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<th>Iwase, Eiji, Pui-Chuen Hui, David Woolf, Alejandro W Rodriguez, Steven G Johnson, Federico Capasso, and Marko Lonar. “Control of buckling in large micromembranes using engineered support structures.” Journal of Micromechanics and Microengineering 22, no. 6 (June 1, 2012): 065028.</th>
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<tr>
<td>As Published</td>
<td><a href="http://dx.doi.org/10.1088/0960-1317/22/6/065028">http://dx.doi.org/10.1088/0960-1317/22/6/065028</a></td>
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<td>Publisher</td>
<td>IOP Publishing</td>
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<tr>
<td>Version</td>
<td>Author’s final manuscript</td>
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<tr>
<td>Accessed</td>
<td>Wed Mar 16 03:04:38 EDT 2016</td>
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Control of buckling in large nanomembranes using engineered support structures

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In this paper we describe a general method to avoid stress-induced buckling of thin and large freestanding membranes. We show that using properly designed supports, in the form of nanobeams, it is possible to reduce the out-of-plane deflection of the membrane while maintaining its stiffness. As a proof of principle, using silicon-on-insulator (SOI) platform, we realized 30-µm-wide, 220-nm-thick, free-standing Si membranes, supported by four 15-µm-long and 3-µm-wide nanobeams. Using our approach, we were able to achieve out-of-plane deformation of the membrane smaller than 50 nm in spite of 39 MPa of compressive internal stress. Our method is general, and can be applied to different material systems with compressive or tensile internal stress.

1. Introduction

Freestanding micro membrane structures are commonly used in microelectromechanical systems (MEMS) to realize, for example, variable capacitors [1], RF switches [1],[2], pressure sensors [3], movable mirrors [4]. In such freestanding structures, deformation by residual internal stress is a well known issue [5]-[7]. The stress, caused by the difference in thermal expansion coefficients of different materials, is often built-in during the process of thin film deposition and is therefore difficult to avoid. This is a problem since large compressive or tensile stress can lead to buckling or breaking of the membrane. The degree of buckling depends on the length/thickness ratio of a membrane structure: if the ratio is 100 or larger buckling can be significant even for low values of compressive stress (on the order of several tens of MPa). To reduce the effect of the internal stress, stress-reduction techniques based on the optimization of the deposition conditions [8], post-deposition annealing [9], stress-compensation by a deposition of another film [4], and ion implantation [9],[10] have been investigated. These are however material-specific solutions, and therefore cannot be applied in all situations. Moreover these stress compensation methods do not work at high temperatures because of the different thermal expansion coefficients. In this paper, we describe general method to control the out-of-plane strain and stiffness by using properly designed supporting beam structure. We use this method to realize large, free-standing Si membranes perforated with lattice of holes to define photonic
crystal (PhC) structure as shown in Figure 1.

Recently, there has been a lot of interest in realization of PhC membranes that support guided resonances for applications in the field of optomechanics [11]-[17]. These membranes are typically realized in semiconductor materials with large optical index, e.g. Si or InGaAs. To ensure a strong optomechanical interaction, thin (~ 200 nm) and large (~ several tens of µm) membrane structures, with length/thickness ratio of ~100, are desired. The small thickness allows for greater flexibility of the membrane (to enable strong response of the structure to the weak forces), while the large area is needed to assure good confinement of guided resonances supported by the membrane. Furthermore, the membrane and the substrate are separated by as few as hundreds of nm [12],[14]-[16], in order to enhance the optomechanical coupling. For all of these reasons, it is essential to reduce buckling of the membrane due to built-in internal stress and avoid failure of the structure.

