# A Computational Investigation of Li\(_9\)M\(_3\)(P\(_2\)O\(_7\))(P\(_4\)O\(_2\)) \((M = V, Mo)\) as Cathodes

The MIT Faculty has made this article openly available. **Please share** how this access benefits you. Your story matters.

| As Published | http://dx.doi.org/10.1149/2.080205jes |
| Publisher | Electrochemical Society |
| Version | Final published version |
| Accessed | Thu Apr 04 21:32:41 EDT 2019 |
| Citable Link | http://hdl.handle.net/1721.1/79579 |
| Terms of Use | Article is made available in accordance with the publisher’s policy and may be subject to US copyright law. Please refer to the publisher’s site for terms of use. |

**Detailed Terms**
A Computational Investigation of \( \text{Li}_9\text{M}_3(\text{P}_2\text{O}_7)_3(\text{PO}_4)_2 \) \((M = \text{V, Mo})\) as Cathodes for Li Ion Batteries

Anubhav Jain, Geoffroy Hautier, Charles Moore, Byoungwoo Kang, Jinhyuk Lee, Hailong Chen, Nancy Twu, and Gerbrand Ceder*†

Massachusetts Institute of Technology, Cambridge Massachusetts 02139, USA

Li ion batteries are the dominant power source for many consumer electronics, and will for the foreseeable future be the storage technology employed for plug-in hybrid electric vehicles (PHEVs) and electric vehicles (EVs). Improving the performance of Li ion batteries would accelerate adoption of PHEVs and EVs, helping to mitigate concerns over pollution and climate change. One method to improve Li ion battery performance is to design new cathode materials that are safe, cost-effective, and possess a high specific energy and energy density.

Many important properties of cathode materials can now be computed using density functional theory calculations. In particular, operating voltage, stability, and safety are relatively simple calculations to automate. The ability to predict many important cathode properties before synthesis makes it possible to rapidly screen cathode materials computationally. We have previously described how such an approach can lead to the discovery of novel cathode materials.

In this section, we study the compound family \( \text{Li}_9\text{M}_3(\text{P}_2\text{O}_7)_3(\text{PO}_4)_2 \) with \( M = \{\text{V, Mo}\} \). \( \text{Li}_9\text{M}_3(\text{P}_2\text{O}_7)_3(\text{PO}_4)_2 \) chemistry contains both monophosphate (PO\(_4\)) and pyrophosphate (P\(_2\)O\(_7\)) groups. Monophosphate-based cathodes have been the subject of much investigation since Padhi et al.'s discovery of LiFePO\(_4\) and its subsequent characterization as safe and high-rate. Lithium metal pyrophosphates have also been the subject of recent study as cathodes, although they have not been tested as extensively as the monophosphates. Presumably, this is in part because a pyrophosphate group's charge-to-weight ratio is lower than that of a monophosphate group, making it more difficult to achieve high specific energies.

The \( \text{Li}_9\text{M}_3(\text{P}_2\text{O}_7)_3(\text{PO}_4)_2 \) compound family emerged from a high-throughput computational screening procedure whereby we substituted transition metals into all known lithium metal phosphates. In particular, a subset of our computations revealed that \( M = \{\text{V, Mo}\} \) substitution for Fe into LiFePO\(_4\) was promising for further study. LiFePO\(_4\) is a known compound that was first reported by Poisson et al. in a non-battery context.

The vanadium version of this compound, \( \text{Li}_9\text{V}_3(\text{P}_2\text{O}_7)_3(\text{PO}_4)_2 \), has a theoretical capacity of 173 mAh/g assuming V\(^{3+}\) to V\(^{5+}\) oxidation. Based on our computational study, it was synthesized experimentally and electrochemically tested by the authors. The experimental synthesis and electrochemical characterization of \( \text{Li}_9\text{V}_3(\text{P}_2\text{O}_7)_3(\text{PO}_4)_2 \) were recently published independently by Kuang et al. Subsequently, Xu et al. reported on the properties of Cr-doped \( \text{Li}_9\text{V}_3(\text{P}_2\text{O}_7)_3(\text{PO}_4)_2 \) and Kuang et al. further characterized its charge and discharge behavior.

In this study, we concentrate on computational results that clarify the electrochemical behavior of \( \text{Li}_9\text{V}_3(\text{P}_2\text{O}_7)_3(\text{PO}_4)_2 \). In addition, we investigate replacement of V by Mo as a potential avenue for its improvement. Such a strategy is promising because Mo could theoretically transfer three electrons per formula unit in the \( \text{Li}_9\text{Mo}_3(\text{P}_2\text{O}_7)_3(\text{PO}_4)_2 \) host. Our computational study finds that substitution of 2/3 of the V site by Mo could lead to higher usable capacity and better intrinsic safety.

Crystal Structure of \( \text{Li}_9\text{M}_3(\text{P}_2\text{O}_7)_3(\text{PO}_4)_2 \)

As reported by Poisson et al., \( \text{Li}_9\text{M}_3(\text{P}_2\text{O}_7)_3(\text{PO}_4)_2 \) forms in the spacegroup P\(_{\text{3}}\)c\(_1\) and contains alternating anion and cation layers in the \( c \)-direction (Figure 1). The anion layers consist of \( \text{M}_3(\text{P}_2\text{O}_7)_3(\text{PO}_4)_2 \) groups. Each M is octahedrally coordinated: two vertices connect to a single P\(_2\)O\(_7\) group, two vertices connect to separate P\(_2\)O\(_7\) groups, and the remaining two vertices connect to separate PO\(_4\) groups (a detailed illustration can be found in Poisson et al.). The anion layer contains a large in-plane cavity that forms a channel along the \( c \)-axis (Figure 1).

The nine lithium ions per formula unit are divided into 3 distinct sites, with occupancies of one, two, and six (Figure 2). Following the notation of Poisson et al., the chemical formula can thus be written as \( \text{Li}_i \text{Li}(2)_i \text{Li}(3)_i \text{V}_i \text{P}_2\text{O}_7)_3(\text{PO}_4)_2 \). The \( \text{Li}(1) \) sites exhibit an octahedral coordination and are positioned along the channel created by the anion layers, sitting along the \( c \)-axis halfway between the anion layers. The \( \text{Li}(2) \) sites are tetrahedrally coordinated, sit close to the anion layers, and are rotated and stacked along the \( c \)-axis (Figure 1). Three vertices of the \( \text{Li}(2) \) tetrahedron each corner-share with one metal polyhedron and one PO\(_4\) group within the same anion layer. The final vertex corner-shares with a PO\(_4\) group in a different anion layer. The \( \text{Li}(3) \) sites form strongly distorted tetrahedra (Figure 1) that share one edge with \( \text{Li}(1) \) and another edge with a MO\(_6\) octahedron.

The two vertices that edge-share with the \( \text{Li}(1) \) site each also corner-share with another \( \text{Li}(3) \) site and a PO\(_4\) group; these PO\(_4\) groups are in separate anion layers. The two vertices that edge-share with the MO\(_6\) octahedron each also corner-share with a PO\(_4\) group; these PO\(_4\) groups are in the same anion layer.

Methodology

General computational methodology.— For the DFT calculations, we follow the general calculation methodology and parameters outlined in a previous paper. Our computations employ the GGA functional as parameterized by Perdew et al. and were performed using the Vienna Ab Initio Simulation Package. We used the rotationally invariant approach to GGA+U proposed by Dudarev et al. to correct self-interaction in Mo and V oxides, using \( U = 3.1 \) for V and \( U = 5.0 \) for Mo according to the methodology of Wang et al. We used a Monkhorst-Pack k-point grid of \( 2 \times 2 \times 2 \) for most calculations.
but sometimes increased the mesh to $4 \times 4 \times 2$ to aid in numerical convergence. The magnetic state of all compounds was assumed to be ferromagnetic.

