**Separated Response Function Ratios in Exclusive, Forward \[superscript ±\] Electroproduction**

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Separated Response Function Ratios in Exclusive, Forward $\pi^\pm$ Electroproduction


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The study of exclusive $\pi^\pm$ electroproduction on the nucleon, including separation of the various structure functions, is of interest for a number of reasons. The ratio $R_L = \sigma_{\pi^+/C6} / \sigma_{\pi^-/C6}$ is sensitive to isoscalar contamination to the dominant isovector pion exchange amplitude, which is the basis for the determination of the charged pion form factor from electroproduction data. A change in the value of $R_T = \sigma_{\pi^-/C6} / \sigma_{\pi^+/C6}$ from unity at small $-t$, to 1/4 at large $-t$, would suggest a transition from coupling to a (virtual) pion to coupling to individual quarks. Furthermore, the mentioned ratios may show an earlier approach to perturbative QCD than the individual cross sections. We have performed the first complete separation of the four unpolarized electromagnetic structure functions above the dominant resonances in forward, exclusive $\pi^\pm$ electroproduction on the deuteron at central $Q^2$ values of 0.6, 1.0, 1.6 GeV$^2$ at $W = 1.95$ GeV, and $Q^2 = 2.45$ GeV$^2$ at $W = 2.22$ GeV. Here, we present the $L$ and $T$ cross sections, with emphasis on $R_L$ and $R_T$.
Measurements of exclusive meson production are a useful tool in the study of hadronic structure. Through these studies, one can discern the relevant degrees of freedom at different distance scales. In contrast to inclusive (e, e′) or photoproduction measurements, the transverse momentum (size) of a scattering constituent and the resolution at which it is probed can be varied independently. Exclusive forward pion electroproduction is especially interesting, because by detecting the charge of the pion, even the flavor of the interacting constituents can be tagged. Finally, ratios of separated response functions can be formed for which nonperturbative corrections may partially cancel, yielding insight into soft-hard factorization of longitudinal to transverse pion pole) or nonforward kinematics (due to angular momentum conservation). Because previous data are unseparated [5], no firm conclusions about possible deviations of $R_L$ from unity were possible.

In the limit of small $-t$, where the photon is expected to couple to the charge of the pion, the transverse ratio $R_T \equiv \sigma_T^-/\sigma_T^+$ is expected to be near unity. With increasing $-t$, the photon starts to probe quarks rather than pions, and the charge of the produced pion acts as a tag on the flavor of the participating constituent. Applying isospin decomposition and charge symmetry invariance to $s$-channel knockout of valence quarks in the hard-scattering regime, Nachtmann [6] predicted the exclusive electroproduction $\pi^-/\pi^+$ ratio at sufficiently large $-t$ to be $(\gamma_T^- n \rightarrow \pi^- p)/ (\gamma_T^+ p \rightarrow \pi^+ n) = (e_d/e_s)^2 = (1/4)$. Previous unseparated $\pi^-/\pi^+$ data [5] trend to a ratio of 1/4 for $|t| > 0.6 \text{ GeV}^2$, but with relatively large uncertainties.

In the transition region between low $-t$ (where a description of hadronic degrees of freedom in terms of effective hadronic Lagrangians is valid) and large $-t$ (where the degrees of freedom are quarks and gluons), $t$-channel exchange of a few Regge trajectories permits an efficient description of the energy dependence and the forward angular distribution of many real- and virtual-photon-induced reactions. The VGL Regge model [7,8] has provided a good and consistent description of a wide variety of $\pi^\pm$ photo- and electroproduction data above the resonance region. However, the model has consistently failed to provide a good description of $p(e, e'\pi^\pm)n$ $\sigma_T$ data [9]. The VGL Regge model was recently extended [10,11] by the addition of a hard deep inelastic scattering process of virtual photons off nucleons. The deep inelastic scattering process dominates the transverse response at moderate and high $Q^2$, providing a better description of $\sigma_T$.

Exclusive $\pi^\pm$ electroproduction has also been calculated in the handbag framework, where only one parton participates in the hard subprocess, and the soft physics is encoded in generalized parton distributions (GPDs). Pseudoscalar meson production, such as $\sigma_T$ in exclusive $\pi^\pm$ electroproduction which is not dominated by the pion pole term, has been identified as being especially sensitive to the chiral-odd transverse GPDs [12,13]. The model of Refs. [13,14] uses a modified perturbative approach based on GPDs, incorporating the full pion electromagnetic form factor and substantial contributions from the twist-3 transversity GPD, $H_T$.

