Optimization of nanofluid volumetric receivers for solar thermal energy conversion

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<td>As Published</td>
<td><a href="http://dx.doi.org/10.1016/j.solener.2011.09.029">http://dx.doi.org/10.1016/j.solener.2011.09.029</a></td>
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<td>Publisher</td>
<td>Elsevier</td>
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<tr>
<td>Version</td>
<td>Author's final manuscript</td>
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<td>Accessed</td>
<td>Fri Dec 14 12:07:52 EST 2018</td>
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OPTIMIZATION OF NANOFLUID VOLUMETRIC RECEIVERS FOR SOLAR THERMAL ENERGY CONVERSION

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ABSTRACT

Improvements in solar-to-thermal energy conversion will accelerate the development of efficient concentrated solar power systems. Nanofluid volumetric receivers, where nanoparticles in a liquid medium directly absorb solar radiation, promise increased performance over surface receivers by minimizing temperature differences between the absorber and the fluid, which consequently reduces emissive losses. We present a combined modeling and experimental study to optimize the efficiency of liquid-based solar receivers seeded with carbon-coated absorbing nanoparticles. A one-dimensional transient heat transfer model was developed to investigate the effect of solar concentration, nanofluid height, and optical thickness on receiver performance. Simultaneously, we experimentally investigated a cylindrical nanofluid volumetric receiver, and showed good agreement with the model for varying optical thicknesses of the nanofluid. Based on the model, the efficiency of nanofluid volumetric receivers increases with increasing solar concentration and nanofluid height. The total receiver-side efficiencies are predicted to exceed 35% when nanofluid volumetric receivers are coupled to a power cycle and optimized with respect to the optical thickness and solar exposure time. This work provides insights as to how nanofluids can be best utilized as volumetric receivers in solar applications, such as receivers with integrated storage for beam-down CSP and future high concentration solar thermal energy conversion systems.

Keywords: volumetric receiver, solar, nanofluid, nanoparticle, direct absorption, CSP
1. INTRODUCTION

The use of concentrated sunlight as a thermal energy source for production of electricity promises to be one of the most viable options to replace fossil fuel power plants. However, the peak efficiencies of existing fossil fuel combined cycle power plants exceed 50% (Langston, 2009) while those of concentrated solar power (CSP) plants are below 20% (Pacheco, 2001; Romero et al., 2002). The relatively poor CSP performance is a result of a low solar-to-thermal efficiency (a combination of receiver and field efficiencies) and moderately low operational temperatures in the power cycle. Improving the conversion of incoming solar radiation to thermal energy at high temperatures is essential to improving the overall power conversion efficiency of CSP plants.

Most concentrated solar thermal technologies today use receivers with absorbing surfaces to convert solar energy from its radiative form into thermal energy. These surfaces are typically black or spectrally selective such that high absorptivity in the solar spectrum is coupled with low emissivity in the infrared (Bogaerts and Lampert, 1983). Although surface-based receivers are efficient at solar to thermal conversion, they are not well suited for transferring heat to a carrier fluid. In particular, at high levels of solar concentration, a large temperature difference between the absorber and the fluid arises. The temperature difference leads to significant emissive losses owing to the quartic dependence of thermal re-radiation on the absorber temperature, and correspondingly, a lowering of the overall conversion efficiency of solar energy. Moreover, the material stability of selective surfaces at temperatures above 800 K has not yet been demonstrated (Pitz-Paal and Trevor, 2008). Alternatively, in a volumetric receiver design, concentrated solar radiation is directly absorbed and more uniformly distributed in the surrounding fluid, which decreases the temperature difference between the absorber and the fluid.

Researchers have suggested various configurations for volumetric receiver designs, including: gas-particle suspensions (Bertocchi et al., 2004; Miller and Koenigsdorff, 1991), liquid films (Bohn and Wang, 1988; Caouris et al., 1978), and metal foams (Fend et al., 2004; Pitz-Paal et al., 1997). In this study, we focus on liquid-based volumetric receivers with integrated storage for central receiver CSP systems with beam-down optics (Epstein et al., 1999; Kribus et al., 1998; Yoge et al., 1998); an example configuration was recently described by Slocum et al. (2011) where hillside heliostats focus light onto a molten salt volumetric receiver. The potential advantage of such volumetric receivers (VR) compared to ideal selective surface receivers (SS) is illustrated in the representative schematic temperature profiles of Figure 1. The exact temperature profiles will depend on the flow characteristics in the receivers, but for the same mean fluid temperature \((T_f)\) and solar heat flux \((CG_0)\), the temperature profile in the VR (Figure 1a) can be favorable because the temperature associated with emissive loss is lower than that of the mean fluid temperature (by \(\Delta T\)). This behavior is referred to as “thermal trapping” in solar thermal literature (Arai et al., 1984; Wijeysundera and Thevendran, 1988), but is physically similar to the “greenhouse effect” (Harries, 2000). On the other hand, the unfavorable temperature profile in the SS (Figure 1b) leads to higher emissive losses. Figure 1c highlights the difference in emissive loss (\(\Delta e\)) between an ideal selective surface with an ideal cutoff wavelength equal to 2 \(\mu m\) (purple) and a non-selective volumetric receiver (black) for the case when the mean fluid temperature is equal to 1000 K and \(\Delta T\) is equal to 250 K. Thus, volumetric receivers, despite being non-selective, can trap thermal energy more effectively and lead to higher receiver efficiencies.
Figure 1. Schematic temperature profiles in a) non-selective volumetric receiver (VR) compared to a b) surface-based receiver (SS) for the same incoming concentrated solar flux \( (CGS) \) and height \( (H) \). The VR has a favorable temperature profile with an inverse \( \Delta T \) between the mean fluid temperature \( (T_f) \) and surface temperature \( (T_{VR}, T_{SS}) \). c) The black and purple lines show the emissive loss for a black body \( (\varepsilon=1 \text{ at the VR surface}) \) and an ideal selective emitter with a sharp cutoff at 2 \( \mu \text{m} \) \( (\varepsilon=\varepsilon(T_{ss}) \text{ for the SS}) \), respectively. For the case when \( T_f=1000 \text{ K} \) and \( \Delta T=250 \text{ K} \), the emissive loss \( (\varepsilon T^4) \) decreases by \( \Delta e \) for the VR.

