Search for a multi-Higgs-boson cascade in $W^+W^-b\bar{b}$ events with the ATLAS detector in pp collisions at $s = 8$ TeV

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I. INTRODUCTION

Recently, a Higgs boson has been discovered by the ATLAS [1] and CMS [2] Collaborations with a mass of approximately 125 GeV. This observation has been supported by complementary evidence from the CDF and D0 Collaborations [3]. The study of such a boson, responsible for breaking electroweak symmetry in the Standard Model (SM), is one of the major objectives of experimental high-energy physics. A vital question is whether this state is in fact the Higgs boson of the SM, or part of an extended Higgs sector (such as that of the minimal supersymmetric Standard Model [4,5]), a composite Higgs boson [6], or a completely different particle with Higgs-like couplings (such as a radion in warped extra dimensions [7,8] or a dilaton [9]).

This article reports a search for particles in an extension to the SM that includes heavier Higgs bosons in addition to a light neutral Higgs boson, $h^0$, with mass $m_{h^0} = 125$ GeV. Rather than assuming a particular theoretical model, this analysis follows a simplified model approach by searching for a specific multi-Higgs-boson cascade topology [10]. Many beyond-the-SM Higgs models introduce a second Higgs doublet. In addition to the $h^0$, such models contain a heavy charged Higgs-boson pair $H^\pm$ and a heavier neutral state $H^0$. An additional pseudoscalar particle, $A$, may also exist within the two-Higgs-doublet model (2HDM) [11] framework, but this analysis assumes it to be too heavy to participate in the cascade decay considered here.

This article reports the first search at the LHC for new particles in the final state $W^\pm W^\mp b\bar{b}$, via the process $gg \rightarrow H^0$ followed by the cascade, $H^0 \rightarrow W^\mp H^\pm \rightarrow W^\mp W^\pm h^0 \rightarrow W^\mp W^\pm b\bar{b}$, as illustrated in Fig. 1. Other production modes, such as associated production or vector-boson fusion lead to different final states and are not considered here. The $W^\pm W^\mp b\bar{b}$ final state also appears in top-quark pair production. In this search, one of the $W$ bosons is assumed to decay to hadrons leading to jets and the other one decays to an electron plus a neutrino ($e + $ jets) or a muon plus a neutrino ($\mu + $ jets). The same final state has been used by CDF in a similar search for Higgs-boson cascades [12]. Other related searches have been performed for charged Higgs bosons in top-quark pair decays $t \rightarrow H^+ b$ [13–18]. Boosted decision trees (BDTs) are used to distinguish the Higgs-boson cascade events from the predominantly $t\bar{t}$ background.

![Diagram showing the Higgs-boson cascade $gg \rightarrow H^0 \rightarrow W^\mp H^\pm \rightarrow W^\mp W^\pm h^0 \rightarrow W^\mp W^\pm b\bar{b}$.]
II. ATLAS DETECTOR AND DATA SAMPLE

The ATLAS experiment [19] at the LHC is a multipurpose particle physics detector with approximately forward-backward symmetric cylindrical geometry [20]. It consists of an inner tracking detector surrounded by a thin superconducting solenoid, electromagnetic and hadronic calorimeters, and a muon spectrometer incorporating three large superconducting toroid magnet assemblies.

The data used in this analysis were collected during 2012 from $pp$ collisions at a center-of-mass energy of 8 TeV using triggers designed to select high transverse momentum $(p_T)$ electrons or muons. The data sample corresponds to an integrated luminosity of 20.3 fb$^{-1}$.

III. SIGNAL AND BACKGROUND SIMULATION

The production of $H^0$ bosons via gluon fusion with $m_{H^0} = 325–1025$ GeV and subsequent decays $H^0 \rightarrow W^+W^-$ with $m_{W^+W^-} = 225–925$ GeV and $H^0 \rightarrow Z^0\tilde{h}^0$ with $m_{\tilde{h}^0} = 125$ GeV, is modeled using the MADGRAPH [21] Monte Carlo (MC) event generator with an effective vertex to model the fermion loop and a narrow natural width of 50 MeV. Additional radiation, hadronization, and showering are described by PYTHIA v6.4 [22]. Thirty-six different mass pairs are tested for the Higgs-boson cascade signal within the above $m_{H^0}$ and $m_{\tilde{h}^0}$ mass ranges.

