High $p_T$ nonphotonic electron production in $p+p$ collisions at $s=200$\textbf{[square root of $s=200$]} GeV

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High $p_T$ nonphotonic electron production in $p + p$ collisions at $\sqrt{s} = 200$ GeV


(CHARM Collaboration)
We present the measurement of nonphotonic electron production at high transverse momentum ($p_T > 2.5$ GeV/$c$) in $p + p$ collisions at $\sqrt{s} = 200$ GeV using data recorded during 2005 and 2008 by the STAR experiment at the Relativistic Heavy Ion Collider (RHIC). The measured cross sections from the two runs are consistent with each other despite a large difference in photonic background levels due to different detector configurations. We compare the measured nonphotonic electron cross sections with previously published RHIC data and perturbative quantum chromodynamics.
I. INTRODUCTION

Heavy quark production in high-energy hadronic collisions has been a focus of interest for years. It is one of the few instances in which experimental measurements can be compared with QCD predictions over nearly the entire kinematical range [1–3]. Because of the large masses of charm and bottom quarks, they are produced almost exclusively during the initial high-$Q$ parton-parton interactions and thus can be described by perturbative QCD calculations.

Measurement of heavy-flavor production in elementary collisions represents a crucial test of the validity of the current theoretical framework and its phenomenological inputs. It is also mandatory as a baseline for the interpretation of heavy-flavor production in nucleus-nucleus collisions [4]. In these heavy-ion collisions, one investigates the properties of the quark-gluon plasma (QGP), which is created at sufficiently high center-of-mass energies. Many effects on heavy-flavor production in heavy-ion collisions have been observed but are quantitatively not yet fully understood [4]. Of particular interest are effects which modify the transverse momentum spectra of heavy-flavor hadrons, including energy loss in the QGP (“jet quenching”) [5–9], as well as collective effects such as elliptic flow [10,11]. In addition, $J/\psi$ might be regenerated in a dense plasma from the initial open charm yield [12], making precise measurements of the transverse momentum spectra in elementary $p + p$ collisions imperative.

Open heavy-flavor production in $p + p$, $d + A$, and $A + A$ collisions at $\sqrt{s_{NN}} = 200$ GeV has been studied at the Relativistic Heavy Ion Collider (RHIC) using a variety of final-state observables [4]. The STAR collaboration measured charm mesons directly through their hadronic decay channels [13–15]. Because of the lack of precise secondary vertex tracking and trigger capabilities, these measurements are restricted to low momenta ($p_T < 3$ GeV/$c$). Both STAR [15,16] and PHENIX [17,18] also measured heavy-flavor production through semileptonic decays of charm and bottom mesons ($D, B \rightarrow \ell \nu \pi X$). While the measured decay leptons provide only limited information on the original kinematics of the heavy-flavor parton, these measurements are facilitated by fast online triggers and extend the kinematic range to high $p_T$.

In this paper, we report STAR results on nonphotonic electron production at midrapidity in $p + p$ collisions at $\sqrt{s} = 200$ GeV using data recorded during the year 2005 (Run2005) and the year 2008 (Run2008) with a total integrated luminosity of 2.8 and 2.6 pb$^{-1}$, respectively.

The present results are consistent with the next-to-leading logarithm (FONLL) calculation within its theoretical uncertainties. Utilizing the measured relative contributions of B and D mesons to nonphotonic electrons which were obtained from a study of electron-hadron correlations (e-h) [19], we determine the invariant cross section of electrons from bottom and charm meson decays separately at $p_T > 3.0$ GeV/$c$.

The article is organized as follows. In Sec. II we describe the STAR detectors and triggers relevant to this analysis. Section III describes the data analysis in detail, and in Sec. IV we present and discuss the results. Section V provides conclusions.

II. EXPERIMENT

A. Detectors

STAR is a large acceptance, multipurpose experiment composed of several individual detector subsystems with tracking inside a large solenoidal magnet generating a uniform field of 0.5 T [20]. The detector subsystems relevant for the present analysis are briefly described in the following.

1. Time projection chamber

The time projection chamber (TPC) [21] is the main charged particle tracking device in STAR. The TPC covers $\pm 1.0$ units in pseudorapidity ($\eta$) for tracks crossing all layers of pads, and the full azimuth. Particle momentum is determined from track curvature in the solenoidal field. In this analysis, TPC tracks are used for momentum determination, electron-hadron separation (using specific ionization $dE/dx$), to reconstruct the interaction vertex, and to project to the calorimeter for further hadron rejection.

2. Barrel electromagnetic calorimeter and barrel shower maximum detector

The barrel electromagnetic calorimeter (BEMC) measures the energy deposited by photons and electrons and provides a trigger signal. It is located inside the magnet coil outside the TPC, covering $|\eta| < 1.0$ and $2\pi$ in azimuth, matching the TPC acceptance. The BEMC is a lead-scintillator sampling electromagnetic calorimeter with a nominal energy resolution of $\delta E/E \sim 14%/\sqrt{E/1 \text{ GeV}} \oplus 1.5%$ [22]. The full calorimeter is segmented into 4800 projective towers. A tower covers 0.05 rad in $\phi$ and 0.05 units in $\eta$. Each tower consists of a stack of 20 layers of lead and 21 layers of scintillator with an active depth of...
23.5 cm. The first two scintillator layers are read out separately providing the calorimeter preshower signal, which is not used in this analysis. A shower maximum detector (BSMD) is positioned behind the fifth scintillator layer. The BSMD is a double layer wire proportional counter with strip readout. The two layers of the BSMD, each containing 18 000 strips, provide precise spatial resolution in $\phi$ and $\eta$ and improve the electron-hadron separation. The BEMC also provides a high-energy trigger based on the highest energy measured by a single tower in order to enrich the event samples with high-$p_T$ electromagnetic energy deposition.

3. Trigger detectors

The beam-beam counters (BBC) [23] are two identical counters located on each side of the interaction region covering the full azimuth and $2.1 < |\eta| < 5.0$. Each detector consists of sets of small and large hexagonal scintillator tiles grouped into a ring and mounted around the beam pipe at a distance of 3.7 m from the interaction point. In both Run2008 and Run2005, the BBC served as a minimum-bias trigger to record the integrated luminosity by requiring a coincidence of signals in at least one of the small tiles ($3.3 < |\eta| < 5.0$) on each side of the interaction region. The cross section sampled with the BBC trigger is $26.1 \pm 0.2(\text{stat}) \pm 1.8(\text{syst}) \text{mb} [24]$ for $p + p$ collisions. The timing signal recorded by the two BBC counters can be used to reconstruct the collision vertex along the beam direction with an accuracy of $\sim 40$ cm.

The data in $d + Au$ collisions recorded during year 2008 is used as a crosscheck in this analysis (see Sec. III E). During this run, a pair of vertex position detectors (VPD) [25] was also used to select events. Each VPD consists of 19 lead converters plus plastic scintillators with photomultiplier-tube readout that are positioned very close to the beam pipe on each side of STAR. Each VPD is approximately 5.7 m from the interaction point and covers the pseudorapidity interval $4.24 < |\eta| < 5.1$. The VPD trigger condition is similar to that of the BBC trigger except that the VPD has much better timing resolution, enabling the selected events to be constrained to a smaller range ($\sim 30$ cm in $d + Au$ run) around the interaction point.

