**Dynamic Controllability of Temporally-flexible Reactive Programs**

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Dynamic Controllability of Temporally-flexible Reactive Programs

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Abstract
In this paper we extend dynamic controllability of temporally-flexible plans to temporally-flexible reactive programs. We consider three reactive programming language constructs whose behavior depends on runtime observations; conditional execution, iteration, and exception handling. Temporally-flexible reactive programs are distinguished from temporally-flexible plans in that program execution is conditioned on the runtime state of the world. In addition, exceptions are thrown and caught at runtime in response to violated timing constraints, and handled exceptions are considered successful program executions.

Dynamic controllability corresponds to a guarantee that a program will execute to completion, despite runtime constraint violations and uncertainty in runtime state. An algorithm is developed which frames the dynamic controllability problem as an AND/OR search tree over possible program executions. A key advantage of this approach is the ability to enumerate only a subset of possible program executions that guarantees dynamic controllability, framed as an AND/OR solution subtree.

Introduction
In the field of AI planning, temporal reasoning plays a central role. Many planning applications involve complex temporal relationships that must be satisfied for a plan to succeed. In order to be robust to uncertainty, many of these applications require flexibility in the timing of actions, both at planning and execution time. To achieve this robustness, the planning community has developed a family of constraint formalisms to model and reason efficiently over large networks of flexible temporal constraints. Such formalisms include; the temporal constraint network (TCN) (Dechter, Meiri, and Pearl 1991), the disjunctive temporal problem (DTP) (Stergiou and Koubarakis 1998), the temporal plan network (TPN) (Kim, Williams, and Abrahmson 2001), the simple temporal problem under uncertainty (STPU) (Vidal and Fargier 1999), and the conditional temporal problem (CTP) (Tsamardinos, Vidal and Pollack 2003). The CTP formalism is distinguished in that it supports both flexible temporal constraints and runtime observations. A host of temporal reasoning algorithms and complexity results have been developed along with these temporal formalisms, such as (Stergiou and Koubarakis 2001) and (Morris, Muscettola, and Vidal 2001). Central to these algorithms is the notion of controllability. Although the terminology differs between formalisms, the central question asked by each is: “Does an execution strategy exist in which the specified timing constraints are guaranteed to be satisfied?” The answer to this question may vary based on the information available to the plan’s executive at runtime. This distinction has guided the community towards defining three separate notions of controllability: weak, strong, and dynamic controllability. Strong controllability requires no information at runtime in order to succeed, weak controllability requires all information ahead of time, and dynamic controllability requires information only as it becomes available.

In this paper, we extend dynamic controllability to temporally-flexible reactive programs with three reactive programming language constructs; conditional execution, iteration, and exception handling. The proposed language is an extension of the Reactive Model-based Programming Language (RMPL) (Williams, et. al. 2003) and is interpreted graphically as a Temporal Plan Network. RMPL also supports; simple temporal constraints, parallel and sequential composition, and non-deterministic choice. We choose to view the dynamic controllability problem as a two-player game between the executive and the environment. The executive picks times for controllable timepoints and makes choices for controllable choice points. Alternatively, the environment picks times for uncontrollable timepoints and makes choices for uncontrollable choice points. The executive is allowed to observe the outcome of uncontrollable timepoints and choice points as they occur, and then use that information to dynamically schedule future controllable timepoints and
choice points in order to guarantee successful program execution. An algorithm is developed which frames the dynamic controllability problem as an AND/OR search tree (Dechter and Mateescu 2007) over possible program executions.

Next we give a simple example of a temporally-flexible reactive program, and we review some necessary background material. Then, we define temporally-flexible reactive programs, and develop an algorithm for determining dynamic controllability. We conclude with a summary and discussion of the experimental results.

A Simple Example
Consider a whole-arm manipulator (WAM) pick-and-place task, depicted in Figure 1. The WAM moves to waypoint W1 (to its left), then down to the ground to grasp an object. After grasping the object, the WAM moves back to W1, travels through W2, and onto W3. Then, the WAM lowers to the ground to release the object. The portion of the task in-which the arm moves from W1 through W2 to W3 is encoded in RMPL in Figure 1. This example demonstrates the use of reactive language constructs to improve plan flexibility and robustness in achieving a goal; “to be at W3”. Each “go” activity has a flexible timing constraint and a flexible operating region (depicted at the top right of Figure 1) which it should not leave. If an obstacle is observed between W1 and W2, the program specifies an alternate route through W2north. If the WAM is displaced from its operating region, a contingency is invoked; the WAM returns to the home position. The until construct is used to attempt the task two times before giving up and remaining at the home position. For example, consider the plot at the bottom right of Figure 1. The WAM was physically disturbed from its operating region several times between W1 and W3. The trajectory taken by the WAM each time to return to the home position is plotted. Dynamic controllability in this example corresponds to a guarantee that the WAM will end up either at the goal, W3, or at a safe contingency location, the home position, within 40 seconds (i.e. with no uncaught exceptions).

