How serious can the stealth bias be in gravitational wave parameter estimation?

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How serious can the stealth bias be in gravitational wave parameter estimation?

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The upcoming direct detection of gravitational waves will open a window to probing the strong-field regime of general relativity. As a consequence, waveforms that include the presence of deviations from general relativity have been developed (e.g., in the parametrized post-Einsteinian approach). TIGER, a data analysis pipeline which builds Bayesian evidence to support or question the validity of general relativity, has been written and tested. In particular, it was shown that the LIGO and Virgo detectors can probe deviations from general relativity in a regime than cannot be tested by Solar System tests or pulsar timing measurements. However, evidence from several detections is required before a deviation from general relativity can be confidently claimed. An interesting consequence is that, should general relativity not be the correct theory of gravity in its strong field regime, using standard general relativity templates for the matched filter analysis of interferometer data will introduce biases in the gravitational wave measured parameters with potentially serious consequences on the astrophysical inferences, such as the coalescence rate or the mass distribution. In this work we consider three heuristic possible deviations from general relativity and show that the biases introduced in the estimated parameters of gravitational waves emitted during the inspiral phase of spinless compact binary coalescence systems assuming the validity of general relativity manifest in various ways. The mass parameters are usually the most affected, with biases that can be as large as 30 standard deviations for the symmetric mass ratio, and nearly one percent for the chirp mass, which is usually estimated with subpercent accuracy. Other parameters do not show a significant bias. We conclude that statements about the nature of the observed sources, e.g., if both objects are neutron stars, depend critically on the explicit assumption that general relativity is the right theory of gravity in the strong field regime.

I. INTRODUCTION

Gravitational waves (GW) generated during the coalescence of compact binary systems (CBC) are the only means to directly probing the space-time in its genuine dynamical regime. Despite the fact that general relativity (GR) has so far passed all experimental tests with great success [1], those tests were performed in situations where the field is weak or stationary and the full nonlinear dynamics of GR were not explored.

On the other hand, when compact objects like neutron stars or black holes coalesce, they approach orbital velocities as high as 50% the speed of light, when very close to merging with the companion.

The LIGO [2,3] and Virgo [4–7] ground-based gravitational wave observatories are currently undergoing major upgrades, and are scheduled to go back online in 2015 and 2016, respectively [8], collecting data with a sensitivity that should allow for a few up to a few tens of CBC detections per year. The exact number will depend on the actual sensitivity reached by the instrument, as well as on the formation rate of compact binary systems, which is still rather uncertain [9]. The worldwide network of GW detectors will continue expand during the decade, with LIGO India [10] and Kagra [11] joining operations by 2020. Additional instruments will dramatically improve the sky localization accuracy of GW sources, as well as increase the number of detectable sources [12].

The prospect of frequent detections calls for the use of a Bayesian framework to tackle model selection problems, as it allows the information from each signal to be used to either infer some underlying general property of the observations (see, for example, [13,14] for applications in the context of cosmology), or accumulate evidence for a specific model to explain the observations (see [15] in the context of measuring the neutron star equation of state and [16] in the context of tests of GR).

Regarding the strong field deviations from GR, the following questions seem interesting:
(i) Will LIGO and Virgo be able to confidently recognize a deviation from GR in a detected signal?
(ii) Should a deviation from GR be visible, will it be possible to associate the GW signal with a given alternative theory of gravity?
(iii) Should a deviation be present but not taken into account in the analysis, how would this affect the estimation of physical (e.g. source masses) and extrinsic (e.g. distance) parameters of the source?

The answers will obviously depend on the actual nature and magnitude of the deviation from GR, which may be one of the existing proposed alternative theories (see [21] and references therein for a list of alternative theories of gravity) or something unanticipated.