B. Material thickness in front of the TPC

Table I shows a rough estimate of material thickness between the interaction point and the inner field cage (IFC) of the TPC during Run2008 in the region relevant to the analysis. The amount of material is mostly from the beam pipe, the IFC, air, and a wrap around the beam pipe. In Run2005, the amount of material is estimated to be $\sim 10$ times larger in front of the TPC inner field cage [26] and is dominated by the silicon detectors which were removed before Run2008. The contribution from the TPC gas is not significant because we require the radial location of the first TPC point of reconstructed tracks to be less than 70 cm (see Sec. III B) in the Run2008 analysis; furthermore, conversion electrons originating from TPC gas have low probability to be reconstructed by the TPC tracking due to the short track length. While the Run2008 simulation describes the material distribution very well, the material budget for the support structure and electronics related to the silicon detectors is not reliably described in the Run2005 simulation [27]. This, however, has little effect on this analysis, as explained in Sec. III D.

C. Triggers and data sets

The data reported in this paper were recorded during Run2005 and Run2008 at $\sqrt{s} = 200$ GeV. All events used in this analysis are required to satisfy a BEMC trigger and a BBC minimum-bias trigger. In addition, event samples using a VPD trigger in the 2008 $d + Au$ collisions are used for systematic cross-checks as described in Sec. III E.

To enrich the data sample with high-$p_T$ electromagnetic energy deposition, the BEMC trigger requires the energy deposition in at least one tower to exceed a preset threshold (high tower). Most of the energy from an electron or a photon will be deposited into a single tower since the tower size exceeds the radius of a typical electromagnetic shower. The Run2008 data sets used here were recorded using three high-tower triggers with different thresholds, corresponding to a sampled luminosity of $\sim 2.6 \text{ pb}^{-1}$. Expressed in terms of transverse energy ($E_T$), the thresholds were approximately 2.6, 3.6, and 4.3 GeV. The Run2005 data sets used here are from two high-tower triggers with $E_T$ thresholds of 2.6 GeV (HT1) and 3.5 GeV (HT2), corresponding to a sampled luminosity of $\sim 2.8 \text{ pb}^{-1}$. In the Run2008 analysis, data sets from different high-tower triggers are treated together after being combined, with double counting avoided by removing duplicates in the corresponding high-tower analog-to-digital converter (ADC) spectra. Trigger efficiencies and prescale factors imposed by the data acquisition system are taken into account during the combination. In the analysis of the Run2005 data, HT1 and HT2 data are treated separately.

In Run2005 the integrated luminosity was monitored using the BBC minimum-bias trigger, while in Run2008, because of the large beam related background due to high luminosity, a high threshold high-tower trigger seeing a
total cross section of 1.49 \mu b was used as luminosity monitor.

III. ANALYSIS

A. Photonic background removal

The main background in this analysis is the substantial flux of photonic electrons from photon conversion in the detector material and Dalitz decay of \( \pi^0 \) and \( \eta \) mesons. These contributions need to be subtracted in order to extract the nonphotonic electron yield, which is dominated by electrons from semileptonic decays of heavy-flavor mesons.

There are two distinct methods for evaluating contributions from photonic electrons. In the cocktail method, the estimated or measured invariant cross sections are used to calculate contributions from various sources (mostly \( \pi^0 \), \( \eta \) mesons), and to derive from those the photonic electron distributions. Given sufficient knowledge of the production yield of those mesons, this method allows one to determine directly the contributions from Dalitz decays. With this method, a detailed understanding of the material distribution in the detector is required in order to evaluate the contribution from photon conversion. Another method, used in this analysis, is less dependent on the exact knowledge of the amount of material. This method reconstructs the photonic electrons through the specific feature that photonic electron-positron pairs have very small invariant mass. Not all photonic electrons can be identified this way since one of the electrons may fall outside of the detector acceptance, or has a very low momentum, in which cases both electrons in the pair are not reconstructed. This inefficiency must be estimated through simulation.

Electron pairs are formed by combining an electron with \( p_T > 2.5 \text{ GeV}/c \), which we refer to as a primary electron, with all other electrons (partners) reconstructed in the same event, with opposite charge sign (unlike sign) or same charge sign (like sign). The upper two panels of Fig. 1 show the invariant mass spectra for primary electrons with \( 2.5 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c \) (left) and \( 8.0 \text{ GeV}/c < p_T < 10.0 \text{ GeV}/c \). The unlike-sign spectrum includes pairs originating from photon conversion and Dalitz decay, as well as combinatorial background. The latter can be estimated using the like-sign pair spectrum. The photonic electron spectrum is obtained by subtracting like-sign from unlike-sign spectrum (unlike-minus-like). The broad shoulders extending toward higher masses in the spectra are caused by finite tracking resolution, which leads to a larger reconstructed opening angle when the reconstructed track helices of two conversion electrons intersect each other in the transverse plane. The overall width of the mass spectra depends on the primary electron \( p_T \), but most photonic pairs are contained in range of \( m_{ee} < 0.24 \text{ GeV}/c^2 \). The lower two panels of Fig. 1 show the simulated invariant mass spectra of the two dominant sources of photonic electrons, \( \pi^0 \) Dalitz and \( \gamma \) conversions, in the same two \( p_T \) regions, which are similar in shape due to similar decay kinematics. The electron spectrum obtained from the unlike-minus-like method is from pure photonic electrons because the combinatorial background is accurately described by the like-sign pair spectrum according to the simulation and the simulated mass spectra are in qualitative agreement with the data. This is also proved by the fact that the distribution of the normalized ionization energy loss (see Sec. III B) can be well described by a Gaussian function expected from electrons as shown in Fig. 4.

We calculate the yield of nonphotonic electrons according to

\[
N(\text{npe}) = N(\text{inc}) \cdot \epsilon_{\text{purity}} - N(\text{pho})/\epsilon_{\text{pho}},
\]

where \( N(\text{npe}) \) is the nonphotonic electron yield, \( N(\text{inc}) \) is the inclusive electron yield, \( N(\text{pho}) \) is the photonic electron yield, \( \epsilon_{\text{pho}} \) is the photonic electron reconstruction efficiency defined as the fraction of the photonic electrons identified through invariant mass reconstruction, and \( \epsilon_{\text{purity}} \) is the purity reflecting hadron contamination in the inclusive electron sample.

Electrons from open heavy-flavor decays dominate nonphotonic electrons. The contribution from semileptonic decay of kaons is negligible for \( p_T > 2.5 \text{ GeV}/c \) [17]. Electrons from vector mesons (\( \rho, \omega, \phi, J/\psi, \gamma \)) decays...
and Drell-Yan processes are subtracted from the measurement (see Sec. III G for details).

B. Electron reconstruction and identification efficiency

In the analysis of the Run2008 data, we select only tracks with \( p_T > 2.5 \text{ GeV}/c \) and \(|\eta| < 0.5\). The event vertex position along the beam-axis \( (V_z) \) is required to be close to the center of the TPC, i.e. \(|V_z| < 30\text{ cm}\). To avoid track reconstruction artifacts, such as track splitting, the selected tracks are required to have at least 52% of the maximum number of TPC points allowed in the TPC, a minimum of 20 TPC points and a distance-of-closest-approach (DCA) to the collision vertex less than 1.5 cm. For hadron rejection we apply a cut of \( n\sigma_e > -1 \) on the normalized ionization energy loss in the TPC [28], which is defined as

\[
n\sigma_e = \log((dE/dx)/B_e)/\sigma_e,
\]

where \( B_e \) is the expected mean \( dE/dx \) of an electron calculated from the Bichsel function [29] and \( \sigma_e \) is the TPC resolution of \( \log((dE/dx)/B_e) \).

