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Critical-current reduction in thin superconducting wires due to current crowding

H. L. Hortensius,1 E. F. C. Driessen,1 T. M. Klapwijk,1 K. K. Berggren,1,a) and J. R. Clem2
1Kavli Institute of Nanoscience, Faculty of Applied Sciences, Delft University of Technology, Delft, The Netherlands
2Ames Laboratory and Department of Physics and Astronomy, Iowa State University, Ames, Iowa 50011 USA

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We demonstrate experimentally that the critical current in superconducting NbTiN wires is dependent on their geometrical shape, due to current-crowding effects. Geometric patterns such as 90° corners and sudden expansions of wire width are shown to result in the reduction of critical currents. The results are relevant for single-photon detectors as well as parametric amplifiers.

Superconducting wires made of strongly disordered superconducting materials such as NbN and NbTiN are used for single-photon detection,1–3 single-electron detection,1 and parametric amplification.2 In all cases, for optimal performance, the devices are biased at as high currents as possible, without exceeding the critical current. In principle, for wires smaller than both the Pearl length \( \Lambda = 2 \lambda^2/d \) (\( \lambda \) is the dirty London penetration depth and \( d \) is the film thickness) and the dirty-limit coherence length \( \xi \), the critical current is determined by the critical pair-breaking current, which has been theoretically calculated over the full temperature range by Kupriyanov and Lukichev.4 These predictions have been tested experimentally in aluminium by Romijn et al.5 and Anthore et al.6 In many practical cases, it is found that the critical current varies from device to device and is significantly lower than this intrinsic maximum value. This reduction is usually attributed to defects in the films and slight variations in width. In addition, for strongly disordered superconductors electronic inhomogeneity may develop, even for homogeneously disordered materials.10 However, Clem and Berggren,11 responding to the observed dependence of the critical currents of superconducting single-photon detectors on the fill factor of the pattern,12 explained that the critical current may depend on geometric factors in the wires, such as bends. In their model analysis, the superconducting wires were narrower than the Pearl length, but wider than the coherence length. Consequently, the current is not necessarily uniform, and the critical current is reached when the current density locally exceeds the critical pair-breaking current. At this current, a vortex enters the superconducting wire, causing the transition to a resistive state.13

In this Letter, we present an explicit comparison of critical currents of superconducting NbTiN nanowires with different geometrical shapes and confirm that the observed critical current depends on the geometry.

In the analysis of Clem and Berggren,11 the sheet-current distribution is calculated for a given geometry using conformal mapping. Then, the critical current is defined as the current at which the Gibbs-free-energy barrier for a vortex to enter the film is reduced to zero. Any geometry where the current is led around a sharp feature, even when spreading into a suddenly widening portion of the wire, is predicted to lead to an increase in local current density at the inner curve of the corner, and a correspondingly reduced critical current. This behavior is similar to that in a normal-metal current divider, in which the shorter, lower-resistance, path around the inner corner carries a higher proportion of the current than the outer, higher-resistance, path. Fig. 1 shows the current streamlines in a superconducting thin-film wire for two cases: (a) a sharp 90° turn and (b) a sudden widening or stub. Note the increased current density in the inner corner. The dashed curve in (a) follows a contour where the current density equals the current density of an infinite straight wire. Outside this contour, the current never exceeds the average current density in the straight wire segment. Therefore, a corner conforming to this geometry will always be able to carry the current supplied to it, without exhibiting a reduction in the critical current. The shape of this optimally rounded corner is given in Eqs. (112) and (113) of Ref. 11. Even though, in the structure in Fig. 1(b), material is added with respect to a straight wire of width \( W \), the critical current is still predicted to be reduced.

Fig. 2 shows examples of the four patterns we used to test the theoretical predictions of Ref. 11: (a) straight wires (3 devices); (b) corners with optimally designed inner curves, (2 devices); (c) corners with sharp inner curves,
Devices were inspected using electron microscopy after electrical testing. All structures designed to be 1 \mu m wide had an actual width of \sim 970 \text{nm}. The inner curves of nominally zero-radius corners were observed to have an inner radius of \sim 60 \text{nm}. We ascribe this curvature to imperfect fabrication resolution.