The dominant SM background to this signature is top-quark pair production. This background is modeled using simulated events from the MC@NLO v4.01 [23] event generator with the CT10 [24] parton distribution functions (PDFs). The parton shower and the underlying event simulation are performed with HERWIG v6.520 [25] and Jimmy v4.31 [26], respectively, using the AUET2 tune [27]. The $t\bar{t}$ cross section for $pp$ collisions at a center-of-mass energy of $\sqrt{s} = 8$ TeV is assumed to be $\sigma_{t\bar{t}} = 253^{+13}_{-11}$ fb for a top-quark mass of 172.5 GeV. It has been calculated at next-to-next-to-leading order (NNLO) in QCD including resummation of next-to-next-to-leading-logarithmic soft-gluon terms with Top $+2.0$ [28–33]. The PDF and $\alpha_s$ uncertainties are calculated using the PDF4LHC prescription [34] with the 68% C.L. of the MSTW2008 NNLO [35,36], CT10 NNLO [24,37] and NNPDF2.3 5f FFN [38] PDF sets, added in quadrature to obtain the normalization and factorization scale uncertainties. Additional $t\bar{t}$ samples used to estimate various systematic effects are generated with POWHEG [39–41] interfaced to HERWIG/JIMMY, POWHEG interfaced to PYTHIA, and AcerMC v3.8 [42] interfaced to PYTHIA. The $t\bar{t}$ modeling is also checked with samples generated by ALPGEN [43] interfaced with HERWIG.

Other backgrounds are expected to originate from vector-boson production with associated jets (W-boson + jets and Z-boson/$\gamma^*$ + jets), as well as single top-quark, diboson (WW, WZ, ZZ), and multijet production. All background predictions, except that for multijet production, are obtained from simulated events.

The $W/Z$-boson + jets contribution is simulated using ALPGEN interfaced to HERWIG/JIMMY, and is normalized to NNLO theoretical cross sections [44,45]. The contribution from single top-quark production is simulated using MC@NLO interfaced to HERWIG/JIMMY for the $s$-channel top-quark production and $Wt$ production, and with AcerMC interfaced to HERWIG and normalized to approximate NNLO theoretical cross sections [46–48]. Finally, diboson production is simulated with HERWIG and normalized to next-to-leading order (NLO) theoretical cross sections [49].

All generated events are passed through the detailed ATLAS detector simulation [50] based on GEANT4 [51], with the exception of the additional samples used to account for systematic effects in $t\bar{t}$ production, for which a parametrized simulation [50] of the calorimeter response is used. The events are then processed with the same reconstruction software as the data. MC events are overlaid with additional minimum bias events generated with PYTHIA to simulate the effect of pileup (additional $pp$ interactions in either the same or close by bunch crossings as the primary interaction); the number of overlaid proton-proton interactions is chosen to match the distribution of the number of additional interactions observed in the data.

Multijet production may mimic the presence of a lepton, but the contribution from these processes is found to be small. It is estimated from the data by the matrix method [52] in the $\mu +$ jets and $e +$ jets channels. The matrix method is a technique to estimate the number of events with a fake, isolated lepton in the signal selection, and uses loose and tight isolation definitions for leptons. The tight isolation definitions are those used in this analysis, and tight leptons are a subset of the loose leptons. In a selection dominated by real leptons, the efficiency ($\epsilon_{\text{real}}$) of a loose lepton to also pass the tight isolation requirements is measured. The rate ($\epsilon_{\text{fake}}$) of loose leptons passing the tight requirements is measured in a multijet-dominated selection. These rates, $\epsilon_{\text{real}}$ and $\epsilon_{\text{fake}}$, are used to estimate the multijet contribution to the analysis selection.

IV. EVENT SELECTION

This analysis relies on the measurement of jets, electrons, muons and the missing transverse momentum ($E_{\text{T}}^{\text{miss}}$) [53]. Since this analysis investigates a final state dominated by top-quark pair production, a selection similar to the top-quark cross-section measurement by the ATLAS Collaboration [54] is used.

Jets are reconstructed using the anti-$k_t$ algorithm [55] with a radius parameter $R = 0.4$, and are calibrated at the energy cluster level [56] to compensate for differing calorimeter response to hadronic and electromagnetic showers. A correction for pileup is applied to the jet energy [57]. Jets are required to have $p_T > 25$ GeV and $|\eta| < 2.5$. 

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Jets from additional \(pp\) interactions are suppressed by requiring the jet vertex fraction (JVF) to be larger than 0.5 for jets with \(p_T < 50\) GeV and \(|\eta| < 2.4\). The JVF variable is defined as the transverse momentum weighted fraction of tracks associated with the jet that are compatible with originating from the primary vertex. The primary vertex is defined as the vertex with the largest \(\sum p_T^2\) of associated tracks. Jets are \(b\) tagged (identified as the product of a \(b\) quark) using the MV1 tagger [58], which combines several tagging algorithms [59] using an artificial neural network. A 70% tagging efficiency is achieved in identifying \(b\) jets with \(p_T > 20\) GeV and \(|\eta| < 2.5\) in simulated \(\ell\ell\) events, while the light-jet rejection factor is 130. Additional corrections to the tagging efficiency and mistagging rate are derived from data and applied to all simulated samples [58,60–62].