We reconstruct clusters in the BEMC and the BSMD by grouping adjacent hits that are likely to have originated from the same incident particle [27]. The selected tracks are extrapolated to the BEMC and the BSMD where they are associated with the closest clusters. The association windows for electrons are determined by measuring the distance between the track projection point at the BEMC (BSMD) and the closest BEMC (BSMD) cluster using photonic electrons from the unlike-minus-like pairs. Figure 2(a) shows the distribution of this distance at the BEMC along the beam direction for electrons from

![Figure 2](image-url)

**FIG. 2.** (a) The distribution of the minimum distance between an electron track projection point at the BEMC and all BEMC clusters along the beam direction from unlike-sign electron candidate pairs (solid line), like-sign electron candidate pairs (dashed line), and unlike-minus-like (closed circles). (b) \( p/E_0 \) distribution from unlike-sign electron candidate pairs (solid line), like-sign electron candidate pairs (dashed line), and unlike-minus-like (closed circles).

unslike-sign, like-sign, and unlike-minus-like pairs requiring \( m_{e^-e^+} < 0.24 \text{ GeV}/c^2 \), a maximum 1.0 cm DCA between two helical-shaped electron tracks, and a 3.0 keV/cm \( dE/dx < 5.0 \text{ keV/cm} \) cut on ionization energy loss for partner tracks. Most electrons are inside a window of \( \pm 20 \text{ cm} \) around the track projection point. The window in the azimuthal plane is determined to be \( \pm 0.2 \text{ rad} \). Figure 2(b) shows the distribution of \( p/E_0 \) for electrons from unlike-sign, like-sign, and unlike-minus-like pairs, where \( E_0 \) is the energy of the most energetic tower in a BEMC cluster. The distribution is peaked around one due to the small mass of the electron and the fact that most electron energy is deposited into one tower. We apply a cut of \( p/E_0 < 2.0 \) to further reduce hadron contamination. Cuts on the association with BSMD clusters are kept loose to maintain high efficiency. Each track is required to have more than one associated BSMD strip in both \( \phi \) and \( \eta \) planes.

The efficiencies of electron identification cuts are estimated directly from the data using pure photonic electrons obtained from the unlike-minus-like pairs requiring \( m_{e^-e^+} < 0.24 \text{ GeV}/c^2 \), a maximum 1.0 cm DCA between two helical-shaped electron tracks, and a 3.0 keV/cm \( dE/dx < 5.0 \text{ keV/cm} \) cut on ionization energy loss for partner tracks. A cut of \( p_T > 0.3 \text{ GeV}/c \) for partners is also applied, selecting a region where the simulation does a good job of describing the data. The efficiency for one specific cut is then calculated as the ratio of electron yield before the cut to that after the cut, while all the other electron identification cuts are applied. To avoid possible correlation among different cuts, efficiencies for all BEMC and BSMD cuts are calculated together. Figure 3(a) shows the breakdown of the electron identification efficiency as a function of \( p_T \). The drop in the low \( p_T \) region comes mainly from BSMD inefficiency, while the drop in the

![Figure 3](image-url)

**FIG. 3 (color online).** Efficiencies of the cuts on number of TPC points (open circles), \( n\sigma_e \) (open triangles), and BEMC (open squares) in (a) the Run2008 and (b) the Run2005 analyses. The closed circles represent the total efficiency which is the product of all individual ones.
high $p_T$ region is caused by the $p/E_0$ cut. The uncertainties in the figure are purely statistical and are included as part of the systematic uncertainties for the cross-section calculation.

To maintain high track quality and suppress photonic electrons from conversion in the TPC gas, we require the radial location of the first TPC point to be less than 70 cm. This cut causes an inefficiency of 12.0 ± 2.0% for non-photonic electrons according to the estimates from both simulation and data.

Through embedding simulated electrons into high-tower trigger events and processing them through the same software used for data production, single electron reconstruction efficiency in the TPC is found to be 0.84 ± 0.04 with little dependence on momentum for $p_T > 2.0$ GeV/c.

The analysis of the Run2005 data is slightly different from that of the Run2008 described above. Only half of the BEMC ($0 < \eta < 1.0$) was instrumented in 2005. Because of the presence of the silicon detectors, and their significant material budget, photonic backgrounds were substantially higher. We select only tracks with $0 < \eta < 0.5$ from $-30$ cm $< V_z < 20$ cm in order to avoid the supporting cone for the silicon detectors in the fiducial volume while keeping track quality cuts identical to those in the Run2008 analysis. However, we apply a tighter cut on the normalized ionization energy loss, i.e. $-0.7 < n\sigma_e < 3.0$, to improve hadron rejection. BEMC clusters are grouped with geometrically overlapping BSMD clusters to improve position resolution and electron-hadron discrimination through shower profile. The clustering algorithm is also modified to increase the efficiency of differentiating two overlapping BSMD clusters by lowering the energy threshold of the second cluster [30]. The minimum angle between track projection point at the BEMC and all BEMC clusters is required to be less than 0.05 rad. We also require each track to have more than one associated BSMD strip in both $\phi$ and $\eta$ planes, and a tightened $p/E$ cut of 0.3 $< p/E < 1.5$, where $E$ is the energy of the associated BEMC cluster. The efficiencies for the electron identification cuts are estimated by embedding simulated single electrons into minimum-bias PYTHIA [31] events. Figure 3(b) shows the breakdown of electron identification efficiency as a function of $p_T$ in the Run2005 analysis. There is no drop at high $p_T$ as in the Run2008 result because the energy of a whole BEMC cluster, instead of the highest tower, is used for the $p/E$ cut. No cut on the first TPC point is applied in this analysis. To avoid the TPC tracking resolution effect that causes the broad shoulder extending toward higher masses in the invariant mass spectrum of the Run2008 analysis, we utilize a 2D invariant mass by ignoring the opening angle in the $\phi$ plane when reconstructing the $e^+e^-$ invariant mass [30]. We require $-3 < n\sigma_e < 3$ for partner tracks, 2D $m_{e^+e^-} < 0.1$ GeV/c$^2$ for pairs, a maximum 0.1/0.05 rad for the opening angle in the $\phi/\theta$ plane, and a maximum 1.0 cm DCA between two electron helices.

A cut of $p_T > 0.3$ GeV/c for partners is also applied so that the simulation can describe the data well.

By following independent analysis procedures from two RHIC runs where the amount of material for photonic background is significantly different, we will be able to validate our approach for measuring nonphotonic electron production.

### C. Purity estimation

After applying all electron identification cuts, the inclusive sample of primary electrons is still contaminated with hadrons. To estimate the purity of electrons in the inclusive sample, we perform a constrained fit on the charged track $n\sigma_e$ distributions in different $p_T$ regions with three Gaussian functions representing the expected distributions of $\pi^\pm$, $K^\pm + p^\pm$, and $e^\pm$. The purity is estimated from the fit.

