Measurement of the production cross sections for a Z boson and one or more b jets in pp collisions at $s = 7$ TeV

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Measurement of the production cross sections for a $Z$ boson and one or more $b$ jets in $pp$ collisions at $\sqrt{s} = 7$ TeV

The CMS collaboration

E-mail: cms-publication-committee-chair@cern.ch

ABSTRACT: The production of a $Z$ boson, decaying into two leptons and produced in association with one or more $b$ jets, is studied using proton-proton collisions delivered by the LHC at a centre-of-mass energy of 7 TeV. The data were recorded in 2011 with the CMS detector and correspond to an integrated luminosity of 5 fb$^{-1}$. The $Z(\ell\ell)+b$-jets cross sections (where $\ell\ell = \mu\mu$ or ee) are measured separately for a $Z$ boson produced with exactly one $b$ jet and with at least two $b$ jets. In addition, a cross section ratio is extracted for a $Z$ boson produced with at least one $b$ jet, relative to a $Z$ boson produced with at least one jet. The measured cross sections are compared to various theoretical predictions, and the data favour the predictions in the five-flavour scheme, where $b$ quarks are assumed massless. The kinematic properties of the reconstructed particles are compared with the predictions from the MADGRAPH event generator using the PYTHIA parton shower simulation.

KEYWORDS: Jet physics, Hadron-Hadron Scattering

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1 Introduction

Z bosons and jets originating from bottom quarks (b jets) are produced copiously in proton-proton collisions at the Large Hadron Collider (LHC). The production of a Z boson with at least one b jet in the detector acceptance, Z+b-jets production, is useful for precision tests of perturbative QCD [1–3]. The production of a Z boson with a single b jet, Z+1b-jet production, provides information relating to the b-quark content of the proton. The study of the production of a Z boson in association with at least two b jets, Z+2b-jets production, is of interest since it is a background in many searches for yet unobserved processes, such as the production of heavier supersymmetry-like Higgs bosons via vector boson fusion, and in studies of the standard model Higgs boson produced in association with a Z boson and decaying to b quarks [4, 5].

The production of a Z boson with b jets originates in proton-proton collisions from gluon-gluon and quark-antiquark interactions, the former being the dominant contribution [3]. A smaller contribution, expected to be less than 5% based on measurements of the effective area for hard double-parton interactions [6, 7], originates from multiple parton interactions (MPIs). The production cross section for a Z boson with at least one b jet has been measured previously at the LHC at $\sqrt{s} = 7$ TeV by the ATLAS [8] and CMS [9] Collaborations and by the CDF [10] and D0 [11] Collaborations at the Tevatron pℓp collider, at $\sqrt{s} = 1.96$ TeV, where the dominant contribution comes from quark-antiquark interactions.
The characteristics of the production of a Z boson in association with b hadrons have been studied at the LHC by the CMS Collaboration [12].

In this paper, measurements are reported of the cross sections at $\sqrt{s} = 7$ TeV for the production of a Z boson with exactly one b jet and separately for the production of a Z boson with at least two b jets. Two event categories are defined according to the b-jet multiplicity, and the yields are corrected for the respective backgrounds and efficiencies, taking into account possible migrations of events between the two categories. The cross sections are estimated at the level of stable final-state particles and are compared with predictions from MADGRAPH [13] in the five-flavour (5F) scheme, where b quarks are assumed massless, and the four-flavour (4F) scheme, where massive b quarks are used, as well as with the next-to-leading-order (NLO) predictions from amc@nlo [14]. The inclusive Z+b-jets cross section is compared to the production of a Z boson in association with jets of any type. The resulting ratio has smaller theoretical and experimental uncertainties than the absolute cross section [15] and is used to elucidate the apparent difference between the measured Z+b-jets cross section [9] and the prediction at the parton level from the mcfm NLO generator [2].

In addition, the distributions of reconstructed kinematic observables for jets and leptons in the Z+2b-jets final state are compared to a Monte Carlo (MC) simulation using the matrix element calculations of MADGRAPH in the five-flavour scheme and using PYTHIA [16] for the simulation of the parton shower and hadronization processes. Understanding the details of the kinematics is important in the search for undiscovered particles as well as for the study of the newly discovered Higgs boson [17–19] in similar topologies.