In particular, volumetric receivers with absorbing small particles in suspension have a high surface-to-volume ratio which minimizes the temperature difference between the absorber and the fluid (Hunt, 1978; Miller and Koenigsdorff, 2000). When the particle size is smaller than the characteristic wavelength of sunlight, less material is required to achieve the same amount of absorption (Hunt, 1978), and challenges related to clogging, sedimentation and erosion can be alleviated.

Past research on small-particle liquid suspensions as VRs has focused on thin liquid films and micro/mini-channel designs. Kumar and Tien (1990) developed a model for particle-laden falling liquid films (1-5 mm thick) incorporating the spectral and directional radiative properties of the particles, and provided a framework for future modeling studies. More recently, Tyagi et al. (2009) numerically investigated a low temperature nanofluid receiver inside a mini-channel; while, Otanicar et al. (2009b) extended this model to include multiple and dependent scattering, and size-dependent optical properties. Otanicar et al. (2010) also experimentally demonstrated the use of different nanofluids in a micro-channel solar collector. However, in these previous studies, the effect of increasing height of the absorbing liquid \( (H \text{ in Figure 1a}) \) beyond the millimeter-scale which can lead to lower emissive loss due to the favorable temperature profile was not considered. Arai et al. (1984) investigated transient radiative heating of a static semi-transparent liquid suspension in a taller receiver design (3 cm) and suggested that such a VR
can be highly efficient. Nevertheless, an optimization of small-particle volumetric receivers with respect to particle loading, solar exposure time and nanofluid height has yet to be conducted. As the height of the nanofluid increases, the transient response, representing the thermal charging of these stationary volumetric receivers, becomes a significant portion of the daily operation because of their large thermal inertia.

In this paper, nano-sized (10-100 nm) solid particles are added to a liquid heat transfer fluid (i.e., nanofluid) to volumetrically absorb concentrated solar radiation. We investigate the design of these nanofluid volumetric receivers with nanofluid heights above 1 mm and develop a transient one-dimensional numerical model that examines the effect of solar concentration, nanofluid height, and nanofluid optical thickness on the temperature distribution inside the receiver (Section 2). We studied the effects of varying the optical thickness and validated the numerical model through experiments with a cylindrical nanofluid volumetric receiver, where the radiative and thermophysical properties of the nanofluid were experimentally characterized (Section 3). The model was subsequently used to determine the optimal exposure time and temperature at which point the nanofluid volumetric receiver should be thermally connected to a power generation cycle (Section 4). Throughout this study, a suspension of carbon-coated nanoparticles in Thermolin® VP-1 is used as a model system for nanofluid receivers, but the results can also apply to other nanofluid VRs. The outcomes of the work suggest that nanofluids have significant potential as receivers with integrated storage for beam-down CSP systems and future high concentration solar thermal applications.

2. NUMERICAL MODEL

We developed a one-dimensional numerical model to investigate a stationary volumetric receiver undergoing transient heat conduction in the absence of free convection inside the receiver. A schematic of the volumetric receiver concept is shown in Figure 2a. The nanofluid is contained between two parallel plates separated by a variable height (H); the length of the receiver in the horizontal direction is assumed to be large compared to the height. The incident solar heat flux (CGs), where C represents concentration of solar radiation, is transmitted through the transparent enclosing window and absorbed volumetrically by the suspended nanoparticles. The absorbed radiation results in volumetric heat generation (qgen). The bottom of the receiver is assumed to be adiabatic and specularly-reflective to incident radiation. Radiative heat loss is modeled separately for spectral Band I and II (see Figure 2b). Convective and conductive heat losses are assumed to be negligible in the high temperature regime of interest where radiative loss dominates (Kumar and Tien, 1990).
2.1 RADIATIVE PROPERTIES

An ideal carrier fluid would be completely transparent to the incoming solar radiation so that the radiative properties can be tuned via the nanoparticles by adjusting their volume fraction. Although they are not currently used as volumetric receivers, high temperature heat transfer fluids in existing solar thermal plants such as Therminol\textsuperscript{8} VP-1 (Solutia Inc.) and certain molten salts have solar-weighted absorption below 10\% (Drotning, 1978; Otanicar et al., 2009a). For this reason, we assume that the absorptive index ($k_f$) of the carrier fluid in Band I is much smaller than its refractive index (i.e., $N_f \approx n_f$) in the following treatment.