Ideally the electron $n\sigma_e$ will follow the standard normal distribution. The actual distribution can be slightly different due to various effects in data calibrations. We can, however, determine its shape in different $p_T$ regions directly from data using photonic electrons from the unlike-minus-like pairs. The left panel of Fig. 4 shows the $n\sigma_e$ distribution for tracks with (a) 2.5 GeV/c $< p_T < 3.0$ GeV/c and (b) 8.0 GeV/c $< p_T < 10.0$ GeV/c from unlike-sign, like-sign pairs as well as for photonic electrons from the unlike-minus-like pairs. Here all electron identification cuts, except the $n\sigma_e$ cut, are applied. The $n\sigma_e$ of photonic electrons are well fitted with Gaussian functions. Figure 4(c) shows the mean and width of the Gaussian fitting functions for pure photonic electron (unlike-minus-like) $n\sigma_e$ distribution as shown in the left panels for each $p_T$ bin. See text for details.
and width of the Gaussian fit as a function of electron $p_T$, which, as discussed above, differ slightly from the ideal values. The solid lines in the figure are fits to the data using a second order polynomial function. The dotted lines are also second order polynomial fits to the data except that the data points are moved up and down simultaneously by 1 standard deviation. The mean, width, and their corresponding uncertainties are used to define the shape of electron $n\sigma_e$ distribution in the following 3-Gaussian fit. The $n\sigma_e$ of $\pi^+$ and $K^+ + p^+$ are also expected to follow Gaussian distributions [28]. Ideally their width is one and their means can be calculated through the Bichsel function [29]. These ideal values are used as the initial values of the fit parameters in the following 3-Gaussian fit.

Figure 5 shows the constrained 3-Gaussian fits to the $n\sigma_e$ distributions of inclusive electron candidates with $2.5 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$ in the Run2008 analysis (upper left), $2.5 \text{ GeV}/c < p_T < 3.5 \text{ GeV}/c$ in the Run2005 analysis (lower left), and $8.0 \text{ GeV}/c < p_T < 10.0 \text{ GeV}/c$ in the Run2008 analysis (right). Here we leave the $n\sigma_e$ cut open. The dotted, dot-dashed, and dashed lines represent, respectively, the fits for $K^+ + p^+$, $\pi^+$, and $e^\pm$. Compared to the Run2008 analysis, the electron component in the Run2005 analysis at similar $p_T$ is more prominent due to the larger conversion electron yield. The solid lines are the overall fits to the spectra. The purity is calculated as the ratio of the integral of the electron fit function to that of the overall fit function above the $n\sigma_e$ cut.

No constraints are applied to the $K^+ + p^+$ and $\pi^+$ functions unless the fits fail. To estimate the systematic uncertainty of the purity, the mean and width of the electron function are allowed to vary up to one, two, three, and four standard deviations from their central values. For each of the four constraints, we calculate one value of the purity. The final purity is taken as the mean and the systematic uncertainty is taken as the largest difference between the mean and the four values from the four constraints. To estimate the statistical uncertainty of the purity, we rely on a simple Monte-Carlo simulation. We first obtain a large sample of altered overall $n\sigma_e$ spectra by randomly shifting each data point in the original spectrum in Fig. 5 according to a Gaussian distribution with the mean and width set to be equal to the central value and the uncertainty of the original data point, respectively. We then obtain the purity distribution through calculating the purity from each of these altered spectra following the same procedure as discussed above. In the end, we fit the distribution with a Gaussian function and take its width as the statistical uncertainty. The total uncertainty of the purity is obtained as the quadratic sum of the statistical and systematic uncertainties.

We follow the same procedure in the Run2008 and the Run2005 analysis except that the overall $n\sigma_e$ distribution in the Run2008 analysis is the combined result from the data sets of all three high-tower triggers as described in Sec. II C, while in the Run2005 analysis, the purity are calculated separately for the two high-tower triggers. Figure 6 shows the purity as a function of electron $p_T$ for the Run2008 (a) and the Run2005 (b) data. Tighter electron identification cuts and much higher photonic electron yield lead to much higher purity for the Run2005 inclusive electron sample.

FIG. 5 (color online). $n\sigma_e$ distribution for inclusive electrons (closed circles) and fits from different components at (a) $2.5 \text{ GeV}/c < p_T < 3.0 \text{ GeV}/c$ in the Run2008 analysis, (b) $2.5 \text{ GeV}/c < p_T < 3.5 \text{ GeV}/c$ in the Run2005 analysis, and (c) $8.0 \text{ GeV}/c < p_T < 10.0 \text{ GeV}/c$ in the Run2008 analysis after applying all electron identification cuts except the $n\sigma_e$ cut. Different curves represent $K^+ + p^+$ (dotted line), $\pi^+$ (dot-dashed line), electrons (dashed line), and the overall fit (solid lines).

FIG. 6. Purity of the inclusive electron sample as a function of $p_T$ in data from (a) Run2008 and (b) Run2005. The 2008 result is from combined data sets of all different high-tower triggers. The 2005 results for the two different high-tower triggers, i.e. HT1 (closed circles) and HT2 (open circles), are plotted separately.
D. Photonic electron reconstruction efficiency

Since photon conversions, \( \pi^0 \) and \( \eta \) meson Dalitz decays are the dominant sources of photonic electrons, they are the components that we used to calculate \( \varepsilon_{\text{pho}} \), the photonic electron reconstruction efficiency, in the analysis of the Run2008 data. The \( \varepsilon_{\text{pho}} \) for each individual component is calculated separately to account for its possible dependence on the decay kinematics of the parent particles. The final \( \varepsilon_{\text{pho}} \) is obtained by combining results from all components according to their relative contribution to the photonic electron yield.

The determination of \( \varepsilon_{\text{pho}} \) is done through reconstructing electrons from simulated \( \gamma \) conversion or Dalitz decay of \( \pi^0 \) and \( \eta \) with uniform \( p_T \) distributions that are embedded into high-tower trigger events. These events are then fully reconstructed using the same software chain as used for data analysis. To account for the efficiency dependence on the parent particle \( p_T \), we use a fit function to the measured \( \pi^0 \) spectrum, the derived \( \eta \) and inclusive photon \( p_T \) spectra as weights. The fit function to the measured \( \pi^0 \) spectrum is provided by the PHENIX experiment in Ref. [32]. The \( \eta \) spectrum is derived from the \( \pi^0 \) measurement assuming \( m_T \) scaling, i.e. replacing \( p_T \) with \( \sqrt{p_T^2 + m_{\pi^0}^2 - m_{\eta}^2} \), while keeping the function form unchanged. Figure 7(a) shows the derived inclusive \( \gamma \) \( p_T \) spectrum (solid line), and an estimate of its uncertainty represented by the region between the dotted and dot-dashed lines. Figure 7(b) shows the uncertainty in linear scale. The inclusive \( \gamma \) spectrum is obtained by adding the direct \( \gamma \) yield to the \( \pi^0 \) and \( \eta \) decay \( \gamma \) yield calculated using PYTHIA. The direct \( \gamma \) yield is obtained from the fit function to the direct \( \gamma \) measurement provided by the PHENIX experiment in Ref. [32]. The dot-dashed line represents the \( \gamma \) spectrum from \( \pi^0 \) and \( \eta \) decay alone. The dotted line is obtained by doubling the direct \( \gamma \) component in the inclusive photon spectrum. By comparing the ratio of the derived inclusive \( \gamma \) yield to that of \( \pi^0 \) and \( \eta \) decay photon with the double ratio measurement in \( \text{Au} + \text{Au} \) most peripheral collisions [33], we found the uncertainty covers the possible variations of the inclusive photon yield.

STAR simulations for \( \gamma \) conversion and Dalitz decay are based on GEANT3 [34] which incorrectly treats Dalitz decays as simple three-body decays in phase space. We therefore modified the GEANT decay routines using the correct Kroll-Wada decay formalism [35]. Their kinematics is strongly modified by the dynamic electromagnetic structure arising at the vertex of the transition which is formally described by a form factor. We included the most recent form factors using a linear approximation for the \( \pi^0 \) Dalitz decay [36], and a pole approximation for the decays of \( \eta \) [37].

