Design of a mechanical clutch-based needle-insertion device

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Design of a mechanical clutch-based needle-insertion device

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Insertion of trocars, needles, and catheters into unintended tissues or tissue compartments results in hundreds of thousands of complications annually. Current methods for blood vessel cannulation or epidural, chest tube, and initial trocar placement often involve the blind pass of a needle through several layers of tissue and generally rely on distinguishable anatomic landmarks and a high degree of clinical skill. To address this simply and without the use of electronics, a purely mechanical clutch system was developed for use in medical devices that access tissue and tissue compartments. This clutch utilizes the surface contact of a buckled filament inside an S-shaped tube to transmit force from the filament (catheter/guide wire) to the tube (needle). Upon encountering sufficient resistance at the tip, such as dense tissue, the catheter buckles and locks within the tube, causing the filament and needle to advance as one. When the needle reaches the target tissue or fluid-filled cavity, the filament unlocks and slides freely into the target region while the needle remains stationary. A similar locking phenomenon has long been observed in drill strings inside drill shafts used by the oil-drilling industry, and oil industry models were adapted to describe the motion of this clutch system. A predictive analytical model was generated and validated with empirical data and used to develop prototypes of a complete device then tested in vivo on muscle tissue and in vivo on a porcine laparoscopic model with promising results.

Introduction

Improperly inserted and positioned needles and catheters often require repeated attempts to achieve correct placement, causing mechanical injury to adjacent tissues or misdirected drug infusion. The associated complications include discomfort from repeated insertion attempts, bleeding, postdural puncture headache, nerve injury, hemodynamic shock, and respiratory arrest (1). Approximately 75,000 inadvertent punctures of the subarachnoid space occur annually in the U.S. alone (2). With the growing problem of obesity, the skin-to-target distance is increasingly variable, and important anatomical landmarks are more difficult to recognize (3). This can result in slower procedure times and the need for greater operative skill.

Current techniques for accessing specific regions of the body with needles, catheters, and trocars typically involve blind guidance where the physician or nurse relies entirely on tactile feedback, experience, superficial anatomical landmarks, and fluid return through the instrument. The operator must sense when the needle (or trocar) enters the target space and discontinue advancement. However, existing needle systems often do not provide sufficient feedback to the physician to indicate correct positioning. Current devices like Veress needles and certain trocars attempt to address these problems with spring-loaded blade sheathes or retractable blades. In both cases, these intended safety features do not always prevent damage to underlying organs (4). Accordingly, the FDA published a report in 2003 regarding laparoscopic procedures stating that most complications occur at initial trocar insertion and stressed the need for medical device companies to improve their products (5).

In addition to spring-loaded devices, a variety of guidance and sensing-based systems have been developed to improve targeted placement of needles and trocars. Examples include ultrasound and active sensing systems on the tips of needles. Although ultrasound guidance can be useful, there are situations where it is inconvenient, does not provide the required resolution, or simply cannot be used.

Over the past 4 decades, only minor improvements to catheterization procedures, such as epidural placement, have been achieved (6). Accordingly, the goal of this work was to develop a reliable, inexpensive, simple, nonelectric automatic clutch system that automatically disengages upon a specific change in tissue resistance for potential use in a variety of common medical procedures including catheterization, laparoscopy, tracheotomy, and placement of chest tubes.

This work initially focused on generating an analytical model for engagement of an automatic mechanical clutch for a needle device using empirical data from a tension/compression testing machine. Next we studied the engagement and disengagement of the clutch upon entering and exiting tissue. Empirical and analytical tools were used with an iterative optimization process to finally develop a functional working prototype that was successfully tested within an animal model.

