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Enabling single-mode behavior over large areas with photonic Dirac cones

Jorge Bravo-Abad, John D. Joannopoulos, and Marin Soljačić

Many of graphene's unique electronic properties emerge from its Dirac-like electronic energy spectrum. Similarly, it is expected that a nanophotonic system featuring Dirac dispersion (two conical bands touching at a single point, the so-called Dirac point) will open a path to a number of important research avenues. To date, however, all proposed realizations of a photonic analog of graphene lack fully omnidirectional out-of-plane light confinement, which has prevented creating truly realistic implementations of this class of systems able to mimic the two-dimensional transport properties of graphene. Here we report on a novel route to achieve all-dielectric three-dimensional photonic materials featuring Dirac-like dispersion in a quasi-two-dimensional system. We further discuss how this finding could enable a dramatic enhancement of the spontaneous emission coupling efficiency (the β-factor) over large areas, defying the common wisdom that the β-factor degrades rapidly as the size of the system increases. These results might enable general new classes of large-area ultralow-threshold lasers, single-photon sources, quantum information processing devices and energy harvesting systems.

Since its isolation from bulk graphite in 2004 (1), graphene—a one-atom-thick sheet of carbon—has attracted an ever-increasing amount of interest (2–7); nowadays, the study of the electronic properties of this two-dimensional (2D) material has become one of the most active areas of condensed matter physics. This general endeavor has also stimulated new directions in related research fields, especially those originally inspired by the physics of electronic transport in crystalline solids. Of particular relevance in this context are photonic materials whose dielectric constant is periodically structured at the subwavelength scale, the so-called photonic crystals (PhCs) (8). By exploiting the analogy between the propagation of electrons in graphene and the propagation of photons in suitably designed 2D PhCs, phenomena such as directional optical waveguiding (9), pseudodiffusive transport of light (10, 11), Klein tunneling (12), and the observation of the Zitterbewegung of photons (13) have been recently proposed. The existence of Dirac points at the center of the Brillouin zone induced by accidental degeneracy in square lattice 2D PhCs has also been discussed recently (14). However, all these systems share the common fundamental drawback that they lack fully omnidirectional out-of-plane light confinement, which has so far prevented the creation of a truly realistic implementation of a photonic counterpart of graphene.

In this article, we propose a feasible approach to achieve simultaneously quasi-two-dimensional light propagation and Dirac cone dispersion in an all-dielectric 3D photonic material particularly suitable for optical device integration. We show how the unique light confining properties of a proper choice of 3D layered PhCs enables creating extended planar defect modes whose dispersion relation exhibits isolated Dirac points inside a complete 3D photonic band gap. In the limit in which the emitter frequency virtually coincides with the Dirac point frequency (i.e., the frequency of the Dirac cone vertex) the number of photonic states available to the emitter approaches one, even if the system features a macroscopic area. Thereby, the photonic materials presented in this article enable the implementation of structures much larger than the wavelength, which nevertheless have values of the β-factor, which measures the fraction of spontaneous emitted radiation captured by a certain targeted mode, close to unity. Due to the crucial role played by the β-factor in various areas of physics (from optoelectronics to quantum computation or energy harvesting), we believe that these results hold a great promise for the development of novel types of nanodevices.

A schematic of the considered photonic material is rendered in Fig. 1. We start by considering the electromagnetic properties of the PhC before the defect plane is introduced; it is a face-centered cubic (fcc) 3D PhC of air (or low-index) cylinders embedded in a dielectric background and oriented along the (1 1 1) direction (15, 16). This peculiar class of layered PhCs can actually be viewed as an alternating stack of two different types of layers. One of the layers has the form of a triangular lattice of finite-height dielectric rods in air (labeled as “rod layer” in Fig. 1A), whereas the other layer can be described as a triangular lattice of air holes milled in a dielectric slab (labeled as “hole layer” in Fig. 1A). This PhC features two important characteristics. First, each of the two types of layers displays a highly symmetric cross-section that mimics a canonical 2D photonic-crystal structure: One is a periodic array of air holes in a dielectric slab, and the other is a periodic array of hexagonal-like rods in air. Second, although neither of the layers displays a complete (omnidirectional) photonic band gap by itself, when the layers are periodically stacked as shown in Fig. 1A, a large complete photonic band gap can be obtained, using practical values of the refractive index contrast (15, 16).