Figure 8(a) shows the photonic electron reconstruction efficiency as a function of electron \( p_T \) for \( \gamma \) conversion, \( \pi^0 \) and \( \eta \) Dalitz decay electrons, which turn out to be very similar because of the similar decay kinematics. The increase towards larger electron \( p_T \) is due to the higher probability of reconstructing both electrons from high \( p_T \) (virtual) photons. The uncertainties shown in the plots are dominated by the statistics of the simulated events. The effect due to the variation of the inclusive photon spectrum shape is found to be negligible for this analysis. Figure 8(b) shows the combined photonic electron reconstruction efficiency for the Run2008 analysis, which is calculated as...
\[ \epsilon_{\text{pho}}(p_T) = \frac{N_{\gamma}^i(p_T)}{N_{\gamma}^i(p_T) + N_{\pi^0}^i(p_T) + N_{\eta}^i(p_T)} \cdot \epsilon_{\gamma}(p_T) \]

\[ + \frac{N_{\pi^0}^i(p_T)}{N_{\gamma}^i(p_T) + N_{\pi^0}^i(p_T) + N_{\eta}^i(p_T)} \cdot \epsilon_{\pi^0}(p_T) \]

\[ + \frac{N_{\eta}^i(p_T)}{N_{\gamma}^i(p_T) + N_{\pi^0}^i(p_T) + N_{\eta}^i(p_T)} \cdot \epsilon_{\eta}(p_T), \]

where \( N_{\gamma}^i \), \( N_{\pi^0}^i \), and \( N_{\eta}^i \) are, respectively, the yield of electrons from photon conversion, \( \pi^0 \) and \( \eta \) Dalitz decay; \( \epsilon_{\gamma} \), \( \epsilon_{\pi^0} \), and \( \epsilon_{\eta} \) are the corresponding photonic electron reconstruction efficiencies. Based on Table I, approximately 36% of the photonic electrons are from \( \pi^0 \) Dalitz decay and about 10% are from \( \eta \) Dalitz decay. Their variations have a negligible effect on the results since \( \epsilon_{\gamma} \), \( \epsilon_{\pi^0} \), and \( \epsilon_{\eta} \) are almost identical. The solid line is a second order polynomial fit to the data. The systematic uncertainty is represented by the region between the dotted lines, which are second order polynomial fits after moving all the data points simultaneously up and down by 1 standard deviation.

For the Run2005 analysis, the dominant source of photonic electrons is conversion in the silicon detectors. We therefore neglect contributions from Dalitz decays while following the same procedure as for the Run2008 analysis to calculate \( \epsilon_{\text{pho}} \). Figure 8(c) shows \( \epsilon_{\text{pho}} \) as a function of \( p_T \) for \( \gamma \) conversion for the Run2005 analysis. The solid line is a fit to the spectrum with a second order polynomial function and the region between the dotted lines represents the uncertainty estimated in the same way as for the Run2008 analysis. The inclusion of the Dalitz decays is estimated to reduce the \( \epsilon_{\text{pho}} \), by less than 0.5% which is well within the systematic error. The uncertainty because of the inaccurate material distribution in the simulation as mentioned in Sec. II B is negligible since the majority of the material, dominated by our silicon detectors, is within a distance of 30 cm from beam pipe and the variation of \( \epsilon_{\text{pho}} \) of photonic electrons produced within this region is small.

E. Trigger efficiency

The trigger efficiency is the ratio of the electron yield from high-tower trigger events to that from minimum-bias trigger events after normalizing the two according to the integrated luminosity. To have a good understanding of trigger efficiency, one needs enough minimum-bias events for the baseline reference. However, for the Run2008 \( p + p \) data, the number of minimum-bias events is too small to be used for this purpose. Fortunately, the Run2008 \( d + Au \) data were taken using the same sets of high-tower triggers as used for the \( p + p \) run. Since the two data sets were taken serially, the high-tower trigger efficiency is expected to be the same. During the \( d + Au \) run, many events also were taken using the VPD trigger, which is essentially a less efficient minimum-bias trigger that can serve as the baseline reference for trigger efficiency analysis. As a cross-check, we also evaluate the trigger efficiency through the Run2008 \( p + p \) simulation.

From the VPD trigger events, we first regenerate a high-tower trigger \( p_T \) spectrum by requiring \( \text{adc}0 \) of BEMC clusters to be larger than the threshold. The \( \text{adc}0 \) is the off-line ADC value of a BEMC cluster’s most energetic tower which is one of the high towers responsible for firing a high-tower trigger. Figure 9(a) shows the \( \text{adc}0 \) distribution of photonic electrons from high-tower trigger events. The sharp cutoff around a value of 200 is the off-line ADC value of the trigger threshold setting. The smaller peak below the trigger threshold is due to electrons which happen to be in events triggered by something other than the electrons. By requiring \( \text{adc}0 \) to be larger than the threshold, we reject these electrons which did not trigger the event since the uncertainty of their yield is affected by many sources and is therefore hard to be evaluated reliably. When the threshold is correctly chosen, the regenerated spectrum shape should be very similar to that of the actual high-tower trigger. We therefore quantitatively determine the trigger threshold as the \( \text{adc}0 \) cut which minimizes the

\[ \chi^2 = \sum_i \left( \frac{N_i(\text{VPD} + \text{adc}0) - N_i(\text{HT})}{\sigma_i^2} \right)^2, \]

where \( N_i(\text{VPD} + \text{adc}0) \) is the regenerated high-tower trigger electron yield from VPD events in the \( i \) th \( p_T \) bin, \( N_i(\text{HT}) \) is the electron yield at the same \( p_T \) bin from the actual high-tower trigger events, and \( \sigma_i \) is the uncertainty

![FIG. 9 color online. (a) \text{adc}0 distribution for high-tower trigger events. (b) \( \chi^2 \) as a function of the \text{adc}0 cut. (c) Raw inclusive electron \( p_T \) spectrum from VPD trigger in Run2008 \( d + Au \) collisions before (open squares) and after applying the \( \text{adc}0 > 193 \) cut (closed circles). (d) \text{adc}0 distribution for data (closed circles) and simulation (solid line) at \( p_T = 4.0 - 5.0 \text{ GeV/c} \). See text for details.](052006-10)
reasonably well. At lower \( \tau \) events assigning a systematic uncertainty identical to the
function of the \( \tau \) generated high-tower spectrum (closed circles) after applying the \( \tau \) > 193 cut used to calculate the trigger efficiency.

To estimate trigger efficiency through simulation, we
tune the simulated single electron \( \tau \) spectrum in each individual \( \tau \) bin to agree with the data in the region above the threshold. The data spectra are obtained from the unlike-minus-like pairs, i.e. pure photonic electrons. As a
demonstration of the comparison, Fig. 9(d) shows the
spectra from data (closed circles) and simulation (solid line) at 4.0 \( \text{GeV}/c < \tau < 5.0 \) \( \text{GeV}/c \). The efficiency is
defined as the fraction of the simulated \( \tau \) spectrum integral above the trigger threshold.

