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Efficiency Improvement of Non-Uniformly-Aged PV Arrays

Yihua Hu, Senior Member IEEE, Jiangfeng Zhang, Jiande Wu, Member, IEEE, Wenping Cao, Senior Member, IEEE, Gui Yun Tian, Senior Member, IEEE, James L. Kirtley, Life Fellow, IEEE

Abstract—The utilization of solar energy by photovoltaic (PV) systems has received much research and development (R&D) attention across the globe. In the past decades, a large number of PV array have been installed. Since the installed PV arrays often operate in harsh environments, non-uniform aging can occur and impact adversely on the performance of PV systems, especially in the middle and late periods of their service life. Due to the high cost of replacing aged PV modules by new modules, it is appealing to improve energy efficiency of aged PV systems. For this purpose, this paper presents a PV module reconfiguration strategy to achieve the maximum power generation from non-uniformly aged PV arrays without significant investment. The proposed reconfiguration strategy is based on the cell-unit structure of PV modules, the operating voltage limit of gird-connected converter, and the resulted bucket-effect of the maximum short circuit current. The objectives are to analyze all the potential reorganization options of the PV modules, find the maximum power point and express it in a proposition. This proposition is further developed into a novel implementable algorithm to calculate the maximum power generation and the corresponding reconfiguration of the PV modules. The immediate benefits from this reconfiguration are the increased total power output and maximum power point voltage information for global maximum power point tracking (MPPT). A PV array simulation model is used to illustrate the proposed method under three different cases. Furthermore, an experimental rig is built to verify the effectiveness of the proposed method. The proposed method will open an effective approach for condition-based maintenance of emerging aging PV arrays.

Index Terms—Maximum power tracking, non-uniform aging, offline reconfiguration, output characteristics, photovoltaics (PVs), solar energy.

I. INTRODUCTION

Solar energy utilization has received much attention across the globe over the last decades [1]-[6]. Currently, photovoltaic (PV) power devices are gaining in popularity in the global renewable energy market, primarily owing to the reducing manufacture costs of PV panels and continuous improvement in power conversion technologies [7]-[8]. In practice, high energy conversion efficiency and long effective service time can help reducing capital and operating costs and thus are highly desired.

With the improvement of materials technologies, monocrystalline silicon and multicrystalline silicon now can be economically produced in large quantities. However, their energy conversion efficiency from solar to electricity is still low. Typical efficiency for monocrystalline silicon solar cells is around 20% while it is 18% for multicrystalline silicon solar cells [9]. On the power electronics side, high-performance switching devices (e.g. silicon carbon (SiC), super junction MOSFETs) and new converter topologies (e.g. multi-level DC-AC and resonant DC-DC converters) can improve energy conversion efficiency [10]-[12]. This part of energy conversion efficiency can reach as high as 95% [12]. However, these figures are typically for nominal and healthy operation of PV cells while in reality they are subject to various faults and aging conditions, which reduce the lifetime of the PV cells and their operational efficiency. For these faulted or aged PV systems, an easy approach to improve energy efficiency is to replace aged PV modules by brand new ones. However, this is not economically acceptable to most of the PV system owners. This paper aims to propose a reconfiguration strategy for faulted or aged PV systems so that the maximum power generation can be improved by simply rearranging the positions of the PV modules. This reconfiguration strategy is derived from the bucket effect of the maximum short circuit current of PV strings, therefore, the basic structure and working principles of a PV system need to be introduced.

There are four levels of components to form a PV system. Namely, PV cell-unit, PV module, PV string and PV array, as illustrated in Fig. 1. In order to restrict hotspots in the PV module, a bypass diode is connected in parallel with PV cells; such a structure is named a cell-unit (including m PV cells). In the PV system considered, assume that n cell-units are connected in series to form a PV module to raise the output voltage, and s PV modules are connected in series to construct...
a PV string. A number of PV strings are connected with diodes and then in parallel to become a PV array. The diodes can stop the current flow between strings, which is harmful.

In order to increase the PV device’s effective service time, fault diagnosis and remedial measures are two important approaches. Since PV panels often operate in outdoor harsh environments, potential hazards from dust, bird-dropping, partial shading and cell aging will affect the power generation performance [13]-[15]. Therefore, detection techniques such as thermal cameras [16]-[21], earth-capacitance measurement (ECM) [22], time-domain reflectometry (TDR) [23], and voltage/current sensors are widely applied to identify the irregularity of PV cells. Upon a fault, a non-uniform temperature distribution can build up on the PV array and a thermal camera can help to locate the faulty PV module. The ECM can locate the disconnection of any PV modules and the TDR can estimate the degradation of PV arrays. Nonetheless, both ECM and TDR are expensive and only be employed as offline fault diagnosis tools [22][23]. References [24] and [25] propose a PV array fault detection method by comparing simulated and measured output powers of PV arrays based on the environment data. Paper [26] analyzes the dynamic current-voltage characteristics to achieve fault diagnosis. In paper [27], machine learning techniques are employed for PV fault detection by measuring PV array voltage, current, irradiance and temperature.

After a fault is diagnosed, certain remedial measures need to take place. In-situ reconfiguration is an effective solution [28]-[34]. But this can only work if a large number of relays are used and the state of health (SoH) information of every PV module is available all the time. These two conditions cause higher system costs and also make the system controls complicated. In-situ reconfiguration also needs powerful CPUs to calculate optimal solutions quickly enough, which increases system costs. Paper [34] proposes a diffusion charge redistribution method to achieve the maximum power. By taking advantage of the intrinsic diffusion capacitance of the solar cells, the number of power devices used is reduced to simplify the system. Nonetheless, the majority of PV arrays are not equipped with online reconfiguration equipment due to the high cost.

So far the PV fault diagnosis and online reconfiguration technology are still under development. In the middle and late lifetime of the PV arrays, aging, especially non-uniform aging, is a severe phenomenon that significantly decreases PV system efficiency [35]-[37]. In the literature, a cost effective technique to improve the energy efficiency of the aged PV arrays is still lacking. This paper attempts to fill the gap by developing an offline reconfiguration strategy for the “middle-aged and elderly” PV arrays so as to maximize the solar power generation.

The paper is organized as follows. Section II introduces mathematical modeling of non-uniform aging PV array. Section III illustrates the detection of aging PV. According to aging information, section IV introduces the optimal PV module reconfiguration algorithm. Section V illustrates the proposed method by analytical study. Section VI presents simulation and experimental results to verify the proposed method, followed by a short conclusion in Section VII.

II. MATHEMATICAL MODELING

A new fault tolerance topology is developed to improve the system performance that also can improve SRM driving system fault tolerance ability.

