Slow Adaptive OFDMA Systems Through Chance Constrained Programming

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Abstract—Adaptive orthogonal frequency division multiple access (OFDMA) has recently been recognized as a promising technique for providing high spectral efficiency in future broadband wireless systems. The research over the last decade on adaptive OFDMA systems has focused on adapting the allocation of radio resources, such as subcarriers and power, to the instantaneous channel conditions of all users. However, such “fast” adaptation requires high computational complexity and excessive signaling overhead. This hinders the deployment of adaptive OFDMA systems worldwide. This paper proposes a slow adaptive OFDMA scheme, in which the subcarrier allocation is updated on a much slower timescale than that of the fluctuation of instantaneous channel conditions. Meanwhile, the data rate requirements of individual users are accommodated on the fast timescale with high probability, thereby meeting the requirements except occasional outage. Such an objective has a natural chance constrained programming formulation, which is known to be intractable. To circumvent this difficulty, we formulate safe tractable constraints for the problem based on recent advances in chance constrained programming. We then develop a polynomial-time algorithm for computing an optimal solution to the reformulated problem. Our results show that the proposed slow adaptation scheme drastically reduces both computational cost and control signaling overhead when compared with the conventional fast adaptive OFDMA. Our work can be viewed as an initial attempt to apply the chance constrained programming methodology to wireless system designs. Given that most wireless systems can tolerate an occasional dip in the quality of service, we hope that the proposed methodology will find further applications in wireless communications.

Index Terms—Adaptive orthogonal frequency division multiple access (OFDMA), chance constrained programming, dynamic resource allocation, stochastic programming.

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I. INTRODUCTION

FUTURE wireless systems will face a growing demand for broadband and multimedia services. Orthogonal frequency division multiplexing (OFDM) is a leading technology to meet this demand due to its ability to mitigate wireless channel impairments. The inherent multicarrier nature of OFDM facilitates flexible use of subcarriers to significantly enhance system capacity. Adaptive subcarrier allocation, recently referred to as adaptive orthogonal frequency division multiple access (OFDMA) [1], [2], has been considered as a primary contender in next-generation wireless standards, such as IEEE802.16 WiMAX [3] and 3GPP-LTE [4].

In the existing literature, adaptive OFDMA exploits time, frequency, and multiuser diversity by quickly adapting subcarrier allocation (SCA) to the instantaneous channel state information (CSI) of all users. Such “fast” adaptation suffers from high computational complexity, since an optimization problem required for adaptation has to be solved by the base station (BS) every time the channel changes. Considering the fact that wireless channel fading can vary quickly (e.g., at the order of milliseconds in wireless cellular system), the implementation of fast adaptive OFDMA becomes infeasible for practical systems, even when the number of users is small.

Recent work on reducing complexity of fast adaptive OFDMA includes [5], [6], etc. Moreover, fast adaptive OFDMA requires frequent signaling between the BS and mobile users in order to inform the users of their latest allocation decisions. The overhead thus incurred is likely to negate the performance gain obtained by the fast adaptation schemes. To date, high computational cost and high control signaling overhead are the major hurdles that prevent adaptive OFDMA from being deployed in practical systems.

We consider a slow adaptive OFDMA scheme, which is motivated by [7], to address the aforementioned problem. In contrast to the common belief that radio resource allocation should be readapted once the instantaneous channel conditions change, the proposed scheme updates the SCA on a much slower timescale than that of channel fluctuation. Specifically, the allocation decisions are fixed for the duration of an adaptation window, which spans the length of many coherence times. By doing so, computational cost and control signaling overhead can be dramatically reduced. However, this implies that channel conditions over the adaptation window are uncertain at the decision time, thus presenting a new challenge in the design of slow adaptive OFDMA schemes. An important question is how to find a valid allocation decision that remains optimal and feasible for the entire adaptation window. Such a problem can be formulated as a stochastic programming problem, where the channel coefficients are random rather than deterministic.
Slow adaptation schemes have recently been studied in other contexts such as slow rate adaptation [7], [8] and slow power allocation [9]. Therein, adaptation decisions are made solely based on the long-term average channel conditions instead of fast channel fading. Specifically, random channel parameters are replaced by their mean values, resulting in a deterministic rather than stochastic optimization problem. By doing so, quality-of-service (QoS) can only be guaranteed in a long-term average sense, since the short-term fluctuation of the channel is not considered in the problem formulation. With the increasing popularity of wireless multimedia applications, however, there will be more and more inelastic traffic that require a guarantee on the minimum short-term data rate. As such, slow adaptation schemes based on average channel conditions cannot provide a satisfactory QoS.

On another front, robust optimization methodology can be applied to meet the short-term QoS. For example, robust optimization method was applied in [9]–[11] to find a solution that is feasible for the entire uncertainty set of channel conditions, i.e., to guarantee the instantaneous data rate requirements regardless of the channel realization. Needless to say, the resource allocation solutions obtained via such an approach are overly conservative. In practice, the worst-case channel gain can approach zero in deep fading, and thus the resource allocation problem can easily become infeasible. Even if the problem is feasible, the resource utilization is inefficient as most system resources must be dedicated to provide guarantees for the worst-case scenarios.

Fortunately, most inelastic traffic such as that from multimedia applications can tolerate an occasional dip in the instantaneous data rate without compromising QoS. This presents an opportunity to enhance the system performance. In particular, we employ chance constrained programming techniques by imposing probabilistic constraints on user QoS. Although this formulation captures the essence of the problem, chance constrained programs are known to be computationally intractable except for a few special cases [12]. In general, such programs are difficult to solve as their feasible sets are often nonconvex. In fact, finding feasible solutions to a generic chance constrained program is itself a challenging research problem in the Operations Research community. It is partly due to this reason that the chance constrained programming methodology is seldom pursued in the design of wireless systems.

In this paper, we propose a slow adaptive OFDMA scheme that aims at maximizing the long-term system throughput while satisfying with high probability the short-term data rate requirements. The key contributions of this paper are as follows.

