Atmospheric characterization of cold exoplanets using a 1.5-m coronagraphic space telescope

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Atmospheric characterization of cold exoplanets using a 1.5-m coronagraphic space telescope

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ABSTRACT

Context. High-contrast imaging is currently the only available technique for the study of the thermodynamical and compositional properties of exoplanets in long-period orbits, comparable to the range from Venus to Jupiter. The SPICES (Spectro-Polarimetric Imaging and Characterization of Exoplanetary Systems) project is a coronagraphic space telescope dedicated to the spectro-polarimetric analysis of gaseous and icy giant planets as well as super-Earths at visible wavelengths. So far, studies for high-contrast imaging instruments have mainly focused on technical feasibility because of the challenging planet/star flux ratio of $10^{-8}$–$10^{-10}$ required at short separations (200 mas or so) to image cold exoplanets. However, the main interest of such instruments, namely the analysis of planet atmospheric/surface properties, has remained largely unexplored.

Aims. The aim of this paper is to determine which planetary properties SPICES or an equivalent direct imaging mission can measure, considering realistic reflected planet spectra and instrument limitation.

Methods. We use numerical simulations of the SPICES instrument concept and theoretical planet spectra to carry out this performance study. We also define a criterion on the signal-to-noise ratio of the measured spectrum to determine under which conditions SPICES can retrieve planetary physical properties.

Results. We find that the characterization of the main planetary properties (identification of molecules, effect of metallicity, presence of clouds and type of surfaces) would require a median signal-to-noise ratio of at least 30. In the case of a solar-type star ≤10 pc, SPICES will be able to study Jupiters and Neptunes up to ∼5 and ∼2 AU respectively, because of the drastic flux decrease with separation. It would also analyze cloud and surface coverage of super-Earths of radius 2.5 Earth radii at 1 AU. Finally, we determine the potential targets in terms of planet separation, radius and distance for several stellar types. For a Sun analog, we show that SPICES could characterize Jupiters ($M\geq 30$ Earth masses) as small as 0.5 Jupiter radii at ≤2 AU up to 10 pc, and super-Earths at 1–2 AU for the handful of stars that exist within 4–5 pc. Potentially, SPICES could perform analysis of a hypothetical Earth-size planet around α Cen A and B. However, these results depend on the planetary spectra we use, which are derived for a few planet parameters assuming a solar-type host star. Grids of model spectra are needed for a further performance analysis. Our results obtained for SPICES are also applicable to other small (1–2 m) coronagraphic space telescopes.

Key words. planetary systems – methods: numerical – techniques: high angular resolution – techniques: image processing – techniques: imaging spectroscopy

1. Introduction

The exoplanet field in astrophysics is extremely rich and diverse. From detection to characterization, many techniques are being used or developed to address the fundamental questions about planetary formation and evolution. Exoplanets span a number of categories much larger than the solar system’s planets do. Since the first discovery, several unexpected types of exoplanets were found from the hot Jupiters (Mayor & Queloz 1995) which are very close to their host stars (≤0.05 AU) to the population of super-Earths (massive telluric planets) which starts to emerge from radial velocity surveys (hereafter RV, Mayor et al. 2011) and transit surveys (e.g., Léger et al. 2009; Charbonneau et al. 2009; Batalha et al. 2011; Borucki et al. 2012). There are so many planet categories already detected even with the detection biases of the current methods (RV, transits, imaging, microlensing) that several instruments/missions will be needed to cover the whole field. Methods such as RV and transits appear to be effective at probing for large close-in exoplanets, and current efforts are to expand their sensitivity to longer-period and smaller exoplanets (Udry & Santos 2007; Seager & Deming 2010). The detection and characterization of long-period/wide-orbit
(≥1 AU) planets are, however, still difficult to accomplish. On the one hand, it requires long-duration monitoring with very stable instruments to detect them from a RV or transit survey. On the other hand, direct imaging has to tackle the high contrast at small angular separation that exist between the planet and its host star.

An extrapolation of the period distribution of giant planets discovered by RV surveys suggests that a large population of these objects at separations larger than 5 AU still remains to be revealed (Marcy et al. 2005). These planets, in particular the population between 5 and 20 AU, are very important for constraining theoretical mechanisms of planetary formation, since it may reside at the boundary between the core-accretion and disk instability regimes (Alibert et al. 2011; Boss 2011). When it comes to the atmospheric characterization of these planets, direct imaging will probably be the most productive technique. Since 2005 (Chauvin et al. 2005; Neuhausser et al. 2005), several massive giant planet candidates were imaged around young stars (<200 Myr), the most emblematic being the four planets around HR 8799 (Marois et al. 2008; Marois et al. 2010) and β Pictoris b (Lagrange et al. 2009, 2010). We note that the planetary nature of the Fomalhaut companion (Kalas et al. 2008) has been recently questioned (Janson et al. 2012). Following these discoveries, spectra were obtained for a few planets (e.g., Mohanty et al. 2007; Janson et al. 2010; Patience et al. 2010; Bowler et al. 2010). A first generation of instruments precisely optimized for the detection and spectral characterization at near- and mid-infrared (IR) wavelengths of young giant planets will see first light in the present decade: SPHERE (Beuzit et al. 2008), GPI (Macintosh et al. 2008), HiCIAO (Hodapp et al. 2008), P1640 Phase II (Hinkle et al. 2011) and FLAO (Esposito et al. 2010) on ground-based telescopes, and JWST (Clampin 2010) and SPICA Coronagraph Instrument (Enya et al. 2011) in space. In the next decade, planet finders on Extremely Large Telescopes, such as EPICS (Kasper et al. 2010) and PFI (Macintosh et al. 2006), may offer the ability to observe mature gas giants, ice giants and possibly super-Earths in the near-IR. Detailed studies were performed to consider the feasibility of large aperture coronagraphs and large baseline interferometers for the detection of Earth twins from space. These studies identified areas of technological development that need to be first addressed, which will delay the realization of Terrestrial Planet Finder missions until ~2025–2030. Meanwhile, observations have demonstrated the extreme diversity of planets. This led to a growing consensus within the community that we will need to study all planet types in order to have a complete understanding of their formation and evolution (Schneider et al. 2008). To address some parts of these questions, a family of small space missions (mainly coronagraphs) have been proposed (Guyon et al. 2010b; Traub et al. 2010) for analyses of ice giants and super-Earths. The study of these missions has mainly focused on technical feasibility, as it is a challenge to achieve large contrast close to a bright star (Trauer & Traub 2007; Guyon et al. 2010a; Belikov et al. 2010). Another area of study is the estimated number of observable exoplanets of a given type (Trauer et al. 2010; Guyon et al. 2010b), based on assumptions of their density distribution. Cahoy et al. (2009) consider signal-to-noise ratios (SNRs) of broad-band (R = 5) photometric measurements assuming planets with grey albedos. The main interest of such missions, the atmospheric characterization, however, has remained highly unexplored so far. Cahoy et al. (2010) analyze colors and coarse spectra (R = 5 and R = 15) of Jupiter and Neptune atmosphere models, but without including instrument limitations such as throughput and noise. From the colors of solar system planets, Traub (2003) suggested that for planets too faint for spectrometry, even coarse colors could help to distinguish between planet types. Cahoy et al. (2010) showed that while a color criterion could not be a means to uniquely distinguish between planet types, due to the intertwined contributions of factors such as metallicity and planet-star separation, colors would still provide some constraints on possible planet types.

Among all of these space coronagraph concept missions, the most recent, SPICES (Spectro-Polarimetric Imaging and Characterization of Exoplanetary Systems) was submitted to the ESA Cosmic Vision call for medium-class missions in 2010 by a consortium of European institutes with American and Japanese participations1 (Boccaletti et al. 2012). SPICES has a twofold motivation: 1) the systematic atmospheric characterization of gas and ice giants as well as super-Earths in the solar neighborhood, and 2) the development and validation of key technologies in order to prepare future direct imaging projects dealing with Earth twins spectral characterization. The science objectives and the technical concept of SPICES are described in Boccaletti et al. (2012). The main science driver is the study of planetary systems as a whole for the understanding of planet formation and evolution. With a maximum imaged field of view of ~13″, SPICES will focus on targets previously identified using other methods (planets and circumstellar disks), but can also detect new planets such as outer planets in known planetary systems and exozodiacal disks <100 zodis. A preliminary estimation of the number of characterizeable planets gives an order of magnitude of 100 objects for an allocated time of three years over the five years of the mission (Boccaletti et al. 2012). The main purpose of the instrument is to obtain flux and polarization spectra at visible wavelengths of cold/mature exoplanets, especially those previously discovered by RV surveys (Udry & Santos 2007) or astrometry with Gaia (Casetano et al. 2008). These surveys will provide the orbital elements and minimum mass of planets, but not the radius which determines the amount of reflected light together with the albedo. It is therefore essential to perform accurate measurements of spectra to possibly distinguish between planet types.

