The Missing Satellite Problem in 3D

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Submitted to MNRAS

ABSTRACT
It is widely believed that the large discrepancy between the observed number of satellite galaxies and the predicted number of dark subhalos can be resolved via a variety of baryonic effects which suppress star formation in low mass halos. Supporting this hypothesis, numerous high resolution simulations with star formation, and associated feedback have been shown to reproduce the satellite luminosity function around Milky Way-mass simulated galaxies at redshift zero. However, a more stringent test of these models is their ability to simultaneously match the satellite luminosity functions of a range of host halo masses and redshifts. In this work we measure the luminosity function of faint (sub-Small Magellanic Cloud luminosity) satellites around hosts with stellar masses \(10.5<\log_{10}M_*/M_\odot<11.5\) to an unprecedented redshift of 1.5. This new measurement of the satellite luminosity function provides powerful new constraining power; we compare these results with predictions from four different simulations and show that although the models perform similarly over-all, no one model reproduces the satellite luminosity function reliably at all redshifts and host stellar masses. This result highlights the continued need for improvement in understanding the fundamental physics that governs satellite galaxy evolution.

Key words: dark matter – galaxies: dwarf – galaxies: evolution – galaxies: luminosity function, mass function

1 INTRODUCTION

One of the significant discrepancies between \(\Lambda\) cold dark matter (CDM) and observation is the apparent lack of structure on sub-galactic scales. This ‘Missing Satellite Problem’ (Klypin et al. 1999; Moore et al. 1999), was first observed in the Local Group and has subsequently been observed in the mass function of isolated field galaxies (Papastergis et al. 2011).

One commonly adopted solution to the missing satellite problem in the context of CDM, is that there are a large number of low mass dark matter subhalos that do not have detectable stars or gas. The key to this solution is developing a comprehensive understanding of star formation in low mass halos. Simulations are now able to invoke a variety of mechanisms including UV heating during reionization, super-nova feedback, stellar winds, and tidal and ram pressure stripping by the host halo in order to reproduce the observed luminosity function of Milky Way satellites down to low masses at redshift zero (e.g Thoul & Weinberg 1996; Gnedin 2000; Kaufmann et al. 2008; Macciò et al. 2010; Springel 2010b; Guo et al. 2011a; Zolotov et al. 2012; Brooks et al. 2013; Starkenburg et al. 2013; Wetzel et al. 2016). Presently, the baryonic solution to the missing satellite problem around Milky Way-like galaxies is not unique, with a variety of models all matching the data reasonably well. Much more information can be gained by comparing with observations of satellites around host galaxies of varying stellar mass and at a range of redshifts. Such a comparison can help distinguish between the roles of environmental and internal processes in regulating star formation in satellite galaxies.

It is also possible that the missing satellite problem is due to incorrect assumptions about dark matter. For instance, if dark matter is warm or significantly self-
interacting, small scale structure can be erased at early times either due to finite particle velocities in the former case (e.g. Colombi et al. 1996) and references therein, or via a combination of dark sector Silk-damping and acoustic oscillations in the latter (Vogelsberger et al. 2015; Cyr-Racine et al. 2015). It is interesting to explore how different dark matter scenarios affect the star formation physics required to reproduce the observed luminosity function relative to the cold dark matter case.

Recent observations have generated a wealth of new information about satellite galaxies at low redshift, finding a significant dependence between the satellite luminosity function and host stellar mass and color (e.g. Guo et al. 2011a; Lin et al. 2011; Lacey et al. 2011; Strigari & Wechsler 2012; Wang & White 2012; Nierenberg et al. 2012; Ruiz et al. 2015; Sales et al. 2015; Lan et al. 2015). Simulations have had varying success at reproducing these trends. For instance, Wang & White (2012) found that the semi-analytic model applied to Millenium II halos matched some of the trend of increasing satellite numbers with host stellar mass, but significantly over-predicted the number of satellites around $\sim 10^{11.5} M_\odot$ hosts relative to observations, as well as the number of bright satellites around lower stellar mass hosts.