2. Design

A 2-D PhC slab structure that supports guided resonances, and that we are interested in studying in this work, is shown in Figure 1(a). It consists of a 220-nm-thick free-standing (square-shaped) Si membrane of width 30 µm, supported by four nanobeams of length 15 µm. The membrane is perforated with PhC lattice of holes with periodicity $a = 1$ µm and hole radius of $r = 200$ nm. The structure was realized in a commercial SOI wafer (SOITEC Inc.) with 220-nm-thick Si device layer and 2-µm-thick BOX (buried oxide) layer. The structure was fabricated using electron beam lithography followed by inductive coupled plasma reactive ion etching (ICP RIE) and HF vapor etching. As shown in Figure 1(b), the 2-D PhC slab structure with simple straight supporting beams is buckled by its own internal stress. Our approach is to design beam structures in order to avoid the out-of-plane deformation without changing the out-of-plane stiffness of beams.

In the case of a simple beam structure with $l$, $w$, $t$ in length, width and thickness respectively, a critical buckling stress $\sigma_c$ is proportional to the inverse second power of the length/thickness ratio. In the case of doubly-clamped beams, the critical buckling stress is given by $\sigma_c = \frac{\pi^2}{3} E \left( \frac{t}{l} \right)^2$, where $E$ is the Young’s modulus of the structure. If the structure has a compressive internal stress $\sigma_0$ larger than the critical buckling stress ($\sigma_0 \geq \sigma_c$), then critical buckling length $l_c = \frac{\pi t}{\sqrt{3 \sigma_0}}$ can be defined so that all the beams with length $l > l_c$ will be buckled. Critical buckling length for $t = 200$ nm thick device layer of SOI wafer can be estimated to be in the range of $l_c = 13-41$ µm, taking into account the internal stress of $\sigma_0 = 10–100$ MPa typical in commercial SOI wafers and Young’s modulus of Si for the <110> direction of 169 GPa. Therefore, buckling can be large even in a structure with several tens of µm in length (Figure 2(a)). We note that the critical buckling length increases to $l_c = 196-620$ µm if the thickness of the Si device layer is increased to $t = 3$ µm. To evaluate the built-in stress in the wafers used in this experiment, we fabricated arrays of doubly-clamped beams with varying length and measured their out-of-plane deflection using a 3-D optical profiler (Olympus LEXT OLS4000, display resolution: 1 nm). The results, shown in Figure
2(b), are in good agreement with the theoretical model discussed above. Using these values, we estimated the compressive internal stress of the Si device layer of the SOI to be 39 MPa, resulting in critical buckling length \( l_c = 26.3 \mu m \). This explains significant buckling of PhC membrane (Figure 1) with total length larger than \( l_c \).

In order to overcome buckling issue, it is necessary to engineer the supporting beams. Fundamentally, buckling appears when a compressive internal stress acts as an axial load to a supporting beam (Figure 3(a)). Therefore, our design methods are classified into three categories based on the type of the deflection induced by compressive stress. “Type 1” method leads to in-plane buckling instead of out-of-plane buckling (Figure 3(b)) due to axial load. “Type 2” method leads to in-plane deformation without buckling (Figure 3(c)) due to axial load. This is achieved by taking advantage of beams with an initial deflection (i.e. curved beams). Type 2 beams can be deformed below the in-plane critical buckling stress, whereas Type 1 beams are deformed only by the in-plane critical buckling stress or more. “Type 3” method uses a lateral beam in order to act compressive stress as a lateral load. (Figure 3(d)). Type 2 and Type 3 can be described as methods of releasing the internal stress by in-plane deformation.

For the Type 1 method to work it is important that in-plane critical buckling stress \( \frac{\pi^2}{3} \frac{E}{w} \left( \frac{w}{l} \right)^2 \) is smaller than the out-of-plane critical buckling stress \( \frac{\pi^2}{3} \frac{E}{t} \left( \frac{w}{l} \right)^2 \). Therefore, an extremely narrow and long beam is required which may be challenging to implement. In addition, Type 1 is only effective in the case of compressive stress, while Type 2 and Type 3 can be used for both compressive and tensile stress.