- We design the slow adaptive OFDMA system based on chance constrained programming techniques. Our formulation guarantees the short-term data rate requirements of individual users except in rare occasions. To the best of our knowledge, this is the first work that uses chance constrained programming in the context of resource allocation in wireless systems.
- We exploit the special structure of the probabilistic constraints in our problem to construct safe tractable constraints (STC) based on recent advances in the chance constrained programming literature.
- We design an interior-point algorithm that is tailored for the slow adaptive OFDMA problem, since the formulation with STC, although convex, cannot be trivially solved using off-the-shelf optimization software. Our algorithm can efficiently compute an optimal solution to the problem with STC in polynomial time.

The rest of the paper is organized as follows. In Section II, we discuss the system model and problem formulation. An STC is introduced in Section III to solve the original chance constrained program. An efficient tailor-made algorithm for solving the approximate problem is then proposed in Section IV. In Section V, we reduce the problem size based on some practical assumptions, and show that the revised problem can be solved by the proposed algorithm with much lower complexity. In Section VI, the performance of the slow adaptive OFDMA system is investigated through extensive simulations. Finally, the paper is concluded in Section VII.

II. SYSTEM MODEL AND PROBLEM FORMULATION

This paper considers a single-cell multiuser OFDM system with \( K \) users and \( N \) subcarriers. We assume that the instantaneous channel coefficients of user \( k \) and subcarrier \( n \) are described by complex Gaussian \(^1\) random variables \( h_{k,n}^{(f)} \sim \mathcal{CN}(0, \sigma_k^2) \), independent \(^2\) in both \( n \) and \( k \). The parameter \( \sigma_k \) can be used to model the long-term average channel gain as \( \sigma_k = (d_k/d_0)^{-\gamma} \cdot s_k \), where \( d_k \) is the distance between the BS and subscriber \( k \), \( d_0 \) is the reference distance, \( \gamma \) is the amplitude path-loss exponent and \( s_k \) characterizes the shadowing effect. Hence, the channel gain \( g_{k,n}^{(f)} = |h_{k,n}^{(f)}|^2 \) is an exponential random variable with probability density function (PDF) given by

\[
 f_{g_{k,n}^{(f)}}(\xi) = \frac{1}{\sigma_k} \exp \left( -\frac{\xi}{\sigma_k} \right). \tag{1}
\]

The transmission rate of user \( k \) on subcarrier \( n \) at time \( t \) is given by

\[
 r_{k,n}^{(f)} = W \log_2 \left( 1 + \frac{p_k g_{k,n}^{(f)}}{\Gamma N_0} \right)
\]

where \( p_k \) is the transmission power of a subcarrier, \( g_{k,n}^{(f)} \) is the channel gain at time \( t \), \( W \) is the bandwidth of a subcarrier, \( N_0 \) is the power spectral density of Gaussian noise, and \( \Gamma \) is the capacity gap that is related to the target bit error rate (BER) and coding-modulation schemes.

In traditional fast adaptive OFDMA systems, SCA decisions are made based on instantaneous channel conditions in order to maximize the system throughput. As depicted in Fig. 1(a), SCA is performed at the beginning of each time slot, where the duration of the slot is no larger than the coherence time of the

\(^1\) Although the techniques used in this paper are applicable to any fading distribution, we shall prescribe to a particular distribution of fading channels for illustrative purposes.

\(^2\) The case when frequency correlations exist among subcarriers will be discussed in Section VI.
channel. Denoting by $x_{k,n}^{(t)}$ the fraction of airtime assigned to user $k$ on subcarrier $n$, fast adaptive OFDMA solves at each time slot $t$ the following linear programming problem:

$$\mathcal{P}_{\text{fast}} : \max_{x_{k,n}^{(t)}} \sum_{k=1}^{K} \sum_{n=1}^{N} x_{k,n}^{(t)} r_{k,n}^{(t)}$$

subject to:

$$\sum_{n=1}^{N} x_{k,n}^{(t)} r_{k,n}^{(t)} \geq q_k, \quad \forall k$$

$$\sum_{k=1}^{K} x_{k,n}^{(t)} \leq 1, \quad \forall n$$

$$x_{k,n}^{(t)} \geq 0, \quad \forall k,n$$

where the objective function in (2) represents the total system throughput at time $t$, and (3) represents the data rate constraint of user $k$ at time $t$ with $q_k$ denoting the minimum required data rate. We assume that $q_k$ is known by the BS and can be different for each user $k$. Since $r_{k,n}^{(t)}$ (and hence $x_{k,n}^{(t)}$) varies on the order of coherence time, one has to solve the problem $\mathcal{P}_{\text{fast}}$ at the beginning of every time slot to obtain SCA decisions. Thus, the above fast adaptive OFDMA scheme is extremely costly in practice.

In contrast to fast adaptation schemes, we propose a slow adaptation scheme in which SCA is updated only every adaptation window of length $T$. More precisely, SCA decision is made at the beginning of each adaptation window as depicted in Fig. 1(b), and the allocation remains unchanged till the next window. We consider the duration $T$ of a window to be large compared with that of fast fading fluctuation so that the channel fading process over the window is ergodic; but small compared with the large-scale channel variation so that path-loss and shadowing are considered to be fixed in each window. Unlike fast adaptive systems that require the exact CSI to perform SCA, slow adaptive OFDMA systems rely only on the distributional information of channel fading and make an SCA decision for each window.