In this work, we have developed a numerical simulation to model the instrument concept of SPICES. Under realistic assumptions of noise, instrument performance and reflected exoplanetary spectra, we test the ability to distinguish between spectra of planets differing in surface gravity, atmospheric composition, metallicity, cloud coverage and surface type. We do not consider polarized light in this paper and leave such a study for future work. Our primary goal is not to refine the instrument concept given in Boccaletti et al. (2012). Firstly, we investigate the exoplanet detection space realistically, and then we may use our results to update the design. Our work will also be beneficial to other space coronagraph proposals. In Sect. 2, we describe the numerical model and the assumptions we use for our study. In Sect. 3, we analyze the effects of speckle noise, read-out noise, exozodis and photon noise on the performance. We specify what kinds of planets can be detected in each case. We then study the impact of the spectral type of the host star. In Sect. 4, we define a criterion that gives the required flux accuracy that the instrument has to produce in order to disentangle

\[ R = \frac{P_{\text{obs}}}{P_{\text{source}}} \]
spectra for similar planet types (Jupiters, Neptunes or super-Earths), but with different values of physical parameters (composition, metallicity or cloud and surface coverage). We conclude that our instrument fulfills these constraints for most of the considered cases. In Sect. 5, we generalize our results to other stellar types to define a parameter space of potential targets.

2. Models

2.1. Numerical model of the instrument

The instrument concept of SPICES is designed to provide polariometric and spectroscopic measurements in the 0.45–0.90 μm range (Fig. 1 and Boccaletti et al. 2012). To achieve high contrasts required to exoplanet characterization, SPICES combines a high-quality off-axis telescope, high-accuracy wavefront control, a broad-band coronagraph with small inner working angle (IWA; the angular separation of 50% throughput), and optical elements and detectors to collect the polarimetric and spectroscopic information. As for the telescope, very low wavefront aberrations have already been demonstrated for Gaia primary mirrors (~8 nm rms on surface), and SPICES can benefit from the same technology. The wavefront control is achieved with the combination of a focal plane wavefront sensor and a deformable mirror (DM). The wavefront sensing is achieved with a self-coherent camera (SCC, Galicher et al. 2008), which is a very simple modification in the coronagraph design. The SCC spatially modulates speckles (residual stellar light) that are recorded in the science image (no additional channel) and can accurately retrieve the wavefront errors (phase and amplitude) that induce these speckles. It then drives a DM to correct for them. As the correction is never perfect, the speckle noise is strongly attenuated, but residual speckles still remain in the image. The SCC provides a means to calibrate them and extract the companion or disk information, without prior information on the spectrum of the latter (Baudoz et al. 2006; Galicher et al. 2010). The DM is a 64 × 64 actuator mirror, as a larger number of actuators increases the field of view which can be corrected. A vortex coronagraph in the focal plane applies an azimuthal phase ramp to the corrected incident wavefront to cancel the starlight (Mawet et al. 2005). The vortex coronagraph can be made achromatic over a wide spectral bandwidth (~50%, Mawet et al. 2010). This type of coronagraph was successfully used by Serabyn et al. (2010) to re-image the HR 8799 multi-planet system. Finally, an integral field spectrograph (IFS) based on a micro-lens array (Antichi et al. 2009) allows recording of a dispersed image of the corrected field of view. Once a (x, y, λ) data cube is reconstructed from the detector image, the SCC speckle calibration is applied to every spectral channel separately, therefore drastically reducing the chromaticity of this device (Galicher et al. 2010). In the current design, the beam is divided into two branches, each assigned to a state of polarization and half of the spectral band. An achromatic modulator, at the very beginning of the instrument, selects the linear polarization direction on the sky that is analyzed by the polarizer in each branch.

We built a numerical code, written in the Interactive Data Language (IDL), to model the instrument concept and to simulate the SPICES performance. Our code operates in three steps:

– Step 1: the simulation of non-coronagraphic and coronagraphic image cubes of on-axis (the star) and off-axis (the planet(s)) sources. The third dimension of the cubes represents the spectral channels. We assume that the image cube extraction from the IFS data is perfect, but correctly account for flat field impact at step 2 (Sect. 2.2).
– Step 2: the normalization of the star and planet spectra, and introduction of noise (photon noise, zodi, exozodi, read-out noise, flat field).
– Step 3: the SCC speckle calibration of the images recorded at step 2 and the measurement of the planet spectra.

In Fig. 2, we show an example of simulated images without detection noise for a single spectral channel (λ = 0.675 μm, Δλ = 0.013 μm), after the coronagraph (Fig. 2, left) and after the speckle calibration (Fig. 2, middle and right). The image field is limited to the zone corrected by the DM (64 × 64 (λ/D)2 which corresponds to ~6 × 6 arcsec2 at λ = 0.675 μm). The corrected zone size is set by the linear number of DM actuators (Galicher et al. 2010). As we introduce both amplitude and phase aberrations in the entrance pupil of the instrument and SPICES uses a sole DM, the speckles are corrected only in one half of the field of view (right half in the images). After speckle calibration, the contrast is enhanced as shown in the middle and right images. With the current SCC, the calibration is more efficient in a diagonal because of the chromatism limitation (Galicher et al. 2010). A new version of the technique is under study to calibrate speckles in all directions. In the left and middle images of Fig. 2, we added two jovian planets of contrasts ~10−8 and ~10−9 at 2.2 and 5.4 λ/D (red circles). The closest planet is detected in the coronagraphic image (left) with a SNR ≥ 25. The farthest planet can be seen in this image if its position is known. However, it is not possible to claim a detection in this image (SNR ≳ 5), whereas it is detected with a SNR ≳ 600 after calibration (middle).

2.2. Instrument assumptions

In terms of contrast, SPICES has to reach values as low as 10−9 at 2 λ/D and 10−10 at 4 λ/D (Boccaletti et al. 2012) to produce interesting science results. Such performance is achieved assuming the parameters and the requirements on noise that are listed in Table 1. We consider these values in the numerical simulation and discuss some of them in this section. The star is assumed to be perfectly centered onto the coronagraph focal plane mask. Since the pointing accuracy is a critical aspect, SPICES
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Fig. 2. Central part of images without detection noise produced by the simulation, after the coronagraph (left) and after the speckle calibration by the self-coherent camera (middle and right). The image size is $64 \times 64 \mu m^2$. In the two left images, there are two jovian planets of contrasts $\sim 10^{-8}$ and $\sim 10^{-9}$ (red circles). In the right image, we indicate the calculation area of the profiles shown in Sect. 3 with a white dotted line. The intensity scales are linear and identical.

Table 1. Assumptions used for the instrument simulations.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Telescope diameter</td>
<td>1.3 m</td>
</tr>
<tr>
<td>Spectral bandwidth</td>
<td>0.45–0.90 μm</td>
</tr>
<tr>
<td>Spectral resolution $R$ ($\lambda = 0.675 \mu m$)</td>
<td>50</td>
</tr>
<tr>
<td>Number of spectral channels</td>
<td>35</td>
</tr>
<tr>
<td>$\Delta \lambda$ per channel</td>
<td>$-0.013 \mu m$</td>
</tr>
<tr>
<td>$\lambda/D$ sampling at 0.45 μm</td>
<td>3 pixels</td>
</tr>
<tr>
<td>Wavefront errors ($\lambda = 0.675 \mu m$)</td>
<td>15 nm rms ($f^{-1}$ PSD$^a$)</td>
</tr>
<tr>
<td>Amplitude aberrations</td>
<td>$0.1%$ ($f^{-1}$ PSD$^a$)</td>
</tr>
<tr>
<td>Number of actuators on the DM</td>
<td>$64 \times 64$</td>
</tr>
<tr>
<td>Phase estimation by the SCC</td>
<td>perfect</td>
</tr>
<tr>
<td>Throughput</td>
<td>23%</td>
</tr>
<tr>
<td>Quantum efficiency</td>
<td>70%</td>
</tr>
<tr>
<td>Maximum integration time</td>
<td>200 h</td>
</tr>
<tr>
<td>Read-out noise</td>
<td>0.2 e- rms per pixel</td>
</tr>
<tr>
<td>Full well capacity</td>
<td>300 000 e-</td>
</tr>
<tr>
<td>Time per single exposure</td>
<td>1000 s</td>
</tr>
<tr>
<td>Flat field accuracy</td>
<td>0.5%</td>
</tr>
<tr>
<td>Zodiacal light</td>
<td>$V = 23.1$ mag arcsec$^{-2}$</td>
</tr>
<tr>
<td>Exozodi level</td>
<td>1 zodi</td>
</tr>
</tbody>
</table>

Notes. The parameter values are discussed in Sects. 2.1, 2.2 and 3.2.