The devices were tested in a dipstick probe in liquid helium with a base temperature of 4.2 K. The temperature of the sample stage was controlled by a heater element. We tested the devices by ramping a low-noise home-built current supply with a programmed ramp from 0 to 500 \mu A and back down to 0 \mu A with a 100 Hz repetition rate and measuring the resulting voltage over the wire. We determined the critical current by recording the current at which a threshold voltage across the device was passed during the positive portion of the current ramp. All results presented here were measured on a single chip and in a single testing session.

Fig. 3 shows the resulting histograms from the critical current measurements at 4.2 K. We recorded 1000 successive critical currents for each device. The straight wires (a) and wires with an optimally rounded inner corner (b) show averaged critical currents ranging from 382 \mu A to 560 \mu A. All three devices with a sharp inner corner (c) exhibit a lower critical current between 280 \mu A and 292 \mu A. Note that two of the sharp-corner histograms are overlapping at 280 \mu A. The device with a straight wire with a stub (d) has a critical current of 358 \mu A. The devices with sharp corners and the device with a stub all exhibit a narrower distribution of critical currents over their 1000 measurements, which can be seen from the height of the peak in the histogram.

We interpret the small variation in critical currents between the three different wires with a sharp corner (c) as an indication that indeed the corner is the dominant weakest link. For the straight (a) and rounded (b) wires, there is no natural point for the switching to nucleate. Therefore, the critical current is sensitive to possible inhomogeneities. For example, on inspection, we discovered that occasionally the wires contain a pinhole of \sim 60-\text{nm}-diameter. These were absent in the devices with the highest critical current. The results for the wires with a sharp corner were independent of the presence of a pinhole. We emphasize that wire-to-wire variations are expected

\[ R = \frac{\rho}{W} \]

To quantify the expected effect, we define the reduction factor \( R \) to be a number between zero and one, where the critical current of the geometry is given by \( I_c = R \cdot I_{c, \text{straight}} \), with \( I_{c, \text{straight}} \), the critical current of an infinitely long wire of width \( W \). \( R = 1 \) for the straight wire and for the optimally rounded corner, indicating an unsuppressed critical current. For the sharp corner and the wire with a stub, \( R \propto (\xi/W)^{1/3} \), with \( \xi \) the coherence length and \( W \) the width of the wire. The suppression is thus larger for shorter coherence length and larger wire width. In order to satisfy the condition \( \xi \ll W \ll A \), we fabricated the wires of width \( W = 1 \mu m \) in a 80 nm thick NbTiN film with a resistivity of 170 \mu O\text{cm}, implying a mean free path \( l \approx 0.6 \text{nm} \). The coherence length \( \xi \approx \frac{\hbar \nu}{2k_B T} \approx 7 \text{nm} \), with \( \xi_0 \) the BCS coherence length, and the Pearl length \( \Lambda \approx 20 \mu m \).

The NbTiN film was grown on a high-resistivity ($\rho > 1 \text{k}\Omega \text{cm}$), hydrogen-passivated silicon substrate using DC magnetron sputtering from a 70% Nb, 30% Ti target, at a pressure of 8 mTorr, a DC power of 300 W, a nitrogen gas flow of 4 sccm, and an argon gas flow of 100 sccm. Onto this film, a 150 nm-thick layer of hydrogen silsesquioxane resist was spin-coated. This layer was patterned using electron-beam lithography (100 keV, \sim 2 \text{mC/cm}^2). The resist was developed in a tetra-methyl ammonium hydroxide solution, and a post-development exposure was performed to harden the resulting etch mask. Finally, the pattern was transferred into the NbTiN film by reactive-ion etching in a 50 W SF$_6$/O$_2$ plasma, using interferometric end point monitoring. Both a large-area test structure and the wires showed a critical temperature of 9.5 K.