We have performed a complete $L/T/LT/TT$ separation in exclusive forward $\pi^\pm$ electroproduction from deuterium. Here, we present the $L$ and $T$ cross sections, with emphasis on $R_L$ and $R_T$ in order to better understand the dynamics of this fundamental inelastic process; the $LT$ and $TT$ interference cross sections will be presented in a future work. Because there are no practical free neutron targets, the $^2\text{H}(e, e'\pi^\pm)N_e$ reactions (where $N_e$ denotes the spectator nucleon) were used. In $\pi^-/\pi^+$ ratios, the corrections for nuclear binding and rescattering largely cancel.

The data were obtained in Hall C at the Thomas Jefferson National Accelerator Facility (JLab) as part of the two pion form factor experiments presented in detail in Ref. [9]. Except where noted, the experimental details and data analysis techniques are as presented in Ref. [9] for the $^1\text{H}(e, e'\pi^\pm)n$ data. Charged $\pi^\pm$ were detected in the high
momentum spectrometer (HMS) while the scattered electrons were detected in the short orbit spectrometer. Given the kinematic constraints imposed by the available electron beam energies and the properties of the HMS and short orbit spectrometer magnetic spectrometers, deuterium data were acquired in the first experiment for nominal ($Q^2$, $W$, $\Delta \epsilon$) settings of (0.60,1.95,0.37), (1.00,1.95,0.32), (1.60,1.95,0.36), and in the second experiment of (2.45, 2.22,0.27). The value $W = 1.95$ GeV used in the first experiment is high enough to suppress most s-channel baryon resonance backgrounds, but this suppression should be even more effective in the second experiment. For each $Q^2$ setting, the electron spectrometer angle and momentum, as well as the pion spectrometer momentum, were kept fixed. To attain full coverage in $\phi$, in most cases additional data were taken with the pion spectrometer at a slightly smaller and at a larger angle than the $\vec{q}$ vector direction for the high $\epsilon$ settings. At low $\epsilon$, only the larger angle setting was possible. The HMS magnetic polarity was reversed between $\pi^+$ and $\pi^-$ running, with the quadrupoles and dipole magnets cycled according to a standard procedure. Kinematic offsets in spectrometer angle and momentum, as well as in beam energy, were previously determined using elastic $e^-p$ coincidence data taken during the same run, and the reproducibility of the optics checked [9].

The potential contamination by electrons when the pion spectrometer is set to negative polarity, and by protons when it is set to positive polarity, introduces some differences in the $\pi^+$ data analyses which were carefully examined. For most negative HMS polarity runs, electrons were rejected at the trigger level by a gas Čerenkov detector containing CsI F$_{10}$. The beam current was significantly reduced during $\pi^-$ running to minimize the inefficiency due to electrons passing through the gas Čerenkov within $\approx$100 ns after a pion has traversed the detector, causing the pion to be misidentified as an electron. A Čerenkov blocking correction (1%–15%) was applied to the $\pi^-$ data using the measured electron rates combined with the effective time window of the gas Čerenkov analog to digital converter, the latter determined from data where the Čerenkov was not in the trigger. A cut on particle speed ($\epsilon/c > 0.95$), calculated from the time-of-flight difference between two scintillator planes in the HMS detector stack, was used to separate $\pi^+$ from protons. Additionally, in the second experiment, an aerogel Čerenkov detector was used to separate protons and $\pi^+$ for central momenta above 3 GeV/$c$. A correction for the number of pions lost due to pion nuclear interactions and true absorption in the HMS exit window and detector stack of 4.5%–6% was applied. For further details, see Ref. [9].

Because the $\pi^-$ data are typically taken at higher HMS detector rates than the $\pi^+$ data, a good understanding of rate-dependent efficiency corrections was required. An improved high rate tracking algorithm was implemented, resulting in high rate tracking inefficiencies of 2%–9% for HMS rates up to 1.4 MHz. Liquid deuterium target boiling corrections of 4.7%/100 $\mu$A were determined for the horizontal-flow target used in the first experiment. The vertical-flow target and improved beam raster used in the second experiment resulted in a negligible boiling correction for those data. The experimental yields were also corrected for dead time (1%–11%).

