Precise Measurement of Deuteron Tensor Analyzing Powers with BLAST

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Precise Measurement of Deuteron Tensor Analyzing Powers with BLAST

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(The BLAST collaboration)

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We report a precision measurement of the deuteron tensor analyzing powers $T_{20}$ and $T_{21}$ at the MIT-Bates Linear Accelerator Center. Data were collected simultaneously over a momentum transfer range $Q^2 = 2.15–4.50$ fm$^{-1}$ with the Bates Large Acceptance Spectrometer Toroid using a highly polarized deuterium internal gas target. The data are in excellent agreement with calculations in a framework of effective field theory. The deuteron charge monopole and quadrupole form factors $G_C$ and $G_Q$ were separated with improved precision, and the location of the first node of $G_C$ was confirmed at $Q^2 = 4.19 \pm 0.05$ fm$^{-1}$. The new data provide a strong constraint on theoretical models in a momentum transfer range covering the minimum of $T_{20}$ and the first node of $G_C$.


The deuteron, as the only two-nucleon bound state, plays an important role in the understanding of nucleon-nucleon interactions including short-range properties and nonnucleonic degrees of freedom [1–3]. During the last two decades, measurements of tensor-polarized observables, made possible by innovative accelerator and target technologies, have provided new experimental information to understand the electromagnetic structure of the deuteron [4–12] and put strong constraints on nuclear models, e.g., Hamiltonian dynamics [13,14], explicitly covariant models [15,16], as well as the latest developments in effective field theory for low-$Q$ physics [17,18]. In this Letter, a high-precision measurement of the deuteron tensor analyzing powers $T_{20}$ and $T_{21}$ over a broad range of low-momentum transfer is reported.

In the one-photon exchange approximation, elastic electron scattering from the deuteron, a spin-1 nucleus, is completely described by three form factors, the charge monopole $G_C$, the quadrupole $G_Q$, and the magnetic dipole form factor $G_M$, which are only functions of the four-momentum transfer squared, $Q^2$. The unpolarized elastic electron-deuteron cross section $\sigma_0$ directly measures $S = A + B\tan^2(\theta_e/2) + C\cot^2(\theta_e/2)$ via $\sigma_0 = \sigma_{\text{Mot}} f_{\text{rec}} S$, where $\sigma_{\text{Mot}} = (\alpha/2E)^2 \cos^2(\theta_e/2)\sin^2(\theta_e/2)$ is the Mott cross section and $f_{\text{rec}} = 1 + 2(E/M)\sin^2(\theta_e/2)$ is the nuclear recoil factor, with $E$ and $\theta_e$ denoting the electron beam energy and scattering angle, respectively, and $M$ the deuteron mass. Therefore, from measurements of $\sigma_0$ at two different angles and the same $Q^2$, two combinations of the deuteron form factors $A(Q^2) = G_C^2 + (8/9)\eta G_Q^2 + (2/3)\eta G_M^2$ and $B(Q^2) = (4/3)\eta(1 + \eta)G_M^2$, with $\eta = Q^2/(4M^2)$, can be derived. It requires at least one more independent measurement in order to separate the charge monopole and quadrupole form factors, $G_C$ and $G_Q$. The additional measurement can be achieved with a tensor-polarized deuterium target, where the tensor-polarized cross section $\sigma = \sigma_0(1 + \frac{1}{\sqrt{2}}P_{zz}A_{J}^T)$ gives rise to a target tensor asymmetry.

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\[
A_d^T = \frac{3\cos^2 \theta^* - 1}{2} T_{20} - \sqrt{\frac{3}{2}} \sin 2\theta^* \cos \phi^* T_{21}
+ \sqrt{\frac{3}{2}} \sin^2 \theta^* \cos 2\phi^* T_{22}. \tag{1}
\]

Here, the polarization direction is described by the polar and azimuthal angles \(\theta^*\) and \(\phi^*\), respectively, in a frame where the \(z\) axis is along the direction of the virtual photon and the \(y\) axis is defined by the vector product of the incoming and outgoing electron momenta. The quantity \(P_{zz} = n_+ + n_- - 2n_0\) is the tensor polarization, where \(n_+, n_0,\) and \(n_-\) are the relative populations of the nuclear spin projections \(m = +1, 0, -1\) along the direction of polarization, respectively. The tensor analyzing powers, \(T_{20}, T_{21},\) and \(T_{22}\), can be expressed as combinations of the three deuteron elastic form factors

\[
T_{20}(Q^2, \theta_e) = -\frac{1}{\sqrt{2}S} \left[ \frac{8}{3} \eta G_c G_Q + \frac{8}{9} \eta^2 G_Q^2 \right]
+ \frac{1}{3} \eta \left[1 + 2(1 + \eta) \tan^2 \theta_e / 2 \right] G_M^2
\]
\[
T_{21}(Q^2, \theta_e) = -\frac{2}{\sqrt{3}S} \eta^3 \left[1 + \eta \sin^2 \theta_e / 2 \right] G_M G_Q \sec \theta_e
\]
\[
T_{22}(Q^2, \theta_e) = -\frac{1}{\sqrt{3}S} \eta G_M^3.
\tag{2}
\]