Suspended nanoparticles with a complex refractive index $N_p$ are utilized to absorb solar radiation in a tunable manner. When the diameter ($D$) of a nanoparticle is small compared to the wavelength of light inside the medium ($x = \pi D n_f / \lambda \ll 1$), the nanoparticle has radiative properties which are well-described by the Rayleigh scattering regime (Bohren and Huffman, 1998). This regime also applies for low volume fraction ($f_v \ll 0.006$) suspensions of polydisperse particles (Brewster and Tien, 1982). If the terms with a higher order of the size parameter are neglected...
(since $x \ll 1$), the particle absorption coefficient ($\kappa_{p,\lambda}$) increases linearly with increasing volume fraction for a given particle material according to:

$$\kappa_{p,\lambda} = \text{Im} \left\{ \frac{m^2 - 1}{m^2 + 2} \right\} \frac{6\pi f_p}{\lambda} \tag{1}$$

where $m = N_p/n_f$ (Bohren and Huffman, 1998; Modest, 2003). Thus, as long as the overall absorption coefficient of the nanofluid is dominated by the nanoparticles, the optical thickness ($\tau_H = \kappa_H H$) for any given nanofluid height ($H$) can be tuned by adjusting the volume fraction ($f_p$) such that most of the solar radiation is absorbed.

For this study, the radiative properties of the nanofluid are approximated using a two-band model. In spectral Band I ($\lambda < 2$ $\mu$m in Figure 2b), the nanofluid is approximated as a gray medium ($\kappa_i \approx \kappa_f$) with a tunable optical thickness and a refractive index equal to one ($n_i = 1$). The gray medium simplification is consistent with the experimental results presented in Section 3.1. In spectral Band II ($\lambda > 2$ $\mu$m), the nanofluid is modeled as fully absorptive ($\varepsilon_{11} = 1$) because the broad vibrational and rotational absorption bands of the liquid are assumed to overlap and dominate the infrared properties ($\kappa_{11} H \gg 1$); this treatment is consistent with previous optical measurements and models of liquids used for direct absorption receivers (Webb and Viskanta, 1985).

### 2.2 GOVERNING EQUATIONS

To model this physical situation in Figure 2a, the radiative transport and transient heat equation are coupled and solved for a large range of temperatures. The thermophysical properties ($k$, $\rho$, $c_p$) of the nanofluid are assumed to be the same as the bulk fluid based on effective medium theory (Nan et al., 1997) for the low volume fractions considered in this study ($f_i << 0.01$). Moreover, because the high surface-to-volume ratio of the particles leads to instant heat transfer to the surrounding medium (Hunt, 1978; Miller and Koenigsdorff, 2000), the particles and the fluid are assumed to be at the same temperature and the nanofluid is modeled as a single-phase isotropic fluid. To simplify the model further, we assume that the material properties of the nanofluid are independent of temperature. (The validity of this assumption will depend on the choice of carrier fluid; for example, over the working temperature range of VP-1, $k$, $\rho$, and $c_p$ do not vary by more than a factor of two).

The radiative transfer equation (RTE) along the $\gamma$-direction for spectral Band I (see Figure 2) is described by:

$$\mu \frac{dI_\lambda}{d\gamma} = \kappa_I (I_{bb,\lambda} - I_\lambda) \tag{2}$$

where $I$ is the radiative intensity and $\mu (= \cos \theta)$ defines the direction of the propagating radiation with respect to the $y$-axis (Modest, 2003). The RTE simultaneously describes how the spectral intensity exponentially decays due to absorption and is augmented by thermal re-emission at high temperatures ($I_{bb}$). The scattering terms are assumed to be negligible because $x \ll 1$.

Solar radiation is assumed to be normally incident ($\mu = 1$) on the receiver and approximated using Planck’s black body distribution ($I_{bb,\lambda}$) at an estimated sun’s temperature of 5800 K ($T_s$); $\Omega_S$ is the solid angle of the sun as seen from the Earth (Modest, 2003), and 0.73 accounts for the average attenuation of sunlight through the Earth’s
atmosphere such that the nominal solar flux \( G_s \) is 1000 W/m\(^2\) (1 sun). The top of the receiver is assumed to be transparent \((\tau_r = 1)\) to the incident radiation as well as thermal re-emission from inside the receiver, while the bottom of the receiver is assumed to specularly reflective \((\rho_r = 1)\); hence, the boundary conditions of the RTE are:

\[
\begin{align*}
I_{\lambda}(y = 0, \mu) &= 0.73 \tau_r C_{\Omega} S_{\lambda b b, \lambda}(T_s) \frac{\delta(\mu - 1)}{2\pi}, & 0 \leq \mu \leq 1 \\
I_{\lambda}(y = H, \mu) &= \rho_r I_{\lambda}(y = H, -\mu), & -1 \leq \mu < 0
\end{align*}
\]

where \( \delta \) is the Dirac-delta function (Modest, 2003). We couple the RTE to the thermal model through the divergence of the radiative heat flux. The radiative heat flux inside the receiver is determined by integrating the radiative intensity over all of the possible propagation directions and wavelengths in spectral Band I:

\[
q_r(y) = 2\pi \int_{\lambda=0}^{\lambda_{amb}} \int_{\mu=-1}^{\mu_{amb}} I_{\lambda, \mu}(y) d\mu d\lambda
\]

where the azimuthal component of the solid angle has been integrated to give the \( 2\pi \) pre-factor. Eq. 4 is differentiated with respect to \( y \) to obtain the divergence of the radiative heat flux, which is easily incorporated as a volumetric heating term into the heat transfer equation describing unsteady heat conduction:

\[
\rho c_p \frac{\partial T}{\partial t} = k \frac{\partial^2 T}{\partial y^2} - \nabla q_r
\]

The initial condition and boundary conditions of Eq. 5 are:

\[
\begin{align*}
T(y, 0) &= T_i \\ 
-k \frac{\partial T}{\partial y} \bigg|_{y=0} &= \varepsilon_H \left( \alpha T^4_{amb} - \int_{\lambda=2}^{\lambda_{amb}} \pi I_{\lambda b b, \lambda}(T(0, t)) d\lambda \right) \\ 
\frac{\partial T}{\partial y} \bigg|_{y=H} &= 0
\end{align*}
\]

We model radiative losses in spectral Band II using the boundary condition at the top of the receiver (Eq. 6-b). For fluid temperatures less than \( \approx 800 \) K, most of the emissive losses are dependent on the fluid properties above 2 \( \mu \)m where it acts as a black body; thus, the surface temperature of the volumetric receiver dominates the amount of heat loss in this regime. At high temperatures, however, thermal re-radiation from within the receiver, captured using the RTE equations, becomes important.

