and \( m(\beta) \). We wish to do so for all \( m \), in particular injective \( m \), hence anchoring the first term at \( m(\alpha) \) implies:

\[
m(s_1/\rho) = m(\alpha) \Rightarrow s_1 = \rho \alpha \tag{3}
\]

Anchoring the second term at \( m(\beta) \) implies:

\[
m\left( \frac{s - s_1}{1 - \rho} \right) = m(\beta) \Rightarrow \rho = \frac{\beta - s}{\beta - \alpha} \tag{4}
\]

Substituting these values into the above equation yields:

\[
m_{\text{shadow}} = \frac{\beta - s}{\beta - \alpha} m(\alpha) + \frac{s - \alpha}{\beta - \alpha} m(\beta) \tag{5}
\]

Hence as \( s \) varies from \( \alpha \) to \( \beta \), the system’s miss rate varies proportionally between \( m(\alpha) \) to \( m(\beta) \) as desired.

Theorem 6. Given a replacement policy and application yielding miss curve \( m(s) \), Talus produces a new replacement policy that traces the miss curve’s convex hull.

Proof. Set sizes \( \alpha \) and \( \beta \) to be the neighboring points around \( s \) along \( m \)’s convex hull and apply Lemma 5. That is, \( \alpha \) is the largest cache size no greater than \( s \) where the original miss curve \( m \) and its convex hull coincide, and \( \beta \) is the smallest cache size larger than \( s \) where they coincide.

Finally, we now apply Theorem 6 to Fig. 2 to show how the partition sizes and sampling rate were derived for a \( s = 4 \) MB cache. We begin by choosing \( \alpha = 2 \) MB and \( \beta = 5 \) MB, as these are the neighboring points on the convex hull (Fig. 3). \( \rho \) is the “normalized distance to \( \beta \)”: 4 MB is two-thirds of the way to 5 MB from 2 MB, so one third remains and \( \rho = 1/3 \). \( s_1 \) is the partition size that will emulate a cache size of \( \alpha \) with this sampling rate. By Theorem 4, \( s_1 = \rho \alpha = 2/3 \) MB. Finally, \( s_2 \) is the remaining cache space, \( 10/3 \) MB. This size works because—by design—it emulates a cache of size \( \beta \): the second partition’s sampling rate is \( 1 - \rho = 2/3 \), so by Theorem 4 it models a cache of size \( s_2/(1 - \rho) = 5 \) MB.

Hence, a fraction \( \rho = 1/3 \) of accesses behave like a \( \alpha = 2 \) MB cache, and the rest behave like a \( \beta = 5 \) MB cache. This fraction changes as \( s \) moves between \( \alpha \) and \( \beta \), smoothly interpolating performance between points on the convex hull.

V. THEORETICAL IMPLICATIONS

A few interesting results follow from the previous section. All of the following should be taken to hold approximately in practice, since the assumptions only hold approximately.

A. Predictability enables convexity

Theorem 6 says that so long as the miss curve is available, it is fairly simple to ensure convex performance by applying Talus. While Talus is general (we later show how it convexifies SRIP, albeit using impractically large monitors), it is currently most practical with policies in the LRU family [42]. Talus motivates further development of high-performance policies for which the miss curve can be cheaply obtained.

Corollary 7. Optimal cache replacement is convex.

Proof. By contradiction. If it were not convex, by Theorem 6 some shadow partitioning would exist that traced its convex hull (we need not compute the shadow partition sizes or sampling rates that trace it to guarantee its existence). This convex hull would achieve fewer misses than the optimal policy.

B. Optimality implies convexity

Theorem 6 gives a simple proof that optimal replacement (MIN) is convex. We are not aware of a prior proof of this fact.

Corollary 8. Bypassing on a miss curve \( m(s) \) achieves performance no better than the miss curve’s convex hull.