Electrons are identified [63] as energy clusters in the electromagnetic calorimeter matched to reconstructed tracks in the inner detector. Selected electrons are required to pass stringent selection requirements that provide good discrimination between isolated electrons and jets. Isolation requirements are imposed in cones of calorimeter energy deposits \(\Delta R(e, \text{deposit}) < 0.2\) and inner-detector tracks \(\Delta R(e, \text{track}) < 0.3\) around the electrons direction where \(\Delta R = \sqrt{(\Delta \eta)^2 + (\Delta \phi)^2}\). The calorimeter isolation is corrected for leakage of the energy of the electron into the isolation cone and for energy deposits from pileup events. Both the calorimeter and the inner-detector isolation requirements are chosen to give 90% efficiency. Selected electrons are required to have transverse momentum \(p_T > 25\) GeV and pseudorapidity in the range \(|\eta| < 2.47\), excluding the calorimeter barrel/end-cap transition region 1.37 < \(|\eta|\) < 1.52.

Muons are reconstructed [64] using information from the muon spectrometer and the inner detector and are required to fulfill isolation requirements. Muons are required to have transverse momentum \(p_T > 25\) GeV and \(|\eta| < 2.5\). The isolation variable \([65,66]\) for muons is defined as \(I_\mu = \sum p_T^{\mu \text{track}} / p_T^{\mu \text{jet}}\), where the sum runs over all tracks (except the one matched to the muon) that pass quality requirements and have \(p_T^{\mu \text{track}} > 1\) GeV and \(\Delta R(\mu, \text{track}) < 10\) GeV/\(p_T^{\mu \text{jet}}\). Muons with \(I_\mu < 0.05\) are selected.

The transverse momentum of neutrinos is inferred from the magnitude of the missing transverse momentum in the event. The missing transverse momentum is constructed from the negative vector sum of the reconstructed jets, the topological calorimeter energy deposits outside of jets, and the muon momenta, all projected onto the transverse plane.

Overlapping objects are subject to a removal procedure. The jet closest to a selected electron is removed, if it is within \(\Delta R(e, \text{jet}) < 0.2\). Electrons with \(\Delta R(e, \text{jet}) < 0.4\) to any remaining jets and muons with \(\Delta R(\mu, \text{jet}) < 0.4\) between the muon and nearest jet are removed since their likely origin is hadron decays.

Events are selected using single-lepton triggers with \(p_T\) thresholds of 24 or 36 GeV for muons and 24 or 60 GeV for electrons (the lower momentum triggers also apply isolation requirements). Events are required to have exactly one reconstructed isolated electron or muon matching the corresponding trigger object and a primary vertex reconstructed from at least five tracks, each with \(p_T > 400\) MeV. At least four jets with \(p_T > 25\) GeV and \(|\eta| < 2.5\) are required, of which at least two must be identified as \(b\) jets. Additional requirements to reduce the multijet background are applied:

(i) in the \(e + \text{jets}\) channel: \(E_{\text{T}}^{\text{miss}} > 30\) GeV and \(m_T^W > 30\) GeV,

(ii) in the \(\mu + \text{jets}\) channel: \(E_{\text{T}}^{\text{miss}} > 20\) GeV and \(m_T^W + E_{\text{T}}^{\text{miss}} > 60\) GeV.

The transverse \(W\)-boson mass is defined as \(m_T^W = \sqrt{2 p_T^\ell p_T^\nu (1 - \cos(\varphi^\ell - \varphi^\nu))}\), where \(p_T^\ell\) is the transverse momentum, \(\varphi\) is the azimuthal angle, and \(\ell\) and \(\nu\) refer to the charged lepton and the neutrino, respectively. Different requirements are used for the muon and electron channels due to different levels of multijet background contamination. The signal preregion (SPR) is defined to contain events that pass these requirements. Table I illustrates the expected yields of the background and the observed number of events in this region.

### Table I. Expected background contributions with their total (systematic and statistical) uncertainties and the observed number of events with exactly one lepton and at least four jets, and in the SPR region, which additionally requires at least two \(b\)-tagged jets. In the table, contributions from processes with light-flavor (LF) \(u, d, s\) quarks and heavy-flavor (HF) \(c, b\) quarks are distinguished.

