Interaction of a spark-generated bubble with a rubber beam: Numerical and experimental study

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Interaction of a spark-generated bubble with a rubber beam: Numerical and experimental study

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In this paper, the physical behaviors of the interaction between a spark-generated bubble and a rubber beam are studied. Both numerical and experimental approaches are employed to investigate the bubble collapse near the rubber beam (which acts as a flexible boundary) and the corresponding large deformation of the beam. Good agreement between the numerical simulations and experimental observations is achieved. The analysis reveals that the ratio of the bubble-beam distance to the maximum bubble radius influences the bubble evolution (from expansion to collapse) and the beam deformation. The stiffness of the beam plays an important role in the elastic beam response to bubble expansion and collapse. The effect of the vapor pressure on both bubble collapses and beam deflections is also examined. The results from this paper may provide physical insight into the complex physics of the bubble-rubber interaction. The understanding is possibly applicable in biomechanics for drug delivery to tissue, which is a soft material. It is also probably useful in the marine industry where ultrasonic bubbles are generated for the defouling of ship surfaces, which has been coated with an elastic material. There is also potential interest in underwater explosions near elastic structures.

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I. INTRODUCTION

The interaction between an oscillating bubble and a flexible boundary is an important phenomenon that is commonly found in nature, marine industrial applications, and medical treatments [1]. The behavior of an oscillating bubble is greatly dependent on the characteristics of a boundary that it is placed near. If the boundary is rigid, the bubble moves towards it; whereas, if the boundary is a free surface, the bubble migrates away from it. The behavior of the bubble near a flexible boundary would fall in-between these mentioned limiting cases and is more complex.

Gibson and Blake [2] and Blake and Gibson [3] performed some of the earliest theoretical and experimental studies on the interaction between an oscillating bubble and an elastic boundary. They found that the flexibility of the boundary is crucial to the response of a nearby cavitation bubble. For an elastic boundary, they found the bubble split into smaller bubbles before collapsing with jets. Shima et al. [4] conducted a set of experiments of spark-generated bubbles in the vicinity of a compliant surface and observed different migratory behaviors during bubble collapse. The compliant surface has been modeled as a membrane with a spring foundation [5] or using a finite element (FE) representation [6]. Both papers found good qualitative agreement with the above experiments. Laser-induced cavitation bubbles near a flexible membrane [7], composite surface [8], elastic boundary [9,10], flat rigid surface, and flat free surface [11] were also studied. Obreschkow et al. [11] revealed a “microjet” enveloped by a “vapor jet” via their carefully conducted experiments and explained the jets of collapsing bubbles using their theoretical model based on the first principle.

On the other hand, complex bubble dynamics, such as splitting and mushroom-shaped collapse were observed in those spark experiments, and further understanding is reinforced through a recent paper conducted by Turangan et al. [12] for the nonequilibrium bubble placed next to a (stretched) membrane. The elasticity of a membrane and the distance between the bubble and the membrane (normalized by the maximum bubble radius) remain as the two key parameters in this problem. Ohl et al. [13,14] conducted low-voltage spark bubble experiments and adopted a boundary element method (BEM) model to predict the dynamics of oscillating bubbles placed near a thick layer of biomaterials of different elasticities.

All the preceding papers, however, dealt with the interaction between a bubble and a thick layer, between a bubble and a very thin membrane, or between a bubble and an infinitely soft material, which can be simplified by an axial symmetry system in simulations. Moreover, the interaction between a bubble and a solid layer with other geometries, such as a slender beam remains to be explored. The present paper addresses this and investigates the physical behavior of the interaction of a spark-generated bubble and an elastic beam both numerically and experimentally. The numerical simulations were accomplished by coupling a three dimensional boundary element (BE) potential flow code with an explicit FE structural solver. The experiments were carried out using high-speed photography for the observations of the spark-generated bubble dynamics as well as the elastic beam deformation.

