Calibrating genomic and allelic coverage bias in single-cell sequencing

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Abstract

Artifacts introduced in whole-genome amplification (WGA) make it difficult to derive accurate genomic information from single-cell genomes and require different analytical strategies from bulk genome analysis. Here we describe statistical methods to quantitatively assess the amplification bias resulting from whole-genome amplification of single-cell genomic DNA. Analysis of single-cell DNA libraries generated by different technologies revealed universal features of the genome coverage bias predominantly generated at the amplicon level (1-10 kb). The magnitude of coverage bias can be accurately calibrated from low-pass sequencing (~ 0.1x) to predict the depth-of-coverage yield of single-cell DNA libraries sequenced at arbitrary depths. We further provide a benchmark comparison of single-cell libraries generated by multi-strand displacement amplification (MDA) and multiple annealing and looping-based amplification cycles (MALBAC). Finally we develop statistical models to calibrate allelic bias in single-cell whole-genome amplification and demonstrate a census-based strategy for efficient and accurate variant detection from low-input biopsy samples.

Introduction

Single-cell sequencing has provided unique insights into the genetic diversity of living organisms and among different cells within the same individual\textsuperscript{1-3}. Recent single-cell analyses have uncovered different clonal populations within a single tumor\textsuperscript{4,5}, revealed genomic diversity in gametes\textsuperscript{6,7} and neurons\textsuperscript{8,9}, and resolved historical cellular lineages during development\textsuperscript{10,11}. Single-cell sequencing also has many potential clinical applications, such as characterization of circulating tumor cells\textsuperscript{12,13} or fine-needle aspirates for clinical diagnostics.
A major drawback of single-cell sequencing, however, is the need to amplify genomic DNA prior to genomic characterizations\textsuperscript{14-17}. Due to the limited processivity (<100 kb) and strand extension rate (<100 nt/second) of DNA polymerases, the amplification of large genomes requires priming and extension at millions of loci, each amplified 10,000 to 1,000,000 fold. Such a large number of polymerase reactions inevitably generate amplification errors that confound the detection of genetic variants (Supplementary Fig. 1). Furthermore, differential priming efficiencies and extension rates result in uneven amplifications across the genome\textsuperscript{18,19} and skewed representations of homologous chromosomes. These variations both compromise variant detection sensitivity and may lead to incorrect genotypes\textsuperscript{5,12}. Although technological innovations may improve the fidelity of whole-genome amplification (WGA)\textsuperscript{15-17,20-23}, statistical fluctuations in the amplifications of millions of different DNA templates will persist.

As genetic variants are detected by the relative abundance of variant-containing DNA templates in the library, non-uniformity in genome coverage directly impacts the sensitivity to detect variants. For example, grossly non-uniform libraries emphasize only over-represented regions of the genome, and contain little information on other regions. Current methods to assess the uniformity of WGA rely on either direct visual inspection or various statistical measures of the sequencing coverage at the base-level\textsuperscript{18,22} or the allele-level\textsuperscript{5,12}. These empirical methods and metrics generally require substantial sequencing (10x or greater) and only gauge the deviation of amplified DNA from the "uniform" bulk DNA at a particular sequencing depth. They fail, however, to characterize the intrinsic non-uniformity resulting from WGA that is independent of sequencing depth (Fig. 1a,b). Moreover, the nature of the main sources of bias remains poorly characterized (Fig. 1c).
Here we report a systematic analysis of the coverage bias in single-cell whole-genome amplification. We show that the structure of individual WGA amplicons imparts a dominant amplification bias on length scales longer than the average size of sequencing fragments. Sequencing at low depths (0.1-1x) can effectively reveal this variation in the amplicon-level coverage, and enable accurate predictions of the depth-of-coverage yield when sequencing single-cell libraries to arbitrary depths. We further characterized the amplification bias between homologous chromosomes using analytically solvable models and validated these model predictions of allelic coverage by experimentally observed coverage at heterozygous sites. These results provide a framework for quality assurance of single-cell libraries and for estimating the sensitivity to detect local variants—such as single-nucleotide variants or chromosomal translocations—present in an individual cell at a given sequencing depth. Finally we demonstrate that the amplification bias in multi-strand displacement amplification (MDA) is more random than recurrent. Although such random bias cannot be corrected systematically, it suggests an efficient census-based strategy to accurately determine somatic genetic variants in small biopsy samples by sequencing multiple single cells from the same sample at modest depths.

Results

Information yield from bulk and single-cell sequencing

In bulk DNA libraries, each sequencing fragment represents genomic information from an individual cell; therefore, the information content increases with the sequencing depth until fragments are sequenced to exhaustion. The information content of a DNA library (“library complexity”) is thus measured by the total number of distinct molecules (sequencing fragments) in the library\textsuperscript{24-26}. This measure is essentially determined by the total number of cells (or the total
amount of genomic DNA) used to prepare the library (**Fig. 1a**, left panel). In single-cell DNA sequencing, whole-genome amplification (WGA) precedes the construction of a DNA library and introduces non-uniformity across the genome: As sequencing depth increases, more genomic regions are uncovered (**Fig. 1a**, right panel). Hence the fraction of the single-cell’s genome uncovered at a given sequencing depth determines the information content of single-cell sequencing. This measure ultimately depends on the uniformity of genome coverage, or the magnitude and spread of whole-genome amplification bias, and is conceptually equivalent to a “single-cell DNA library complexity.”

**Amplicon-level bias dominates coverage variation**

Visual inspection of single-cell sequencing coverage suggests that the genome coverage varies at many different length scales (**Fig. 1b**). To systematically evaluate the amplification bias in single-cell libraries, we sequenced multi-strand displacement amplified (MDA) DNA libraries of diploid RPE-1 cells (5-10x) and compared the sequencing coverage to a matched, unamplified bulk DNA library (~12x). To eliminate the effects of sequencing depths, we computationally down sampled the bulk and single-cell DNA libraries and calculated the auto-correlation of base-level coverage in diploid chromosome 1 at various depths to examine coverage correlations at all length scales (**Fig. 2a**, **Supplementary Fig. 2**). Both bulk and MDA libraries exhibited a correlation at length scale $l_c \approx 100$ bp, reflecting the sequencing read length (101 bp). Looking more closely we also identified a correlation at $l_c \approx 250$ bp, corresponding to the average size of the paired-end fragments (**Supplementary Fig. 2**). As expected, the magnitude of such correlations at the fragment scale decays with increasing sequencing depth.