<table>
<thead>
<tr>
<th>Source</th>
<th>(e/\mu + \geq 4) jets</th>
<th>SPR yields</th>
</tr>
</thead>
<tbody>
<tr>
<td>(\ell\bar{\ell})</td>
<td>36.0^{+3.7}_{-3.8} \times 10^4</td>
<td>14.0^{+2.1}_{-2.0} \times 10^4</td>
</tr>
<tr>
<td>W-boson + jets LF</td>
<td>16.0^{+8.2}_{-8.3} \times 10^4</td>
<td>6.0^{+4.2}_{-4.1} \times 10^2</td>
</tr>
<tr>
<td>W-boson + jets HF</td>
<td>8.6^{+4.4}_{-4.4} \times 10^4</td>
<td>4.6^{+2.5}_{-2.4} \times 10^3</td>
</tr>
<tr>
<td>Z-boson + jets LF</td>
<td>26.0^{+6.2}_{-6.4} \times 10^3</td>
<td>11.0^{+8.3}_{-8.7} \times 10^3</td>
</tr>
<tr>
<td>Z-boson + jets HF</td>
<td>4.9^{+1.1}_{-1.0} \times 10^3</td>
<td>6.7^{+1.7}_{-1.6} \times 10^2</td>
</tr>
<tr>
<td>Single top-quark</td>
<td>16.0^{+2.0}_{-2.0} \times 10^3</td>
<td>46.0^{+7.0}_{-7.1} \times 10^2</td>
</tr>
<tr>
<td>WW, WZ, ZZ</td>
<td>26.0^{+5.4}_{-5.5} \times 10^2</td>
<td>6.9^{+1.9}_{-2.0} \times 10^1</td>
</tr>
<tr>
<td>Fake leptons</td>
<td>1.8^{+1.8}_{-1.8} \times 10^4</td>
<td>8.6^{+8.6}_{-8.6} \times 10^2</td>
</tr>
<tr>
<td>Total</td>
<td>68.0^{+14.0}_{-14.0} \times 10^4</td>
<td>15.1^{+2.4}_{-2.4} \times 10^4</td>
</tr>
<tr>
<td>Observed</td>
<td>664876</td>
<td>151123</td>
</tr>
</tbody>
</table>

### V. EVENT RECONSTRUCTION AND MULTIVARIATE ANALYSIS

#### A. Event reconstruction

The Higgs-boson cascade event reconstruction begins with identification of the leptonically decaying \(W\) boson. It is assumed that the missing transverse momentum is due to the resulting neutrino. The neutrino pseudorapidity is set to the value which results in an invariant mass of the lepton 

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and neutrino closest to the nominal W-boson mass \[67\]; in the case of degenerate solutions, the smallest magnitude of pseudorapidity is chosen. Next, the two \b-tagged jets are used to reconstruct the lightest Higgs-boson candidate, \(h^0\); if there are more than two \b-tagged jets, the two jets with the highest \b-tagging scores \[58\] are used. The hadronically decaying W boson is identified from the remaining jets as the pair with reconstructed dijet mass closest to the nominal W-boson mass. The charged Higgs-boson candidate \(H^\pm\) is constructed from the light \(h^0\) and the W-boson candidate which gives the larger value of \(m_{\ell\ell}\). The heavy neutral Higgs-boson candidate \(H^0\) is then formed as \(b\bar{b}WW\).

Figure 2 illustrates the reconstructed mass distributions for the \(h^0\), \(H^\pm\), and \(H^0\) in simulation for selected mass values. Note that incorrect choice of neutrino rapidity or incorrect assignment of jets to the \(W\)-boson or Higgs-boson candidates will lead to a broadening of the reconstructed mass distributions, rather than a systematic bias.

Since the dominant background is top-quark pair production, the two \(b\) quarks and two \(W\) bosons are combined in \(Wb\) pairs to give top-quark candidates. The combination which minimizes the sum of the absolute value of their differences from the nominal top-quark mass \[67\] for both pairs is chosen. The invariant masses of the top-quark candidates are useful to discriminate \(t\bar{t}\) events from the Higgs-boson signal. The masses \(m_t, m_\ell\) of the two top-quark candidates and the absolute values of their differences \(|m_t - m_\ell|\) are calculated.

**B. Multivariate analysis**

A multivariate analysis is performed to distinguish the Higgs-boson cascade from \(t\bar{t}\) events. Several reconstructed kinematic quantities, including the invariant masses of the Higgs-boson candidates as described above, are used as inputs to a BDT classifier, provided in the TMVA \[68\] package. TMVA provides a ranking for the input variables, which is derived by counting how often an input variable is used to split decision tree nodes, and by weighting each split occurrence by the square of the gain in signal-to-background separation it has achieved and by the number of events in that node. Several combinations of input variables are tested in training the BDTs. The inputs for the BDTs are optimized for the best expected cross-section limits while avoiding overtraining, and the variable rankings of TMVA are used as heuristics in choosing the BDT inputs. Seven kinematic variables are chosen to achieve the best expected result across the entire signal mass grid:

(i) \(m_{bb}, m_{b\bar{b}WW}\) and \(m_{b\bar{b}WW}\), as described above;
(ii) \(\Delta R(b, \bar{b})\), the angular distance between the pair of \b-tagged jets used to reconstruct the light Higgs-boson candidate;
(iii) leptonically \(m_\ell\), the top-quark mass reconstructed using the leptonically decaying \(W\) boson;
(iv) hadronically \(m_t\), the top-quark mass reconstructed using the hadronically decaying \(W\) boson;
(v) \(|m_t - m_\ell|\).