Description of the Mechanical Clutch

To create a device that mechanically detects when a needle passes from a high-resistance tissue region into a low-resistance region, we have taken advantage of 2 mechanical effects: buckling and a capstan-like effect. Specifically, a simple mechanical clutch was developed based on the sliding resistance of a flexible filament (such as a catheter or guide wire) within a constant-diameter S-shaped tube. A sufficient compressive force along the filament axis causes it to buckle and lock inside the tube (Fig. 1). The S-shape causes the filament to buckle at a lower compressive force and, by acting like a capstan, wedges and locks the filament in place. A sufficiently high coefficient of friction can cause the filament to rapidly lock (or jam) inside the tube when compressed. Once locked, an increase in compressive force applied


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to the filament is transferred to the tube, causing the tube (needle) and filament to advance together as one. The moment that the needle breaks through into a lower-resistance tissue or open cavity, such as the lumen of the vessel or epidural space, the opposing force of the tissue on the tip of the filament rapidly drops, the filament unbucks, and the needle no longer advances. In other words, when the filament unbucks, it can no longer transmit force to the needle so the needle stops advancing. These series of events are possible because there is no direct force being applied to the needle; direct force is applied only by the operator to the filament (wire or catheter). In addition to automatically stopping within the target tissue or cavity, this system may be useful for a one-step rapid insertion of a guide wire or catheter, which may significantly reduce the time of these procedures. Because the tissue resistance is application-specific, the behavior of the device can be tuned for specific applications.

The locking action of the clutch in S-shaped tubes was modeled with nylon or PTFE filaments inside steel tubes using a tension/compression-testing machine [supporting information (SI) Fig. S1]. Using this machine, we applied a force to the input side of the filament while measuring the force at the output (Fig. S2). Ten and 23 S-tube shapes with differing design parameters were tested with nylon and PTFE filaments, respectively (Tables S1 and S2). The design parameters included number of bends, average bend radius, and arc length of bends (Fig. S4). An analytical model including these parameters was generated to predict the behavior of the clutch system during development and to iterate toward a functional prototype.

**Analytical Model for Predicting Engagement/Disengagement of the Clutch**

Insight for an analytical model was drawn from oil-well drill strings used in the petroleum industry. Drill strings are often in compression and have the tendency to buckle and “lock” (jam) inside the well if the compressive load exceeds a critical threshold (7). This critical locking point depends on the buckling point of the drill string and length and shape (curvature and number of curves) of the drill hole. Extensive work has been performed to model and predict buckling and frictional drag of the drill string in the drill hole (8). Previously described analytical models for drill strings created the basis for our model to predict the compressive forces in the filament and its locking point. Specifically, Eqs. 1 and 2 were derived by He and Kyllingstad to predict the normal contact forces between the drill string and the well wall (9).

\[ F_{1nbC} = \frac{F^2}{4EI} \]  
\[ F_{1nbC} = [(f_1mg\sin\theta + F_\alpha a_\alpha)^2 + (F_\alpha a_\phi \sin\theta)^2]^\frac{1}{2} \]  

Eq. 1 applies to a helically buckled drill string in a straight well. It was assumed (see Model Assumption Validations for validation) that the filaments in our systems always formed a helix when buckled. Eq. 2 applies to both straight and curved wells before buckling; however, in an unbuckled state, the contact force in the straight section would be negligible (Fig. 1 A and C). Removing all other negligible terms and approximating the inclination build rate (\(a_\phi\)) as 1/R (for descriptions of approximation see SI Text), Eq. 2 reduced to:

\[ F_{1nbC} = \frac{F_{1n}}{R} \]  

With these simplifications, it becomes apparent that \(F_{1nbC}\) and \(F_{1nbc}\) represent the contact forces for the curved and straight
segments of tubing respectively. To determine the frictional resistive force along the tube axis (sliding resistance), the contact forces of the filament on the tube, \( F_{\text{in bc}} \) and \( F_{\text{inc}} \) were multiplied by the friction coefficient (\( \mu \)) and respective tubing segment lengths (\( L \)):

\[
F_{\text{contact,straight}} = \mu L_{\text{straight}} F_{\text{in bc}} \tag{4}
\]

\[
F_{\text{contact,curved}} = \mu L_{\text{curved}} F_{\text{in}} \tag{5}
\]