Let $x_{k,n} \in [0,1]$ denote the SCA for a given adaptation window. Then, the time-average throughput of user $k$ during the window becomes

$$\bar{r}_k = \sum_{n=1}^{N} x_{k,n} \bar{r}_{k,n}$$

where

$$\bar{r}_{k,n} = \frac{1}{T} \int_{t}^{t+T} r_{k,n}^{(t)} dt$$

is the time-average data rate of user $k$ on subcarrier $n$ during the adaptation window. The time-average system throughput is given by

$$\bar{t} = \sum_{k=1}^{K} \sum_{n=1}^{N} x_{k,n} \bar{r}_{k,n}$$

Now, suppose that each user has a short-term data rate requirement $q_k$ defined on each time slot. If $\sum_{n=1}^{N} x_{k,n} r_{k,n}^{(t)} < q_k$, then we say that a rate outage occurs for user $k$ at time slot $t$, and the probability of rate outage for user $k$ during the window $[t_0, t_0 + T]$ is defined as

$$P_k^{\text{out}} = \Pr \left\{ \sum_{n=1}^{N} x_{k,n} r_{k,n}^{(t)} < q_k \right\}, \quad \forall t \in [t_0, t_0 + T]$$

where $t_0$ is the beginning time of the window.

Inelastic applications, such as voice and multimedia, that are concerned with short-term QoS can often tolerate an occasional dip in the instantaneous data rate. In fact, most applications can run smoothly as long as the short-term data rate requirement is satisfied with sufficiently high probability. With the above considerations, we formulate the slow adaptive OFDMA problem as follows:

$$\mathcal{P}_{\text{slow}} : \max_{x_{k,n}} \sum_{k=1}^{K} \sum_{n=1}^{N} x_{k,n} \mathbb{E} \left\{ r_{k,n}^{(t)} \right\}$$

subject to:

$$\Pr \left\{ \sum_{n=1}^{N} x_{k,n} r_{k,n}^{(t)} \geq q_k \right\} \geq 1 - \epsilon_k, \quad \forall k$$

$$\sum_{k=1}^{K} x_{k,n} \leq 1, \quad \forall n$$

$$x_{k,n} \geq 0, \quad \forall k,n$$

where the expectation in (4) is taken over the random channel process $g = \{g_{k,n}^{(t)}\}$ for $t \in [t_0, t_0 + T]$, and $\epsilon_k \in [0,1]$ in (5) is the maximum outage probability user $k$ can tolerate. In the above formulation, we seek the optimal SCA that maximizes the expected system throughput while satisfying each user’s short-term QoS requirement, i.e., the instantaneous data.

1It is practical to assume $x_{k,n}$ as a real number in slow adaptive OFDMA. Since the data transmitted during each window consists of a large mount of OFDM symbols, the time-sharing factor $x_{k,n}$, can be mapped into the ratio of OFDM symbols assigned to user $k$ for transmission on subcarrier $n$.

2In (4), we replace the time-average data rate $r_{k,n}$ by its ensemble average $\mathbb{E} \left\{ r_{k,n}^{(t)} \right\}$ due to the ergodicity of channel fading over the window.
rate of user \( k \) is higher than \( q_k \) with probability at least \( 1 - \epsilon_k \). The above formulation is a chance constrained program since a probabilistic constraint (5) has been imposed.

III. SAFE TRACTABLE CONSTRAINTS

Despite its utility and relevance to real applications, the chance constraint (5) imposed in \( P_{\text{slow}} \) makes the optimization highly intractable. The main reason is that the convexity of the feasible set defined by (5) is difficult to verify. Indeed, given a generic chance constraint \( \Pr\{F(x, \mathbf{r}) > 0\} \leq \epsilon \) where \( \mathbf{r} \) is a random vector, \( x \) is the vector of decision variable, and \( F \) is a real-valued function, its feasible set is often nonconvex except for very few special cases [12, 13]. Moreover, even with the nice function in (5), i.e., \( F(x, \mathbf{r}) = q_k - \sum_{n=1}^{N} x_{k,n} \lambda_{k,n}^{(f)} \) is bilinear in \( x \) and \( \mathbf{r} \), with independent entries \( r_{k,n} \) in \( \mathbf{r} \) whose distribution is known, it is still unclear how to compute the probability in (5) efficiently.

To circumvent the above hurdles, we propose the following formulation \( P_{\text{skw}} \) by replacing the chance constraints (5) with a system of constraints \( \mathcal{H} \) such that (i) \( x \) is feasible for (5) whenever it is feasible for \( \mathcal{H} \), and (ii) the constraints in \( \mathcal{H} \) are convex and efficiently computable. The new formulation is given as follows:

\[
P_{\text{skw}} : \max_{x_{k,n}} \sum_{k=1}^{K} \sum_{n=1}^{N} x_{k,n} \mathbb{E}\left\{ r_{k,n}^{(f)} \right\}
\]

s.t. \( \inf_{\theta > 0} \left\{ q_k + \theta \sum_{n=1}^{N} \Lambda_k(-\log x_{k,n}) - \theta \log \epsilon_k \right\} \leq 0, \quad \forall k \) (7)

\[
\sum_{k=1}^{K} x_{k,n} \leq 1, \quad \forall n \quad \text{(8)}
\]

\[
x_{k,n} \geq 0, \quad \forall k, n \quad \text{(9)}
\]

where \( \Lambda_k(\cdot) \) is the cumulative generating function of \( r_{k,n}^{(f)} \), and

\[
\Lambda_k(-\log x_{k,n}) = \log \left[ \int_0^{\infty} \left( 1 + \frac{p k}{\Gamma N_0} \right)^{-\frac{\xi}{\sigma_k}} \frac{1}{\sigma_k} \exp\left( -\frac{\xi}{\sigma_k} \right) d\xi \right]. \quad \text{(10)}
\]

In the following, we first prove that any solution \( x \) that is feasible for the STC (7) in \( P_{\text{skw}} \) is also feasible for the chance constraints (5). Then, we prove that \( P_{\text{skw}} \) is convex.