In the Run2008 analysis the raw \( \tau \) spectrum of nonphotonic electrons is obtained by combining the data sets of all three high-tower triggers. Since the shape of the combined spectrum is the same as that of the high-tower trigger with the lowest threshold, we only need to estimate the trigger efficiency of this lowest threshold trigger. Figure 10 shows the trigger efficiency as a function of \( \tau \) that is calculated using \( d + Au \) VPD events (closed circles) and simulated events (closed triangles) in the Run2008 analysis. At \( \tau > 3.5 \) \( \text{GeV}/c \), they agree with each other reasonably well. At lower \( \tau \), the simulated results are not reliable because the numerator in the efficiency calculation is only from a tail of the spectrum and a small mismatch between simulation and data can have a large impact on the results. On the other hand, the results from VPD events suffer from low statistics at high \( \tau \). The final efficiency is therefore taken to be the combination of the two, i.e., at \( \tau < 3.5 \) \( \text{GeV}/c \), the efficiency is equal to that from VPD events assigning a systematic uncertainty identical to the
statistical uncertainty of the data point, while at high \( \tau \), the efficiency is equal to the simulated results, and the systematic errors are from the tuning uncertainty.

In the Run2005 analysis, the efficiencies of the two high-tower triggers are estimated separately. While there are more minimum-bias events for Run2005 than for Run2008, the statistics are poor at \( \tau > 2.0 \) \( \text{GeV}/c \). We thus rely on a fit to the spectrum, which consists of minimum-bias events at low \( \tau \) and high-tower trigger events at high \( \tau \) where the trigger is expected to be fully efficient, as the baseline reference for the trigger efficiency evaluation. Figure 11 shows the raw inclusive electron \( \tau \) spectrum from minimum-bias, HT1 and HT2 events. The fit uses a power-law function \( A(1 + \tau / B)^{-n} \). The regions where we expect the HT1 and the HT2 trigger to be fully efficient are above 4.5 and 6.0 \( \text{GeV}/c \), respectively. The dashed line shows the fit uncertainty, obtained from many fit trials. In a single fit trial, each data point is randomized with a Gaussian random number, with the mean to be the central value and the rms to be the statistical uncertainty of the data point. Additional systematic uncertainty coming from fits using different functions is included in the cross-section calculation and is not displayed in the figure. Figure 12 shows the efficiency of HT1 (a) and HT2 (b) triggers, defined as the ratio of the raw HT1 or HT2 inclusive electron spectrum to the baseline fit function. We used error functions to parametrize both efficiencies. The dashed lines represent the uncertainty, obtained in the same way as for the Fig. 11 fits.

High-tower trigger efficiency for photonic and nonpho-
tonics can be different. Unlike nonphotonic electrons, a photonic electron always has a partner. In case both share the same BEMC tower, the deposited energy will be higher than that for an isolated electron and will lead to a higher efficiency. The effect can be quantified by

\[
\chi^2/\text{ndf} = 18.8/29
\]

FIG. 10 (color online). \( \tau \) dependence of high-tower trigger efficiency from data (closed circles), simulation (closed triangles), and combined results (solid line) for Run2008 analysis. The dashed lines represent the uncertainty. See text for details.

FIG. 11 (color online). Raw inclusive electron \( \tau \) spectrum for minimum-bias (closed circles) and two high-tower triggers, i.e. HT1 (closed circles) and HT2 (open squares) together with a power-law fit (solid line) and fit uncertainty (dashed line) for Run2005 analysis.
comparing the ratio of the isolated electron yield to the yield of electrons with partners in minimum-bias events to the same ratio in high-tower trigger events. We found that the difference is negligible at $p_T > 2.5 \text{ GeV}/c$, while the trigger efficiency for photonic electron is 20%–30% higher than for nonphotonic electron in the lower $p_T$ region.

F. Stability of the luminosity monitor

The BBC trigger was used to monitor the integrated luminosity for Run2005. During Run2008, because of the large beam background firing the BBC trigger, a high threshold high-tower trigger was used as the luminosity monitor. To quantify the stability of the monitor with respect to BBC, we calculate the BBC cross section as a function of run number using $\sigma_{\text{BBC}} = N_{\text{minbias}}/L$, where $L = N_{\text{mon}}/N_{\text{mon}}$, $\sigma_{\text{mon}}$ is the monitor cross section which is estimated to be $1.49 \mu\text{b}$ using low luminosity runs, $N_{\text{minbias}}$ and $N_{\text{mon}}$ are, respectively, the number of events from the BBC trigger and the monitor after correcting for prescaling during data acquisition. Here a run refers to a block of short term (~30 minutes) data taking. Figure 13(a) shows the distribution of the calculated $\sigma_{\text{BBC}}$. There are two peaks in the figure. The dominant one centered around 25 mb contains most of the recorded luminosity in Run2008. The minor one centered at a higher value comes from events taken at the beginning and the end of Run2008 represented by the regions beyond the two dashed lines in Fig. 13(b) showing the calculated BBC cross section as a function of run number. After removing these runs taken at the beginning and the end of Run2008, the minor peak disappeared and the performance of the monitor appeared to be very stable.

In the data analysis, we also reject those with $\sigma_{\text{BBC}} < 20 \text{ mb}$ or $\sigma_{\text{BBC}} > 30 \text{ mb}$. We fit the $\sigma_{\text{BBC}}$ distribution with a Gaussian function and assign the width of the function (2.3%) as the systematic uncertainty of the $\sigma_{\text{mon}}$ with respect to BBC cross section.

The integrated luminosity sampled by the high-tower triggers are ~2.6 and ~2.8 $\text{pb}^{-1}$ for Run2008 and Run2005, respectively.

G. Contribution from vector mesons

The main background sources of electrons that do not originate from photon conversion and Dalitz decay are electromagnetic decays of heavy ($J/\psi$, $\Upsilon$) and light vector mesons ($\rho$, $\omega$, and $\phi$) as well as those from Drell-Yan process.

The electrons from $J/\psi$ decay contribute noticeably to the observed nonphotonic electron signal as pointed out in Ref. [38]. In order to estimate the contribution from $J/\psi \rightarrow e^+e^-$ to the nonphotonic electron yield, we combine the measured differential $J/\psi$ cross sections from PHENIX [39] and STAR [40]. For each data point we add the statistical and systematic uncertainties, except the global uncertainties, in quadrature. Figure 14(a) shows the measured $J/\psi$ differential cross section from the two experiments. While the PHENIX measurement dominates the low to medium-$p_T$ region, the STAR measurement dominates the high-$p_T$ region. The combined spectrum is fit using a power-law function of the form $E^3d\sigma/d^3p|_{\gamma=0} = A(\exp(bp_T - b\gamma^2) + p_T/p_0)^{-n}$, where $A = 5.24 \pm 0.87 \text{ mb \cdot GeV}^{-2}\text{c}^3$, $a = 0.32 \pm 0.04 \text{ GeV}^{-1}\text{c}$, $b = 0.06 \pm 0.03 \text{ GeV}^{-2}\text{c}^2$, $p_0 = 2.59 \pm 0.21 \text{ GeV}/c$, and $n = 8.44 \pm 0.61$ are fit parameters. The $\chi^2$/NDF of the fit is 27.8/25. To obtain the uncertainty of the fit, the global uncertainties of the STAR and the PHENIX (10% [41]) measurements are assumed to be uncorrelated. We move the PHENIX data up by 10% and repeat the fit to obtain the band of 68% confidence intervals. The upper edge of the band is treated
as the upper bound of the fit. Following the same procedure except moving the PHENIX data down by 10%, we obtain the lower bound of the fit as the lower edge of the band. Furthermore, since we are considering a rather large $p_T$ range ($p_T < 14.0 \text{ GeV}/c$), we cannot assume that the $p_T$ and rapidity distributions factorize. We use PYTHIA to generate $dN/dy(p_T)$ and implement a Monte Carlo program using the above functions as probability density functions to generate $J/\psi$ and decay them into $e^+ e^-$ assuming the $J/\psi$ to be unpolarized. The decay electrons are filtered through the same detector acceptance as used for the nonphotonic electrons. The band in Fig. 14(b) shows the invariant cross section of $J/\psi$ decay electrons as a function of the electron $p_T$. The uncertainty of the derived yield comes from the uncertainty of the fit to the $J/\psi$ spectra and is represented by the band which is also shown in Fig. 14(c) in linear scale.