Consistency for STPs, DTPs, and TPNs
The simple temporal problem (STP), the disjunctive temporal problem (DTP), and the temporal plan network (TPN) are all graphical models for analyzing temporally flexible networks of activities. In each model, a graph is constructed which consists of nodes and edges, \((v,e)\). Nodes represent instantaneous timepoints (real-valued variables), while edges represent timing constraints between nodes. An example of each is shown in Figure 2. In an STP, each edge from node \(i\) to node \(j\) is labeled with an interval, \([lb,ub]\), which represents a metric timing constraint, \(lb \leq X_i - X_j \leq ub\). DTPs and TPNs generalize STPs by allowing disjunctions between timing constraints.

The DTP and TPN differ from one another slightly; the DTP can be mapped into a meta-CSP while the TPN can be mapped into a meta-Conditional CSP as demonstrated in (Tsamardinos and Pollack 2003) and (Effinger 2006).

Weak, Strong, Dynamic Controllability for STPU
In many applications, activity durations are not under the control of the executing agent and instead depend on external factors. To address this issue, the Simple Temporal Problem with Uncertainty (STPU) was developed. STPUs are similar to STPs except that edges are divided into *controllable* and *uncontrollable* edges (Vidal and Fargier 1999). The uncontrollable edges represent activities of uncertain duration, whose finish timepoints are controlled by nature, termed *uncontrollable*...
timepoints. All other timepoints are controllable timepoints, which are freely controllable by the executive.

The definition of consistency for an STP needs to be extended for an STPU because the executive does not get to pick the times of execution for uncontrollable timepoints. Instead, an execution strategy is needed for assigning times to just the controllable timepoints such that all constraints are satisfied regardless of the values taken by the uncontrollable timepoints. Several such execution strategies exist, and they are classified in Figure 3, based on the information available to the agent at runtime.

<table>
<thead>
<tr>
<th>STNU Controllability</th>
<th>Description</th>
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<tbody>
<tr>
<td>Weak Controllability</td>
<td>An execution strategy that is guaranteed to succeed for only one set of values taken by the uncontrollable timepoints at runtime. This strategy assumes that uncontrollable durations are known or can be predicted a-priori.</td>
</tr>
<tr>
<td>Strong Controllability</td>
<td>A static execution strategy that is guaranteed to succeed for all possible sets of values taken by the uncontrollable timepoints at runtime. This strategy doesn’t need any knowledge at runtime to succeed.</td>
</tr>
<tr>
<td>Dynamic Controllability</td>
<td>A dynamic execution strategy that is guaranteed to succeed for all possible sets of values taken by the uncontrollable timepoints at runtime. This strategy relies on knowledge acquired at runtime in order to dynamically schedule future timepoints in order to satisfy all timing constraints. Hence, this strategy needs access to all runtime information as it becomes available.</td>
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Figure 3: STNU Controllability Classifications

**Weak, Strong, Dynamic Consistency for CTP**

The Conditional Temporal Problem (CTP) (Tsamardinos, Vidal, and Pollack 2003) augments the STP and DTP formalisms with observation nodes. Observation nodes have outgoing edges with labels attached that are associated with runtime observations. The CTP formalism allows for the analysis of plans with conditional threads of execution and flexible temporal constraints. Similarly to the STNU, in Figure 4, three notions of consistency are defined for the CTP: weak, strong, and dynamic consistency. The term consistency is used instead of controllability because all CTP timepoints are controllable.

