How temporal patterns in rainfall determine the geomorphology and carbon fluxes of tropical peatlands

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How temporal patterns in rainfall determine the geomorphology and carbon fluxes of tropical peatlands

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Tropical peatlands now emit hundreds of megatons of carbon dioxide per year because of human disruption of the feedbacks that link peat accumulation and groundwater hydrology. However, no quantitative theory has existed for how patterns of carbon storage and release accompanying growth and subsidence of tropical peatlands are affected by climate and disturbance. Using comprehensive data from a pristine peatland in Brunei Darussalam, we show how rainfall and groundwater flow determine a shape parameter (the Laplacian of the peat surface elevation) that specifies, under a given rainfall regime, the ultimate, stable morphology, and hence carbon storage, of a tropical peatland within a network of rivers or canals. We find that peatlands reach their ultimate shape first at the edges of peat domes where they are bounded by rivers, so that the rate of carbon uptake accompanying their growth is proportional to the area of the still-growing dome interior. We use this model to study how tropical peatland carbon storage and fluxes are controlled by changes in climate, sea level, and drainage networks. We find that fluctuations in net precipitation on timescales from hours to years can reduce long-term peat accumulation. Our mathematical and numerical models can be used to predict long-term effects of changes in temporal rainfall patterns and drainage networks on tropical peatland geomorphology and carbon storage.

Significance

A dataset from one of the last protected tropical peat swamps in Southeast Asia reveals how fluctuations in rainfall on yearly and shorter timescales affect the growth and subsidence of tropical peatlands over thousands of years. The pattern of rainfall and the permeability of the peat together determine a particular curvature of the peat surface that defines the amount of naturally sequestered carbon stored in the peatland over time. This principle can be used to calculate the long-term carbon dioxide emissions driven by changes in climate and tropical peatland drainage. The results suggest that greater seasonality projected by climate models could lead to carbon dioxide emissions, instead of sequestration, from otherwise undisturbed peat swamps.


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Once the peatland surface is sufficiently domed, water is shed so rapidly that no more organic matter can be waterlogged within the confines of the drainage network, and peat accumulation stops (10). This maximally domed shape sets a limit on how much carbon a peat dome can sequester and preserve under a given rainfall regime (11). If the peat dome is flatter than its stable shape for the current climate, it will sequester carbon and grow; if it is more domed than its stable shape, it will release carbon and subside as peat decomposes. [In the tropical peat literature, “subsidence” is used for a decline in the peat surface elevation, regardless of mechanism (5).] The volume of this stable shape times the average carbon density of the peat defines a capacity for storage of carbon as peat within the drainage boundary.

If we can predict the stable shapes of peat domes and how they evolve over time in a given climate, we can determine how peatland carbon storage capacity and carbon fluxes are affected by changes in rainfall regime, drainage network, and sea level. However, when predicting the stable shapes of peat domes and their evolution toward these shapes, there are two complicating factors: (1) The boundaries imposed by drainage networks have complex shapes and (2) rainfall is intermittent and variable. The water table rises during rainstorms and falls during dry periods, even when the peat surface is stable. These fluctuations in the water table seem to be important because it is widely believed that seasonality of rainfall affects tropical peat accumulation (12, 13). But how should we take these fluctuations into account to predict the slow development and stable shapes of peat domes? Understanding the global impact of changes in rainfall amount and variability, drainage networks, and sea level on tropical peatland carbon storage and fluxes requires a theory that can accommodate the complicated drainage networks and intermittent rainfall of the real world.

Ingram (10) made the first prediction of the limiting shape of a temperate peat dome imposed by the balance between rainfall and groundwater flow. Assuming constant rainfall, he computed the steady-state shape of a peat dome with uniform permeability between parallel rivers. Clymo (14) later developed a simple dynamic model for accumulation of peat at a single point in the landscape. Clymo’s model assumed that the thickness of peat above the water table would not change and focused on anaerobic decomposition in deeper waterlogged peat. Hilbert et al. (15) later built on Clymo’s model to allow a varying thickness of peat above the water table via a simple water balance whereby drainage increases linearly with peat surface elevation. Hilbert’s model inspired a series of increasingly sophisticated models for vegetation dynamics and peat accumulation at a point. The most recent of these point models computes water table depth from monthly rainfall, using a site-specific model (16). Meanwhile, numerical models have been used to simulate peat accumulation under constant rainfall (17, 18).