Some literature exists which answers the point (i) above: the authors and collaborators have shown [16,17] how advanced LIGO and Virgo will be sensitive to quite generic (heuristic) deviations from GR. They have built a pipeline (TIGER) which has been shown to detect a variety of arbitrary deviations from GR, thus not requiring the data analyst to know the deviation’s form. Its efficiency was tested by simulating several kinds of deviations from GR, of comparable magnitude, and it has been found that deviations from GR will eventually be evident by combining evidence (in a Bayesian framework) from several signals.

The exact number of detections required to confidently claim a deviation from GR, depends on what deviation was added, but it usually is $O(10)$. Even though this proves that non-GR effects beyond solar system and pulsar tests can be measured, it implies that the biases of the point (iii) above will be present not only for unmeasurable deviations (stealth bias)$^1$, but also for deviations whose measurability requires building up evidence with several signals. That implies that, should a deviation from GR be present, it may not be discovered immediately, and GR waveforms might be used for the first few detections, introducing a bias in the parameter estimation process.

The idea of “fundamental bias,” i.e., bias in estimated gravitational wave parameters induced by the assumption that GR is correct, was first introduced in [18]. Subsequently, [21] coined the term “stealth bias” to describe the class of fundamental biases that cannot be corrected a posteriori, since the data do not provide enough evidence to favor an alternative theory of gravity. With the use of analytic approximations, [19] follows up by exploring the conditions, expressed in terms of signal-to-noise (SNR) ratio and magnitude of the deviation from GR, in which single events will be affected by stealth bias. They conclude that significant systematic bias might occur, even for deviations that are not yet excluded by observational constraints.

However, [19] takes an approach which is valid for loud signals. Because we expect the sources to be distributed uniformly in comoving volume, the majority of the gravitational wave events will be weak, with SNR close to the threshold necessary for a confident detection. For this reason, a full numerical study as close to the real data analysis process as possible is necessary to get more general answers which are valid for signals in a broad range of SNR and parameters.

In this paper, we investigate the transition regime from stealth bias to fundamental bias, considering heuristic deviations from GR that are too small to be confidently detected from any single source observation, but that can be detected after multiple detections, and we assess their effect on parameter estimation for signals from CBC systems. In particular, we focus on the inferences that can be drawn about the class of observed systems from the measurement of the masses. We find that before enough evidence is accumulated to detect a deviation from GR, the mass measurements can be heavily biased when measured with GR templates. We thus recommend that any astrophysical conclusion drawn by gravitational waves observations should be explicitly conditional on the validity of GR.

The rest of this paper is structured as follows. In Sec. II we present the experimental setup and the example deviations from GR that were considered; in Sec. III we present results for each of the deviations; finally, in Sec. IV we draw conclusions and discuss our findings.

II. METHOD

The bias induced by an unaccounted for deviation from GR in the detected gravitational wave will strongly depend on the exact shape and magnitude of the deviation. Thus, to perform our analysis, we had to choose how to modify the GW signals. While the most natural choice would have been to select some proposed alternative theories of gravity, we have decided not to do so. The reason is twofold: (i) at the moment of writing (with the exception of the investigation of a massive gravity theory in [20,21]) no full Bayesian analysis has been performed to check to what extent those theories can be confirmed or ruled out with GW observations; (ii) the class of alternative theories for which usable waveforms are available is very limited, thus limiting the scope of our investigation.

Particularly in view of (ii), we have picked some of the heuristic GR deviations investigated in [16,17]. We chose deviations that are detectable, but only when evidence from $O(10)$ detections is accumulated. Until then, the analysis with standard GR templates may not be unambiguous and, when a detection is made, no final statements may be made.
about, e.g., the nature of the source [e.g. a binary black hole (BBH) vs a black hole–neutron star (NSBH) or a binary neutron star (BNS)].

Specifically, in addition to standard GR waveforms, we have considered three possible deviations from GR:

(i) 10\% deviation in the 1.5 post-Newtonian (PN) phase coefficient ([16], IV A.1);
(ii) an extra term in the phase of the GW, corresponding to a “1.25” PN order ([16], IV C);
(iii) an extra term in the phase, whose frequency content depends on the total mass of the binary system ([17], 3.1).