Types 2 and 3 are based on the similar idea: the stiffness of a simple straight beam against an axial load (i.e. in-plane stiffness) is \( E \frac{wt}{l} \). Therefore, if part of the beam has in-plane stiffness smaller than \( E \frac{wt}{l} \), the part can relieve the internal stress by its elastic deformation. However, we do not want to reduce the out-of-plane stiffness (i.e. out-of-plane spring constant), because the supporting beams have to play two roles: (1) reducing the out-of-plane deformation and (2) supporting the membrane structure. Therefore we use a “multiple narrow beam structure”, shown in Table 1. Table 1 shows the in-plane and out-of-plane stiffness of a simple straight beam and Type 3 beams. Using a “multiple narrow beam structure” it is possible to reduce the in-plane stiffness while maintaining the same out-of-plane stiffness, compared to a simple straight beam. That is, if we change from a simple lateral beam to \( n \) beams with \( 1/n \) in width, we can get \( 1/n^2 \) times smaller stiffness in the in-plane direction while maintaining the same out-of-plane stiffness (shown in Table 1). The same analysis applies to Type2 beams, and is shown in Table 2.

3. Fabrication and evaluation

To verify our designs, we fabricated the structures discussed in previous section, using the same SOI wafer as in Figure 2. The SEM images and the beam deflections measured using a 3-D optical profiler are shown in Figure 4. The length,
width and thickness of the beams are 100 µm, 3 µm and 220 nm, respectively. Figure 4(c) shows a simple straight beam with 1,212 nm of out-of-plane deflection due to buckling. Figure 4(e) shows multiple narrow Type 2 structures which consist of 8 narrow curved beams with 200 nm widths. Figure 4(f) shows multiple narrow Type 3 structures which consist of 15 narrow lateral beams with 200 nm widths. Maximum deflections of the multiple-narrow Type 2 and Type 3 structures are 280 nm and 114 nm, respectively. As can be seen, the out-of-plane deflections are highly reduced using our proposed methods. Figure 4(d) is a beam with multiple narrow straight beams without initial deflection, so the beam also suffers out-of-plane buckling of 1,211 nm. Though we could not measure the in-plane deformation in Figure 4(e), we can obviously confirm the effect of initial deflection (i.e. curved beam) by comparing to the out-of-plane deflection of Figure 4(d).

Figure 1(b) and Figure 5(a), (b) show the photonic crystal membrane structures with simple, Type 2 and Type 3 supporting beams, respectively. Using the profiler, we measured the maximum deflections of Type 2 and Type 3 to be 49 nm and 33 nm, respectively. This is more than an order of magnitude smaller than a maximum deflection (568 nm) measured for the membrane with simple supporting beams (Figure 1(b)). Finally, we note that since the supporting beams relieve the internal stress, the membrane itself does not bend (below the resolution of our apparatus) under the internal stress, and is very flat. This is of great importance for photonic applications that we envisioned.

4. Discussion

Approaches to reduce the out-of-plane buckling/deflection by designing proper supports, using methods that fall in categories Type 2 [18] or Type 3 [19],[20], have previously been studied. The novel aspect of our work is application of multiple narrow beam structures that offer very important advantages over other methods: in-plane and out-of-plane stiffness can be designed almost independently. That is, by increasing \( n \), we can reduce the in-plane stiffness of the beam without changing the out-of-plane stiffness.