<table>
<thead>
<tr>
<th>CTP Consistency</th>
<th>Description</th>
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<tbody>
<tr>
<td>Weak Consistency</td>
<td>An execution strategy that is guaranteed to succeed for only one set of observations that may occur at runtime. This strategy assumes that all observations can be predicted or are known a-priori.</td>
</tr>
<tr>
<td>Strong Consistency</td>
<td>A static execution strategy that is guaranteed to succeed for all possible sets of observations that may occur at runtime. This strategy doesn’t need any observational data at runtime to succeed.</td>
</tr>
<tr>
<td>Dynamic Consistency</td>
<td>A dynamic execution strategy that relies on observations acquired at runtime in order to dynamically schedule future choices and timepoints in order to satisfy all timing constraints. This strategy needs access to runtime observations as they become available.</td>
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</tbody>
</table>

Figure 4: CTP Consistency Classifications

Observations that have occurred in the past. This is accomplished by enumerating all possible component STPs for a CTP, called execution scenarios, and placing them in a parallel network by conjoining each scenario’s start and end nodes. Then, disjunctive constraints are added to the network to ensure that identical nodes across scenarios are only scheduled independently after a distinguishing observation has been made. The disjunctive constraints plus the underlying component STPs constitute a new DTP which is then checked for dynamic consistency using existing DTP solving techniques. If the reformulated DTP is consistent, then the original CTP is dynamically consistent. The reformulated DTP is then executed using the standard DTP dispatching techniques.

**AND/OR Search**

An AND/OR search tree is defined by a 4-tuple \( \langle S, O, S_0, S_\ast \rangle \) (Dechter and Mateescu 2007). \( S \) is a set of states partitioned into OR states and AND states. \( O \) is a set of two operators. The OR operator generates children states for an OR state, which represent alternative ways for solving a problem. The AND operator generates children states for an AND state, which represents a decomposition into subproblems, all of which need to be solved. The start state, \( s_0 \), is the only state with no parent state. States with no children are called terminal states, \( S_\ast \), and are marked as Solved (S) or Unsolved (U).

A solution subtree, \( T \), of an AND/OR search tree is a subtree which:

1. Contains the start state, \( s_0 \).
2. If state \( n \) in \( T \) is an OR state, then exactly one child state of \( n \) must be in \( T \).
3. If state \( n \) in \( T \) is an AND state, then all child states of \( n \) must be in \( T \).
4. All terminal nodes are “Solved” (S).

A common example of AND/OR search is the two-player game. Consider a simple example shown in Figure 5. Both a hero and a villain pick a number from the set, \{0,2\}. If the additive total equals two, the hero wins, otherwise the villain wins. The possible outcomes are shown in Figure 5. In Figure 6a, the AND/OR tree is depicted for the case where the villain must choose first. In Figure 6b, the AND/OR tree is depicted for the case where the hero must choose first. Notice that a subtree which satisfies the definition of a solution subtree is available for case 6a but not for case 6b. To be guaranteed a win (i.e. to be “dynamically controllable”) the hero must be allowed to choose last. Otherwise the villain can foil the hero.
In this section, we introduce temporally-flexible reactive programs consisting of seven constructs: conditional execution, iteration, exception handling, non-deterministic choice, parallel and sequential composition, and simple temporal constraints. The proposed language is an extension of the Reactive Model-based Programming Language (RMPL), which can be interpreted graphically as a Temporal Plan Network (TPN). The syntax for the proposed language is presented in Figure 7. A TPN explicitly represents the semantics implied by the RMPL syntax. The mapping from RMPL constructs to TPN elements is presented in Figure 10. A TPN is comprised of five node types and two edge types, as described in Figure 8. Arcs with no annotation are assumed to have bounds of $[0,0]$. The until construct consists of an uncontrollable choice between each number of possible iterations, bounded by $n$. The try-catch construct consists of an uncontrollable choice between the nominal thread of execution and each contingency. A contingency consists of an uncontrollable duration (to account for the uncertain timing of a thrown exception) followed by a handler for the exception type. Each catch clause, as well as the uncontrollable duration, in a try-catch construct is specified by the program’s author, and represents the time window over which a program is robust to that particular exception. Threads of execution that include caught and handled exceptions are considered successful execution paths, and must be tested for temporal consistency with the rest of the program. Labels are attached to uncontrollable choice out-edges to represent the condition under which an edge is taken at runtime.

A TPN is comprised solely of TPN primitive activities, as defined in Definition 1. Each TPN primitive activity has an associated simple temporal constraint and a set of exceptions that it may throw. At a minimum, each TPN primitive activity has two exceptions, $\{e_{lb}, e_{ub}\}$, which are thrown if the activity completes $lb$ or doesn’t complete by $ub$, respectively. More exceptions may be defined. For instance, in the WAM example, an exception is thrown when the WAM leaves its operating region.