### 2.3 SOLUTION METHODOLOGY

An analytical solution to Eqs. 2-6 cannot be obtained due to the quartic dependence of radiation on the temperature profile. Instead we solve this set of equations numerically by separating them into two steps. First, we explicitly
solve the RTE equations (Eqs. 2-4) by separating the intensity into the collimated part (i.e., incident radiation) and the diffuse part (i.e., re-emission), and determining the radiative heat flux through numerical integration of Eq. 4 for a given temperature profile at time \( t_i \). Second, the divergence of the radiative heat flux is found by differentiating Eq. 4 with respect to \( y \), which is then incorporated into the energy equations (Eqs. 5-6) to determine the temperature profile at a subsequent time \( t_{i+1} \). This new temperature profile is subsequently re-introduced into the first step, and the two-step procedure is repeated; the methodology is similar to the one described by Kumar and Tien (1990). To solve Eqs. 5-6, a finite difference scheme is used to solve the equations and the boundary conditions along the \( y \)-direction, while the 4th order Runge-Kutta method is used to step explicitly in time. A mesh refinement study along the \( y \)-direction is performed until the maximum variance in the temperature profile is below 0.01 K. An energy balance is performed for each solution to ensure energy conservation.

2.4 TEMPERATURE PROFILES

Figure 3 shows transient temperature profiles of the nanofluid obtained with the numerical model. In all three cases and throughout this study, typical values for the thermophysical properties of Therminol® VP-1 at room temperature were used (\( k = 0.1357 \) W/mK; \( \rho = 1060 \) kg/m3; \( c_p = 1570 \) J/kgK); for simplicity, they are assumed not to vary with temperature. Although VP-1 begins to break down around 650 K (Moens and Blake, 2008), we extrapolate the material properties of VP-1 to higher temperatures, assuming that molten salts can replace VP-1 as the carrier fluid without significantly altering our model because they have similar radiative properties (Drotning, 1978; Webb and Viskanta, 1985). The initial temperature of the nanofluid is set to room temperature (300 K). With these parameters fixed, the numerical model is used to investigate the effect of solar concentration (\( C \)), nanofluid height (\( H \)), and optical thickness (\( \tau_H \)).
Figure 3. Developing temperature profiles for volumetric receivers from the model with $\tau_H = 1.7$ and varying solar concentrations and nanofluid heights: a) $C = 25, H = 2.5$ cm, b) $C = 100, H = 2.5$ cm, c) $C = 100, H = 10$ cm. The profiles were obtained at regular time intervals: a,c) 5 mins, b) 1.25 mins. The red profiles indicate inverted temperature profiles (i.e., the bulk mean temperature exceeds the top surface temperature).
In this sub-section, we explore the effects of $H$ and $C$ on the developing temperature profiles while maintaining a constant $t_H = 1.7$ (the reason for this choice of $t_H$ will become apparent in Section 4). Figure 3a shows temperature profiles in a 2.5 cm receiver with 25 suns of incident solar radiation ($CG_s = 25 \text{ kW/m}^2$); in Figure 3b, $H$ remains the same while $C$ is quadrupled ($CG_s = 100 \text{ kW/m}^2$); and lastly, in Figure 3c, the height is quadrupled ($H = 10 \text{ cm}$) while $C$ is maintained at 100.

The results in all three cases show that, initially, the temperature at the top of the receiver is higher than the bulk. However, as the temperature profiles develop, the top surface becomes nearly fixed at a temperature while the mean fluid temperature continues to increase leading to inverted temperature profiles (i.e., the bulk mean temperature exceeds the top surface temperature). This temperature profile inversion, characteristic of all three sets of developing profiles, occurs between 600-800 K because the radiative losses from the top surface begin to balance the local solar heat generation in that area, while the rest of the fluid continues to absorb solar radiation and rise in temperature. As temperatures above 1000 K are reached locally in the profile, thermal re-radiation from within the volumetric receiver becomes more important. The radiative mechanism of heat exchange between the relatively hotter and colder spots inside the receiver is more effective than pure conduction, leading to near isothermal profiles at high temperatures in the lower regions of the receiver ($0.2 < y/H < 1$).

A comparison of Figure 3a with 3b shows that increasing the incident solar heat flux (by increasing $C$) results in increased curvature in the temperature profiles; furthermore, the profiles begin to approach steady state at shorter exposure times and at higher mean temperatures. Similarly, when the nanofluid height is quadrupled (from 3b to 3c), the profile curvature is even more pronounced; however, the exposure time needed to reach the same temperatures as before is inversely proportional to the height. Thus, with increasing $C$ and decreasing $H$, higher temperatures are achieved in shorter periods of time. This result is intuitive if we approximate the behavior of the nanofluid with a lumped capacitance model.

The numerical results also indicate that the profile inversion is more pronounced for taller receivers. Based on the magnitude of the profile inversion and Figure 1, the results suggest that the receiver efficiency increases with increasing $C$ and $H$. These effects will be explored further in Section 4, but first, the numerical model is compared to experiments in Section 3.