This paper is organized as follows. The spark-generation bubble experiment is described in Sec. II. The necessary details of the numerical methods are provided in Sec. III. The numerical and experimental results are presented in Sec. IV, which deals with the effects of the relative stand-off distance on the bubble evolution and the beam deformation, and explores the influence of the material properties on the bubble-beam interaction. Section IV also discusses the vapor pressure effect in both bubble dynamics and beam motions. Finally, Sec. V summarizes this paper.
II. EXPERIMENTS

The spark-generated bubble experimental setup used in this paper is illustrated in Fig. 1. It is composed of an electrical circuit to generate the spark bubble, a Perspex tank of dimensions 25 cm × 25 cm × 25 cm filled with tap water to a height of 24 cm, a high-speed imaging system, and a Perspex fixture to hold a rubber beam down at both ends. This low-voltage underwater spark-discharge method is very similar to the ones used in several other cavitation bubble investigations [12,14–18].

The electrical circuit is basically made up of a charging circuit and a discharge circuit separated by a mechanical switch. In the charging circuit, two capacitors with a total capacitance of 6900 μF are charged by a 60 V direct current power supply through a 1 kΩ resistor. The discharge circuit is composed of a pair of 0.1 mm diameter copper wires in contact and submerged under water. As soon as the capacitors are charged to 60.0 V, the discharge circuit is engaged, and a spark is created at the contact point between the electrodes. This spark turns into an oscillating vapor bubble with a maximum radius of about 5 mm in a violent process that breaks the thin electrodes. The diameter electrodes used are much smaller than the maximum bubble diameter, hence, they are believed to have a negligible effect on the system dynamics [16,17]. The contact point between the electrodes is adjusted to be at varying heights \( H \) above the centroid of a silicone rubber strip. The rubber strip has a density of 1.170 kg/m\(^3\), a tensile strength of 8.34 GPa, and is supported by a Plexiglas fixture made up of two 10 mm × 10 mm (square cross section) × 100 mm (length) beams erected 50 mm apart and fixed down to the base of the tank (see Fig. 1). Both ends of the rubber beam are secured down onto the top of the fixture stands with stainless steel screws and 10 mm outer diameter stainless steel washers on each side. The portion of the rubber beam suspended has dimensions of 50 mm (\( L \)) × 10 mm (\( W \)) × 1.5 mm (\( H \)). The top surface of the rubber beam is 120 mm above the floor of the tank when at rest, and the spark bubble is created at a height \( H \) of up to 20 mm for this paper.

All experiments are performed under atmospheric pressure and at room temperature (24 °C). A Photron Fastcam-APX RS high-speed camera is used at 20 000 fps, and a shutter speed of 1/40000 s is used to capture the dynamics of the problem. Viscosity effects remain negligible in this paper due to the relatively large size of the bubbles [19]. Surface tension effects are also unimportant as the Weber number for an oscillating bubble in water is on the order of 10\(^3\) [20,21].

III. NUMERICAL METHODS

A model that described the interaction between a spark-generated bubble and a rubber beam is considered as shown in Fig. 2. The bubble has a distance \( H \) from its initial center to the upper surface of the rubber beam. A Cartesian coordinate system \( O_{xyz} \) is used with the \( z \) axis pointing in the opposite direction of gravity, and its origin is at the center of the upper surface of the beam. \( R \) is the bubble radius, \( H \) is the distance of the bubble center to the upper surface of the beam, and \( D \) is the bubble center to the free surface on top. Note that, in all cases studied, the free surface is very far away and is deemed not to be influencing the bubble dynamics.

![Diagram of experimental setup](image-url)
and on the wet surface of the structure,
\[ \rho \frac{\partial \Phi}{\partial t} = p_{\text{ref}} - \frac{1}{2} \rho |\vec{u}|^2 - \rho g z - p_s, \]
where \( \Phi \) is a velocity potential that obeys the relation for the velocity vector \( \vec{u} = \nabla \Phi \), \( \rho \) is the density of the fluid, \( g \) is the gravity acceleration, \( p_{\text{ref}} \) and \( p_s \) are the reference pressure and vapor pressure, and \( p_s \) is the pressure of the fluid in contact with the wet surface of the structure.

Numerically, Eqs. (1) and (2) can be solved for \( \Phi \) if the initial conditions, which initiate the bubble, are known. However, in practice, the initial conditions are not always available for use. Since it is difficult to correlate the discharge energy of the circuit to the initial conditions of the spark bubble, we propose using a small equivalent charge weight \( W \) to determine the initial conditions of the spark bubble with reference to the scaling law for different bubbles [23]. This is based on the principle that the potential energy \( E \) (converted from the electric spark) for a bubble to reach its maximum volume is similar to the potential energy \( W \) of the circuit to the initial conditions of the spark bubble.