The first step was to generate a catalog of 150 events, with component masses uniformly distributed in the range [1.2–2.8]\(M_\odot\). The position and orientation parameters were uniformly distributed on the unit sphere, while the distances were distributed uniformly in comoving volume in the distance range [50–400] Mpc, keeping only events with network SNRs in a realistic range [10–25].

In addition to the standard GR catalog, three catalogs of non-GR signals were generated by assuming the same events as in the GR catalog but adding the deviations described in the aforementioned list. Henceforth we will refer to those modified catalogs as \(d_{\chi 3}\) (1.5PN deviation), NonPN (“1.25PN” deviation) and powerM (deviation with a mass dependent power of the frequency). All the signals in the four catalogs (three non-GR plus one GR), were thus identical except for the eventual non-GR contribution to the phase.

Each signal in the four catalogs was analyzed using LALINFERENCE\_NEST, [22,25,26], a Bayesian parameter estimation code based on the Nested sampling [27] algorithm. The analysis for the three non-GR catalogs were performed using GR templates, thus simulating the situation in which a non-GR deviation is present in the waveform, but it is not accounted for in the analysis. We also analyzed the GR catalog (using GR templates) to have an idea of the typical uncertainties and (eventual) biases due to poor sampling, noise, etc., in the “optimal” case when the template perfectly matches the injected signal.

Each of the simulated waveforms was added to zero mean stationary Gaussian noise with a power spectral density corresponding to the design sensitivity of advanced LIGO and Virgo [23], as coded in the LALSIMULATION library [28]. The signals were generated using the so-called TaylorF2 approximant [29], as produced by the LALSIMULATION package which is part of the LIGO algorithm library [28], considering phase contributions up to the 3.5 PN order (O PN in amplitude). No spins were considered in the waveform due to computing limitations. Generic spins would force us to use time domain waveforms (e.g. SpinTaylorT4, [29]) which are much slower to calculate, making it impractical when analyzing \(O(100)\) signals, given the limited computational resources.

The TaylorF2 approximant models the inspiral regime of a CBC, and is written in the frequency domain as

\[
h(f) = \frac{1}{D} \frac{A(\theta, \phi, t, \psi, M, \eta)}{\sqrt{F(M, \eta; f)}} f^{2/3} \exp[i(\psi - \psi_{\text{GR}})] , \tag{2.1}
\]

where \(D\) is the luminosity distance to the source, \((\alpha, \delta)\) are right ascension and declination, \((t, \psi)\) give the orientation of the orbital plane with respect to the line of sight, \(M\) is the chirp mass, and \(\eta\) is the symmetric mass ratio. They are defined in terms of the component masses \((m_1, m_2)\), as \(\eta = m_1 m_2 / (m_1 + m_2)^2\) and \(M = (m_1 + m_2)^{3/5}\). \(t_c\) and \(\phi_c\) are the time and phase at coalescence, respectively. \(F(M, \eta; f)\) is an expansion in powers of the frequency \(f\) with coefficients that depend on mass (and eventual spins) and

\[
\psi^{\text{GR}}(t_c, \phi_c, M, \eta; f) = 2\pi f t_c - \phi_c - \pi/4 + \sum_{i=0}^{7} [y_i + (\chi_i^{(i)} \ln f)] f^{(i-5)/3} . \tag{2.2}
\]

The explicit forms of the coefficients \(y_i\) and \(\chi_i^{(i)}\) in \((M, \eta)\) are given, for example, in [30].