An Example TPN

The TPN for the simple WAM example is depicted in Figure 9. A timing constraint $[0,40]$ is placed in parallel with the rest of the TPN to enforce a 40 second time limit. Next, an uncontrollable choice is added for each possible iteration of the until construct, denoted by $n=1$ and $n=2$. Further iterations are bypassed once the halting condition, $in(W3)$, is met. The if-else construct branches on the presence of an obstacle, taking one of two possible routes. Finally, if an exception is thrown, the contingency is invoked by switching execution to the contingent thread.

**Figure 6:** a. And/Or search tree when Villain goes first.  
b. And/Or search tree when Hero goes first.  
c. And/Or solution subtree for a.  
d. No valid And/Or solution subtree exists for b.

**Figure 7:** RMPL Bakus-naur syntax

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<tr>
<th>TPN element</th>
<th>Graphical Symbol</th>
<th>Description</th>
</tr>
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<tbody>
<tr>
<td>Controllable timepoint</td>
<td><img src="image" alt="Symbol" /></td>
<td>An instantaneous timepoint whose execution time is controlled by the executive.</td>
</tr>
<tr>
<td>Uncontrollable timepoint</td>
<td><img src="image" alt="Symbol" /></td>
<td>An instantaneous timepoint whose execution time is NOT controlled by the executive and must be observed.</td>
</tr>
<tr>
<td>Controllable choice node</td>
<td><img src="image" alt="Symbol" /></td>
<td>A non-deterministic choice point that the executive gets to pick at runtime.</td>
</tr>
<tr>
<td>Uncontrollable choice node</td>
<td><img src="image" alt="Symbol" /></td>
<td>An uncontrollable choice point that the executive does NOT get to pick at runtime and must be observed.</td>
</tr>
<tr>
<td>Choice end node</td>
<td><img src="image" alt="Symbol" /></td>
<td>A timepoint where alternative threads from a choice point re-converge.</td>
</tr>
<tr>
<td>Controllable time constraint</td>
<td><img src="image" alt="Symbol" /></td>
<td>A solid arrow; A controllable metric timing constraint.</td>
</tr>
<tr>
<td>Uncontrollable time constraint</td>
<td><img src="image" alt="Symbol" /></td>
<td>A dashed arrow; An uncontrollable metric timing constraint.</td>
</tr>
</tbody>
</table>

**Figure 8:** A description of TPN elements

**Figure 9:** TPN for the Simple WAM Example
Definition 1 - TPN Primitive Activity
A TPN primitive activity is a 5-tuple \((\text{string}, n_i, n_j, \text{STC}, e)\).
- \text{string} represents a command or timing constraint.
  - Commands take the form \(a(p_1,p_2,...)\).
  - Timing constraints have the empty string, \text{null}.
- \(n_i\) is a time event representing the start of the activity.
- \(n_j\) is a time event representing the end of the activity.
- \(\text{STC}\) enforces a metric timing constraint on the activity:
  - \([lb,ub]\) - A controllable metric timing constraint,
  - \([lb?ub]\) - An uncontrollable metric timing constraint.
- \(e\) is a set \(\{e_{lb}, e_{ub}, e_1, e_2, ..., e_n\}\) of supported exceptions.

Definition 2 – Candidate Execution
A candidate execution, \(s_c\), of a TPN is an assignment of choices to controllable and uncontrollable choice nodes in a TPN. \(V_c\) denotes the set of controllable choices, while \(V_u\) denotes the set of uncontrollable choices.

Definition 3 – Complete Execution
A complete execution, \(s_c\), is a candidate execution which can be defined constructively in the following manner:

1. A choice is made to the first choice node encountered along each parallel thread of execution emanating from the start node.
2. Each thread activated by a previous choice is traversed, and again a choice is made to the first choice node encountered along each parallel thread of execution. Repeat (2) until the end node is reached.

In a complete execution, all threads start at the start node and end at the end node. No encountered choices remain unassigned, and no unencountered choices are assigned extraneously.

Definition 4 - TPN Fringe
The TPN fringe is defined as the current state of execution progress in a TPN and is used to distinguish between already executed nodes and nodes that are next in line for execution. The TPN fringe consists of exactly the set of nodes that are capable of being executed next during TPN execution. This rules out any previously executed node; any node constrained to occur after an unexecuted node; and any node pairs on mutually exclusive program branches, (i.e., along different candidate executions).