Non-uniform aging is a common problem in PVs which can be caused by lasting dust, shading, or water corrosion over a long period of time [13][14]. Usually, there are many reasons to cause aging differences. Due to the harsh operating environments, hail or stone can break the glass of some PV modules. New modules are usually needed to replace broken modules so that the aging difference between new and old modules is high. Modules in the same locations can also suffer differently from aging influences depending on the relative positions they are in. The modules at front and sides may be subjected to worse conditions such as duct and abrasion. Furthermore, modules in the same batch can also have aging differences due to product quality variations. This is particularly true when they work towards the end of their service life. This paper addresses these aging differences and attempts to increase their overall output and lifetime expansion of PV array by offline reconfiguration.

A. Model of Healthy PV Cells

The electrical characteristics of PVs are influenced by both temperature and illumination. The electrical model of the PV cell is expressed by [2].

\[ I = I_L - I_S [\exp(\frac{e \cdot V}{n \cdot k \cdot T}) - 1] \]  
(1)

\[ \varepsilon = \frac{q}{N_{S} \cdot K \cdot A} \]  
(2)

where

- \( I \) is the current of the PV cell (A).
- \( I_L \) is the light-generated current (A).
- \( I_S \) is the saturation current (A).
- \( e \) is the electron charge (C).
- \( V \) is the voltage across the PV cell (V).
- \( n \) is the ideality factor.
- \( k \) is the Boltzmann constant (J/K).
- \( T \) is the cell temperature (K).
- \( q \) is the charge of the fundamental unit of positive charge (C).
- \( N_{S} \) is the number of solar cells.
- \( K \) is a constant.
- \( A \) is the area of a single solar cell (m²).

Fig. 1 Componential structure of the PV array.
where \( I \) is the PV module output current, \( I_1 \) is the photon current, \( q \) is the quantity of electric charge, \( A \) is the diode characteristic factor, \( K \) is the Boltzmann constant, \( I_0 \) is the saturated current, \( T_m \) is the PV module temperature, \( G \) is the irradiance, \( V \) is the output voltage, \( G_{ref} \) is the reference irradiance (1000 W/m²), \( I_{ref1}, I_{ref2} \) are the reference values for \( I_1 \) and \( I_0 \), \( k_i \) is the current-temperature coefficient provided by the PV manufacturer. \( T_{ref} \) is the reference temperature, \( N_i \) is the number of series-connected cells, \( T_m \) is the PV module temperature. \( e \) is a constant depending on \( q, N_i, K, A \), and is calculated by the following equation:

\[
I_{sc_{ref}} - I_{app_{ref}} = \frac{I_{sc_{ref}} - I_{app_{ref}}}{\exp(-\frac{V_{app_{ref}}}{T_{ref}}) - 1}
\]

where \( I_{app_{ref}}, V_{app_{ref}} \) and \( V_{sc_{ref}} \) are the maximum power point (MPP) current, short-circuit current, MPP voltage and open-circuit voltage at a reference condition defined by the relevant standard.

B. Terminal Characteristics of Aged Cells

When a PV cell is subject to aging, a direct indication is its lower output power than normal. Due to the p-n junction characteristics of the PV cell, its open-circuit voltage only changes slightly while the short-circuit current changes dramatically. According to references [38][39], the degradation of short-circuit current is about 10%, while the degradation open-circuit voltage is 2% in average after one year operation, which means the short circuit has a dominated influence. From [36], the short current has close change rate with power loss. Reference [40] also gives the conclusion that the short current has dominated influence while the open circuit voltage with negligible change after a 1.5 year aging experiment. Therefore, in this paper, we take use of the short-circuit current to evaluate the aging condition of PV cells; and use the same open circuit voltage to approximate aging conditions of PV cells.

Fig. 2 presents a cell unit with \( m \) non-uniformly aged PV cells, where \( I_{sc1}, I_{sc2}, I_{sc3} \ldots I_{scm} \) are the short-circuit current for cells 1, 2, 3 \ldots \( m \), respectively. There are three ranges in the current-voltage output characteristics. In Range 1, the maximum current is the minimum of all cells current \( (I_{sc1}, I_{sc2}, I_{sc3}, \ldots I_{scm}) \) and all the cells generate electricity. Range 2 is a transitional interval. Its equivalent circuit is presented in Fig. 3 and its terminal output voltage is given in Eq. (6). Due to a voltage drop on \( R_e \), the output voltage of the cell-unit is lower than a healthy cell-unit.

\[
\sum_{i=1}^{m} V_{cell_i} - i_{s2} \cdot R_e = V_{cu}
\]

where \( V_{cell} \) is the output voltage of the PV cell, \( R_e \) is the equivalent resistance of aged PV cell, and \( V_{cu} \) is the output voltage of the cell-unit.

As \( i_{s2} \) increases, \( V_{cu} \) decreases to zero. The current switches from Range 2 to Range 3. In Range 3, the cell-unit is bypassed by a diode, and the corresponding terminal voltage is -0.5 V (i.e. diode voltage drop). In Ranges 1 and 2, the current passing the cell-unit is \( i_{s2} = i_{cm} \) where \( i_{cm} \) is the PV module current. In Range 3, the current passing the bypass diode is \( i_s \), which is equal to \( i_{cm} \).

From the analysis of Range 1-3, it can be found that the non-uniform aging of PV cells limits the power generation capacity of cell-units. This is termed the “bucket effect”.

C. Model of Non-Uniformly Aged Cells

A PV array can age differently at the cell-unit, module and string levels.

For a cell-unit with \( m \) series-connected PV cells, the relationship between the output current \( i_{cu} \) and the terminal output voltage \( V_{cu} \) depends on the PV’s operating points. To facilitate discussion on the three ranges, it is assumed that the magnitude of the short-circuit currents for \( m \) cells is

\[
i_{cell1} \leq i_{cell2} \leq \cdots \leq i_{cellm}
\]

Define \( i_{cell} \) as the actual current passing the PV cells. When the current \( i_{cell} \) starts to increase from 0 to \( I_{sc1} \), all the cells generate electricity. When \( i_{cell} \) exceeds \( I_{sc1} \) but less than \( I_{sc2} \), cell \( i_1 \) cannot generate electricity; it is either bypassed or turned into a resistor because of the bucket effect. As a result, the relationship of \( i_{cell} \) and \( V_{cu} \) is summarized as follows.

1) If \( i_{cell} \leq I_{sc1} \), the unit-cell operates in Range 1.

\[
i_{cu} = i_{cell} \leq I_{sc1}
\]

\[
V_{cu} = m V_{cell}
\]

Where \( V_{cell} \) is equal to the voltage of every cell.

2) If \( i_{cell} > I_{sc1} \), the cell-unit operates in Range 3.

\[
V_{cu} = 0.5 V
\]

\[
i_{cell} = 0
\]

\[
i_{cu} = i_{diode}
\]

where \( i_{diode} \) is the bypass current flowing through the diode.