(a) $f$ is the spatial frequency of the optical defect, PSD refers to power spectral density.

will include a dedicated procedure for a precise control of the coronagraph alignment at the level of $\sim 0.2$ mas (Boccaletti et al. 2012). Our simulations showed that this value keeps the speckle noise at a level of $\sim 10^{-10}$ between 2 and 4 $\lambda/D$, which is below the photon noise (Sect. 3.3). In the optical design of the instrument, the whole spectral band is split into two branches, the first branch covering the 0.45–0.7 μm band ($\Delta \lambda/\lambda = 43\%$) and the second branch the 0.65–0.9 μm band ($\Delta \lambda/\lambda = 32\%$). The overlapping is for calibration purposes. We assume that all phase and amplitude aberrations are located in planes conjugated to the instrument pupil and we use the matrix direct Fourier transform (Soummer et al. 2007) to propagate the light. Fresnel propagation effect will be included using the PROPER library (Krist 2007). The main impact will be a partial modification of the speckle pattern with wavelength (Marois et al. 2006). This will not impact the SCC wavefront estimation since each spectral channel is treated separately, but it will reduce the efficiency of the wavefront correction with a sole DM (Shaklan & Green 2006). A slightly undersized Lyot stop is used for the coronagraph (95% of the pupil diameter). We consider that the vortex coronagraph performance is achronatic for SPICES’ spectral bands. Current vortex coronagraphs are limited to contrasts of $\sim 4 \times 10^{-8}$ for a 20% bandwidth, but strong efforts have been made in the past few years to develop them in laboratory, test them on the sky and further improve their performance (Serabyn et al. 2011). 15 monochromatic images are co-added to simulate each spectral channel image. The SCC requires an oversampling with respect to Shannon’s criterion. The pixel number per spatial resolution element ($\lambda/D$) is 3 at the minimum wavelength. The SCC fringes are tilted at 45° with respect to the pixel grid. We use a $f^{-1}$ power law ($f$ is the spatial frequency of the optical defect) for the power spectral density (PSD) of the phase aberrations, since it quite well reproduces the aberrations measured on the VLT and HST mirrors (Bordé & Traub 2006). Simulations indicate that the amplitude aberrations will have to be 0.1% in order to meet SPICES’ requirements if they follow a $f^{-1}$ PSD, but this value will be more stringent if the exponent is $>1$ (Galicher 2009, Chap. IV.2, Fig. IV.2.2). SPICES’ optical aberrations are expected to evolve very slowly with time. SPICES will be located at the L2 point, which is believed to be a very stable environment. This may be confirmed by the Gaia and JWST missions. Assuming such a stable environment, we plan to allocate a significant amount of time at the beginning of the mission for the purpose of accurately estimating SPICES’ aberrations. Then, the DM will compensate for the slow variations. In our simulation, the SCC perfectly estimates for the wavefront aberrations (phase and amplitude). The perfectly estimated wavefront is projected onto the $64 \times 64$ DM using the method of energy minimization in the pupil plane (Bordé & Traub 2006). The DM influence functions are modeled by adapting the formula of Huang et al. (2008) to fit the parameters of a realistic DM. Finally, the numerical noise introduced by the extraction of individual spectra from the IFS to build data cubes is assumed negligible.

In step 2, blackbody spectra for the star and planetary spectra from Cahoy et al. (2010) and Stam (2008) for the planets are introduced. The latter are discussed in detail in Sect. 2.4. Photon and read-out noise, flat field variations, and zodiacal and exozodiacal light are accounted for. The instrument throughput is set to 23%, considering $\sim 15$ optical surfaces of reflectivity 90% from the primary mirror to the detector, and the quantum efficiency of the detector is 70%. Using an algorithm to correct for cosmic ray contamination, Robberto (2009) found that single exposures of 1000 s will keep cosmic-ray induced
glitches negligible with respect to a read-out noise level of a few e- rms per pixel. We adopt this single exposure for our simulations and we do not account for glitches. The detector flat field is modeled as gaussian noise with a mean of 1 and a rms of 0.5%. The IFS spreads the spectrum of an object point on different detector pixels. As a consequence, every pixel of the $(x, y, \lambda)$ cube is affected by a specific flat field. We use the measured values of zodiacal light from Giavalisco et al. (2002). An exo-zodiacal disk with a 60°–inclination with respect to a face-on orbit and a 45°-orientation from the horizontal direction is simulated using the Zodipic algorithm (Kuchner 2004). The inclination value is the statistical median assuming a uniformly random orientation. The orientation corresponds to the SCC fringe. The actual scientific strategy of SPICES requires prior knowledge of the orientation of the planet orbit. This has to be achieved by combining astrometric measurements with RV data. The present and near-future instruments like VLT/PRIMA and Gaia (we note that stars with $V < 6$ are too bright for the latter) can in principle provide the information. We also plan to use a new version of the SCC that could enlarge the high-contrast part of the image and thus, could relax the constraints on the orbital knowledge.

2.3. Selecting spectral bandwidth and resolution

In this section we discuss the different parameters we have to take into account for the choice of SPICES’ spectral bandwidth and resolution. To determine the spectral bandwidth, we first examine theoretical spectra representative of Jupiter, Neptune and terrestrial atmospheres (Fig. 3, giant planet models from Cahoy et al. 2010; and Earth models from Stam 2008). The spectra are calculated for visible wavelengths: 0.35–1 $\mu$m for Cahoy et al. (2010) and 0.3–1 $\mu$m for Stam (2008). We note that a 0.45–0.90 $\mu$m bandwidth offers a good compromise and enables to measure Rayleigh scattering at the blue wavelengths as well as the molecular absorption bands in the red part. The trade-off for the long-wavelength cut-off results from a technological limitation, since visible detectors have weak efficiencies above 0.90 $\mu$m. Therefore, SPICES will not measure the wide and strong water absorption band at 0.94 $\mu$m in the spectrum of Earth analogs (Fig. 3). Although deep absorption bands are easily identifiable in model spectra, their depth would be hard to measure given the SPICES' performance. However, other similar features but at different wavelengths are also present in planetary spectra. Similarly, giant planets feature a strong methane band at 0.89 $\mu$m at the boundary of SPICES’ bandpass, but there are weaker bands at, for instance, 0.62, 0.73 and 0.79 $\mu$m. Measuring absorption bands at different wavelengths allows to infer the gas abundances, if the cloud top altitudes can be derived from a known gas which is well mixed in the atmosphere (Stam 2008, and references therein). Polariometry combined with flux could also help to break the degeneracy (Stam et al. 2004). For the telluric planets, Des Marais et al. (2002) define the spectral bandwidths and list the molecules that exoplanet missions should address: molecular oxygen (O$_2$), ozone (O$_3$), water (H$_2$O), methane (CH$_4$) and carbon dioxide (CO$_2$). The spectral range of SPICES (0.45–0.90 $\mu$m) permits to measure all these molecules except CO$_2$. In addition to atmospheric gases, Seager et al. (2005) have emphasized the scientific interest of the detection of surface features like the “red edge” (the rise of the clear Earth spectrum beyond 0.7 $\mu$m in Fig. 5). Nevertheless, several studies showed that this measurement is difficult for the Earth itself (e.g., Woolf et al. 2002; Arnold et al. 2002; Montañés-Rodríguez et al. 2005). Seager et al. (2005) note that the “red edge” should be detected with molecular oxygen to be sure that it is related to vegetation, because minerals may present a similar feature but at different wavelengths. From the comparison of widths of SPICES’ spectral channels and of molecular bands, we find that a spectral resolution of at least 50 is required to identify the main bands of the spectra of giant planets as well as super-Earths (Tables 3 and 4 and Figs. 4 and 5). Our analysis confirms previous results (Schneider et al. 2009).

2.4. Planetary atmosphere models

The following Sects. 2.4.1 and 2.4.2 describe the models we use in our simulation. In this paper, we consider two sets of models, one for giant planets and one for telluric planets. Cahoy et al. (2010)’s models cover a large range of star-planet separations and planet metallicities. Stam (2008)’s models assume different planet surfaces and atmospheric structures (cloudy and clear atmospheres). Table 2 summarizes the main parameters we consider for these models. We set a maximum mass of 10 Earth masses ($M_\oplus$) for the super-Earths, which corresponds to a maximum radius of 2.5 Earth radii ($R_\oplus$) from the mass-radius relation of Grasset et al. (2009). Recall that Stam’s atmosphere models assume an Earth-like planet.