Each of the signals in the non-GR catalogs had an extra term added to the phase. These were:

1. \(d_{\chi 3}\): For the \(d_{\chi 3}\) deviation, the 1.5 PN phase terms were shifted by \(10\%\), \(\psi_3 \rightarrow \psi_3(1 + 0.1)\). That is: \(\psi = \psi^{\text{GR}} + 0.1 \psi_3(1 + 0.1)\). That is: \(\psi = \psi^{\text{GR}} + \frac{3}{128}(\pi M f)^{-2/3}\)

2. NonPN: In this case the parameter of the \((\pi M f)\) term is not normally present in the PN series (that would be \(\chi_{-5}/3\) with \(i\) an integer): \(\psi = \psi^{\text{GR}} - 2.2 \frac{3}{128}(\pi M f)^{-2/3}\). The prefactor was chosen to make the magnitude of this deviation comparable to the previous one at a reference frequency of 150 Hz for a system of 1.5–1.5\(M_\odot\).

3. powerM: Finally, for the powerM catalog, the power of \((\pi M f)\) was a function of the total mass of the system \(M\): \(\psi = \psi^{\text{GR}} + \frac{3}{128}(\pi M f)^{-2 + i M \eta}\). Here again the prefactor was such that the magnitude of this deviation is comparable to the other two at the same reference frequency and mass.

The reader is referred to [16,17] for more details about these deformation, their magnitude and their measurability with Advanced LIGO and Virgo.

III. RESULTS

A. GR injection with GR recovery

In this section we describe the performance of the parameter estimation (PE) process in the case where both
component masses are estimated with Fisher matrix, \([22]\) with the MCMC code, while the estimated, with subpercent relative errors (e.g.\([31]\)) is not present in the literature. The boxes indicate the lower to upper quartile values of the data, with a line at the median. The whiskers show 1.5 times the interquantile range, while the symbols are the remaining data points. In every SNR bin under consideration the relative error for the symmetric mass ratio is smaller than 0.1%, and usually \(\lesssim 0.03\%\) for medium-high SNR signals.

![FIG. 1 (color online). Chirp mass percentage relative error, \(\Gamma_M\), for the GR catalog set of events as a function of the optimal SNR. The boxes indicate the lower to upper quartile values of the data, with a line at the median. The whiskers show 1.5 times the interquantile range, while the symbols are the remaining data points. In every SNR bin under consideration the relative error for the symmetric mass ratio is smaller than 0.1%, and usually \(\lesssim 0.03\%\) for medium-high SNR signals.](image1)

As for the symmetric mass ratio \(\eta = m_1 m_2 / (m_1 + m_2)^2\), we find that the error can be as large as \(\sim 5\%\), but is generally \(\lesssim 2\%\) for medium-low SNR events, and \(\lesssim 1\%\) for louder events, as shown in Fig. 2.

In particular, we find that for 50% (90%) of the signals the relative error for the symmetric mass ratio is smaller than 1% (2%).

![FIG. 2 (color online). Symmetric mass ratio percentage relative error, \(\Gamma_\eta\), for the GR catalog set of events as a function of the optimal SNR. The bias can be as large as \(\sim 5\%\), but, in general, are \(\sim 2\%\) events with medium SNR (\(\sim 15\)), and \(\lesssim 1\%\) for louder event. cannot be an uncontroversial choice for this upper bound. We thus choose the reasonable value of \(2.0 M_\odot\) \([36]\). Henceforth, we will label an object lighter (heavier) than \(2.0 M_\odot\) as “neutron star” (“black hole”).](image2)
The following subsections will be devoted to analyses of the non-GR catalogs. As a general statement, because all the variations from GR we considered affect the phase of the waveform, we would expect that intrinsic parameters, i.e., the mass parameters, are the most affected by the unaccounted deviation. We will see that this is generally the case.