The PV cells can work in Range 2 if there exists an integer \( k \) satisfying the conditions:

\[
i_{sc1} \leq i_{cell} \leq I_{sc1+k}
\]
(m−k)V_{cell}−i_{cell}\sum_{j=1}^{k}R_{ej} \geq 0 \quad (14)

When the cell-unit operates in Range 2, \( i_{cu} = i_{cell} \) and

\[ V_{cu} = (m−k)V_{cell}−i_{cell}\sum_{j=1}^{k}R_{ej} \quad (15) \]

where \( R_{ej} \) is the equivalent resistance of the \( j \)th cell.

Usually, Ranges 1 and 3 are the steady-state operational conditions while Range 2 is a short transitional range between the two and can often be ignored.

A PV string consists of \( s \) PV modules, with the terminal voltage \( V_{string} \) and current \( i_{string} \). Let the terminal voltage, current and maximum current from the \( k \)th PV module be \( V_{module,k} \), \( i_{module,k} \) and \( i_{max, module,k} \), respectively. The following relationship can be established.

\[ i_{string} = i_{module,1} = i_{module,2} = \ldots = i_{module,s} \quad (16) \]

\[ V_{string} = V_{module,1} + V_{module,2} + \ldots + V_{module,s} \quad (17) \]

Similarly, the bucket effect indicates that the maximum current in the PV string is limited by the minimum \( i_{max, module,k} \) of those non-bypassed modules. That is, \( i_{string} \leq i_{max, module,k} \), \( 1 \leq k \leq s \), and the \( k \)th module is not bypassed.

In practice, the cell-units within a PV module may be aged differently and thus have different maximum short-circuit currents. This case is called the “general non-uniform aging” in the paper. A simpler case for non-uniformly aged PV modules is that all cell-units in the same PV module are aged uniformly so that the whole PV module can be characterized with a single maximum short-circuit current of any cell-unit. This is termed the simplified non-uniform aging in this paper.

A PV array consists of \( p \) parallel-connected PV strings; its terminal voltage and current are denoted by \( V_{array} \) and \( i_{array} \), respectively. Let the terminal voltage and current for the \( j \)th PV string be \( V_{string,j} \) and \( i_{string,j} \), respectively. Therefore:

\[ V_{array} = V_{string,1} = V_{string,2} = \ldots = V_{string,p} \quad (18) \]

\[ i_{array} = i_{string,1} + i_{string,2} + \ldots + i_{string,p} \quad (19) \]

The power output from the PV array is the sum of \( p \) strings, and is also limited by the bucket effect. That is, the maximum power output from the simplified non-uniform aging PV array can be written as \( \sum_{j=1}^{p} \min\{P_{j,k}^{max} : 1 \leq k \leq s \} \), and the \( (j,k) \)th module is un-bypassed, where \( P_{j,k}^{max} \) is the maximum power output from the un-bypassed PV module at the position \((j,k)\) (\( k \)th module in the \( j \)th string) of the PV array. Define \( i_{module,j,k} \) as the maximum short-circuit current in the \((j,k)\) module; and \( q \) as the number of PV modules which generate electricity in the \( j \)th string. Thus, \((s-q)\) PV modules are bypassed by diodes in the \( j \)th string. Then the maximum power \( P_{j,k}^{max} \) is calculated as

\[ P_{j,k}^{max} = qV_{module,j}i_{j,q}^{p} \quad (20) \]

where \( V_{module,j} \) is the MPP voltage supplied by a PV module, and \( i_{j,q}^{p} \) is the \( q \)th largest short-circuit current within the set { \( i_{module,j,1}, i_{module,j,2}, \ldots, i_{module,j,s} \) }. For a normal PV module consisting of 3 cell-units, \( V_{module} = 3V_{cu} \), and \( V_{cu} \) is the MPP voltage a PV cell-unit can provide.

### III. Detection of PV Aging

Aged modules have two typical characteristics: abnormal temperature and terminal electricity characteristics [3]. Accordingly, the detection of PV aging relies on the effective identification of one of the two characteristics.

#### A. Thermal Cameras

When the PV array is operational, a part of effective solar energy on the PV panel is transferred into electricity while the rest is transferred into heat. Assume that the temperature difference between PV cells and cover glass is neglected; cell temperature is uniform in a healthy module; and there is no thermal propagation across PV cells. Then the energy balance can be established as [5]:

\[ S = V \cdot I + H_{ps}A_{m}(T_{m}−T_{a}) \quad (21) \]

\[ S = G \cdot A_{m} \quad (22) \]

where \( S \) is the effective solar absorbed flux, \( T_{a} \) is the ambient temperature, \( H_{ps} \) is an overall heat exchange coefficient in relation to the total surface area of the module, \( A_{m} \) is the PV module area.

Eqs. (1) and (21) form a parameter-based model with key parameters \( I, V, T_{m}, S, H_{ps} \) and \( T_{a} \). Fig. 4 illustrates a multi-physical link of the PV array in the parameter-based model, where \( E \) represents the electrical output power of the PV cell. The electrical model is mainly influenced by effective solar energy \( S \) and module temperature \( T_{m} \), as illustrated in Eqs. (3) and (22). The thermal characteristic is mainly influenced by electrical power and effective solar energy, as shown in Eq. (21). The temperature \( T_{a} \) and the total effective solar energy \( S \) are linked by the electro-thermal characteristics. For a given \( S \), the module temperature depends on the electrical power of the PV module. The parameters \( T_{m}, I \) and \( V \) can be retrieved using thermography, current, and voltage sensors, respectively.

![Fig. 4 Energy conversion within the PV array [3].](image)

When operating in Range 1, all the cells contribute to electricity generation and it is impossible to distinguish an aged module from the PV string. When operating at range 3, the most aged cells cannot generate electricity at the string current working point so that a short circuit occurs at the cell-unit by its bypass diode. Therefore, At Range 3, the aged cell-unit is open-circuited and there is no solar energy transferred into electricity. This leads to a higher temperature in the aged cell-unit than the healthy ones. By changing the
working points of PV array, all aged cell-units can be located from their thermal images.

**B. Time Domain Reflectometry (TDR)**

TDR is another aging detection method. In TDR, a signal is injected into the transmission line, and the signal will be distorted when mismatch occurs [22, 23]. Like a radar, the TDR method analyzes the input signal and output signal, as shown in Fig. 5; the aging condition can be estimated according to the signal degradation. Note that illumination can influence the impedance of PV cell; therefore, TDR can only be used in the night.

![Fig. 5 Theory of TDR.](image)

Both of the thermal camera and TDR equipment can be used temporarily to obtain the aging information of PV array. This is to say, there is no need to permanently install the reconfiguration equipment while temporary renting will be sufficient to obtain the PV aging information. This saves hardware investment.

**IV. OPTIMAL PV MODULE CONFIGURATION**

In addition to three-phase 12/8 SRM driving systems, four-phase 8-slot/6-pole (8/6) SRM driving systems are also widely used. The proposed fault tolerance also can be used in four phase 8/6 SRM.

After an aged module is detected, a remedial measure can be employed to rearrange the faulted PV modules, prior to the replacement of the faulted modules which increases capital costs.