From the degraded spectra of Figs. 4 and 5 (see Sect. 2.3 for the discussion of the spectral resolution), the planet/star contrast is expected to be $\sim 10^{-8}$–$10^{-10}$ for Jupiters and $\sim 10^{-9}$–$10^{-11}$ for Neptunes and super-Earths, depending on the separation from the star and on the wavelength. Note that Cahoy et al. (2010) and Stam (2008) present geometric albedo spectra, while we plot contrast curves using the following formula:

$$C(\lambda) = A(\lambda, \alpha) \frac{R_p^2}{a^2}$$  \hspace{1cm} (1)

where $\lambda$ is the wavelength, $C(\lambda)$ is the planet/star contrast spectrum, $A(\lambda, \alpha)$ is the planet albedo spectrum at phase angle $\alpha$, $R_p$ is the planet radius and $a$ is the star-planet separation. Phase angle is the angle star-planet-observer: when the planet is behind the star $\alpha = 0^\circ$, and when the planet is in front of the star $\alpha = 180^\circ$. In this work, we only consider the case of a
Table 2. Parameters of the exoplanetary atmosphere models used in this paper.

<table>
<thead>
<tr>
<th>Planet</th>
<th>Separations (AU)</th>
<th>Radius</th>
<th>Metallicity (solar units)</th>
<th>Atmospheric structure</th>
<th>Surface type</th>
</tr>
</thead>
<tbody>
<tr>
<td>Jupiter</td>
<td>0.8, 2, 5, and 10</td>
<td>$R_J$</td>
<td>1 and 3</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>Neptune</td>
<td>0.8, 2, 5, and 10</td>
<td>$R_N$</td>
<td>10 and 30</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>Super-Earth</td>
<td>1</td>
<td>$2.5 R_E$</td>
<td>0, 50 and 100% clouds</td>
<td>Forest, ocean and forest-ocean mix</td>
<td></td>
</tr>
</tbody>
</table>

Notes. $R_J$, $R_N$ and $R_E$ refer to Jupiter, Neptune and Earth radii respectively.

Fig. 4. Theoretical models of Jupiter-like (left panel) and Neptune-like (right panel) atmospheres degraded to the resolution of SPICES (models adapted from Cahoy et al. 2010).

Table 3. List of molecules observable at $R = 50$ in the Jupiter and Neptune models of Fig. 4.

<table>
<thead>
<tr>
<th>Molecule</th>
<th>Approximate $\lambda$ ($\mu$m)</th>
<th>Note</th>
</tr>
</thead>
<tbody>
<tr>
<td>CH$_4$</td>
<td>0.54</td>
<td></td>
</tr>
<tr>
<td>CH$_4$</td>
<td>0.62</td>
<td></td>
</tr>
<tr>
<td>H$_2$O</td>
<td>0.65</td>
<td>for 0.8-AU models</td>
</tr>
<tr>
<td>CH$_4$</td>
<td>0.66</td>
<td></td>
</tr>
<tr>
<td>CH$_4$</td>
<td>0.73</td>
<td></td>
</tr>
<tr>
<td>CH$_4$</td>
<td>0.79</td>
<td></td>
</tr>
<tr>
<td>H$_2$O</td>
<td>0.82</td>
<td>for 0.8-AU models</td>
</tr>
<tr>
<td>CH$_4$</td>
<td>0.84</td>
<td></td>
</tr>
<tr>
<td>CH$_4$</td>
<td>0.86</td>
<td></td>
</tr>
</tbody>
</table>

planet at its maximum elongation from the star, $\alpha = 90^\circ$. The flux reflected by a planet depends on both its albedo and its radius (Eq. (1)). To determine the albedo from observations, we need to independently estimate for the radius. We can use theoretical mass-radius relations (e.g., Fortney et al. 2007; Baraffe et al. 2008; Grasset et al. 2009). The polarimetric capabilities of SPICES could also help to establish the planetary properties without prior information about the planet’s radius (Stam et al. 2004; Stam 2008). This will be subject for future work. When we will study SPICES’ ability to retrieve the planet properties from measured spectra in Sect. 4, we assume that the radius is known.

2.4.1. Theoretical spectra of Jupiter and Neptune analogs

We use the models of Cahoy et al. (2010), who calculate atmospheric structures of old ($\sim 4.5$ Gyr) Jupiter and Neptune analogs in radiative equilibrium with the radiation of a solar-type host star at separations of 0.8, 2, 5 and 10 AU, for different metallicities and for optical wavelengths (0.35 to 1 $\mu$m). This range matches the separations of the planets that small space coronagraphs can potentially observe. Table 3 lists the main spectral bands observable with a spectral resolution of 50. Several theoretical spectra of Jupiter and Neptune analogs are shown in Fig. 4. Unlike young planets, which are dominated by thermal radiation, the star-planet separation drastically alters the structure and composition of mature planetary atmospheres. Therefore, a simple scaling of the amount of reflected light with distance is not sufficient to model realistic spectra and to derive the actual performance of a mission like SPICES. If planets are too warm for any molecules to condense into clouds, their spectra are dominated by Rayleigh scattering. This is illustrated for the case of a separation of 0.8 AU in Fig. 4. At 2 AU, bright water clouds form and dominate the atmospheric opacity all over the spectrum. At 5 AU, ammonia clouds form above the water clouds. At 10 AU, the same clouds form but at a deeper pressure level, and Rayleigh scattering again dominates the reflected flux at short wavelengths. The planet is $\sim 4$ times fainter than the Jupiter at 5 AU, as expected in the case where the flux decrease follows an inverse square power law of separation. For all cloudy planets (2, 5 and 10 AU), the clouds are optically thick. The Neptune spectra exhibit the same but stronger absorption bands as the Jupiter spectra. Increasing the planet metallicity usually decreases its albedo. The exception is the 2-AU Jupiter model for short wavelengths because for this case the water clouds are high in the atmosphere and thick. Cahoy et al. (2010) note that the metallicity increase produces larger differences between the
see the spectra of the 50% cloudy ocean and 50% cloudy forest planets in blue and green dashed lines respectively). At short wavelengths Rayleigh scattering dominates while at long wavelengths scattering by clouds is the most important process. Stam (2008) uses a weighted sum of homogeneous models to simulate a quasi horizontally inhomogeneous model representative of the Earth (70% of the surface covered by ocean and 30% by forest) with different cloud coverages. In this paper, we use different weighted sums for simulating three cloud coverages (0, 50 and 100%) and three surface types (forest, forest-ocean equally mix and ocean), as indicated in Table 2.

### 2.4.3. Planet contrasts as a function of the stellar type

The atmospheric structures of the models were calculated by assuming ∼4.5-Gyr planets in radiative equilibrium with the flux of a Sun-like parent star. These models can be transposed to other stellar types assuming flux conservation with the standard formula:

$$4\pi R_p^2 \sigma T_{eq}^4 = (1 - A_B) \pi R_p^2 \frac{L_\star}{4\pi a^2}$$

where $R_p$ is the planet radius, $\sigma$ is Stefan’s constant, $T_{eq}$ the planet atmosphere equilibrium temperature, $A_B$ the planet Bond albedo and $L_\star$ the host star luminosity. This formula does not account for the effects of the wavelength dependence of the star emission on the atmosphere (Marley et al. 1999; Fortney et al. 2007).

Because we are using models with discrete values (especially separations and stellar luminosity), we cannot extrapolate the planet spectra to any separations around any stars. Instead, we calculate the correspondence between separations and stellar luminosity, considering $T_{eq}$ and $A_B$ only depend on the incident stellar flux at the planet position $L_\star/a^2$. Therefore, Eq. (2) becomes:

$$L_\star \propto a^2 \Rightarrow a_{G2} = a_{A0} \sqrt{L_{G2}/L_{A0}}$$

where $a_{G2}$ is the star-planet separation for a star of spectral type $S_p$, $a_{A0}$ the star-planet separation for a G2 star and $L_{G2}$ the star luminosity in solar units. For example, a Jupiter at 2 AU from a solar-like star would have the same atmospheric structure as a Jupiter at ∼10.5 AU from an A0 star. Table 5 gives the correspondences for different star-planet separations and stellar types.