\[
\frac{\text{number of counts}}{\text{number of devices}} \sim \frac{I_c}{\mu A} \times 10^2
\]

\[ a: \text{Straight wire} \]

\[ b: \text{Rounded corner} \]

\[ c: \text{Sharp corner} \]

\[ d: \text{Stub} \]
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FIG. 4. Temperature dependence of (a) the critical current $I_c$ and (b) the width of the critical current distribution $\Delta I_c$ for straight wires (black squares), optimally rounded corners (blue circles), sharp corners (red triangles), and a wire with a stub (green diamonds). The dashed curve in (a) is a fit following Kupriyanov and Lukichev.7

To provide further evidence for the impact of sharp corners on the critical current, in Fig. 4, we plot the temperature dependence of the critical current and of the width of the distribution of the critical current between 5.5 K and 8 K. For even higher temperatures, the current-voltage curves no longer exhibit a sharp transition from the superconducting to the normal state. At each temperature, histograms like the ones in Fig. 3 were taken with 1000 current ramps for each wire. The critical current $I_c$ was taken to be the median of the critical current distribution. The width of the critical current distribution $\Delta I_c$ was defined as the difference between the third and first quartile.

As shown in Fig. 4, the wires containing a sharp corner exhibit a significantly decreased critical current and a decreased width of their distribution of critical current, as seen before in Fig. 3. For all wires, the critical current decreases with increasing temperature, as expected. The difference between the unaffected and reduced critical currents decreases as the temperature is increased towards $T_c$. The dashed curve in Fig. 4(a) is a fit following Kupriyanov and Lukichev.7 This fit gives us a critical temperature $T_C = 11.1$ K, in contrast to $T_C$ determined from low-bias $R(T)$ measurements of 9.5 K. We systematically observe such a difference, also in other NbTiN devices. Recently, Benfatto et al. discussed the effects of a broadened Berezinskii-Kosterlitz-Thouless transition in disordered superconductors, which might explain this observation.17

Another difference between wires is the width of their critical-current distribution, as shown in Fig. 4(b). For straight wires, the critical-current variance is approximately proportional to the critical current over the temperature range studied, $\Delta I_c/I_c(T)$ is constant. However, the wires with sharp geometric features exhibit a qualitatively different temperature dependence of $\Delta I_c$. First, the critical-current distribution is consistently narrower. Furthermore, the absolute width of their critical-current distribution varies little with temperature, while the critical current decreases with increasing temperature. We interpret this difference also as being due to the sharp features, noting that they provide a natural weak spot at which the wire will initiate its transition to the normal state. In contrast, in the straight and optimally rounded devices, a fluctuation at any point in the wire could cause it to switch, and so the switching effect is not localized.

Finally, we return to the stub device (Fig. 2(d)). It is counterintuitive that a wider cross-section would lead to a lower critical current. As shown in Fig. 3, however, the stub device is at the lower end of the critical currents. Moreover, in Fig. 4(a), the temperature dependence is deviating from that of the straight wires, analogous to that of the sharp corners. Similarly, Fig. 4(b) shows that the width of the critical current distribution is narrow, again analogous to the sharp corners. These observations taken together are taken as evidence that the stub indeed creates a dominant weakest link.

In summary, we have shown a clear reduction of the critical current in devices containing a sharp geometric feature. It is shown that the reduction of the critical current can be avoided by the inclusion of an optimally rounded corner. We further note that even in cases when $W > \Lambda$, which we have not treated theoretically or experimentally, as long as the condition $\xi < W$ is still satisfied, one would
expect these phenomena to be important. The avoidance of critical current reduction may have an immediate impact on the performance of superconducting single-photon detectors and parametric amplifiers based on superconducting nanowires.

Note added in proof: During review of this paper, we became aware of recent related experimental work by Henrich et al.18

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