**A. Theoretical Analysis**

From Eq. (20), it is noted that the maximum power output of a PV array depends on the maximum short-circuit current of each PV modules. Therefore, it is possible to rearrange aged PV modules in a PV array in order to maximize the power output. Now, reorganizing all the maximum short circuit current values from the highest to the lowest:

$$\beta_1 > \beta_2 > \ldots > \beta_{ps}$$

(23)

where $\beta_i$ is the highest current and $\beta_{ps}$ the lowest from maximum short circuit currents

\[\{i_{\text{module},j,k};\ j = 1, \ldots, p; \ k = 1, \ldots, s\}\]

When the PV array power generation is maximal, the number of working PV modules should be equal to that of un-bypassed modules in all strings. This number (denoted by $\alpha$) may vary between 1 and $s$. Thus the output voltage of the PV string equalizes this number multiplied by $V_{\text{module}}$.

**Proposition:** The maximum power output from a simplified non-uniform aging PV array is

$$\max\{P_{\text{module}}^1, P_{\text{module}}^2, \ldots, P_{\text{module}}^s\}$$

where $P_{\text{module}}^1$, $P_{\text{module}}^2$, $\ldots$, $P_{\text{module}}^s$ are determined by:

$$P_{\text{module}}^1 = (\beta_1 + \beta_2 + \ldots + \beta_{(p-1)} + \beta_p)V_{\text{module}}$$

(24)

$$P_{\text{module}}^2 = 2(\beta_2 + \beta_3 + \beta_4 + \ldots + \beta_{(p-1)} + \beta_p)V_{\text{module}}$$

(25)

$$\vdots$$

$$P_{\text{module}}^s = s(\beta_1 + \beta_2 + \beta_3 + \ldots + \beta_{(p-1)} + \beta_p)V_{\text{module}}$$

(27)

Consider a 2 × 3 PV array for example. This array has two strings and each string has 3 PV modules ($p=2$, $s=3$). The module maximum short-circuit currents are 0.9 pu, 0.8 pu, 0.2 pu; 0.4 pu, 0.5 pu, 0.7 pu, respectively. If each string has only one operational module, the maximum powers from the first and second strings are 0.9 $V_{\text{module}}$ and 0.7 $V_{\text{module}}$, respectively. The total power output is 1.6 $V_{\text{module}}$. If each string has two operational modules, the maximum power is (0.8+0.8) $V_{\text{module}}$ = 1 $V_{\text{module}}$ from the first string and (0.5+0.5) $V_{\text{module}}$ = 1 $V_{\text{module}}$ from the second string due to the bucket effect. The total power output is 2.6 $V_{\text{module}}$. If all modules are operational, the maximum power is (0.2+0.2+0.2) $V_{\text{module}}$ = 0.6 $V_{\text{module}}$ for the first string, and (0.4+0.4+0.4) $V_{\text{module}}$ = 1.2 $V_{\text{module}}$ for the second string. The total maximum power output is 1.8 $V_{\text{module}}$.

From this analysis, the maximum possible power generation is equal to the max{1.6 $V_{\text{module}}$, 2.6 $V_{\text{module}}$, 1.8 $V_{\text{module}}$} = 2.6 $V_{\text{module}}$. Now re-arrange these maximum short-circuit currents as follows:

$$\beta = 0.9 > \beta = 0.8 > \beta = 0.7 > \beta = 0.5 > \beta = 0.4 > \beta = 0.2$$

The power generation of the rearranged PV modules can be maximized when there are 1, 2 or 3 modules generating electricity in each string ($\alpha$ is unknown).

If $\alpha = 1$, there is one module generating electricity in a string, then the rearrangement (0.9 pu, 0.7 pu, 0.4 pu; 0.8 pu, 0.5 pu, 0.2 pu) can ensure the maximum power generation. The corresponding maximum power is $\beta_1V_{\text{module}}$ from the first string and $\beta_2V_{\text{module}}$ from the second string, thus the total power output is ($\beta_1 + \beta_2)V_{\text{module}} = 1.7V_{\text{module}}$. This explains Eq. (24).

If $\alpha = 2$, there are two modules generating electricity in each string, the rearrangement (0.9 pu, 0.8 pu, 0.4 pu; 0.7 pu, 0.5 pu, 0.2 pu) will produce the maximum power. The maximum power is calculated by ($\beta_2 + \beta_2)V_{\text{module}} = 2\beta_2V_{\text{module}}$ for the first string and ($\beta_4 + \beta_4)V_{\text{module}} = 2\beta_4V_{\text{module}}$ for the second string. The total power is $2(\beta_2 + \beta_4)V_{\text{module}} = 2.6V_{\text{module}}$. This explains Eq. (25).

If $\alpha = 3$, all the three modules in a string generate electricity, and the rearrangement (0.9 pu, 0.8 pu, 0.7 pu; 0.5 pu, 0.4 pu, 0.2 pu) will generate the maximum power. The maximum power is calculated by ($\beta_3 + \beta_3 + \beta_3)V_{\text{module}} = 3\beta_3V_{\text{module}}$ for the first string and ($\beta_6 + \beta_6 + \beta_6)V_{\text{module}} = 3\beta_6V_{\text{module}}$. The
total maximum power is \( 3(\beta_1 + \beta_2) V_{\text{module}} = 2.7 V_{\text{module}} \). This explains Eq. (27). Clearly, this maximum power is greater than that for the unarranged arrays (2.6 \( V_{\text{module}} \)).

Now the general proposition can be proved by applying mathematical induction to \( a \). The proof for \( a = 1 \) is easy and now consider the case to deduce the statement for \( a = 2 \) from \( a = 1 \), while the general proof is omitted as it is a simple repetition of this proof for \( a = 2 \). In fact, for \( a = 2 \), we can assume the maximum short-circuit currents of the two un-bypassed PV modules in the \( l \)-th string are \( \gamma_l^1 \) and \( \gamma_l^2 \), \( l = 1, 2, \ldots, p \). Without loss of generality, we can further assume that \( \gamma_1^1 > \gamma_2^1 > \gamma_3^1 > \ldots > \gamma_p^1 > \gamma_{p+1}^1 \) and \( \gamma_1^1 > \gamma_2^1 > \gamma_3^1 > \ldots > \gamma_p^1 > \gamma_{p+1}^1 \). Then the maximum power generated, denoted by \( P^*_{\text{module}} \), is

\[
P^*_{\text{module}} = 2(\gamma_1^2 + \gamma_2^2 + \gamma_3^2 + \ldots + \gamma_p^2) V_{\text{module}} \quad (28)
\]

By definition of \( \beta_1, \beta_2, \ldots \), and \( \beta_{ps} \) in (23), \( \beta_2 \) is the second largest maximum short-circuit current within these \( ps \) modules. \( \gamma_{p+1}^1 \) is not the largest PV module maximum short-circuit current as there is \( \gamma_l^1 \) which is greater than \( \gamma_2^1 \). Therefore, \( \beta_2 \geq \gamma_2^1 \). Similar reasoning deduces that \( \beta_1 \geq \gamma_1^2, \ldots, \beta_{ps} \geq \gamma_p^2 \),

\[
P^*_{\text{module}} = 2(\beta_1 + \beta_2 + \beta_3 + \ldots + \beta_{ps}) \quad (28)
\]

Then, \( P^*_{\text{module}} \) is the maximum possible power output for \( a = 2 \).