Next, consider creating an extended planar electromagnetic defect mode in the 3D PhC described above. In order to do that, we introduce into the structure a single defect layer that perturbs the original periodic sequence rod layer/hole layer/rod layer along the (1 1 1) direction. In particular, we remove a hole layer of the structure and replace it by a triangular lattice of finite-height dielectric rods with circular cross-section (green cylinders in Fig. 1A), whose radius, height, and dielectric constant are given by \( r_c, h_g, \) and \( \epsilon_c \), respectively.

It is known (16, 17) that the introduction of line defects into layered 3D PhCs of the type described above enables the implementation of localized electromagnetic states whose dispersion relation, field profiles, and polarization are in a close correspondence with those associated with the corresponding 2D PhC geometries. Similarly, one would expect that the spectral properties of the planar extended states localized in the defect layer rendered in Fig. 1A should, to some extent, inherit properties associated with the Bloch states of the bona fide 2D counterpart of this defect layer (i.e., those that are present in a triangular array of infinitely long high-index rods). On the other hand, it...
has been demonstrated that the intrinsic symmetry properties of 2D PhCs based on a triangular lattice can induce the presence of Dirac points near high-symmetry points of the band structure (9–11). Thus, this line of reasoning suggests the feasibility of creating a single 3D physical system simultaneously featuring quasi-two-dimensional light propagation and Dirac cone dispersion. In addition to these two features, it is also crucial that the Dirac cone dispersion is isolated within a given frequency bandwidth, or, equivalently, that the Dirac cone is fully separated from the rest of the bands present in the band structure. Only by combining all three of these features in the same system, it is possible to fully exploit the analogy between electronic and photonic graphene. We emphasize that although, in principle, it is not challenging to obtain each of these three characteristics separately in a photonic structure, achieving all three of them concurrently in the same 3D physical system is not straightforward.

To explore to which extent these ideas can be implemented in a realistic system, we have carried out a systematic numerical analysis of the evolution of the corresponding band structures as a function of the geometrical parameters and the dielectric constants, defining both the underlying 3D PhC, as well as the defect layer. This numerical study is based on the following three-step optimization approach. First, we have optimized the geometrical parameters of the defect layer as if instead of being embedded as a defect in a 3D PhC, it was in a free-standing configuration (i.e., surrounded by air regions). The goal of this first step is finding a 2D PhC rod slab, formed by a triangular lattice of finite-height high-dielectric cylinders, that displays an isolated Dirac point inside the light cone. Second, we have optimized the geometrical parameters of the 3D PhC in which the defect layer is embedded (the layered 3D PhC described above, without any defect). The goal of this second optimization step is to find both the refractive index and the optimal geometrical parameters of the considered 3D PhC, so that it displays a large full-photonic band gap approximately centered at the Dirac frequency found in the first step of the optimization. Finally, we have used a systematic trial-and-error procedure to determine the optimal way of inserting the defect layer into the 3D PhC, so that the dispersion relation of the free-standing 2D PhC rod slab, particularly the Dirac point, is not significantly perturbed by the interaction of the defect layer with its surrounding dielectric media. This numerical analysis was performed by means of the plane-wave expansion method to Maxwell’s equations (18) using a supercell large enough in the (1 1 1) direction so the properties of an isolated defect plane in an infinite 3D PhC are accurately reproduced. Our calculations show that, for the optimal structure, the radii of the air holes within the hole layer and the equivalent cylinders (17) in the rod layer are \( r_h = 0.41a \) and \( r_r = 0.18a \), respectively (\( a \) is the lattice constant of the in-plane triangular lattice defined within each layer; see Fig. 1A). The thicknesses of the hole and rod layers are \( t_h = 0.32a \) and \( t_r = 0.50a \), respectively, whereas the refractive index of the high-dielectric material is assumed to be \( n = 2.5 \). The low-refractive index of the structure is taken to be air. On the other hand, the defect layer of this optimal system features \( n_d = 3.1 \), \( r_d = 0.32a \), and \( h_d = t_r \). In addition, from this numerical study we have also obtained that the optimal configuration is that in which the cylindrical rods of the defect layer are aligned with the rods forming the two rod layers located right above and below the defect plane (see Fig. 1A).