Kinematic quantities such as $t$ and missing mass $M_X$ were reconstructed as quasi-free pion electroproduction, $\gamma N \rightarrow \pi^+N'$, where the virtual-photon interacts with a nucleon at rest. The former is calculated using $t = (p_{\text{target}} - p_{\text{recoil}})^2$, which can differ from $(p_{\pi} - p_{\pi})^2$ due to Fermi motion and radiation. Missing mass cuts were then applied to select the exclusive final state (Fig. 1). Because of Fermi motion in the deuteron, this cut is taken wider than for a hydrogen target. Real and random coincidences were isolated with a coincidence time cut of $\pm 1$ ns. Background from aluminum target cell walls (2%–4% of the yield) and random coincidences (~1%) were subtracted from the charge-normalized yields on a bin by bin basis.

The virtual-photon cross section can be expressed in terms of contributions from transversely and longitudinally polarized photons, and interference terms

$$2\pi \frac{d^2\sigma}{dt d\phi} = \frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} + \sqrt{2\epsilon(1+\epsilon)} \frac{d\sigma_{LT}}{dt} \cos\phi$$

$$+ \epsilon \frac{d\sigma_{LT}}{dt} \cos 2\phi.$$  

(1)

Here, $\epsilon = (1 + 2(|\vec{q}|^2/Q^2)\tan^2(\theta/2))^{-1}$ is the virtual-photon polarization, where $\vec{q}$ is the three-momentum transferred to the quasi-free nucleon, $\theta$ is the electron scattering angle, and $\phi$ is the azimuthal angle between the scattering and the reaction plane.

For each charge state, the data for $d^2\sigma/dtd\phi$ were binned in $t$ and $\phi$ and the individual components in Eq. (1) determined from a simultaneous fit to the $\phi$ dependence of the measured cross sections at two values of $\epsilon$. The separated cross sections are determined at fixed values of $W$, $Q^2$, common for both high and low values of $\epsilon$. Because the acceptance covers a range in $W$ and $Q^2$, the measured

![FIG. 1 (color online). Missing mass of the undetected nucleon calculated as quasi-free pion electroproduction for a representative $\pi^+$ setting. The diamonds are experimental data, and the red line is the quasi-free Monte Carlo simulation. The vertical line indicates the $M_X$ cut upper limit.](image-url)
cross sections, and hence the separated response functions, represent an average over this range. They are determined at the average values (for both $\epsilon$ points together), $\bar{Q}^2$, $\bar{W}$, which are different for each $t$ bin. The experimental cross sections were calculated by comparing the experimental yields to a Monte Carlo simulation of the experiment. The simulation uses a quasi-free $N(e, e'\pi^\pm)N'$ model, where the struck nucleon carries Fermi momentum, but the events are reconstructed in the same manner as the experimental data, i.e., assuming the target is a nucleon at rest. The Monte Carlo simulation includes a detailed description of the spectrometers, multiple scattering, ionization energy loss, pion decay, and radiative processes.

The separated cross sections, $\sigma_L$ and $\sigma_T$, are shown in Fig. 2. Even if $\pi^+$ production on $^2\text{H}$ occurs only on the proton, the deuterium cross section cannot be directly connected to the free $^1\text{H}$ cross section because the Monte Carlo cross-section model ignores off-shell effects and averages over the nucleon momentum distribution in $^2\text{H}$. The uncertainties in the separated cross sections have both statistical and systematic sources. The statistical uncertainty in $\sigma_T + \epsilon\sigma_L$ is 5%–10% for $\pi^-$ settings, and more uniformly near 5% for $\pi^+$ settings. Systematic uncertainties that are uncorrelated between high and low $\epsilon$ points are amplified by a factor of $1/\Delta\epsilon$ in the $L/T$ separation. This uncertainty ($\sim 1.3%/\Delta\epsilon$) is dominated by uncertainties in the spectrometer acceptance, uncertainties in the efficiency corrections due to Čerenkov trigger blocking and analysis cuts, and the Monte Carlo model dependence. Scale systematic uncertainties of $\sim 3%$ (not shown in the figure) propagate directly into the separated cross sections. They are dominated by uncertainties in the radiative corrections, pion decay and pion absorption corrections, and the tracking efficiencies. The systematic uncertainty due to the simulation model and the applied $M_X$ cut (model-dependence) was estimated by extracting new sets of $L/T/LT/TT$ cross sections with alternate models and tighter $M_X$ cuts.

In the $\sigma_T$ response of Fig. 2, the pion pole is evident by the sharp rise at small $-t$. $\pi^-$ and $\pi^+$ are similar, and the data at different $Q^2$ follow a nearly universal curve versus $t$, with only a weak $Q^2$ dependence. The $T$ responses are flatter versus $t$.