**B. PV Module Rearrangement Algorithm**

Assume the maximum short-circuit currents of all the PV modules are given by \( \{I_{\text{module},j,k}\} = 1, \ldots, p; \ k = 1, \ldots, s \} \), and it is re-arranged from the highest to lowest as in Eq. (23) through four steps.

**Step 1:** Calculate \( P^*_{\text{module}} \), \( P^*_{\text{module}} \), \( P^*_{\text{module}} \), \ldots, \( P^*_{\text{module}} \) from Eq. (25).

**Step 2:**

Find the maximum from \( \{P^*_{\text{module}}, P^*_{\text{module}}, P^*_{\text{module}}, \ldots, P^*_{\text{module}}\} \) and define the maximum as \( P^*_{\text{module}} \) where \( s^* \) is an integer from \( \{1, 2, 3, \ldots, s\} \) so that

\[
P^*_{\text{module}} = \max\{P^*_{\text{module}}, P^*_{\text{module}}, P^*_{\text{module}}, \ldots, P^*_{\text{module}}\}.
\]

This implies that each PV string has \( s^* \) non-bypassed modules (generating electricity) when the maximum power output of the PV array is achieved.

**Step 3:**

Rearrange the PV modules as follows:

1. **3.1** Group the modules with maximum short-circuit currents \( \beta_1, \beta_2, \ldots, \beta_s \) in the first PV string.
2. **3.2** Group the modules with maximum short-circuit currents \( \beta_{s+1}, \beta_{s+2}, \ldots, \beta_{2s} \) in the second PV string.
3. **3.3** Group the modules with maximum short-circuit currents \( \beta_{2s+1}, \beta_{2s+2}, \ldots, \beta_{3s} \) in the third PV string which is different to 3.1 and 3.2.
4. **3.4** Repeat the above procedure to place modules with maximum short-circuit currents \( \beta_{3s+1}, \beta_{3s+2}, \ldots, \beta_{4s} \), \( \beta_{4s+1}, \beta_{4s+2}, \ldots, \beta_{5s} \), \ldots, \( \beta_{(p-1)s+1}, \beta_{(p-1)s+2}, \ldots, \beta_{ps} \), and ensure that each of these \( \beta_{js+1}, \beta_{js+2}, \ldots, \beta_{(j+1)s} \), \( 3 \leq j \leq p-1 \), must occupy a different string.

**3.4** Place the remaining \( (ps-ps^*) \) PV modules arbitrarily in the remaining places of the \( p \) strings. Note that each string has \( (s-s^*) \) unoccupied places to accommodate PV modules. Therefore, there are \( (ps-ps^*) \) remaining places in these \( p \) strings.

This algorithm can be illustrated by the following flowchart.

![Flowchart](Image)

**V. ANALYTICAL STUDIES**

**A. Simplified Non-Uniform Aging Cases**

A \( 2 \times 2 \) PV array is employed in case studies where the maximum short-circuit current of each PV module is given in per unit (pu). The specifications of the PV modules are tabulated in Table I. The healthy PV module has the maximum short current, which is marked as 1 pu. The PV array aging condition can be expressed as 1 pu, 0.5 pu; 0.2 pu, 0.1 pu to represent the conditions from healthy to aged. When PV array connected as (1 pu, 0.1 pu; 0.5 pu, 0.2 pu), their output curve is shown in Fig. 7.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Open-circuit voltage</td>
<td>44.8 V</td>
</tr>
<tr>
<td>Short-circuit current</td>
<td>5.29 A</td>
</tr>
<tr>
<td>Power output</td>
<td>180 W</td>
</tr>
<tr>
<td>MPP current</td>
<td>5 A</td>
</tr>
<tr>
<td>MPP voltage</td>
<td>36 V</td>
</tr>
<tr>
<td>Current temperature coefficient</td>
<td>0.037% K</td>
</tr>
<tr>
<td>Voltage temperature coefficient</td>
<td>-0.34% K</td>
</tr>
<tr>
<td>Power temperature coefficient</td>
<td>-0.48% K</td>
</tr>
<tr>
<td>Nominal operating cell temperature</td>
<td>46 ±2°C</td>
</tr>
</tbody>
</table>
Following Step 1 of the reconfiguration algorithm, $p=s=2$ these the maximum short-circuit currents can be re-ordered as: $\beta_1=1>\beta_2=0.5>\beta_3=0.2>\beta_4=0.1$. Therefore, the maximum power output is $P_{\text{max}}=\max\{(1+0.5)V_{\text{module}}(\text{pu})\}, 2(0.5+0.1)V_{\text{module}}(\text{pu})\}=1.5V_{\text{module}}(\text{pu})$. This maximum power is achieved by choosing only one module from each string for electricity generation, i.e., $s^*=1$. The existing sequence of the PV modules in this PV can generate this maximum power. Therefore, there is no need for rearrangement.

Note that there are only three options for rearrangement: (1 pu, 0.1 pu; 0.5 pu, 0.2 pu), (1 pu, 0.5 pu; 0.1 pu, 0.2 pu) and (1 pu, 0.2 pu; 0.1 pu, 0.5 pu) where the notation $(a, b; c, d)$ indicates that the two modules $(a$ and $b)$ with the maximum short-circuit currents are placed in one string, and the other two modules $(c$ and $d)$ are in another string. These are simulated in Fig. 10(a) and (b). It is clear that the arrangements (1 pu, 0.1 pu; 0.5 pu, 0.2 pu) and (1 pu, 0.2 pu; 0.1 pu, 0.5 pu) provide the identical maximum power (224 W) while the arrangement (1 pu, 0.5 pu; 0.1 pu, 0.2 pu) has the maximum power of 207 W. The arrangement (1 pu, 0.2 pu; 0.1 pu, 0.5 pu) has also the maximum power 1.5pu$V_{\text{module}}$. Obviously, the output powers in Fig. 7 and Fig. 8(b) are both 224 W, suggesting a good agreement between the analytical and simulation results.

The second case is for the 2 $\times$ 2 PV array with the aging parameters of (1 pu, 0.3 pu; 0.5 pu, 0.4 pu). The output power is obtained by simulation and presented in Fig. 9.

