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Reducing deformation anisotropy to achieve ultrahigh strength and ductility in Mg at the nanoscale

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In mechanical deformation of crystalline materials, the critical resolved shear stress (CRSS; \(\tau_{\text{CRSS}}\)) is the stress required to initiate movement of dislocations on a specific plane. In plastically anisotropic materials, such as Mg, \(\tau_{\text{CRSS}}\) for different slip systems differs greatly, leading to relatively poor ductility and formability. However, \(\tau_{\text{CRSS}}\) for all slip systems increases as the physical dimension of the sample decreases to approach eventually the ideal shear stresses of a material, which are much less anisotropic. Therefore, as the size of a sample gets smaller, the yield stress increases and \(\tau_{\text{CRSS}}\) anisotropy decreases. Here, we use in situ transmission electron microscopy mechanical testing and atomistic simulations to demonstrate that \(\tau_{\text{CRSS}}\) anisotropy can be significantly reduced in nanoscale Mg single crystals, where extremely high stresses (~2 GPa) activate multiple deformation modes, resulting in a change from basal slip-dominated plasticity to a more homogeneous plasticity. Consequently, an abrupt and dramatic size-induced “brittle-to-ductile” transition occurs around 100 nm. This nanoscale change in the CRSS anisotropy demonstrates the powerful effect of size-related deformation mechanisms and should be a general feature in plastically anisotropic materials.

In this regard, we show that \(\tau_{\text{CRSS}}\) may sound counterintuitive. Here, we choose to investigate experimentally is the dislocation free-arm length, \(D\), which will lead to a reduced \(\tau_{\text{CRSS}}\) (nonbasal) \(\tau_{\text{CRSS}}\) (basal) that should give rise to latent hardening and more homogeneous plastic flow. In this regard, we are encouraged by the theoretical prediction that ideal shear strengths [theoretical upper bound to CRSS (9)] of Mg are far less anisotropic, with an anisotropy ratio of ~2 as determined from our first-principles calculations (detailed in SI Text). Broadly speaking, the tradeoffs between strength and ductility are well recognized in the materials science community (10, 11), so enhancing ductility by increasing both \(\tau_{\text{CRSS}}\) (basal) and \(\tau_{\text{CRSS}}\) (nonbasal) should sound counterintuitive. Here, we find that this strategy indeed can work and that the plastic anisotropy ratio, \(A(D)\), is an essential quantity that can be engineered by nanostructuring.

The parameter \(D\) we choose to investigate experimentally is the size of a single crystal domain. As illustrated in Fig. 1A, according to the well established “smaller is stronger” trend (12–14), \(\tau_{\text{CRSS}}\) (basal) and \(\tau_{\text{CRSS}}\) (nonbasal) should both increase with decreasing \(D\). However, because \(\tau_{\text{CRSS}}\) (basal) and \(\tau_{\text{CRSS}}\) (nonbasal) have upper bounds at their respective ideal shear strengths (9) at small \(D\), an anisotropy ratio of ~100 is simply unsustainable. As such, \(A(D)\) is predicted to decrease gradually from ~100 to ~2, which should facilitate more stable and homogeneous plastic flow due to interactions between more dislocation slip systems in three dimensions (i.e., latent hardening). Generally, \(\tau_{\text{CRSS}} \sim \beta G b / L + \tau_0\), where \(L\) is the dislocation free-arm length, \(\beta\) is dimensionless quantity ~1, \(G\) is the shear modulus, \(b\) is the Burgers vector, and \(\tau_0\) is the lattice friction stress (15, 16). Considering the dislocation free-arm length in coarse-grained materials is usually on the order of \(10^{-6}\) m, the value of \(\beta G b / L\) is roughly several megapascals; thus, the huge difference between the \(\tau_{\text{CRSS}}\) for basal and nonbasal slip is mainly determined by the anisotropic lattice friction stress \(\tau_0\). This has been evidenced by previous experiments and simulations, which showed \(\tau_0\) (basal) \(\approx 10^{-5}\) \(\tau_0\) (nonbasal) (17–19). Interestingly, as the grain size/sample size decreases to the same order as the dislocation free-arm length, \(L\) will become directly regulated by \(D\) so that \(L \propto D^\alpha\), where \(\alpha\) is a positive exponent. As grain/sample size becomes nanoscale, the value of \(\beta G b / L\) will be \(10^3\)–\(10^4\) times larger, and then \(\tau_{\text{CRSS}}\) will no longer be determined by \(\tau_0\) but by the sample dimension (20). It is also of note that the Hall–Petch scaling \(\tau_{\text{CRSS}} \sim k D^{-\alpha/2} + \tau_0\) cannot stay true for very small values of \(D\) because \(\tau_{\text{CRSS}}\) is limited by the ideal shear strength, when homogeneous dislocation nucleation can occur even at a temperature of 0 K (21, 22). With this physical context and the related boundary conditions for the \(A(D)\) function, we expect a more isotropic and homogeneous plastic flow with dimensional refinement and strength elevation.