For cascades originating from a high-mass Higgs boson, the reconstructed top-quark masses along with \(m_{WWbb}\) are the highest-ranked input variables. For the low-mass Higgs-boson cascades, \(m_{bb}\) and \(\Delta R(b, \bar{b})\) have the highest rank. Since the kinematics of the Higgs-boson cascade vary greatly with the masses of the heavy and intermediate Higgs bosons, a different BDT is trained for each signal mass hypothesis.

Only MC events that pass the SPR requirements are used in the training of the BDTs. Each BDT is constructed as a forest with 750 decision trees, and is trained against simulated background event samples. The stochastic gradient boosting method \[68\] is used to improve classification accuracy and its robustness against statistical fluctuations. Each BDT is checked for overtraining with a statistically independent test sample.

For each of the 36 signal mass points, a final threshold is chosen for its respective BDT output which gives the best expected sensitivity, measured using the same confidence-level calculations as applied to the data and described below. A counting experiment is then performed using events that pass those BDT output thresholds. In this way, the BDT thresholds divide the SPR into 36 nonorthogonal signal regions, one for each signal mass point.
VI. BACKGROUND VALIDATION IN CONTROL REGIONS

The modeling of the SM backgrounds is validated in three background-dominated control regions. The control regions retain the requirements of one lepton and at least four jets, and each region has additional requirements. In control regions with fewer than two $b$-tagged jets, the two jets with the highest $b$-tagging scores are used to reconstruct the lightest Higgs boson, $h^0$. The following control regions are used:

(i) Control Region 1 (CR1): at least four jets, exactly one lepton and no $b$-tagged jets. This region validates primarily the $W$-boson + jets modeling. This region is background enriched relative to the hypothetical signal due to the $b$-tag veto.

(ii) Control Region 2 (CR2): at least four jets, exactly one lepton and exactly one $b$-tagged jet. This region validates primarily the modeling of the $t\bar{t}$ background.

(iii) Control Region 3 (CR3): at least four jets, exactly one lepton, at least two $b$-tagged jets, and $m_{bb} > 150$ GeV. This region focuses primarily on validation of the modeling of the $t\bar{t}$ background with kinematics similar to the hypothetical signal, but is background enriched due to the $m_{bb} > 150$ GeV requirement.

This background is fractionally larger, compared to a hypothetical signal, here than in the signal region due to the $b$-tagging cut, which preferentially selects the higher $p_T$ $b$ quarks from top-quark decay. Although a potential signal would not be absent in this control region, the different levels of signal and $t\bar{t}$ contributions allow a test of $t\bar{t}$ modeling by comparing levels of agreement between data and prediction in the signal and CR2 regions.

Figures 3 and 4 illustrate the modeling of the Higgs-boson mass reconstruction in CR1, CR2 and CR3. The data and simulation agree within total uncertainties over the entire phase space. This is important, as the BDT may utilize any part of this phase space to build a powerful discriminant.

**FIG. 3** (color online). Distributions of $m_{bb}$ with uncertainties in the control regions CR1 (top) and CR2 (bottom). The data (black points) are compared to the background model (stacked histogram). In control regions with fewer than two $b$-tagged jets, the two jets with the highest $b$-tagging scores are used. The final bin contains any overflow events. Two choices of signal hypotheses are also shown.

**FIG. 4** (color online). Distributions of $m_{bb}$ (top) and $m_{bbWW}$ (bottom) with uncertainties in the control region CR3. The data (black points) are compared to the background model (stacked histogram). The final bin contains any overflow events. Two choices of signal hypotheses are also shown.
addition, the BDT output in each of the three control regions is compared to the predicted output and found to agree within statistical and systematic uncertainties.

VII. SYSTEMATIC UNCERTAINTIES

Several sources of systematic uncertainties are relevant to this analysis.

Instrumental systematic uncertainties are related to the reconstruction of physics objects. For jets, systematic uncertainties on the jet energy scale, energy resolution, and reconstruction efficiency are included. For leptons, the systematic uncertainties from the momentum or energy scale and resolution, trigger efficiency, reconstruction, and identification efficiency are incorporated. Systematic uncertainties related to the performances of the $b$ tagging and JVF requirements are also included.