Dynamic Controllability of Temporally-flexible Reactive Programs
In this section, we define dynamic controllability for temporally-flexible reactive programs. Then, we focus on developing an algorithm to determine dynamic controllability. Our approach is inspired by the approach taken in (Tsamardinos, Vidal, and Pollack 2003) to determine dynamic controllability of CTPs. However, our definition of successful execution differs from prior work.

In temporally-flexible reactive programs, constraint violations (i.e., exceptions) are allowed as long as they are caught and handled by an exception handler. The programmer is given the flexibility to decide whether, how, and when exceptions should be caught. Because handled exceptions are considered successful program executions, they must be tested for consistency with the rest of the program. Each handler must be guaranteed to have time to complete in response to caught exceptions, or the TPN is identified as uncontrollable. This approach tends to overconstrain TPNs with many modeled exceptions. In response, we develop a more reasonable approach called \(N\)-fault dynamic controllability which ensures robustness to at most \(n\) exceptions at runtime.

Definition 5 – Dynamic Controllability
Dynamic controllability of temporally-flexible reactive programs can be viewed as a two-player game between the executive and the environment. The executive picks times for controllable timepoints and makes choices for controllable choice points. Alternatively, the environment
picks times for uncontrollable timepoints and makes choices for uncontrollable choice points. The executive is allowed to observe the outcome of uncontrollable timepoints and choice points as they occur, and then use that information to dynamically schedule future uncontrollable timepoints and choices in order to guarantee successful execution. This strategy needs access to runtime observations as they become available.

An algorithm is developed which frames the dynamic controllability problem for temporally-flexible reactive programs as an AND/OR search tree over candidate program executions. To guarantee dynamic controllability, the algorithm starts from the beginning of a TPN and branches generatively over the $TPN_{fringe}$ as decisions are able to be made either by the executive or by the environment. As in the two-player game example, an OR state is constructed when a decision is made by the executive, while an AND state is constructed when a decision is made by the environment. The result is an AND/OR search tree that explicitly encodes the constraints implied by dynamic controllability. Just as in the two-player game example, the AND/OR search tree considers all possible orderings of decisions that are able to be made between the executive and the environment. Each state in the search tree is comprised of a set of simple temporal constraints. The original program is dynamically controllable if and only if an AND/OR solution subtree exists in which all simple temporal constraints are satisfied. If a program is determined to be dynamically controllable, the AND/OR solution subtree serves as a program execution strategy to ensure successful program execution.

**Definition 6 – N-fault Dynamic Controllability**

To determine $N$-fault dynamic controllability, we artificially constrain the choices made by the environment when constructing an AND/OR search tree. Along each branch, we keep track of the number of exceptions the environment has “chosen” to throw so far, and limit that number to $N$. This results in an AND/OR solution subtree which is robust to at most $N$ runtime exceptions, but is more compact than a full AND/OR solution subtree.

**Definition 7 – AND/OR Search Tree Encoding of a TPN**

An AND/OR search tree encoding of a TPN that determines the property of dynamic controllability is a 4-tuple $\langle S, O, S_0, s_0 \rangle$. Where,

- $S$ is a set of states partitioned into OR and AND states. Each state is comprised of a set of TPN primitive activities (Definition 1), $S = \{a_1, a_2, \ldots, a_n\}$.
- $O$ is a set of operators used to construct the child states for each state in $S$. These are defined below.
- $s_0$ is the start state.
- $S_0$ is a set of terminal states with no children. Terminal states are NOT simply marked as solved (S) or unsolved (U), however. To determine dynamic controllability of an AND/OR subtree, all timing constraints that comprise the subtree comprise a consistent STP. Consistency is determined by performing an all-pairs shortest path computation on each subtree, as it is constructed.

**Definition 8 – AND/OR Solution Subtree**

A solution subtree, $T$, is a subtree of the AND/OR search tree which:

1. Contains the start state, $s_0$.
2. If state $n$ in $T$ is an OR state, then exactly one child state of $n$ must be in $T$.
3. If state $n$ in $T$ is an AND state, then all child states of $n$ must be in $T$.
4. All timing constraints that comprise the subtree form a consistent STP.