Fig. 1B summarizes the dispersion diagram obtained for this structure. Shaded violet areas in this figure show the projected band structure for the perfectly periodic 3D PhC (i.e., without the defect layer). In this case, the dispersion diagram was obtained by plotting the frequencies \( \omega \) of the extended bulk states of the system as a function of the in-plane wavevector \( \mathbf{k}_\parallel \), in the irreducible Brillouin zone of the underlying in-plane 2D triangular lattice. The considered system exhibits a large 3D complete photonic band gap (shaded yellow area), centered at frequency \( \omega = 0.497 (2\pi a/c) \) (\( c \) is the light velocity in vacuum) and featuring a gap-midgap ratio of approximately 8%. The dispersion relation of the guided modes of the defect plane are also rendered in Fig. 1B (red lines). As can be seen, these defect bands indeed display a Dirac point at \( \omega_D = 0.506 (2\pi a/c) \) (see Fig. 1B and the inset of Fig. 1A), fully lying within the omnidirectional photonic band gap of the periodic system (yellow area in Fig. 1B). Importantly, this Dirac point is completely isolated from all of the rest of the frequencies of the band structure of the system within a bandwidth \( \Delta \omega = 0.026 (2\pi a/c) \). Finally, the strong out-of-plane photonic band gap confinement of the electromagnetic fields at \( \omega = \omega_D \) is clearly observed in the inset of Fig. 1A, which displays the corresponding cross-section along the \( yz \) plane of the electric-field intensity distribution. These results demonstrate the feasibility of creating a complete photonic analog of graphene in a realistic 3D physical system. We emphasize that the obtained results are scalable to many different frequency regimes and therefore could be used to enhance performance of different classes of active optical devices.

We now turn to demonstrate how the proposed class of photonic systems can enable an unprecedented control of light–matter interaction over large areas. In order to do that, we apply the commonly employed procedure to probe the properties of light–matter interaction in a complex electromagnetic environment:
We study the radiation process of a point quantum emitter embedded in the system under analysis (19, 20). As it was discovered by Purcell more than 60 years ago, the rate of spontaneous emission of a quantum light emitter can be strongly enhanced or suppressed by tailoring the density of electromagnetic states of the environment in which the emitter is embedded (21). The emitter is modeled as a two-level system, characterized by a transition frequency $\omega_t$, an emission bandwidth (i.e., a transition bandwidth) of $\Delta \omega_t$, and a dipolar transition moment $d = \hat{d}.d$. In particular, we analyze the spontaneous emission coupling efficiency, the so-called $\beta$-factor. In a multimode photonic system, the $\beta$-factor quantifies the portion of all spontaneously emitted photons that couple into a given mode (22). This physical magnitude is of a paramount importance in modern optoelectronics and quantum information processing since the performance of an active nanophotonic device, or a single-photon emitter, can often be greatly enhanced by increasing the value of $\beta$ (22–24) [recent examples include ultralow-threshold lasers (25–27) and single-photon sources (28, 29) based on PhC cavities].

The dependence of the $\beta$-factor on the particular electromagnetic environment in which the considered emitter is embedded can be elucidated by examining its link with the corresponding photonic local density of states (LDOS), $\rho(r, \hat{d}, \omega)$. For a nondissipative system, the LDOS can be written as (19)

$$\rho(r, \hat{d}, \omega) = \sum_{\nu} \epsilon(r)|E_{\nu}(r) \cdot \hat{d}|^2 \delta(\omega - \omega_{\nu})$$

where the index $\nu$ labels the different source-free normal solutions to Maxwell’s equations obtained for the considered photonic structure; $E_{\nu}(r)$ and $\omega_{\nu}$ are their corresponding $E$-field profile and frequency, respectively, $\epsilon(r)$ stands for the dielectric constant distribution.