Due to the presence of multiple ($\geq 4$) jets and the dominant $t\bar{t}$ background (roughly 90% in the signal region), significant systematic uncertainties are associated with jets and the modeling of the $t\bar{t}$ background. Table II lists the impact of these uncertainties on the background estimates and signal efficiency for an example signal region given by the BDT threshold for a signal with $m_{t\bar{t}} = 425, 225$ GeV.

Several sources of uncertainty on the jet energy scale calibration are considered, such as uncertainties due to pileup and the light-quark and gluon composition. These uncertainties on the background estimates and signal efficiency are included. For both leptons, uncertainties on the trigger, identification, and reconstruction efficiencies are incorporated.

Systematic uncertainties associated with leptons are found to have a small effect, typically less than 1% relative to background estimates and signal efficiency. For muons, the uncertainty in the momentum scale and resolution is accounted for. For electrons, the uncertainties in the energy scale and resolution are included. For both leptons, uncertainties on the trigger, identification, and reconstruction efficiencies are incorporated.

The uncertainty due to the modeling of initial- and final-state quark and gluon radiation (ISR/FSR) is estimated using $t\bar{t}$ events produced with the AcerMC generator interfaced with PYTHIA, where the parameters controlling ISR/FSR are varied in a range suggested by the data in the analysis of Ref. [70]. For the signal, events generated with varied ISR/FSR parameters in PYTHIA are compared to the nominal simulation; the differences in background yields and signal efficiency estimates are taken as a systematic uncertainty.

The systematic uncertainty due to the modeling of $t\bar{t}$ production is estimated by comparing results obtained with MC@NLO, POWHEG, and ALPGEN signal samples. An uncertainty due to the theoretical $t\bar{t}$ cross section [71] is applied to the overall $t\bar{t}$ normalization. Since this is the dominant background effect on the total background uncertainty is substantial (about 5% relative to the background estimate); the total normalization uncertainty on the background is 5.5%.

Since non-$t\bar{t}$ processes account for less than 10% of the background in the signal region, systematic uncertainties associated with them are found to have a small impact on the overall background uncertainty. The systematic uncertainty related to the modeling of $W$-boson + jets is determined by varying the parametrization of the renormalization and factorization scales in ALPGEN. As default, both scales are set to $(m_W^2 + (p_T^W)^2)$ and this is varied by factors of 2 and by changing the form to $(m_W^2 + \sum_{jets} p_T^2)$. This systematic uncertainty is found to be small (< 1%). An overall uncertainty of 4% is applied to the $W$-boson + jets estimate due to uncertainties in the cross section, with an additional 24% per jet added in quadrature due to the uncertainty in Berends scaling [72]. This results in a

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**TABLE II.** Details of the systematic uncertainties relative to the total expected background and the signal efficiency in the signal region for a Higgs-boson cascade signal with $m_{H^+} = 225, 425$ GeV. The signal region for this mass point is defined as the events that pass the BDT threshold for this mass sample. The positive and negative relative shifts have been averaged for compactness.

<table>
<thead>
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<th>Uncertainty</th>
<th>Background Yields</th>
<th>$m_{H^+} = 225$ GeV</th>
<th>$m_{H^+} = 425$ GeV</th>
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<td>Jet vertex fraction</td>
<td>±1.6</td>
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<td>$b$-tagging efficiency</td>
<td>±8.8</td>
<td>±14</td>
<td>±8.8</td>
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<td>Jet energy scale</td>
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<td>Jet energy resolution</td>
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<td>±11</td>
<td>±1.1</td>
</tr>
<tr>
<td>Jet reconstruction efficiency</td>
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<td>±&lt;1.0</td>
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<td>$\mu$ momentum</td>
<td>±&lt;1.0</td>
<td>±&lt;1.0</td>
<td>±&lt;1.0</td>
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<td>±&lt;1.0</td>
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<td>Lepton identification efficiency</td>
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<td>Quark/gluon radiation</td>
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<td>Total uncertainty</td>
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</tbody>
</table>

Sources are added in quadrature and listed as one systematic uncertainty in Table II. As a further uncertainty, the jet energy is smeared to cover any disagreements in the jet energy resolution measured in data and in simulated event samples. A jet reconstruction efficiency [69] systematic uncertainty is applied by randomly discarding a fraction of low-$p_T$ jets in the simulated events. The jet $b$-tagging efficiencies are evaluated in data and MC [58]. The difference is corrected with a scale factor, the uncertainty of which is treated as a systematic uncertainty. A small discrepancy in the efficiency of the JVF requirement has been observed between data and MC simulation. The JVF requirement is varied to cover this observed discrepancy, and the resulting change in the expected background is taken as a systematic uncertainty.