### Methods

#### Field Measurements

We established a field site in one of the last pristine peat swamp forests in Southeast Asia and then used measurements from this site to develop a mathematical model for the geomorphic evolution of tropical peatlands that is simpler, yet more general than Ingram’s model for high-latitude peatlands. Our model makes it possible to predict effects of changes in rainfall regime and drainage networks on carbon storage and fluxes in tropical peatlands. The model predicted, perhaps surprisingly, that surface peat would be older near dome margins. We tested these predictions by radiocarbon dating core samples and comparing the age of each sample to the simulated age at its location and depth. Finally, we explored the future of tropical peatlands under climate projections by simulating the geomorphic evolution of an idealized peat dome under projected changes in rainfall patterns and drainage.

#### Morphology vs. Microtopography

Superimposed on the gross morphology of a peat dome is a fine microtopography of meter-scale depressions, or hollows, separated by higher areas, or hummocks (19, 20). The hummocks consist of partly decomposed logs, branches, and leaves lodged among living buttresses, stilt roots, pneumatophores, and giant rhizomes. Whereas the microtopography in high-latitude peat bogs may have regular and oriented patterns (21), surveys by Lampela et al. (20) in a tropical peat swamp in Central Kalimantan showed no orientation or regularity. Similarly, our microtopography survey and other observations revealed no regular patterns or channels in peat dome microtopography.

In describing the evolution of peat dome morphology, we want to capture the effects of the hummock-and-hollow microtopography without explicitly simulating its details. Measurements from the 12 piezometers along our microtopography transect showed that the water table is relatively smooth, even though the peat surface is highly irregular on a spatial scale of centimeters to meters (Fig. 3). We therefore represent the peat surface by a reference surface \( \rho \), smooth like the water table, that underlies the actual peat surface \( \rho \). We refer to this reference surface \( \rho \) as the land surface. The peat surface \( \rho \) is a “texture” that sits on the smooth land surface \( \rho \). The bottoms of hollows provide the most readily identifiable local reference elevation (20), so we define the land surface \( \rho \) as a smooth surface fit through the bottoms of hollows (local minima in the peat surface \( \rho \)). On the basis of this definition, we determined the current land surface at our site by smoothing a raster map obtained from local minima in LiDAR last-return points. We also used the transect survey and piezometer data to find the land surface \( \rho \) along the microtopography survey transect (SI Methods).

#### Groundwater Flow

We model the dynamics of the water table \( H \) subject to net precipitation \( q_n \) (rainfall intensity \( R \) minus evapotranspiration, ET), using Boussinesq’s equation for essentially horizontal groundwater flow

\[
S_y \frac{\partial H}{\partial t} = q_n + \nabla \cdot (T \nabla H),
\]

where

- \( S_y \) is the specific yield of the peat
- \( q_n \) is the net precipitation
- \( T \) is the transmissivity
- \( \nabla \cdot (T \nabla H) \) is the mass flux due to gravity
- \( \nabla \) is the divergence operator
- \( \partial H/\partial t \) is the change in water table depth with time

### References

The peat surface is stable, neither growing nor subsiding \( \langle \partial p / \partial t \rangle = 0 \) wherever the water table fluctuates in such a way that peat production is balanced by decomposition over time

\[
fp = (p - H) \alpha
\]

where angle brackets \( \langle \rangle \) indicate a time average.

Several other studies have shown a leveling off of soil CO\(_2\) efflux at very low water tables (25, 26), and it is also likely that very high water tables ultimately limit net carbon uptake by trees (primary production) (16). However, including these effects did not affect simulations because these extreme water table heights and depths were neither observed at our site nor predicted by simulations of our site. We also did not include anaerobic decomposition below the water table because analyses of peat cores from tropical sites in Asia (2), including our site (27), do not show detectable loss of waterlogged peat from anaerobic decomposition.