In addition to host stellar mass and morphology, redshift provides another important dimension along which to constrain star formation models, as different star formation processes occur on a broad range of time scales. Recent studies have begun to measure the number of satellites around higher redshift hosts at $z \sim 0.4 - 2$ (Newman et al. 2012; Nierenberg et al. 2012; Tal et al. 2014; Nierenberg et al. 2013b; hereafter N13)) compared the measurement of the satellite luminosity function in bins of both redshift from 0.1-0.8 and host stellar mass to theoretical predictions from Guo et al. (2011b), Lu et al. (2012) and Menci et al. (2012), finding that although all the models matched the luminosity function of Milky Way satellites, they each predicted significantly different luminosity functions in the other host mass and redshift regimes, demonstrating the power of comparing to observations outside of the Local Group.

In this work we extend our observation of the satellite luminosity function to fainter satellites and higher redshifts using deep, near-IR imaging from Cosmic Assembly Near-infrared Deep Extragalactic Legacy Survey (CANDELS (Grogin et al. 2011; Koekemoer et al. 2011). With the power of near-IR images, we are able to double our redshift baseline (from redshift 0.8 to 1.5) and reach an order of magnitude fainter satellites at $z \sim 0.8$, with respect to our previous work. We combine the new measurement with lower redshift results from Nierenberg et al. (2012) (hereafter N12), and compare these results with four state-of-the-art simulations. The models are: 1) a CDM merger tree simulation with semi-analytic star formation (Menci et al. 2014), 2) a WDM merger tree with the same semi-analytic star formation implementation as in the CDM case also by (Menci et al. 2014), 3) a CDM N-body simulation with Bayesian-tuned semi-analytic star formation from Lin et al. (2014) and 4) Illustris which is a CDM N-body simulation with dynamical star formation (Vogelsberger et al. 2014b).

For the observational results, we assume a flat ΛCDM cosmology with $h = 0.7$ and $\Omega_m = 0.3$. We note that although these values are slightly different from those used in each of the simulations, the variations caused by adjusting these parameters are much smaller than the measurement uncertainties. All magnitudes are given in the AB system (Oke 1974).

2 DATA

To study the properties of satellites at a wide range of redshifts, we combine data from the COSMOS field (Scoville et al. 2007) and the CANDELS fields. The relatively wide COSMOS survey has $\sim 1.7$ square degrees of HST F814W imaging, and is useful for constraining the satellite luminosity function at lower redshift and for higher stellar mass hosts. All results from COSMOS I814 imaging in this work are taken from N12 which contains a detailed discussion of the data that was used.

CANDELS has $\sim 0.25$ square degrees of deep, near-infrared F160W, F140W and F125W HST imaging which enables the detection of fainter satellite galaxies at higher redshifts than COSMOS. To detect satellites in CANDELS, we make extensive use of data products provided by the 3D-HST team (Brammer et al. 2012; Skelton et al. 2014), which include reduced HST imaging as well as photometric, stellar mass and redshift catalogs.

2.1 Host galaxy selection

We study satellites around host galaxies with stellar masses $10.5 < \log_{10}[M_*/M_\odot] < 11.5$ between redshifts $0.1 < z < 1.5$, using the stellar mass and redshift catalogs from the 3D-HST survey for CANDELS, and from Ilbert et al. (2009), Lilly et al. (2007) for COSMOS. The host stellar mass limits were selected to ensure sufficient signal of at least $\sim 1$ satellite per host on the low mass end, and a well constrained halo-mass to satellite mass relation on the higher mass end. The latter restriction is important because we select satellites based on $R_{200\Delta}$ of the hosts. Where possible, spectroscopic redshifts were used, otherwise photometric redshifts were used from Ilbert et al. (2009) in COSMOS, and from 3D HST photometric catalogs in CANDELS for objects with photometric redshift quality indicator $Q_z < 3$ as recommended by Brammer et al. (2008).

We require hosts to be isolated, defined by being at least $R_{200\Delta}$ away from all galaxies more than twice as massive and at the same redshift ($z - z_{\text{host}})/z_{\text{host}} < 0.007$. We estimate $R_{200\Delta}$ from the stellar mass to halo mass relation from Dutton et al. (2010).

In total, COSMOS contains 3038 host galaxies between redshifts 0.1 - 0.8 which matched our criteria. Figure 1 of N12 shows the stellar mass distribution in bins of redshift for COSMOS hosts. The deeper and narrower CANDELS has 1708 host galaxies between redshifts 0.4 to 1.5. Figure 1 shows the stellar mass distribution of CANDELS hosts in bins of redshift.