The crystal structures of $\text{Li}_9\text{V}_3\text{Mo}_1\text{O}_{40}(\text{P}_2\text{O}_7)_3(\text{PO}_4)_2$ were generated by starting with the positions of the $\text{Li}_9\text{Fe}(\text{P}_2\text{O}_7)_3(\text{PO}_4)_2$ crystal structure as reported in the Inorganic Crystal Structure Database (ICSD)\textsuperscript{6, 35} and performing two consecutive structural relaxations using the AFLLOW software.\textsuperscript{36} Because Li positions can sometimes be difficult to resolve by X-ray diffraction, we computed the $\text{Li}_9\text{V}_3(\text{P}_2\text{O}_7)_3(\text{PO}_4)_2$ structure starting with slight adjustments to the experimentally-reported Li positions. We calculated 50 structures with the Li starting positions subjected to a random displacement of 0.1–0.2 Å, but did not find a lower-energy ground state.

Many of our calculations involve testing multiple cation orderings to find a ground state. All ground states determined through this procedure were recomputed with electronic and ionic cutoffs tightened by a factor of ten, i.e., electronic cutoff of $n \times 5 \times 10^{-6}$ eV and ionic cutoff of $n \times 5 \times 10^{-5}$ eV where $n$ represents the number of atoms in the cell. For these calculations, we expect our total energies to be converged to approximately 10 meV/f.u. ($\sim$0.2 meV/atom) with respect to electronic and ionic cutoff energy.\textsuperscript{6}

$\text{Li}_x\text{V}_3(\text{P}_2\text{O}_7)_3(\text{PO}_4)_2$ convex hull methodology.— For each integer $x$ in $\text{Li}_x\text{V}_3(\text{P}_2\text{O}_7)_3(\text{PO}_4)_2$, we computed the ab initio energy of 100 unique orderings of Li\textsuperscript{+} ions\textsuperscript{37} with the lowest electrostatic energy (as determined by Ewald summation).\textsuperscript{38} This strategy was first described by Hautier et al.\textsuperscript{39} For $x = 3$ to $x = 5$, we calculated 25 additional orderings for which we enforced the Li(1) and Li(2) occupancies to be zero. These additional orderings were high in electrostatic energy, but were computed to more thoroughly test which Li arrangement is energetically favorable upon delithiation.

Voltage profiles.— To determine the voltage profiles for the $M = \text{Mo}$ and $M = \{\text{Mo},\text{V}\}$ systems, we did not perform an exhaustive search for the lowest energy Li configurations at intermediate states of delithiation. Instead, we used the lowest-energy Li orderings determined for $\text{Li}_9\text{V}_3(\text{P}_2\text{O}_7)_3(\text{PO}_4)_2$ to compute the voltage profiles for all Mo-doped compounds. For $x < 3$ (for which no V orderings exist), we computed up to 25 Li orderings. Although using the Li orderings determined for $M = \text{V}$ in the Mo-doped compounds is an approximation, we expect that these orderings will be close in energy to the ground state and will produce reasonably accurate voltage profiles. For the mixed Mo-V compounds, our approximation may be less valid as charge ordering of the metals might more strongly influence cation site energies. However, our assumption is somewhat supported by a previous study from Morgan et al., which demonstrated that similar voltage features occur for pure vanadium NASICON cathodes compared to alloyed NASICON cathodes.\textsuperscript{40}

Li-V antisite defect energies.— Vanadium migration upon charging has been linked with irreversible structure changes and capacity loss in layered $\text{Li}_x\text{VO}_2$,\textsuperscript{41} and spinel $\text{Li}_x\text{V}_2\text{O}_4$.\textsuperscript{42} As a first step toward investigating whether V migration might play a role in the observed capacity loss,\textsuperscript{26, 28} for $\text{Li}_x\text{V}_3(\text{P}_2\text{O}_7)_3(\text{PO}_4)_2$, we calculated V-Li antisite defect energies for both fully lithiated and fully delithiated states.

For fully lithiated $\text{Li}_x\text{V}_3(\text{P}_2\text{O}_7)_3(\text{PO}_4)_2$, we started with a 98 atom unit cell and calculated all 108 possible exchanges of one Li site for one V site, i.e., $(\text{Li}_{17}\text{V}_1)(\text{V}_{24})(\text{P}_2\text{O}_7)_3(\text{PO}_4)_2$. For the delithiated state, we calculated all possible exchanges of Li and V in our ground state ordering for $\text{Li}_x\text{V}_3(\text{P}_2\text{O}_7)_3(\text{PO}_4)_2$, which contains one Li(1) site and two Li(3) sites. We additionally calculated orderings in which we exchanged V with an empty Li(2) site (without affecting Li(1) and Li(3) positions).

Phase Diagrams to Assess Thermodynamic Stability and Safety.— We computed 0 K, 0 atm phase diagrams for Li-V-P-O, Li-Mo-P-O, and Li-V-Mo-P-O using methods described in previous publications.\textsuperscript{43, 44} Data was taken from the Materials Project database\textsuperscript{45} using crystal structures from the ICSD.\textsuperscript{34, 35} We assessed safety by calculating the critical $O_2$ chemical potential for oxygen release in the charged state according to the methodology outlined by Ong et al.\textsuperscript{3} Oxygen chemical potential ranges for typical binary oxides can be found in the supporting information of Hautier et al.\textsuperscript{36} We assessed thermodynamic stability of the target compounds by assessing their decomposition energy into known compounds as determined by our phase diagrams. Positive decomposition energies reflect instability of the compound with respect to decomposition; a decomposition energy of zero represents a stable phase.

Diffusion.— We computed migration barriers for Li motion using the Nudged Elastic Band (NEB) method.\textsuperscript{46, 47} We used the GGA functional\textsuperscript{29} (without +U) to avoid charge localization and the need to calculate multiple charge orderings for each NEB. Lattice parameters were fixed at the calculated GGA+U values. All NEB calculations were performed with a single Li vacancy in the primitive cell, Li(1) sites (center).
which contains two formula units and two Li layers as illustrated in Figure 1.

**Experimental.**— $Li_xV_3(P_2O_7)_3(PO_4)_2$ was synthesized by mixing stoichiometric ratios of $Li_2CO_3, NH_4H_2PO_4$, and $V_2O_5$. The powder mixture was ground manually and then dry ball milled in a Paul O. Abbe, Inc., rotary ball mill at 300 RPM for 15 hours. The precursors were pressed into disk-shaped pellets and precipitated at 350 °C for 10 hours under a reducing gas mixture of 3% H$_2$ and 97% Ar. The resulting mixture was re-ground manually using a mortar and pestle, re-pelletized, and subjected to a heat-treatment of 700 °C for 10 hours in an environment of 3% H$_2$ and 97% Ar to produce the desired phase. X-ray characterization was performed using a Rigaku Diffractometer using Cu Kα radiation (Figure 5) with 0.02° scanning steps and 3s sample time. Rietveld refinement and profile matching of the powder diffraction data were performed with XPert HighScorePlus using space group P3c1. Electrochemical tests were performed in a Swagelok style cell using a cathode composed of 80 wt% active material, 15 wt% carbon black, and 5 wt% polytetrafluoroethylene (PTFE) binder mixed using mortar and pestle in an Ar-filled glove box. The total weight of the cathode was approximately 1.83 mg. Lithium metal foil was used as the anode, Celgard 2500 was used as the separator, and 1M LiPF$_6$ in 1:1 ratio of ethylene carbonate:dimethyl carbonate solution was used as the electrolyte. Electrochemical tests were performed at room temperature in galvanstatic mode on a Maccor 4000 tester at C/10 rate (assuming theoretical capacity of 173 mAh/g) between 2.0 and 4.7 V. Before the first charge, the cell was allowed to rest for 6 hours. All cell tests had 1 minute open-circuit rest at the end of each charge and discharge.

**Structure and Stability of Li$_x$M$_3$($P_2O_7$)$_3$(PO$_4$)$_2$**

The lithiated phases Li$_x$M$_3$($P_2O_7$)$_3$(PO$_4$)$_2$—Table I lists computed and known lattice parameters for $M = \{Fe, Al, V, and Mo\}$ versions of the Li$_x$M$_3$($P_2O_7$)$_3$(PO$_4$)$_2$ structure. Our computed lattice parameters are approximately 0.1 Å–0.2 Å larger than those reported in experiments (regardless of metal), which is typical of the GGA functional. Some of the c lattice discrepancy may be attributed to the incomplete description in GGA of van der Waals interactions between layers.