**Numerical Simulations.** We built a numerical model of waterlogging and peat accumulation based on Eqs. 1 and 2 to simulate peat dome geomorphogenesis and carbon fluxes. These two equations are coupled by the water table elevation \( H \) and the specific groundwater flow \( p \), both of which vary in time and space. The equations require four parameters: (i) a specific yield function \( S_y \), (ii) a transmissivity function \( T \), (iii) a rate of peat production \( f_p \), and (iv) a decomposition rate constant \( \alpha \). The model uses a finite volume scheme (Fig. S1) with special features designed to handle the severe nonlinearity of the transmissivity function \( T \) (SI Expanded Description of Peat Dome Simulation).

We determined the specific yield and transmissivity functions \( S_y, T \) from the response of the water table to heavy rain and dry spells (Results and Discussion). We then fitted the parameters for peat accumulation \( f_p, \alpha \) by simulating the 2,700-y evolution of a peat dome at our field site in Brunei and matching the simulated modern peat surface to the peat surface measured by LiDAR. We tested our model against radiocarbon dates from peat cores extracted from the peatland and then used the model to answer general questions about carbon fluxes from tropical peatlands after perturbation by climate change and drainage.

**Limitations of Modeling Approach.** Our goal was to build the simplest model that can make reasonable quantitative predictions of tropical peat dome dynamics. In most Southeast Asian peatland complexes, every area between rivers is occupied by a peat dome, so it is not apparent how any peat dome could now expand to fill a larger area. However, domes tend to be larger in older peatlands, suggesting a long-term process of dome coalescence. We did not attempt to model these long-term changes in river networks. We also did not consider changes in hydraulic conductivity near the surface caused by compaction or changes in microtopography under agriculture.

**Results and Discussion**

**Carbon Storage Capacity of Tropical Peatlands.**

**Local water balance is dominated by flows near the surface.**

Eighteen months of data on water table height in five piezometers along a 2.5-km transect (Fig. 5) show two distinctive features of water table behavior in tropical peatlands. First, when the water table is high, it falls very rapidly; and second, the water table height relative to the land surface remains approximately uniform during dry intervals between rains (Fig. 5 E and F). During heavy rain, the effects of evapotranspiration and outward flow are negligible, and the rainfall intensity vs. rate of increase in water table height gives the specific yield. Between rain events, the water table declines because of evapotranspiration and the divergence of groundwater flow.

Transmissivity \( T \) is a function of water table height \( \zeta \) and controls the divergence of groundwater flow \( \nabla \cdot (T \nabla \zeta) \). We determined the effect of water table height on transmissivity
We observe that water table height is uniform ($\nabla \zeta = 0$). If transmissivity $T$ is also spatially uniform, the groundwater divergence term simplifies to the transmissivity times the peat surface Laplacian $\nabla \cdot [T \nabla (p + \zeta)] = T \nabla^2 p$. The time derivative $\partial p / \partial t$ of the land surface elevation is negligible because peat accumulation or loss is much slower than rise or fall of the water table, so the term $p$ can be dropped from the time derivative. We observe that the fluctuations in water table height $\partial \zeta / \partial t$ are uniform, as is net precipitation $q_n$, so the groundwater divergence term $T \nabla^2 p$ must also be spatially uniform. Thus, Boussinesq’s equation simplifies to an ordinary differential equation (ODE) describing the uniform fluctuation of the water table relative to the peat surface

$$S_n \frac{d\zeta}{dt} = q_n + T \nabla^2 p.$$  

where the peat surface Laplacian $\nabla^2 p$ is uniform.