2.2 CANDELS Satellite candidate selection

We use the 3D HST PSF-matched photometric catalogs to select the majority of satellite candidates. These catalogs were created with SourceExtractor (Bertin & Arnouts 1996; hereafter SE) on PSF matched, variance weighted mean.
combined F160W, F140W and F125W images. Satellite candidates include all non-stellar objects brighter than F160W < 25 AB magnitudes between 0.07 < R/R200,host < 0.5 where R200,host is estimated based on the host stellar mass and stellar mass to halo mass relation from Equation 3 of Dutton et al. (2010) for early-type galaxies. The limit of F160W<25 magnitude is chosen to ensure over 90% detection completeness in both the CANDELS deep and wide imaging based on Figure 14 from Skelton et al. (2014), while the radial limits ensure accurate photometry near the host galaxies, and a favorable ratio of satellites to background/foreground objects in the outer region.

As we demonstrated in Nierenberg et al. (2011 hereafter, N11) and N12, even with deep, high resolution HST imaging, photometric accuracy and completeness suffer within several effective radii of a bright central galaxy. To counter this, we empirically model and subtract the host light profile, and then perform our own object detection and photometry in small regions near the host galaxies, using SE parameters which match those used to create the 3D HST catalogs. We then add the new object detections to the full 3D HST catalogs, and update the photometry only for the region near the host galaxies. This method improves completeness and photometric accuracy very near the host galaxies (N11, N12). We perform the empirical host subtraction separately in both the detection image, as well as in the F160W science image. We then apply the same empirical photometric correction to the F160W MAG_AUTO as applied to make the 3DHST photometric catalogs (see Skelton et al. 2014 Figure 10).

3 STATISTICAL ANALYSIS

We detect satellites statistically in monochromatic F160W data in CANDELS (F814 for COSMOS), as an increase in the number density of objects relative to the background/foreground number density measured outside of the host galaxy R200. The statistical model framework is described in detail in N11 and N12. The measurement is made in two subdivided bins of host stellar mass 10.5 < log10[M*/M⊙] < 11, 11 < log10[M*/M⊙] < 11.5 and three bins of redshift 0.1 < z < 0.4, 0.4 < z < 0.8, 0.8 < z < 1.5. Each redshift and host stellar mass bin, is treated as an independent data set. Results for CANDELS and COSMOS are inferred separately. Model parameter definitions and priors are listed in Table 1 for CANDELS, and Table 1 in N12 for the COSMOS.

In brief, the number density of objects around the host galaxies is parametrised as the sum of a uniformly distributed number of background/foreground objects, and a population of satellite galaxies with a power-law spatial distribution with projected slope γp. In this work, we update the model relative to N11 and N12, by directly inferring the slope and bright end cutoff of the satellite luminosity function rather than iteratively inferring the cumulative number of satellites brighter than a fixed δm = m_sat - m_host, for a series of δm values. We model the luminosity function of satellites in units of δm as a Schechter function with faint end slope αsat and bright end cutoff of δm,0:

$$P(\delta_{m,\text{sat}} | \alpha_{\text{sat}}, \delta_{m,0}) \propto 10^{\frac{\delta_{m,0} - \delta_{m,\text{sat}}}{\alpha_{\text{sat}}}} \exp \left[ -10(\delta_{m,0} - \delta_{m,\text{sat}}) \right]$$

The total model number of satellites per host, Nsat, between 0.07 < r/R200 < 0.5 is defined between δm,min,o and δm,max,o, the minimum and maximum values respectively where the luminosity function can be measured reliably for the majority of the sample. These values vary depending on the average magnitude of the hosts in each redshift bin, as δm,max,o for a given host is 25 - m_host, the satellite luminosity function of brighter hosts can be measured to lower values of δm. Table 1 gives the values of the limits δm,min,o and δm,max,o selected for the inference in each host redshift and stellar mass bin.

We adopt priors on the satellite spatial distribution, the background/foreground number density, and the slope of the background/foreground luminosity function. In N12 we found that γp = −1.1 ± 0.3 over a wide range of redshifts, satellite luminosities and host stellar masses and morphologies, so for this work we adopt a Gaussian prior on γp with mean -1.1 and standard deviation 0.3. As we show in N12, adopting this prior does not affect the mean inferred number of satellites, but it does decrease the uncertainty, and is useful for constraining the properties of satellites around the much smaller sample of CANDELS host galaxies.