Besides the fragment-level correlations, the bulk DNA sequencing coverage showed minimal correlation between loci separated by more than 1 kb. In contrast, single-cell libraries
exhibited a prominent correlation in 1-100 kb that is independent of the sequencing depth. Independent sequencing of the same single-cell library to 0.1x on the Illumina MiSeq platform and to 9x on the HiSeq platform revealed the same correlation with a characteristic length $l_c \approx 33$ kb (Fig. 2a). The sequencing-depth-independent correlation reflects the intrinsic non-uniformity in the DNA library and suggests a characteristic length scale of amplification bias.

The predominant correlation at $l_c$ suggests adjacent loci within this distance have comparable coverage. This observation implies the primary source of coverage variation (or amplification bias) is at or above the distance $l_c$. Therefore, statistical variation of coverage at the single-base level should reflect coverage variation at the amplicon level. To test this hypothesis, we computed the cumulative distribution of bin-level coverage (bin size $\approx 17$Kb, half of $l_c$). Normalizing the bin-level coverage by the mean depth-of-coverage, we found the cumulative distribution of bin-level coverage to be nearly identical between independent sequencing at 9x or at 0.1x (Fig. 2b), confirming that the amplicon-level coverage variation is intrinsic to the amplified DNA but independent of the sequencing depth. Furthermore, the cumulative distribution of single-base coverage at 9x sequencing depth aligned with the bin-level coverage (Fig. 2b, Supplementary Fig. 2), suggesting that the amplicon-level variation was indeed the dominant source of non-uniformity in single-cell libraries.

To further validate this conclusion, we computed the depth-of-coverage (DoC) curves and the Lorenz curves for the bulk RPE-1 library and a single RPE-1 library by MDA at different bin sizes (Supplementary Fig. 3). For the bulk library, the distribution of single-base level coverage is indistinguishable from that evaluated at the bin level when the bin size is smaller than the fragment size ($\approx 300$ bp); above this scale the bin-level distribution is more uniform than the single-base level distribution, reflecting smoothing of coverage non-uniformity.
By contrast, for the MDA generated library, the distribution of single-base level coverage remains constant until the bin size exceeds the amplicon size $\sim$ 10 kb. Characterization of coverage non-uniformity by Lorenz curves also confirmed that the same bias was observed for bin sizes less than or comparable to the amplicon size and was independent of the sequencing depth. In particular, at sequencing depths $\ll 1x$, the majority of the genome is uncovered and shows no variation in the single-base-level coverage; amplification bias, however, is manifested in the correlation between covered loci and can be evaluated by low-pass sequencing. For typical MDA-generated libraries, the amplicon size ($\sim l_c$) is on the order of 10 kb, hence at 0.1x sequencing depth there are $0.1 \times 10^4 /100 \approx 10$ reads (assuming 100 bp single-end reads) on average for each amplicon. As long as the number of reads per amplicon is much larger than the statistical variation due to random selection in sequencing (e.g., assuming poisson distribution, the standard deviation of the observable is given by the square root of the expectation), the percentage of such amplicons can be accurately calculated. At 0.1x sequencing, the amplicon-level coverage can accurately predict the fractional genome coverage down to 0.1x mean depth, when there is approximately one read for each of these under-represented amplicons; below this depth, low-pass sequencing at 0.1x cannot distinguish between regions that are severely under-amplified ($< 0.1x$ mean depth) and those that dropped out of amplification.

**Magnitude of amplicon-level variation determines coverage**

We tested the validity of the correlation analysis by analyzing DNA libraries generated from different types of cells and by different amplification technologies. For this purpose, we analyzed single-cell sequencing data of additional RPE-1 samples (Supplementary Fig. 2) and data from multiple published studies, including frozen glioblastoma nuclei (Supplementary Fig. 4), single diploid lymphoblastoid cells (Supplementary Fig. 5), frozen single neuron
nuclei (Supplementary Fig. 6), single sperms (Supplementary Fig. 7), and SW480 tumor cells (Supplementary Fig. 8); all samples were amplified by MDA. SW480 cells were also amplified by quasi-linear multiple annealing and looping-based amplification cycles (MALBAC). The amplicon size in MDA-generated libraries ranged from 5 to 50 kb, with the sperm libraries having the lowest $l_c \approx 5$ kb (Supplementary Fig. 7). Interestingly, MDA of hundreds or thousands of neurons exhibited similar amplicon sizes between 10-20 kb (Supplementary Fig. 6), consistent with estimates by standard and alkaline gel electrophoresis. In contrast, MALBAC showed a much shorter correlation length ~ 600 bp (Supplementary Fig. 8), consistent with the reported average amplicon size (500-1500 bp). We also found significant correlations at the fragment-size level in one single-cell library and the reference bulk library that persisted at high sequencing depths (Supplementary Fig. 5); these correlations reflected substantial GC bias at the fragment level absent in the other bulk libraries and likely arose during library preparation due to PCR. Despite the vastly different correlation lengths evident in MDA and MALBAC amplifications, our analysis accurately predicted the cumulative coverage distribution in all libraries sequenced to above 10x from computationally down-sampled sequencing data at 1x or less (Supplementary Fig. 2, 4-8).

To benchmark the performance of different single-cell libraries, we compared the fraction of covered genome ($\geq 1x$) when each library was sequenced to 1x. This percentage was either computed directly from down-sampled data (when the original data had higher depths) or inferred from the depth-of-coverage curve when the original data had lower depths. The coverage benchmark was plotted against the magnitude of amplicon-level variation as measured by the plateau correlation strength at the amplicon scale (Methods) (Fig. 2c). As expected, smaller amplification bias results in a larger fraction of covered genome. Out of the five
published single-cell DNA sequencing studies analyzed here, the single-neuron libraries had the
best overall uniformity, followed by the two single YH1 libraries; the MALBAC libraries overall
had less amplification bias than MDA, although optimized MDA libraries performed equally
well. The frozen glioblastoma libraries (59 total) exhibited a range of variations that can be fitted
by an empirical relationship
\[ y = \frac{0.86}{1.2 + \sqrt{x}} \]  
(1)
where \( y \) is the percentage of covered genome and \( x \) is the (dimensionless) correlation magnitude.