Proposition 1: Suppose that \( q_{k,n}^{(f)} \) and hence \( r_{k,n}^{(f)} \) are independent random variables for different \( n \) and \( k \), where the PDF of \( q_{k,n}^{(f)} \) follows (1). Furthermore, given \( \epsilon_k > 0 \), suppose that there exists an \( \hat{x} = [\hat{x}_{1,1}, \cdots, \hat{x}_{N,1}, \cdots, \hat{x}_{1,K}, \cdots, \hat{x}_{N,K}]^T \in \mathbb{R}^{NK} \) such that

\[
G_k(\hat{x}) \triangleq \inf_{\theta > 0} \left\{ q_k + \theta \sum_{n=1}^{N} \Lambda_k(-\log x_{k,n}) - \theta \log \epsilon_k \right\} \leq 0, \quad \forall k.
\]

Then, the allocation decision \( \hat{x} \) satisfies

\[
\Pr\left\{ \sum_{n=1}^{N} \hat{x}_{k,n} r_{k,n}^{(f)} \geq q_k \right\} \geq 1 - \epsilon_k, \quad \forall k. \quad \text{(12)}
\]

Proof: Our argument will use the Bernstein approximation theorem proposed in [13]. Suppose there exists an \( \hat{x} \in \mathbb{R}^{NK} \) such that \( G_k(\hat{x}) \leq 0, \) i.e.,

\[
\inf_{\theta > 0} \left\{ q_k + \theta \sum_{n=1}^{N} \Lambda_k(-\log x_{k,n}) - \theta \log \epsilon_k \right\} \leq 0. \quad \text{(13)}
\]

The function inside the \( \inf_{\theta > 0} \) is equal to

\[
q_k + \theta \sum_{n=1}^{N} \log \mathbb{E}\left\{ \exp\left( -\log x_{k,n} r_{k,n}^{(f)} \right) \right\} - \theta \log \epsilon_k
\]

\[
= q_k + \theta \log \mathbb{E}\left\{ \exp\left( \left( -\sum_{n=1}^{N} \hat{x}_{k,n} r_{k,n}^{(f)} \right) \right) \right\} - \theta \log \epsilon_k
\]

\[
= \log \mathbb{E}\left\{ \exp\left( \left( q_k - \sum_{n=1}^{N} \hat{x}_{k,n} r_{k,n}^{(f)} \right) \right) \right\} - \theta \log \epsilon_k
\]

\[
= - \theta \log \epsilon_k
\]

where the expectation \( \mathbb{E}\{\cdot\} \) can be computed using the distributional information of \( q_{k,n}^{(f)} \) in (1), and (15) follows from the independence of random variable \( r_{k,n}^{(f)} \) over \( n \).

Let \( F_k(x, \mathbf{r}) = q_k - \sum_{n=1}^{N} x_{k,n} r_{k,n}^{(f)} \). Then, (13) is equivalent to

\[
\inf_{\theta > 0} \left\{ \theta \log \left\{ \mathbb{E}\left\{ \exp\left( -\log F_k(x, \mathbf{r}) \right) \right\} \right\} - \theta \log \epsilon_k \right\} \leq 0. \quad \text{(17)}
\]

According to Theorem 2 in Appendix A, the chance constraints (12) hold if there exists a \( \theta > 0 \) satisfying (17). Thus, the validity of (12) is guaranteed by the validity of (11).

Now, we prove the convexity of (7) in the following proposition.

Proposition 2: The constraints imposed in (7) are convex in \( x = [x_{1,1}, \cdots, x_{N,1}, \cdots, x_{1,K}, \cdots, x_{N,K}]^T \in \mathbb{R}^{NK} \).

Proof: The convexity of (7) can be verified as follows. We define the function inside the \( \inf_{\theta > 0} \) in (11) as

\[
H_k(x, \theta) \triangleq q_k + \theta \sum_{n=1}^{N} \Lambda_k(-\log x_{k,n}) - \theta \log \epsilon_k, \quad \forall k. \quad \text{(18)}
\]

It is easy to verify the convexity of \( H_k(x, \theta) \) in \( (x, \theta) \), since the cumulant generating function is convex. Hence, \( G_k(\hat{x}) \) in (11) is convex in \( x \) due to the preservation of convexity by minimization over \( \theta > 0 \).
the barrier function in path-following algorithms or providing the (sub-)gradient in primal-dual methods (see [14] for details of these algorithms). Fortunately, we can employ interior point cutting plane methods to solve Problem $\hat{\mathcal{P}}_{\text{skw}}$ (see [15] for a survey). Before we delve into the details, let us briefly sketch the principles of the algorithm as follows.

**Algorithm 1 Structure of the Proposed Algorithm**

**Require:** The feasible solution set of Problem $\hat{\mathcal{P}}_{\text{skw}}$ is a compact set $\mathcal{X}$ defined by (7)–(9).

1: Construct a polytope $X^0 \supset \mathcal{X}$ by (8) and (9). Set $i \leftarrow 0$.

2: Choose a query point (Section IV-A-1) at the $i$th iteration as $x^i$ by computing the analytic center of $X^i$. Initially, set $x^0 = e/K \in X^0$ where $e$ is an $N$-vector of ones.

3: Query the separation oracle (Section IV-A-2) with $x^i$:

4: if $x^i \in \mathcal{X}$ then

5: generate a hyperplane (optimality cut) through $x^i$ to remove the part of $X^i$ that has lower objective values.

6: else

7: generate a hyperplane (feasibility cut) through $x^i$ to remove the part of $X^i$ that contains infeasible solutions.

8: end if

9: Set $i \leftarrow i + 1$, and update $X^{i+1}$ by the separation hyperplane.

10: if termination criterion (Section IV-B) is satisfied then

11: stop.

12: else

13: return to step 2.

14: end if

Suppose that we would like to find a point $x$ that is feasible for (7)–(9) and is within a distance of $\delta > 0$ to an optimal solution $x^*$ of $\hat{\mathcal{P}}_{\text{skw}}$, where $\delta > 0$ is an error tolerance parameter (i.e., $x$ satisfies $\|x - x^*\|_2 < \delta$). We maintain the invariant that at the beginning of each iteration, the feasible set is contained in some polytope (i.e., a bounded polyhedron). Then, we generate a query point inside the polytope and ask a “separation oracle” whether the query point belongs to the feasible set. If not, then the separation oracle will generate a so-called separating hyperplane through the query point to cut out the polytope, so that the remaining polytope contains the feasible set. Otherwise, the separation oracle will return a hyperplane through the query point to cut out the polytope towards the opposite direction of improving objective values.