Therefore, the measurement of tensor-polarized observables, combined with \(A\) and \(B\), allows the determination of \(G_c, G_Q,\) and \(G_M\). It is useful to consider the quantity \(\tilde{T}_{20} = (T_{20} + \delta) / (1 - \delta)\), in which the small correction by \(\delta = [1/2(1 + \eta) + \tan^2(\theta_e / 2)] \beta / 3\) eliminates the dependence on \(\theta_e\) and \(G_M\), resulting in

\[
\tilde{T}_{20}(Q^2) = -\frac{8}{3} \eta G_c G_Q + \frac{8}{9} \eta^2 G_Q^2
\]
\[
\tilde{T}_{20}(Q^2) = -\frac{8}{3} \eta G_c G_Q + \frac{8}{9} \eta^2 G_Q^2
\tag{3}
\]

which can be directly converted into the ratio \(G_c / G_Q\). Dividing out the leading \(Q^2\) dependence provides a reduced quantity \(\tilde{T}_{20R}(Q^2) = -\tilde{T}_{20}(Q^2) / \sqrt{2G_c^2 + \frac{8}{9} \eta^2 G_Q^2}\), in which details of the low-\(Q\) region are enhanced. The deuteron quadrupole moment is given by \(Q_d = G_Q(0)/M^2 = 25.83/\text{fm}^2\) [19]; hence, with \(G_c(0) = 1\), one has \(\tilde{T}_{20R}(0) = 1\). The magnetic form factor is normalized as \(G_M(0) = \mu_d M/M_N\), with \(\mu_d = 0.857 438 \text{ 230 8}\) nuclear magnetons [20], where \(M_N\) is the nucleon mass.

Tensor-polarized observables can be measured as tensor moments of recoiling deuterons with unpolarized beam and target [4,8,11] or as tensor asymmetries with a tensor-polarized target [5–7,9,10,12]. The experiment reported in this Letter used a highly polarized deuterium gas target with a large acceptance magnetic spectrometer, which is different from all previous experiments.

The experiment was carried out with the Bates Large Acceptance Spectrometer Toroid (BLAST) in the South Hall Ring of the MIT-Bates Linear Accelerator Center; see [21,22] for details. An electron beam of up to 300 mA was stored with 65\% longitudinal polarization preserved with a Siberian snake. The beam energy was 850 MeV, and the typical average current was 150 mA with a lifetime of about 20 minutes. Highly polarized atomic deuterium gas was generated by an atomic beam source in nuclear vector \((T + /V+ : m = 1)\) and tensor \((T- : m = 0)\) polarization states and injected into a 60 cm long, 15 mm diameter cylindrical windowless target storage cell cooled to 100 K and embedded in the ring vacuum [23]. A modest target holding magnetic field defined the polarization direction of the target spin. The target states were switched every 5 minutes by rf transition units in the atomic beam source. In addition, the helicity \(h\) of the electron beam was flipped every injection cycle.

The combination of polarized beam, polarized hydrogen, and vector-tensor-polarized deuterium target and a large acceptance spectrometer allowed asymmetry data to be collected simultaneously, over a large \(Q^2\) range, in many reaction channels, such as \(^1\)\(H(e, e'p)\) [24], \(^2\)\(H(e, e'n)\) [25], \(^3\)\(H(e, e'p)\), and \(e-\)\(d, e-\)\(d\) elastic scatterings [22]. The results and further impact from the latter reaction channel are reported here.

The large acceptance spectrometer [21] was built around eight copper coils providing a toroidal magnetic field of up to 3.8 kG around the beam line. The two horizontal sectors were instrumented with drift chambers for momentum, angular, and vertex reconstruction, covering polar angles to 3.8 kG around the beam line. Background from beam halo scattered off the aluminum target cell wall was studied with the same target cell without gas or with hydrogen flowing through. The cell wall background was below 0.1\% and negligible.