Except for the single-sperm libraries that exhibited substantial bias, all other analyzed data
closely followed this relationship. This result suggested that the uniformity of genome coverage
is solely determined by the amplicon-level variation but not the amplicon size. Therefore, one
can directly employ this empirical relationship to benchmark the uniformity of single-cell
libraries by the correlation magnitude that can be accurately computed from low-pass sequencing
\( \sim 0.1x \).

We further selected the best single-cell libraries from each study and compared the
fraction of genome covered at different depths as observed in the original high-depth sequencing
(Fig. 2d). Due to the different sequencing depths applied to these libraries, we plotted all
cumulative genome coverage against the normalized depth (by the mean depth). The benchmark
of amplification uniformity as measured by the depth-of-coverage curve agrees with the
computed correlation magnitude (Fig. 2c inset).

Finally we also analyzed the base-level coverage in single-cell libraries amplified by
degenerate oligonucleotide primed PCR (DOP-PCR)\textsuperscript{28}. The correlation was evident both at the
read length level (\( \sim 50 \) bp) and on a longer scale \( \sim 200 \) bp (Supplementary Fig. 9) that is
consistent with the size of purified DOP-PCR product. In comparison to MDA or MALBAC generated libraries, the smaller overall correlation magnitude (at the amplicon level) explains the better uniformity of DOP-PCR. Interestingly, even for the MDA generated libraries, shorter amplicon size tends to result in better uniformity (Supplementary Fig. 9); the underlying mechanism for this observation requires further characterization.

**Genome coverage variation reflects allele-level bias**

Coverage at the locus-level includes contributions from homologous chromosomes (the allele-level coverage). The same non-uniformity in the genome coverage, however, may result from different combinations of non-uniformity at the allelic level (Fig. 3a). Although allele coverage determines the sensitivity to detect heterozygous variants, we rarely consider this aspect in bulk sequencing due to the comparable contributions of all alleles and largely uniform coverage of the genome. In single-cell libraries, however, we often observe disproportionately represented alleles and numerous loci may exhibit “allelic dropout”\(^5,12\). Consequently, the detection sensitivity of hemizygous variants is measured by the allele coverage and needs to be derived from the genome coverage.

To predict the allele coverage from the locus-level genome coverage, we considered two limiting scenarios: a “segregated template model” (STM) assuming completely independent amplification of homologous chromosomes, and a “mixed template model” (MTM) assuming identical coverage of homologous chromosomes (as expected in bulk sequencing) (Fig. 3a). The difference between the two models is most evident in highly amplified regions: STM implies preferential amplification of one allele while MTM suggests that both alleles have been highly amplified. Both models are analytically solvable and can be easily implemented computationally (Methods, Supplementary Fig. 10).
We compared the model predictions for allele-level coverage to the observation at germline heterozygous sites detected from bulk DNA sequencing (Fig. 3b, Supplementary Figs. 5,11). For glioblastoma libraries (Fig. 3b), both locus- and allele-level coverage was calculated from disomic chromosome 12 at 1x sequencing depth. Coverage at heterozygous sites was evaluated for different disomic chromosomes (5, 12, and 13) from higher-depth sequencing at 9-10x. As expected, the total coverage (reference plus alternate bases) at these sites agreed well with the prediction for locus-level coverage, reflecting similar amplification bias for different chromosomes with the same copy number. Meanwhile, coverage of either reference or alternate bases followed the same distribution as predicted by the STM model. These results suggested homologous chromosomes are amplified almost independently during WGA and manifest the same degree of amplification bias. This discovery was further underscored by the agreement between the observed coverage of monosomic chromosome 10 and the STM allele-coverage prediction (Supplementary Fig. 11).

We further verified that coverage of alternate or reference alleles was indeed independent of each other in the glioblastoma samples by looking at the distribution of alternate and reference reads at heterozygous sites in disomic chromosome 5 (Supplementary Fig. 12). Interestingly, the two-cell RPE-1 libraries showed positive correlations between the counts of the reference and of the alternate alleles (Supplementary Fig. 12), consistent with the MTM model (Supplementary Fig. 11). Of the two published single YH1 libraries5, one agreed better with the MTM model and the other agreed with the STM model (Supplementary Fig. 5). Whether this difference resulted from the cell’s initial condition (frozen vs. fresh), the stage of cell cycle, or other factors requires further characterization.

Census-based strategy enables efficient variant detection
Our analytical prediction of the allele coverage measures the average probability of capturing a single variant read in single-cell sequencing. In sequencing analysis, however, more than one observation of the variant is necessary to mitigate sequencing errors. This requirement substantially reduces the percentage of detectable variants at low sequencing depths. In one example (GBM#4, correlation magnitude \( \approx 4 \) for disomic chromosomes), the normalized allele coverage implied that only 13.3% of clonal hemizygous variants could be confidently detected at a mean sequencing depth of 1x when requiring at least two reads for each variant (Supplementary Fig. 11). This percentage increased with sequencing depth to a limit of 79% at 100x. In contrast, the sensitivity to detect a sub-clonal mutation with allelic fraction of 0.4 in a bulk library at 10x sequencing is \( \sim 80\% \) and quickly reaches \( > 95\% \) at a sequencing depth of 20x\(^2\). The reduced dependence of detection sensitivity on sequencing depth for single-cell libraries suggested that deep sequencing of an individual library is not an efficient approach to increase power for detecting variants from libraries prepared by WGA.

To overcome this challenge, we devised an approach to sequence a large number of single-cell genomes at only modest depths (\( \sim 1x \)). We simultaneously controlled for errors resulting from random MDA artifacts or from sequencing by requiring true variants to appear in multiple libraries (“census based”) (Fig. 4a). We expected this population-based approach to be effective only when the amplification bias is random, but not recurrent (Fig. 1c). We thus evaluated the correlation between the coverage of reference and alternate alleles in four independent glioblastoma libraries. The small covariance (\( \sim 0.01 \)) between the coverage of each given allele in different libraries is consistent with random MDA bias (Table 1). These data contrasted with recurrent locus-specific amplification bias in degenerate-oligonucleotide-primed PCR methods such as GenomePlex\(^3\).
We next examined how many single cells sequenced to the same total depth would maximize the total allele coverage by census-based variant detection using a representative library with modest bias (GBM#4, correlation magnitude $\approx 4$) (Fig. 4b). In all cases, our model predicted maximum allele coverage when each individual cell was sequenced to a modest depth ($\sim 1x$). We repeated this calculation using each of the other libraries as the representative, and found that the optimal depth for detecting clonal and sub-clonal variants is always $\leq 1x$ (Fig. 4c).