### Table 5. Star-planet separations for giant planets extrapolated to other stellar types assuming Eq. (3).

<table>
<thead>
<tr>
<th>Spectral type</th>
<th>Luminosity ($L_\odot$)</th>
<th>Separations (AU)</th>
</tr>
</thead>
<tbody>
<tr>
<td>A0</td>
<td>28</td>
<td>4.2</td>
</tr>
<tr>
<td>F0</td>
<td>4.8</td>
<td>1.8</td>
</tr>
<tr>
<td>G2</td>
<td>1</td>
<td>0.8</td>
</tr>
<tr>
<td>K0</td>
<td>0.45</td>
<td>0.5</td>
</tr>
<tr>
<td>M0</td>
<td>0.09</td>
<td>0.24</td>
</tr>
</tbody>
</table>

#### Notes. The values for the solar-type star are those modeled by Cahoy et al. (2010).

The values for the solar-type star are those modeled by Cahoy et al. (2010).
We use Eqs. (3) and (4) to derive the star-planet separations and contrasts in Sect. 3. While this calculation is a fairly good estimation for the giant and cloudy telluric planet models, it is less accurate for the clear terrestrial models. For stars cooler than the Sun, Wolshtencroft & Raven (2002) suggest that the “red edge” could indeed be shifted towards wavelengths redder than 1 μm, if the photon number involved in the photosynthesis processes is greater than for the mechanism operating on Earth. If this hypothesis is verified, the “red edge” will be outside the bandwidth covered by SPICES and undetectable. However, Kiang et al. (2007) warn that a theory predicting the “red edge” wavelength for a given stellar type assuming the same mechanism as on Earth is still missing.

3. Performance in detection

The instrument model presented in Sect. 2.1 provides an estimation of the achievable contrast map in the field of view for each spectral channel. In this section, we estimate the average contrast that is reached in the darkest area of the field of view (area contained by the dotted lines in Fig. 2) as a function of the angular separation from the central star. As we explained in Sect. 2.2, we assume that the planet orbital parameters are known and its position can be matched with the orientation of the corrected area.

3.1. Impact of speckle noise

Figure 6 shows SPICES’ contrast curves against angular separation (λ₀ = 0.675 μm) for all spectral channels, before and after the speckle calibration by the SCC. We see that the speckle subtraction is necessary to reach the requirement of ~10⁻¹⁰ at a few λ/D (Sect. 2.2). The wavelength dispersion of the performance is due to the phase aberration dependence on wavelength (λ⁻¹) and the SCC calibration dependence on spectral resolution (Galicher et al. 2010). Recall that we set the same bandwidth for all channels so spectral resolution increases with wavelength. The steep increase of the detection limit around 32 λ/D corresponds to the DM cut-off spatial frequency. This cut-off and the more efficient SCC calibration at small separations explain the degradation with angular separation.

To have a clear and simple view of the performance, we plot radial profiles averaged on all the spectral channels against the physical separation in AU for three star distances in Fig. 7. The performance is limited at short separations by the corona of the star, and at large separations by the size of the DM corrected area (cut-off at 32 λ/D). As we express the x-axis in AU, the contrast curve scales with the star distance. We also plot the positions of Jupiter of 1 solar metallicity and 1 Jupiter radius (R_J), Neptune of 10 solar metallicities and 1 Neptune radius (R_N), and 2.5-R_E cloudy planets. We assume that the super-Earth properties do not evolve with separation for the considered range. We recall that Stam (2008) uses a temperature-pressure profile of the Earth so the model is relevant for a separation of 1 AU. For stars at 20 pc, the farthest Jupiters (5 and 10 AU) and Neptunes (5 AU) are detected with SNR > 5. The 10-AU Neptune is below the curve (SNR ≃ 4.5). For a 10-pc star, the same planets are still detected as well as planets as close as 2 AU. For the closest star we consider (3 pc), planets as close as 1 AU are very well detected and characterized (Sect. 4). In this case, the 10-AU Jupiter and 5-AU Neptune are not detected with the current instrument design because of the speckle calibration degradation with angular separation. Solutions may exist to improve the detection at these large angular separations (≥18 λ/D) such as spectral deconvolution (Sparks & Ford 2002).

In addition, we plot the averaged contrast levels for zodiacal light and a 1-zodi exodisk (star distance of 10 pc). Recall that they increase as the square of the star distance. Although the instrument concept can reduce speckle noise below a contrast of 10⁻¹⁰, the final performance is limited by these extended background sources. The considered exo-zodiacal disk limitation is at the level of Neptunes and super-Earths. Therefore, to obtain a correct estimation of planet fluxes, the zodiacal and exo-zodiacal contributions must be carefully calibrated and removed. The exo-zodiacal disk intensity has been identified as critical for Earth-twin detection. To address this question,
3.2. Impact of detection noise

Due to a small primary mirror (typically 1.5 m in diameter) together with a spectral resolution $R = 50$, space coronagraphs like SPICES will be limited by photon noise (from the stellar background and the planet) or read-out noise for most of the targets, because very long exposures would be required to reach the instrument limitation at $\sim 10^{-10}$. For instance, $-10000$ h are needed to achieve $\sim 10^{-10}$ at 5σ for a G2 star at 10 pc. From this exposure time and assuming that the noise follows the photon noise behavior (proportional to the square root of the photon number), we estimate the total integration time required to detect a super-Earth at $\text{SNR} = 5$, for typical values of distance and contrast accessible to SPICES. It is 200 h for a planet of contrast $2.5 \times 10^{-10}$ at 2 AU around a solar-type star at 5 pc. No detailed study of the maximum integration time per target has been carried out to date for SPICES. In this paper, we set the maximum integration time per target to 200 h. This is a good trade-off between achieving high contrasts and observing a large number of targets during the mission.

We present the impact of photon and read-out noise on SPICES’ performance for the case of a G2 star at 3 and 10 pc in Fig. 8. We note that the read-out noise is a major limitation for the furthest star but not for the closest. This is due to the fact that the full well capacity of the detector (Table 1) is not filled after a 1000-s exposure in both cases. The number of single exposures and read-out noise level are thus the same, but the photon count is greater for the closest star. We note that the dozen of stars located within 3 pc have types later than G (the exception being Sirius). Thus, the read-out noise will not be a fundamental limitation for close stars. We base the read-out noise requirement on the farthest star and set its value to 0.2 e- rms per pixel. Electron multiplying CCDs can achieve such a low read-out noise, and a large set of devices have been qualified for space during the Gaia preparation (Smith et al. 2006).

As indicated in the previous section, an exo-disks can prevent the detection of faint planets if its photon noise becomes too important. To help to prepare a target list, we estimate the exo-zodi level that may hamper the detection of SPICES’ targets. Figure 9 presents the performance for different exo-zodi levels and two distances of a solar-type star. The read-out noise is set to 0.2 e- rms per pixel. We assume that the exo-disks have no structure and can be subtracted out from the data to the precision imposed by photon noise. We find that the exo-disks photon noise does not significantly limit the performance up to 10 zodis, but begins preventing the Neptune and super-Earth detection when larger than 10 zodis. For exposures shorter than 200 h (more dominant photon noise), the acceptable exo-zodi level is lower.

3.3. Impact of stellar type

Assuming a generic exposure time of 200 h and an exo-zodi disk of 1 zodi, we test the detectability of planets for several stellar types. Figure 10 presents the 5-σ detection levels for three stars of type G2, A0 and M0 and several distances (3, 10, and 20 pc). We consider the star-planet separations given in Table 5 (they scaled by $L^1/2$), and we apply Eq. (4) to find the wavelength-averaged planet contrasts. For a G2 star (Fig. 10, top), SPICES can potentially access jovian planets, icy giants and super-Earths with separations smaller than $\sim 6$, $\sim 3$ and $\sim 2$ AU respectively. No planet is detected at distances larger than $\sim 10$ pc. The detectability of the closest planets (0.8 to 2 AU) will be limited by the coronagraph IWA ($\sim 2 \lambda/D$) for stars

![Fig. 8. 5-σ detection profiles accounting for the photon noise of G2 star at 3 (blue lines) and 10 pc (red lines), and for read-out noise levels from 0 to 3 e- rms per pixel.](image)

![Fig. 9. 5-σ detection profiles for a Sun analog at 3 and 10 pc and exo-zodi level that may hamper the detection of SPICES' targets.](image)
Fig. 10. 5-σ detection profiles for a 200-h exposure compared to averaged planet contrasts for G2 (top), A0 (middle) and M0 (bottom) type stars and several star distances.

at 4 to 10 pc. As for an A0 parent star (Fig. 10, middle), Jupiter-like planets are not detected when further than 10 AU for stars within 20 pc. The separation ranges considered by Cahoy et al. (2010) and Stam (2008) in the case of a G2 star do not allow to study planets at separations shorter than ~4 AU around an A0 star. Nonetheless, we can roughly estimate that Neptune analogs and super-Earths can be detected in the range 2–4 AU for stars closer than 10 pc. There are no A stars within 5 pc (except for the Sirius binary system) so we do not plot the 3-pc curve. Finally, the very close M stars (Fig. 10, bottom) at 3–5 pc are of great interest for detecting Jupiter-like planets in the 0.5–4 AU range as well as super-Earths in close orbits at 0.5–1 AU.