2 CMS detector and event samples

The data used in this analysis were collected with the Compact Muon Solenoid (CMS) detector. The central feature of the CMS apparatus is a superconducting solenoid of 6 m internal diameter that provides a magnetic field of 3.8 T. Within the field volume are a silicon pixel and strip tracker, a crystal electromagnetic calorimeter (ECAL), and a brass/scintillator hadron calorimeter. Muons are detected in gas-ionisation detectors embedded in the steel flux return yoke of the magnet. A more detailed description of the CMS detector can be found elsewhere [20]. A right-handed coordinate system is used in CMS, with the origin at the nominal interaction point, the $x$ axis pointing to the centre of the LHC ring and the $y$ axis pointing up, perpendicular to the plane of the LHC ring. The polar angle $\theta$ is measured from the positive $z$ axis, which points along the anticlockwise beam direction, and the azimuthal angle $\phi$ is measured in the $x$-$y$ plane. The pseudorapidity is given by $\eta = -\ln[\tan(\theta/2)]$.

The data were collected in 2011 at a proton-proton centre-of-mass energy of 7 TeV and correspond to an integrated luminosity of $\mathcal{L} = 5.05 \pm 0.11$ fb$^{-1}$ [21]. During the course of data taking, the instantaneous luminosity increased from $10^{32}$ to $3.5 \times 10^{33}$ cm$^{-2}$s$^{-1}$, resulting in an average number of proton-proton interactions per bunch crossing (pileup) of 9.7 with an RMS of 4.7.
Events are selected using dimuon and dielectron triggers. The dimuon transverse momentum ($p_T$) trigger thresholds were increased from 7 GeV on both muons to 13 and 8 GeV on the leading and subleading muons, respectively, as the instantaneous luminosity increased during the data taking period [22]. The dielectron trigger has thresholds of 17 and 8 GeV, loose identification criteria, and very loose isolation requirements [23].

In order to compare the data to the theoretical expectations, signal events and the expected backgrounds (Z+jets, $t\bar{t}$, and ZZ) are generated by MC simulation and simulated within the CMS detector using GEANT4 [24]. Inclusive Z+jets and $t\bar{t}$ events are simulated with MadGraph 5.1.1.0, using PYTHIA 6.424 with the ZZ tune [25, 26] for the parton showers, hadronization, and MPIs. The CTEQ6L1 parton distribution functions (PDFs) [27] are used. The ZZ sample is simulated using PYTHIA. The Z+jets sample is also used to extract the signal efficiencies and for the comparison of kinematic distributions.

The simulated samples used for comparison with data are normalized to the cross sections expected from theory in the full acceptance. The cross section for the Z+jets sample, 3048 pb, is normalized to match the next-to-NLO prediction for inclusive Z production obtained with FEWZ [28] and the CTEQ6m PDFs [27]. NLO predictions obtained from MCFM are used for the normalization of the $t\bar{t}$ sample, 157.5 pb, and the ZZ sample, 6.2 pb [29]. The simulated Z+jets sample is split into three subsamples, according to the underlying production of b jets, c jets, or jets originating only from gluons or ud,s quarks (hereafter called light-parton jets), with no requirement on the $p_T$ or $\eta$ of the jets. These subsamples are labelled Z+b, Z+c, and Z+l, respectively.

### 3 Event reconstruction and selection

The reconstruction and selection of events with a Z boson that decays into a pair of muons or electrons, and one or more b jets are based on the criteria used in the measurement of the inclusive Z+b-jets cross section at CMS [9]. For the identification of muons, jets, and missing transverse energy, the CMS particle-flow event reconstruction is used. This algorithm combines the information from all subdetectors to identify and reconstruct the individual particles produced in the collision [30, 31].

The leptons in the analysis are required to originate from the primary vertex, which is chosen as the vertex with the largest quadratic sum of the $p_T$ of its constituent tracks. Muons are reconstructed by combining the information from both the silicon tracker and the muon spectrometer in a global fit. Tight requirements, including particle-flow identification, are applied to the muon candidates to ensure high purity [22]. Electrons are identified by combining tracker tracks and ECAL clusters, including the ECAL deposits from bremsstrahlung [23]. An isolation variable, which is defined as the sum of the magnitudes of the transverse momenta of the particles reconstructed in a cone around the lepton candidate, $\Delta R = \sqrt{(\Delta \eta)^2 + (\Delta \phi)^2} < 0.4$ (0.3), relative to the transverse momentum of the lepton, is used to reject muons (electrons) that are embedded in jets. Charged particles not associated with the primary vertex are not considered in forming the isolation variable. To reduce the effect from pileup, the contribution of neutral particles is corrected by subtracting the energy deposited in the isolation cone by charged particles not associated with
the primary vertex, multiplied by a factor of 0.5. This factor corresponds approximately
to the ratio of neutral to charged hadron production in the hadronization process of pileup
interactions [22, 23]. After this correction, the isolation variable is required to be less than
20% for muons and 15% for electrons.