The invariant cross section of electrons from $Y$ decays ($Y \rightarrow e^+ e^-$), represented by the dot-dashed line in Fig. 14(b), is calculated in a similar fashion as that for the $J/\psi$ except that the input $Y$ spectrum is from a next-to-leading-order perturbative quantum chromodynamics (pQCD) calculation in the color evaporation model (CEM) [42]. We have to rely on model calculations since so far no invariant $p_T$ spectrum in our energy range has been measured. However, in a recent measurement STAR reported the overall production cross section for the sum of all three $Y(1S + 2S + 3S)$ states in $p + p$ collisions at $\sqrt{s} = 200 \text{ GeV}$ to be $B \times d\sigma/dy = 114 \pm 38^{+23}_{-24} \text{ pb}$, which is consistent with the CEM prediction [43].

Adding the statistical and systematic uncertainty in quadrature, the total relative uncertainty of this measurement is $\sim 39\%$, which is the value we assigned as the total uncertainty of the $Y$ feed-down contribution to the nonphotonic electrons at all $p_T$.

The contribution to the nonphotonic electron yield from the light vector mesons is estimated using PYTHIA, assuming the meson spectra follow $m_T$ scaling. We generate a sample of decay electrons using light vector mesons with flat spectra in $p_T$ as input. To derive the differential cross section of the electrons, we keep only those electrons within the same detector acceptance as that for the nonphotonic electrons and weight them with the spectra of $\rho$, $\omega$, and $\phi$. The meson spectra are obtained by replacing the $p_T$ with $\sqrt{p_T^2 + m_h^2 - m_\pi^2}$ in the same fit function as for the $\pi^0$ measurement (see Fig. 7). Here $m_h$ is the mass of the vector meson. The relative yields of the mesons to $\tau$ [17] are also taken into account during this process. We include the decay channels $\phi \rightarrow e^+ e^-$, $\phi \rightarrow \eta e^+ e^-$, $\omega \rightarrow e^+ e^-$, $\omega \rightarrow \pi^0 e^+ e^-$, and $\rho \rightarrow e^+ e^-$ in the calculation. The derived electron differential cross section is represented by the solid line in Fig. 14(b). We assign a 50% systematic uncertainty to cover the uncertainty of the $\pi^0$ measurement and the meson to pion ratios.

The contribution to the nonphotonic electron yield from the Drell-Yan processes is represented by the dotted line in Fig. 14(b) and is estimated from a leading-order pQCD calculation using the CTEQ6M parton distribution function with a $K$-factor of 1.5 applied and without a cut on the electron pair mass [44]. No uncertainty is assigned to this estimate.

IV. RESULTS

A. Nonphotonic electron invariant cross section

The invariant cross section for nonphotonic electron production is calculated according to

$$E \frac{d^3 \sigma}{dp_T^3} = \frac{1}{L} \frac{1}{2 \pi p_T \Delta y} \frac{N_{\text{np}}} {\epsilon_{\text{rec}} \epsilon_{\text{trig}} \epsilon_{\text{fid}} \epsilon_{\text{BBC}}} ,$$

where $N_{\text{np}}$ is the nonphotonic electron raw yield with the $V_z$ cuts, $\epsilon_{\text{rec}}$ is the product of the single electron reconstruction efficiency and the correction factor for momentum resolution and finite spectrum bin width, $\epsilon_{\text{trig}}$ is the high-trigger efficiency, $\epsilon_{\text{fid}}$ is the electron identification efficiency, $L$ is the integrated luminosity with the $V_z$ cuts, and $\epsilon_{\text{BBC}} = 0.866 \pm 0.08$ is the BBC trigger efficiency. The systematic uncertainties of all these quantities are listed in Table II. The relative uncertainty of $L \cdot \epsilon_{\text{BBC}}$ in maximum range is 14% including uncertainties in tracking efficiency [24]. Assuming a flat distribution within the range, we estimate the $L \cdot \epsilon_{\text{BBC}}$ uncertainty to be 8.1% in 1 standard deviation. The uncertainty of $N_{\text{np}}$ is the quadratic sum of the uncertainties from the estimation of $\epsilon_{\text{pho}}$, purity and the light vector meson contribution. The uncertainty of $\epsilon_{\text{rec}}$ is the quadratic sum of the uncertainties from
TABLE II. Sources of systematic uncertainty for the nonphotonic electron invariant yield in $p + p$ collisions. Type A are point to point uncertainties. Type B are scaling uncertainties which move data points in the same direction. Type C are the scaling uncertainties that are common to both Run2008 and Run2005. The range in each individual source covers the variation of the systematic uncertainty as a function of $p_T$.

<table>
<thead>
<tr>
<th>source</th>
<th>Run2008</th>
<th>Run2005</th>
</tr>
</thead>
<tbody>
<tr>
<td>$N_{npe}$</td>
<td>5.0–48.1% (A)</td>
<td>8.5–38.0% (A)</td>
</tr>
<tr>
<td>$\epsilon_{eid}$</td>
<td>6.5–25.2% (A)</td>
<td>0.7–2.0% (A)</td>
</tr>
<tr>
<td>$\epsilon_{frg}$</td>
<td>1.8–10.0% (A)</td>
<td>0.3–16% (A)</td>
</tr>
<tr>
<td>$\epsilon_{rec}$</td>
<td>2.3–33.3% (A)</td>
<td>1.0–3.5% (A)</td>
</tr>
<tr>
<td>$\epsilon_{BBC}$</td>
<td>15.7% (B)</td>
<td>11.0% (B)</td>
</tr>
<tr>
<td>$L \cdot \epsilon_{BBC}$</td>
<td>2.3% (B)</td>
<td>8.1% (C)</td>
</tr>
</tbody>
</table>

Correcting the track momentum resolution, the finite spectrum bin width as well as the estimation of single electron reconstruction efficiency. The range of the uncertainty for each individual quantity covers the variation of the uncertainty as a function of $p_T$. In order to compare with the result in Refs. [16,17], we do not subtract the $J/c\gamma$ and Drell-Yan contribution from the nonphotonic electron invariant cross section shown in Figs. 15 and 16.

Figure 15(a) shows the ratio of nonphotonic to photonic electron yield as a function of $p_T$ in $p + p$ collisions in Run2008 (closed circles) and Run2005 (open triangles). The ratio for Run2008 is much larger because there was much less material in front of the TPC for Run2008. Figure 15(b) shows the nonphotonic electron invariant cross section ($^{+}_{-}\sigma_{+}$) as a function of $p_T$ in $p + p$ collisions from the Run2008 analysis (closed circles) and the Run2005 analysis (open triangles). Despite the large difference in photonic background, the two measurements are in good agreement.