We calculate a density of 2.65 g/cm$^3$ for $M = V$ and 2.92 g/cm$^3$ for $M = Mo$. The lower theoretical density of the Li$_x$M$_3$($P_2O_7$)$_3$(PO$_4$)$_2$ compared with olivine LiFePO$_4$ (3.49 g/cm$^3$) is expected because the olivine structure has very high density compared to other phosphate structures.\(^{25}\) The lower structural density of the Li$_x$M$_3$($P_2O_7$)$_3$(PO$_4$)$_2$ structure leads to a lower theoretical volumetric capacity per electron than LiFePO$_4$. The theoretical volumetric capacities for Li$_x$V$_3$($P_2O_7$)$_3$(PO$_4$)$_2$ (two electrons) and Li$_x$Mo$_3$($P_2O_7$)$_3$(PO$_4$)$_2$ (three electrons) are 460 mAh/cm$^3$ and 662 mAh/cm$^3$ compared with 592 mAh/cm$^3$ for LiFePO$_4$. The high operating voltage of the Li$_x$M$_3$($P_2O_7$)$_3$(PO$_4$)$_2$ compounds may partially compensate for its low structural density. We calculate a theoretical specific energy of 1907 Wh/kg and 2003 Wh/kg for Li$_x$V$_3$($P_2O_7$)$_3$(PO$_4$)$_2$ and Li$_x$Mo$_3$($P_2O_7$)$_3$(PO$_4$)$_2$, respectively, assuming $V^{2+}$ to $V^{3+}$ and $Mo^{3+}$ to $Mo^{4+}$ oxidation. As a comparison, the theoretical specific energy for LiFePO$_4$ is 2035 Wh/kg. However, the full theoretical capacity of Li$_x$M$_3$($P_2O_7$)$_3$(PO$_4$)$_2$ compounds may not be achievable in practice as outlined in the Discussion. Likewise, the practical electrode density of LiFePO$_4$ is severely diminished by the need for carbon coating and nanosizing. The electrode density of Li$_x$M$_3$($P_2O_7$)$_3$(PO$_4$)$_2$ may be competitive with or even exceed that of LiFePO$_4$ if good electrochemical performance can be obtained from large particles or with less conductive carbon. Kuang et al. estimate the electronic conductivity of Li$_x$V$_3$($P_2O_7$)$_3$(PO$_4$)$_2$ to be about an order of magnitude higher than that of LiFePO$_4$.\(^{26}\)

We assessed the thermodynamic stability of the lithiated phases by generating Li-V-P-O and Li-Mo-P-O ground state phase diagrams as described in the methodology. The phase diagrams indicate that in the case of both $M = V$ and $M = Mo$, the reaction competing for stability is:

$$\text{Li}_x\text{M}_3((\text{P}_2\text{O}_7)_3(\text{PO}_4)_2 \rightarrow 2\text{Li}_3\text{PO}_4 + 3\text{Li}_x\text{MP}_2\text{O}_5 \ [4.1]}$$

The calculated reaction energy of 4.1 is ~3 meV/atom for $M = V$ and ~7 meV/atom for $M = Mo$, indicating that there is a mild driving force for decomposition. However, it should be noted that the computed values are within typical GGA+U errors\(^{44,48}\) and also within energy differences caused by finite temperature effects. In previous work, for example, we observed that most phosphate cathodes known to exist experimentally have decomposition energies computed to be less than approximately 10 meV/atom in magnitude.\(^{22}\)

In addition to Li$_x$V$_3$($P_2O_7$)$_3$(PO$_4$)$_2$ and Li$_x$Mo$_3$($P_2O_7$)$_3$(PO$_4$)$_2$, we also evaluated the energies of the mixed metal compounds Li$_y$V$_{1-x}$Mo$_x$($P_2O_7$)$_3$(PO$_4$)$_2$ for $y = 1/3, 1/2, and 2/3$. We calculated all symmetrically distinct orderings of metal substitutions. In all cases, mixing energies are within the convergence limits of our calculations (Table II). Because entropic effects will further stabilize the mixture, our results indicate that a potential Mo/V mixture should not phase separate into Li$_y$V$_{1-x}$Mo$_x$($P_2O_7$)$_3$(PO$_4$)$_2$ and Li$_y$Mo$_{1-x}$V$_x$($P_2O_7$)$_3$(PO$_4$)$_2$. However, like their single-metal counterparts, we expect the mixed-metal systems to be mildly unstable (approximately 4–5 meV/atom) with respect to decomposition into LiPO$_4$, Li$_x$VP$_2$O$_7$, and Li$_x$MoP$_2$O$_7$. It is plausible that the yet undiscovered Li$_y$Mo$_{1-x}$V$_x$($P_2O_7$)$_3$(PO$_4$)$_2$ could be synthesized.

**Structure of delithiated Li$_{y-3/2}$V$_{1/3}$Mo$_{1/2}$($P_2O_7$)$_3$(PO$_4$)$_2$**—To help clarify the observed electrochemical behavior of Li$_x$V$_3$($P_2O_7$)$_3$(PO$_4$)$_2$ upon deintercalation,\(^{26,28}\) we compute the convex energy hull for Li$_y$V$_{1-x}$Mo$_x$($P_2O_7$)$_3$(PO$_4$)$_2$ according to the methodology described in Table II.

| Table II. Calculated 0K mixing energies of Li$_{y-3/2}$V$_{1/3}$Mo$_{1/2}$($P_2O_7$)$_3$(PO$_4$)$_2$ for $y = 1/3, 1/2, and 2/3$. Positive energies indicate unfavorable mixing, but all mixing energies are within the accuracy limits of our calculation. (12 meV/f.u. corresponds to approximately 0.25 meV/atom) Our calculations indicate that there should not be an enthalpic barrier to mixing Mo and V, although there is a mild driving force for decomposition into other solid phases. Table II.

<table>
<thead>
<tr>
<th>Mixing energy</th>
<th>y = 1/3</th>
<th>y = 1/2</th>
<th>y = 2/3</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 meV/f.u.</td>
<td>1 meV/f.u.</td>
<td>−12 meV/f.u.</td>
<td></td>
</tr>
</tbody>
</table>
The $x = 5$ composition is unstable and phase separates into $x = 4$ and $x = 6$ (Figure 3).

At $x = 4$, the lowest energy structure contains one Li(1) site and three Li(3) sites (Figure 3). Our calculations indicate that a Li(3) atom migrates to the Li(1) site when charging from $x = 6$ to $x = 4$, indicating another change in site energetics. As we observed for $x = 8$, reorganization between Li(1) and Li(3) may be facile due to their shared edge. The $x = 4$ ground state provides further evidence that cation-cation interactions play an important role in the Li$_9$V$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$ electrochemical profile.

The $x = 3$ state removes an additional Li(3) site; the fully delithiated Li$_5$V$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$ contains one Li(1) site and two Li(3) sites. However, it should be noted that we find a competing ordering containing three Li(3) sites that is competitive in energy.

In summary, our computations show an ordered state at $x = 8$ due to removal of Li from the Li(1) site; this was initially hypothesized by Xu et al. based on examination of the electrochemical charge/discharge curves and recently found computationally by Kuang et al. While we compute energetics similar to Kuang et al. for removing the first Li site (Li(1) → Li(3) → Li(2)), our detailed study further reveals that these site energetics change as function of Li content. In particular, after removal of the first Li, removal of Li(2) sites become more favorable than removal of Li(3) sites. Were this not the case, the voltage curve would only display two plateaus, corresponding to Li(1) removal followed by removal of five Li(3) sites. Our finding that Li site energetics change with Li content explains why the experimental voltage curve of Li$_9$V$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$ displays three voltage plateaus, corresponding to Li(1) → Li(2) → Li(3) removal.