We constrain the properties of the background/foreground galaxy in annuli outside of the region where we detect satellite galaxies. This method has been shown to accurately characterise the density of both random line of sight structure, as well as correlated structure which is not gravitationally bound to the host galaxies (Chen 2008, Liu et al. 2011). We select annuli between 1 < R/R200,host < 2 to measure both the back-

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1 SE CLASS_STAR < 0.8 and 3D HST star_flag != 1

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ground/foreground number density, $\Sigma_b$, and the slope of the number counts $\alpha_b$, where $N_b(m) \propto \Sigma_b m^{\alpha_b}$. These values do not depend strongly on the choice of the annuli or radius, given the measurement uncertainty. We include $\Sigma_b$ and $\alpha_b$ as model parameters with Gaussian priors with mean and standard deviations given by the values measured in the outer annuli. This enables us to directly account for the effects of measurement uncertainties in $\Sigma_b$ and $\alpha_b$ in the inferred satellite properties. The prior values for these parameters are listed in Table 1.

### 4 RESULTS

The inferred median values and $1\sigma$ uncertainties for the satellite luminosity function parameters in CANDELS are given in Table 2 for the four host stellar mass and redshift bins. For all host stellar mass and redshift regimes, the prior values for the projected number density radial profile of satellites $\gamma_p$, the number density of foreground/background objects and the slope of the background/foreground number counts were recovered, with no tightening of the constraints. This was expected given that the prior on $\gamma_p$ is derived from the much larger COSMOS sample, while the background/foreground number density is measured in a much larger region than the region in which satellite properties are inferred. Figure 2 shows the inferred cumulative satellite luminosity function for CANDELS (dark hatched region) and COSMOS (black points) with satellite numbers extrapolated to be between 0.07 < r/R$_{200,\text{host}}$ < 1 based on the inferred value of the slope of the satellite number density radial profile $\gamma_p$.

For CANDELS we plot in black, regions which do not overlap with COSMOS, and which had a significant number of hosts (> 10) with $\delta_{m,\text{max},i} = 25 - m_{\text{host}}$, to ensure that the luminosity function is well constrained by the data. In light grey we show the extrapolation of the luminosity function to fainter values of $\delta_m$ where the data is less constraining, which is reflected in the increased uncertainty in the inferred luminosity function at these values. We also extrapolate the CANDELS results to brighter values of $\delta_m$ to demonstrate the consistency with COSMOS results, and to show the overall shape of the luminosity function in the higher redshift bin. The number of satellites is well constrained and consistent with prior measurements of the luminosity function from COSMOS. N12 gives a detailed comparison between the lower redshift (0.1 < z < 0.4) COSMOS results and other results from the literature.

The inferred slope of the satellite luminosity function is $\alpha_s \sim -1.2 \pm 0.5$, consistent within the measurement uncertainties for all the redshift and host stellar mass regimes. The bright cutoff, $\delta_{m,o}$, is approximately 1 ± 1, again consistent between the four regimes.

This result is broadly consistent with the measurement uncertainties with the low redshift $z$-0.01 – 0.05 luminosity function measurement of satellites brighter than $M_r \sim -14$ from [Lan et al. 2015] which fit a double Schechter function to their satellites and found a slope of $\sim -1$ for satellites with absolute magnitudes brighter than -18 (corresponding to $\delta_m$ values of $\sim 2 - 3$ depending on host stellar mass), and slope of $\sim -1.6$ for satellites fainter than -18. Our result is also consistent with measurements of the slope of the stellar mass function of field galaxies and satellites between redshifts $\sim 0 - 4$ which typically find values of $\alpha$ between -1 to -2 ([Grazian et al. 2015] [Duncan et al. 2014] [Baldry et al. 2012] [Santini et al. 2012] [Graus et al. 2016] [Lan et al. 2015] e.g.). Our data is not constraining enough to test whether satellite galaxies follow the field galaxy trend of decreasing $\alpha$ with increasing redshift.