In a physical sense, this added mass is the weight \( W \) of the fluid contained in the beam at the cross section; it ranges from 1.21 to 1.14, and the ratio of the specific heats \( \gamma \) equals 1.25 for a TNT charge. With the initial conditions \( V_0 \) and \( p_0 \), Eqs. (1) and (2) can be solved for \( \Phi \), which enables the simulation of bubble behavior and the prediction of the pressure anywhere in the fluid via a BEM.

The dynamics of the rubber beam in response to the nearby bubble is simulated via the finite element method (FEM). The material model proposed by Blatz and Ko for rubber [26] is employed for this paper in which the strain energy density function can be expressed as
\[ W = \frac{G}{2} \left( f(J_1 - 1) + (1 - f)(J_2 - 3) + \frac{1 - 2\nu}{\nu} \left( J_3 - 3 \right) - 1 \right) \left( 1 - f \right) \left( J_3 - 1 \right), \]
In Eq. (7), \( G \), \( \nu \), and \( f \) are the material constants; \( J_1 \), \( J_2 \), and \( J_3 \) are the invariants defined as \( J_1 = \lambda_1^2 + \lambda_2^2 + \lambda_3^2 \), \( J_2 = 1/\lambda_1^2 + 1/\lambda_2^2 + 1/\lambda_3^2 \), and \( J_3 = \lambda_1 \lambda_2 \lambda_3 \), where \( \lambda_1 \), \( \lambda_2 \), and \( \lambda_3 \) are the principal stretch ratios of the deformation at the point considered. Note that, as \( J_1 = 1 \), Eq. (7) becomes the well-known Mooney-Rivlin strain-energy density for incompressible materials [27]. Furthermore, the special case, which assumes \( J_1 = 1 \) and \( f = 1 \) in Eq. (7), may be reviewed as the neo-Hookean incompressible material [27]. Blatz and Ko suggested using \( f = 1 \) and \( J_1 \neq 0 \) based on their experiments [26], which is appropriate for solid rubber provided the extension is less than about 200%. The strain energy (7) then can be simplified to
\[ W = \frac{G}{2} \left( (J_1 - 1) + \frac{1 - 2\nu}{\nu} \left( J_3 - 1 \right) - 1 \right). \]

We calculate the spark-generated bubble using a potential flow code based on the BEM [22,28–31] and compute the structural response of the rubber beam to bubble pressure using an explicit solver based on the FEM with the implementation of the material constitutive equations for the rubber material [32]. The interaction of the bubble and the elastic beam is simulated via the coupling between the BE code and the FE solver. In the coupling computation, the pressure at the interface (or wet surface of the beam) in a fluid domain induced by the nonequilibrium bubble is calculated using the BE code, and it is then given as inputs to the FE solver. The FE solver then calculates the displacements of the rubber beam, which are then returned as inputs for the fluid BE code.

In the view that a beam’s response to an external pressure in air differed from the beam in its response to the same pressure in water and the Blatz and Ko model was employed for a rubber material with the FE solver [32], an added mass was included in the FE solver accordingly [32] in the simulation for the beam in response to the pressure induced by bubble oscillations. In a physical sense, this added mass is the weight added to the beam due to the acceleration or deceleration of the beam. It must move some volume of surrounding fluid with it as it moves. For the rectangular cross section of the beam, the added mass was estimated by [33,34] \( m_{\text{add}} = \alpha \pi R^3 \), where \( \alpha \) is the coefficient depending on the ratio of the width to the thickness at the cross section; it ranges from 1.21 to 1.14, corresponding to a ratio of \( b/h \) from 5 to 10 [33,34].
IV. RESULTS AND DISCUSSIONS

A. Bubble collapse at different $H' = H/R_m$

The collapses of the spark-generated bubbles near the rubber beam were recorded experimentally and were calculated using the coupled BEM and FEM codes. In this paper, three relative standoff distances ($H' = H/R_m$) were considered: $H' = 0.97$, $H' = 1.38$, and $H' = 3.10$. For the purpose of comparison, the beam has the same size, the same material parameters, and the same boundary conditions as those described in the above experiment. The density of the fluid, the reference pressure, and the vapor pressure \cite{12} are assumed to be 1000 kg/m$^3$, 0.1, and 0.5 MPa, respectively.