3. EXPERIMENTAL STUDY

3.1 NANOFLUID PREPARATION AND PROPERTIES

Carbon-coated cobalt nanoparticles (NanoAmor Inc.) suspended in Therminol® VP-1 were prepared and studied in this work. C-Co nanoparticles were chosen because graphite has a predictable broadband absorption in the visible and near-IR spectrum. The magnetic (cobalt) core of the nanoparticles could potentially be utilized to control the distribution of the particles inside the receiver; this topic, however, is beyond the scope of this study. Therminol® VP-1 was chosen because of its optical transparency and widespread use in solar thermal power plants.
Figure 4. a) Scanning electron micrograph (SEM) and b) Transmission electron micrograph (TEM) of carbon-coated cobalt nanoparticles (NPs) with an average diameter of 28 nm. c) Image of C-Co/VP-1 nanofluid at varying volume fractions ($f_v$) compared to pure Therminol® VP-1. d) Spectral absorption coefficient ($\kappa_{p,\lambda}$) of NPs in suspension at corresponding volume fractions ($f_v$). Inset shows the linear dependence of $\kappa_{p,\lambda}$ with $f_v$ for two wavelengths, $\lambda$=0.55µm and $\lambda$=1.5µm.

Figure 4 shows images of the nanoparticles (NPs) obtained in a high-resolution SEM (Figure 4a) and TEM (Figure 4b). The average diameter of the predominantly spherical nanoparticles is 28 nm according to the manufacturer. The nanoparticles readily dispersed and suspended in Therminol® VP-1 after 30 minutes in a sonicating bath. The suspensions did not require any surfactant to achieve stability exceeding several days.

To determine the radiative properties of the nanoparticles, a differential measurement technique was performed using a spectrophotometer (Cary 500i, Varian Inc.). For this measurement, cuvettes of equal pathlengths (10 mm) were used, and the difference in transmission between a sample of nanofluid and a reference of pure VP-1 was determined. The measurement technique is similar to the one recently described by (Sani et al., 2010). The effects of scattering and multiple reflections through media of different optical thickness are assumed to be negligible.

Suspensions of the carbon-coated NPs in VP-1 (C-Co/VP-1) with varying volume fractions were prepared, ranging from 2.5 ppm ($f_v = 2.5E-6$) to 10 ppm ($f_v = 10E-6$). The experimental results for the spectral absorption coefficient at three different volume fractions are plotted in Figure 4d showing a slight decay in absorption over the range of wavelengths and a general increase in absorption coefficient with increasing $f_v$. Since the resulting volumetric heat generation is obtained through an integration over the wavelength range of incident solar radiation
and the absorption characteristics of the C-Co NPs in suspension are not a strong function of wavelength over this range, a solar-weighted absorption coefficient can be used to approximate the resulting volumetric heat generation. This approximation agrees well with the two-band model suggested in Section 2.1. A line of best fit was determined relating each spectral absorption coefficient to the volume fraction, as shown in the inset of Figure 4d for two particular wavelengths. The experimentally determined linear relationship between \( f_v \) and \( \kappa_{\lambda, f} \) agrees with Eq. 1 and the simplifications made in Section 2.1. The absorption coefficient of Therminol® VP-1 (\( \kappa_{\lambda, f} \)) was deduced from measurements taken by Otanicar et al. (2009a). Using the experimentally determined slope of best fit at each wavelength (\( b_{\lambda, f} \)), the effective absorption coefficient of the nanofluid (\( \kappa_{\lambda} \)) is predicted as a function of the volume fraction according to Eq. 7.

\[
\kappa_{\lambda} = \kappa_{f,\lambda} + b_{\lambda, f} f_v
\]  

(7)

To determine the volume fraction needed for a particular optical thickness (\( \tau_H \)), a simple iterative algorithm using the semi-empirical approach described above was used in this study. For example, for the 6 cm tall receiver studied in Section 3.2 and the spectrum illustrated in Figure 5b, the corresponding volume fraction is 4.3 ppm for \( \tau_H = 4 \). A relatively high volume fraction suspension was initially prepared (\( f_v = 0.001 \)); then, it was diluted in multiple steps with VP-1 to obtain the needed volume fraction.

<table>
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<th>Target Opt. Thick. (( \tau_H ))</th>
<th>( f_v ) (ppm)</th>
<th>( k ) (mW/mK) ( ^* )</th>
<th>( c_p ) (kJ/kgK) ( ^<em>^</em> )</th>
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<tr>
<td>Pure Therminol® VP-1</td>
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<td>144.2 +/- 1.4</td>
<td>1.68 +/- .03</td>
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<tr>
<td>1</td>
<td>0.94 +/- .1</td>
<td>145.2 +/- 0.7</td>
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</tr>
<tr>
<td>2</td>
<td>2.1 +/- .1</td>
<td>145.1 +/- 0.8</td>
<td>1.67 +/- .03</td>
</tr>
<tr>
<td>4</td>
<td>4.3 +/- .1</td>
<td>145.0 +/- 0.7</td>
<td>1.67 +/- .03</td>
</tr>
</tbody>
</table>

\( ^* \) at 30 +/- 5 °C, measured using Hot Wire Method

\( ^*^* \) at 31 +/- 1 °C, measured using a differential scanning calorimeter (DSC823 Polymer DSC, Mettler-Toledo)

Table 1 shows the volume fractions needed to achieve several optical thicknesses of the C-Co/VP-1 nanofluid, as well as their corresponding experimentally determined thermophysical properties. The thermal conductivity (\( k \)) of the nanofluids was obtained using the Hot Wire Method (Healy et al., 1976), whereas, the ASTM standard test method (E1269-05) was followed to obtain specific heat (\( c_p \)) using a differential scanning calorimeter (Polymer DSC823, Mettler-Toledo). Within the experimental uncertainty, the data suggests that the thermophysical properties are not significantly affected by the addition of NPs, as expected for such low volume fractions.