From Step 1 of the reconfiguration algorithm, $p=s=2$, these maximum short-circuit currents can be re-ordered as: $\beta_1=1>\beta_2=0.5>\beta_3=0.4>\beta_4=0.3$. The maximum power is given by $P_{\text{max}}^*=\max\{(1+0.5)V_{\text{module}}(\text{pu})\}, 2(0.5+0.3)V_{\text{module}}(\text{pu})\}=1.6V_{\text{module}}(\text{pu})$. That is, $s^*=2$ and all the modules must generate electricity. From Step 3.1, the two modules with maximum short-circuit currents $\beta_1=1$ and $\beta_2=0.5$ are placed in one string while the other two modules with $\beta_3=0.4$ and $\beta_4=0.3$ are in another string. Therefore, the maximum power output can be achieved by the arrangement option (1 pu, 0.5 pu; 0.4 pu, 0.3 pu).

Similar to case 1, there are three possible options in case 2: (1 pu, 0.3 pu; 0.5 pu, 0.4 pu), (1 pu, 0.4 pu; 0.5 pu, 0.3 pu), and (1 pu, 0.5 pu; 0.4 pu, 0.3 pu). It can be seen from Figs. 9 and 10 that the maximum power output from the three rearrangements are 238 W, 244 W, and 273 W, respectively. Therefore, the re-arranged PV array can gain 35 W more power than the original PV array configuration.

From the two case studies, the proposed rearrangement strategy can effectively improve the output power of non-uniformly aged PV arrays. Furthermore, in the process of the rearrangement, the MPP voltage area can be located which assists in the online maximum power point tracking (MPPT). Taking case 1 for example, the global MPP is located in the MPP area of one module. In case 2, the global MPP is located in the MPP area of two modules while the exact global MPP voltage is determined by the module temperature.
B. General Non-Uniform Aging Cases

For general non-uniform aging modules, it is very difficult to obtain any results similar to the obtained proposition. Consider a \( p \times s \) PV array with 3 cell-units in each PV module. The total number of possible arrangements of the PV modules is \( \binom{p}{s} \binom{ps-s}{3} \binom{ps-2s}{3} \cdots \binom{ps-3s}{3} \binom{s}{3} / p! \), which is a huge number when \( p \) or \( s \) is big. For example, when \( p=5, s=10 \), this number equals \( 4.0279 \times 10^9 \). Therefore, it is very difficult to calculate the maximum power for all the possible PV module arrangements for large \( p \) or \( s \) by enumerative search. Algorithms from combinatorial optimization (e.g. branch and bound methods) can be applied to search for the optimal maximal power when the number of possible rearrangements is huge.

Table II presents an example of a \( 3 \times 3 \) array with the general non-uniform aging PV array with 3 cell-units in each PV module. For this PV array, there are \( \binom{9}{3} \binom{9}{3} \binom{9}{3} / 3! = 280 \) possible rearrangement options. Assume the PV arrays are arranged as in Table II where the maximum short-circuit currents of 3 cell-units in a PV module are put in a pair of parentheses. For instance, the option (0.9 pu, 0.8 pu, 0.7 pu) indicates the maximum short-circuit currents of the 3 cell-units in the first PV module.

Assuming the output voltage to be fixed at \( \alpha V_{cu} \), \( \alpha = 1, 2, \ldots, 9 \). In this case, the maximum power output can be calculated by rating the maximum power output of all possible \( \alpha \). By doing so, the maximum power is found to be 10.5 pu \( V_{cu} \) at \( \alpha = 7 \).

Table III illustrates alternative PV module rearrangements for the maximum power output out of possible 280 options. The global maximum power is 12 pu \( V_{cu} \) when the voltage is 8 pu \( V_{cu} \). Compared to the original maximum power (10.5 pu \( V_{cu} \)), this arrangement has improved by 12.5% in power output.

C. Optimal PV Rearrangement under Converter Input Voltage Limit

Due to the limitation of inverter operations while PV arrays are connected to the grid, the minimum bus voltage of a single phase inverter should be higher than 311V (220V/50Hz); and the minimum bus voltage of three phase inverter should be higher than 538V (380V/50Hz). The corresponding PV array operation points must be higher than the minimum bus voltage in a single stage converter. Therefore, the working voltage limit is introduced to the PV module reconfiguration strategy. The Proposition and algorithm in Section IV.B can be revised as follows to cater for this voltage limit. In fact, assume that a converter input voltage limit requires the input voltage to be \( V_{high} \) at least. Then it is straightforward that the maximum possible power output is:

\[
\max \{ P_i^{max} : s \geq i \geq \theta \}.
\]

And the searching algorithm in Section IV.B only needs to search for those \( P_i^{max} \) with \( i \geq \theta \).

VI. IMPLEMENTATION AND EXPERIMENTAL VALIDATION

In order to validate the proposed strategy, a 9 kW array under a non-uniform aging condition is used for simulation and experimental tests. Three cases representing PV array without rearrangement, rearrangement without considering working voltage limit and rearrangement with considering working voltage limit are investigated below.

A. Simulation

Case 1:

A PV array model is built in Matlab. The per-unit maximum short-circuit current for each PV module in the \( 5 \times 10 \) PV array \( (p=5, s=10) \) is tabulated in Table IV. The corresponding output characteristics are calculated and presented in Fig. 11. Without a rearrangement, the maximum output power is 4587 W.
In this PV array, there are $\alpha$ modules generating electricity in each string, while the rest $(10-\alpha)$ modules are bypassed by diodes. $\alpha$ is between 1 and 10. It suffices to calculate the maximum power for each $\alpha$ and then find the greatest power from the 10 calculations. Firstly, let us sort the maximum short-circuit currents for PV strings from largest to smallest, as in Table V.

$$\begin{align*}
\text{Maximum short-circuit currents (pu)} & = 0.9, 0.8, 0.8, 0.8, 0.8, 0.8, 0.8, 0.8, 0.7, 0.7, 0.7, 0.7, 0.7, 0.7, 0.7, 0.7, 0.6, 0.6, 0.6, 0.5, 0.5, 0.5, 0.5, 0.4, 0.4, 0.4, 0.4, 0.3, 0.3.
\end{align*}$$

Now consider the optimal PV module rearrangement. The maximum short-circuit currents are re-organized from the highest to lowest as follows:

- For $\alpha = 1$, the maximum power is given by
  $$V_{\text{module}} = (0.9 + 0.9 + 0.8 + 0.9 + 0.9) \text{ pu} = 4.4 V_{\text{module}} \text{ (pu)}$$
  \quad (29)

- For $\alpha = 2$, the maximum power is
  $$V_{\text{module}} = 2 \times (0.9 + 0.9 + 0.8 + 0.8 + 0.9) \text{ pu} = 8.6 V_{\text{module}} \text{ (pu)}$$
  \quad (30)

Similarly, for $\alpha = 3, 4, \ldots, 10$, the maximum powers are calculated as:

- $12.3 V_{\text{module}} \text{ (pu)}$,
- $15.6 V_{\text{module}} \text{ (pu)}$,
- $19.5 V_{\text{module}} \text{ (pu)}$, $22.8 V_{\text{module}} \text{ (pu)}$,
- $25.9 V_{\text{module}} \text{ (pu)}$, $26.4 V_{\text{module}} \text{ (pu)}$, $24.3 V_{\text{module}} \text{ (pu)}$,
- $20 V_{\text{module}} \text{ (pu)}$. Therefore, the maximum power output is $26.4 \text{ pu}$ $V_{\text{module}}$ when there are 7 PV modules in each PV string generating electricity.