To simulate bubble behavior and to predict the pressure anywhere in the fluid, the equivalent small charges of TNT were estimated by Eq. (4) with the prescribed maximum radius $R_m$ that matches the bubble from the experiments. With the equivalent small charges of TNT, the initial data of $V_0$ and $p_0$ can be obtained using Eqs. (5) and (6) accordingly, which enables the simulation of bubble behavior and the prediction of the pressure anywhere in the fluid by solving Eqs. (1) and (2). The initial bubble radius $R_0$ and the initial pressure $P_0$ used in the simulations are $R_0 = 0.157R_m$ and $p_0 = 44.3p_{ref}$.

<table>
<thead>
<tr>
<th>Case</th>
<th>$H'$</th>
<th>$R_m$ (mm)</th>
<th>$W$ (g)</th>
</tr>
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<tr>
<td>1</td>
<td>0.97</td>
<td>4.64</td>
<td>$2.7 \times 10^{-5}$</td>
</tr>
<tr>
<td>2</td>
<td>1.38</td>
<td>4.76</td>
<td>$2.8 \times 10^{-5}$</td>
</tr>
<tr>
<td>3</td>
<td>3.10</td>
<td>4.64</td>
<td>$2.7 \times 10^{-5}$</td>
</tr>
</tbody>
</table>

FIG. 3. (Color online) Collapse phase of the spark bubble, which is initiated very far ($H' = 3.18$) from the rubber beam. The scale bar is given in the first frame. The times for each frame are 0.75, 1.1, 1.2, 1.3, 1.45 ms from the first spark observed (which is taken to be time $= 0.0$ ms then). The bubble grows from 0.0 ms to its maximum size of $R_m = 4.64$ mm at 0.75 ms. It is observed that the bubble collapses spherically (frames 1–4) and then rebounds (frame 5). The rubber beam below hardly moves. (a) Experimental results, (b) numerical results.
The estimated charge weights of TNT and the corresponding maximum radii of the bubbles are listed in Table I.

Figure 3 shows the collapse phase of the spark bubble, which is initiated very far ($H' = 3.18$) from the rubber beam. The time sequences shown for each frame are 0.75, 1.1, 1.2, 1.3, 1.45 ms from the first spark observed (which is taken to be time =0.0 ms then). The simulation results match well with the experimental results for all the time frames. The bubble grows from 0.0 ms to its maximum size of $R_m = 4.64$ mm at 0.75 ms. It is observed that the bubble collapses spherically (frames 1–4) and then rebounds (frame 5).

Figure 4 shows the collapse phase of the spark bubble at $H' = 1.38$ from the rubber beam. The bubble grows from 0.0 ms to its maximum size of $R_m = 4.76$ mm at 0.75 ms. Thereafter, the bubble contracts with a jet towards the beam as it collapses, and the beam moves slightly towards the bubble. The bubble reexpands after 1.25 ms. The experimental spark bubble collapses at 1.25 ms, whereas, in numerical simulation, the bubble contracts with a slightly longer time, collapsing at 1.36 ms. The longer collapse time predicted in the simulations for cases 2 (Fig. 4) and 3 (Fig. 5) might arise from a higher vapor pressure (0.5 bar) assumed in the simulation, which may retard the bubble collapse. The actual vapor pressure in the spark bubble, however, cannot be measured easily. From the previous papers [12,17], we estimate it to be between 0.3 and 0.7 bar. The variation could be due to the fact that the electrodes are wound around the wires and that they have to be replaced after several sets of experiments. The tightness of the winding as well as the contact area of the electrodes seems to have some influence on the vapor pressure (estimated from the bubble’s collapse time).