Proof. Consider a cache that accepts a fraction \( \rho \) of accesses and bypasses \( 1 - \rho \). This is equivalent to sampling a fraction \( \rho \) of accesses into a “partition of size \( s \)” (the full cache), and sending the remainder to a “partition of size zero” (bypassed). By Theorem 4, this yields a miss rate of:

\[
m_{\text{bypass}}(s) = \rho m(s/\rho) + (1 - \rho) m(0/(1 - \rho)) \tag{6}
\]

Fig. 5: Optimal bypassing at 4 MB for the Fig. 3 miss curve.
Assumption 3 and hence Theorem 4 are consequently less well as optimal bypassing on that policy. Talus allows the system’s partitioning algorithm—whatever Talus does not propose its own partitioning algorithm. Instead, the distinction is sometimes relatively unimportant (e.g., in DIP [37]), but it can be significant. For example, with a high miss rate many lines can occupy the lowest priority in DRRIP, so a “bypassed” line may not even be the first evicted.

Additionally, unlike Assumption 3, most policies do not sample by address, but instead sample lines via other methods not strictly correlated to address. For example, DIP inserts lines at high priority every 32nd miss, regardless of address [37]. Assumption 3 and hence Theorem 4 are consequently less accurate for these policies.

Finally, this corollary also says that Talus will perform as well as optimal bypassing on that policy. It says nothing about the performance of Talus vs. bypassing for different baseline policies, although the intuition behind Corollary 8 is still useful to reason about performance in such cases. For example, PDP comes close to our description of optimal bypassing, so one might expect Talus on LRU to always outperform PDP. However, PDP evicts MRU among protected lines and sometimes outperforms Talus on LRU. Hence this result is a useful but inexact tool for comparing policies (see Sec. VII-C).

VI. PRACTICAL IMPLEMENTATION

Talus builds upon existing partitioning solutions, with minor extensions in hardware and software. Our implementation is illustrated in Fig. 7 and described in detail below.

A. Software

Talus wraps around the system’s partitioning algorithm. Talus does not propose its own partitioning algorithm. Instead, Talus allows the system’s partitioning algorithm—whatever it may be—to safely assume convexity, then realizes convex performance. This occurs in pre- and post-processing steps.

In the pre-processing step, Talus reads miss curves from hardware monitors (e.g., UMOSs [36] or the SRRIP monitors described later) and computes their convex hulls. These convex hulls are passed to the system’s partitioning algorithm, which no longer needs to concern itself with cliffs.

In the post-processing step, Talus consumes the partition sizes generated by the partitioning algorithm, and produces the appropriate shadow partition sizes and sampling rates. It does so using Theorem 6 and the convex hulls.

![Fig. 6: Comparison of Talus (convex hull) vs. optimal bypassing for the miss curve in Fig. 3.](image)

Because Talus traces the convex hull, it performs at least as well as optimal bypassing. However, this claim comes with a few important caveats: most replacement policies do not really bypass lines. Rather, they insert them at low priority. The distinction is sometimes relatively unimportant (e.g., in DIP [37]), but it can be significant. For example, with a high miss rate many lines can occupy the lowest priority in DRRIP, so a “bypassed” line may not even be the first evicted.

Additionally, unlike Assumption 3, most policies do not sample by address, but instead sample lines via other methods not strictly correlated to address. For example, DIP inserts lines at high priority every 32nd miss, regardless of address [37]. Assumption 3 and hence Theorem 4 are consequently less accurate for these policies.

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B. Hardware

Talus works with existing partitioning schemes, either coarse-grained (e.g., set [29, 38] or way [1, 7, 36] partitioning) or fine-grained (e.g., Vantage [40] or Futility Scaling [48]).

Talus extends these by (i) doubling the number of partitions in hardware, (ii) using two shadow partitions per “logical” (i.e., software-visible) partition, and (iii) adding one configurable sampling function to distribute accesses between shadow partitions. The sampling function consists of an 8-bit hash function (we use inexpensive H3 [6] hashing) and an 8-bit limit register per logical partition. Each incoming address is hashed. If the hash value lies below the limit register, the access is sent to the α partition. Otherwise it is sent to the β partition.

**Deviation from assumptions:** The theory relies on a few assumptions (Sec. IV-A) that are good approximations, but not exact. We find that our assumptions hold within a small margin of error, but this margin of error is large enough to cause problems if it is not accounted for. For example, although applications are stable between intervals, they do vary slightly, and sampling adds small deviations, even over many accesses. Unaccounted for, these deviations from theory can “push β up the performance cliff,” seriously degrading performance.