To test this experimentally, we sequenced each of the following subsets of single glioblastoma libraries to 20x total depth: 59 libraries ($\sim 0.33x$ per library), 22 libraries ($\sim 1x$ per library), two libraries ($\sim 10x$ each, group A) with minimal bias (correlation magnitude $\approx 0.9$ for disomic chromosomes), and two libraries ($\sim 10x$ each, group B) with average bias (correlation magnitude $= 2-4$). We genotyped germline heterozygous SNPs and detected somatic single nucleotide variants (sSNVs) and small insertion/deletions (indels) by the census-based strategy and compared the call sets with results from bulk DNA sequencing. For germline SNPs in disomic chromosome 5, we observed that census-based detection in the two pools of single-cell libraries (59 and 22 each) each uncovered more than 80% of all SNPs detected in bulk, while the two sets of two libraries with minimal and average bias uncovered only $\sim 30\%$ and $\sim 5\%$ of the heterozygous sites, respectively (Fig. 4d). A similar improvement in sensitivity was observed for the detection of sSNVs and indels among the single cells sequenced to $\sim 0.33x$ and $\sim 1x$ per library (as opposed to $\sim 10x$ per library), detecting more somatic variants found in bulk whole-exome sequencing with fewer private or false positive calls (Fig. 4e, Supplementary Data 1 - 5). The false positive calls usually occur at low allele frequencies within each library and likely reflect recurrent amplification errors and sequencing errors. Such errors are less frequent when the library is sequenced to a low depth and can be suppressed by requiring more than one read.
for each variant. Together, these data validate our statistical estimates of the variant detection
sensitivity from a population of single cell libraries and demonstrate that a census-based strategy
using only modest depths of sequencing for many single cells can substantially improve both
sensitivity and specificity for detecting variants compared to deep sequencing of individual
libraries.

Discussion

Here we have established a universal method to characterize the amplification bias in
single-cell DNA libraries at both locus and allele levels. Based on our discovery that intrinsic
amplification bias occurs predominantly at the amplicon level, we demonstrated that the
cumulative distribution of bin-level coverage (with bin size set to the length scale of dominant
amplification bias) directly predicts the depth-of-coverage at any sequencing depth. We further
derived a quantitative measure of amplification bias that can directly predict locus-level coverage
via an empirical relationship. Our analysis thus provides a statistical description of the
relationship between the genomic coverage of single-cell DNA libraries and the intrinsic
amplification bias. This metric provides a robust benchmark that enables a quantitative
prediction of the complexity of single-cell libraries from low-pass sequencing (0.01~0.1x).

We demonstrated that amplification of different chromosomes (including different
homologous chromosomes) in a single cell is often independent (“segregated template model”),
reflecting random priming and amplification. This biophysical feature is fundamentally different
from amplification from bulk DNA, where allele-level coverage is strongly
correlated\textsuperscript{31,32} (“mixed template model”). We proposed analytically solvable models that can
quantitatively predict the allele coverage of single-cell libraries at any sequencing depth. These
models provide the basic framework for estimating the detection sensitivity of hemizygous
genetic variants by single-cell sequencing.

The characteristic length in the coverage autocorrelation also determines the scale at
which the source of amplification bias should be characterized. In bulk DNA libraries, a
dominant bias at the fragment length level is shown to be associated with the sequence content
(GC%), but such bias quickly decays at longer length scales (Supplementary Fig. 5 and 6). In
MDA-generated libraries, however, we observed substantial variation even in regions with
similar GC content (Supplementary Fig. 6). This is in sharp contrast to MDAs from bulk
samples. Such a wide range of variation reflects random priming bias instead of recurrent
polymerase extension bias, and may also depend on the size of DNA templates after cell lysis,
which is known to affect displacement efficiency. Our discoveries of the amplicon-level
correlation and independent allele amplifications are both consistent with the dominant bias
being generated in the early stage of amplification of single DNA templates and reflect the
discrete nature of single-molecule biochemical reaction. As early stage bias can be exponentially
amplified during subsequent cycles of amplification, limited amplification should result in better
uniformity.

The random nature of single-cell genome amplification further underscores the necessity
of single-cell specific bioinformatic tools and experimental design. Deep sequencing of single-
cell libraries to recover measures of variant alleles easily extends the sequencing cost and
becomes prohibitive for libraries with extreme bias. Our analyses suggest a more practical
approach by (1) preparing individual sequencing libraries from many independent samples, and
(2) ranking and selecting the best libraries based on the complexity and the allelic coverage
predicted based on low-pass whole-genome sequencing of each library (~0.1x) before extensive sequencing.

For clinical samples with a limited number of cells, such as fine-needle aspirates or circulating tumor cells, the most interesting genetic variants are shared among the cells, including both sub-clonal and clonal variants. For this purpose it is most efficient to perform “census-based variant detection” from multiplexed sequencing of independently amplified single-cell DNA libraries each sequenced to modest depths (~ 1x). The census-based variant detection strategy simultaneously controls random errors due to sequencing (0.1-1% per sequenced base) or amplification (~ 1% loci with error reads exceeding 10% allele frequency, Supplementary Fig. 7, Refs. 27 and 34) and maximizes the total allele coverage at a given sequencing depth by sampling many independently amplified libraries, thus enabling accurate detection of somatic variants and dissection of clonal heterogeneity.

One technical complication in single-cell sequencing is DNA contamination. Contamination of non-human-genomic DNA before whole-genome amplification will result in a large percentage of sequencing reads that are not mapped to the reference assembly, which can be readily identified and excluded by low-pass sequencing. The census-based strategy also effectively controls human genomic DNA contamination limited to one single-cell library. Contaminations to multiple single-cell libraries are usually present at many more copies than a single-cell genome at the affected loci and should be recognizable as they are substantially amplified after whole-genome amplification.