On the other hand, from Fermi’s golden rule (19–21), one finds that, in 3D, the spontaneous emission rate of the considered quantum emitter $\Gamma$ is proportional to the LDOS accessible to the emitter $\Gamma = (4\pi|d|^2\omega_t/\hbar\epsilon_0)\rho(r, \hat{d}, \omega_t)$. Thus, assuming the targeted mode to be a normal mode of the system, $E_{\nu}(r)$, of frequency $\omega_{\nu}$, one can write the $\beta$ factor as (see SI Text),

$$\beta = \frac{\omega_t g(\omega_t)\epsilon(r)|E_{\nu}(r) \cdot \hat{d}|^2}{\int d\omega|g(\omega)|^{2} \rho(\omega, \hat{d}, \omega)}$$

where $g(\omega)$ is the lineshape of the transition, centered at $\omega_t$ and characterized by full-width-half-maximum (FWHM) of $\Delta \omega_t$. Note that the factor $g(\omega_t)$ in the numerator accounts for the fact that $\beta$ decreases as the emission frequency is detuned from $\omega_t$. Hereafter $\omega_t = \omega_{\nu}$ is assumed.

Eq. 2 clearly shows that the $\beta$ factor can be enhanced by introducing a physical mechanism that minimizes the density of photonic states lying within the transition linewidth. In fact, the large values for $\beta$ reached in subwavelength volume photonic resonators (25–29) can be viewed as a particular instance of this physical picture. Such nanoresonators are designed to have a volume small enough so that only one resonant mode lies within the transition linewidth. This makes them to effectively act as single-mode structures, which as deduced from Eq. 1 leads to values $\beta \approx 1$ (provided that the coupling with the radiation modes existing outside the resonator is negligible). Although very relevant in a number of contexts, this cavity-based approach does not admit a straightforward extension for large-area control of $\beta$. In the rest of this article, we show how the general class of isolated Dirac points discussed above do enable such large-area control.

To gain physical insight into the effect of the Dirac cone dispersion on the $\beta$ factor, we evaluate the magnitude of $\beta$ in the following three cases (all of them 3D): first, the case of a homogeneous material; second, the case in which the dielectric material is periodically structured so that $\omega_t$ lies in the vicinity of the lower edge of a 3D photonic band gap; and, third, the case of the structure displayed in Fig. 1—i.e., a system exhibiting simultaneously quasi-two-dimensional light propagation and an isolated Dirac point near $\omega_t$. Fig. 2 A–C illustrates each of these dispersion relations (for simplicity in the visualization, in Fig. 2 A and B, only the 2D counterparts of the corresponding cases are rendered). Importantly, in all three cases we also assume that the EM field in the system is confined in a finite volume $V$, such that $V \gg \lambda^3$ (the dependence on volume is addressed below).

The homogeneous case is characterized by the following dispersion relation: $\omega(k) = ck/n$ (where $n$ is the refractive index and $k = |k|$, with $k = (k_x, k_z)$). Then, making use of the isotropy of the medium, one can derive the following simple expression for the $\beta$ factor: $\beta = (1/V)\omega_t g(\omega_t)/F_T(\omega)$, where $F_T(\omega) \equiv \int d\omega|g(\omega)|^{2} \rho_{\omega_t}(\omega)$, with $\rho_{\omega_t}(\omega) = (1/(2\pi n^2c))(\omega/\omega_t)^2$. Similarly, for the case of the photonic band gap, taking $\omega(k) = \omega_g - A_k^2(\omega_g)$ being the center of the gap and, see Fig. 1B, and $A_k$ is a constant which has to be determined from calculations of the band structure; physically, $A_k$ defines the curvature of the dispersion relation close to $\omega_g$, one finds that the magnitude of $\beta$ can be calculated using the same expression given above for the homogeneous case but replacing $F_T(\omega)$ by $F_g(\omega) \equiv \int d\omega|g(\omega)|^{2} \rho_{\omega_g}(\omega)$, with $\rho_{\omega_g}(\omega) = (4\pi^2 A_k^2)^{-1}(\omega - \omega_g)^{-1/2}$.