**Lattice parameter changes upon delithiation.**—Upon intercalation, the resulting lattice parameter changes can sometimes lead to mechanical fracture of particles, leading to capacity loss on cycling. A similar effect might be responsible for irreversible capacity loss observed in Li$_5$V$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$. Therefore, we investigated the change in lattice parameters upon Li removal from Li$_9$V$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$ and Li$_5$Mo$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$ (Figure 4). For Li$_9$V$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$, we calculate that Li removal always leads to $c$-lattice parameter increase, whereas the $a$-lattice parameter decreases or only slightly increases. Our calculations indicate a significant $c$-lattice expansion of 13.7 Å to 14.6 Å during charge. These calculated results disagree qualitatively with recent experiment.
The discrepancy between computation and experiment for the c-lattice parameter likely stems from the inability of standard GGA functionals to accurately model van der Waals interactions between lattice parameter. While the x\textsuperscript{c}tions indicate both the layers in the functionals to accurately model van der Waals interactions between lattice parameter to always increase upon charge, our calculations display a slight decrease of 0.0435 Å. For x < 8, our calculations indicate that the c-lattice parameter expansion and contraction upon delithiation.

The discrepancy between computation and experiment for the c-lattice parameter likely stems from the inability of standard GGA functionals to accurately model van der Waals interactions between the layers in the c-axis. Without these interactions, the attraction between the anion layers may be underestimated, leading to overestimation of the c-lattice parameter as is the case in our study. The discrepancy in the calculated a lattice parameter is not as severe as that for the c-lattice parameter. From x = 9 to x = 8, our calculations indicate that the a lattice parameter expands by 0.0125 Å, in good agreement with the results of Kuang et al.,\textsuperscript{28} which indicate a very slight increase of 0.013 Å. From x = 8 to x = 4, the calculations indicate that the a lattice parameter contracts, which we speculate is due to V\textsuperscript{3+} being oxidized to the smaller V\textsuperscript{4+} and V\textsuperscript{5+}. From x = 4 to x = 3, the calculations indicate a slight increase of the a lattice parameter. While the x = 3 state should contain only smaller V\textsuperscript{5+} ions, the high valence of +5 might lead to electronic repulsion that overcomes ionic size effects. The calculated a lattice parameter trends for x < 8 are in slight disagreement with experiments. From x = 8 to x = 7, the measurements by Kuang et al. indicate that the a lattice parameter slightly increases by 0.039 Å, whereas our calculations display a slight decrease of 0.0435 Å. For x < 7, comparison between experiment and computation is difficult. There are no measurements by Kuang et al. for x = 4, and for 4 < x < 7 the experiments indicate a two-phase mixture, with the two measured phases having very different a lattice parameters (9.812 Å and 9.439 Å at x = 4).\textsuperscript{28} However, it is important to note that despite the individual discrepancies in experimental and computed a and c lattice parameters, the trends in the calculated volume change are still in rough agreement with the experimental data (Table III).

For x = 4, our computations indicate that the a and b lattice parameters become inequivalent (a = 9.771 Å, b = 9.697 Å). At this delithiation level, XRD and HRTEM measurements by Kuang et al.\textsuperscript{28} indicate the presence of a two-phase mixture. Kuang et al.\textsuperscript{28} suggest that one of the phases has P\textsuperscript{3} symmetry and contains two unit cells (i.e., 196 atoms), which was not modeled in this work.

For M = Mo, we evaluated volume changes upon delithiation by using the Li orderings calculated for M = V. For x = 9 to x = 3, we calculate similar contractions of the a-lattice parameter and expansion of the c-lattice parameter as for M = V (Figure 4). However, it is probable that the lattice parameter trends for M = Mo suffer from the same lack of accurate van der Waals characterization as we observed for M = V. In this case, only trends in calculated cell volumes may be useful, as we found for M = V.

For M = Mo, we find that the c-lattice parameter increases with Li extraction for x > 3 but decreases with Li extraction for x < 3. This calculated behavior is in many respects qualitatively similar to what is observed for the complete deintercalation of LiCoO\textsubscript{2}.\textsuperscript{50} The contraction of the c-lattice parameter at low x may be related to two factors. First, the removal of volume-occupying Li atoms could directly cause c-lattice contraction at low x as was previously hypothesized for LiCoO\textsubscript{2}. Second, the anion layers (which include the transition metal) become more charge-neutral upon Li removal, which could reduce repulsion between layers and thereby reduce the c lattice parameter.

Stability during delithiation.— While we previously observed that the fully lithiated Li\textsubscript{9-V\textsubscript{3}(P\textsubscript{2}O\textsubscript{7})\textsubscript{3}(PO\textsubscript{4})\textsubscript{2}} was marginally unstable with respect to the competing reaction 4.1, we find that slightly delithiated Li\textsubscript{3-V\textsubscript{3}(P\textsubscript{2}O\textsubscript{7})\textsubscript{3}(PO\textsubscript{4})\textsubscript{2}} is energetically stable. The Li-V-P-O computed phase diagram indicates that the relevant competing reaction for Li\textsubscript{9-V\textsubscript{3}(P\textsubscript{2}O\textsubscript{7})\textsubscript{3}(PO\textsubscript{4})\textsubscript{2}} is to Li\textsubscript{3-P\textsubscript{2}O\textsubscript{7}}, Li\textsubscript{3}P\textsubscript{2}O\textsubscript{5}, Li\textsubscript{2}V\textsubscript{2}(PO\textsubscript{4})\textsubscript{3}, and two other phases having very different a lattice parameters (9.812 Å and 9.439 Å at x = 4).\textsuperscript{28} However, it is important to note that despite the individual discrepancies in experimental and computed a and c lattice parameters, the trends in the calculated volume change are still in rough agreement with the experimental data (Table III). For x = 4, our computations indicate that the a and b lattice parameters become inequivalent (a = 9.771 Å, b = 9.697 Å). At this delithiation level, XRD and HRTEM measurements by Kuang et al.\textsuperscript{28} indicate the presence of a two-phase mixture. Kuang et al.\textsuperscript{28} suggest that one of the phases has P\textsuperscript{3} symmetry and contains two unit cells (i.e., 196 atoms), which was not modeled in this work.

For M = Mo, we evaluated volume changes upon delithiation by using the Li orderings calculated for M = V. For x = 9 to x = 3, we calculate similar contractions of the a-lattice parameter and expansion of the c-lattice parameter as for M = V (Figure 4). However, it is probable that the lattice parameter trends for M = Mo suffer from the same lack of accurate van der Waals characterization as we observed for M = V. In this case, only trends in calculated cell volumes may be useful, as we found for M = V.

For M = Mo, we find that the c-lattice parameter increases with Li extraction for x > 3 but decreases with Li extraction for x < 3. This calculated behavior is in many respects qualitatively similar to what is observed for the complete deintercalation of LiCoO\textsubscript{2}.\textsuperscript{50} The contraction of the c-lattice parameter at low x may be related to two factors. First, the removal of volume-occupying Li atoms could directly cause c-lattice contraction at low x as was previously hypothesized for LiCoO\textsubscript{2}. Second, the anion layers (which include the transition metal) become more charge-neutral upon Li removal, which could reduce repulsion between layers and thereby reduce the c lattice parameter.
Mo$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$, because Mo can be oxidized to 6+. Removing the final Li in Li$_x$Mo$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$ causes a spike in the instability reaching approximately 90 meV/atom (Figure 7) with respect to Mo(PO$_4$)$_2$ and P$_2$O$_5$. This magnitude of instability could promote capacity fade due to cathode decomposition to inactive phases during cycling.

### Voltage Profiles of Li$_x$M$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$

Using the methodology outlined by Aydinol et al.\(^4\) and our convex hull from Figure 3, we are able to compute voltage profiles for Li$_x$M$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$. We compare our computed results with the experimental data obtained according to the methods described in section 3.7. The cathode sample used for electrochemical testing was confirmed to be single-phase Li$_x$V$_1/3$Mo$_{2/3}$O$_{10}$ by X-ray diffraction with $R_p = 12.529$ and $R_{exp}$ (R expected) = 3.182.