**Defining the Operators, $O$**

The operators to construct the AND/OR search tree from a TPN are encoded recursively in a function called $RecursivelyExpand()$. Pseudocode follows, along with a walkthrough of the algorithm on the WAM example.

**Function N-Fault Dynamically Controllable TPN (startnode, N)**

1. $TPN_{fringe} = startnode; \ s = 0; // fault count$
2. $s = 0; \ parent(s, 0) = null; // and/or start state$
3. ConvertUncontrollableTimepoints();
4. AND-OR-tree = $RecursivelyExpand( startnode, s, TPN_{fringe}, I, N )$
5. if SolutionSubtreeExists( AND-OR-tree ) return TRUE
   else return FALSE

**Function RecursivelyExpand (startnode, s, TPN_{fringe}, i, N)**

1. while (not empty( TPN_{fringe} ))
2. if IntermediateTemporalConsistencyCheck( s, TPN_{fringe} )
3. if any node in TPN_{fringe} is a controllable or uncontrollable choice
4. ExpandFringe( s, TPN_{fringe}, i, N )
5. else if \{ s, TPN_{fringe}\} = BumpFringe( s, TPN_{fringe} )
6. else Remove state s from AND-OR-tree.

**Function ExpandFringe ( s, TPN_{fringe}, i, N)**

1. Create an (OR) constraint with parent s, and create a child state:
2. for each node $p$ in TPN_{fringe}
3. $c = null; \ parent(c) = s$; // Creates the new OR state $c$ with parent s
4. $TPN_{fringe\ _copy} = TPN_{fringe}; // Copies a copy of the TPN_{fringe}$
5. for each node $c$ in TPN_{fringe} and its copy, denoted $a_{copy}$
6. $e = [0,0]; \ start(e) = a; \ end(e) = a_{copy}; // Creates [0,0] edge, e,
   // between each node and its copy
7. $c += e; // puts edge $e$ into the andor state $c$
8. if node $p$ is a controllable timeline node
9. ExpandNode( $p_{copy}, c, TPN_{fringe\ _copy}, i, N$)
10. else if node $p$ is an uncontrollable choice node
11. ExpandUncontrollableChoice( $p_{copy}, c, TPN_{fringe\ _copy}, i, N$)
12. else if node $p$ is a controllable choice node
13. ExpandControllableChoice( $p_{copy}, c, TPN_{fringe\ _copy}, i, N$)

**Function ExpandNode ( p, s, TPN_{fringe}, i, N)**

1. for each node $a$ in TPN_{fringe} except $p$
2. $c = [0,inf]; \ start(c) = p; \ end(c) = a; // Constrains node $p$ to occur
3. $s += c; // before all other TPN_{fringe} nodes$
4. Remove node $p$ from TPN_{fringe}
5. Add all children $d$ of node $p$ to TPN_{fringe}
6. Add all edges $e$ traversed to children $d$ into the andor state $s$, $s += e$
7. $RecursivelyExpand( s, TPN_{fringe}, i, N)$
4. Create an uncontrollable choice with two possibilities
   6. choice2: the edge terminates

5. TPNfringe_copy = TPNfringe; // Creates a copy of the TPNfringe
   4. // between each node and its copy
10. c += e; // between each node and its copy
18. RecursivelyExpand( c , TPNfringe_copy , i , N )

12. function ExpandControllableChoice( p , s , TPNfringe , i , N
   5. function ExpandUncontrollableChoice( p , s , TPNfringe, i , N

1. Find all nodes, which are also in TPNfringe and its copy, denoted a_copy
5. if eout is not the nominal thread, continue; //skip contingencies
6. Create a new OR state c with parent s
8. TPNfringe_copy += end(eout) // Add chosen out-edge endnode
10. c += eout; // Add chosen out-edge eout into new andor state c
15. Remove node p_copy from TPNfringe_copy
16. TPNfringe_copy += end(eout) // Add chosen out-edge endnode
18. RecursivelyExpand( c , TPNfringe_copy , i , N )

1. Create a (OR) constraint with parent s, and create a child state c:
5. e = [0,0]; start(e) = a; end(e) = a_copy; // Creates [0,0] edge, e,
8. RecursivelyExpand( TPNfringe_copy , i , N )
11. c += e; // to occur before all other TPNfringe nodes