### B. $d\chi_3$ injection with GR recovery

In this section we report the analysis of the $d\chi_3$ catalog, i.e., the signals in which a 10% deviation in the 1.5PN phase terms is present. Here and in what follows we will use two figures of merit for the stealth bias: the relative offset with respect to the injected value:

$$\Delta_\alpha \equiv \frac{\bar{\alpha} - \alpha_{\text{true}}}{\alpha_{\text{true}}}$$

and the effect size, $\Sigma$, defined in Eq. (3.1)

We found that the chirp mass estimation, Fig. 3, is only mildly affected, with relative offsets that, even if larger (up to \(\sim 10\) times) than the typical uncertainties for this parameter in the GR case, are still well below the percent level. As a consequence, the selection of BNS events for a test of GR based on the measured chirp mass \([37]\) will not be affected by stealth bias.

On the other hand, the mass ratio is heavily affected by the presence of the $d\chi_3$ deviation. This finding is not totally unexpected, cf. Fig. 3 in \([16]\). The relative offset is $\sim 15\%$ for all the signals, while the measurement becomes more precise for loud signals. $\Sigma_\eta$ thus gets larger and larger, with the loudest events being measured $\sim 20$ standard deviations away from the injected values, Fig. 4.

Since the bias is always negative, the parameter estimation algorithm systematically underestimates the value of $\eta$.
the mass ratio. In other words, each system is seen as having component masses that are more different than reality. This is also shown in Table III in which the overwhelming majority of the signals are identified as NSBH systems. Note the difference compared to the GR catalog, Table I. In the GR case systems were either not assigned to any mass bin or correctly identified. In the case in which a $d\chi_3$ departure from GR is present, systems are misidentified 95% of the times for the BNS case and 98% of the times for BBH. The NSBH bin is now 100% (it was 44% for GR), since all the signals for which a decision could not be made in the GR catalog are being pushed toward very low mass ratios. Not a single BNS or BBH gets assigned to the correct mass bin.

The seriousness of the bias is evident from Fig. 5 in which we compare the distribution of the injected mass ratios (continuous red line) the posterior medians for the GR catalog (blue dashed line) and the $d\chi_3$ catalog (green line with vertical hatch). As expected, in the GR catalog the median estimated values match closely the injected ones. On the contrary, in the $d\chi_3$ catalog the distribution of the posterior medians is shifted toward smaller values of $\eta$ and has barely any overlap with the distribution of the injected values. The distribution of the recovered symmetric mass ratios for $d\chi_3$

<table>
<thead>
<tr>
<th>Rec. as</th>
<th>BNS</th>
<th>NSBH</th>
<th>BBH</th>
<th>Unassigned at 2(\sigma)</th>
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</thead>
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<tr>
<td>Inj. as</td>
<td>BNS</td>
<td>0</td>
<td>95%</td>
<td>0</td>
</tr>
<tr>
<td>NSBH</td>
<td>0</td>
<td>100%</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>BBH</td>
<td>0</td>
<td>98%</td>
<td>0</td>
<td>2%</td>
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</table>

peaks at $\eta \sim 0.21$, which means that the most massive star is seen as twice as massive as the lighter object.

We further verified whether the bias on the symmetric mass ratio depends on the injected values of the masses of the system, and we found that it does not. Indeed, the non-GR phase terms at a given frequency do not vary significantly over the mass parameters range we are probing here. On the other hand, the powerM deviation shows a much stronger dependence on the masses, with the magnitude of the shift inversely proportional to the masses. We will indeed see in Sec. III D that the bias is larger for BNS.

Finally, we remark that, as expected with phase-only deviations, none of the extrinsic parameters shows significant biases with respect to the GR catalog.

C. NonPN injection with GR recovery

In this subsection we investigate the NonPN catalog, for which the deviation from GR predictions can be, with an abuse of notation, dubbed “1.25PN.” For this catalog the relative offset introduced in the chirp mass estimation is moderate, even though it is generally larger than for the $d\chi_3$ catalog, being usually around $0.25$–$0.3\%$ for all of the event.

We find that the offset in $\eta$ is comparable in both magnitude and sign to what was seen for the $d\chi_3$ runs, i.e., the posterior medians are systematically underestimated. This is shown in Fig. 6.