In Figure 6 the computed voltages are displayed for $M = V$ along the side of the experimentally measured voltage during the first cycle from 2.0 V to 4.7 V. We chose this voltage range because previous studies by Kuang et al.\(^26\) demonstrated that charging to higher than 4.8 V results in a discharge curve that is qualitatively different from the first charge curve.\(^26\)

The first voltage step (below $\sim$30 mAh/g on charge) represents removal of Li from the Li(1) site. Our computations underestimate the voltage of this step. Whereas the computations predict a voltage of 3.09 V, we measure an experimental charge voltage of 3.65 V. The discharge voltage is closer to our computation (approximately 3.22 V for the final 30 mAh/g shown), but measurements by Kuang et al.\(^28\) suggest that the electrode might have slightly changed after completing a charge-discharge cycle. Our calculations are thus overstabilizing Li$_x$V$_1/3$Mo$_{2/3}$O$_{10}$ relative to Li$_x$V$_1/3$Mo$_{2/3}$O$_{10}$. Part of the error might be attributed to the fact that our $U$ value, which was calibrated using formation enthalpies for binary vanadium oxides, might be suboptimal for predicting voltages in the Li$_x$M$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$ crystal structure. A higher value of $U$ would raise the voltage,\(^52\) and prior work indicates that appropriate $U$ values in phosphates\(^52,53\) may be higher than those in the oxides.\(^32\) Recent calculations by Kuang et al.\(^28\) on Li$_x$V$_1/3$Mo$_{2/3}$O$_{10}$ indeed predict a higher voltage of 3.4V for the first step using $U$ equal to 4.0. However, it is also possible that the underestimated computed voltage stems from an incomplete understanding of the Li$_x$V$_1/3$Mo$_{2/3}$O$_{10}$ structure, causing it to be understabilized in our calculation. Although we computed 50 Li$_x$V$_1/3$Mo$_{2/3}$O$_{10}$ structures with slightly modified lithium positions to try to find an alternate ground state (see Methodology), we did not find a structure with significantly lower energy than that of the original structure.

Our calculations successfully reproduce the large voltage step between removing the first and second/third Li sites (Figure 6). Our convex hull indicated that this voltage step arises from switching from Li(1) removal to Li(2) removal. Our computed voltage (4.17 V) for the second voltage step is lower than the measured average charge voltage (4.37 V), but closer to the discharge voltage (approximately 4.14 V for the matching step). Our experimental data displays a region of solid solution-like behavior between the first and second plateau that is not reflected in the computation. This might indicate the presence of disorder between Li(1) and Li(2) vacancies. To understand the nature of the solid solution, calculations for $7 < x < 8$ using large supercells may be needed. In addition, subtle effects on the voltage curve often arise from entropic contributions to the free energy that are not modeled in this work. A cluster expansion approach might help reveal the nature of the solid solution.\(^54\)

We calculate an approximately 0.3 V step between removing the third and fourth Li (approximately 87 mAh/g), corresponding to a transition from the V$^{3+/4+}$ to V$^{4+/5+}$ redox couple (Figure 6). This calculated voltage step is in agreement with general results obtained from a large number of vanadium phosphates\(^22\) but is not present in the experimental curves, either in the present study or previously reported experiments.\(^20,28\) It is conceivable that there is disproportionation of V$^{4+/5+}$ in the material as has been previously suggested for vanadium NASICON cathodes,\(^40\) although recent XPS data from Kuang et al.\(^26\) demonstrates that the oxidation state of V transitions from 3+ $\rightarrow$ 4+ $\rightarrow$ 5+ during charge. It therefore remains unclear why there is no observable voltage step at approximately 87 mAh/g in the experiments.

At approximately 100 mAh/g, the experimental charge curve exhibits a small voltage step (Figure 6). This step is not predicted by our computations, and is less pronounced in the electrochemical data reported by Kuang et al.\(^26\). In addition, the capacity extracted from this step appears to be non-reversible. Therefore, this voltage step may represent a side reaction rather than topotactic removal of Li.

In addition to studying $M = V$, we also calculated voltage curves for the hypothetical Mo-doped compounds Li$_x$V$_{1-x}$Mo$_{3+}$O$_{10}$ for $y$ = 1/3, 1/2, 2/3, and 1. The full set of calculated voltage curves are presented in Figure 7. For the pure Mo compound ($y = 1$), we note that in theory up to 9 Li$^+$ may be extracted from the structure as Mo may be oxidized to Mo$^{5+}$. At $x = 6$, we see only a small voltage step of about 0.1 V corresponding to the transition from the Mo$^{5+/6+}$ to the Mo$^{4+/5+}$ redox couple. The small voltage difference between the Mo$^{3+/4+}$ to Mo$^{4+/5+}$ redox couples is typical both in phosphates and in oxides.\(^22\) Figure 7 also demonstrates a larger voltage step at $x = 3$ of approximately 0.5 V, in line with observations that the Mo$^{2+/3+}$ and Mo$^{3+/4+}$ redox couples are approximately 0.3 V apart in phosphates.\(^22\) The large final step at $x = 1$ indicates that removing the final Li$^+$ (from the Li(1) site) leads to an unstable structure. This is also reflected by the sharp increase in the decomposition energy for $x = 0$ (Figure 7).

For the mixed Mo-V compounds, the voltage profile is complex because there exist three distinct Li sites and a total of five active redox couples (V$^{1+/2+}$, V$^{2+/3+}$, Mo$^{1+/2+}$, Mo$^{2+/3+}$, Mo$^{3+/4+}$). By analyzing the calculated final magnetic moments on the transition metal ions, we determined that oxidation of the ions in the mixed compounds occurs in the order: Mo$^{3+/4+}$, V$^{1+/2+}$, Mo$^{2+/3+}$, V$^{2+/3+}$, Mo$^{3+/4+}$. The order is somewhat surprising as we would have expected V$^{2+/3+}$ oxidation to occur after Mo$^{3+/4+}$; data-mined voltages across phosphates demonstrate that the Mo$^{5+/6+}$ couple in general tends to be approximately 0.4 V lower in voltage than V$^{2+/3+}$.\(^22\) It should be noted that GGA+$U$ cannot always be relied upon to localize the hole on the appropriate metal, and the order may change depending on the values of $U$ assigned to Mo and V.

Because we expect Mo voltages to be lower than V voltages,\(^22\) we also expected that, across the same range of $x$, the Mo-doped samples would reduce the average voltage from the pure V sample. This is indeed borne out in the calculations; the average voltage from $x = 9$ to $x = 3$ is reduced by 0.1–0.15 V per 1/3 Mo doped (Figure 7). As the
pure V compound is too high in voltage toward the end of charge, we hypothesized that lowering the average voltage might be beneficial for electrochemical performance. However, this advantage is dampened by two factors. First, the Mo doping reduces the voltage of the initial charge step by 0.3–0.4 V due to activation of the Mo$^{3+}/4+$ couple rather than V$^{4+}/5+$. This is undesirable because the initial V$^{4+}/5+$ experimental voltage of 3.75 V is safe and provides good energy density. Second, although Mo doping theoretically increases the capacity due to the possibility of using the Mo$^{6+}$ redox state, it is unclear that this capacity can be fully achieved in practice. Removing the final Li$^+$ sites (below about $x = 3$) from the Mo-doped materials leads to unstable structures that increase the voltage to over 4.6 V (Figure 7). Therefore, although Mo doping reduces the average voltage, and theoretically may exchange more Li$^+$, the capacity near the end of charge may be unusable due to high voltage. We discuss this trade-off in greater detail in the Discussion.

**Safety and Stability of the Delithiated Phases**

As Li ion batteries become integrated into automotive applications, the issue of safety upon heating becomes of great concern as O$_2$ released from the cathode can react with the electrolyte to cause thermal runaway. Recently, Ong et al. presented a computational methodology to evaluate the intrinsic safety of Li ion battery cathodes by calculating the critical oxygen chemical potential ($\mu_{\text{O}_2\text{crit}}$) at which charged cathodes release O$_2$. In their study, Ong et al. observed that MnPO$_4$ was much more prone to O$_2$ release (and thereby less safe) than FePO$_4$, against the intuition of many researchers in the field but in agreement with experimental measurements. Subsequently, Hau- tier et al. evaluated on a large scale the safety of all interesting battery redox couples in the phosphates chemistry. In particular, they observed that V$^{5+}$ and Mo$^{6+}$ have on average a similar $\mu_{\text{O}_2\text{crit}}$. Using the same methodology, we evaluated the intrinsic safety of delithiated Li$_3$V$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$ and the effect of Mo substitution.