We can then proceed to the next iteration with the new polytope. To keep track of the progress, we can use the so-called potential value of the polytope. Roughly speaking, when the potential value becomes large, the polytope containing the feasible set has become small. Thus, if the potential value exceeds a certain threshold, we can terminate the algorithm. As will be shown later, such an algorithm will in fact terminate in a polynomial number of steps.

We now give the structure of the algorithm. A detailed flow chart is shown in Fig. 2 for readers’ interest.

**A. Cutting-Plane-Based Algorithm**

1) **Query Point Generator:** (Step 2 in Algorithm 1): In each iteration, we need to generate a query point inside the polytope $X^i$. For algorithmic efficiency, we adopt the analytic center (AC) of the containing polytope as the query point [17]. The AC of the polytope $X^i = \{ x \in \mathbb{R}^{NK} : A_i x \leq b^i \}$ at the $i$th iteration is the unique solution $x^i$ to the following convex problem:

$$\max_{\{x, s^i\}} \sum_{m=1}^{M^i} \log s^i_m$$

$$s^i \cdot s^i = b^i - A_i x^i.$$  \hspace{1cm} (19)

We define the optimal value of the above problem as the potential value of the polytope $X^i$. Note that the uniqueness of
the analytic center is guaranteed by the strong convexity of the potential function $\mathbf{s}^i \rightarrow -\sum_{m=1}^{M_i} \log s^i_m$, assuming that $X^i$ is bounded and has a nonempty interior. The AC of a polytope can be viewed as an approximation to the geometric center of the polytope, and thus any hyperplane through the AC will separate the polytope into two parts with roughly the same volume.

Although it is computationally involved to directly solve (19) in each iteration, it is shown in [18] that an approximate AC is sufficient for our purposes, and that an approximate AC for the $(i + 1)^{st}$ iteration can be obtained from an approximate AC for the $i^{th}$ iteration by applying $O(1)$ Newton steps.

2) Separation Oracle: (Steps 3–8 in Algorithm 1): The oracle is a major component of the algorithm that plays two roles: checking the feasibility of the query point, and generating cutting planes to cut the current set.

- Feasibility Check

We write the constraints of $\hat{P}_{\text{skew}}$ in a condensed form as follows:

$$G_k(x) = \inf_{\varrho \geq 0} \left\{ H_k(x, \varrho) \right\} \leq 0, \quad \forall k$$

$$A^0 x \leq b^0$$

where

$$A^0 = \begin{bmatrix} I_N & I_N & \ldots & I_N \\ -I_{NK} \end{bmatrix} \in \mathbb{R}^{(N+NK) \times NK}$$

$$b^0 = \begin{bmatrix} e_N^T \\ 0_{NK}^T \end{bmatrix} \in \mathbb{R}^{N+NK}$$

with $I_N$ and $e_N$ denoting the $N \times N$ identity matrix and $N$-vector of ones respectively, and (21) is the combination of (8) and (9). Now, we first use (21) to construct a relaxed feasible set via

$$X^0 = \{ x \in \mathbb{R}^{NK} : A^0 x \leq b^0 \}. \quad (22)$$

Given a query point $x \in X^0$, we can verify its feasibility to $\hat{P}_{\text{skew}}$ by checking if it satisfies (20), i.e., if $\inf_{\varrho \geq 0} \left\{ H_k(x, \varrho) \right\}$ is no larger than 0. This requires solving a minimization problem over $\varrho > 0$. Due to the unimodality of $H_k(x, \varrho)$, we can simply take a line search procedure, e.g., using Golden-section search or Fibonacci search, to find the minimizer $\varrho^*$. The line search is more efficient when compared with derivative-based algorithms, since only function evaluations are needed during the search.

- Cutting Plane Generation

In each iteration, we generate a cutting plane, i.e., a hyperplane through the query point, and add it as an additional constraint to the current polytope $X^i$. By adding cutting plane(s) in each iteration, the size of the polytope keeps shrinking. There are two types of cutting planes in the algorithm depending on the feasibility of the query point.

If the query point $x^i \in X^i$ is infeasible, then a hyperplane called feasibility cut is generated at $x^i$ as follows:

$$\left( \frac{u^{i, R}}{\|u^{i, R}\|} \right)^T (x - x^i) \leq 0, \quad \forall \varrho \in \mathbb{R}^K \quad (23)$$

where $\| \cdot \|$ is the Euclidean norm, $\mathbb{R}^K = \{ k : H_k(x^i, \varrho^i) > 0, \varrho^i = 1, 2, \ldots, K \}$ is the set of users whose chance constraints are violated, and $u^{i, R} = [u^{i, R}_1, \ldots, u^{i, R}_N, \ldots, u^{i, R}_1, \ldots, u^{i, R}_N, \ldots, u^{i, R}_N]^T \in \mathbb{R}^{NK}$ is the gradient of $G_R(x)$ with respect to $x$; see the equation shown at the bottom of the page. The reason we call (23) a feasibility cut(s) is that any $x$ which does not satisfy (23) must be infeasible and can hence be dropped.