Both leptons are required to have $p_T^{\ell} > 20$ GeV and pseudorapidity $|\eta^{\ell}| < 2.4$. Opposite
charges for the leptons are required when forming pairs. In the case of multiple lepton
combinations, the lepton pair with the invariant mass closest to the nominal Z-boson mass
is selected as the Z candidate. The efficiency of the dilepton selection is estimated using
the tag-and-probe method [32] in events with at least two leptons and a jet passing
the requirements detailed below. The offline selection efficiencies are estimated from data
and simulations, and data/simulation ‘scale factors’ are estimated to correct for the differ-
ences; trigger efficiencies are estimated from data alone. All simulated events are corrected
differences between data and simulation by applying the trigger efficiencies and the
data/simulation scale factors as a function of $p_T$ and $\eta$ for each lepton.

Jets are reconstructed by clustering individual particle-flow objects using the anti-
k_T jet clustering algorithm [33] with a distance parameter of 0.5, as implemented in the
FASTJET program [34, 35]. Jets are calibrated using photon+jet, Z+jet, and dijet events to
ensure a uniform energy response in $p_T$ and $\eta$ [36]. The contribution to the jet transverse
energy from pileup is estimated on an event-by-event basis using the jet-area method [37]
and is subtracted. The reconstructed jets are required to have $p_T^{j} > 25$ GeV and to be
separated from each of the selected leptons by at least $\Delta R(\ell, j) = 0.5$. Furthermore, jets are
required to have $|\eta^{j}| < 2.1$ to ensure optimal b-tagging performance. Loose identification
criteria [36] are applied in order to reject jets coming from beam background, calorimeter
noise, and isolated photons. Jets originating from pileup in the Z+jets sample, and thereby
contributing falsely to the cross section ratio, are suppressed by requiring the momentum of
particle tracks originating from the selected primary vertex compared to the jet momentum
be at least 10%. The remaining background caused by jets from pileup is $\sim 2\%$ in the Z+jets
data sample.

Jets originating from b quarks are tagged by taking advantage of the long b-hadron
lifetime. The ‘Simple Secondary Vertex’ (SSV) b-tagging algorithm employs a three-
dimensional flight distance significance between the primary vertex and a secondary vertex
in a jet. To maximise the selection efficiency of the Z+b-jets process for multiple b jets, the
high-efficiency version of the SSV b-tagging algorithm is used, which considers secondary
vertices built from two or more tracks. The discriminant value to define b-tagged jets
is chosen such that the probability of tagging a light-parton jet (mistagging fraction) is
less than 1%, with a b-tag efficiency of $\sim 55\%$. The b-tagging efficiencies and mistagging
fractions are measured in the data and simulation as functions of the $p_T$ and $\eta$ of the jet
using inclusive jet samples, where the tagging efficiency in the data is $\sim 5\%$ smaller than
the efficiency in the simulations [38]. Simulated events are corrected for this difference,
taking into account the data/simulation scale factor for each b-tagged jet, depending on
the generator-level flavour.

After the application of the b-tagging requirement, the sample is divided into nonover-
lapping categories according to the number of b-tagged jets in the sample: the Z+1b-jet
sample contains events with exactly one b-tagged jet, while the Z+2b-jets sample contains
the events with at least two b-tagged jets. In order to suppress background from \( \bar{t}t \) production in both samples, the reconstructed dilepton invariant mass \( M_{\ell\ell} \) is required to have a value between 76 and 106 GeV. In figure 1 the dielectron invariant mass distribution shows the effectiveness of this requirement.