It is interesting to compare these new high redshift satellite observations with local observations of Milky Way mass hosts. Assuming the Milky Way has approximately doubled in stellar mass since $z$~1 (e.g. [Behroozi et al. 2010] [Lehnert et al. 2014]), Milky Way progenitors fall on the lower end of the lower stellar mass hosts in the redshift bin 0.8-1.5. Hosts in this stellar mass bin have $\sim 2 \pm 0.7$ satellite galaxies with $\delta_m > 4$, and $\sim 0.8 \pm 0.3$ with $\delta_m > 2$ corresponding to the present day magnitude offsets between the Small Magellanic Cloud (SMC) and the Milky Way, and the Large Magellanic Cloud (LMC) and the Milky Way respectively. This frequency is marginally higher, but still consistent within the measurement uncertainties, with low redshift observations where Milky Way stellar mass hosts have about 0.3±0.1 and 0.2 ± 0.1 SMCs and LMCs respectively (see also [Liu et al. 2011] [Guo et al. 2011a] [Lares et al. 2011]).

### 5 COMPARISON WITH THEORETICAL MODELS

This new measurement of faint satellites provides a new constraint for models of galaxy formation. We compare our results with four theoretical predictions described below. Three of the predictions are from either semi-analytic or hydrodynamical models applied to cold dark matter cosmologies, and the fourth prediction is a semi-analytic model applied to a warm dark matter cosmology.

#### 5.1 Menci

The Menci model is a semi-analytic model applied to dark matter merging trees. We include a summary of the dark matter and semi-analytic models below, we refer the reader to Menci et al. (2014) for a detailed description.

In this work we consider both a Cold and a Warm dark matter merging tree. Both models track subhalos after they have entered the virial radius of the main halo, enabling them to coalesce with the central galaxy after orbital energy

<table>
<thead>
<tr>
<th>$\log(M_{\text{host}}/M_\odot)$</th>
<th>$z_{\text{host}}$</th>
<th>$N_{s,o}$</th>
<th>$\alpha_s$</th>
<th>$\delta_{m,o}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>10.5-11.0</td>
<td>0.4-0.8</td>
<td>3.1</td>
<td>-1.2 ± 0.4</td>
<td>1.1 ± 1.0</td>
</tr>
<tr>
<td>10.5-11.0</td>
<td>0.8-1.5</td>
<td>0.7-0.6</td>
<td>-0.8 ± 0.5</td>
<td>0.9 ± 1.0</td>
</tr>
<tr>
<td>11.0-11.0</td>
<td>0.4-0.8</td>
<td>3.1-2</td>
<td>-0.8 ± 0.5</td>
<td>2.1 ± 2.0</td>
</tr>
<tr>
<td>11.0-11.5</td>
<td>0.8-1.5</td>
<td>3.1-2</td>
<td>-1.1 ± 0.6</td>
<td>0.9 ± 2.0</td>
</tr>
</tbody>
</table>

Table 2. Inferred median and one sigma confidence intervals for the parameters defining the satellite luminosity function, in bins of host galaxy stellar mass and redshift. Parameters are defined in Table 1. Note that the normalisation of the luminosity function $N_{s,o}$ is defined over different intervals of $\delta_m = m_{\text{sat}} - m_{\text{host}}$ of the luminosity function for each of the bins, shown in parentheses to account for the fact that the completeness varies with redshift and host stellar mass.
loss due to dynamical friction, merge with another sub-halo, or survive as a satellite halo. Cold Dark Matter halo merging trees are generated through a Monte Carlo procedure adopting the merging rates given by the Extended Press & Schechter (EPS, see Lacey & Cole 1993) formalism. The WDM power spectrum is generated using the method described by Menci et al. (2012), with some modifications for the present work. First, we have included a sharp-k filter to relate the power spectrum to the variance of density perturbations (see Benson et al. 2013; Schneider et al. 2013). Secondly, we assume a thermal relic mass \( m_X = 1.5 \text{ keV} \) for the WDM candidate which yields a power spectrum corresponding to that produced by (non-thermal) sterile neutrinos with mass \( m_{\nu, \text{sterile}} \approx 6 - 12 \text{ keV} \), depending on the production mechanism (see, e.g. Abazajian 2014) for a dark matter interpretation of the origin of the recent unidentified X-ray line reported in stacked observations of X-ray clusters (Buul et al. 2014; Boyarsky et al. 2014). This particle mass is consistent with observational limits \( m_X \gtrsim 1.5 \text{ keV} \) from high redshift galaxies Schultz et al. (2014) and ultra-faint dwarf galaxies (Lovell et al. 2012; 2014; Horiiuchi et al. 2014), although still in tension with Lyman-\( \alpha \) forest constraints which yield \( m_X \gtrsim 3.3 \text{ keV} \) (Viel et al. 2013). A discussion of the various uncertainties which may affect the constraints is given in Abazajian et al. (2011) and in Garzilli et al. (2015).