Now consider the optimal PV module rearrangement. The maximum short-circuit currents are re-organized from the highest to lowest as follows:

- $0.9 \text{ pu}$ $0.9 \text{ pu}$ $0.9 \text{ pu}$ $0.9 \text{ pu}$ $0.9 \text{ pu}$ $0.9 \text{ pu}$ $0.9 \text{ pu}$ $0.8 \text{ pu}$ $0.8 \text{ pu}$ $0.8 \text{ pu}$ $0.8 \text{ pu}$ $0.8 \text{ pu}$ $0.8 \text{ pu}$ $0.8 \text{ pu}$ $0.8 \text{ pu}$ $0.8 \text{ pu}$ $0.8 \text{ pu}$ $0.8 \text{ pu}$ $0.8 \text{ pu}$ $0.8 \text{ pu}$ $0.8 \text{ pu}$ $0.8 \text{ pu}$ $0.7 \text{ pu}$ $0.7 \text{ pu}$ $0.7 \text{ pu}$ $0.7 \text{ pu}$ $0.7 \text{ pu}$ $0.7 \text{ pu}$ $0.7 \text{ pu}$ $0.7 \text{ pu}$ $0.6 \text{ pu}$ $0.6 \text{ pu}$ $0.6 \text{ pu}$ $0.5 \text{ pu}$ $0.5 \text{ pu}$ $0.5 \text{ pu}$ $0.5 \text{ pu}$ $0.4 \text{ pu}$ $0.4 \text{ pu}$ $0.4 \text{ pu}$ $0.4 \text{ pu}$ $0.3 \text{ pu}$.

According to Eq. (23), $\beta_1 = 0.9, \beta_2 = 0.9, \ldots, \beta_{10} = 0.3$.

Following Steps 1 and 2 in the reconfiguration algorithm, the maximum power is now calculated by:

$$V_{\text{module}} = \max\{4.5 \text{pu}, 8.8 \text{pu}, 12.6 \text{pu}, 16.8 \text{pu}, 20.5 \text{pu}, 24 \text{pu}, 28 \text{pu}, 30.4, 32.4, 32\} = 32.4 V_{\text{module}} \text{ (pu)}$$

This corresponds to the case that the output voltage is $9 V_{\text{module}} \times s^*=9$. There are 9 PV modules in each string which generate electricity. Given that the original maximum power output is only $26.4 V_{\text{module}} \text{ (pu)}$, this re-arranged PV array can generate $32.4 V_{\text{module}} \text{ (pu)}$. This is because those six modules are brought back to the generation side by the reorganization (see Table VI). The corresponding output characteristics are illustrated in Fig. 12. As can be seen that the maximum output power is 5242 W with the rearrangement, which is 655 W more than that without the rearrangement (4587 W). Obviously, its energy efficiency is improved by increasing 14.28% power generation.

Table VI is constructed by the rearrangement algorithm as follows. From Step 3.1, 9 modules with the maximum short-circuit currents (0.9 pu 0.9 pu 0.9 pu 0.9 pu 0.9 pu 0.9 pu 0.9 pu 0.9 pu 0.9 pu 0.8 pu) are grouped in the first string. From Step 3.2, further 9 modules with the current of (0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu) are placed in the second string. When $j = 2, 3, 4, 27$, their respective modules are put in the third, fourth and fifth strings following Step 3.4. Now, 45 PV modules are reorganized in the PV array, leaving 5 modules un-sorted. These 5 modules have the maximum short-circuit currents of 0.4 pu, 0.4 pu, 0.4 pu and 0.3 pu. Since each string has only one unoccupied place, the 5 modules can be arbitrarily placed to fill the gap, as instructed in Step 3.5. The remaining modules in each of the 5 strings is bypassed and become idle; they are not in operation. The bucket effect determines that all first 9 PV modules in each string with higher maximum short circuit currents are operational to generate power.
Following a similar procedure as the previous example, the maximum power output equals $10 \, V_{\text{module}}$, which is achieved when all the 50 modules are activated to generate electricity. Now consider the optimal rearrangement. From the algorithm in Section IV-B, it is easy to find that the maximum power is $11.4 \, V_{\text{module}}$ (pu), which can be achieved by allowing 6 modules generating electricity in each PV string, and the corresponding I-V curves are presented in Fig. 14.