For the Dirac case, the calculation of $\beta$ is more involved that in the previous two cases. First, we take into account that an excited dipole embedded in the defect layer displayed in Fig. 1A only decays via the guided modes confined within the layer; the decay into any other modes surrounding the layer (e.g., bulk Bloch modes) is prevented by an omnidirectional photonic band gap. Then, for small enough values of $h_d$ (so only the fundamental mode guided in the $z$ direction is excited), the quasi-2D light propagation inside the defect layer can be described by the dispersion relation corresponding to in-plane Bloch states (i.e., states with $k_z = 0$): $\omega(k) = \omega_g + A_{\parallel}k_{\parallel} = \omega_g + A_{\parallel}k_{\parallel,0}$ (see details

![Fig. 2. Dispersion relations of three representative photonic materials and typical spectrum of a quantum emitter.](image-url)
In SI Text). In this expression, \( A_D \) is a constant that can be obtained from band-structure calculations and \( k_{IL} \) defines the coordinates in \( k \) space of the Dirac cone vertex, whereas the plus and minus signs correspond to \( \omega > \omega_D \) and \( \omega < \omega_D \), respectively. (Note that, physically, \( A_D \) corresponds to the slope of the Dirac cone.) Thus, the total density of states accessible to the emitter can be written as \( \rho_D(\omega) = (1/2\pi)A_D^2(\omega - \omega_D) \). This, in turn, yields the following expression for the spontaneous emission coupling efficiency \( \beta = (1/A)\omega g(\omega)/F_D(\omega) \), with \( F_D(\omega) = \int \rho_D(\omega)/\omega^2 d\omega \). Here \( A \) is the transversal area of the defect layer (i.e., the total volume of the defect layer is \( V = A \times h_d \)).

We now quantify the values of \( \beta \) for each of the above cases using realistic parameter values. To allow for a direct comparison among the three considered class of systems, we introduce a renormalized spontaneous emission coupling efficiency \( \eta \) as we show below, it enables reaching values of \( \beta \) that are of the order of magnitude with respect to the band-edge case. This is an important result, because, for the Dirac case we define \( \eta_D = \beta_D/A/\omega^2 \). This normalization allows us, on one hand, to remove from the discussion the obvious dependence of \( \beta \) on the size of the system and thus focus exclusively on the photonic properties. On the other hand, it also removes the geometrical factor \( V/A \) that enhances the \( \beta \) factor in the Dirac case with respect to the other two cases. This factor stems from the electromagnetic confinement in the \( z \) direction of the guided modes in the Dirac structure and therefore cannot be ascribed to the Dirac spectrum. Furthermore, in our calculations we assume that the transition lineshape is described by a Lorentzian centered at \( \omega_s = 2.1 \times 10^{15} \text{ s}^{-1} \) (i.e., an emission wavelength of 900 nm) and featuring a relative full width at half maximum (FWHM) \( \omega_s/\omega_1 = 10^{-4} \); values more than one magnitude smaller for \( \omega_s/\omega_1 \) can be reached using, for instance, quantum dots at low temperatures. In the homogeneous case a refractive index \( n = n_d \) is chosen, whereas for the band-edge and Dirac cases, the values of the dispersion relation parameters \( A_p \) and \( A_D \) are taken from band-structure calculations: \( A_p = 1.2 \times c A_p/(2\pi) \) and \( A_D = 0.3 c \times A_D/\omega_1 \) (a is lattice constant defined in Fig. 1A), which for operation at the considered emission wavelength, takes a value of 450 nm). We note that for a direct comparison between the band-edge and Dirac cases, the value of \( A_p \) was obtained from the \( M \) point of the band-structure results shown in Fig. 1B.