---

**Fig. 3.** Microtopography and water table dynamics in a tropical peatland. (A) Cartoon of tropical peat cross-section showing variables $\tilde{p}$, the peat surface; $p$, the “land surface,” a smooth surface fit through local minima in $\tilde{p}$; $H$, water table elevation; and $\zeta$, water table height relative to the land surface, $\zeta = H – p$. The peat surface $\tilde{p}$ is irregular on a spatial scale of meters, with higher areas (hummocks) separating local depressions (hollows) that are not connected into channels. (B) Total station survey of peat elevation $\tilde{p}$ (black circles) along a transect and the land surface $p$ (dashed black line). The minimum, median, and maximum water table elevations $H$ from each of 12 piezometers along the transect are also shown (dashed blue lines). The absolute elevation of the survey points comes from matching local minima among survey points within 20-m × 20-m squares (white diamonds) with local minima in LiDAR last return data within the same squares (red diamonds). The land surface $p$ is represented by the dashed horizontal black line. (C) Water table dynamics along a survey transect (B) in late 2012, relative to the land surface $p$. What appears to be a single blue line is superimposed data from the 12 piezometers shown in B. Also shown are the average minimum, median, and maximum water table elevations above the land surface during the same time period for all 12 piezometers.

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**Fig. 4.** Peat accumulation and CO$_2$ flux vs. water table height in tropical peatlands. (A) Peat accumulation represents the balance between peat production and decomposition. (B) Aerobic decomposition is one of the two main sources of peat surface CO$_2$ flux; the other source is root respiration. A shows peat accumulation or loss vs. water table height from model calibration (solid line) and from literature subsidence data (circles, ref. 4; triangles, ref. 22). The straight line was not fitted to these data, but rather arose naturally from calibration to match the model surface of the Mandomar peat dome (Fig. 7). In B, soil surface CO$_2$ flux vs. water table height at our site in Brunei Darussalam (white circles) was very similar to fluxes in other tropical peatlands (squares, ref. 23; diamonds, ref. 19; triangles, ref. 24; pentagons, ref. 9; and hexagons, ref. 25).
The peat surface Laplacian describes the curvature of the peat surface: It is equal to the sum of the second derivatives of the surface elevation in two perpendicular horizontal directions \( (\nabla^2 p = \partial^2 p / \partial x^2 + \partial^2 p / \partial y^2) \). Thus, analysis of water table dynamics predicts uniform curvature of the peat surface where water table fluctuations are uniform. This uniformity of surface elevation curvature can be tested against elevation maps.

Maps of the peat surface Laplacian are highly sensitive to microtopographic noise in the surface elevation map because the Laplacian uses second derivatives. However, by the divergence theorem, the average Laplacian within any closed contour is equal to the integral of the normal gradient along the contour divided by the enclosed area. Therefore, we can examine the uniformity of the surface Laplacian by studying the slope of a regression between the integrated normal gradient and the enclosed area (Fig. 6). Indeed, we find a linear relationship between the integrated normal gradient along each contour and the area enclosed by the contour in our LiDAR-derived peat surface elevation map, indicating a uniform surface Laplacian value until peat production balances decomposition (Eq. F). In this way, we can compute the stable topography of any tropical peatland by solving Poisson’s equation (Eq. 7) for the stable peat surface morphology \( p_\infty \) using the appropriate Laplacian value for that climate.

Climate and drainage network determine tropical peatland carbon storage capacity. By specifying the stable peatland topography, the uniform-Laplacian principle gives the peat carbon storage capacity inside any drainage boundary and in any given climate. The volume under the surface satisfying Poisson’s equation \( \nabla^2 p_\infty \) is minus the average net precipitation divided by the average transmissivity

\[
\nabla^2 p_\infty = \langle q_n \rangle / \langle T \rangle
\]

We can compute the stable topography of any tropical peatland by solving Poisson’s equation (Eq. 7) for the stable peat surface morphology \( p_\infty \), using the appropriate Laplacian value for that climate. The average transmissivity \( \langle T \rangle \) is a complicated function of the temporal pattern of rainfall and the hydrologic–biological system. However, for any rainfall regime, one can find the stable surface Laplacian \( \nabla^2 p_\infty \) by repeatedly simulating water table fluctuations (Eq. 5) with a trial Laplacian \( \nabla^2 p \) and adjusting the Laplacian value until peat production balances decomposition (Eq. 3) everywhere in the peatland (SI Methods). In this way, one finds a shape parameter \( \langle \nabla^2 p_\infty \rangle \) that describes stable peatland morphology under a given rainfall regime in any drainage network.
2,300-y development, we predict that in about 2,500 y it will reach a stable shape with a mean peat depth of 4.54 m (max 7.10 m) and store 1,800 t C · ha⁻¹ (Fig. S3; simulations of dynamics are described in the next section).