<table>
<thead>
<tr>
<th>TABLE IV THE 5×10 PV ARRAY WITHOUT REARRANGEMENT IN CASE 1</th>
</tr>
</thead>
<tbody>
<tr>
<td>Row (string)</td>
</tr>
<tr>
<td>0.8 pu 0.8 pu 0.3 pu 0.6 pu 0.8 pu 0.9 pu 0.8 pu 0.9 pu 0.6 pu 0.9 pu</td>
</tr>
<tr>
<td>0.8 pu 0.8 pu 0.4 pu 0.7 pu 0.9 pu 0.7 pu 0.8 pu 0.8 pu 0.8 pu 0.9 pu</td>
</tr>
<tr>
<td>0.8 pu 0.8 pu 0.8 pu 0.7 pu 0.6 pu 0.5 pu 0.5 pu 0.7 pu 0.7 pu 0.7 pu</td>
</tr>
<tr>
<td>0.8 pu 0.8 pu 0.7 pu 0.7 pu 0.9 pu 0.4 pu 0.4 pu 0.7 pu 0.8 pu 0.8 pu</td>
</tr>
<tr>
<td>0.8 pu 0.8 pu 0.8 pu 0.7 pu 0.7 pu 0.7 pu 0.9 pu 0.5 pu 0.4 pu 0.9 pu</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>TABLE V REARRANGED STRINGS IN CASE 1</th>
</tr>
</thead>
<tbody>
<tr>
<td>Row (string)</td>
</tr>
<tr>
<td>0.9 pu 0.9 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.6 pu 0.6 pu 0.3 pu</td>
</tr>
<tr>
<td>0.9 pu 0.9 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.7 pu 0.7 pu 0.4 pu</td>
</tr>
<tr>
<td>0.8 pu 0.8 pu 0.8 pu 0.7 pu 0.7 pu 0.7 pu 0.7 pu 0.6 pu 0.5 pu 0.5 pu</td>
</tr>
<tr>
<td>0.9 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.7 pu 0.7 pu 0.7 pu 0.4 pu 0.4 pu</td>
</tr>
<tr>
<td>0.9 pu 0.9 pu 0.8 pu 0.8 pu 0.8 pu 0.7 pu 0.7 pu 0.7 pu 0.5 pu 0.4 pu</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>TABLE VI REARRANGEMENT OF THE 5×10 ARRAY IN CASE 1</th>
</tr>
</thead>
<tbody>
<tr>
<td>Row (string)</td>
</tr>
<tr>
<td>0.9 pu 0.9 pu 0.9 pu 0.9 pu 0.9 pu 0.9 pu 0.9 pu 0.8 pu 0.8 pu 0.4 pu</td>
</tr>
<tr>
<td>0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.4 pu</td>
</tr>
<tr>
<td>0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.8 pu 0.4 pu</td>
</tr>
<tr>
<td>0.8 pu 0.7 pu 0.7 pu 0.7 pu 0.7 pu 0.7 pu 0.7 pu 0.7 pu 0.7 pu 0.4 pu</td>
</tr>
<tr>
<td>0.7 pu 0.7 pu 0.7 pu 0.6 pu 0.6 pu 0.6 pu 0.5 pu 0.5 pu 0.5 pu 0.3 pu</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>TABLE VII THE 5×10 PV ARRAY WITHOUT REARRANGEMENT FOR CASE 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>Row (string)</td>
</tr>
<tr>
<td>1 pu 0.7 pu 1 pu 0.2 pu 0.3 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu</td>
</tr>
<tr>
<td>1 pu 0.2 pu 0.2 pu 0.3 pu 0.4 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu</td>
</tr>
<tr>
<td>1 pu 0.3 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu</td>
</tr>
<tr>
<td>0.2 pu 0.2 pu 1 pu 0.3 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu</td>
</tr>
<tr>
<td>0.3 pu 1 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>TABLE VIII THE 5×10 PV ARRAY WITH REARRANGEMENT IN CASE 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>Row (string)</td>
</tr>
<tr>
<td>1 pu 1 pu 1 pu 1 pu 1 pu 1 pu 0.7 pu 0.4 pu 0.3 pu 0.3 pu 0.3 pu</td>
</tr>
<tr>
<td>0.3 pu 0.3 pu 0.3 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu</td>
</tr>
<tr>
<td>0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu</td>
</tr>
<tr>
<td>0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu</td>
</tr>
<tr>
<td>0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu 0.2 pu</td>
</tr>
</tbody>
</table>

Fig. 14 Output characteristics of the 5×10 array with the rearrangement (case 2).
B. Experimental Tests

In the experiment, a 1620 W 3×3 array is employed to verify the proposed technique based on the availability. The PV module parameters are identical to those in Table I. The aging condition is realized by covering the two modules (PV21 and PV31) with plastic membrane. The test results are given in Fig. 15. The array output characteristics are obtained and presented in Table IX and Fig. 15 before and after the rearrangement. For the PV array without the reconfiguration presented in Fig. 15(a), its maximum output power is 520 W, shown in Fig. 15(b). After applying the proposed strategy to the PV array, the PV array is rearranged (by swapping PV21 and PV32 positions), as shown in Fig. 15(c). Experimental results show that the maximum output power in the rearranged array is 590 W, illustrated in Fig. 15(d), which increases 13.5%. Furthermore, because of this rearrangement, the global MPP shifts from a two-module MPP area to a three-module MPP area, which can be directly used for the online global MPPT.

<table>
<thead>
<tr>
<th>Component</th>
<th>Before rearrangement</th>
<th>After rearrangement</th>
</tr>
</thead>
<tbody>
<tr>
<td>MPP voltage</td>
<td>67.6 V</td>
<td>100 V</td>
</tr>
<tr>
<td>MPP current</td>
<td>7.7 A</td>
<td>5.9 A</td>
</tr>
<tr>
<td>Power level</td>
<td>520 W</td>
<td>590 W</td>
</tr>
</tbody>
</table>

VII. CONCLUSION

Non-uniform aging of PV modules is a common phenomenon in the PV power plants since they often operate a long time in harsh environmental conditions. The non-uniform aging decreases the PV array maximum output power and can damage the PV modules if left untreated. Without rearranging non-uniformly aged PV arrays, typical online global-MPPT schemes can only track a compromised maximum rather than its potential maximum power.

This paper has presented a new PV array reconfiguration strategy to maximize the power generation of non-uniformly-aged PV arrays without replacing aged PV
modules. It is found that the bucket effect is the key factor affecting the operating mechanisms of PV arrays under non-uniform aging conditions. The cell-unit structure of PV module is investigated to study the aging characteristics of PV modules. The mathematical models for non-uniformly aged PV arrays are built. An optimized reconfiguration algorithm is developed to take the full use of aged PV array for maximum power output. The proposed strategy has been tested by simulated on three cases and validated by experiments on a 1620-W PV array.

While the existing online reconfiguration methods may provide online reconfiguration in real time for small PV arrays but require large amount of relays, auxiliary power supply and high-end controllers. As PV cell aging is a slow process, the feature of online measurement in real time may not be useful to justify the exponential increase in material and computational costs. In contrast, the proposed offline method only needs inexpensive equipment to perform periodic inspections of PV cells (during maintenance). Therefore, the developed technique can significantly improve energy efficiency and cost efficiency of PV systems of any size. It opens one effective approach for condition based maintenance in conjunction with in-situ smart monitoring [17, 21], which is important for large scale aged PV arrays.

<table>
<thead>
<tr>
<th>Item</th>
<th>Online reconfiguration</th>
<th>Proposed reconfiguration</th>
</tr>
</thead>
<tbody>
<tr>
<td>Hardware for Reconfiguration</td>
<td>Number of relays needed for a $p \times s$ array is: $(c_p) = \frac{ps(ps-1)}{2}$</td>
<td>Manual work, no hardware investment</td>
</tr>
<tr>
<td>Hardware for Sensor</td>
<td>(a) PV module conditions (e.g. current and voltage) should be monitored on site (b) Powerful controllers are needed for online sensor signal collection and processing</td>
<td>(a) No sensors installed on site (b) The PV module’s healthy conditions can be monitored by thermal camera when the PV array needs to be maintained. The thermal camera can be rented for short time usage.</td>
</tr>
<tr>
<td>Auxiliary facilities</td>
<td>(a) Power supply for sensors (b) Power supply for relays (c) Signal transmitters</td>
<td>Not needed</td>
</tr>
<tr>
<td>Software (Algorithm differences)</td>
<td>(a) Do not consider cell-unit structure yet (b) Need strong controller to support online computing</td>
<td>(a) Consider cell-unit structure of PV modules (b) Offline computing, no need for high performance controllers</td>
</tr>
<tr>
<td>Recommended PV array size</td>
<td>Small scale PV arrays</td>
<td>Large and small scale PV arrays</td>
</tr>
<tr>
<td>Recommended application scenarios</td>
<td>Small-scale array regularly affected by shadows</td>
<td>Efficiency improvement for non-uniform aging PV arrays</td>
</tr>
</tbody>
</table>

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**REFERENCES**


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