Thus, using these parameters, from the numerical evaluation of the expression for \( \beta \) given above, we obtain \( \eta_D = 68.2 \), \( \eta_p = 4.0 \times 10^4 \), and \( \eta_s = 3.6 \times 10^6 \). As readily deduced from these values, the Dirac dispersion introduces an enhancement factor of about four orders of magnitude with respect to the homogeneous case and about one order of magnitude with respect to the band-edge case. This is an important result, because, as we show below, it enables reaching values of \( \beta \approx 1 \) over macroscopic areas. Physically, the origin of this dramatic increase of \( \eta \) (and consequently of \( \beta \)) can be understood in terms of the rapid decrease of the number of photonic states available to the emitter as its emission frequency approaches the frequency of the Dirac point. In particular, in contrast to the homogeneous and band-edge cases, in the Dirac case when \( \omega_s \to \omega_D \) (i.e., as emission frequency approaches the Dirac vertex frequency), the number of modes accessible to the emitter approaches unity, making the whole structure to effectively behave as a single-mode system, even if it features a large area. The specific magnitude of the enhancement factor reported above for the Dirac case with respect to the band-edge case could, in general, be controlled by the ratio of the slopes at emission frequency of the corresponding dispersion relations (conical and parabolic, respectively), \( A_D/A_p \). Note also that the LDOS is strictly zero at \( \omega_D \) and \( \omega_p \) in the band-edge and Dirac cases, respectively. Therefore, in the calculations for each case, we have assumed \( \omega_D \) to be slightly detuned (by a quantity much smaller than \( \omega_D \) and \( \omega_p \)) from \( \omega_D \) and \( \omega_p \).

We now focus on analyzing the dependence on size of the enhancement of \( \beta \) enabled by isolated photonic Dirac cones. The physical origin of this dependence stems from the fact that for values of the area \( A \) such that \( A > \lambda^2 \) cannot be safely assumed, it is necessary to account for the discreteness of the eigenmodes in the system: The only states that will be allowed to exist are those characterized by a wavevector \( \mathbf{k} = (k_x, k_y) \) whose value coincides with one of the nodes of the rectangular grid defined by the discrete set of values \( \{2\pi n_x/L, 2\pi n_y/L\} \) (with \( n_x \) and \( n_y \) being arbitrary integers, and where the system is assumed to be square shaped with side length \( L \).—i.e., \( A = L^2 \)). Therefore, the influence of these finite-size effects on \( \beta \) can be computed by using the discrete version of Eq. 2 (see SI Text).

Fig. 3 shows the computed results for \( \beta \) as a function of the normalized emission linewidth \( \Delta \omega_s/\omega_s \) for several values of the lateral size of the system, ranging from \( L/a = 10 \) to \( L/a = 10^5 \). As observed, in the considered cases, \( \beta \) tends to 1 when \( \Delta \omega_s/\omega_s \) approaches the lower limit of the interval displayed in the figure (\( \Delta \omega_s/\omega_s = 10^{-5} \)). This is due to the fact that for all the considered system sizes, a linewidth \( \Delta \omega_s/\omega_s \lesssim 10^{-3} \) is smaller than the frequency interval between the adjacent modes, and therefore the structure is actually acting as a single-mode system (much in the same way as occurs in large-\( \beta \) photonic nanocavities). As \( \Delta \omega_s/\omega_s \) is increased, a growing number of modes enter into the interval where \( g(\omega) \) is negligible, and therefore the value of \( \beta \) starts decreasing. Because the frequency interval between adjacent modes is smaller for larger values of \( A \), the decrease of the \( \beta \) factor with \( \Delta \omega_s/\omega_s \) starts sooner for larger values of \( A \). Finally, we note that if lateral edges of the defect layer are not perfectly reflecting, the magnitude of the \( \beta \)-factor for the smaller values of \( A \) could be reduced due to the radiation energy leakage occurring through those lateral edges of the defect layer.

In conclusion, we have demonstrated that a 3D photonic material can exhibit isolated Dirac cones in its dispersion relation. The proposed approach is readily accessible experimentally, both for fabrication and measurement. In addition, we have shown how the proposed class of systems enables achieving unprecedentedly large values of \( \beta \)-factor over large areas. We believe that these results could open new avenues in a variety of different fields. Thus, the large \( \beta \) factors demonstrated in this work may lead to the realization of important applications such as low-threshold large-area lasers, enhanced single-photon sources, and novel efficient platforms for solar energy harvesting.

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