We account for these deviations by adjusting the sampling rate ρ to build in a margin of safety into our implementation. (The effect of adjusting ρ by X% is to decrease α by X% and increase β by X%.) We have empirically determined an increase of 5% ensures convexity with little loss in performance.

**Talus on way partitioning:** Talus works on way partition-
ing, but way partitioning can somewhat egregiously violate Assumption 2. Specifically, way partitioning forces coarse-grain allocations that can significantly reduce associativity. This means that the coarsened shadow partition sizes will not match the math, and Talus will end up interpolating between the wrong points. We address this by recomputing the sampling rate from the final, coarsened allocations: $\rho = s_1/\alpha$.

**Talus on Vantage**: Vantage partitioning supports many partitions sized at line granularity, and is a good fit for Talus. However, Vantage does not partition a small fraction of the cache, known as the unmanaged region (10% of the cache in our evaluation). Vantage can give no guarantees on capacity for this region. Hence, at a total capacity of $s$, our Talus-on-Vantage implementation assumes a capacity of $s' = 0.9s$. Using Talus with Futility Scaling [48] would avoid this complication.

**Inclusion**: Talus can cause performance anomalies with inclusive LLCs. By sampling accesses into a small partition, Talus can back-invalidate lines that are frequently reused in lower cache levels and cause LLC accesses that aren’t reflected in the sampled miss curve. We use non-inclusive caches to avoid this problem. Alternatively, one could sample the miss curve at lower cache levels (e.g., at the L2), or lower-bound the emulated sizes of the shadow partitions.

**C. Monitoring**

We gather LRU miss curves with utility monitors (UMONS). We use 64-way, 1 KLine UMONs to monitor the full LLC size. However, if this was the only information available, Talus would miss the behavior at larger sizes and be unable to trace the convex hull to these sizes. This matters for benchmarks with cliffs beyond the LLC size (e.g., libquantum).

**Miss curve coverage**: To address this, we add a second monitor per partition that samples accesses at a much lower rate. By Theorem 4, this models a proportionally larger cache size. With a sampling rate of $1 : 16$ of the conventional UMON, we model 4× LLC capacity using just 16 ways.

With 32-bit tags, monitoring requires 5 KB per core (4 KB for the original UMON plus 1 KB for the sampled one).

**Other replacement policies**: Talus can work with other policies, but needs their miss curve. UMONs rely on LRU’s stack property [30] to sample the whole curve with one monitor, but high-performance policies do not obey the stack property. We evaluate Talus with SRRIP by using multiple monitor orpers, one per point on the miss curve. By sampling at different rates, each monitor models a cache of a different size. We use 64-point curves, which would require 64 × 4 = 256 KB of monitoring arrays per core, too large to be practical. CRUISE [18] takes a similar approach (using set sampling instead of external monitors) to find the misses with both half of the cache and the full cache, in effect producing 3-point miss curves; producing higher-resolution curves would be similarly expensive. Perhaps future implementations can reduce overheads by using fewer monitors and dynamically adapting sampling rates, but this is non-trivial and orthogonal to our purpose: demonstrating that Talus is agnostic to replacement policy.

**D. Overhead analysis**

Talus adds small hardware overheads. Doubling the number of partitions adds negligible overhead in way partitioning [1, 7]; in Vantage, it requires adding an extra bit to each tag (each tag has a partition id) and adding 256 bits of state per partition [40]. Adaptive sampling requires an 8-bit hash function and an 8-bit limit register per partition. Monitors need 5 KB/core, of which only 1 KB is specific to Talus (to cover larger sizes). In the evaluated 8-core system with an 8 MB LLC, extra state adds up to 24.2 KB, a 0.3% overhead over the LLC size.

Talus adds negligible software overheads. First, Talus computes the convex hulls in linear time in size of the miss curve using the three-coins algorithm [31]. Second, it computes the shadow partition sizes by finding the values for $\alpha$ and $\beta$ (logarithmic time in size of convex hull) and a few arithmetic operations for Theorem 6 (constant time). These overheads are a few thousand cycles per reconfiguration (every 10 ms), and in return, enable simpler convex optimization.