To further suppress the \( \bar{t}t \) background in the Z+2b-jets sample, the missing transverse energy (\( E_T^{\text{miss}} \)) is evaluated and events with a value significantly different from zero are vetoed. The \( E_T^{\text{miss}} \) is calculated by forming the negative vector sum of the transverse momenta of all particles in the events. The \( E_T^{\text{miss}} \) significance is more robust than the \( E_T^{\text{miss}} \) itself against pileup, and offers an event-by-event assessment of the likelihood that the observed \( E_T^{\text{miss}} \) is consistent with zero given the reconstructed content of the event and known measurement resolutions of the CMS detector [39]. In figure 2 the \( E_T^{\text{miss}} \) significance distribution is shown after requiring a Z candidate and two b-tagged jets. The distributions for the Z+b and \( \bar{t}t \) components motivate the selection of events with a reconstructed \( E_T^{\text{miss}} \) significance less than 10, which results in a high signal efficiency and small systematic uncertainty.

All simulated events are corrected for the differences between data and simulation in the pileup distributions, b-tagging efficiencies, and lepton reconstruction efficiencies. The data yields as well as the predicted yields are summarised in table 1.

4 Backgrounds

Events not originating from the Z+b-jets production process, but nevertheless contributing to the final reconstructed event yield after the full selection, are expected to originate from
Table 1. Data yields in the selected samples and a comparison to the expectation from various sources based on MC simulations. The expected yields are estimated using the theoretical predictions for the cross sections. Uncertainties are statistical only.

<table>
<thead>
<tr>
<th>Selection</th>
<th>Data</th>
<th>Total simulation</th>
<th>Z+b</th>
<th>Z+c</th>
<th>Z+l</th>
<th>tτ</th>
<th>ZZ</th>
</tr>
</thead>
<tbody>
<tr>
<td>Z(μμ)+1b-jet</td>
<td>13090</td>
<td>12904± 77</td>
<td>6810± 58</td>
<td>3647± 41</td>
<td>1829± 29</td>
<td>549± 3</td>
<td>69± 1</td>
</tr>
<tr>
<td>Z(μμ)+2b-jets</td>
<td>522</td>
<td>480± 13</td>
<td>350± 12</td>
<td>34± 4</td>
<td>5± 1</td>
<td>80± 1</td>
<td>11± 1</td>
</tr>
<tr>
<td>Z(ee)+1b-jet</td>
<td>9672</td>
<td>9924± 67</td>
<td>5218± 50</td>
<td>2844± 36</td>
<td>1364± 25</td>
<td>445± 3</td>
<td>53± 1</td>
</tr>
<tr>
<td>Z(ee)+2b-jets</td>
<td>362</td>
<td>357± 11</td>
<td>258± 10</td>
<td>27± 3</td>
<td>2± 1</td>
<td>62± 1</td>
<td>8± 1</td>
</tr>
</tbody>
</table>

tτ, Z+jets, and ZZ production. For the Z+1b-jet sample, the main background originates from Z bosons produced in association with non-b jets; for the Z+2b-jets sample, another sizable background originates from tτ production, with another nonnegligible contribution from ZZ production.

The background originating from tτ production is estimated by means of a binned fit to the wide dilepton invariant-mass spectrum, 61 < Mℓℓ < 121 GeV, as shown for the electron channel in figure 1. The shape of the invariant-mass distribution for Z+jets events is taken from Z-boson-enriched data samples, while the distribution (template) for tτ is based on simulation.

As a control method, two other distinct parameterizations are employed for the probability density functions of the Z+jets and tτ contributions: (i) Z+jets templates based on simulation together with tτ templates based on distributions in data samples, and (ii) an empirical parameterization. These tτ templates are acquired from an opposite-flavour (μ/e) dilepton sample in which the tτ contribution is enriched. The empirical parameterizations employ a relativistic Breit-Wigner distribution to describe the Z+jets contribution and a polynomial distribution to describe the tτ contribution; the parameters of both probability density functions are free to vary in the fit. As another control method, a multivariate matrix-element approach [40] is used to distinguish signal and background.

In all channels the results obtained with the various parameterizations and methods are consistent with each other and with the expectations from simulation. The fraction of events from tτ, fττ, estimated from the fit within the wide mass window is interpolated to the signal mass window (76 < Mℓℓ < 106 GeV). The differences between the tτ estimates derived from alternative parameterizations are used to estimate the related systematic uncertainty.

The background due to mistagged c and light-parton jets is estimated from the mass distribution of the secondary vertices (M_SV) of the b-tagged jets. For the Z+1b-jets sample, exactly one jet per event is b-tagged, and hence one secondary vertex per event is reconstructed and analyzed. For the Z+2b-jets sample the distributions of the M_SV of both the leading (in p_T) and subleading b-tagged jets are used.