At the current stage, errors introduced during WGA prohibit an accurate characterization of individual genetic variants within a single cell. (This task can be accomplished through independent amplifications of biological replicates after cell division.) It is however possible to
infer global features of mutagenesis, such as the mutation rates in tumor progenitor cells or circulating tumor cells, by single-cell sequencing after correcting the total number of detected genetic variants by the statistical power for detecting variants in a single-cell library sequenced to a certain depth. Our analyses have laid the foundation for single-cell genetic variant detection by calibrating the amplification bias at both genomic and allelic levels.

**Methods**

**Amplification and sequencing of RPE-1 cells**

The hTERT RPE-1 cell line stably expressing GFP-H2B was cultured and treated as previously described. Briefly, cells were transfected with a pool of siRNAs (Smartpool, Dharmacon) against p53 using RNAiMAX (Invitrogen) according to the manufacturer’s instructions. 18-hours later cells were treated with Nocodazole (100 ng/ml; Sigma) for 6 hours. G2/M arrested cells were harvested by mitotic shake-off and replated after three washes with medium. 4h after replating, G1- released cells were sorted into 384-well tissue culture plates and cultured. Confirmed single cells were allowed to divide once, before being washed twice with PBS and lysed and amplified within the 384-well tissue culture plate as outlined above.

Amplified DNA from two RPE-1 cells after one round of cell division was subject to standard whole-genome DNA library preparation and assessed by low-pass sequencing ~ 0.1x using the MiSeq platform (Illumina). DNA libraries of RPE cells (3 total) were then sequenced to 4-9x on the HiSeq2500 platform (Illumina). Bulk RPE-1 DNA was sequenced to ~12x on the HiSeq2500 platform (Illumina).

**Processing of single-cell sequencing data**
Sequencing reads from published studies were downloaded from the NCBI Short Read Archive. For the diploid YH genome, we downloaded all sequencing runs of the bulk reference (SRR294761) and two single-cell samples, “BGI_YH1” (SRR294759), and “BGI_YH2” (SRR294760). For diploid neurons, we downloaded all the data from SRP014781, including sequencing data for the bulk DNA, and for the whole-genome amplified products from single-cell DNA, 100-cell DNA, and 50,000-cell DNA. For haploid sperms, we downloaded the deep sequencing data of 8 single sperm libraries, “Sperm23” (SRS344176), “Sperm24” (SRS344190), “Sperm27” (SRS344191), “Sperm28” (SRS344192), “Sperm101” (SRS344222), “Sperm113” (SRS344223), “Sperm135” (SRS344224), “Sperm136” (SRS344225). For SW480 tumor cells, we obtained data corresponding to the bulk reference (SRS374235), a single-cell MDA library (SRS375060), and five single-cell MALBAC libraries (SRS373654, SRS374233, SRS375671, SRS375672, SRS375673). Data of the glioblastoma libraries were generated from a previous study and can be accessible from SRP052627.

Reads were aligned to the human genome reference (hg19/GRCh37) using bwa (http://bio-bwa.sourceforge.net/) in the paired-end mode. The RPE and glioblastoma libraries were aligned by “bwa aln” followed by “bwa sampe” with default parameters. The remaining data were aligned by “bwa mem”. PCR duplicates were removed by MarkDuplicates from PICARD (http://picard.sourceforge.net/). Sequencing data of the glioblastoma libraries and the matching blood were recalibrated and indel-realigned by GATK (http://www.broadinstitute.org/gatk/) before variant detection.

Down-sampling of deep sequencing data to ~1x was done by DownsampleSam from PICARD. Base-level sequencing coverage was enumerated by the DepthOfCoverage module from GATK with minimum read mapping quality set to 5.
To evaluate the allele coverage in RPE-1 MDA libraries, we detected heterozygous SNPs in Chr.1 of the RPE-1 cells from the sequencing of bulk RPE-1 DNA (~12x) and individual MDA libraries by **UnifiedGenotyper** from GATK; only variants with Qual. ≥ 100 and at least three reference and three alternate reads in the bulk sample were selected to evaluate the allele coverage in MDA libraries. For other samples, we genotyped HapMap SNPs (v3.3) to estimate the allelic coverage; only variants found to be heterozygous in the matching blood with Qual. ≥ 500 were selected and genotyped in each set of glioblastoma libraries. Somatic single-nucleotide variants and small insertions/deletions were detected by **HaplotypeCaller** from GATK in each set of glioblastoma libraries and in the bulk library, and by **MuTect** from bulk whole-exome sequencing.

**Computation of auto-correlation function of sequence coverage**

The dimensionless auto-correlation function of coverage is defined as

\[ G(\Delta) = \frac{\langle C(x)C(x+\Delta) \rangle - \langle C(x) \rangle^2}{\langle C(x) \rangle^2}. \]  

(1)

The brackets denote average over all genomic loci \( x \) and \( \Delta \) measures the spread of correlation. In computing the auto-correlation functions we only include regions not adjacent to the assembly gaps. (Adjacency is determined by the step \( \Delta \).)

The correlation function is fitted to an exponential form to estimate the correlation length \( l_c \):

\[ G(\Delta) = a + be^{-\Delta/l_c}. \]  

(2)

For MDA, the correlation length \( l_c \) is on the order of 10 kb and the correlation function \( G(\Delta) \) is roughly constant above the fragment length (~300 bp) and below the correlation length \( l_c \). In this regime, \( G(\Delta) \) can be written as
Here $\overline{C}$ is the average coverage within each bin $[x, x + \Delta)$. It becomes evident that $G(\Delta)$ measures the standard deviation of bin-level coverage. For convenience, we choose to evaluate $G(\Delta)$ at $\Delta = 1$ kb as a quantitative metric of the magnitude of amplification bias (correlation strength).

**Statistical models for predicting allele coverage from genome coverage**

The power to detect a genetic variant is given by the probability that this variant locus (usually of one chromosome) is represented in the sequencing data, or the relative abundance of variant-supporting reads. But the direct observable in sequencing data is the total number of reads covering all possible alleles, i.e.,

$$C = m_1 + m_2 + \cdots + m_n,$$

where $C$ is the total observed coverage at a given locus as a sum of contributions from each allele denoted by $m_i$.