**VII. Evaluation**

We evaluate Talus in a variety of settings, to demonstrate the following claims from Sec. I:

- Talus avoids performance cliffs, and is agnostic to replacement policy and partitioning scheme.
- Talus on LRU achieves performance competitive with high-performance policies and avoids pathologies.
- Talus is both predictable and convex, so simple convex optimization improves shared cache performance and fairness.

Talus is the first approach to combine high-performance cache replacement with the versatility of cache partitioning.

**A. Methodology**

We use zsim [41] to evaluate Talus in single-threaded and multi-programmed setups. We simulate systems with 1 and 8 OOO cores with parameters in Table I.

We perform single-program runs to evaluate Talus’s convexity and performance on LLCs of different sizes. We also simulate SRRIP, DRRIP, and PDP, which are implemented as proposed. DRRIP uses $M = 2$ bits and $\epsilon = 1/32$ [19]. For fairness, these policies use external auxiliary tag directories (DRRIP) and monitors (PDP) with the same overheads as Talus monitors (Sec. VI). We use SPECcpu2006 apps, executed for 10 B instructions after fast-forwarding 10 B instructions.

We also perform multi-programmed runs to evaluate Talus’s cache partitioning improvements (simplicity, performance, and fairness). We compare LRU, TA-DRRIP [19], and several cache partitioning schemes with and without Talus. Our methodology resembles prior work [17, 40]. We run random mixes of

| Cores | 1 (ST) or 8 (MP), 2.4 GHz, Silvermont-like OOO [20]: 8B-wide ifetch; 2-level bpref with 512×10-bit BHSRs + 1024×2-bit PHT, 2-way decode/issue/rename/commit, 32-entry IQ and ROB, 10-entry LQ, 16-entry SQ |
| L1 caches | 32 KB, 8-way set-associative, split D/I, 4-cycle latency |
| L2 caches | 128 KB priv per-core, 8-way set-associative, inclusive, 6-cycle |
| L3 cache | Shared, non-inclusive, 20-cycle; 32-way set-associate with way-partitioning or 4/52 zcache with Vantage; 1 MB/core |
| Coherence | MESI, 64 B lines, no silent drops; sequential consistency |
| Main mem | 200 cycles, 12.8 GBps/channel, 1 (ST) or 2 (MP) channels |

**TABLE I**: Configuration of the simulated systems for single-threaded (ST) and multi-programmed (MP) experiments.
We evaluate Talus on three partitioning schemes: Vantage (V), way partitioning (W), and ideal (I). On all schemes, Talus closely traces LRU’s convex hull.

SPEC CPU2006 apps, with 1B instructions per app after a 20B fast-forward. We use a fixed-work methodology: all apps are kept running until all finish 1B instructions, and we only consider the first 1B instructions of each app to report aggregate performance. We report weighted speedup relative to LRU, $(\sum_i I_P C_i / I_P C_{i, LRU})/N_{apps}$, which accounts for throughput and fairness; and harmonic speedup, $1/\sum_i (I_P C_{i, LRU} / I_P C_i)$, which emphasizes fairness [36, 43]. We repeat runs to achieve 95% confidence intervals with SRRIP.

B. Talus yields convex miss curves

We first evaluate the miss curves (MPKI vs. LLC size) Talus produces in different settings and demonstrate its convexity. **Talus is agnostic to partitioning scheme:** Fig. 8 shows Talus with LRU on two representative SPEC CPU2006 apps, libquantum and gobmk. (Other apps behave similarly.) We evaluate Talus on three partitioning schemes: Vantage (Talus+V/LRU), way partitioning (Talus+W/LRU), and idealized partitioning on a fully-associative cache (Talus+I/LRU).

In all schemes, Talus avoids LRU’s performance cliffs, yields smooth, diminishing returns, and closely traces LRU’s convex hull. Because Vantage partitions only 90% of the cache, Talus+V/LRU’s performance lies slightly above the convex hull. This is particularly evident on libquantum. Likewise, variation between reconfiguration intervals causes small deviations from the convex hull, especially evident on gobmk.