It is thus not surprising that our findings resemble the $d\chi_3$ catalog. Nearly the totality of events are seen as NSBH, Table IV.

D. powerM injection with GR recovery

In this subsection we describe our findings for the powerM catalog. As described in Sec. II, these signals
are characterized by the presence of an extra term in the GW phase whose power of the frequency is a function of the total mass of the system. This is a rather different, and richer, situation than $d\chi_3$ or NonPN, where all signals had non-GR shifts with the same frequency dependence, and we may thus expect the resulting bias to manifest itself differently.

We find that the bias in the chirp mass, Fig. 7, is usually smaller than in the other catalogs, even though several outliers are present for which the offset is several tenths of a percent. We also notice that unlike the other two deviations, the sign of the bias is not the same for all events, but tends to be negative for low-mass events and slightly positive for the most massive sources. Such an effect should not come as a total surprise, given that by its very nature this deviation strongly depends on the mass of the system.

As for $\eta$, Fig. 8, we observe that the sign of the bias is now positive. Component masses will thus be seen as more equal than they actually are.

This is shown in Table V: 64% of BNS injections are now being recovered as BNS. This is more than in the GR injections case, where the number was 45%. The explanation is that some of the events for which a decision could not be made for GR injections have been pushed up to higher $\eta$ to the BNS cell. The same line of thought applies to the NSBH injections: 44% of them were correctly recognized in the GR catalog while only 29% are still seen as NSBH, and 9% are mislabeled as BNS. Finally, we do not see much difference for the BBH injections, which is due to the fact that the magnitude of the powerM non-GR shift gets very small for chirp masses $\gtrsim 2M_\odot$ (see Fig. 9, top panel).

### Table IV. Fraction of signals recovered as a BNS, NSBH, or BBH at two sigma confidence level for NonPN signals.

<table>
<thead>
<tr>
<th>Rec. as</th>
<th>BNS</th>
<th>NSBH</th>
<th>BBH</th>
<th>Unassigned at 2$\sigma$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Inj. as</td>
<td>BNS</td>
<td>0</td>
<td>100%</td>
<td>0</td>
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<tr>
<td></td>
<td>NSBH</td>
<td>0</td>
<td>100%</td>
<td>0</td>
</tr>
<tr>
<td></td>
<td>BBH</td>
<td>0</td>
<td>98%</td>
<td>2%</td>
</tr>
</tbody>
</table>

### Table V. Fraction of signals recovered as a BNS, NSBH, or BBH at two sigma confidence level for powerM injections.

<table>
<thead>
<tr>
<th>Rec. as</th>
<th>BNS</th>
<th>NSBH</th>
<th>BBH</th>
<th>Unassigned at 2$\sigma$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Inj. as</td>
<td>BNS</td>
<td>64</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td></td>
<td>NSBH</td>
<td>9</td>
<td>29%</td>
<td>0</td>
</tr>
<tr>
<td></td>
<td>BBH</td>
<td>0</td>
<td>0</td>
<td>50%</td>
</tr>
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FIG. 9 (color online). Top: bias for the estimation of $M$ as function of the injected values of $M$ and $\eta$. Bottom: bias for the estimation of $\eta$ as function of the injected values of $M$ and $\eta$. The bias becomes larger for smaller injected values of $M$.

We would thus expect, just back from the envelop of calculations, low-mass events to be more heavily biased than higher mass events, which is indeed what we have found. The top panel in Fig. 9 shows the bias for the chirp mass (color bar) for the various events, labeled by their injected $M$ and $\eta$. The circles are proportional to the loudness of the event. It is clear how the bias for the chirp mass strongly depends on the injected $M$, and is more important for low chirp mass systems.

The equivalent plot for the mass ratio $\eta$, Fig. 9 bottom panel, shows dependence on both the injected $M$ and and $\eta$, with large-$\eta$ events getting a smaller bias on $\eta$. That is easily understandable. Because the effect of the powerM deviations from GR is to increase the recovered value of $\eta$, events which were already very close to the upper bound ($\eta = 0.25$) will be less biased for the simple reason that their posterior distribution cannot move any higher. For those events the effects of the non-GR shift will mostly be to narrow down the $\eta$ posterior distribution.