From the second last image of Fig 5, it is also observed that the lower part of the numerical bubble does not fit so well with the experimental spark bubble. There is a counterjet in the experiment, which could be due to the shock wave reflected from the surface. This is not modeled in the simulation. Another plausible reason may be that, in the simulation, the pressure (including vapor pressure) inside the bubble is assumed to be uniformly distributed at each time instant, whereas, the pressure (including vapor pressure) in the experimental spark bubble is unlikely to be
FIG. 5. (Color online) The spark bubble nearer \((H' = 0.97)\) to the rubber beam. The scale bar is given in the first frame. The times for each frame (in milliseconds) are as indicated. The bubble grows from 0.0 ms to its maximum size of \(R_m = 4.64\) mm at 0.75 ms. The bubble expansion causes the beam to deform downwards. From 0.95 ms, the bubble contracts nonspherically. The bubble bottom is flattened, and it forms an elongated shape. (a) Experimental results with the bubble collapsing at 1.25 ms. (b) Numerical results with the bubble collapsing at 1.36 ms.

(almost) instantaneously uniform, especially when the bubble is collapsing violently near the beam.

An overview of the above three cases for all the time frames, however, shows that the simulation results for bubble evolution match reasonably with the experimental results, although there still is room for improving the simulation if we could estimate the pressure inside the bubble with higher accuracy. This could be part of our future work.

B. The beam with different materials in response to bubble evolution

The deflection of the rubber beam induced by the spark-generated bubble was also investigated numerically and experimentally. Table II lists the beam maximum deflections predicted from the simulation and measured from the experiment, respectively. The simulation results match reasonably with the experimental data, which attest that the present simulation is fairly effective.

We extended the simulations to the beam with different materials in response to the bubble evolution at \(H' = 0.97\). In the previous paper [13], several aspects of a bubble oscillating near different biomaterials were explored. In this paper, we placed much emphasis on the response of the biomaterials to bubble oscillation. This is because a nonequilibrium bubble can be made to oscillate and to collapse in the vicinity of nearby tissues or organs in some medical procedures [13]. Furthermore, the behavior of the tissues or organs in response to the bubble oscillation will, in turn, influence the success of the clinical procedures, and the collateral damages, if any, will be borne by the patients. For more details on the type of medical situations where an oscillating bubble might occur next to biomaterials, the reader is encouraged to refer to Ref. [13]. In general, when ultrasound, shock waves, or laser systems are used for medical treatment, it is possible that cavitation

<table>
<thead>
<tr>
<th>Case</th>
<th>(H')</th>
<th>(z_{\text{Expt.}}) ((\text{mm})^a)</th>
<th>(z_{\text{Sim.}}) ((\text{mm}))</th>
<th>(z_{\text{Expt.}}) ((\text{mm})^a)</th>
<th>(z_{\text{Sim.}}) ((\text{mm}))</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.97</td>
<td>-0.641</td>
<td>-0.607</td>
<td>0.214</td>
<td>0.217</td>
</tr>
<tr>
<td>2</td>
<td>1.38</td>
<td>-0.435</td>
<td>-0.421</td>
<td>0.174</td>
<td>0.212</td>
</tr>
<tr>
<td>3</td>
<td>3.10</td>
<td>-0.171</td>
<td>-0.150</td>
<td>-0.00</td>
<td>0.021</td>
</tr>
</tbody>
</table>

\(^a\)The \(z\) axis points in the opposite direction of the gravitational acceleration vector.
bubbles may form within the bodily fluid, e.g., in an ultrasonic liposuction procedure (an oscillating bubble near fat tissue) and others. This paper can also be regarded as an extension of the previous paper [13] in which the bubble behaviors near the different biomaterials were explored extensively.

Table III lists the parameters of the materials, which are taken from Refs. [13,35,36]. The parameters of the rubber material [35] fall in-between the muscle and the cartilage [13], which are regarded as soft biomaterials. Figure 6 shows the central deflection of the beam $z_{bc}$ for four different materials. The maximum downward deflection increases as the beam stiffness (or Young’s modulus) decreases. The beam with the muscle material exhibits the largest deflection when the bubble reaches its maximum radius. The maximum upward deflection decreases as the beam stiffness (or Young’s modulus) decreases when the bubble collapses. This may be explained by the fact that more energy is needed to revert the beam to its original state for the softer material, such as the muscle, and furthermore, the bubble jet would be away from the surface of the beam as its material becomes softer. A higher value of the maximum upward deflection for the beam with the cartilage is also observed; this may be explained by the fact that the density of the beam with the cartilage is lower than the density of the beam with the cervical bone.