If the point $x^i$ is feasible, then an optimality cut is generated as follows:

$$\left( \frac{v}{\|v\|} \right)^T (x - x^i) \leq 0 \quad (24)$$

The cumulant generating function $\Lambda_k(\cdot)$ in (10) can be evaluated numerically, e.g., using rectangular rule, trapezoid rule, or Simpson’s rule, etc.
Here, \( A^i \) and \( b^i \) are obtained by adding the cutting plane to the previous polytope \( X^{i-1} \). Specifically, if the oracle provides a feasibility cut as in (23), then
\[
A^i = \begin{bmatrix} A^{i-1} \\ (u_k^i / ||u_k^i||) T \end{bmatrix} \in \mathbb{R}^{(M^{i-1}+|K|) \times NK}
\]
\[
b^i = \begin{bmatrix} b^{i-1} \\ (u_k^i / ||u_k^i||) T x^i \end{bmatrix} \in \mathbb{R}^{M^{i-1}+|K|}
\]
where \( M_{i-1} \) is the number of rows in \( A_{i-1} \), and \(| \cdot |\) is the number of elements contained in the given set; if the oracle provides an optimality cut as in (24), then
\[
A^i = \begin{bmatrix} A^{i-1} \\ (v/||v||) T \end{bmatrix} \in \mathbb{R}^{(M^{i-1}+1) \times NK}
\]
\[
b^i = \begin{bmatrix} b^{i-1} \\ (v/||v||) T x^i \end{bmatrix} \in \mathbb{R}^{M^{i-1}+1}.
\]

B. Global Convergence & Complexity (Step 10 in Algorithm 1)

In the following, we investigate the convergence properties of the proposed algorithm. As mentioned earlier, when the polytope is too small to contain a full-dimensional closed ball of radius \( \delta > 0 \), the potential value will exceed a certain threshold. Then, the algorithm can terminate since the query point is within a distance of \( \delta > 0 \) to some optimal solution of \( \mathcal{P}_{\text{slow}} \). Such an idea is formalized in [18], where it was shown that the analytic center-based cutting plane method can be used to solve convex programming problems in polynomial time. Upon following the proof in [18], we obtain the following result:

Theorem 1: (cf. [18]) Let \( \delta > 0 \) be the error tolerance parameter, and let \( m \) be the number of variables. Then, Algorithm 1 terminates with a solution \( x \) that is feasible for \( \mathcal{P}_{\text{slow}} \) and satisfies \( ||x - x^*||_2 < \delta \) for some optimal solution \( x^* \) to \( \mathcal{P}_{\text{slow}} \) after at most \( O(m/\delta^2) \) iterations.

Thus, the proposed algorithm can solve Problem \( \mathcal{P}_{\text{slow}} \) within \( O((NK/\delta^2)) \) iterations. It turns out that the algorithm can be made considerably more efficient by dropping constraints that are deemed “unimportant” [19]. By incorporating such a strategy in Algorithm 1, the total number of iterations needed by the algorithm can be reduced to \( O(K\log^2(1/\delta)) \). We refer the readers to [15] and [19] for details.

C. Complexity Comparison Between Slow and Fast Adaptive OFDMA

It is interesting to compare the complexity of slow and fast adaptive OFDMA schemes formulated in \( \mathcal{P}_{\text{slow}} \) and \( \mathcal{P}_{\text{fast}} \), respectively. To obtain an optimal solution to \( \mathcal{P}_{\text{fast}} \), we need to solve a linear program (LP). This requires \( O(\sqrt{NK}L_0) \) iterations, where \( L_0 \) is number of bits to store the data defining the LP [20]. At first glance, the iteration complexity of solving a fast adaptation \( \mathcal{P}_{\text{fast}} \) can be lower than that of solving \( \mathcal{P}_{\text{slow}} \), when the number of users or subcarriers are large. However, it should be noted that only one \( \mathcal{P}_{\text{slow}} \) needs to be solved for each adaptation window, while \( \mathcal{P}_{\text{fast}} \) has to be solved for each time slot. Since the length of adaptation window is equal to \( T \) time slots, the overall complexity of the slow adaptive OFDMA can be much lower than that of conventional fast adaptation schemes, especially when \( T \) is large.

Before leaving this section, we emphasize that the advantage of slow adaptive OFDMA lies not only in computational cost reduction, but also in reducing control signaling overhead. We will investigate this in more detail in Section VI.

V. PROBLEM SIZE REDUCTION

In this section, we show that the problem size of \( \mathcal{P}_{\text{slow}} \) can be reduced from \( NK \) variables to \( K \) variables under some mild assumptions. Consequently, the computational complexity of slow adaptive OFDMA can be markedly lower than that of fast adaptive OFDMA.

In practical multicarrier systems, the frequency intervals between any two subcarriers are much smaller than the carrier frequency. The reflection, refraction and diffusion of electromagnetic waves behave the same across the subcarriers. This implies that the channel gain \( g_{k,n}^{(t)} \) are identically distributed over \( n \) (subcarriers), although this observation is not needed in our algorithm derivations in the previous sections.

When \( g_{k,n}^{(t)} \) for different \( n \) are identically distributed, different subcarriers become indistinguishable to a user \( k \). In this case, the optimal solution, if exists, does not depend on \( n \). Replacing \( x_{k,n} \) by \( x_k \) in \( \mathcal{P}_{\text{slow}} \), we obtain the following formulation:

\[
\begin{align*}
\mathcal{P}_{\text{slow}}': \quad & \max_k \sum_{n=1}^{N} x_k \mathbb{E}\{ r_k^{(t)} \} \\
\text{s.t.} & \quad \inf_{\epsilon > 0} \{ \epsilon_k + \epsilon N A_k (\theta^{-1} x_k) - \epsilon \log \epsilon_k \} \leq 0, \forall k \\
& \quad \sum_{k=1}^{K} x_k \leq 1 \\
& \quad x_k \geq 0, \forall k.
\end{align*}
\]