3.2 EXPERIMENTAL SETUP

The goal of this experimental study was not to replicate the environmental conditions and solar concentration levels that would be typical of a central-receiver design in the field, but to experimentally demonstrate the concept of a
nanofluid volumetric receiver, study the effect of optical thickness and compare the results to the numerical model developed in Section 2. Figure 5a and c show the main components of the setup, including the solar simulator, beam-down mirror, volumetric receiver, thermocouple array and data acquisition system.

A 1.6 kW solar simulator (SS 1600W Fully Reflective, Scienctech Inc.) was used as the radiative source for the experiments. The spectral power output of the solar simulator is shown in Figure 5b, as well as the spectral attenuation due to absorption along a receiver with \( \tau_H = 4 \). The solar simulator matches with the AM1.5 spectrum well and meets ASTM Class A standards for spectral match, temporal stability and spatial uniformity. Before the experiments, the average radiative heat flux incident on the receiver was measured with a power meter and thermopile detector (1918-C and 818p, Newport Optical) to be \( 2460 \pm 163 \text{ W/m}^2 \).

A custom thin-walled cylinder was machined to hold the nanofluid, shown in Figure 5d. The chamber was fabricated using stainless steel because of its relatively low thermal conductivity (15 W/mK) considering its high structural rigidity and high temperature stability. The chamber was insulated using low-density foam.

Two flanges were used to secure the interchangeable optics to the top and bottom of the cylinder and seal the nanofluid inside. A high-purity quartz window (1357T33, McMaster) sealed the top of the cylinder; while the bottom surface was sealed using an enhanced aluminum mirror (NT46-616, Edmund Optics), acting as a reflector.
The solar simulator weighted transmissivity (0.926) of the quartz window was measured using a spectrophotometer (Cary 5E, Varian Inc.). During the experiments, the radiation from the solar simulator was beamed down to the receiver using an enhanced aluminum mirror (NT32-666, Edmund Optics); a laser-cut piece of reflective plastic was used to shield the thermocouples from direct radiation in order to more accurately measure the surrounding fluid temperature.

Temperature measurements were taken using type-K thermocouple probes (KMQXL-062G-6, Omega); the probes extended to the centerline of the receiver and were spaced 1 cm apart along the height of the receiver. Seven temperature measurements along the 6 cm height were measured simultaneously for 12 minutes, beginning at the instant the simulated solar radiation reached the receiver.

A data acquisition system was used to record the temperature of each thermocouple averaged over one second. The thermocouple probes were calibrated using a temperature-controlled bath with 0.05 K resolution (RE-207, Lauda-Brinkmann). Measurements of temperature close to the wall of the chamber were typically 1-2 K lower than at the centerline, but the vertical profile was determined to be a weak function of the radial distance away from the centerline.

### 3.3 RESULTS AND COMPARISON WITH NUMERICAL MODEL

Figure 6a, b, and c show experimentally obtained developing temperatures profiles at increments of 100 seconds (triangular symbols) for C-Co/VP-1 nanofluids studied in the test chamber described above with target optical thicknesses of 1, 2 and 4, respectively; the total uncertainty in the temperature measurements is ±1.7 K for 6a, ±0.6 K for 6b and ±0.7 K for 6c. To predict the heat generation profiles (Figure 6 insets), Equation 2 was solved numerically in the cold medium limit (Modest, 2003) using the experimentally determined absorption coefficients (Figure 4d) and the solar simulator spectrum (Figure 5b).
Figure 6. Comparison of the experimentally obtained temperature profiles with numerical results at 100 s intervals for receivers of varying optical thickness: a) $\tau_H = 1$, b) $\tau_H = 2$, c) $\tau_H = 4$. Insets show predicted heat generation profiles based on radiative properties from Figure 4d and solar simulator spectra from Figure 5b.
For all three cases, the shape and decaying nature of the heat generation profile is reflected in the shape of the temperature profiles. With increasing optical thickness, the heat generation profile is increasingly localized to the top of receiver where most of the losses occur.

The numerically predicted temperature profiles (black lines) are shown for the same time increments as the experimental data. To predict these profiles, the numerical model (described in Section 2) was solved using the solar simulator spectrum as the input radiation and the experimental thermophysical properties and absorption coefficients. A convective heat loss coefficient from the top surface \( h_{NC} = 5 \text{ W/m}^2\text{K} \) was calculated analytically and added because the experiments were conducted at temperatures below 350 K where the relative importance of natural convection cannot be neglected as compared to radiative loss. Also, because of the transient nature of the experiment and the comparable vertical \( (H = 6 \text{ cm}) \) and horizontal lengths \( (6.35 \text{ cm inner diameter}) \) of the receiver, our 1-D numerical model was modified for comparison with the experimental results. By design, the walls and optics directly in contact with the nanofluid are thin enough \( (Bi << 1/6) \) to be approximated as being at the same temperature as the fluid. Based on a measured weight and heat capacity, the total heat capacitance of the walls is 222 J/K, while that of the nanofluid is 288 J/K. Thus, a significant portion of the thermal energy is stored in the sidewalls. Using a lumped capacitance model, we estimated that 56.5 % of the incident energy results in heating the nanofluid, while the rest of the energy is stored in the sidewalls. By incorporating this scaling factor (which can be estimated \( a \text{ priori} \)), the model and experimental results show good agreement. These types of application-dependent improvements on the basic model from Section 2 can be obtained and implemented.