Our calculations indicate that safety is indeed a concern for delithiated Li$_3$V$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$, despite the presence of phosphate groups in the structure. Delithiated Li$_3$V$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$ is thermodynamically unstable by 32 meV/atom, and its decomposition is predicted to release O$_2$ gas according the reaction:

$$\text{Li}_3\text{V}_3\text{(P}_2\text{O}_7\text{)}_3\text{(PO}_4\text{)}_2 \rightarrow 2\text{VP}_2\text{O}_7 + 1/2 \text{O}_2 + \text{VOPO}_4 + 3\text{LiPO}_3$$

where the O$_2$ energy has been adjusted for ambient conditions using the correction derived by Wang et al. Because fully charged Li$_3$V$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$ thermodynamically favors O$_2$ release, its safety will depend on kinetic limitations to O$_2$ release rather than a thermodynamic ‘safeguard’. The intrinsic safety concern of this material may limit the ability to reduce particle size to improve electrochemical performance, as smaller particles increase reactivity of the cathode with the electrolyte.

We note that Mo doping improves the safety of Li$_3$V$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$. Although delithiated Li$_3$Mo$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$ is more thermodynamically unstable (46 meV/atom) than Li$_3$V$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$, its decomposition products do not include O$_2$ gas:

$$\text{Li}_3\text{Mo}_3\text{(P}_2\text{O}_7\text{)}_3\text{(PO}_4\text{)}_2 \rightarrow \text{Mo}_2\text{P}_4\text{O}_{15} + \text{LiMo(PO}_4\text{)}_2 + 2\text{LiPO}_3$$

Charged Li$_3$Mo$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$ is therefore predicted not to release O$_2$ under ambient conditions. The $\mu_{\text{O}_2\text{crit}}$ for oxygen release of Li$_3$Mo$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$ is $-0.96$, similar to the value we compute for delithiated NASICON V$_2$(PO$_4$)$_3$ ($\mu_{\text{O}_2\text{crit}} = -1.06$), which has been reported to decompose at approximately 200°C (with the first exothermic peak occurring at 220°C) in the presence of electrolyte.

Fully delithiated Mo$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$ also is not predicted to release O$_2$ under ambient conditions, again producing solid reaction products (driving force is 88 meV/atom):

$$\text{Mo}_3\text{(P}_2\text{O}_7\text{)}_3\text{(PO}_4\text{)}_2 \rightarrow \text{Mo}_2\text{P}_4\text{O}_{15} + \text{LiMo(PO}_4\text{)}_2 + \text{2LiPO}_3$$

The $\mu_{\text{O}_2\text{crit}}$ of Mo$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$ is $-0.12$, indicating that its safety should be comparable to charged Li$_3$CoO$_2$, which has been reported to decompose between 170 and 230°C. Thus, while the Mo-doped cathodes demonstrate a higher driving force for decomposition in the charged state, the decomposition products are solid phases which are less likely to be of concern for cathode safety.
Li-V Antisite Defects

When charging to 4.8 V, Kuang et al. report that the subsequent discharge of Li$_9$V$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$ displays different electrochemical behavior. In particular, the discharge voltage drops approximately 0.5 V and voltage plateaus become less pronounced.\(^{26}\) Despite the shift in electrochemistry, Kuang et al.’s initial study does not report any significant changes in the XRD pattern of the cathode before and after electrochemistry. Kuang et al.\(^{25}\) argue that structural integrity is still maintained. We investigated whether the differences in charge and discharge electrochemical behavior might be due to an exchange of Li and V sites. Such antisite defects could affect the energetics of charging/discharging while perhaps being difficult to detect via XRD.

Table IV lists the calculated antisite defect energies for fully delithiated and fully lithiated Li$_9$V$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$ in which one Li and one V were exchanged in the 98-atom unit cell. In the lithiated state, the most favorable antisite defect is exchange of V$^{3+}$ with the Li$^{2+}$ site energy of 1.43 eV. This energy is quite high and should lead to low defect concentrations. In the dilute limit, the defect concentration can be expressed as:

\[
c = \frac{N}{V} \exp \left( -\frac{E_F}{kT} \right)
\]

where \(c\) is the defect concentration, \(N/V\) is the number of possible defect configurations per unit volume, \(E_F\) is the defect formation energy, \(k\) is the Boltzmann constant, and \(T\) is temperature. For one formula unit of Li$_9$V$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$, there exist six potential exchanges of Li(2) and V$^{3+}$ sites; using the computed formula unit volume, the defect concentration \(c\) would be an extremely low 0.007 cm$^{-3}$.\(^{22}\) We did not consider the possibility of Li and V exchange simultaneously accompanied by Li site rearrangement.

Given the extremely high calculated antisite defect energies in the fully charged and fully discharged states (1.43 eV to 4.5 eV), we speculate that the presence of antisite defects is not responsible for the change in the electrochemical profile of Li$_9$V$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$. However, it should be noted that antisite defects were not investigated for intermediate lithiations, and it cannot be ruled out that the antisite defect energy is more favorable at an intermediate lithium level. It is also possible that other types of defects may be present in this material and further exploration of the defect chemistry of Li$_9$V$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$ may yield new insights.

**Table IV. Antisite defect energies (eV) of V exchanged with the given Li site.** For Li$_9$V$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$, no Li(2) sites exist in our equilibrium structure; the calculation marked with an asterisk (*) refers to V$^{3+}$ exchanging with a vacancy on the Li(2) site.

<table>
<thead>
<tr>
<th>Li(1)</th>
<th>Li(2)</th>
<th>Li(3)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Li$_9$V$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$</td>
<td>2.538</td>
<td>1.438</td>
</tr>
<tr>
<td>Li$_7$V$_5$(P$_2$O$_7$)$_3$(PO$_4$)$_2$</td>
<td>4.370</td>
<td>4.512$^*$</td>
</tr>
</tbody>
</table>

**Diffusion**

**Diffusion in Li$_9$V$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$.** The crystal structure of Li$_9$V$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$ contains Li layers and large c-axis channels that contain only Li (Figure 1). A topological depiction of Li sites and connections between sites within the Li-layer is illustrated in Figure 8. The main features are rings of Li(3) sites with an Li(1) site in the center. The rings are connected to one another via Li(2) sites.

The most obvious pathway for Li diffusion is within the large c-axis channels (between layers). For this pathway, we computed the Li vacancy migration barrier to be 740 meV (Table V), indicating that channel diffusion is likely slow.

An alternate diffusion path for Li is to diffuse across the Li layer. However, both our GGA+$U$ calculations and our NEB calculations indicate that Li vacancies are not stable at Li(3) sites and relax easily to Li(1) sites. This restricts the number of potential diffusion paths. One plausible diffusion path within the Li layer is a simultaneous Li(1) → Li(3) and Li(3) → Li(2) migration of the vacancy so that the vacancy does not rest on an Li(3) site. We calculated the total activation energy of this transition to be extremely large at nearly 1.3 eV (Table V).

Much of this net barrier can be traced to the fact that a vacancy in the Li(2) site is thermodynamically much higher in energy than a vacancy in the Li(2) site. The Li(2) site energy compared to the Li(1) site energy is 959 meV higher according to GGA+$U$ calculations, and 978 meV in the GGA calculations considered here. The net diffusion of Li(1) vacancies to Li(2) sites is largely hindered by the much higher site energy of vacancies in the Li(2) site.

A third potential path for Li(1) vacancy diffusion is a simultaneous hop involving 4 Li ions: Li(1) → Li(3), Li(3) → Li(2), Li(2) → Li(3), and Li(3) → Li(1). While it appears unlikely that four Li ions are migrating simultaneously, the balance between entering and departing Li from the high-energy Li(1) site may produce a lower net migration barrier. We did not investigate this complex transition in this study.