Systematic uncertainties associated with leptons are found to have a small effect, typically less than 1% relative to background estimates and signal efficiency. For muons, the uncertainty in the momentum scale and resolution is accounted for. For electrons, the uncertainties in the energy scale and resolution are included. For both leptons, uncertainties on the trigger, identification, and reconstruction efficiencies are incorporated.

The uncertainty due to the modeling of initial- and final-state quark and gluon radiation (ISR/FSR) is estimated using $t\bar{t}$ events produced with the AcerMC generator interfaced with PYTHIA, where the parameters controlling ISR/FSR are varied in a range suggested by the data in the analysis of Ref. [70]. For the signal, events generated with varied ISR/FSR parameters in PYTHIA are compared to the nominal simulation; the differences in background yields and signal efficiency estimates are taken as a systematic uncertainty.

The systematic uncertainty due to the modeling of $t\bar{t}$ production is estimated by comparing results obtained with MC@NLO, POWHEG, and ALPGEN signal samples. An uncertainty due to the theoretical $t\bar{t}$ cross section [71] is applied to the overall $t\bar{t}$ normalization. Since this is the dominant background effect on the total background uncertainty is substantial (about 5% relative to the background estimate); the total normalization uncertainty on the background is 5.5%.

Since non-$t\bar{t}$ processes account for less than 10% of the background in the signal region, systematic uncertainties associated with them are found to have a small impact on the overall background uncertainty. The systematic uncertainty related to the modeling of $W$-boson + jets is determined by varying the parametrization of the renormalization and factorization scales in ALPGEN. As default, both scales are set to $(m_W^2 + (p_T^W)^2)$ and this is varied by factors of 2 and by changing the form to $(m_W^2 + \sum_{jets} p_T^2)$. This systematic uncertainty is found to be small (< 1%). An overall uncertainty of 4% is applied to the $W$-boson + jets estimate due to uncertainties in the cross section, with an additional 24% per jet added in quadrature due to the uncertainty in Berends scaling [72]. This results in a
48% uncertainty for events with four jets, contributing to the overall 5.5% uncertainty on the background normalization.

The systematic uncertainty due to single top-quark, diboson, and Z-boson + jets production is evaluated by varying their cross sections within their uncertainties as described in Ref. [52]. Since these contributions are small, the systematics associated with them are found to be negligible (< 1%).

Finally, the luminosity uncertainty, measured using techniques similar to those described in Ref. [73], is 2.8%.

VIII. RESULTS

The yields in the signal regions are given in Table III. The observed yields are found to be consistent with SM background expectations, within uncertainties. The BDT outputs for three example signal mass points are illustrated in Fig. 5.
FIG. 5 (color online). Distributions of the BDT output in the signal regions for three example signal mass points, \( m_{\phi'} \), \( m_{\phi'} = 1025, 225 \text{ GeV} \) (top), \( m_{\phi'} = 625, 325 \text{ GeV} \) (middle), \( m_{\phi'} = 1025, 625 \text{ GeV} \) (bottom). Signal histograms have been scaled to a production cross section of \( 1 \text{ pb} \). BDT thresholds are shown as dashed lines for each mass point. The background model is shown as the colored stacked histogram. The final bin contains any overflow events.

The background model is shown as the colored stacked histogram. BDT thresholds are shown as dashed lines for each mass point. The final bin contains any overflow events.

FIG. 6 (color online). The expected (top) and observed (middle) 95% C.L. upper limits on the cross section for \( gg \to H^0 \to W^\pm W^\mp h^0 \to W^\pm W^\mp b\bar{b} \) as a function of \( m_{\phi'} \) and \( m_{\phi''} \). The ratio (bottom) of the observed 95% C.L. upper limits on the cross section to the theoretical cross section for a heavy Higgs boson produced via gluon-gluon fusion at the SM rate.

The 95% confidence-level production cross-section upper limits for various signal hypotheses are obtained using the CLs frequentist method [74], with the profile likelihood ratio of the number of events that pass the BDT threshold as the test statistic [75] as implemented in Ref. [76]. Systematic uncertainties are treated as nuisance parameters and the calculation uses the asymptotic approximation [75]. Table III presents the signal efficiencies, the
Theoretical cross sections of the heavy Higgs boson, \( \sigma(H^0) \), are calculated using this benchmark, as well as QCD soft-gluon resummations up to NNLO in QCD. NLO electroweak corrections are also applied, as well as QCD soft-gluon resummations up to next-to-next-to-leading log. Using this benchmark, the cross-section upper limits observed are greater than the theoretical cross sections of the heavy Higgs boson, \( H^0 \), for all mass points tested. Therefore, the current limits are not stringent enough to exclude models with SM-like production rates even with 100% branching ratios for both \( H^0 \to H^\pm W^\mp \) and \( H^\pm \to h^0 W^\mp \) and SM values for BR (\( h^0 \to b\bar{b} \)).