In the curved regions of the tube, the filament transitions back and forth from one tube wall to the other as shown in Fig. 1 A and B. The transition segments (i.e., regions that are not in contact with the tube wall) were summed into a length term (\( L_{\text{transition}} \)) that was subtracted from \( L_{\text{curved}} \) to get the true contact length of the filament. The transition length depends not only on the filament diameter and the inner tube diameter but also on the applied compressive force, moment of inertia, and modulus of elasticity of the filament. To simplify this, \( L_{\text{transition}} \) was approximated as the transition length if the filament were unbuckled (Fig. 1A) and, thus, would depend only on the filament diameter, radial clearance between the filament and tube i.d., and curvature of the tube as shown in Eq. 6 (this approximation is justified below in Model Assumption Validations).

\[
F_{\text{contact,curved}} = \mu (L_{\text{curved}} - L_{\text{transition}}) F_{\text{in bc}} \tag{6}
\]

Substituting Eqs. 2 and 3, respectively, into Eqs. 4 and 6 yields:

\[
F_{\text{contact,straight}} = \frac{\mu L_{\text{straight}} F_{\text{in}}^2}{4EI} \tag{7}
\]

\[
F_{\text{contact,curved}} = \frac{\mu (L_{\text{curved}} - L_{\text{transition}}) F_{\text{in}}}{R} \tag{8}
\]

Finally, to obtain the resulting output force (\( F_{\text{out,predicted}} \)), the contact forces (\( F_{\text{contact,curved}} \) and \( F_{\text{contact,straight}} \)) were subtracted from the applied input force (\( F_{\text{in}} \)):

\[
F_{\text{out,predicted}} = F_{\text{in}} - (F_{\text{contact,curved}} + F_{\text{contact,straight}}) \tag{9}
\]

Substituting Eqs. 7 and 8 into Eq. 9 yields:

\[
F_{\text{out,predicted}} = F_{\text{in}} - \left[ \frac{\mu (L_{\text{curved}} - L_{\text{transition}}) F_{\text{in}}}{R} + \frac{\mu L_{\text{straight}} F_{\text{in}}^2}{4EI} \right] \tag{10}
\]

As is common with idealized analytical models of mechanical systems, the predicted value amplitudes did not exactly match the measured compression test data. Instead, the predicted forces followed similar trends but were much larger than the measured forces. After further analysis of the contributions of each component of the equation and comparing with measured data, \( F_{\text{contact,curved}} \) was found to be the cause of the overprediction. As with traditional buckled beam equations, a correction factor was required to align the trends with the empirical data. Without a correction factor, the analytical model could predict empirical trends but not the absolute values required for practical engineering applications. It was hypothesized that this correction factor might include a dimensionless constant (\( D/L \)) and a scaling factor (\( C \)). Before additional experimentation with the tension/compression-testing machine, the data were reanalyzed with the inclusion of the dimensionless constant to determine a suitable scaling factor. From this analysis of the empirical and model data, we determined that the scaling factor should be between 35 and 50. Inclusion of this factor significantly enhanced the accuracy of the model predictions. To study this further, and to determine how robust the addition of a dimensionless constant was to predict the empirical data, we chose to vary the length of the straight region of the S-tubes (tube shapes Cii–iv and Gii–iv in Tables S1 and S2). Changing the straight segment length alters the number of helices that the filaments form and has a significant effect on the compressive force required to reach the lock point. With the newly generated empirical data, the scaling factor was further iterated to a final value of 40 to maximize the predictive accuracy of the model. Representative data from these tests are shown in Fig. 2. Using 40\( D_{\text{filament}}/L_{\text{straight}} \) yielded:

\[
F_{\text{out,predicted}} = F_{\text{in}} - \left[ \frac{\mu (L_{\text{curved}} - L_{\text{transition}}) F_{\text{in}}}{R} + \frac{10 \mu D_{\text{filament}} F_{\text{in}}^2}{EI} \right] \tag{11}
\]

