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Efficient stochastic simulation of reaction–diffusion processes via direct compilation

Mieszko Lis, Maxim N. Artymov, Srinivas Devadas and Arup K. Chakraborty

1Computer Science and Artificial Intelligence Laboratory and the Departments of 2Chemistry, 3Chemical Engineering and 4Biological Engineering, Massachusetts Institute of Technology, Cambridge, MA 02139, USA

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ABSTRACT

We present the Stochastic Simulator Compiler (SSC), a tool for exact stochastic simulations of well-mixed and spatially heterogeneous systems. SSC is the first tool to allow a readable high-level description with spatially heterogeneous simulation algorithms and complex geometries; this permits large systems to be expressed concisely. Meanwhile, direct native-code compilation allows SSC to generate very fast simulations.

Availability: SSC currently runs on Linux and Mac OS X, and is freely available at http://web.mit.edu/irc/ssc/.

Contact: mieszko@csail.mit.edu

Supplementary information: Supplementary data are available at Bioinformatics online.

1 BACKGROUND

Cells interact with their environment via receptors that bind to extracellular molecules; these events are then translated into functions by biochemical signaling networks. Non-linearities arising from the complex topology of such networks often make it difficult to intuit qualitative behavior of signaling modules. Moreover, recent imaging experiments have revealed that signaling components are organized into spatial patterns that modulate signaling (Grakoui et al., 1999; Lee et al., 2003). Finally, extrinsic and intrinsic stochastic effects, which make each cell’s response unique, can be important when small numbers of signaling molecules are involved (Artymov et al., 2007). As computational studies are increasingly becoming necessary complements to genetic, biochemical and imaging experiments in unraveling this non-intuitive behavior of cell signaling networks, efficient and easy to use tools that can carry out stochastic simulations of biochemical networks, both in well-mixed and spatially inhomogeneous approximations, have become key technologies.

Since the original stochastic simulation algorithm (Gillespie, 1977), basic computer science techniques have reduced the rate at which the per-step computation time grows with the number of possible reactions to logarithmic growth (Gibson and Bruck, 2000; Li and Petzold, 2006; Wylie et al., 2006), or optimized performance by noting that a few reactions account for most events (Cao et al., 2004; Mccollum et al., 2006); more recently, Slepy et al. (2008) have reduced per-step computation to expected constant time via an elegant composition-rejection algorithm. Similar techniques have been applied to reduce spatially heterogeneous simulation time to logarithmic (Elf and Ehrenberg, 2004). The combinatorial growth of the instantiated reaction network size, another limiting factor for complex systems, has been addressed either by generating species and reactions on the fly (Faeder et al., 2005; Lok and Brent, 2005) during a Gillespie-based simulation, by representing each molecule separately (Morton-Firth and Bray, 1998), or ingeniously do away with explicit counts altogether by adjusting the sampling distribution (Danos et al., 2007; Yang et al., 2008). Efficient formulation of such simulations in a general programming language like C or FORTRAN, however, is not a trivial task: while simulating a few reactions is fast even with a simple implementation, a system with thousands of reactions and subvolumes demands more complex algorithms which are much more tricky to code. The programming burden has been reduced by libraries (e.g. Li et al., 2008) as well as by simulators for well-mixed (e.g. Gillespie et al., 2006; Mauch, 2009) and spatially inhomogeneous (e.g. Hatte et al., 2005; Meier-Schellersheim et al., 2006) models. File formats like SBML ( Hucka et al., 2008 ), developed to express biochemical models, can be read by several simulators.

The modeling task is further complicated by the explosion in combinatorial complexity which arises when modeling post-translational modification or reactions local to one molecule in a complex (Hlavacek et al., 2006): in SBML (and, indeed, in most simulators) all possible species and each combination of every possible reacting complex must be written out as a separate reaction, which renders expressing even modestly complex reaction networks impractical. To mitigate these limitations, BioNetGen (Faeder et al., 2009) and κ ( Danos and Laneve, 2004 ) have proposed higher level specifications where the reactants in each reaction are written as patterns covering many possible species; such descriptions not only naturally correspond to the intuitive concept of a biochemical reaction, but are significantly smaller and therefore more readable as well as much less error-prone.

The main contribution of the Stochastic Simulation Compiler (SSC) that we present here lies in combining a higher level specification required for modeling larger systems with the ability to model spatially heterogeneous systems. It differs from BioNetGen and κ because their syntax and expansion algorithms offer no
2 IMPLEMENTATION

2.1 Tool flow

The tool flow resembles a programming language compiler. The user writes a high-level description of the reaction system (see Supplementary Material for examples), using patterns to select and change specific parts of compounds (similar to how a cell biologist would describe a known or hypothesized cell signaling network). Regions are specified using Constructive Solid Geometry (CSG); meanwhile, while MesoRD allows such regions and geometries, it suffers from the combinatorial complexity limitations described above. In addition, SSC produces fast simulations (cf. Supplementary Material) by directly generating machine code tailored to a specific architecture.