IV. CONCLUSIONS

In this work we have shown how parameter estimation for gravitational wave signals can be strongly affected by deviations from general relativity, should they not be taken into account in the waveform used as templates. For the purpose of illustration, we have considered three heuristic deviations from GR, whose non-GR nature would eventually be recognizable using evidence from several, $O(10)$, detections.

We created a catalog of 150 inspiral signals emitted by spinless compact binary coalescence systems, that were analyzed a total of 4 times: injecting the "correct" GR signal, or injecting one of the 3 deviations from GR.

We have seen that the effect of those deviations on the mass ratio can be very different. It can lead to a heavy systematic underestimation of $\eta$ (dP3 and NonPN catalog), where the mass ratio is biased toward 2:1, i.e., $\eta \sim 0.22$, or larger, or to an overestimation of $\eta$, powerM catalog, where the distribution of recovered $\eta$'s is pushed toward the upper boundary at 0.25 and the systems seen as equal-mass.

For the sake of argument, and without claim of astrophysical validity, we have labeled compact objects lighter (heavier) than $2M_\odot$ as neutron star (black hole). We have shown that when GR templates are used for injection and for the analysis, our current parameter estimation algorithms are able to recognize the nature of the injected systems, at the 2$\sigma$ confidence level, $\sim 50\%$ of the time. Moreover, none of the GR signals were assigned to the wrong source class.

The situation was reversed when injections were allowed to depart from GR and analyzed using GR templates. For the $dP3$ (NonPN) catalog, for example, $95\%$ ($100\%$) of the injected NSBH were mistaken for NSBH. For the powerM catalog, only $29\%$ of the injected NSBH were recognized as such, while $9\%$ of them were mistaken for BNS. Even though the numerical details of our findings would change if different mass thresholds were to be chosen, our conclusions can be summarized in two points:

(i) if the templates used are a good representation of the detected signals, $50\%$ of the time we can infer the nature of the detected signal at a $2 - \sigma$ confidence level;
(ii) if the templates do not match the signal waveforms well, the measured component masses of a system are an unreliable (and potentially disastrous) indicator of the class of the system.

Therefore, any future inference that will be drawn from an in-depth analysis of GW signals with state-of-the-art parameter estimation algorithms is critically and explicitly dependent on the underlying theory of gravity assumed.

The study herein reported focused on the bias introduced by the presence of non-GR phase terms in the signal waveform when those are not present in the template. However, it is easy to appreciate that similar effects will be introduced by other possible mismatches (e.g., unknown large post-Newtonian orders, tidal effects, spins, eccentricity, different waveform families). It is therefore imperative for the GW community to concentrate on the development of as accurate waveforms as possible or on the development...
of methods to be robust against the potential systematics that our approximate waveforms might introduce.

The uniqueness of the non-GR stealth bias, however, is that it cannot be eliminated with more precise numerical simulations or analytic models, as it represents the very uncertainty on our understanding of gravity in its strong-field regime.

Furthermore, the conclusions drawn from studies that rely on the correct identification of the component objects of a compact binary source (e.g., the measurement of the differential rate of coalescence in each class of systems or the measurement of the mass function) will have to be conditional on the assumption that GR is the correct description of the physics of the system. However, it is not farfetched to assume that if a deviation from GR is eventually detected, all inferences will be corrected a posteriori.

In conclusion, the somewhat exotic, but with very real effects, “stealth bias” is nothing more than a consequence of our assumptions about the theory of gravity describing the process of gravitational radiation. This is a common phenomenon in every inference process, since the conclusions always depend on the assumptions, but it is particularly worrying in the gravitational wave physics context, since it deals with the very foundations of our understanding of gravity.

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