To validate the analytical model for differences in the properties of the filament, PTFE and nylon filaments were used that...
model predictions, including the predicted locked (flat) regime maximum (and any additional force results in advancement of completely lock because of the low friction coefficient. However, even with the helix formed, the filament did not pressed, and the filament was clearly observed to form a helix (Fig. 3) at less than half of the cutoff load (load cell capacity). The compressive force required for the string to transi-

strings have 2 unique buckling modes, a 2D sine wave and a helix (9–11). The analytical model was used to refine the prototype tube to design the lock point based on the yield stress for a less-dense filament through the tissue. To create a safety factor, we chose to design the lock point based on the yield stress of the filament within the curved segments of the tube (i.e., the segments that did not contact the tube wall) were equal in the unbuckled and buckled states. SolidWorks CAD models were generated to compare the projected transition lengths. Pictures of the actual side-to-side path of a black filament ($D_{\text{filament}} = 0.99$ mm) through the glass tube ($D_{\text{tube}} = 1.5$ mm) were used to recreate the geometry in equivalent CAD models (Fig. S3). In this case (where $D_{\text{tube}}/D_{\text{filament}} = 1.51$), it was determined that the buckled transition length was $\approx 75\%$ of the unbuckled transition length. In the limiting case when $D_{\text{tube}}/D_{\text{filament}}$ approaches 1.0 (i.e., no space between the filament and the inner wall of the tube), these transition lengths become equal. For the case of the nylon ($D_{\text{filament}} = 0.90$ mm) and PTFE ($D_{\text{filament}} = 0.97$ mm) filaments tested in the steel tubes ($D_{\text{tube}} = 1.22$ mm) by using the tension/compression system, the diameter ratios were 1.26 and 1.35, respectively. Given that these filaments occupied more space within the tube, the transition lengths between the unbuckled and buckled states were much closer than that for the black filament in the glass tube. Specifically, the buckled transition lengths were within $\approx 15\%$ of the unbuckled transition lengths for nearly all systems tested, which translates to an error of $<7\%$ difference in contact lengths. In other words, the majority of the filament length is in contact within the tube wall for the curved segment ($L_{\text{curved}} - L_{\text{transition}}$), and thus it was assumed that this would not significantly alter the predictive accuracy of the model.

Prototype Test with Muscle Tissue in Vitro
To study how the prototypes would lock and advance through muscle tissue, the tube/filament system was modified, and a sharp tip was added to the end of the steel tubes. Specifically, because all tests with the tension/compression system were performed against a noncompliant surface (i.e., a flat metal surface), the lock point would always be reached without any advancement of the filament. However, with a compliant substrate (e.g., tissue), it is essential that the tissue supplies sufficient opposing force to the filament to produce locking, otherwise the filament would advance along the tissue, thus preventing engagement of the clutch. To ensure that locking would occur well before advancement of the filament along the tissue, the tissue yield stress of candidate tissues was analyzed. If the contact lengths for the filaments are known, with the tissue yield stress, one can calculate the minimum compressive force required to advance the filament along through the tissue. To ensure engagement of the clutch, the compressive force required for locking must be less than the compressive force required for advancement of the filament through the tissue. To create a safety factor, we chose to design the lock point based on the yield stress for a less-dense tissue [liver tissue, which has a yield stress of 2.5 $\times$ $10^5$ Pa (12)]. The analytical model was used to refine the prototype tube properties (tube diameter, bend radius, number of curves, and lengths). For experiments with muscle tissue, we used a clinically available Arrow PTFE coated spring-wire guide ($D_{\text{filament}} = 0.76$ mm) with the central Nitinol wire removed (for increased flexibility). To increase the contact area between the filament and tissue, and to decrease the contact pressure required to achieve locking, a metal ball (D = 0.79 mm) was affixed to the tip of the filament. The properties of the prototypes that were tested on muscle tissue are described in Table S4 (rows 1 and 2).

Use of the prototype required one hand to guide the tube (needle) while the other hand applied a force to the filament through a makeshift hand piece (Fig. 1E). Success of early prototype devices was defined by locking of the clutch and advancement of the complete unit. Based on this criterion, the initial success rate was 49% (28 of 57 tests). It was assumed that the significant failure rate was due to the compressive force being

![Fig. 3. A helically buckled filament (white) is visible inside a glass tube filled with blue dye. Regions where the filament touches the wall can be distinguished by its white appearance given a minimal amount of blue dye that exists between the filament and wall at points of contact.](image-url)
applied to too small an area at the tip of the filament. Thus, the system was further refined by increasing the diameter of the tube (needle) to fit an increased metal ball diameter \( D = 1.59 \text{ mm} \) attached to the end of the filament. These changes increased the success rate to 75\% (65 of 87 tests).