The processes affecting baryons are connected in the same way to the evolution of both Cold and Warm dark matter halos. The baryonic model includes atomic cooling into rotationally supported discs following Mo et al. (1998). Star formation occurs quiescently over long time scales (\( \sim 1 \text{ Gyr} \)), and in bursts (\( \sim 1 \text{ Myr} \)) triggered by galaxy interactions and disc instabilities. Star formation is suppressed via feedback from supernova and active galactic nuclei as described in Menci et al. (2008). The luminosity is computed by convolving the star formation histories of the galaxy progenitors with a synthetic spectral energy distribution, which we take from Bruzual & Charlot (2003) assuming a Salpeter IMF. The model includes tidal stripping of part of the stellar content of each satellite galaxy following Henriques & Thomas (2010).

### 5.2 Lu

The Lu model is a semi-analytic model applied to a set of halo merger trees extracted from a large cosmological N-body simulation, the Bolshoi Planck simulation, which is same as the Bolshoi simulation (Klypin et al. 2011), but with a cosmology favored by Planck data (Planck Collaboration et al. 2015) with parameters \( \Omega_{m,0} = 0.30711 \), \( \Omega_{\Lambda,0} = 0.69289 \), \( \Omega_{b,0} = 0.048 \), \( h = 0.7 \), \( n = 0.96 \), and \( \sigma_8 = 0.82 \). The mass resolution of the simulation allows the model to track halos and subhalos with mass \( \sim 10^9 M_{\odot} h^{-1} \). The prescriptions for the baryonic processes implemented in the SAM are detailed in Lu et al. (2014). The model parameters governing star formation and feedback are tuned using an MCMC optimization to match the local galaxy stellar mass function (Moustakas et al. 2013). Therefore, it is guaranteed to produce a global galaxy stellar mass function for the stellar mass range between \( 10^9 \) and \( 10^{12} M_{\odot} \) at redshift zero within the observational uncertainty for the given parameterization of the model.

### 5.3 Illustris

The Illustris simulation (Vogelsberger et al. 2014b) modeled a 106 Mpc\(^3\) volume including both dark matter and baryons using the AREPO simulation code (Springel 2010a). The Illustris model includes a range of physical processes (including radiative gas cooling, star formation, stellar feedback, and AGN feedback) that have been tuned to produce broad agreement with the cosmic star formation rate density and redshift \( z = 0 \) stellar mass function (Vogelsberger et al. 2013; Torrey et al. 2014). For a full description of the Illustris simulation setup, see Vogelsberger et al. (2014a) and Genel et al. (2014). The galaxy luminosities used here are assigned using the methods described in Torrey et al. (2015).

### 5.4 Comparison Results

We compute the satellite luminosity function from the Lu and Illustris simulations by including all objects within \( R_{200} \) of a host halo, where \( R_{200} \) is estimated using the same stellar mass to halo mass relation as was applied to the observations (Dutton et al. 2010). We note that the number of objects within \( R_{200} \) is significantly lower than the total number of subhalos identified by the FOF algorithm for both Illustris and Lu models. However, the number does not depend strongly on whether the Dutton et al. (2010) relation is used to estimate the host virial radius, or whether the simulation value of \( R_{\text{vir}} \) is directly used. For the Menci CDM and WDM merging trees, we directly use the simulation definition of satellite membership which is determined by the host virial radius.

We compute the \( \chi^2 \) between the model number of satellites per host and the measured numbers as a function of

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**Table 1.** Model parameter definitions and priors. (a) \( U(\text{min}, \text{max}) \) is a uniform prior between the min and max values. (b) \( G(\text{mean}, \text{std}) \) is a Gaussian prior defined by the mean and standard deviation.
\( \delta_m \), for discrete values of \( \delta_m \) spaced in intervals of 0.5 for COSMOS data and 1 for CANDELS data. In regions where both CANDELS and COSMOS data overlapped, the COSMOS data is used in the comparison with theory owing to its higher precision. Although our data is composed of measurements in both F814W and F160W, the luminosity function of satellites as a function of \( \delta_m = m_{\text{sat}} - m_{\text{host}} \) does not have a significant dependence on observed band in any of the theoretical models for redshifts \(< 0.8 \).