The target tensor asymmetry of Eq. (1) is derived experimentally as

\[
A_d^T = \sqrt{2} \frac{Y^+ - Y^-}{P_{zz} 2Y^+ + Y^-},
\tag{4}
\]

where \(Y^+\) and \(Y^-\) are the charge-normalized yields with the target in the \(T+ (m = \pm 1)\) and the \(T- (m = 0)\) state,
Two asymmetries were measured simultaneously corresponding to electrons scattered into the left and right sector.

Two sets of data were taken during late 2004 and early 2005. The integrated luminosities were 140 pb\(^{-1}\) and 340 pb\(^{-1}\), corresponding to 370 kC and 560 kC integrated charge, respectively. The target spin was directed in the horizontal plane on average to 31.7° and 47.7° to the left side of the beam for the 2004 and 2005 data sets, respectively, with each with about ±0.5° uncertainty. The spin angle in each case varied by a few degrees along the cell and was corrected using a carefully measured field map. The average spin angle was calibrated simultaneously with the target tensor polarization by comparing the elastic tensor asymmetries at low momentum transfer 1.75 < Q < 2.15 fm\(^{-1}\) to Monte Carlo simulations based on parametrization III [26] of previous experimental data. The uncertainty in the normalization is estimated to be ±5%, which is dominated by the dispersion between the three parametrizations [26]. The tensor polarizations for the 2004 and 2005 data sets were P\(_{zz}\) = 0.683 ± 0.015 ± 0.013 ± 0.034 and 0.563 ± 0.013 ± 0.023 ± 0.028, respectively, where the three uncertainties are statistical, systematic, and due to the parametrization, in that order. The small T\(_{zz}\) component in A\(_{T}\) was subtracted using the above parametrization, and T\(_{20}\) and T\(_{21}\) were extracted by solving the two-by-two linear equations relating the experimental asymmetries for electrons in the left and right sector of the detector and the two analyzing powers. For comparison to existing data, T\(_{20}\) and T\(_{21}\) have been adjusted to the conventionally accepted angle \(\theta_c = 70^\circ\).

Table I and Fig. 1 show the results for T\(_{20}\) and T\(_{21}\) with statistical and total systematic uncertainties. The largest systematic uncertainty is due to the parametrization of world data in the calibration of P\(_{zz}\). Other sources of systematic errors include the Q\(^2\) determination, the spin orientation, and the statistical uncertainty in P\(_{zz}\). In order to highlight the low-Q region, the values for T\(_{20}\) were converted to \(\tilde{T}_{20}\) using parametrization III [26] for \(\delta\); the results are depicted in Fig. 2.

The values for T\(_{20}\) measured in this work are in agreement with previous data; yet, they are much more precise. Our data cover a wide kinematic range, providing a strong constraint on the Q\(^2\) evolution of T\(_{20}\) in an important region which contains the minimum of T\(_{20}\) and the first node of G\(_C\). The T\(_{21}\) results are consistently larger in magnitude than all the models and previous measurements at high Q, albeit still consistent within the systematic errors.

The nonrelativistic model with meson exchange and relativistic corrections by Arenhövel et al. [13] agrees

### Table I

<table>
<thead>
<tr>
<th>Q (fm(^{-2}))</th>
<th>T(_{20})</th>
<th>T(_{21})</th>
<th>G(_C)</th>
<th>G(_Q)</th>
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<tr>
<td>2.228</td>
<td>-0.780 ± 0.021</td>
<td>-0.149 ± 0.016</td>
<td>0.1223(14)</td>
<td>3.87(26)</td>
</tr>
<tr>
<td>2.404</td>
<td>-0.877 ± 0.026</td>
<td>-0.148 ± 0.013</td>
<td>0.0953(14)</td>
<td>2.99(20)</td>
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<tr>
<td>2.603</td>
<td>-1.016 ± 0.077</td>
<td>-0.224 ± 0.031</td>
<td>0.0701(17)</td>
<td>2.36(18)</td>
</tr>
<tr>
<td>2.827</td>
<td>-1.172 ± 0.044</td>
<td>-0.312 ± 0.053</td>
<td>0.0479(21)</td>
<td>1.84(15)</td>
</tr>
<tr>
<td>3.063</td>
<td>-1.244 ± 0.031</td>
<td>-0.433 ± 0.072</td>
<td>0.0314(33)</td>
<td>1.37(12)</td>
</tr>
<tr>
<td>3.319</td>
<td>-1.251 ± 0.074</td>
<td>-0.64 ± 0.12</td>
<td>0.0139(33)</td>
<td>1.09(15)</td>
</tr>
<tr>
<td>3.560</td>
<td>-1.15 ± 0.083</td>
<td>-0.57 ± 0.17</td>
<td>0.0087(26)</td>
<td>0.76(31)</td>
</tr>
<tr>
<td>3.823</td>
<td>-1.13 ± 0.06</td>
<td>-0.68 ± 0.21</td>
<td>0.0065(15)</td>
<td>0.52(24)</td>
</tr>
<tr>
<td>4.140</td>
<td>-0.70 ± 0.05</td>
<td>-0.74 ± 0.23</td>
<td>0.0003(17)</td>
<td>0.36(48)</td>
</tr>
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</table>