From the current exoplanet database (Schneider et al. 2011), we assess that only a handful of known extrasolar planets match the limitations described here. However, we note that RV surveys are not complete in the case of early and late stellar types (A and M in particular, Udry & Santos 2007) and at long periods (a few AUs) even for nearby stars.

4. Performance in spectrometry

In this section, we analyze the SPICES performance more in detail, by estimating SNRs of the measured planetary spectra. The objective is to set the constraints on the SNR to allow the differentiation between planetary models: impact of physical star-planet separation and metallicity for the Jupiter and Neptune analogs (Sects. 4.2 and 4.3), and variations due to cloud and surface coverage for the rocky planets (Sect. 4.4).

4.1. Criterion of characterization

We first explain our characterization criterion. The underlying question is to know if a measured spectrum $S$ is reproduced by one of two model spectra noted $M_i$ ($i$ referring to the model index, $i = 1, 2$). This depends on the noise of the measured spectrum $N = S/SNR$. We define the following criteria of comparison of $S$ to $M_i$:

$$\text{crit}_i = \text{median}_\lambda \left( \frac{S(\lambda) - M_i(\lambda)}{N(\lambda)} \right)$$

(5)

where the median is calculated over the spectral channels. We choose the median because it accounts well for the overall quality of a spectrum. For a given measurement ($S$, $N$), the model which best matches the measured spectrum gives the lowest criterion value. Substituting the definition of $N$ to express crit as a function of SNR and assuming the latter is nearly constant on the measured spectrum, we can write:

$$\text{crit}_i = \text{median}_\lambda \left( \frac{S(\lambda) - M_i(\lambda)}{S(\lambda)} \right) \times \text{SNR}.$$  

(6)

In this paper, we use theoretical models to assess the instrument performance and to set the SNR required to measure differences between them ($S = M_1$ and $M_2 = M_2$). We consider that the models are differentiated when their difference is 10 times above the measured noise so $\text{crit}_i = 10$. Inverting Eq. (6) and calling $\text{SNR}_r$ the value of the required SNR, we finally obtain:

$$\text{SNR}_r = 10 \times \frac{1}{\text{median}_\lambda \left( \frac{M_1(\lambda) - M_2(\lambda)}{M_1(\lambda)} \right)}.$$  

(7)

As an example, when we study the metallicity (Sects. 4.2 and 4.3), $M_1$ will be the lowest metallicity model and $M_2$ the highest metallicity model. We consider different spectral bandwidths to determine $\text{SNR}_r$ (Eq. (7)) when analyzing different...
Table 6. Values of SNR, derived from Eq. (7).

<table>
<thead>
<tr>
<th>Planet</th>
<th>Parameter</th>
<th>SNR,</th>
<th>Note</th>
</tr>
</thead>
<tbody>
<tr>
<td>Jupiter</td>
<td>0.8/2 AU</td>
<td>15</td>
<td></td>
</tr>
<tr>
<td>Jupiter 0.8 AU</td>
<td>metallicity 1/3x</td>
<td>30</td>
<td></td>
</tr>
<tr>
<td>Jupiter 2 AU</td>
<td>metallicity 1/3x</td>
<td>30</td>
<td>CH₄ bands</td>
</tr>
<tr>
<td>Jupiter 5 AU</td>
<td>metallicity 1/3x</td>
<td>30</td>
<td>CH₄ bands</td>
</tr>
<tr>
<td>Neptune</td>
<td>0.8/2 AU</td>
<td>15</td>
<td></td>
</tr>
<tr>
<td>Neptune 0.8 AU</td>
<td>metallicity 10/30x</td>
<td>30</td>
<td></td>
</tr>
<tr>
<td>Neptune 2 AU</td>
<td>metallicity 10/30x</td>
<td>25</td>
<td>CH₄ bands</td>
</tr>
<tr>
<td>Forest Earth</td>
<td>0/50/100% clouds</td>
<td>25</td>
<td>blue channels</td>
</tr>
<tr>
<td>Ocean Earth</td>
<td>0/50/100% clouds</td>
<td>25</td>
<td>blue channels</td>
</tr>
<tr>
<td>Clear Earth</td>
<td>0/50/100% forests</td>
<td>12</td>
<td>red channels</td>
</tr>
<tr>
<td>50% cloudy Earth</td>
<td>0/50/100% forests</td>
<td>30</td>
<td>red channels</td>
</tr>
<tr>
<td>Cloudy Earth</td>
<td>0/50/100% forests</td>
<td>220</td>
<td>red channels</td>
</tr>
</tbody>
</table>

Table 7. Maximum star distance at which SPICES resolves the planet separation at the central wavelength of the bandwidth.

<table>
<thead>
<tr>
<th>Planet separation (AU)</th>
<th>Star distance (pc)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.8</td>
<td>4</td>
</tr>
<tr>
<td>1</td>
<td>5</td>
</tr>
<tr>
<td>2</td>
<td>10</td>
</tr>
<tr>
<td>5</td>
<td>25</td>
</tr>
</tbody>
</table>

planetary properties. For instance, metallicity strengthens the bands (Fig. 4), and cloud and surface coverage alter the spectrum at blue and red wavelengths respectively (Fig. 5). We give the calculated SNR, in Table 6 and we specify the spectral channels in the last column. We stress the point that the SNR, values correspond to the spectrum of the brightest planet considered for each analyzed property: for instance, the low-metallicity planets for the Jupiters and Neptunes (Sects. 4.2 and 4.3) and the cloudy planets for the super-Earths (Sect. 4.4).

In the remainder of this section, we study the ability of SPICES to disentangle planetary models. For each planet separation, we consider the distance at which the star-planet system is resolved at quadrature (Table 7) and we derive the exposure time to achieve the SNR, values quoted in Table 6. We restrain the study to the case of a solar-type star and we assume a maximum exposure time of 200 h (∼8 days). We perform our simulations for five independent realizations of speckle pattern. We then average our results to minimize the impact of an optimistic σ error. The SNR, dependence on exposure time change from one observed planet to another as a function of the planet intensity and location in the diffraction pattern of the host star. We fit power-law curves since we expect SNR, to be proportional to the square root of the integration time, if the dominant noise is the photon noise, or SNR, to be constant, if it is the speckle noise. We find that all exponents are close to 0.5, which corresponds to the case of photon noise limitation. SNR, rapidly increases with time for the brightest Jupiter models (separations of 0.8 and 2 AU), while the growth is slower for the faintest model (5 AU). We use Fig. 11 to derive all the exposure times given in this section.

As long as astrometric measurements are not available, the orbital inclination is unknown for non-transiting planets detected by RV. We recall that we use an inclination of 60° which is the statistical median for random orientations (Sect. 2.2). Although direct imaging is able to put constraints on this parameter, it requires several images in practice covering the orbit and high SNRs. The fact that planets are easier to observe at quadrature is also not particularly favorable for a precise determination of inclination and then mass. Therefore, in the case of a single observation, the physical separation of the planet to the star is poorly constrained, particularly since eccentricity could also be significant (Udry & Santos 2007). We can thus confuse a giant planet close to its star with a large planet at large separation if their projected separation is the same on the image. In addition, for an eccentric orbit, a planet’s albend can depend strongly on the orbital position: the planet can be almost cloud-free near perihelion and covered by clouds near aphelion. The spectroscopic characterization could help to break degeneracies in these parameters, if the spectral differences are large enough to be detected. Considering the theoretical models, giant planet spectra mostly differ in the blue, where Rayleigh scattering dominates for a planet at 0.8 AU. The application of the criterion defined in Eq. (7) to giant planet spectra indicates that SNR, = 15 permits to distinguish between the atmospheres of two giants at 0.8 and 2 AU respectively (Table 6). This performance is achieved in ∼30 min for a distance of 4 pc (Fig. 11), which corresponds to the upper limit at which a separation of 0.8 AU is accessible to SPICES (Table 7). We plot the two spectra as they would be measured by the instrument with 1-σ error bars as well as the corresponding models in Fig. 12. As expected, the blue half of the bandwidth is the region where the two spectra can be distinguished with no ambiguity. SPICES will be able to

Fig. 11. Evolution of the median value of SNR, (see text) as a function of exposure time for Jupiter planets (symbols). The curves are power-law fits. We plot 1-σ error bars.

4.2. Jupiter models

We consider the models of Jupiter analogs described in Sect. 2.4.1 for several separations and metallicities. Figure 11 shows the evolution with exposure time of the median SNR measured from the simulated data (SNR,). We represent each data point with its corresponding 1-σ error bar. The SNR, dependence on exposure time change from one observed planet to another as a function of the planet intensity and location in the diffraction pattern of the host star. We fit power-law curves since we expect SNR, to be proportional to the square root of
measure Rayleigh scattering and estimate the star-planet separation. However, we note that these measurements would be possible for a few stars only because of the small angular resolution.