The other critical property of the prototype was disengagement of the clutch upon exit from the tissue. In theory, the clutch should disengage when the opposing tissue force against the filament decreases below the compressive locking force. Upon disengagement, the filament should advance alone while the needle automatically stops. Later tests were considered a success only when the needle stopped \(< 3–4 \text{ mm} \) after exiting the tissue and the filament disengaged and deployed (Fig. 4). Results were determined through visual observation and tactile response in the hand piece. Common failures included filament deployment before complete exit of the needle through the muscle tissue and delayed deployment of the filament after exit from the tissue. Of the prototypes that achieved sufficient locking, 31\% (17 of 55) led to successful disengagement of the clutch. Twenty-three percent (7 of 31) of the failed attempts occurred because the filament deployed before complete exit of the tissue, whereas 77\% (24 of 31) resulted from delayed deployment of the filament after exiting the tissue. We considered premature filament deployment to be a more favorable result than overadvancement of needle, which, in practice, could damage underlying organs. When filament deployment was delayed, it was generally due to a small piece of tissue that had become wedged between the needle tip and the filament, preventing disengagement of the clutch. It is noteworthy that the metal ball typically remained \( \approx 0.5–1.0 \text{ mm} \) behind the point of the needle tip (inside the needle) until the needle exited from the muscle tissue. These failures were addressed by decreasing the inner diameter of the needle to reduce the gap between the metal ball and needle from 0.24 mm to 0.11 mm.

Altogether, the in vitro tests demonstrated a proof of concept for the engagement and disengagement of the clutch, whereas the analytical model was useful to iterate the prototype design to improve the locking mechanism for needle advancement through muscle tissue. Therefore, the prototypes with the best performances were selected for in vivo testing in a porcine model.

### Prototype Testing with in Vivo Porcine Model

The performance of a proof-of-concept clutch-based needle device was evaluated in a deceased porcine model. Each needle was inserted transabdominally in unique locations and was recorded with a laparoscopic video camera. Three prototype devices based on the in vitro prototypes that had the lowest locking points (Table S4, rows 5–7) were tested: 2 3-bend S-tubes (the second having enhanced curvature to promote earlier locking) and a 4-bend S-tube. These prototypes used smaller diameter tubing (i.d. = 1.70 mm), larger diameter ball \( D = 1.59 \text{ mm} \), and a spring-wire guide filament (Table S5; see also Fig. S4).

Laparoscopic videos showed that the prototype clutches engaged equally well for all 3 devices. This was due to the sufficiently low locking points and the handmade nature of the needle tips used, which were not as sharp as clinically available needles. This caused more force to be applied to the tip of the filament, promoting rapid engagement of the clutch. This also pushed the peritoneum away from the abdominal wall. Upon penetration of the peritoneum, a section of the needle tip appeared to have advanced into the cavity (average \( \approx 2.2 \text{ cm} \), standard deviation \( \approx 1.1 \text{ cm} \)). However, close inspection of the videos showed that all filaments disengaged immediately upon penetration and that \( > 60\% \) of the overshoot can be attributed to the peritoneum being pushed into the abdominal cavity and not to the needle advancing through the peritoneum (Fig. 5 and Movie S1 and Movie S2). The in vivo tests included a result where the needle was accidentally passed through the same hole in the peritoneum and another result where excessive force was applied to the needle, causing advancement after the filament disengaged, which was easily rectified by using less force.

The potential of the prototype clutch-based device to prevent injury was shown when a needle pressed the peritoneum in close proximity of the underlying viscera \( (\approx 3–5 \text{ mm}) \) but did not harm the viscera even after penetrating the peritoneum. This was achieved by the immediate disengagement and deployment of the filament, which prevented the needle from further advancement. We believe that these results demonstrate the potential to design an automatic mechanical clutch medical device to stop the advancement of a needle upon entry into a lower-resistance tissue compartment (e.g., abdominal cavity).