The main discrepancy between the model and experimental results is evident in the temperature profiles near the top surface for \( \tau_H = 4 \) \( (6c) \); the experimental results show a smaller temperature gradient than that of the model prediction. We attribute the discrepancy to the relatively large difference in temperature between the top and the bottom of the receiver which induces a re-distribution of heat via the conductive side-walls; this conjugate heat transfer is not captured in our model. In general, the good agreement between the model and experiment (within a 20% difference) suggests that the developed model can be used to investigate volumetric receiver efficiency.

4. RECEIVER OPTIMIZATION

In this section, the volumetric receiver design is optimized on the basis of two important metrics for solar thermal applications: receiver efficiency \( (\eta_{\text{rec}}) \), and receiver-side net system efficiency \( (\eta_{\text{sys}}) \). The efficiency of a solar thermal receiver is the ratio of collected thermal energy to the total incident energy (Tyagi et al., 2009):

\[
\eta_{\text{rec}} = \frac{\text{Thermal Energy Stored}}{\text{Incident Solar Energy}} = \frac{mc_p(T_f - T_i)}{CG_iA_{rec}t_{\text{exp}}} \tag{8}
\]

The metric in the above form applies to stationary receivers undergoing transient heating, where \( m \) is the mass of the nanofluid, \( t_{\text{exp}} \) is the total amount of time exposed to solar radiation and \( A_{rec} \) is the top surface area of the receiver.

However, the aim of a solar thermal receiver is not only to convert concentrated solar radiation into thermal energy as efficiently as possible, but also, to achieve the highest possible temperatures while retaining this high
efficiency. The reason to achieve high fluid temperatures becomes evident when a power conversion cycle is placed in series with the solar thermal receiver. Thermal coupling of a stationary volumetric receiver with integrated storage to a power generation system can potentially be achieved through heat exchange with the walls of the nanofluid volumetric chamber or utilizing a flow heat exchanger and a separate cold-storage tank. For simplicity, we assume that this coupling can be accomplished such that there is minimal effect on receiver efficiency. A logical choice to quantify this increase in power conversion efficiency with increasing final mean fluid temperature is the Carnot efficiency:

\[ \eta_c = 1 - \frac{T_{\text{amb}}}{T_f} \]  

(9)

The total receiver-side efficiency of the solar thermal power generation system becomes:

\[ \eta_{\text{sys}} = \eta_{\text{rec}} \eta_c \eta_{\text{II}} \]  

(10)

which incorporates a constant second-law efficiency (\( \eta_{\text{II}} \)) to account for irreversibilities of the power generation cycle, which we assume to be \( \eta_{\text{II}} = 0.66 \) (Singh et al., 2000).

The opposing trends of the receiver efficiency and the Carnot efficiency with increasing temperature give rise to an optimum system efficiency (\( \eta_{\text{sys}}^{\text{opt}} \)) (Pitz-Paal and Trevor, 2008). We study the effects of the following parameters on the receiver and system efficiency: concentration (\( C \)), nanofluid height (\( H \)), and optical thickness (\( \tau_H \)).

**Effect of optical thickness:** Figure 7a shows the effect of optical thickness on the receiver efficiency (Eq. 8). As discussed previously, the optical thickness of a nanofluid volumetric receiver can be adjusted by varying the volume fraction of the nanoparticles. With increasing optical thickness, volumetric absorption will more closely resemble surface absorption because the photon penetration depth will decrease. With shorter penetration depths, the heat release is localized to the top of the receiver where most of the losses occur; hence, a volumetric receiver with \( \tau_H = 4 \) is less efficient than one with \( \tau_H = 1.7 \). On the other hand, if the optical thickness is too small (as is the case when \( \tau_H = 1 \)), the receiver is unable to absorb all of the incident solar radiation. Using the maximum system efficiency as a metric (\( \eta_{\text{sys}}^{\text{opt}} \)), the optimum optical thickness was determined to be 1.7 (\( \pm 0.1 \)), as shown in the inset of Figure 7a. The optical thickness was fixed to this optimum value for the remainder of the study.
Figure 7. Parametric study of receiver efficiency with mean fluid temperature for variable optical thickness, solar concentration, and nanofluid height: a) $\tau_H$ ranging from 0.5 to 4. Inset shows system efficiency with varying optical thickness with the optimum at $\tau_H = 1.7$. b) $C$ ranging from 10 to 100, and c) $H$ ranging from 0.1 to 25 cm. The baseline in all of the graphs (solid black) shows the case when $\tau_H = 1.7$, $C = 50$, and $H = 2.5$ cm.
Effect of solar concentration:
Increasing the concentration \( C \) of solar radiation incident on a volumetric receiver has the effect of increasing the steady state or stagnation temperature. Higher concentration levels allow the receiver to maintain a high efficiency over a wider range of temperatures and delay the sharp decrease in efficiency as the receiver asymptotes to its stagnation temperature, as seen in Figure 7b. Therefore, receiver efficiency increases with \( C \) for the range considered.

A surface plot showing optimum system efficiency in the parameter space of \( C \) and \( H \) for a nanofluid volumetric receiver with \( \tau_H = 1.7 \) coupled to an idealized power cycle is shown in Figure 8a. The results show that the optimum system efficiency increases with concentration level.