Figure 16(a) shows the nonphotonic electron ($^{+}_{-}\sigma_{+}$) invariant cross section obtained by combining the Run2008 and the Run2005 results using the “best linear unbiased estimate” [45]. The corrected result of our early published measurement using year 2003 data [16] is shown in the plot as well. The published result exceeded pQCD predictions from FONLL calculations by about a factor of 4. We, however, uncovered a mistake in the corresponding analysis in calculating $\epsilon_{pho}$. The details are described in the erratum [16]. To see more clearly the comparison, Fig. 16(b) shows the ratio of each individual measurement, including PHENIX results, to the FONLL calculation. One can see that all measurements at RHIC on nonphotonic...
electron production in $p + p$ collisions are now consistent with each other. The corrected run 2003 data points have large uncertainties because of the small integrated luminosity ($\sim 100 \text{ nb}^{-1}$) in that run. FONLL is able to describe the RHIC measurements within its theoretical uncertainties.

B. Invariant cross section of electrons from bottom and charm meson decays

Electrons from bottom and charm meson decays are the two dominant components of the nonphotonic electrons. Mostly due to the decay kinematics, the azimuthal correlations between the daughter electron and daughter hadron are different for bottom meson decays and charm meson decays. A study of these azimuthal correlations has been carried out on STAR data and is compared with a PYTHIA simulation to obtain the ratio of the bottom electron yield to the heavy-flavor decay electron yield ($e_B/(e_B + e_D)$) [19], where PYTHIA was tuned to reproduce STAR measurements of D mesons $p_T$ spectra [46]. Using the measured $e_B/(e_B + e_D)$, together with the measured nonphotonic electron cross section with the electrons from $J/\psi$, $Y$ decay and Drell-Yan processes subtracted, we are able to disentangle these two components.

The bottom electron cross section is calculated as $e_B/(e_B + e_D)$ times the nonphotonic electron cross section with the contribution from $J/\psi$, $Y$ decay and Drell-Yan processes subtracted. The same procedure applies to the charm electrons except that $(1 - e_B/(e_B + e_D))$ is used instead. The specific location of $p_T$, where the $e_B/(e_B + e_D)$ is measured, is different from that of the nonphotonic electrons. To accommodate the difference, we calculate $e_B/(e_B + e_D)$ in any given $p_T$ in nonphotonic electron measurements through a linear interpolation of the actual $e_B/(e_B + e_D)$ measurements. As an estimation of the systematic uncertainty of the interpolated value, we also repeat the same procedure using the curve predicted by FONLL. Figure 17 shows the invariant cross section of electrons ($e^{-}\bar{e}^{-}$) from bottom (upper left) and charm meson (upper right) decay, together with the ratio of the corresponding measurements to the FONLL predictions for bottom (lower left) and charm electrons (lower right). The solid circles are experimental measurements. The error bars and the boxes are, respectively, the statistical and systematic uncertainties. The solid and dotted curves are the FONLL predictions and their uncertainties. The dashed and dot-dashed curves are the FONLL prediction for $B \rightarrow D \rightarrow e$, i.e. electrons from the decays of D mesons which in turn come from B meson decays.

FIG. 17 (color online). Invariant cross section of electrons ($e^{-}\bar{e}^{-}$) from bottom (upper left) and charm meson (upper right) decay, together with the ratio of the corresponding measurements to the FONLL predictions for bottom (lower left) and charm electrons (lower right). The solid circles are experimental measurements. The error bars and the boxes are, respectively, the statistical and systematic uncertainties. The solid and dotted curves are the FONLL predictions and their uncertainties. The dashed and dot-dashed curves are the FONLL prediction for $B \rightarrow D \rightarrow e$, i.e. electrons from the decays of D mesons which in turn come from B meson decays.

$3 \text{ GeV}/c < p_T < 10 \text{ GeV}/c$ from bottom and charm meson decays to be, respectively,

$$
\frac{d\sigma_{(B\rightarrow e) + (B\rightarrow D\rightarrow e)}}{dy_e} \bigg|_{y_e=0} = 4.0 \pm 0.5(\text{stat}) \\
\pm 1.1(\text{syst}) \text{ nb} \frac{d\sigma_{D\rightarrow e}}{dy_e} \bigg|_{y_e=0} = 6.2 \pm 0.7(\text{stat}) \pm 1.5(\text{syst}) \text{ nb},
$$

where $y_e$ is the electron rapidity. The 8.1% global scale uncertainty from the BBC cross section is included in the total systematic uncertainty.

Relying on theoretical model predictions to extrapolate the measured results to the phase space beyond the reach of the experiment, one can estimate the total cross section for charm or bottom quark production. We perform a PYTHIA calculation with the same parameters as in Ref. [15]. After normalizing the $p_T$ spectrum to our high-$p_T$ measurements and extrapolating the results to the full kinematic phase space, we obtain a total bottom production cross section of 1.34$\mu$b. However, with the PYTHIA calculation using the same parameters except MSEL = 5, i.e. bottom production processes instead of minimum-bias processes as in the former calculation, we obtain a value of 1.83$\mu$b. The PYTHIA authors recommend the minimum-bias processes [31]. This large variation between the extracted total
bottom production cross sections comes mostly from the large difference in the shape of the bottom electron spectrum in the two PYTHIA calculations with MSEL = 1 and with MSEL = 5. Since both calculations are normalized to the measured data, the difference in the shape shows up at \( p_T < 3 \text{ GeV}/c \). The fact that the PYTHIA calculation with MSEL = 5 only includes leading-order diagrams of bottom production causes the difference between the PYTHIA calculations. Measurements in the low \( p_T \) region are therefore important for the understanding of bottom quark production at RHIC. Both values are consistent with the FONLL [2] prediction, \( 1.87^{+0.99}_{-0.67} \mu \text{b} \), within its uncertainty.

V. CONCLUSIONS

STAR measurements of high \( p_T \) nonphotonic electron production in \( p + p \) collisions at \( \sqrt{s} = 200 \text{ GeV} \) using data from Run2005 and Run2008 agree with each other despite the large difference in background. This measurement and PHENIX measurement are consistent with each other within the quoted uncertainties. After correcting a mistake in the photonic electron reconstruction efficiency, the published STAR result using year 2003 data is consistent with our present measurements. We are able to disentangle the electrons from bottom and charm meson decays in the nonphotonic electron spectrum using the measured ratio of \( e_B/\left( e_B + e_D \right) \) and the measured nonphotonic cross section. The integrated bottom and charm electron cross sections \( \left( \frac{\sigma}{\sigma_{e}} \right) \) at 3 GeV/c < \( p_T < 10 \text{ GeV}/c \) are determined separately as

\[
\frac{d\sigma(B \rightarrow e^- \gamma \rightarrow e^- + X)}{dy_e} \bigg|_{y = 0} = 4.0 \pm 0.5 \text{(stat)} \pm 1.1 \text{(syst)} \text{ nb}
\]

\[
\frac{d\sigma(D \rightarrow e^- \gamma \rightarrow e^- + X)}{dy_e} \bigg|_{y = 0} = 6.2 \pm 0.7 \text{(stat)} \pm 1.5 \text{(syst)} \text{ nb}
\]

FONLL can describe these measurements within its theoretical uncertainties. Future measurements on low-\( p_T \) electrons from bottom meson decay are important to overcome the large uncertainties of the derived total bottom quark production cross section that originate mostly from the large variations of theoretical model prediction in the low-\( p_T \) region.

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[41] C. L. D. Silva (private communication).


[44] W. Vogelsang (private communication).