We include the covariance between data points in our \( \chi^2 \) estimate, which is significant owing to the fact that we are considering the cumulative numbers of satellites, and thus the same host galaxy will contribute to the number of satellites in multiple bins. The covariance matrix between data points was computed using 2500 draws from the Markov Chain Monte Carlo results for CANDELS while for COSMOS it was computed by bootstrap resampling the input data and re-inferring the satellite numbers. The black hatched region of the CANDELS measurement shows the range of CANDELS data which was used to compute the \( \chi^2 \).

Table 2 lists the \( \chi^2 \) values between the models and observed luminosity for each bin in host stellar mass and redshift, along with the corresponding number of data points. The \( \chi^2 \) values were 61, 72 and 59 for the Lu, Menci and Illustris CDM models, and 54 for the Menci WDM model for 53 degrees of freedom. Accounting for the number of degrees of freedom, the \( \chi^2 \) goodness-of-fit test gives an approximately \( \sim 20\% \), \( 5\% \), \( 15\% \) and \( 60\% \) chance that the data was drawn from each model respectively. These values are approximately equivalent, with only the Menci CDM model being somewhat disfavoured relative to the others, but at less than a 2\( \sigma \) confidence, and the Menci WDM model performing the best.

6 DISCUSSION

This data provides an important new constraint for models of satellite galaxy formation and evolution. While overall there is not a strong preference for a particular model, it is interesting to consider how the models performed in the different regimes. In particular, the Menci WDM model provides the best overall match to the luminosity function around higher mass hosts while the Lu and Illustris models match the luminosity function of low-mass hosts at low redshifts. There is some tension between the numbers of faint satellites in the redshift range 0.4 – 0.8 for lower mass hosts, for all of the models, which somewhat underestimate the slope of the satellite luminosity function. Overall, models which produce accurate predictions for Milky Way mass hosts at low redshifts tend to underestimate the number of satellite galaxies found around those hosts at higher redshifts and at higher stellar masses, and vice versa.

This measurement provides complementary constraints to measurements of field galaxy properties. In particular, the Illustris and Menci CDM models both significantly over-predict the number of low mass galaxies \(< M_*/M_\odot < 10 \) at redshift 0.4. We combine these new results with lower redshift (0.1-0.8) measurements from COSMOS imaging from Nierenberg et al. (2012). We compare these results to predictions from four theoretical models (Vogelsberger et al. 2014a, Nierenberg et al. 2013a, Fiacconi et al. 2016). While none of the models was significantly ruled out, different models matched the observations more or less well in different regimes of redshift and host stellar mass, which highlights the value of this data set in distinguishing between models which performed similarly at redshift zero around Milky-Way-mass host galaxies. This data provides important new constraining power for future implementations of feedback and dark matter physics in these models.

7 SUMMARY

Using CANDELS F160W imaging, we measure the luminosity function of faint satellites around hosts with stellar masses between \( 10.5 < \log_{10} M_*/M_\odot < 11.5 \) to a redshift of 1.5. The deep imaging enables us to detect satellites with \( \delta_m = m_{\text{sat}} - m_{\text{host}} = 4 \) (fainter than the SMC) to an unprecedented redshift of 1.5, and to detect \( \delta_m = 7 \) satellites between redshifts 0.4-0.8. We combine these new results with lower redshift (0.1-0.8) measurements from COSMOS imaging from Nierenberg et al. (2012). While none of the models was significantly ruled out, different models matched the observations more or less well in different regimes of redshift and host stellar mass, which highlights the value of this data set in distinguishing between models which performed similarly at redshift zero around Milky-Way-mass host galaxies. This data provides important new constraining power for future implementations of feedback and dark matter physics in these models.
Table 3. Model $\chi^2$ values, after accounting for covariance in the data, for each host stellar mass and redshift bin. We note that a continuous luminosity function is inferred CANDELS data, but to compare with predictions from simulations we sample the luminosity function values at discreet points spaced every 0.5 $\delta m$ within the dark hatched region of Figure 2.