In the case of simple beam, the internal stress before (\( \sigma_0 \)) and after (\( \sigma_f \)) releasing are the same, up to the critical buckling stress \( \sigma_c \) or the breaking stress \( \sigma_b \) (Figure 6). Therefore the simple beam can be used as long as the internal stress \( \sigma_0 \) is a value between \( \sigma_c \) and \( \sigma_b \). In the case of Type 2 or Type 3 beams, with smaller in-plane stiffness, \( \sigma_0 \) and \( \sigma_f \) are different due to the in-plane elastic deformation of the beam. Therefore, we define two new parameters allowable compressive stress \( \sigma_{AC} \) and allowable tensile stress \( \sigma_{AT} \) defined in a following way: if the initial stress \( \sigma_0 \) is \( \sigma_{AC} \) and \( \sigma_{AT} \), the final stress \( \sigma_f \) would be \( \sigma_c \) and \( \sigma_b \), respectively (see Figure 6). As a result, Type 2 and Type 3 beams can be used as long as the initial internal stress \( \sigma_0 \) has a value between \( \sigma_{AC} \) and \( \sigma_{AT} \). In the case of the multiple narrow beam structure, \( \sigma_{AC} \) and \( \sigma_{AT} \) are proportional to \( n^2 \). Therefore it is always possible choose \( n \) which satisfies this condition, which makes approach general and useful for range of geometries and films deposited using different techniques. However, in practice the upper limit of \( n \) is set by the minimum resolution of the fabrication process, since the larger the \( n \), the smaller the width of each beam in multi-beam section. If the
characteristic beam width is $w_0$ and the minimum available width on the fabrication is $w_{\text{min}}$. $n$ should be smaller than $w_0/w_{\text{min}}$. For example, our characteristic beam width was 3 µm and the minimum resolution is approximately 50 nm because of electron beam lithography, so the upper limit of $n$ is 60. As we mentioned, the allowable stresses $\sigma_{\text{AC}}$ and $\sigma_{\text{AT}}$ are proportional to $n^2$, so our method can deal with wide range of the internal stress. This is another unique feature of our method, and has not been investigated before. The approach is material-platform agnostic which further adds to its versatility. In addition, because our method can release internal stress of any magnitude as long as the stress is smaller than the allowable internal stresses, we do not have to know the precise internal stress of the membrane. In other words, if we choose a large enough value $n$, our beams make proper in-plane deformations according to the magnitude of internal stress, automatically. This is very effective, especially for mitigation of temperature induced stress the value of which can greatly vary with temperature: our approach’s “self-adaptability” to internal stress makes it effective for a wide range of temperatures.

Though our method highly reduced the out-of-plane deflection, the structures still have finite deflection < 50 nm. We believe that this is due to stress gradient of the membrane and/or a bending moment at its ends, which also can cause asymmetric upward and downward deflections. Indeed, it can be seen in Figure 2(b) that the upward and downward deflections are slightly different (~ 80 nm). The stress gradient comes from the wafer fabrication process and the bending moment at the ends comes from the residue of the sacrificial layer under the membrane. Since the 2-D PhC slab region is very flat (in Figure 5(a), (b)) and the most of the deflection is due to the supporting beam region, we can conclude that the residual deflection is not due to the stress gradient, but rather due to the bending moment at the beam ends. Though our method cannot deal with a stress gradient and a bending moment at the ends, these effects cause little deflection.

5. Conclusions

We proposed a method to reduce the out-of-plane deflection of a membrane structure due to its internal stress, while maintaining the out-of-plane stiffness of the structure. Using the multiple narrow Type 2 and Type 3 supporting beam structures, it is possible to precisely engineer the residual stress simply by changing number of beams ($n$). Applying our methods to a commercial SOI wafer with 39 MPa of compressive internal stress, we were able to reduce the out-of-plane deflection of the freestanding membrane for more than order of magnitude, from 568 nm to below 50 nm. In the cases of Type 2 and Type 3 structures, the maximum deflections were 49 nm and 33 nm, respectively. The characteristic length and thickness of the membrane structure is 60 µm and 220 nm, respectively, so that the length/thickness ratio of our membrane structure is 273 and the maximum deflection/length ratio is less than 1/1,000. These values mean the freestanding thin and large membrane structure has little out-of-plane bending. In addition, our method can deal with a range of stress values and therefore it is suitable for compensation of not only the compressive but also the tensile internal stress. Furthermore, it can be used at high temperature, since it can handle temperature induced stress.
Acknowledgement

This work was supported by the Defense Advanced Research Projects Agency (DARPA) under Contract No. N66001-09-1-2070-DOD. The deflection measurement was performed by the 3-D optical profiler Olympus LEXT OLS4000 owned by Prof. Robert Woods at Harvard University. The microstructure fabrication was carried out using the facilities of Center for Nanoscale Systems (CNS) at Harvard University.