FIG. 1 (color online). Results for T\(_{20}\) and T\(_{21}\) [grey (red online) dots] compared to previous data [4] (open dots), [5,6] (open upright triangles), [7] (solid upright triangles), [8] (solid dots), [9] (open squares), [10] (solid squares), [11] (open stars), [12] (solid down triangles), and various theoretical predictions. The theoretical curves are nonrelativistic models with relativistic corrections [13] (long dashed line), [14] (dashed line), relativistic models [15] (dash-dotted line), [16] (dotted line), and effective field theory [17,18] (grey error band). Parametrization III [26], used for normalization, is shown (solid line) for reference. The shaded area represents the systematic uncertainties. The first two points at low Q [shown as grey (red online) stars] were used to calibrate polarization and spin angle, while the remaining nine points [shown as grey (red online) dots] represent new measurements.
with our data very well, while it deviates from the experimental results of [11] at higher \( Q \). Although the calculation by Schiavilla \textit{et al.} [14] agrees with \( T_{20} \) measured in this work, it appears to underpredict the size of \( T_{21} \). The relativistic calculation of Phillips \textit{et al.} [15] does not agree with our data at low \( Q \) even while \( T_{21} \) is in good agreement. The agreement improves at higher \( Q \). The agreement is also much improved when our data are normalized to [15], which indicates a good prediction of the “shape” of \( T_{20} \). An overall good description is given by the relativistic calculation of Phillips \textit{et al.} [16].

The recent effective field theory (EFT) calculation by Phillips [17,18] in the framework of chiral perturbation theory is only valid below a momentum transfer of \( \approx 3 \) fm \(^{-1} \), up to which it agrees with our data very well. It should be noted that the quadrupole form factor \( G_Q \) plays an important role in both \( T_{20} \) and \( T_{21} \); yet, none of the potential models [13–16] of \( G_Q \) reproduce the static deuteron quadrupole moment \( Q_2 \) when extrapolated to \( Q = 0 \). This has been identified by the EFT calculation in [18] as a relativistic short-range effect, where the suggested renormalization leads to excellent agreement with our data, which can be best seen in Fig. 2.

The charge monopole and quadrupole form factors \( G_C \) and \( G_Q \) were separated for each \( Q \) value using existing data for structure function \( A \), \( T_{20} \), and \( T_{21} \) by minimizing the quantity

\[
\chi^2 = \left[ \frac{A - A'}{\delta A} \right]^2 + \left[ \frac{T_{20} - T_{20}^e}{\delta T_{20}} \right]^2 + \left[ \frac{T_{21} - T_{21}^e}{\delta T_{21}} \right]^2,
\]

in which \( T_{20} \) and \( T_{21} \) are the measured values and \( A' \), \( T_{20}^e \), and \( T_{21}^e \) were calculated from \( G_C \), \( G_Q \), and \( GM \). In the fit, \( G_C \) and \( G_Q \) were varied while \( G_M \) and \( A \) were fixed by parametrization I [26]. The uncertainty in \( A \) was computed from the covariance matrix of the parametrization. The resulting values for \( G_C \) and \( G_Q \) are shown in Table I and Fig. 3.

The full parametrization I [26] of the deuteron form factors was refit with the results of Ref. [12] and of the present Letter included, and all 18 parameters, including the location of the first nodes of all three form factors, were allowed to vary. The fit confirms the location of the first node of \( G_C \) at \( 4.19 \pm 0.05 \) fm \(^{-1} \), consistent with previous findings [12,26].

In conclusion, we have measured the deuteron tensor analyzing powers in the momentum transfer range of 2.15 to 4.50 fm \(^{-1} \). Our results are consistent with previous data, yet with much improved precision. The wide kinematic coverage provides unique information on the \( Q \) dependence of \( T_{20} \) and \( T_{21} \). Our data are in excellent agreement with recent results in the EFT framework, which offers a solution for the long-standing problem of the deuteron quadrupole moment. Our data have enabled the separation of the deuteron form factors \( G_C \) and \( G_Q \) in the low \( Q \) region and have confirmed the location of the first node of \( G_C \).

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