**Author contributions:** Q.Y., L.Q., R.K.M., J.L., and A.M.M. designed research; Q.Y. and L.Q. performed research; Q.Y., L.Q., R.K.M., J.L., and A.M.M. analyzed data; and Q.Y., L.Q., R.K.M., J.L., and A.M.M. wrote the paper.

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Fig. 1. (A) Schematic representation of the concept of reducing the CRSS anisotropy by decreasing the size scale. (B) Typical stress–strain curves of samples with different sizes. In addition to the “smaller is stronger” trend, the samples with extremely small size show a dramatically longer plastic stage. (Inset) Crystallography and loading condition are shown. (C) Plot of yield strength vs. the inverse of the sample gauge size $d^{-1}$, the power law regime, and the stress saturation regime, respectively, can be seen. (D) Plot of fracture strain and uniform elongation before necking vs. sample gauge size $d$ showing a significant transition in plasticity when the sample size approaches ~100 nm.

**Results**

Here, we use quantitative in situ transmission EM (TEM) tensile tests on single crystal Mg samples with different sample sizes to probe directly the nanoscale size effect on the plastic anisotropy. We investigated samples that were prepared by focused ion beam (FIB) milling, followed by low-energy Argon ($\text{Ar}^+$) cleaning. All the experiments presented here were performed on pure Mg single crystals loaded in tension along an axis $45^\circ$ from the basal plane, which is schematically shown in Fig. 1B (Inset). This orientation was chosen specifically to favor basal slip. The sample sizes ranged from ~850 nm to 80 nm. The possible Ga$^+$ contamination from the FIB process was analyzed before mechanical testing by high-resolution TEM characterization. The results show that the thickness of the surface damage layer resulting from the milling is about 2 nm (details are provided in SI Text). The detailed experimental process is described in SI Text as well, including examples of the initial dislocation structure (Fig. S1), where it can be seen that the size of the sample inherently limits the length of the dislocations. This method offers several advantages: (i) the crystal orientation can be well defined to benefit a certain slip system, and more clear analysis and comparison can be achieved; (ii) the dimension is the only tunable parameter (no grain boundaries or constraint from neighboring grains) and can be well controlled to regulate the length of the dislocations; (iii) the in situ TEM technique can provide a direct relation between the microstructural evolution and the mechanical response of a sample; and (iv) because we eliminated the texture effect and grain boundary effect, the fundamental mechanism can be directly assigned to the intrinsic size effect. The same results were reproduced in nanocompression tests on Mg nanoparticles (no FIB damage) and in molecular dynamics (MD) simulations, which verified the intrinsic nature of this nanoscale size effect.

Fig. 1B shows a comparison between typical stress–strain curves from different sample sizes. Special attention should be paid to the samples smaller than 100 nm, where ultrahigh yield stresses and significantly larger values of failure strain are observed. In addition, when calculated as true stress (shown in SI Text), the extended elongation in samples smaller than 100 nm actually demonstrates work hardening (shown in Fig. S2). The relation between size and strength is plotted in Fig. 1C (here, we define the yield strength as the stress at which the first deviation from linearity is found in the stress–strain curve). The curve first shows a power law relation, where the exponent $\alpha$ is around 1, until about ~100 nm, where the yield strength saturates at around 2 GPa. For comparison, we have used ab initio calculations to find the theoretical tensile strength of Mg in the tested orientation to be ~3.6 GPa (details are provided in SI Text), indicating that over half of the theoretical strength was achieved experimentally. Coincident with the plateau in strength, there is a significant transition in the elongation to failure, as shown in Fig. 1D. The values of fracture strain suddenly jump to over ~10% when the sample size is reduced to ~100 nm and reach almost 30% in specific cases, compared with 4% in larger samples. The scatter in the data might be partly due to the difficulty in precisely controlling the aspect ratio at the nanoscale. However, it is worth noting that the uniform elongation before necking should be independent of the aspect ratio. Therefore, we calculated the true stress–strain value (details are provided in SI Text) and plotted the uniform elongation with size (Fig. 1D), where the same trend of transition was observed. The corresponding deformation mechanisms that are responsible for the size-related mechanical behavior are described below. The largest samples demonstrate work hardening and necking behavior as shown in Fig. 1B and Fig. 2 A and B. The strength was higher than the bulk counterpart due to the limited sources.
in the confined volume. As the sample size was decreased to between ~200 and ~400 nm, the ductility became dramatically limited. Dislocation activities were much more localized (shown in Fig. 2 C and D), and failure occurred at ~3–4% engineering strain due to localized shear along the basal plane, as shown in Fig. 2E. So, although significant size strengthening was achieved around 200–400 nm, the plastic anisotropy, A(D), remained large and the higher stresses led to rapid shear localization and poor ductility. Detailed analysis and the related movies (Movies S1–S3) are presented.