The uniformity of the stable peat surface Laplacian is an approximation that requires that (i) peat accumulation rate \( \partial p/\partial t \) is a nondecreasing function of water table height, (ii) flow of water is proportional to water table gradient (Boussinesq’s equation), and (iii) transmissivity is independent of location because flow through deep peat is negligible compared with near-surface flow. In reality, groundwater flow through deeper peat will result in a deviation of the stable peat dome surface from the uniform-Laplacian shape in very large peat domes. Specifically, groundwater flow through deep, low-permeability near-surface peat near the boundary. Deep groundwater flow should be manifested as a downward (dome center) or upward (dome margin) trend in the water table during nights without rain when the water table is low; no such trend is apparent in our piezometer data (Fig. 5D), suggesting that deep groundwater flow is small. A small deep groundwater flow term is further supported by radiocarbon dating of porewater dissolved organic carbon at our site (31), which suggests a maximum downward velocity of water of about 1 m/y or at most a 1.4-mm water table decline during a single 12-h night, 1/16th of the 22-mm water table decline from evapotranspiration during the day (Fig. 5). (Evapotranspirative flux is about 1/10th of the rate of decline of the water table from evapotranspiration because about 1/10th of the deep peat cross-section is available for water flow; see specific yield curve in Fig. 5B.)

A shape parameter related to our stable peatland Laplacian (Eq. 7) appeared in Ingram’s model for temperate peatland morphology (10) assuming constant precipitation, uniform hydraulic conductivity, and simple river geometry (Ingram’s parameter is net precipitation divided by hydraulic conductivity, instead of average transmissivity). Our result is more general, because it handles varying rainfall and arbitrary landscapes, but is also mathematically simpler, because of our finding that transmissivity in tropical peatlands is approximately independent of peat depth.

Dynamics of Tropical Peatland Topography and Carbon Fluxes. Peat accumulation parameters regulate dome dynamics. Our analysis shows how the rate of peat production \( f_p \) and decomposition rate constant \( \alpha \) affect both the stable morphology and the dynamics of tropical peat domes. These parameters of the peat accumulation function (Eq. 2) have an indirect but strong effect on the stable peatland Laplacian and hence peatland carbon storage capacity via the mean transmissivity \( \langle T \rangle \) (Eq. 7) because the mean water table depth must be equal to the ratio of the peat production rate to the decomposition rate constant \( f_p/\alpha \); Eq. 3). A higher decomposition rate constant implies a higher mean water table in stable peat domes, meaning...
a higher transmissivity, a smaller stable surface Laplacian, and less carbon storage. If both peat production \( j_p \) and the decomposition rate constant \( \alpha \) increase together, carbon storage capacity does not change, but peat dome dynamics are faster. Fit parameters match literature data. Peat accumulation parameters fitted to the topography of a peat dome at our Brunei field site agree with published data from other sites and also with our other field data (next section). We obtained peat accumulation parameters \( j_p, \alpha \) by simulating the evolution of the dome (Fig. 7) and minimizing the least-squares difference between the simulated peat surface and the modern peat surface measured by LiDAR. We then compared our calibrated peat accumulation function to literature data on subsidence in drained, vegetated peat swamps (4, 22). Our linear peat accumulation function was not calibrated to these subsidence data from the literature—only to the modern peat surface—but nonetheless matched the subsidence data almost exactly (Fig. 4A; \( j_p = 1.46 \text{ mm y}^{-1}, \alpha = 1.80 \text{ d}^{-1} \)). Our soil CO\(_2\) chamber measurements were also very similar to those from other sites, suggesting that the effect of water table on fluxes is similar at our site and in other tropical peatlands (Fig. 4B).

The uniform-Laplacian principle predicts a central bog plain and old peat near the surface at bog margins. We find that a tropical peat dome reaches its stable shape first at its boundaries, because the stable dome surface is lowest there (Figs. 7 and 8 and Fig. S2). Meanwhile, the interior of the peat dome continues growing at an approximately uniform rate, forming a relatively flat (smaller-magnitude Laplacian) central bog plain. The vegetation of tropical bog plains may not be distinct (1), unlike the unforested bog plains of high-latitude peatlands (21); instead, we define the bog plain of a tropical peat dome as the central region that has not yet reached its stable Laplacian. Whereas the dome center continues to accumulate peat and sequester carbon, the margin has reached its stable shape and stopped growing, so peat near the surface is older there.