Finally, $\pi^-/\pi^+$ ratios of the separated cross sections were formed to cancel nuclear binding and rescattering effects. Many experimental normalization factors cancel to a high degree in the ratio (acceptance, target thickness, pion decay, and absorption in the detectors, radiative corrections, etc.). The principal remaining uncorrelated systematic errors are in the tracking inefficiencies, target boiling corrections, and Čerenkov blocking corrections.

Figure 3 shows the first experimental determination of $R_T$. The ratio is approximately 0.8 near $-t_{\text{min}}$ at each $Q^2$ setting, as predicted in the large $N_c$ limit calculation of Ref. [15]. The data are generally lower than the predictions of the pion-pole dominated models [8,10,11]. Under the naive assumption that the isoscalar and isovector amplitudes are real, $R_L = 0.8$ gives $A_S/A_V = 0.06$. This is relevant for the extraction of the pion form factor from electroproduction data, which uses a model including some isoscalar background. This result is qualitatively in agreement with the findings of our pion form factor analyses [1,16], which found evidence of a small additional contribution to $\sigma_L$ not taken into account by the VGL Regge model in our $Q^2 = 0.6$–1.6 GeV$^2$ data at $W = 1.95$ GeV, but little evidence for any additional contributions in our $Q^2 = 1.6$–2.45 GeV$^2$ data at $W = 2.2$ GeV. The main conclusion to be drawn is that pion exchange dominates the forward longitudinal response even $\sim 10m_N^2$ away from the pion pole.

Also in Fig. 3 are the first $R_T$ results in electroproduction. At $Q^2 = 0.6$, 1.0 GeV$^2$, $R_T$ drops rapidly and given the small $t$-range covered, it is not apparent if this drop is due to $t$ or $Q^2$ dependence. However, the values at $Q^2 = 1.6$ and 2.45 GeV$^2$ overlap, suggesting that $R_T$ is primarily a function of $-t$, dropping from about 0.6 at $-t = 0.15$ to about 0.3 at $-t = 0.3$ GeV$^2$. Interestingly, photoproduction data in this $t$ range [17] give similar values. It is noteworthy that the unseparated data of Ref. [5] reach a value of 0.3 at a much higher value of $-t$. A value of $-t = 0.3$ GeV$^2$ seems quite low for quark-charge scaling arguments to apply.

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\begin{figure}[h]
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\caption{Separated exclusive $\pi^\pm$ electroproduction cross sections from deuterium. Because the data were taken at different values of $W$, all cross sections were scaled to a value of $W = 2.0$ GeV according to $1/(W^2 - M^2)$. The error bars indicate statistical and uncorrelated systematic uncertainties in both $\epsilon$ and $-t$, combined in quadrature. The shaded error bands indicate the model dependence of $\sigma_L$. The $\sigma_T$ model dependence (not shown) is smaller.}
\end{figure}
directly. This might indicate the partial cancellation of soft QCD corrections in the transverse $\pi^-/\pi^+$ ratios. Previous photoproduction measurements of $R_T$ have hinted at quark-partonic behavior, but such nonforward, $Q^2 = 0$ measurements are inherently more difficult to interpret due to sea quark and $u$-channel contributions. Indeed, the photoproduction measurements at sufficiently high $-t$ first dip down toward $1/4$ then increase at backward angles [18]. The models of Refs. [7,10,11] do not accurately predict $R_T$ at $-t_{\text{min}}$, although [11] does much better at higher $-t$. The Goloskokov-Kroll GPD-based model is in reasonable agreement, but the parameters in this model are optimized for small skewness ($\xi < 0.1$) and large $W > 4$ GeV. The application of this model to the kinematics of our data requires a substantial extrapolation and one should be cautious in this comparison. Indeed, although the model does a reasonable job at predicting the $\pi^-/\pi^+$ ratios, the agreement of the model with $\sigma_T$ is not good [14]. Further theoretical work is clearly needed to investigate alternative explanations of the observed ratios.

To summarize, our data for $R_L$ trend toward unity at low $-t$, indicating the dominance of isovector processes in forward kinematics, which is relevant for the extraction of the pion form factor from electroproduction data [1,16,19]. The evolution of $R_T$ with $-t$ shows a rapid falloff consistent with $s$-channel quark knockout. Since $R_T$ is not dominated by the pion pole term, this observable is likely to play an important role in future transverse GPD programs. Further work is planned after the completion of the JLab 12 GeV upgrade, including complete separations at $Q^2 = 5$–10 GeV$^2$ over a larger range of $-t$ [20].

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