One might be concerned that small non-convexities cause problems when using convex optimization with Talus. However, recall from Fig. 7 that Talus produces convex miss curves from LRU’s in a pre-processing step, not from measuring Talus itself. The distinction is subtle but important: these curves are guaranteed to be convex; Fig. 8 shows that Talus achieves performance very close to these curves in practice. Thus, the system’s partitioning algorithm can assume convexity with confidence that Talus will achieve the promised performance. **Talus is agnostic to replacement policy:** Fig. 9 shows Talus with SRRIP replacement and way partitioning (Talus+W/SRRIP) on libquantum and mcf. The purpose of this experiment is to demonstrate that Talus is agnostic to replacement policy; SRRIP is hard to predict, so we use impractical 64-point monitors (Sec. VI-C). As with LRU, Talus eliminates the cliff in libquantum and lbm and traces SRRIP’s convex hull. Finally, note that DRRIP achieves similar performance to Talus+W/SRRIP with lower monitoring overheads, but DRRIP is unpredictable and not guaranteed to be convex in general, so it lacks the partitioning benefits of Talus on LRU.

**Talus is agnostic to prefetching:** We have reproduced these results using L2 adaptive stream prefetchers validated against Westmere [41]. Prefetching changes miss curves somewhat, but does not affect any of the assumptions that Talus relies on.

**Talus is agnostic to multi-threading:** We have run Talus with LRU on the multi-threaded benchmark suite SPEC OMP2012, where it achieves convex miss curves similar to Fig. 8 and Fig. 9. With non-inclusive caches and directories to track the L2 contents, shared data is served primarily from other cores, rather than through the LLC. Hence, Talus’s assumptions hold, and it works equally well on multi-threaded apps.

We have only observed significant non-convexities in Talus on benchmarks with exceptionally low memory intensity (e.g., on povray and tonto, which have <0.1 L2 MPKI). These benchmarks do not access the LLC frequently enough to yield statistically uniform access patterns across shadow partitions. However, since their memory intensity is so low, non-convexities on such applications are inconsequential.

In the remainder of the evaluation, we use Talus with Vantage partitioning and LRU replacement (Talus+V/LRU).

C. Talus with LRU performs well on single programs

**MPKI:** Fig. 10 shows MPKI curves from 128 KB to 16 MB for six SPEC CPU2006 benchmarks. We compare Talus+V/LRU with several high-performance policies: SRRIP, DRRIP, and PDP, and include LRU for reference.

Generally, Talus+V/LRU performs similarly to these policies. On many benchmarks (not shown), all policies perform identically to LRU, and Talus+V/LRU matches this performance. On perlbench, libquantum, lbm, and xalancbmk (and others not shown), Talus+V/LRU outperforms LRU and matches the high-performance replacement policies.

On perlbench, cactusADM, libquantum, and lbm, Talus+V/LRU outperforms one or more high-performance policies. perlbench and cactusADM are examples where PDP performs poorly. These benchmarks have a cliff following a convex region in the LRU miss curve. Since PDP is based on bypassing, it cannot achieve convex performance on such applications, and Talus+V/LRU outperforms it (Sec. V-C). lbm is an example where RRIP policies perform poorly (Gems also shows this behavior). We found that DRRIP is largely convex.
Fig. 10: Misses per kilo-instruction (MPKI) of Talus (+V/LRU) and high-performance replacement policies on representative SPEC CPU2006 benchmarks from 128 KB to 16 MB. Talus achieves good performance and avoids cliffs.

on SPEC CPU2006, but this comes at the price of occasionally under-performing LRU and sacrificing its predictability.

Since Talus+V/LRU works by simply avoiding cliffs in LRU, it never degrades performance over LRU, and outperforms RRIP on such benchmarks. However, this is a limitation as well as a strength: Talus’s performance is limited by the performance of the replacement policy it operates on. On some benchmarks this is significant. For instance, mcf and cactusADM benefit tremendously from retaining lines that have been reused. LRU does not track this information, so it is not available to Talus+V/LRU. Policies that capture reused lines (RRIP especially, somewhat for PDP) will outperform Talus+V/LRU on such benchmarks. This limitation is not inherent to Talus, though—any predictable replacement policy that captured such information would allow Talus to exploit it.