Figure legends

Figure 1  (a) Schematic image of a target structure and the typical lengths. The structure consists of the thin and large 2-D PhC slab and supporting beams. (b) Buckling of the thin and large membrane structure by its own internal stress.

Figure 2  Deformation by the internal stress on a commercial SOI wafer with 220 nm in a device layer thickness $t$. (a) The doubly-clamped beams are buckled upward or downward. (b) Evaluation of the internal stress. Each length of the beams is $l = 4, 10, 20, 30, 40, 50, 60, 70, 80, 90, 100 \, \mu m$. The horizontal axis is an effective beam length $l_{\text{eff}}$ which means that designed beam length $l$ plus a constant undercut-length. In this graph, undercut length is 23 \, \mu m. Blue and red dots are deflections of upward and downward buckling, respectively. Error bars refer to the standard deviations. The difference between upward and downward buckling should be come from stress gradient and bending moment at the ends. The dashed line is a fitting curve of a theoretical deflection $v_{\text{max}} = 2 \left( \frac{a_0 l w t}{E} \frac{l^2}{\pi^2} - \frac{l^2}{3} \right)$ under $\sigma_0$, of 39 \, MPa.

Figure 3  Classification of beam structure that overcome out-of-plane buckling due to an axial load. The principle is based on inducing in-plane deformation to overcome out-of-plane one due to an axial load.

Table 1  In-plane and out-of-plane stiffness of a simple straight beam and Type 3 beams. Stiffness is defined by a load/deformation ratio (i.e. $F/v_{\text{max}}$). In the case of a simple straight beam, the in-plane stiffness is $E \frac{w t}{l}$ and the out-of-plane stiffness is proportional to $E \frac{w t^3}{l^3}$. The coefficients $a, b$ are determined by load and end conditions. For example, in the case of a doubly-clamped beam under point loading at the center, $a=16$. In the case of a guided-clamped beam under point loading at the free end, $a=b=1$. 
Table 2  In-plane and out-of-plane stiffness of Type 2 beams. We can use the same analysis as with the Type 3 under the assumption that length/width ratio is large.

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Figure 6  Controlling the allowable stress using engineered support structures: The released membrane structure is flat when (no buckling) when the final internal stress after releasing $\sigma_f$ is between $\sigma_c$ and $\sigma_b$, where $\sigma_c$ and $\sigma_b$ are the critical buckling stress and the breaking stress, respectively. This corresponds to an initial internal stress before releasing $\sigma_0$, it means that $\sigma_0$ is a value between $\sigma_{AC}$ and $\sigma_{AT}$, where $\sigma_{AC}$ and $\sigma_{AT}$ are the allowable compressive and tensile stress, respectively. In the case of a simple straight beam, $\sigma_{AC}$ and $\sigma_{AT}$ should be the same as $\sigma_c$ and $\sigma_b$, respectively. But the beam has smaller stiffness beam with $k$ in the in-plane stiffness, $\sigma_{AC}$ and $\sigma_{AT}$ is enlarged approximately as $\frac{k_0}{k} \sigma_c$ and $\frac{k_0}{k} \sigma_b$, where $k_0 = \frac{Ew_0^3}{l_0^3}$, $l_0$ is the beam length from end to end, and $w_0$ is the beam width at the end. If the multiple-narrow Type 2 or Type 3 structure is used, the in-plane stiffness $k$ is described by the formula $k = \frac{a}{n^2} E \frac{w_0^2 t}{l^2}$ as shown in Table 1 and 2.

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Table 2 In-plane and out-of-plane stiffness of Type 2 beams. We can use the same analysis as with the Type 3 under the assumption that length/width ratio is large.

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<td>Multiple Narrow Type 2 Structure</td>
<td>( \sum a_i \times E \frac{mwy^{2i+1}l}{l^{2i+1}} = a_1 \times E \frac{w^3l}{l^3} \frac{1}{n^3} )</td>
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<th>(d)</th>
<th>(e)</th>
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<td>max deflection</td>
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<td>1,211 nm</td>
<td>280 nm</td>
<td>114 nm</td>
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