Older peat near dome margins has not been predicted before, so we collected 22 additional radiocarbon dates from basal and near-surface peat samples to test this prediction. These radiocarbon dates confirmed that near-surface peat was older near dome margins than at the same depths toward the interior of the same domes (Fig. 7C). We also compared radiocarbon dates in deeper peat to simulated ages at the same locations and depths, excluding basal samples from the mangrove peat before the establishment of the peat swamp forest (Fig. 7 and SI Methods) (1, 27). Radiocarbon dates and simulated ages at the same locations and depths matched well (Fig. 7B). We did not expect radiocarbon dates from cores to match simulated peat ages exactly because (i) the drainage network may have shifted during the 2,300 y of dome growth, (ii) tree root growth may inject young carbon into peat below the surface, and (iii) tree falls in peat swamp forests remove older peat to form tip-up pools that then fill with younger peat. In an earlier study, we estimated that replacement of older peat by younger peat in tip-up pools would bias radiocarbon dates of deep peat to about 500 y later than when material was first deposited in that stratum (figure 11 in ref. 27), consistent with the offset between measured radiocarbon dates and ages simulated by our model (Fig. 7B).

**Carbon sequestration rate is proportional to bog plain area.** The centripetal pattern of dome development makes the rate of carbon sequestration roughly proportional to the area of the central
bog plain (Fig. 8). Under a given climate, the rate of sequestration decreases as the dome approaches its stable shape and the central region of peat accumulation—the bog plain—shrinks in area. For example, our simulations imply that the current rate of CO₂ sequestration at our site (0.80 t ha⁻¹ y⁻¹, 100-y average) is less than one-quarter of its initial rate about 2,300 y ago (3.81 t ha⁻¹ y⁻¹), and CO₂ sequestration is more than five times faster at the dome interior (1.89 t ha⁻¹ y⁻¹, 6.37 km from the river) than at its edge (0.36 t ha⁻¹ y⁻¹, 1 km from the river; Fig. S3). The mechanism of tropical peat dome development that we describe therefore creates landscape-scale patterns in local carbon fluxes and radiocarbon date profiles. Local measurements of carbon fluxes or radiocarbon dates cannot be upscaled to regional fluxes without considering dome morphology because the flatter interior of each peat dome sequesters carbon whereas the margins do not (Fig. 8). Old peat near the peatland surface (2), although in some cases caused by local climate change or disturbance, also can be expected at the margin of any peat dome.

**Future Effects of Changes in Drainage Networks and Climate.** Our analysis provides a simple way of predicting long-term change in peat dome morphology and carbon storage in response to changes in drainage network, climate, or sea level because the stable peat surface Laplacian completely specifies the stable peat topography with given drainage boundary conditions. If the drainage network changes, we can solve Poisson’s equation in the new drainage boundary to compute the gain or loss of peat, and the net carbon emissions, as the peat surface approaches its new stable topography. If the climate changes, we can compute a new stable Laplacian value for the new climatic conditions and determine how much a currently stable peatland will grow or subside.

**Subdivision of a peatland by drainage canals reduces carbon storage.** The average surface elevation of a stable peat dome is proportional to the area of the dome because of the uniform-Laplacian principle. If we scale the area of a peat dome by some factor k by multiplying both x and y coordinates by √k, the surface elevation p must increase by the same factor k to keep the same Laplacian. Therefore, the carbon storage capacity of a peat dome scales with its area. For example, a peat dome that is cut into halves of approximately the same shape as the original dome will have one-half the carbon storage capacity (half the mean stable peat depth) of the original dome. This provides a straightforward way to estimate the long-term impacts of artificial drainage networks that are now affecting over 50% of the peatlands of Southeast Asia (32) and from which a robust quantification of carbon emissions is urgently needed (6).