**Diffusion in Li$_9$V$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$.**— We calculated migration barriers in Li$_9$V$_3$(P$_2$O$_7$)$_3$(PO$_4$)$_2$ assuming vacancies in all Li(1) sites. Thermodynamically, we expect the Li(2) site to be removed next, as discussed previously. We evaluated several diffusion paths for which the Li(2) vacancy first migrates to the closest Li(3) site, and then migrates to an adjacent Li(3) site. This series of hops is sufficient to form a percolating diffusion network through the Li layer (see Figure 8).

For the first portion of the diffusion path, Li(2) → Li(3) vacancy migration, we calculated an activation barrier of 518 meV. For the second portion of the diffusion path, Li(3) → Li(2) migration, we evaluated four different hops. The first hop tested is through the Li channel and crosses Li layers, similar to Li(1) diffusion in the channel.

The remaining three hops are illustrated in Figure 9. Each Li(3) site is closely coordinated to three oxygen ions which form a ring around...
the large c-axis channels. The first Li(3) → Li(3) migration pathway we tested consists of a Li-ion entering into the channel by passing between its neighboring oxygen ions, then exiting the channel via an analogous path (‘inside’ path). The second pathway consists of traveling around the exterior of the channel (‘outside’ path). The third pathway follows a S-shape which is interior to the channel near one Li(3) site and exterior near the other Li(3) site, transitioning between the two by passing through the oxygen triangle between the Li(3) site-coordinated oxygen triangles.

For the Li(3) → Li(3) migration across Li layers, the migration barrier of 1534 meV and net activation energy of 1691 meV are extremely high (Table V). The high migration barrier is not surprising because it essentially involves promoting a Li(3) vacancy to the Li(1) site and then Li(1) vacancy in-channel diffusion. From our results for the fully lithiated case, we can estimate the first part of this migration to be approximately 442 meV and the latter to be 740 meV (Table V).

For the three remaining Li(3) → Li(3) paths, our calculations indicate that the most favorable transition occurs via the ‘inside’ path with a low net activation energy of 465 meV (Table V). The S-route and outside migration paths have higher activation energies of 646 meV and 745 meV, respectively.

The energy profile of the migration path from Li(2) to Li(3) is plotted in Figure 10. Our results indicate that the rate-limiting step should be the first portion of Li(2) → Li(3) diffusion with an activation barrier of 518 meV.

Our calculations on Li9V3(P2O7)3(PO4)2 indicate very slow diffusion within the Li-layer (1.3 eV barrier) and faster but still sluggish inter-layer diffusion (740 meV). In contrast, our calculations on Li9V3(P2O7)3(PO4)2 indicate reasonably quick diffusion within the Li-layer (518 meV) and very slow inter-layer diffusion (1.7 eV). The discrepancy can be understood simply from the large difference in site energies. When more than 8 Li are present per formula unit, vacancies are only expected on the Li(1) sites, and in-layer diffusion is sluggish because it requires traversing an Li(2) site. When fewer than 8 Li are present per formula unit, all Li(1) sites are vacant and additional vacancies will occupy either Li(2) or Li(3) sites. These additional vacancies may move freely within the layer, but inter-layer diffusion is sluggish because it first requires moving a Li from a Li(3) site into a vacant Li(1) site.

Our calculations are in reasonable agreement with experimental diffusivity measurements by Poisson et al.24 on the isostructural Li9Al3(P2O7)3(PO4)2 and Li9Fe3(P2O7)3(PO4)2 where the inter-layer activation barriers were determined to be 1.22 eV and 1.20 eV, respectively, and the in-layer activation barriers were determined to be 660 meV and 690 meV, respectively. Although it is not known whether samples from Poisson et al. might have been slightly Li deficient, the activation barriers they report fall between our calculated values for Li9V3(P2O7)3(PO4)2 and Li9V3(P2O7)3(PO4)2.

The calculated in-plane diffusion activation energy for Li9V3(P2O7)3(PO4)2 is higher than some commercialized cathode materials, which have activation barriers of approximately 400 meV or less.59–61 However, the higher activation barrier may be partially mitigated by the defect tolerant 2D diffusion network and the large diffusion distance per 518 meV activation (over 9 Å). It would be interesting to investigate the effect of layer spacing on diffusivity as was previously conducted by Kang et al. for the layered oxides.62

Given the large calculated migration barrier for Li(1) diffusion, it is somewhat surprising that the experimental data reported by Kuang et al. displays only a small overpotential for the Li9V3(P2O7)3(PO4)2 to Li9V3(P2O7)3(PO4)2 voltage step at a moderate C/10 rate.26 Combined with the evidence that theory underestimates the magnitude of this voltage step, this suggests that the Li9V3(P2O7)3(PO4)2 to Li9V3(P2O7)3(PO4)2 might involve complicated intercalation behavior that would benefit from further study.

### Discussion and Cathode Design

From a design perspective, Li9M3(P2O7)3(PO4)2 is a promising cathode for optimization amongst potential phosphate materials. A recent analysis by Hautier et al. demonstrates that amongst one-electron phosphates, only chemistries utilizing the Mn2+/3+ and Cu1+/2+ redox couples are capable of surpassing LiFePO4’s specific energy while retaining a reasonable voltage (Mn2+/3+ in the form of LiMnP04 is currently the subject of intense study, and Cu1+/2+ cathodes will likely be difficult to design). Beyond the one-electron phosphates, Hautier et al. suggested that the V4+/5+ and Mo3+/4+ redox couples are promising avenues to design phosphates with high specific
Our compositional analysis of Mo-doped samples reveals that it increases the magnitude of voltage steps during cycling. In particular, the first lithiation step drops by 0.3–0.4 V, making its voltage too low, and the last lithiation step rises close to or above 5 V (Figure 7). The high final voltage step is not intrinsic to the Mo5+/Mo3+ couple but rather due to a high energy needed to extract the final Li+ sites from the Li9Mo3(P2O7)3(PO4)2 structure. This hypothesis is supported by Figure 7, which demonstrates that the voltage of the last Mo5+/Mo3+ step in Mo-doped samples varies from approximately 4.5 V to approximately 6 V depending on the x value at which the Li site is removed. This interpretation is also consistent with data-mined voltages for Mo5+/Mo3+ in phosphates by Hautier et al. that indicate Mo5+/Mo3+ voltages are typically approximately 4 V in the absence of strong Li+ site effects.

The hypothetical Mo-doped samples have slightly higher decomposition energies and slightly higher volume changes than the pure V version (Figure 7). While the decomposition energies of Mo-doped Li9V3(P2O7)3(PO4)2 are higher, the decomposition products are solid phases that should lead to better intrinsic safety with respect to O2 release (Figure 7). The higher values of volume change for Mo-doped compounds may be some cause for concern, but may need to be validated through experimental studies or further computational studies that include explicit van der Waals contributions to the energy.

Although the pure V and pure Mo compounds provide in theory 173 mAh/g and 226 mAh/g of capacity, respectively, it is not clear that the full theoretical capacities can be reversibly and safely attained in practical cells. To evaluate more quantitatively the relative benefits and disadvantages of Mo-doping, we establish several design criteria to be met over the entire intercalation process:

- **Voltage must be between 3.0 V and 4.6 V**
- **Intrinsic safety $\mu_{O2-cm}$ must be less than zero** (no thermodynamic driving force for O2 release under ambient conditions)
- **Overall volume change must be under 10%**

While these are fairly inclusive criteria, our goal is to allow for some error in the calculations to avoid excluding any potentially promising candidates. We note that an upper cutoff voltage of 4.6 V was the highest voltage demonstrated by Kuang et al. to demonstrate good cyclability.

We present in Table VI the range of $x$ for Li9V3−xMo3x(P2O7)3(PO4)2 for which each design criterion is met. We then define a "usable intercalation range" by determining the range of $x$ that meet all design criteria. It is important to note that other factors, such as Li+ diffusivity, may also play a role in determining usable capacity. For this analysis, we have ignored potential diffusion.
Table VI. Lithiation ranges for which $Li_xV_3(P_2O_7)\text{P}(PO_4)_2$ (for $y = 0, 1/3, 1/2, 2/3, \text{ and 1}$) meet the design criteria specified in the columns. We define a usable intercalation range for each material as the intercalation range that meets all design criteria. We find that only $y = 2/3$ doping expands the usable range of $Li_xV_3(P_2O_7)\text{P}(PO_4)_2$.