Note that the problem structure of \( \mathcal{P}_{\text{slow}}' \) is exactly the same as that of \( \mathcal{P}_{\text{slow}} \), except that the problem size is reduced from \( NK \) variables to \( K \) variables. Hence, the algorithm developed in Section IV can also be applied to solve \( \mathcal{P}_{\text{slow}}' \) with the following vector/matrix size reductions:

\[
A^0 = [e_N, -I_K] T \in \mathbb{R}^{(1+K) \times NK}, \quad b^0 = [1, 0, \ldots, 0] T \in \mathbb{R}^{1+K}
\]

in (21),

\[
\begin{bmatrix} u_1^T \\
\vdots \\
u_K^T \end{bmatrix} \in \mathbb{R}^{K \times (1+K)}
\]

and

\[
\mathbf{v} = [-e^{T} r_k^{(t)} \ldots, -e^{T} r_K^{(t)}] \in \mathbb{R}^{K \times (1+K)}
\]

in (24). Compared with \( \mathcal{P}_{\text{slow}} \), the iteration complexity of \( \mathcal{P}_{\text{slow}}' \) is now reduced to \( O(K\log^2(1/\delta)) \). Indeed, this can even be lower than the complexity of solving one \( \mathcal{P}_{\text{fast}} - O(\sqrt{NK}L_0) \), since \( K \) is typically much smaller than \( N \) in real systems. Thus, the overall complexity of slow adaptive OFDMA is significantly lower than that of fast adaptation over \( T \) time slots.

VI. SIMULATION RESULTS

In this section, we demonstrate the performance of our proposed slow adaptive OFDMA scheme through numerical simulations. We simulate an OFDMA system with four users and 64 subcarriers. Each user \( k \) has a requirement on its short-term
data rate $q_k = 20$ bps. The four users are assumed to be uniformly distributed in a cell of radius $R = 100$ m. That is, the distance $d_k$ between user $k$ and the BS follows the distribution $f(d) = 2d/R^2$. The path-loss exponent $\gamma$ is equal to 4, and the shadowing effect $s_k$ follows a log-normal distribution, i.e., $10\log_{10}(s_k) \sim \mathcal{N}(0, 8 \text{ dB})$. The small-scale channel fading is assumed to be Rayleigh distributed. Suppose that the transmission power of the BS on each subcarrier is 90 dB measured at a reference point 1 meter away from the BS, which leads to an average received power of 10 dB at the boundary of the cell. In addition, we set $W = 1$ Hz and $N_0 = 1$, and the capacity gap is $\Gamma = -\log(5 \text{ BER})/1.5 = 5.0673$, where the target BER is set to be $10^{-4}$. Moreover, the length of one slot, within which the channel gain remains unchanged, is $T_0 = 1$ ms. The length of the adaptation window is chosen to be $T = 1$ s, implying that each window contains 1000 slots. Suppose that the path loss and shadowing do not change within a window, but varies independently from one window to another. For each window, we solve the size-reduced problem $\overline{P}^\text{skw}$, and later Monte-Carlo simulation is conducted over 61 independent windows that yield nonempty feasible sets of $\overline{P}^\text{skw}$ when $\epsilon_k = 0.1$.

In Figs. 3 and 4, we investigate the fast convergence of the proposed algorithm. The error tolerance parameter is chosen as $\delta = 10^{-2}$. In Fig. 3, we record the trace of one adaptation window and plot the improvement in the objective function value (i.e., system throughput) in each iteration, i.e., $\Delta\overline{b} = \overline{b}^i - \overline{b}^{i-1}$. When $\Delta\overline{b}$ is positive, the objective value increases with each iteration. It can be seen that $\Delta\overline{b}$ quickly converges to close to zero within only 27 iterations. We also notice that fluctuation exists in $\Delta\overline{b}$ within the first 11 iterations. This is mainly because during the search for an optimal solution, it is possible for query points to become infeasible. However, the feasibility cuts (23) then adopted will make sure that the query points in subsequent iterations will eventually become feasible. The curve in Fig. 3 verifies the tendency. As $\overline{P}^\text{skw}$ is convex, this observation implies that the proposed algorithm can converge to an optimal solution of $\overline{P}^\text{skw}$ within a small number of iterations. In Fig. 4, we plot the number of iterations needed for convergence for different application windows. The result shows that the proposed algorithm can in general converge to an optimal solution of $\overline{P}^\text{skw}$ within 35 iterations. On average, the algorithm converges after 22 iterations, where each iteration takes 1.467 s.

Moreover, we plot the number of iterations needed for checking the feasibility of $\overline{P}^\text{skw}$. In Fig. 5, we conduct a simulation over 100 windows, which consists of 61 feasible windows (dots with cross) and 39 infeasible windows (dots with circle). On average, the algorithm can determine if $\overline{P}^\text{skw}$

---

10 The distribution of user’s distance from the BS $f(d) = 2d/R^2$ is derived from the uniform distribution of user’s position $f(x, y) = 1/\pi R^2$, where $(x, y)$ is the Cartesian coordinate of the position.

11 The average received power at the boundary is calculated by $90 \text{ dB} + 10 \log_{10}(100/1) = 10 \text{ dB}$ due to the path-loss effect.

12 The coherence time is given by $T_0 = 9c/16\pi f_c v$, where $c$ is the speed of light, $f_c$ is the carrier frequency, and $v$ is the velocity of mobile user. As an example, we choose $f_c = 2.5$ GHz, and if the user is moving at 45 miles per hour, the coherence time is around 1 ms.

13 The simulation results show that all the feasible windows appear with similar convergence behavior.

14 We conduct a simulation on Matlab 7.0.1, where the system configurations are given as: Processor: Intel(R) Core(TM)2 CPU P8400@2.26 GHz 2.27 GHz, Memory: 2.00 GB, System Type: 32-bit Operating System.
Fig. 6. Comparison of system spectral efficiency between fast adaptive OFDMA and slow adaptive OFDMA.

Fig. 7. Outage probability of the four users over 61 independent feasible windows.

that within each window that contains 1000 slots, the control signaling has to be transmitted 1000 times in the fast adaptation scheme, but once in the slow adaptation scheme. In Fig. 6, the line with circles represents the performance of the fast adaptive OFDMA scheme, while that with dots corresponds to the slow adaptive OFDMA. The figure shows that although slow adaptive OFDMA updates subcarrier allocation 1000 times less frequently than fast adaptive OFDMA, it can achieve on average 71.88% of the spectral efficiency. Considering the substantially lower computational complexity and signaling overhead, slow adaptive OFDMA holds significant promise for deployment in real-world systems.