In the presence of amplification bias both $C$ and $m_i$'s vary across the genome. The distribution of $C$ across different loci can be straightforwardly evaluated from the depth-of-coverage curve; here we want to infer the statistical distribution of $m_i$ when the distribution of $C$ is known. The segregated template model (STM) assumes that amplifications of homologous chromosomes are independent. As a consequence, the counts of reference and of alternate bases at heterozygous sites are independent, and one highly amplified allele may dominate over the remaining ones. In the mixed template model (MTM), different alleles are assumed to be
amplified to the same extent at every individual locus. As a result, the counts of reference and of alternate bases at heterozygous sites follow a symmetric binomial distribution.

In mathematical terms, $m_i$’s are independent of each other but follow the same distribution in STM. In this scenario, one can numerically compute the distribution of $m_i$ from the characteristic functions $C(k)$ and $m(k)$ (i.e., the Fourier transforms of the probability distribution for $C$ and $m$) which satisfy

$$C(k) = m(k)^n.$$  \hspace{1cm} (5)

Here we present an iterative method to calculate the distribution of $m_i$ and illustrate this method using a diploid genome (i.e., $n = 2$).

At a given sequencing depth, denote the total percentage of loci that are covered $\geq 1x$ by $f$, the percentage of loci that are covered in a particular allele is denoted by $P(m_i \geq 1) = \lambda$. \hspace{1cm} (7)

It is then straightforward to see that

$$P(C \geq 1) = 1 - \prod_i (1 - P(m_i \geq 1))$$ \hspace{1cm} (8)

or

$$f = 1 - (1 - \lambda)^n.$$ \hspace{1cm} (9)

Hence in a region with $n$ alleles, the probability that a given allele is covered is given by
For diploid genomes, this becomes
\[ \lambda = 1 - (1 - f)^{1/2} . \]  

We can expand this further to compute the coverage at higher depths. For example,
\[ P(C \geq 2) = P(m_1 = 0)P(m_2 \geq 2) + P(m_1 = 1)P(m_2 \geq 1) + P(m_1 \geq 2) \]  

If we denote the percentage of loci where total coverage is at or above two as \( f_2 \), and the percentage of loci covered at or above two for each allele as \( \lambda_2 \), then we have
\[ f_2 = (1 - \lambda)\lambda_2 + (\lambda - \lambda_2)\lambda + \lambda_2, \]  
or
\[ \lambda_2 = \frac{f_2 - \lambda^2}{2(1 - \lambda)}. \]  
The iteration can be continued to calculate the allele coverage at any depth,
\[ P(C \geq M) = \sum_{k=0}^{M-1} p(m_1 = k)P(m_2 \geq M - k) + P(m_1 \geq M) \]  
or (denoting \( \lambda_0 = 1, \lambda_1 = \lambda, \) etc.)
\[ f_M = \sum_{k=0}^{M-1} (\lambda_k - \lambda_{k+1})\lambda_{M-k} + \lambda_M = \sum_{k=1}^{M-2} (\lambda_k - \lambda_{k+1})\lambda_{M-k} + 2(1 - \lambda)\lambda_M + \lambda_{M-1}\lambda \]  
which gives
\[ \lambda_M = \frac{1}{2(1 - \lambda)} \left[ f_M - \lambda \lambda_{M-1} - \sum_{k=1}^{M-2} (\lambda_k - \lambda_{k+1})\lambda_{M-k} \right]. \]
In the mixed template model, we assume that the local coverage $C$ is a mixture of all alleles randomly sampled at the same frequency. In disomic regions, this implies that $m$ follows a binomial distribution $B(C, 0.5)$ at any total coverage $C$. Under this model we have

$$
\lambda = P(m \geq 1) = \sum_{t=1}^{M} P(C = t) \left( 1 - 0.5^t \right)
$$

$$= \frac{1}{2} P(C \geq 1) + \frac{1}{2^2} P(C \geq 2) + \cdots
$$

$$= \frac{1}{2} f + \frac{1}{4} f_2 + \cdots + \frac{1}{2^t} f_t + \cdots
$$

(18)

where the sum runs over all observed local coverage ($t = 1, 2, \ldots M$). The series converges quickly as both $f_t$ and the exponential prefactor decay quickly. Furthermore, one easily verifies that when $f$ is small, this result is equal to the segregated template model to the leading order ($1/2 f$).

It is also straightforward to calculate the allele coverage at higher depths.

$$
\lambda_k = P(m \geq k) = \sum_{t=k}^{M} P(C = t) \left( 1 - 2^{-t} \sum_{s=0}^{k-1} \frac{t!}{s!(t-s)!} \right). 
$$

(19)

Census-based detection sensitivity from a pool of single-cell libraries

As the percentage of genome that is covered at or above 1x at any sequencing depth can be estimated, we can also predict the census-based detection power for hemizygous variants in a pool of single-cell libraries. Consider a total number of $Y$ libraries having similar amplification bias and the probability of observing a hemizygous variant in any of the $Y$ libraries is given by $\lambda$, then the probability for observing this variant in a subset of libraries ($X$ out of $Y$) is given by

$$P(\text{Covered in } \geq X \text{ libraries}) = 1 - \sum_{m=0}^{X-1} \frac{Y!}{m!(Y-m)!} \lambda^m (1-\lambda)^{Y-m}.$$ 

(20)

We can then compute this for a sub-clonal variant at clonal fraction $y$ in a total of $Z$ libraries from
\[ P(\text{Covered in} \geq X \text{ libraries}) = 1 - \sum_{Y=0}^{X-1} \frac{Z!}{(Z-Y)!Y!} y^Y \]
\[ - \sum_{Y=X}^{Z} \frac{Z!}{(Z-Y)!Y!} y^Y \sum_{m=0}^{X-1} \frac{Y!}{m!(Y-m)!} \lambda^m (1 - \lambda)^{Y-m} \]  

where random selection of cells containing the sub-clonal variant follows a binomial distribution \( B(Z,y) \).
References


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Author contributions

C.Z.Z. and V.A.A. initiated the project and carried out the analysis. C.Z.Z. performed analysis of amplification bias; V.A.A. performed analysis of census-based detection sensitivity with help from C.Z.Z. J.F., H.C., C.M., and K.L. prepared sequencing libraries for the RPE cell line and glioblastoma samples. C.Z.Z., V.A.A., J.C.L., and M.M. wrote the manuscript with help from all authors. M.M. and J.C.L. supervised the study.