<table>
<thead>
<tr>
<th>Voltage</th>
<th>Safety</th>
<th>Volume</th>
<th>Usable range</th>
</tr>
</thead>
<tbody>
<tr>
<td>3.0–4.6 V</td>
<td>$\mu_{02-\text{em}} &lt; 0$</td>
<td>Change &lt;10%</td>
<td>$x = 9–4$ (5 Li$^{+}$)</td>
</tr>
<tr>
<td>$Li_xV_3(P_2O_7)\text{P}(PO_4)_2$</td>
<td>$x = 9–5$</td>
<td>$x = 9–3$</td>
<td>$x = 9–4$ (5 Li$^{+}$)</td>
</tr>
<tr>
<td>$585 \text{ Wh/kg}$</td>
<td>$144 \text{ mAh/g}$</td>
<td>$111 \text{ mAh/g}$</td>
<td>$135 \text{ mAh/g}$</td>
</tr>
<tr>
<td>$Li_xV_3\text{Mo}_1(P_2O_7)\text{P}(PO_4)_2$</td>
<td>$x = 8–2$</td>
<td>$x = 9–2$</td>
<td>$x = 8–4$ (4 Li$^{+}$)</td>
</tr>
<tr>
<td>$466 \text{ Wh/kg}$</td>
<td>$111 \text{ mAh/g}$</td>
<td>$115 \text{ mAh/g}$</td>
<td>$159 \text{ mAh/g}$</td>
</tr>
<tr>
<td>$Li_xV_3\text{Mo}_{0.5}(P_2O_7)\text{P}(PO_4)_2$</td>
<td>$x = 8–1.5$</td>
<td>$x = 9–1.5$</td>
<td>$x = 8–3$ (5 Li$^{+}$)</td>
</tr>
<tr>
<td>$576 \text{ Wh/kg}$</td>
<td>$135 \text{ mAh/g}$</td>
<td>$670 \text{ Wh/kg}$</td>
<td>$670 \text{ Wh/kg}$</td>
</tr>
<tr>
<td>$Li_xV_3\text{Mo}_2(P_2O_7)\text{P}(PO_4)_2$</td>
<td>$x = 8–2$</td>
<td>$x = 9–1$</td>
<td>$x = 8–2$ (6 Li$^{+}$)</td>
</tr>
<tr>
<td>$503 \text{ Wh/kg}$</td>
<td>$127 \text{ mAh/g}$</td>
<td>$670 \text{ Wh/kg}$</td>
<td>$670 \text{ Wh/kg}$</td>
</tr>
</tbody>
</table>

limitations of the Li(1) site. Therefore, our analysis is meant to represent a ‘best-case’ scenario.

We predict that full capacity will not be reversibly and safely attainable for any of the $Li_xM_x(P_2O_7)\text{P}(PO_4)_2$ materials tested. The pure V material, $Li_xV_3(P_2O_7)\text{P}(PO_4)_2$, does not meet our criteria for O$_2$ release at full charge, leading to a ‘best-case’ predicted capacity of 144 mAh/g or 5 Li$^{+}$. High voltage is also a concern for the pure V material as we calculate the last voltage step to be at 4.59 V, and our calculations were observed to slightly underestimate experimental voltages in the high-voltage regime. Thus far, 5 Li$^{+}$ has been the maximum capacity of $Li_xV_3(P_2O_7)\text{P}(PO_4)_2$ reported in experiments.

With the exception of $y = 2/3$, our calculations indicate that Mo doping will not expand the number of usable Li that may be extracted from $Li_xV_3\text{Mo}_y(P_2O_7)\text{P}(PO_4)_2$. For $y = 1/2$ and $y = 1$, predicted voltage and safety concerns limit the usable range to 5 Li$^{+}$, equivalent to the case of $Li_xV_3(P_2O_7)\text{P}(PO_4)_2$. However, even if the full usable range of 5 Li$^{+}$ could be reversibly extracted from the Mo-doped samples, these materials will exhibit a lower gravimetric and volumetric capacity than their pure V counterpart due to the greater weight of Mo and the larger unit cell of Mo-doped materials (Table VI). They might, however, display other advantages such as a higher diffusivity due to larger lattice parameters of the unit cell.

For $y = 2/3$, we predict that up to 6 Li$^{+}$ may be extracted within the guidelines of our design criteria. The capacity over this range is 158.9 mAh/g at an average of 4.2 V, providing an overall theoretical specific energy of approximately 670 Wh/kg (over 10% improvement relative to LiFePO$_4$). Our calculations indicate that $Li_xV_3\text{Mo}_2(P_2O_7)\text{P}(PO_4)_2$ is a promising material for future experimental investigation.

While we studied many aspects of $Li_xV_3(P_2O_7)\text{P}(PO_4)_2$, several areas would benefit from further investigation. In particular, further clarifying the diffusion paths and diffusion barriers in this material could yield new ideas for optimization. As one example, tuning the c-lattice parameter to enhance 2D diffusion in layered materials has been investigated previously and may also be relevant for $Li_xV_3(P_2O_7)\text{P}(PO_4)_2$. Finally, while we focused on Mo-doping to reduce voltage, recent computational studies in silicates have suggested N and F doping as a strategy to reduce end-of-charge-voltage. This may be an alternative strategy to apply to $Li_xV_3(P_2O_7)\text{P}(PO_4)_2$.

Conclusions

$Li_xM_y(P_2O_7)\text{P}(PO_4)_2$ is a new and promising compound family for Li ion battery cathodes suggested by high-throughput computation which have been successfully synthesized and tested. We present the first detailed computational investigation of $Li_xM_y(P_2O_7)\text{P}(PO_4)_2$ for $M = \{\text{Mo, V}\}$. For $M = V$, we find that the first voltage step corresponds to Li(1) removal and the second and third steps correspond to Li(2) removal. Further deintercalation leads to removal and rearrangement of the Li(3) and Li(1) sites. We find that the relative energies of the Li(1), Li(2), and Li(3) sites change qualitatively with lithiation level, and that this effect is crucial to predicting the steps in the voltage curve of $Li_xV_3(P_2O_7)\text{P}(PO_4)_2$.

For $Li_xV_3(P_2O_7)\text{P}(PO_4)_2$, we determined that the experimentally-observed capacity loss upon cycling is likely not the result of cathode decomposition to other phases. In addition, we calculate only small overall voltage changes, indicating that mechanical fracture of particles may not be the main cause of capacity loss upon cycling. We concluded that Li vacancy diffusion within the channel should be slow, but diffusion within the layer (assuming Li(1) vacancies) should be moderately fast. Finally, we determined that fully charged $Li_xV_3(P_2O_7)\text{P}(PO_4)_2$ may suffer from poor intrinsic safety.

Mo-doping onto the M site should improve the safety of $Li_xM_y(P_2O_7)\text{P}(PO_4)_2$, but might lead to detrimental voltage steps during charge/discharge. We determined that a mixture of 2/3 Mo and 1/3 V on the M site could potentially produce a usable specific energy that surpasses that of LiFePO$_4$ by over 10%. Further investigation of diffusion paths and anion doping might reveal alternate strategies to improve the electrochemical performance of the promising $Li_xM_y(P_2O_7)\text{P}(PO_4)_2$ compound family.

Acknowledgments and Funding

The authors thank Robert Doe, Xiaohua Ma, Shyue Ping Ong, and Jae Chul Kim for their efforts on this collaborative project and Robert Daniel for performing preliminary optimization studies of the V-based material. We acknowledge funding from Umicore and Robert Bosch as well as the Department of Energy Basic Energy Sciences under contract #DE-FG02-96ER45571. A. Jain acknowledges funding from the DOE CSGF grant #DE-FG02-97ER25308. This research was supported in part by the National Science Foundation through TeraGrid resources provided by Texas Advanced Computing Center (TACC) under grant number TG-DMR970008S.

References