The dynamic response of a peat dome to changes in rainfall and sea level also depends on its area because of the centrifugal pattern of dome development (Fig. 8). Because of their higher stable mean depth, larger-area domes reach their stable shape more slowly than smaller-area domes.

**Relative effects of climate change on carbon storage capacity are independent of drainage network.** Although peatland drainage networks play a central role in determining absolute carbon storage and dynamics, we can calculate the proportional effect of climate change on long-term carbon storage of a tropical peatland independent of the drainage network. Poisson’s equation (Eq. 7) must be solved in each drainage boundary to obtain the topography of the stable peat surface. However, we can then predict the effects of changes in climate independent of the drainage network because of the linearity of the Laplacian operator. By the definition of linearity for a mathematical operator, a peat surface Laplacian that is larger by some factor k corresponds to a peat surface that is vertically stretched by the same factor (k√k/p = ∇²kp) and therefore has a mean peat depth that is larger by the same factor. Thus, carbon storage capacity per area p∞ is proportional to the stable peat surface Laplacian

\[ p∞ ∝ Ω^2p∞. \]

**Dynamic simulations converge to new stable morphologies after changes in conditions.** Our simulations of peat dome dynamics demonstrate the convergence of initially stable domes to new, stable, uniform-Laplacian morphologies after perturbations (Fig. 9). The simulations show the effect of increased total rainfall (Fig. 9A and E), which is a recognized climate feedback for tropical peatlands (12), and also show that artificial drainage for agriculture (Fig. 9D) can dominate all natural feedbacks if not curtailed (4, 16). In addition, our simulations demonstrate a third feedback: The increase in rainfall variability from warming climates (33) can cause peat loss if not compensated by an increase in total rainfall (Fig. 9 C and F). For these simulations, we generated new rainfall time series as similar to current rainfall as possible but with larger annual and El Niño–Southern Oscillation (ENSO) fluctuations (Fig. S4 A and B and SI Setting Annual and ENSO Amplitudes of Rainfall). Either greater seasonality or a stronger ENSO decreased peatland carbon storage capacity, but an increase in seasonality had a larger maximum effect, partly because the magnitude of the ENSO fluctuation is smaller. In contrast, sea level rise could drive peat accumulation in the long term by elevating the tidal rivers draining most peat domes (Fig. 9 B and E). In general, losses can be much more rapid than accumulation (Fig. 9E), because subsidence of drained peatlands can be far faster than typical accumulation rates (4). For example, the estimated area-averaged current CO₂ sequestration rate at our site is 0.80 t ha⁻¹ y⁻¹, whereas Hooijer et al. (5) estimated CO₂ emissions of at least 73 t ha⁻¹ y⁻¹ from tropical peatlands under plantation agriculture.

**Intermittency of rainfall reduces tropical peatland carbon storage.** We find that fluctuations in net precipitation on timescales from hours to years can reduce long-term peat accumulation. We further explored the effects of variability in rainfall seen in our

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**Fig. 10.** Effects of climate change on carbon storage capacity of tropical peatlands. (A) Simulated carbon storage capacity (contours) vs. time-averaged rainfall and interval between storms in a simple rainfall model (Poisson process for storm incidents, exponentially distributed rain depth per storm). The balance between rainfall and groundwater flow sets a limit on the curvature of the peat surface and therefore limits the amount of carbon that can be stored as peat in a peatland. This carbon storage capacity is proportional to the Laplacian of the stable peat surface elevation (Results and Discussion), so the relative effect of changes in rainfall patterns on carbon storage capacity can be calculated independent of the drainage network. Higher rainfall increases carbon storage capacity, whereas increased time between storms reduces it. (B) Carbon storage capacity (contours) as in A, but driven by rainfall at our site (diamond) or with a weakened or strengthened annual or El Niño–Southern Oscillation fluctuation in rainfall. The vertical shift to lower carbon storage with increased annual variation in rainfall (up arrow) corresponds to the simulated effect of increased seasonality in Fig. 9.
dynamic simulations (Fig. 9) by computing the effect of interstorm arrival time and annual and ENSO fluctuations on peatland carbon storage capacity (Fig. 10). The simulations demonstrate that long-term peat accumulation is controlled by variation in rainfall, not only by mean rainfall, because fluctuations in the water table cause exponential changes in groundwater flow. The high outward flow during peak water tables is not compensated by low flow rates after the water table declines. For example, a steady drizzle at the same average intensity as the intermittent rainfall actually observed at our site would sustain more than 10 times more long-term carbon storage (19.5 k t ha\(^{-1}\) vs. 1.80 k t ha\(^{-1}\); Fig. S4 D and E). The intermittency of tropical convective storms significantly affects long-term carbon storage: Carbon storage capacity can decrease by one-third depending on whether convective storms arrive every 14 h on average, as at our site, or every 24 h, with the same mean rainfall (Fig. 10A).