2.2 Reaction expansion

Most biologically relevant signaling reactions are conceptually local, that is, they ‘see’ only a part of a larger molecule or complex (say, a single phosphorylation site). Therefore, we write reactions and diffusions locally, using pattern matching to recognize and modify parts of complexes, and rely on the compiler to derive all the possible cases in all regions. Similarly, only initially present compounds are specified; the compiler generates the rest from the initial set and the reactions.

Formally, the reactions and diffusion form a graph term-rewriting system, which is fully evaluated to generate the simulator. Briefly, each expansion step considers a rule in the system, finding all possible cases in all regions. Similarly, only initially present compounds are specified; the compiler generates the rest from the initial set and the reactions.

2.3 Direct code generation

We obtain the efficiency of hand-optimized code by directly generating assembly code from the fully expanded set of reachable species and reactions. This allows us to avoid the interpretive overhead of consulting dependency graphs to determine which copy counts and propensities must be recomputed.

The generated code is also tailored for model complexity and processor architecture. For most sizes, the compiler creates a separate, straight-line segment of code for each possible reaction in a region; each segment is parameterized only on the subvolume (or, in the case of diffusion, two subvolumes), and directly updates and propagates the affected propensities (see Section 2.4). This avoids pipeline stalls and cache flushes caused by mispredicted branches, and reduces the number of data memory reads and writes (which are the performance bottleneck) to the absolute minimum. (See Supplementary Material for a detailed description of the code generation method).

2.4 Reaction–diffusion simulation algorithm

The simulation algorithm is similar to the logarithmic-time versions of the direct stochastic simulation algorithm (Li and Petzold, 2006; Wylie et al., 2006). The simulation-time representation details may be found in the Supplementary Material; briefly, the reactions in each subvolume (or on each boundary between subvolumes) are arranged in an n-ary heap with the leaves corresponding to individual reaction propensities and each node carrying the combined propensity of the reactions underneath—the topmost node for each subvolume is, then, the propensity of any reaction taking place within. The subvolume and boundary reaction propensities are, in turn, themselves arranged in a heap where each leaf is either a subvolume or a boundary propensity; the topmost node is the propensity of any reaction in the system taking place (and, hence, the range from which the random number should be selected).

Simulation proceeds as follows: a random number r is selected from range [0, R) where R is the propensity of any reaction taking place; then the subvolume and reaction corresponding to r is selected by n-ary search in the heap. Next, the reaction is ‘executed’, that is, the copy numbers of the affected species are adjusted as the reaction dictates. Finally, the propensity of each reaction whose substrate copy counts were altered is recomputed, and the partial propensities are propagated up the propensity heap until the new R is recomputed and the cycle can be repeated.

Since the propensity heap in each subvolume (or boundary) has height logarithmic in the number of reactions within, and the heap above is logarithmic in the number of subvolumes and boundaries, the total tree depth scales roughly logarithmically in the number of reactions in the system. Both the reaction selection/search and copy number/propensity update step, therefore, run in time logarithmic in the number of reactions.

3 PERFORMANCE

We compared spatially homogeneous SSC against BioNetGen 2.0.46 (Faeder et al., 2009) (since, like SSC, it builds reaction networks from pattern-matching rules), and against simulators built with the StochKit library (Li et al., 2008); because of the complexity of the larger models, we had SSC automatically generate the required StochKit C++ configurations. To test real-world performance, we selected two toy systems and two more realistic systems with various reaction counts: a dimer decay model (Gillespie, 2001) with four reactions, a simplified EGFR signaling model (Blinov et al., 2006) with 64 reactions, a model for the earliest events in...


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T-cell signaling (Wylie et al., 2006) with 1120 reactions, and an enhanced version of the same with 2422 reactions. To test spatially heterogeneous models, we compared the latest development revision of MesoRD (Hattne et al., 2005), SVN r559; we used the T-cell signaling model above where single molecules (but not compounds) were permitted to diffuse around a membrane interface, which was divided into 100, 10,000, and 50,000 subvolumes. All simulations produced the same results (modulo random seed variation and precision loss during floating point arithmetic). To focus on measuring only the simulation time, we disabled all output except the final species counts, and repeated each experiment 5-fold to account for initial random seed variation and possible effects of other processes executing on the system.

We found that SSC consistently outperformed the faster of the two spatially homogeneous simulators we tested by 2 x to 6 x, with the advantage growing with the size of the model (see Supplementary Fig. 3). For spatially heterogeneous simulation, we found that SSC was ∼50 x faster than MesoRD, although both scaled very well with the number of subvolumes (see Supplementary Fig. 4).

4 CONCLUSIONS

We have described the SSC, a new tool for exact stochastic simulations of biochemical reaction networks. SSC is, to our knowledge, the first tool to combine a succinct high-level description (which avoids combinatorial complexity explosion) with spatially resolved simulation where species and reactions may be restricted to specific regions of arbitrarily complex shapes, and unique in resolving simulation where species and reactions may be restricted (which avoids combinatorial complexity explosion) with spatially homogeneous simulators we tested by 2 x to 6 x, with the advantage growing with the size of the model (see Supplementary Fig. 3). For spatially heterogeneous simulation, we found that SSC was ∼50 x faster than MesoRD, although both scaled very well with the number of subvolumes (see Supplementary Fig. 4).

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REFERENCES