<table>
<thead>
<tr>
<th>$z$</th>
<th>$\log_{10}[M_{\text{host}}^*/M_{\odot}]$</th>
<th># Data Points</th>
<th>Menci CDM</th>
<th>Menci WDM</th>
<th>Lu</th>
<th>Illustris</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.1 - 0.4</td>
<td>10.5 - 11</td>
<td>13</td>
<td>17</td>
<td>18</td>
<td>10</td>
<td>9</td>
</tr>
<tr>
<td>0.4 - 0.8</td>
<td>10.5 - 11</td>
<td>9</td>
<td>6</td>
<td>11</td>
<td>13</td>
<td>12</td>
</tr>
<tr>
<td>0.8 - 1.5</td>
<td>10.5 - 11</td>
<td>11</td>
<td>31</td>
<td>9</td>
<td>18</td>
<td>20</td>
</tr>
<tr>
<td>Total</td>
<td>54</td>
<td>72</td>
<td>55</td>
<td>59</td>
<td>61</td>
<td></td>
</tr>
</tbody>
</table>

Figure 2. The cumulative luminosity function of satellite galaxies of hosts divided by bins of redshift (from left to right) and stellar mass (from top to bottom) between 0.07 < $r/R_{200}$ < 1.0. Black points with error bars and hatched region show the one sigma confidence interval from COSMOS F1814W and CANDELS F160W imaging respectively. The black points and hatched region were used to compute $\chi^2$ values for the comparison with theory, while the gray region represents extrapolations of the inferred luminosity function. Blue, purple and red lines lines are theoretical predictions with Cold Dark Matter from Lu et al. (2014), Menci et al. (2014), and Illustris (Vogelsberger et al. 2014b). The green luminosity function is the same star formation model as for the Menci CDM model, but applied to a Warm Dark Matter halo mass function (Menci et al. 2012).

Our conclusions are summarised as follows:

(i) We infer the parameters of the satellite luminosity function faint end slope to be $\alpha_s = -1 \pm 0.5$, and the bright cutoff relative to the host magnitude to be $\delta_{m,0} = 1 \pm 1$, consistent over all redshift and stellar host stellar mass bins within the measurement uncertainties.

(ii) We detect Small Magellanic Cloud-luminosity satellite galaxies to a redshift of 1.5, and find that Milky Way-like progenitors at redshift $\sim 1$ have consistent numbers of LMC/SMC analogs with redshift zero galaxies. In general, the cumulative number of satellites per host as a function of the offset between host and satellite magnitude is constant as a function of redshift within the measurement uncertainties, but is higher for hosts with higher stellar masses.

(iii) The theoretical models varied in their ability to predict the satellite luminosity function in different regimes of host stellar mass and redshift. Overall they performed similarly, however, models which fit the luminosity function of the satellites of low stellar mass hosts tended to underpredict the number of satellites around higher stellar mass hosts. Future predictions will need an adjusted implementation of stellar feedback as a function of host stellar mass and redshift in order to resolve this discrepancy.

ACKNOWLEDGMENTS

We thank R. Skelton and I. Momcheva for very helpful discussions and support with the 3D-HST data. Support for
this work was provided by NASA through grant number HST-AR 13732 from the Space Telescope Science Institute, which is operated by AURA, Inc., under NASA contract NAS 5-26555.

The Bolshoi and MultiDark simulations have been performed within the Bolshoi project of the University of California High-Performance AstroComputing Center (UC-HiPACC) and were run at the NASA Ames Research Center. The MultiDark-Planck (MDPL) and the BigMD simulation suite have been performed in the Supernova supercomputer at LRZ using time granted by PRACE.

PT acknowledges support from NASA ATP Grant NNX14AH35G. PT and MV acknowledge support through an MIT RSC award. The Illustris simulation was run on the CURIE supercomputer at CEA/France as part of PRACE project RA0844, and the SuperMUC computer at the Leibniz Computing Centre, Germany, as part of project pr85je. The analysis presented in this paper was run on the Harvard Odyssey and CfA/ITC clusters and though allocation TG-AST150059 granted by the Extreme Science and Engineering Discovery Environment (XSEDE) supported by the NSF.

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