We now study SPICES' ability to measure the spectral differences between Jupiter models with 1 and 3 times the solar metallicity for star-planet separations of 0.8, 2 and 5 AU at levels an order of magnitude above the noise. As indicated in Table 6, this requires $SNR_r \approx 30$ for all separations. For the 0.8-AU Jupiters, this value is achieved within the distance for which our instrument can resolve such a planet ($\leq 4$ pc). In particular, an integration time of 2 h satisfies the criterion for a star at 4 pc, and the differences between the measured spectra are 10 times larger than the noise over the blue half of the spectra (Fig. 13, top panel). Recall that the error bars shown in the figures are at 1$\sigma$.

Similarly, the $SNR$ criterion is satisfied for the 2-AU planets at the maximum distance of 10 pc for an exposure time of $\sim 30$ h. Metallicity effects are larger in the methane bands for this case and we focus on the 0.73-$\mu$m methane band and the blue edge of the 0.89-$\mu$m deep band to disentangle the spectra (Fig. 13, middle panel). For a 5-AU Jupiter, the two metallicity cases are distinguished in 200 h at a distance of 7 pc in the methane bands at 0.62 and 0.73 $\mu$m and on the blue edge of the deep feature at 0.89 $\mu$m (Fig. 13, bottom panel). We note that for the 0.8- and 5-AU cases, the metallicity effects can mimic a radius variation by shifting the whole spectrum, while for the 2-AU case they alter the flux specifically in the absorption bands. We conclude that for resolved systems, SPICES will be able to analyze metallicity enhancements as small as a factor of 3 for all 0.8- and 2-AU Jupiter targets around solar-type stars. As planets at 5 AU are fainter, they will be accessible only for G2 stars within 7 pc, considering the maximum exposure time of $\sim 200$ h.

4.3. Neptune models

Figure 14 is similar to Fig. 11 but for the Neptune analogs and is used to derive the integration times mentioned below. According to Table 6, the distinction between the 0.8- and 2-AU planets requires $SNR_r \approx 15$ in the blue part of the spectral range. Similarly to the Jupiter spectra, the spectrum of very close-in Neptunes will feature a negative spectral slope, due to Rayleigh scattering, which noticeably differs from the nearly flat spectrum of a farther planet. For the maximum distance of 4 pc at which a 0.8-AU Neptune is angularly resolved by SPICES, this value is
reached in \( \sim 50 \) h. Therefore, the same analysis can be performed for closer solar-type targets (as we explained in the previous section, Rayleigh scattering would be measurable for a few objects only). The simulated measurements for the 4-pc Neptunes at 0.8 and 2 AU are plotted in Fig. 15. The 0.8- and 2-AU Neptune spectral differences can be measured for \( \lambda < 0.58 \) \( \mu \)m, whereas the spectral measurements are degenerate for redder wavelengths given the noise level.

We then test if SPICES can distinguish metallicity effects between Neptunes of 10 and 30 times the solar metallicity (Table 2). We recall that these values are those studied by Cahoy et al. (2010). The required SNR\(_r\) is \( \sim 30 \) over the full spectral range for disentangling the 0.8-AU spectra. It is \( \sim 25 \) in the methane bands for the 2-AU planet spectra (Table 6). For the 0.8-AU planets, a \( \sim 200\)-h exposure is requested to measure metallicity variations for distances as far as 4 pc. The spectral differences are detected over the blue channels up to \( \sim 0.65 \) \( \mu \)m (Fig. 16, top panel). For a separation of 2 AU, the bottom panel of Fig. 16 shows that the metallicity signatures mainly impact the methane bands at 0.62 and 0.66 \( \mu \)m as well as on the edges of the 0.79-\( \mu \)m deep band. We find that SPICES can distinguish the spectra for stars within \( \sim 6 \) pc.

### 4.4. 2.5-\( R_E \) planet models

In this section, we analyze SPICES’ capability to measure the properties of super-Earths, and in particular the effects of cloud and surface coverage for planets at 1 AU (their parameters are given in Table 2). Figure 17 represents the SNR\(_r\) evolution as a function of the exposure time for several models of planets discussed in this section. The labels “clear” and “cloudy” refer to the models with 0% clouds and 100% clouds respectively. The star distance is limited to 5 pc (Table 7) to allow the planet to be angularly separated from the star. A few G-type stars would thus be accessible to SPICES.

We first investigate the impact of cloud coverage for both forest and ocean surfaces. The influence of clouds is more important in the blue (Fig. 18, for surfaces entirely covered with forest), because of the strong “red edge” reflection in the red,
Fig. 17. Same as Fig. 11 but for the 2.5-\(R_E\) planet models discussed in Sect. 4.4.

Fig. 18. Measured (symbols) and model (lines) spectra of 2.5-\(R_E\) forest planets at 1 AU for cloud coverage of 0, 50 and 100%.

and \(\text{SNR}_r \sim 25\) (Table 6) is needed to measure the difference between 0, 50, and 100% clouds. At the maximum distance of 5 pc, this performance is met in \(\sim 150\) h for a super-Earth entirely covered with forest around a G2 star (Figs. 17 and 18). Systems closer than 5 pc will also be accessible for the characterization of the cloud coverage. We do not compute the exposure time for surfaces covered by ocean, but it will be similar since \(\text{SNR}_m \sim 25\) (Table 6) and the cloudy spectra are nearly identical for both surfaces (green and blue dotted lines in Fig. 5). Figure 18 also shows that the main atmospheric gases (\(\text{O}_2\) and \(\text{H}_2\text{O}\)) are quite well retrieved whatever the cloud coverage (\(\text{SNR}_m > 5\) and \(>15\) respectively). The broad ozone signature is mostly detectable when the cloud coverage is large (\(\text{SNR}_m \sim 23\)). We recall that the band wavelengths are given in Table 4.

Information about the planet surface can be obtained for moderate cloud coverage, because it produces noticeable signatures (Fig. 19). The differences between surface types are larger for a clear atmosphere, especially in the half red part of the spectral range. We consider three generic cases of planets with an ocean, an equally mixed surface of ocean and forest, and a forest. To separate these cases, \(\text{SNR}_r \sim 12\) (Table 6) is required on the forest model and \(\text{SNR}_m > 12\) is achieved in a \(\sim 200\)-h observation for the worst case of a G2 star at 5 pc (Fig. 19, top panel). SPICES can distinguish these three cases for any terrestrial planets on a 1-AU orbit within 5 pc. If we consider 50% cloud coverage, surface effects are more difficult to distinguish and would require \(\text{SNR}_r \sim 30\) in the red part (Table 6). The exposure time exceeds the limit of 200 h for a target at 5 pc, which rather limits the sample to 4 pc (Fig. 19, bottom panel). Molecular oxygen and water absorptions as well as the “red edge” can still be measured. On the contrary, 100% cloud coverage definitely prevents the identification of surfaces since it would require \(\text{SNR}_r \sim 220\). This performance that is out of reach of a small telescope like SPICES in a reasonable amount of time. In the favorable case of a Sun-like star at 2 pc (\(\alpha\) Cen A is the sole known case), the instrument achieves \(\text{SNR}_m \sim 110\) and allow to distinguish between cloudy planets totally covered with ocean and forest respectively.
5. Potential targets

In this section, we extend the results obtained above in order to determine the minimum planet radius accessible to SPICES for each planet category studied in the previous section. We also study the volume of the planet sample which can be characterized (metallicity, cloud coverage, surface type) with SPICES. The models used are the gas giants with metallicity 1, the ice giants with metallicity 10, the cloudy forest Earths for the cloud coverage measurement, and the forest Earths with 0 and 50% clouds for the surface type analysis. We consider that the planet flux increases as the square of its radius and that the atmosphere composition and structure remain the same. We set the following values of SNR: 30 for all Jupiters and Neptunes and 25, 12 and 30 respectively for the Earths (Table 6). We assume a maximum exposure time of 200 h and three host stars of type G2, A0 and M0. We carry out this study for the four models of Jupiter and Neptune at 0.8, 2, 5 and 10 AU and the Earth model at 1 AU. We recall that these separations are relevant for a G2 star and the corresponding separations for A0 and M0 stars are given in Table 5. We consider the following radius ranges for the planets:

- \( R_p \leq 2.5 R_E \) for the Earths (Grasset et al. 2009).
- \( 0.5 R_N \leq R_p \leq 1.5 R_N \) for the Neptunes. The lower limit is the radius for the maximum mass we consider for the Earths (10 \( M_E \)). The upper value corresponds to a maximum mass of 30 \( M_E \) in the mass-radius relation of Fortney et al. (2007).
- \( 0.5 R_J \leq R_p \leq 1.1 R_J \) for the Jupiters. We derive the lower value from the upper mass limit we assume for the Neptunes. The upper limit corresponds to the maximum radius of a 4.5-Gyr planet at 1 AU in Fortney et al. (2007). We note that transit measurements find potentially larger planets (up to \( 1.4 R_J \)), but very close to the star. The inflated radius of these planets could be explained by additional mechanisms to stellar radiation (Fortney et al. 2010).