A Simple Walkthrough

The algorithm starts by placing the TPN start node in the TPN_fringe, and then expands recursively via the function RecursivelyExpand(). Uncontrollable timepoints are handled by converting them into uncontrollable choices via ConvertUncontrollableTimepoints(). This function reflects the environment’s ability to execute an uncontrollable timepoint at any time up to the last instant. RecursivelyExpand() then proceeds in two possible ways. If the TPN_fringe contains either a controllable or uncontrollable choice node, ExpandFringe() is called. If not, then BumpFringe() is called, which “bumps” the fringe to the next choice or uncontrollable choice node to expand. ExpandFringe() creates a branch for each node in the TPN_fringe, and creates a new OR state which consists of a copy of the TPNfringe. This is depicted graphically in Figure 11 for the first call to ExpandFringe() for the WAM example. Next, ExpandFringe() proceeds differently depending on the type of node p. If at any point the subtree becomes temporally inconsistent, the function IntermediateTemporalConsistencyCheck() prunes the subtree from the ANDOR tree. In the WAM example, two nodes are expanded, a controllable timepoint node and an uncontrollable choice node, via functions ExpandNode() and ExpandUncontrollableChoice(), respectively. The ANDOR tree after these function calls is depicted in Figure 12. Intuitively, the AND/OR search tree ensures that for at least one ordering of the two nodes in TPN_fringe, both possible outcomes for the uncontrollable choice node will be consistent.
Experimental Results and Discussion

AND/OR search trees can be solved using standard search techniques, such as depth-first search. One, some, or all solution subtrees may be found. The ability to enumerate just one solution subtree, which corresponds to a subset of possible program executions that guarantees dynamic controllability, is considered a key advantage of this approach. In Figure 13, we show that tractability can be improved by placing an upper limit on robustness to the number of faults at runtime. Four categories of randomly generated programs were tested for dynamic controllability. The program generator creates programs with three parallel threads of execution with randomly chosen RMPL constructs. To increase program complexity, the maximum depth of nested constructs was increased from 1 to 4.

For example, in Category 3, a program may consist of a contingent choice construct, nested within a try-catch construct, nested within a controllable choice construct. We observe that computation time is driven almost solely by the number of faults we wish to be robust to, regardless of the complexity of the original plan. Approximately an order of magnitude improvement is seen for each unit reduction in the number N for N-fault controllability. Intuitively, this can be understood as reducing the number of variables in the underlying CSP problem for each fault that is ignored.

The approach taken in this paper was inspired by the work of (Tsamardinos, Vidal, and Pollack 2003) to determine dynamic consistency of CTPs. Our work is novel in a few key respects:

- The definition of a successful execution is extended to include execution paths with constraint violations (i.e. exceptions) as long as they are caught and handled by an exception handler.
- Temporally-flexible reactive programs bridge the gap between the most common embedded programming language constructs used in practice to build reactive systems (loops, conditions, and exceptions) and the formalisms employed by temporally-flexible planners.
- The proposed algorithm achieves greater compactness than prior art by exploiting two structural restrictions of temporally-flexible programs.
  1. Threads of execution in a TPN are physical processes which always proceed forward in time.
  2. Branches in a TPN always emanate from a single program point and coalesce to a single program point. The proposed algorithm could be extended to support arbitrary disjunctions, but this would require some additional bookkeeping.
- To model looping, conditions, and exception handling, a plan representation is provided which supports both activities of uncontrollable duration (to model the uncertain timing of a thrown exception) as well as uncontrollable outcomes (to model the uncertainty in the type of exception thrown, loop halting, etc…)

Conclusion

In this paper, we extend dynamic controllability of temporally-flexible plans to temporally-flexible reactive programs. In temporally-flexible reactive programs, program execution is conditioned on the runtime state of the world, and exceptions are thrown and caught at runtime in response to violated timing constraints. Handled exceptions are considered successful program executions, and dynamic controllability corresponds to guarantee that a program will execute to completion, despite runtime constraint violations and uncertainty in runtime state. An algorithm is developed which frames the dynamic controllability problem as an AND/OR search tree over possible program executions. A key advantage of this approach is the ability to enumerate only a subset of possible program executions that guarantees dynamic controllability, framed as an AND/OR solution subtree. To improve tractability, an approach is developed called N-fault dynamic controllability which ensures robustness to at most n exceptions at runtime.

References

Kim, Williams, and Abrahmson, 2001. Executing Reactive, Model-based Programs through Graph-based Temporal Planning. IJCAI.