Figure 7 shows the distribution of the internal energy over the beams with various materials when a bubble collapses at $t = 1.39\text{ ms}$. It is observed that the energy distributes locally around the center of the beams and attenuates outward to the beam ends. The beam with the muscle material gains the highest energy and shows the lowest energy at the two ends on being compared with the beams of the other materials. The energy distribution pattern of the beam with the rubber material is close to the beam with the cartilage material, hence, indicating that the rubber material would be a potential substitute for the soft biomaterials.

### Table III. The parameters used in the simulation for various materials.

<table>
<thead>
<tr>
<th>Material</th>
<th>Density (kg/m$^3$)</th>
<th>Young’s modulus (kPa)</th>
<th>Poisson ratio</th>
</tr>
</thead>
<tbody>
<tr>
<td>Muscle</td>
<td>1060</td>
<td>790</td>
<td>0.45</td>
</tr>
<tr>
<td>Rubber</td>
<td>1190</td>
<td>2350</td>
<td>0.46</td>
</tr>
<tr>
<td>Cartilage</td>
<td>1300</td>
<td>5000</td>
<td>0.4</td>
</tr>
<tr>
<td>Cervical bone</td>
<td>3000</td>
<td>7300</td>
<td>0.22</td>
</tr>
</tbody>
</table>

C. Effect of vapor pressure

When an electrical spark generates a bubble, the energy deposited at the electrodes is initially stored in a high temperature and high pressure plasma. It is found to have a rather high vapor pressure [12,15], which is difficult to measure in the experiments. However, it is possible to estimate the vapor pressure based on a curve fitting of the numerical results with the experimental observations. Buogo and Cannelli [15] found that, in their experiment on a spark-generated bubble, the vapor pressure varied with the temperature; it reached 0.3 bar corresponding to a vapor temperature of 69 °C.
various vapor pressures: solid line: $p_v = 0$ bar; dashed-dotted line: $p_v = 0.25$ bar; dashed line: $p_v = 0.35$ bar; and dotted line: $p_v = 0.50$ bar. The central deflection of the beam reduces as the vapor pressure increases with its maximum value occurring sequentially.

Turangan et al. [12] found that, with a higher vapor pressure of $p_v = 0.5$ bar, the bubble radius-time curve from their simulations matched well with their experimental results. Figure 8 shows the bubble radius-time histories for various vapor pressures in our simulations. The bubble reaches its maximum radius and collapses at different times with the different vapor pressures. The period of the bubble increases as the vapor pressure increases. As a result, the beam, in response to bubble collapse, varies with the vapor pressure as shown in Fig. 9. The central deflection of the beam is reduced as the vapor pressure increases. The time instant at which the beam deflection reaches its maximum value is also delayed as the vapor pressure becomes higher. This appears reasonable since a higher vapor pressure may dissipate more energy. A proper estimation of the vapor pressure may come from curve fitting of the radius-time histories from experiments and simulations, respectively, which may range from 0 to 0.5 bar ($0 \text{ bar} < p_v \leq 0.5 \text{ bar}$).

V. CONCLUSION

We have studied the interaction of a spark-generated bubble with a rubber beam via both simulations and experiments. The experimental setup for spark-generated bubbles was described, and three selected experimental cases were compared with the simulations employing the coupled BE potential flow code and FE structural solver. The simulations reasonably described the bubble dynamic (or bubble growth and collapse), the rubber-beam deflections, and the behavior of the bubble-rubber-beam interaction. The parametric study illustrated the significant influence of the rubber beam on the bubble evolution at $H' \leq 1$. Exploring the interaction between the spark bubble and the beam with different materials showed that the beam with softer material experienced the larger deflection when the bubble reached its maximum radius and also gained the higher energy at the bubble’s collapse. The simulation results also demonstrated that the vapor pressure retarded the bubble collapse and, thus, influenced the deflection of the beam. From the curve fitting of the radius-time histories from experiments and simulations, respectively, the vapor pressure in a spark bubble could be estimated, and it ranges from 0 to 0.5 bar.

In a future paper, the simulation method for the prediction of the vapor pressure in the bubble with higher accuracy to accommodate its variation in a bubble collapse will be explored.

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