Competing interests

M.M. is a founder and equity holder of Foundation Medicine, a for-profit company that provides next-generation sequencing diagnostic services.

Data access
The sequence data have been deposited in the Short Read Archive from NCBI under the following accession codes: RPE-1 bulk (SRX858057); two-cell RPE libraries (SRX858832, SRR1779331 for RPE#1, SRR1779329 for RPE#2, SRR1779330 for RPE#3); single RPE libraries (SRX858836, SRX858838, SRX858840, SRX858841); glioblastoma bulk whole-genome sequencing (SRX848889); glioblastoma bulk whole-exome sequencing (SRX857666); single-glioblastoma nuclei pool #1 (59 nuclei, SRX858332); single-glioblastoma nuclei pool #2 (22 nuclei, SRR1778915, SRR1779027, SRR1779078, SRR1779079, SRR1779080, SRR1779083, SRR1779085, SRR1779088, SRR1779089, SRR1779091, SRR1779092, SRR1779093, SRR1779095, SRR1779098, SRR1779157, SRR1779161, SRR1779163, SRR1779167, SRR1779172, SRR1779174, SRR1779175, SRR1779177); deeply sequenced single-glioblastoma nuclei (SRX858848, SRR1779345 for GBM #1, SRR1779347 for GBM #2; SRR1779348 for GBM #3; SRR1779350 for GBM #4); whole-genome sequencing of blood reference for the glioblastoma patient (SRX851083); whole-exome sequencing of the blood reference for the glioblastoma patient (SRX857684).
**Figure legends:**

**Figure 1 | Non-uniformity in genome coverage and its impact on the sequencing yield (a)**
Dependence of the information yield on the sequencing depth. Deeper sequencing of bulk libraries yields information on a larger population of cells; deeper sequencing of whole-genome amplified single-cell libraries reveals information on a larger fraction of the genome (thick lines).

**(b)** Genome coverage bias at different levels. “Amplification bias” (top): Whole-genome amplification generates coverage bias at the amplicon level, which is around 10-50 kb for multi-strand displacement amplification. “Sequencing bias” (bottom): Non-uniformity in the selection of sequencing fragments can be caused by multiple sources of bias including whole-genome amplification: the variation in sequencing coverage can be observed from 100 bp to multiple megabases. (c) Schematic representations of recurrent and random amplification bias from multiple independent amplifications of the same DNA material.

**Figure 2 | Statistical analysis of whole-genome amplification bias and coverage uniformity**
**(a)** Autocorrelation in the genome coverage of a two-cell RPE-1 DNA library (RPE#1) amplified by multi-strand displacement amplification (MDA). The same library independently sequenced to 0.1x (open triangles) and to 8x (solid triangles) exhibits a correlation above 1kb that is invariant at intermediate depths (shaded triangles) from downsampling of the 9x sequencing data. Black dashed curve represents exponential fitting of the autocorrelation in the 1-100 kb range as $2 + 0.17e^{\Delta l_c/l_c}$ with a correlation length $l_c = 33$ kb. This correlation is absent in the bulk library sequenced to different depths. Both the bulk and the MDA-generated libraries show a sequencing-fragment-level correlation ($l_c = 100$ bp) that decays with the sequencing depth. (b) The identical normalized cumulative coverage at bin size $1/2 l_c$ evaluated from the 9x (solid) and from the 0.1x sequencing (dashed) reflects the same amplicon-level variation due to MDA. The agreement between bin-level (dashed and solid lines) and base-level (red dots) depth-of-coverage curves further suggests that the bin-level variation contributes the dominant amplification bias. See Supplementary Figs. 2,4-8 for more examples of the correlation (a) and coverage (b) analysis of single-cell sequencing data from different studies. (c) Relationship between genome coverage (% covered at 1x mean sequencing depth) and amplification bias (measured by the
amplitude of the amplicon-level correlation) of single-cell libraries from different studies. Coverage is evaluated at Chr.1 for both haploid sperms and diploid cells, as well as the SW480 tumor cells (disomic in Chr.1), and at Chr.10 (monosomic), Chr.12 (disomic), and Chr.13 (disomic) for glioblastoma nuclei. The inverse dependence is fitted with an empirical formula, \( y = 0.86/(1.2+\sqrt{x}) \). (d) Comparison of the cumulative coverage in the most uniform single-cell library from each study. Data were directly evaluated from high-depth sequencing of all samples except the neuron library for which the curve was interpolated from 0.5x sequencing as in (b).

**Figure 3 | Amplification bias of homologous chromosomes.** (a) Schematic illustration of the “mixed template model” and the “segregated template model” reflecting different allele-level contributions to the same locus-level coverage. (Methods, Supplementary Fig. 10). (b) Comparison of the allele coverage predictions (“Pre.”) from 1x sequencing depth with the observed coverage at heterozygous sites (“Obs.”) at 9x sequencing depth in three single glioblastoma libraries. The combined coverage of reference and alternate bases (red dots) at 9x sequencing validates the prediction from 1x sequencing (dashed curve). The allele coverage (reference or alternate) is then predicted from the combined coverage assuming mixed templates (MTM, blue dotted lines) or segregated templates (STM, green dotted lines) and compared to the coverage of reference (blue triangles) or alternate (green triangles) bases at heterozygous sites. The predictions were made from the sequence coverage in disomic Chr. 12 but the agreement with observations in different disomic chromosomes demonstrate that amplification bias is consistent in all chromosomes.