As the sample size was reduced to below ~100 nm, there was a remarkable shift in deformation behavior seen both from the stress–strain curves (Fig. 1B) and the in situ observations (Fig. 3). The stress vs. strain behavior shows an extremely long plastic stage with flow stresses close to ~2 GPa (and strain hardening when considering the true stress; SI Text). We must emphasize that the 2-GPa stress here should be compared with local stress instead of the global stress in polycrystalline materials. Comparing samples before and after the tests shows significant elongation and reduction in cross-sectional area (an example is given in Fig. 3A and Movie S4). Fig. 3B and Movie S5 show an example of the motion of a $<c+a>$ dislocation with a Burgers vector along $[11\bar{2}3]/[\bar{1}2\bar{3}3]$, even though basal slip is strongly favored in this orientation (details of dislocation analysis are shown in Fig. S3). Compared with the easy glide of basal dislocations, the low mobility observed in the $<c+a>$ dislocation during its pinning/unpinning motion indicates stronger dislocation interactions and a greater likelihood of the crystal maintaining a high dislocation density during deformation. This effect would lead to a stronger dislocation interaction, creating plastic strain along both the $<c>$ and $<c+a>$ directions, and would explain the high ductility observed in this size regime. However, it is also possible to observe nonbasal slip in larger samples, as illustrated by previous studies (5, 23–25). Therefore, the critical mechanism for the improved ductility in the small size regime should be not only the activation of nonbasal slip but the relative amount of the nonbasal contribution to plastic strain. To illustrate this further, we investigated the slip steps at the surface of deformed samples in the small size regime; a typical high-resolution TEM image is shown in Fig. 3C. The related diffraction pattern and the crystallography viewed from this direction are shown schematically in the lower part in Fig. 3C, with detailed trace analysis described in SI Text. Importantly, it was observed that nonbasal slip steps, including both $<c>$ and $<c+a>$ slip, were found in similar amounts as basal slip. Consistent with the transition in plastic behavior in this size regime, the fracture surfaces changed to a “cup-cone” shape as shown in Fig. 3D, compared with the pure shear localization on the basal plane seen in the larger samples. All these observations lead one to conclude that the $\tau_{CRSS}$ anisotropy must be significantly reduced at sample sizes below 100 nm so that a full complement of slip systems, including the critically important $<c+a>$ dislocations, is activated and significantly contributes to the plastic deformation, leading to ultrahigh strength and ductility.

To clarify further the influence of FIB damage on the results from the tensile samples, we also performed in situ TEM compression tests on FIB-free Mg nanoparticles with different sizes but of similar orientation to the tensile samples. The Mg nanoparticles were produced by a dc arc plasma method, and their
shows the load-displacement curve of a relatively large particle and a small particle, and Fig. 4C displays the TEM images for a large particle and a small particle before and after compression, respectively. From the mechanical data, in situ movies (Movies S6 and S7), and diffraction analysis, it was clear that the large particles (∼400 nm) mainly deformed by means of the localized shear along the basal planes, which generated significant strain bursts and a catastrophic load drop on the mechanical curve. On the other hand, the smaller particles (∼100 nm) deformed through more homogeneous dislocation activity that resulted in more continuous plastic flow. The dislocation analysis in the deformed particles revealed a large number of $\langle c + a \rangle$ dislocations; no localized shear and strain bursts occurred in these particles. The strong activity of nonbasal slip in smaller particles indicated the significant reduction of CRSS anisotropy, which was consistent with the tensile results above.