Our simulations with smoothed rainfall intensity and evapotranspiration show that models must consider the effects of subdiurnal fluctuations in rainfall to correctly predict the long-term evolution and carbon storage of tropical peatlands. The exact details of the fluctuations in rainfall are not important, in the sense that many distinct rainfall time series can give the same stable surface Laplacian and the same carbon storage capacity. However, carbon storage capacity can be severely overestimated by simulations that entirely ignore the effects of fluctuations in rainfall. We find that the effects of neglecting fluctuations in rainfall by computing the stable surface Laplacian after averaging net precipitation on hourly and longer intervals. Treating rainfall intensity and evapotranspiration as constant each hour, instead of every 20 min, increased the simulated stable surface Laplacian by a few percent, but averaging over 1 d led to an overestimate by 20%, over 1 wk by 100%, over 1 mo by 400%, and over 1 y by more than 1000% (Fig. S4 D and E).

Conclusions

The mathematical and numerical models presented here predict the long-term effects of changes in rainfall regimes and drainage networks on the morphology of tropical peat domes. Because tropical peat domes are mostly organic carbon, these predictions of peat dome morphogenesis also quantify peat dome carbon storage capacity and carbon fluxes. Our approach shows that tropical peatlands approach a limiting shape in which the Laplacian of the land surface is uniform. This stable peatland surface Laplacian can be computed from any rainfall time series and completely summarizes the effects of the rainfall pattern on the stable morphology and storage capacity of carbon within the peatland drainage boundary.

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4. Covenenb J, Dommern R, Joosten H (2010) Greenhouse gas fluxes from tropical peatlands approach a limiting shape in which the Laplacian of the land surface is uniform. This stable peatland surface Laplacian can be computed from any rainfall time series and completely summarizes the effects of the rainfall pattern on the stable morphology and storage capacity of carbon within the peatland drainage boundary.

The uniform-Laplacian principle is supported by a range of observations: (i) The peat surface Laplacian is approximately uniform in a region near the dome edge (Fig. 6C); (ii) water table behavior is uniform where the surface Laplacian is uniform and is different in the dome interior (Fig. 5A); (iii) water table behavior is the same in areas with differing gradients within the uniform-Laplacian region (Fig. 5A); (iv) transmissivity increases exponentially at high water tables, so that local water balance is dominated by flow near the surface (Fig. 5C); and (v) peat accumulation parameters match literature data, even though those data were not used for calibration (Fig. 44).

Our analysis underscores the importance of considering geomorphology when measuring and modeling carbon fluxes in tropical peatlands. On a growing peat dome, the perimeter of the dome reaches a steady elevation first while central areas continue to accumulate carbon (Fig. 8). This pattern of dome morphogenesis implies that the locations of ground-truth carbon flux measurements within tropical peat domes are important considerations for earth system models (34). For example, measurements of carbon flux in the center of a growing dome overestimate the average flux for the whole dome, because peat accumulation is fastest in the center (Fig. 8 and Fig. 53). The distribution of peat dome areas within a peatland complex is also important, because smaller domes reach their stable shapes faster after a change in conditions. Improved earth system models could use the uniform-Laplacian principle to efficiently account for the effects of changing rainfall, sea level, and drainage on tropical peat carbon storage, given a realistic distribution of peat dome sizes. The approach outlined here also provides a framework for including the effects of other long-term processes that remain understudied, such as shifts in river networks, changes in tree community composition, and saltwater intrusion from rising sea levels.