**IPC**: Fig. 11 shows IPC vs. LRU for the policies shown in Fig. 10 at 1 MB and 8 MB. These sizes correspond to the per-core LLC capacity, and the LLC capacity of the 8-core CMP. (Beyond 8 MB differences among policies steadily diminish.) The left side of Fig. 11 shows the IPC vs. LRU for every benchmark that is affected at least 1%, and the right side shows the gmean speedup across all 29 SPEC CPU2006 benchmarks.

Talus+V/LRU improves performance whenever other policies do, and gives similar benefits, except for a few cases where DR-RRIP outperforms all others at 1 MB. Significantly, Talus+V/LRU never causes large degradations, while at 8 MB other policies all cause significant degradations for some benchmark.

Averaging over SPEC CPU2006, Talus+V/LRU gives IPC benefits comparable to other policies. At 1 MB, it is similar to PDP and SRRIP, but trails DR-RRIP (1.9% vs. 2.4%, 2.2%, 3.8%, respectively); at 8 MB, it outperforms PDP, SRRIP, and DR-RRIP (1.0% vs. 0.69%, -0.03%, 0.39%).

In summary, Talus avoids LRU’s inefficiencies and approaches state-of-the-art replacement policies, without adopting an empirical design that sacrifices LRU’s predictability.

**D. Talus simplifies cache management and improves the performance and fairness of managed LLCs**

We now evaluate Talus+V/LRU on an 8-core CMP with a shared LLC. These experiments demonstrate the qualitative benefits of Talus: Talus is both predictable and convex, so simple partitioning algorithms produce excellent outcomes. We apply partitioning to achieve two different goals, performance and fairness, demonstrating the benefits of *software control of the cache*. Hardware-only policies (e.g., TA-DRRIP) are fixed at design time, and cannot adapt to the changing needs of general-purpose systems. Both of Talus’s properties are essential: predictability is required to partition effectively, and convexity is required for simple algorithms to work well.

**Performance**: Fig. 12 shows the weighted (left) and harmonic (right) speedups over unpartitioned LRU for 100 random mixes of the 18 most memory intensive SPEC CPU2006 apps. Fig. 12 is a *quantile plot*, showing the distribution of speedups by sorting results for each mix from left to right along the x-axis.

Moreover, we compare two partitioning algorithms: hill climbing and Lookahead [36]. Hill climbing is a simple algorithm that allocates cache capacity incrementally, giving capacity to whichever partition benefits most from the next little bit. Its
implementation is a trivial linear-time for-loop. Lookahead is a quadratic heuristic that approximates the NP-complete solution of the non-convex optimization problem. Equivalent algorithms achieve linear-time common case performance, at the cost of extra complexity [2]. Talus+V/LRU uses hill climbing, and partitioned LRU is shown for both Lookahead and hill climbing.

Weighted speedups over LRU are up to 41%/gmean of 12.5% for hill climbing on Talus+V/LRU, 34%/10.2% for Lookahead on LRU, 39%/6.3% for TA-DRRIP, and 16%/3.8% for hill climbing on LRU. Thus Talus+V/LRU achieves the best performance of all schemes with simple hill climbing, whereas partitioned LRU sees little benefit with hill climbing. This is caused by performance cliffs: with non-convexity, hill climbing gets stuck in local optima far worse than the best allocation. In contrast, since Talus+V/LRU is convex, hill climbing is optimal (in terms of LLC hit rate).

Lookahead avoids this pitfall, but must make “all-or-nothing” allocations: to avoid a cliff, it must allocate to sizes past the cliff. This means that if the most efficient allocation lies beyond the cache capacity, Lookahead must ignore it. Talus+V/LRU, in contrast, can allocate at intermediate sizes (e.g., along the LRU plateau) and avoid this problem. Hence Talus+V/LRU outperforms Lookahead by 2%. Finally, TA-DRRIP under-performs partitioning, trailing Talus+V/LRU by 5.6% gmean over all mixes.

Talus+V/LRU also improves fairness, even while optimizing for performance, illustrated by harmonic speedups in Fig. 12(b). Harmonic speedups over LRU are gmean 8.0% for hill climbing on Talus+V/LRU, 7.8% for Lookahead on LRU, 5.2% for TA-DRRIP, and -1.8% for hill climbing on LRU. Talus+V/LRU modestly outperforms Lookahead in harmonic speedup. In contrast, TA-DRRIP’s harmonic speedup is well below partitioned schemes, while hill climbing on LRU actually degrades performance over an unpartitioned cache.