Figure 20 gives the minimum planet radius (in \( R_E \) units) for which SPICES is able to characterize the metallicity of giants or the cloud and forest coverage of terrestrial planets. The colors refer to the planet type (Jupiter, Neptune or Earth) and the line styles to the planet model (separation for the giants and cloud coverage for the Earths).

For G2 stars (Fig. 20, top panel), SPICES reaches the lowest radius we consider \( (0.5 R_J \sim 5.5 R_E) \) for the 0.8- and 2-AU Jupiters, for all stars within respectively 4 and 10 pc. About twenty G stars could be probed for Jupiters at 2 AU, while a few stars could be searched for Jupiters at 0.8 AU. For a Jupiter at 5 AU, the upper limit in radius \( (1.1 R_J \sim 12 R_E) \) is reached when the star is at 8.5 pc. The radius linearly decreases as the star distance decreases down to \( 8 R_E \) at 4 pc (flux proportional to the square ratio of the planet radius to the star distance). At shorter distances, the deviations from the linearity are due to the speckle noise. When the star distance decreases, the angular separation of the star-planet system increases and the level of the speckle background increases, especially towards the edges of the dark hole (Fig. 6). As for Neptune-like planets, the minimum radius scales nearly linearly with distance from \( \sim 2 \) to \( 4 R_E \) at 0.8 AU, and from 2 to 6 \( R_E \) at 2 AU. SPICES can characterize cloudy and clear telluric planets at 1 AU around a few G2 stars up to 5 pc (IWA limitation). Potentially, it is able to reach Earth-size planets for very close stars like \( \alpha \) Cen A (\( \sim 1.3 \) pc).

For A0 stars (middle panel), the only planet SPICES can study among the planetary atmosphere models we consider is the cloud-free Jupiter. We already noted the lack of models for separations smaller than \( \sim 4 \) AU (Sect. 3.3). The shortest separation available is 4.2 AU (Table 5), which is angularly resolved by SPICES when the star is closer than 21 pc. For this planet, the upper limit of the detectable radius roughly follows a linear
Table 8. Maximum star distance at which SPICES resolves the planet separation at the central wavelength of the bandwidth in the case of a M0 host star.

<table>
<thead>
<tr>
<th>Planet separation (AU)</th>
<th>Star distance (pc)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.24</td>
<td>7.2</td>
</tr>
<tr>
<td>0.3</td>
<td>1.5</td>
</tr>
<tr>
<td>0.6</td>
<td>3</td>
</tr>
<tr>
<td>1.5</td>
<td>7.5</td>
</tr>
<tr>
<td>3</td>
<td>15</td>
</tr>
</tbody>
</table>

determined that the contrast reached by the instrument meets the top-level requirements ($\sim 10^{-7}$ at 2 $\lambda/D$ and $\sim 10^{-10}$ at 4 $\lambda/D$). Then, we analyzed the impact of different sources of noise: detector read-out noise, exo-zodiacal intensity and photon noise considering several stellar types. We confirmed previous analyses that exodisks might be a major limitation for the characterization of faint planets, like Neptunes and super-Earths, because it biases the planet photometry (for disk intensity $\gtrsim 1$ zodi) and adds photon noise (≥ a few 10 zodi). Exodisk intensity calibration and target selection will be necessary to reduce this limitation. Using planet models calculated for a Sun-like star and assuming flux conservation, we found that the brightest stars (types AF) would not be the most favorable targets for SPICES. For instance, only planets with clear atmospheres will be detectable around A0 stars within ~20 pc. On the contrary, stars of types GKM will allow the detection of a large variety of planets as far as ~12 pc for a G2 star and ~7.5 pc for a M0 star: cloud-free, water-cloud and ammonia-cloud Jupiters, cloud-free and water-cloud Neptunes and telluric planets. After this general study of contrast performance, we focused on spectrometric abilities on planets around a solar-type star. We defined a criterion on the SNR of the measured spectra to determine if SPICES or an analog space mission could probe several planetary properties by disentangling their spectra (clouds and metallicity for giant planets, cloud and surface coverage for telluric planets). The results are very encouraging since SPICES could characterize the metallicity of Jupiters and Neptunes up to 10 pc and 6 pc respectively for a G2 star. The cloud and surface coverage of a super-Earth orbiting a Sun analog would also be characterized for systems closer than 5 pc. For A0 stars, the instrument could study the metallicity of cloud-free Jupiters closer than 17 pc. For M0 stars, cloudy Jupiters and Neptunes could be accessible at distances $\lesssim 7.5$ pc and $\lesssim 3$ pc respectively, and super-Earths at distances $\lesssim 3$ pc. These results would give a potential target list of $\sim 300$ stars. We also estimated the minimum radius for the planets SPICES could detect.

6. Conclusions

In this paper, we presented an analysis and an estimation of the performance of SPICES, a small coronagraphic space mission operating in the visible. From numerical simulations of the instrument concept given in Boccaletti et al. (2012), we first
polarimetric performance of SPICES, as we expect that the combination of flux and polarization measurements can remove degeneracies that arise when retrieving planet properties from flux measurements alone. Circumstellar disks are another science case to study (dust distribution, rings, planet gaps). Finally, another point of great interest would be to apply the methods we used here to a larger telescope like the Terrestrial Planet Finder Coronagraph (Levine et al. 2009). Indeed, one of the main results of our work is that the optimal targets of SPICES would be at separations of ~0.8–2 AU, because of the drastic decrease of the reflected flux. For these cases, the performance is limited by the angular resolution of the telescope and not the photon noise. The choice of the telescope diameter was anterior to this study and resulted from a trade-off between the science objectives and the budget allocated to a medium-class mission. We now consider to submit a larger (2.5–3 m) instrument as a large-class mission when a call for proposals will be issued. Besides these considerations, such a telescope will access a larger volume of target stars and will be less sensitive to zodiacal and exozodiacal contributions for planet spectra measurement (Traub & Oppenheimer 2010).

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Huitson, M., & Gillon, M. 2011, in The Search for Habitable Planets, ed. S. Seager
http://www.blue-dots.net

Table 9. SPICES performance summary for exoplanet spectroscopic characterization.

<table>
<thead>
<tr>
<th>Planet</th>
<th>Probed property</th>
<th>A0</th>
<th>Stellar type</th>
<th>M0</th>
<th>Sections</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>1 AU ≤ a ≤ 4.2 AU</td>
<td>0.25 AU ≤ a ≤ 0.8 AU</td>
<td>–</td>
<td>2.4.1, 4.2, and 5</td>
</tr>
<tr>
<td>Jupiter</td>
<td>Rayleigh scattering</td>
<td>5 pc ≤ d ≤ 17 pc</td>
<td>1.3 pc ≤ d ≤ 4 pc</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td></td>
<td>Solar metallicity 1x/3x</td>
<td>0.5 Rj ≤ Rp ≤ 1.1 Rj</td>
<td>0.25 AU ≤ a ≤ 5 AU</td>
<td>0.25 AU ≤ a ≤ 3 AU</td>
<td>–</td>
</tr>
<tr>
<td></td>
<td>Cloud coverage 0/50/100%</td>
<td>–</td>
<td>0.25 AU ≤ a ≤ 0.8 AU</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>Earth</td>
<td>Forest coverage 0/50/100%</td>
<td>0.5 Rj ≤ Rp ≤ 1.5 Rj</td>
<td>0.25 AU ≤ a ≤ 2 AU</td>
<td>0.25 AU ≤ a ≤ 1.5 AU</td>
<td>–</td>
</tr>
<tr>
<td></td>
<td>Forest coverage 0/50/100%</td>
<td>0.6 Rj ≤ Rp ≤ 1.1 Rj</td>
<td>1.3 pc ≤ d ≤ 10 pc</td>
<td>1.3 pc ≤ d ≤ 7.5 pc</td>
<td>–</td>
</tr>
<tr>
<td></td>
<td>–</td>
<td>1.3 pc ≤ d ≤ 4 pc</td>
<td>–</td>
<td>–</td>
<td></td>
</tr>
</tbody>
</table>

Notes. We strongly encourage the reader to refer to the rest of the paper to access the assumptions and the detail of the studies.

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