Effect of nanofluid height:
When the emissive loss is dominated by the top surface temperature, the effect of nanofluid height may be understood by considering that increasing \( H \) will amplify the temperature difference between the mean fluid temperature and the surface temperature (as shown in Figure 3). Figure 7c shows how \( \eta_{rec} \) decreases with increasing nanofluid height for temperatures below 700 K, which corresponds to a region where the surface temperature is higher than the mean fluid temperature. For higher temperatures (800-1200 K), \( \eta_{rec} \) increases with increasing nanofluid height because the profile inversion has occurred. At very high temperatures (above 1300 K), \( H \) has no effect on receiver efficiency because the dominant volumetric losses (spectral Band I) are only affected by the optical thickness, since they are governed by the RTE (Eq. 2).

In the temperature range where net system efficiency is maximized (800-1200 K), taller nanofluid VRs achieve improved receiver efficiencies because of the profile inversion. Thus, the optimum system efficiency of nanofluid volumetric receiver increases as the volume \( (i.e., \, nanofluid \, height) \) is increased, as shown in Figure 8a. An upper limit on the nanofluid height is determined by the optical clarity of the carrier fluid since the radiative properties and the optical thickness of the nanofluid need to be dominated by the nanoparticles for this analysis to be valid.

Optimal exposure time and temperature:
With the efficiency of the nanofluid volumetric receiver optimized with respect to optical thickness, we investigate the effects of concentration and nanofluid height on the exposure time and temperature at the optimum system efficiency. Each \( \eta_{opt}^w \) determined in Figure 8a corresponds to a specific final mean temperature (Figure 8b) and exposure time (Figure 8c).

The optimal final mean temperatures are shown in Figure 8b. The trends for optimal temperature follow very closely the trends for optimum system efficiency (Figure 8a) because the system efficiency is strongly dependent on the temperature due to the power cycle efficiency. This analysis shows that nanofluid volumetric receivers need to be stable at very high temperatures in order to reach the predicted optimum system efficiencies. In future work, the material durability at such high temperatures needs to be addressed.
Figure 8. Surface plots showing: a) optimum system efficiency in the parameter space of $C$ and $H$ for nanofluid VRs ($\tau_\mu = 1.7$), b) optimal final mean temperature, and c) optimal exposure time corresponding to the optimum system efficiency in (a).
As shown in Figure 8c, the amount of exposure time ($t_{exp}$) needed to achieve optimum system efficiency decreases with increasing concentration and decreasing nanofluid height for nanofluid VRs with $\tau_H = 1.7$. Exposure time is an important quantity in solar thermal plants because a shorter exposure time translates to the capability to store more thermal energy for a limited amount of hours of sunlight.

The results indicate that volumetric receivers are advantageous for applications with high levels of solar concentration such as central receiver designs. Furthermore, because of the increasing efficiency with nanofluid height, nanofluid VRs are well-suited for ground-based liquid receiver tanks with integrated storage where a “reflective tower” (Epstein et al., 1999) or hillside mounted heliostats (Slocum et al., 2011) are used to beam down concentrated solar radiation.

This study provides an important starting point for system-level studies that can extend this analysis to more specific applications by incorporating non-idealities associated with optical concentration, pumping, and storage. As shown in Figure 8a, nanofluid VRs can achieve high ideal system efficiencies exceeding 35% in the parametric space considered.

5. CONCLUSIONS

Nanofluid volumetric receivers for high solar flux and high temperature solar thermal applications were investigated. A 1-D numerical model was developed to predict temperature profiles based on direct absorption by the nanoparticles and thermal re-emission at high temperatures. The radiative properties of the nanofluid were tuned by adjusting the particle loading to achieve a desired optical thickness. An experimental setup was used to measure temperature profiles in suspensions of 28 nm carbon-coated cobalt nanoparticles in Therminol® VP-1 for varying nanofluid optical thicknesses; the experimental results are in good agreement with the numerical modeling results (within a 20% difference). The model shows that receiver efficiency increases with increasing nanofluid height and incident solar flux, and that the optimum optical thickness for a non-selective volumetric receiver is $1.7 \pm 0.1$. When connected to a power cycle, optimum system efficiencies exceeding 35% are predicted when $C > 100$ and $H > 5$ cm. The outcomes of the study provide an important perspective as to how nanofluids can be best utilized as volumetric receivers in concentrated solar applications.

NOMENCLATURE

- $A$: Total surface area exposed to solar radiation [m$^2$]
- $b$: Slope of best fit between $\kappa_{p,j}$ and $f_v$ [m$^{-1}$]
- $Bi$: Biot number
- $C$: Solar concentration factor [-]
- $c_p$: Heat capacity [J/kg-K]
- $D$: Particle diameter [m]
- $e$: Emissive power [W/m$^2$]
- $E_{b}$: Black body emission [W/m$^2$-m]
- $f_v$: Particle volume fraction [-]
- $G$: Incident radiative heat flux [W/m$^2$]
- $H$: Nanofluid height [m]
- $I$: Radiative intensity [W/m$^2$-m-sr]
ACKNOWLEDGEMENTS

The authors would like to thank the King Fahd University of Petroleum and Minerals in Dhahran, Saudi Arabia, for partially funding the research reported in this paper through the Center for Clean Water and Clean Energy at MIT and KFUPM. Also, Andrej Lenert acknowledges the support of the MIT Energy Initiative and the National Science Foundation Graduate Fellowship. We sincerely thank: Daniel Kraemer and Jianjian Wang for their experimental help, Mattheus Ueckermann for his numerical advice, and members of the CSPonD project at MIT for the insightful discussions.
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