The only scheme that is competitive with naïve hill climbing on Talus+V/LRU is Lookahead, an expensive heuristic whose alternatives are complex. This shows that, by ensuring convexity, Talus makes high-quality partitioning simple and cheap.

**Fairness:** Fig. 13 shows three case studies of eight copies of benchmarks on the 8-core system with LLC sizes from 1 MB to 72 MB. This system represents a homogenous application in a setting where fairness is paramount. Fig. 13 shows three benchmarks: libquantum, omnetpp, and xalancbmk, all of which have a performance cliff under LRU. We compare the execution time of a fixed amount of work per thread for various schemes (lower is better) vs. unpartitioned LRU with a 1 MB LLC. As before, we compare Talus+V/LRU against partitioned LRU and TA-DRRIP. In this case, we employ fair partitioning (i.e., equal allocations) for LRU and Talus+V/LRU, and Lookahead on LRU.

libquantum has a large performance cliff at 32 MB. With eight copies of libquantum, unpartitioned LRU does not improve performance even at 72 MB, as the applications interfere in the cache (Fig. 13a, left). Likewise, fair partitioning with LRU provides no speedup, since each application requires 32 MB to perform well. Lookahead improves performance, but at the cost of fairness: after 32 MB, Lookahead gives the entire cache to one application, boosting its performance without benefiting the others. This leads to a large gap between the IPCs of different cores, shown by the coefficient of variation of core IPC (i.e., the standard deviation of IPCs divided by the mean IPC; Fig. 13a, right). TA-DRRIP thrashes in the cache, and never settles on any single core to prioritize.

In contrast, Talus+V/LRU gives steady gains with increasing LLC size, achieving the best performance except when Lookahead briefly outperforms it (due to Vantage’s unmanaged region;
We have presented Talus, a novel application of partitioning with the versatility of cache partitioning. TA-DRRIP improves performance in these benchmarks, but at the cost of grossly unfair allocations. Unlike libquantum, Talus uses convexity to improve performance. Over all sizes, Talus+VLRU gives steady performance gains and never significantly sacrifices fairness.

These results hold for other benchmarks. Most are barely affected by partitioning scheme and perform similarly to LRU. Across all benchmarks, Talus+VLRU with fair partitioning has at most 2% coefficient of variation in core IPC and averages 0.3%, whereas Lookahead/TA-DRRIP respectively have up to 85%/51% and average 10%/5%. While Lookahead or TA-DRRIP reduce execution time in some cases, they sacrifice fairness. Hence most cores speed up, except for one or a few unloved cores that cannot maintain their working set, resulting in unfair performance. Over all sizes, Talus+VLRU improves performance over various benchmarks, but Talus offers a simpler alternative: naive, equal allocations.

The performance improvements are possible because Lookahead and TA-DRRIP use redundant information to reduce execution time. Hence, as when optimizing performance, Talus makes high-quality partitioning simple and cheap. We have shown that Talus, using much simpler algorithms, improves shared cache performance and fairness over prior partitioning approaches and thread-aware replacement policies. Both of Talus’s qualitative contributions—predictability and convexity—were necessary to achieve these outcomes: Predictability is needed to make informed decisions, and convexity is needed to make simple algorithms work well.

VIII. CONCLUSION

Convexity is important in caches to avoid cliffs and thereby improve cache performance and simplify cache management. We have presented Talus, a novel application of partitioning that ensures convexity. We have proven Talus’s convexity rigorously under broadly applicable assumptions, and discussed the implications of this analytical foundation for designing replacement policies. Talus improves performance over LRU and, more importantly, allows for simple, efficient, and optimal allocation of cache capacity. Talus is the first approach to combine the benefits of high-performance cache replacement with the versatility of cache partitioning.

ACKNOWLEDGMENTS

We thank the reviewers for their helpful feedback. This work was supported in part by NSF grant CCF-1318384.

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ACKNOWLEDGMENTS

We thank the reviewers for their helpful feedback. This work was supported in part by NSF grant CCF-1318384.