**Discussion**

The proposed mechanism for the enhanced ductility also agrees well with our results from computational simulations. First, our generalized stacking fault (GSF) γfi calculations (Fig. 5A) show that maximum $\gamma fi$ values are 2.57 GPa for full basal and 1.30 GPa for partial basal and 1.99 GPa and 2.62 GPa for prismatic and pyramidal, respectively, which are good approximations of ideal shear strengths, are comparable with the ~2 GPa tensile yield stress observed in samples smaller than 100 nm, which indicates that it is energetically possible for the applied stress to overcome the dislocation nucleation barriers of all these slip systems. In addition to the energetic considerations, we investigated the dynamical behavior of dislocations by performing a series of MD simulations of tensile tests on Mg nanostructures with the same orientation as in the experiments (details are provided in SI Text and Figs. S4–S9). As can be seen in Fig. 5B, the simulation results are consistent with the experimental results, including the size-independent stress saturation and the high-level flow stresses achieved. Detailed analysis of the simulations reveals the nucleation of multiple types of dislocations even though the crystal orientation heavily favors basal slip (Fig. 5C and Movie S8) and also cross-slip from the basal plane to the prismatic plane. As shown in Fig. 5D, before eventually slipping out of the samples, different types of dislocations can interact with each other and temporarily increase the dislocation density, contributing to the plastic strain while preserving the flow stress. Another critical factor for combined ultrahigh strength and ductility is the dispersed nucleation in the smallest size regime (one example is shown in Movie S9), which facilitates more uniform deformation. From the experimental and simulation results, it can be concluded that the extremely high strength in the smallest samples can "turn on" dislocation behavior that is uncommon in bulk materials, including surface nucleation, cross-slip, and $\langle c + a \rangle$ slip, all of which strongly enhance the ductility by the reduction of plastic anisotropy. An increase in ductility at small size scales has been proposed for brittle materials, where energetic scaling laws are used to analyze fracture (28). However, in our case, the scaling of fracture does not seem to be the dominant effect, because the extensive plastic deformation we observe before planar localization would alter these energetic scaling laws so that the simple size scaling of a planar fracture criterion cannot be applied here.

Our rationale and strategy to engineer A(D) should be quite general for high plastically anisotropic materials. Internal dimension refinement is one practical method for limiting the dislocation length, L, which should enhance CRSS levels and suppress A(D). We believe that boundaries would also be an effective way to engineer A(D) because of two special features. First, stress concentrations near boundaries result in much higher local stresses compared with the global stress, so it is possible to achieve the critical stress required to reduce deformation anisotropy; this phenomenon is more significant in nanocrystalline materials (29). Second, because of variations in atomic arrangement, nonideal boundaries offer clear sources for the nucleation and emission of dislocations (30, 31). It has been reported that Mg alloys processed by equal channel angular processing or hot rolling for grain refinement exhibit not only higher yield stresses but larger elongations at room temperature (32–34). However, conflicting results have also been reported mainly due to the texture characteristics and complication of deformation twinning (35, 36). By eliminating the complicating effects of grain boundaries and compatibility from neighboring grain orientations, our in situ TEM experiments revealed the intrinsic size dependence of plastic anisotropy and offered clear evidence that it is indeed possible to achieve both high strength and high ductility by tuning the external dimensions of the sample. The result is that the $\tau_{CRSS}(D)$ for basal and nonbasal slip can be on the same order in confined dimensions even though they are strongly anisotropic at larger sizes. Presumably, the critical dimension for this effect to manifest is material-dependent and sensitive to the chemical composition and GSF energy.

It is worth noting that the yield strength saturated when the transition occurred at 100 nm, with the stress value close to the ideal strength. The high strengths and shorter dislocation lengths can help to turn on alternative slip behavior that is not common in bulk materials (37, 38). In essence, small dimensions lead to high strengths that can activate secondary deformation mechanisms that make the deformation more uniform by promoting latent hardening and dislocation storage, leading to high ductility. More
broadly, we have revealed the size dependence of plastic anisotropy and the intrinsic nanoscale size effect of the reduction in plastic anisotropy to show that high strengths can be beneficial for ductility and formability in plastically anisotropic materials.

**Materials and Methods**

Single crystal Mg and Mg nanoparticles are tested under tension and compression, respectively. The crystal orientations of each are chosen to favor basal slip. Detailed materials and methods are described in SI Text, including dislocation analysis, deformation characteristics, trace analysis of the slip steps, and details of the density functional theory and MD calculations.

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