### Conclusions

This work showed that an automatic mechanical clutch could be designed and manufactured from a rigid tube and flexible filament for medical use in accessing tissue or tissue compartments. The analytical model of the clutch mechanism was developed from theory previously described for oil well drill strings with empirical data from tension/compression tests. The developed model accurately predicted the performance of the clutch for all variables tested. Specifically, \( > 160 \) tests were
performed on 17 different tubes and 2 filament types, and the results consistently fell within acceptable ranges of the model predictions. Using this refined analytical model, a functional prototype was developed and iterated, eventually achieving a 75% success rate for engagement of the clutch against muscle tissue in vitro. After demonstrating the potential disengagement of the clutch within the muscle tissue, proof-of-concept in vivo experiments were performed. For 6 attempts in a laparoscopic pig abdomen model, the clutch engagement was 100%. Although we observed overshoot in each case as the peritoneum tented (because of our hand-sharpened needles), the needle came to a complete stop, and the compressive force transitioned to the filament, which disengaged in all experiments. It is important to consider that not all clinical applications involve a drastic change of resistance, as we observed with the laparoscopic model, and that this may vary substantially when advancing a needle. Although further refinement of the clutch is necessary to ensure that no false positive or overshoot events occur, the proof-of-concept devices showed great promise and may solve many of the challenges associated with accessing tissue compartments.

The mechanical clutch-based medical device does not require electronics or additional accessories and may provide a simple method for the safe placement of needles and deployment of catheters in a wide range of medical procedures. Using the analytical model, it may be tuned for specific tissue applications and tissue variation. It is expected to provide increased tactile feedback with an automatic stopping function with potential to reduce the risk of overshoot injuries. Further improvements to this system will focus on enhancing the cutting edges and geometry of the needle tip to prevent overshoot of the needle, in addition to testing within multiple tissues and animal models. For an explanation of nomenclature, see Table 1.

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**Table 1. Nomenclature used in this study**

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<th>Variable</th>
<th>Definition</th>
<th>Unit of measure</th>
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<td>(a_i)</td>
<td>Inclination build rate</td>
<td>rad/m</td>
</tr>
<tr>
<td>(a_A)</td>
<td>Azimuth build rate</td>
<td>rad/m</td>
</tr>
<tr>
<td>(D_{\text{filament}})</td>
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<tr>
<td>(E)</td>
<td>Modulus of elasticity</td>
<td>N/m²</td>
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<tr>
<td>(f_b)</td>
<td>Buoyancy factor</td>
<td>—</td>
</tr>
<tr>
<td>(F_{\text{tubc}})</td>
<td>Contact force per unit length of helically buckled filament</td>
<td>N/m</td>
</tr>
<tr>
<td>(F_{\text{tribc}})</td>
<td>Contact force per unit length of nonbuckled filament</td>
<td>N/m</td>
</tr>
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<td>(F_{\text{a}})</td>
<td>Input force</td>
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<tr>
<td>(F_{\text{contact, curved}})</td>
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</tr>
<tr>
<td>(F_{\text{contact, straight}})</td>
<td>Predicted contact force for straight tubing</td>
<td>N</td>
</tr>
<tr>
<td>(F_{\text{m}})</td>
<td>Input force</td>
<td>N</td>
</tr>
<tr>
<td>(F_{\text{out, predicted}})</td>
<td>Predicted output force</td>
<td>N</td>
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<tr>
<td>(I)</td>
<td>Moment of inertia of filament</td>
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<tr>
<td>(L_{\text{curved}})</td>
<td>Length of curved section of design tube</td>
<td>m</td>
</tr>
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<td>(L_{\text{straight}})</td>
<td>Length of long straight section of design tube</td>
<td>m</td>
</tr>
<tr>
<td>(L_{\text{transition}})</td>
<td>Length of filament that does not touch tube wall</td>
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