As mentioned earlier, is more conservative than the original problem , implying that the outage probability is guaranteed to be satisfied if subcarriers are allocated according to the optimal solution of . This is illustrated in Fig. 7, which shows that the outage probability is always lower than the desired threshold .

Fig. 7 shows that the subcarrier allocation via could still be quite conservative, as the actual outage probability is much lower than . One way to tackle the problem is to set to be larger than the actual desired value. For example, we could tune from 0.1 to 0.3. By doing so, one can potentially increase the system spectral efficiency, as the feasible set of is enlarged. A question that immediately arises is how to choose the right , so that the actual outage probability stays right below the desired value. Towards that end, we can perform a binary search on to find the best parameter that satisfies the requirement. Such a search, however, inevitably involves high computational costs. On the other hand, Fig. 8 shows that the gain in spectral efficiency by increasing is marginal. The gain is as little as 0.5 bps/Hz/subcarrier when is increased drastically from 0.05 to 0.7. Hence, in practice, we can simply set to the desired outage probability value to guarantee the QoS requirement of users.

In the development of the STC (7), we considered that the channel gain are independent for different ’s and ’s.
While it is true that channel fading is independent across different users, it is typically correlated in the frequency domain. We investigate the effect of channel correlation in frequency domain through simulations. A wireless channel with an exponential decaying power profile is adopted, where the root-mean-square delay is equal to 37.79 ns. For comparison, the curves of outage probability with and without frequency correlation are both plotted in Fig. 9. We choose the tolerance parameter to be \( \epsilon_k = 0.3 \). The figure shows that with frequency-domain correlation, the outage probability requirement of 0.3 is violated occasionally. Intuitively, such a problem becomes negligible when the channel is highly frequency selective, and is more severe when the channel is more frequency flat. To address the problem, we can set \( \epsilon_k \) to be lower than the desired outage probability value.\(^\text{16}\) For example, when we choose \( \epsilon_k = 0.1 \) in Fig. 9, the outage probabilities all decreased to lower than the desired value 0.3, and hence the QoS requirement is satisfied (see the line with dots).

**VII. CONCLUSION**

This paper proposed a slow adaptive OFDMA scheme that can achieve a throughput close to that of fast adaptive OFDMA schemes, while significantly reducing the computational complexity and control signaling overhead. Our scheme can satisfy user data rate requirement with high probability. This is achieved by formulating our problem as a stochastic optimization problem. Based on this formulation, we design a polynomial-time algorithm for subcarrier allocation in slow adaptive OFDMA. Our simulation results showed that the proposed algorithm converges within 22 iterations on average.

In the future, it would be interesting to investigate the chance constrained subcarrier allocation problem when frequency correlation exists, or when the channel distribution information is not perfectly known at the BS. Moreover, it is worthy to study the tightness of the Bernstein approximation. Another interesting direction is to consider discrete data rate and exclusive subcarrier allocation. In fact, the proposed algorithm based on cutting plane methods can be extended to incorporate integer constraints on the variables (see, e.g., [15]).

Finally, our work is an initial attempt to apply the chance constrained programming methodology to wireless system designs. As probabilistic constraints arise quite naturally in many wireless communication systems due to the randomness in channel conditions, user locations, etc., we expect that chance constrained programming will find further applications in the design of high performance wireless systems.

**APPENDIX A**

**BERNSTEIN APPROXIMATION THEOREM**

*Theorem 2*: Suppose that \( F(x, r) : \mathbb{R}^n \times \mathbb{R}^m \to \mathbb{R} \) is a function of \( x \in \mathbb{R}^n \) and \( r \in \mathbb{R}^m \), and \( r \) is a random vector whose components are nonnegative. For every \( \epsilon > 0 \), if there exists an \( x \in \mathbb{R}^n \) such that

\[
\inf_{\varrho > 0} \{ \Psi(x, \varrho) - \varrho \epsilon \} \leq 0 \tag{25}
\]

then \( \Pr \{ F(x, r) > 0 \} \leq \epsilon \).

*Proof: (Sketch)* The proof of the above theorem is given in [13] in details. To help the readers to better understand the idea, we give an overview of the proof here.

It is shown in [13] (see section 2.2 therein) that the probability \( \Pr \{ F(x, r) \geq 0 \} \) can be bounded as follows:

\[
\Pr \{ F(x, r) > 0 \} \leq \mathbb{E} \{ \psi(\varrho^{-1} F(x, r)) \}.
\]

Here, \( \varrho > 0 \) is arbitrary, and \( \psi(\cdot) : \mathbb{R} \to \mathbb{R} \) is a nonnegative, nondecreasing, convex function satisfying \( \psi(0) = 1 \) and \( \psi(z) > \psi(0) \) for any \( z > 0 \). One such \( \psi \) is the exponential function \( \psi(z) = \exp(z) \). If there exists a \( \hat{\varrho} > 0 \) such that

\[
\mathbb{E} \{ \exp(\hat{\varrho}^{-1} F(x, r)) \} \leq \epsilon
\]

then \( \Pr \{ F(x, r) > 0 \} \leq \epsilon \). By multiplying by \( \hat{\varrho} > 0 \) on both sides, we obtain the following sufficient condition for the chance constraint \( \Pr \{ F(x, r) > 0 \} \leq \epsilon \) to hold:

\[
\Psi(x, \hat{\varrho}) - \hat{\varrho} \epsilon \leq 0, \tag{26}
\]

\(^{16}\)Alternatively, we can divide \( N \) subcarriers into \( N/N_c \) subchannels (each subchannel consists \( N_c \) subcarriers), and represent each subchannel via an average gain. By doing so, we can treat the subchannel gains as being independent of each other.
In fact, condition (26) is equivalent to (25). Thus, the latter provides a conservative approximation of the chance constraint.

REFERENCES


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