The limits are most stringent in the high \( H^0 \) and \( H^\pm \) mass regions, where the ratio of the limits to the theoretical cross section is nearly unity. This search produces tighter bounds than those obtained by the CDF Collaboration [12].

Additionally, the results of this search are interpreted in the context of a heavy CP-even Higgs boson of a type-II two-Higgs-doublet model [78] produced via gluon fusion. This model has seven free parameters: the mass of the CP-even Higgs bosons (\( m_{h^0} \) and \( m_{H^\pm} \)), the mass of the charged scalar (\( m_{h^\mp} \)), the mixing angle between the CP-even Higgs bosons (\( \alpha \)), the ratio of the vacuum expectation values of the two Higgs doublets (\( \tan \beta \)), and the \( Z_2 \)-symmetry soft-breaking-term coefficient of the Higgs potential (\( \Lambda_{2HDM}^2 \)).

The parameter space of the type-II 2HDM is sampled for given values of \( m_{h^0} \) and \( m_{H^\pm} \) and assuming \( m_{h^0} = 125 \text{ GeV} \) and \( \sin(\beta - \alpha) \geq 0.99 \). The latter assumptions are made in order to maintain a SM-like Higgs boson with properties similar to those observed at the LHC. The gluon-fusion production cross section is calculated with SusHi [79] at NNLO precision in QCD corrections, and the branching ratio of the cascade \( H^0 \to W^\mp H^\pm \to W^\mp W^\pm h \to W^\mp W^\pm b\bar{b} \) with 2HDMC [80]. Only parameter space points that satisfy theory constraints are considered. The theory constraints include Higgs-potential stability, tree-level unitarity for Higgs-boson scattering [81], and the perturbative nature of the quartic Higgs-boson couplings, as these are implemented in 2HDMC. The type-II 2HDM phase space is scanned with a million random points per \( (m_{h^0}, m_{H^\pm}) \) pair. The majority of the spanned phase space violates the theoretical constraints mentioned above. The points with

<table>
<thead>
<tr>
<th>( m_{H^\pm} [\text{GeV}] )</th>
<th>( m_{H^\pm} [\text{GeV}] )</th>
<th>( \tan(\beta) )</th>
<th>( \sin(\beta - \alpha) )</th>
<th>( m_h [\text{GeV}] )</th>
<th>( \Lambda_{2HDM}^2 [\text{TeV}^2] )</th>
<th>( \sigma(H^0) [\text{pb}] )</th>
<th>( \text{BF}(H^0 \to h^0 W^+ W^-) )</th>
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<td>225</td>
<td>20</td>
<td>0.99</td>
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<td>0.404</td>
<td>41</td>
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<tr>
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<td>0.99</td>
<td>486</td>
<td>1.8 \times 10^{-2}</td>
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<td>0.288</td>
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<tr>
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<td>1</td>
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<td>5.2 \times 10^{-2}</td>
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<td>0.659</td>
<td>1.1</td>
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<tr>
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<tr>
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<td>0.999</td>
<td>920</td>
<td>3.4 \times 10^{-1}</td>
<td>0.1</td>
<td>0.003</td>
<td>243</td>
</tr>
</tbody>
</table>
the lowest cross section times branching fraction $\sigma \times BF$ (excluded)/$\sigma \times BF$ (theory) which satisfy the above constraints are shown in Table IV, where $\sigma$ is the cross section and BF is the branching fraction. None are excluded by the limits presented here.

In conclusion, the first LHC search for a topology in which a heavy Higgs boson decays via a cascade of lighter charged and neutral Higgs bosons has been performed by the ATLAS experiment using data corresponding to an integrated luminosity of 20.3 fb$^{-1}$ in $pp$ collisions at $\sqrt{s} = 8$ TeV. No significant excess of events above the expectation from the SM background was found and limits on the production cross section have been set.

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[20] ATLAS uses a right-handed coordinate system with its origin at the nominal interaction point (IP) in the center of the detector and the $z$ axis along the beam pipe. The $x$ axis points from the IP to the center of the LHC ring, and the $y$ axis points upwards. Cylindrical coordinates $(r, \phi)$ are used in the transverse plane, $\phi$ being the azimuthal angle around the beam pipe. The pseudorapidity is defined in terms of the polar angle $\eta$ as $\eta = -\ln \tan(\theta/2)$.
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