**Figure 4 | Variant detection in single-cell genomes.** (a) Census-based variant calling requires that acceptable variants be observed in at least two independent single-cell libraries. (b) Estimates of the census-based detection sensitivity for a population of independently amplified single-cell libraries all assumed to have similar amplification bias as GBM#4 (Supplementary Fig. 11). Optimal detection sensitivity is achieved at roughly 0.5x depth-per-library regardless of the sub-clonal fraction or the total sequencing depth. (c) Optimal depth-per-library for census-based variant detection in a population of independently amplified single-cell libraries assumed to have similar coverage bias. The range of the optimal depths is calculated based on the
amplification bias observed in single glioblastoma libraries in Fig. 2b. For libraries with more bias or for the detection of variants with lower clonal fractions it is optimal to sequence more libraries at modest depths (0.1-0.5x). (d) Observed coverage of reference and alternate bases at heterozygous SNP sites in disomic Chr.5 as an estimate of the census-based detection sensitivity for clonal variants. A varying number of single glioblastoma nuclei (59, 22, and 2) were sequenced to the same total depth (20x) and genotyped at germline heterozygous SNP sites. Group (A) included two cells with the best uniformity and group (B) included two cells with average uniformity. For either heterozygous coverage or the detection of alternate bases, the larger pools offer better sensitivity than the two groups of two cells. (e) Comparison between somatic non-synonymous variants detected in different sized pools of single cells sequenced to the same total depths (20x). The truth set (48 variants in total) included 43 variants that were detected in both 30x whole-genome and 120x whole-exome sequencing of bulk tumor DNA, plus five additional variants detected in bulk whole-genome and single-cell sequencing. At the same overall sequencing depth, census-based detection from a population of cells (59 and 22) offers higher sensitivity and better specificity over deep sequencing of two libraries. A larger number of private/false positive mutations are observed when individual samples are sequenced to higher depths, and these private calls often arise from sporadic sequencing errors that coincide with amplification errors.

Tables:

Table 1 | Overlap and correlation between allele coverage in independent single-cell libraries by multi-strand displacement amplification. Allele coverage in each library is evaluated by the number of covered HapMap heterozygous SNP sites in disomic chromosome 5 detected in bulk sequencing (combining blood and bulk tumor) by UnifiedGenotyper (Qual. ≥ 500). (a) In each single-cell library, coverage of A and B alleles is almost equal and the expected overlap assuming random A or B allele coverage—the estimated coverage of heterozygous sites—is comparable to the observed number of heterozygous sites. (b) The overlap between different single-cell libraries’ coverage of each allele is also close to the expected overlap based on random allele coverage.
Fig. 1

a  Library complexity and sequencing yield

original genome

bulk DNA libraries

DNA library

whole-genome amplified single-cell DNA libraries

b  Coverage bias at different levels

amplification bias

WGA amplicons

10 ~ 50 kb for MDA

sequencing bias

sequencing fragments

variation at different scales

~ 1 kb

C  Recurrent and random amplification bias

recurrent amplification bias

random amplification bias

WGA1

WGA2

WGA3
Fig. 2

(a) Correlation at the fragment level

\[ \sim 2 + 0.17 e^{-\Delta/l_c} \]

\( l_c \approx 33 \text{ kb} \)

(b) Normalized auto-correlation

(c) Fraction of genome covered

\[ y = \frac{0.86}{1.2 + \sqrt{x}} \]

(d) Normalized depth
**Fig. 3**

**a Amplification of homologous chromosomes**

<table>
<thead>
<tr>
<th>Allelic distortion in amplification</th>
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</thead>
<tbody>
<tr>
<td>allele A</td>
</tr>
</tbody>
</table>

**locus-level** (combined)

- Correlated coverage of allele A and allele B
- Independent coverage of allele A and allele B

**b Allele coverage predictions for single glioblastoma libraries**

- **GBM #1**: Obs. (Chr. 5) vs. Pre. (Chr. 12)
- **GBM #2**: Obs. (Chr. 13) vs. Pre. (Chr. 12)
- **GBM #3**: Obs. (Chr. 12) vs. Pre. (Chr. 12)

**Observation from 9x**
- combined
- ref allele
- alt allele

**Prediction from 1x**
- locus-level
- MTM
- STM
**Fig. 4**

**a** census-based variant calling

- Library #1
- Library #2
- Library #3

* accept (variant allele detected in ≥ 2 libraries)
* reject (variant allele detected in 1 library only)

Census-based sensitivity = % allele covered in ≥ 2 libraries

**b** predicted census-based sensitivity

- 20x total sequencing depth
- 40x total sequencing depth
- 60x total sequencing depth

**c** predicted optimal depth per library

**d** observed census-based sensitivity (germline/clonal)

- SNPs detected (%)
- SSNVs/indels detected (#)

- Both alleles (correct genotype)
- At least alt. allele

- 20x total
- 40x total

**e** observed census-based sensitivity (somatic/subclonal)

- Also in bulk
- Private / false positive

- 20x total
- 40x total

# cells sequenced
**Table 1a** | Coverage at heterozygous sites in single glioblastoma nuclei libraries

<table>
<thead>
<tr>
<th></th>
<th>Depth</th>
<th>Total</th>
<th>Reference</th>
<th>Alternate</th>
<th>Allelic %</th>
<th>Hets (est.)</th>
<th>Hets (obs.)</th>
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</thead>
<tbody>
<tr>
<td>(i)</td>
<td>9.2x</td>
<td>49,457</td>
<td>40,345</td>
<td>40,356</td>
<td>72%</td>
<td>28,931</td>
<td>29,336</td>
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<tr>
<td>(ii)</td>
<td>8.1x</td>
<td>48,745</td>
<td>39,569</td>
<td>39,521</td>
<td>70%</td>
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<td>28,149</td>
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<tr>
<td>(iii)</td>
<td>6.6x</td>
<td>35,765</td>
<td>22,163</td>
<td>21,549</td>
<td>39%</td>
<td>8,486</td>
<td>7,950</td>
</tr>
<tr>
<td>(iv)</td>
<td>9.0x</td>
<td>37,507</td>
<td>23,763</td>
<td>23,883</td>
<td>42%</td>
<td>10,084</td>
<td>10,144</td>
</tr>
</tbody>
</table>

Total germline heterozygous SNPs in Chr. 5: 56,278 (qual. ≥ 500, HapMap)

**Table 1b** | Overlap between independent single-nuclei libraries (Covariance = $p_{AB} - p_A \cdot p_B$)

<table>
<thead>
<tr>
<th></th>
<th>Allele A</th>
<th>Allele B</th>
<th></th>
<th>Allele A</th>
<th>Allele B</th>
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<th>Allele B</th>
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<td>40,356</td>
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