As described in detail in [9], templates are obtained from simulations to model the M_SV distributions for the various jet flavours; separate templates are constructed for b jets, c jets, and light-parton jets. These templates are used in maximum-likelihood fits to extract the fractions of b, c, and light-parton jets from the data for both the Z+1b-jet and the
Figure 3. Distributions of the secondary vertex mass of the leading (in $p_T$) b-tagged jet of the dimuon Z+2b-jets sample (left) and the subleading b-tagged jet of the dielectron Z+2b-jets sample (right). The overlaid distributions are the results of the fit described in the text.

Z+2b-jets samples. In the Z+2b-jets sample the distributions of the leading and subleading jets are fitted separately. The results of fits to the one-dimensional $M_{SV}$ distributions after the Z+2b-jets selection are shown in figure 3. The fractions of correctly tagged b jets in the Z+1b-jet and Z+2b-jets samples are estimated to be $\sim 55\%$ and $80-85\%$, respectively. The estimated fraction of correctly tagged b jets is checked by comparing the fit results to (i) the results obtained with templates constructed from an independent MC sample, and (ii) the direct expectations from simulation, and are found to be in agreement. Effects due to gluon splitting in the modelling of the distributions have been studied and found to be negligible.

Subsequently, the fractions of correctly tagged b jets are transformed into the purities $P_{b}^{Z+1b}$ and $P_{b}^{Z+2b}$, i.e. the fractions of events in the two samples that contain correctly tagged b jets; events in the Z+2b-jets sample with two correctly tagged b jets are considered as Z+2b-jets signal events, whereas events with one mistagged jet in the Z+2b-jets sample are considered for the Z+1b-jet signal yield. In order to estimate these ratios from the results of the one-dimensional fits, the various combinations in which two jets are b-tagged in the Z+2b-jets sample are studied in simulations. The systematic uncertainty related to the b purity is evaluated by varying the mistagging rates and production rates within their uncertainties. As a cross-check, a fit is performed to the two-dimensional distribution of the $M_{SV}$ values for the leading and subleading b-tagged jets, and consistent results are obtained.

A small background from ZZ events is expected in the Z+2b-jets sample. This contribution ($N_{ZZ}$) is estimated from MC simulations, using the cross section and uncertainty from the CMS measurement \cite{41} for the normalization. The yield from a SM Higgs boson with mass of 125 GeV \cite{18, 19, 42} that decays into two b jets, and is produced in association with a Z boson, is expected to be approximately 20% of the ZZ contribution, i.e. 2.1 events.
Table 2. The estimates of the purities, the $t\bar{t}$ fractions, and the ZZ backgrounds for the various b-jet multiplicities and lepton flavours, including statistical and systematic uncertainties.

in the $Z(\mu\mu)+2b$-jets final state and 1.7 events in $Z(ee)+2b$-jets final state. The resulting effect on the $Z+2b$-jets cross section is expected to be $\sim0.6\%$.

The background contributions are summarized in table 2. The backgrounds due to $t\bar{t}$ and ZZ production increase when requiring two b-tagged jets, because of the relatively harder spectra of these sources of background compared to the signal. At the same time, the backgrounds due to light-parton jets decrease, since the probability of mistagging two jets is smaller. The corrected signal yield ($N_{\text{sig}}$) is obtained by subtracting the backgrounds from the number of selected events ($N_{\text{rec}}$), and is estimated as

$$N_{\text{sig}}^{Z+1b} = N_{\text{rec}}^{Z+1b} \times (P_{Z+1b}^{Z+1b} - f_{t\bar{t}}^{Z+1b}) - N_{ZZ}^{Z+1b} + f_{1b}^{Z+2b} \times N_{\text{rec}}^{Z+2b},$$

$$N_{\text{sig}}^{Z+2b} = N_{\text{rec}}^{Z+2b} \times (P_{Z+2b}^{Z+2b} - f_{t\bar{t}}^{Z+2b}) - N_{ZZ}^{Z+2b}.$$

Here, $f_{1b}^{Z+2b}$ is the fraction of events in the $Z+2b$-jets sample for which one jet is mistagged, which is $16 \pm 5\%$. The resulting contribution to the $Z+1b$-jet cross section is $\sim1\%$.

5 Efficiencies and migrations

In order to extract a cross section at the particle level, the background-subtracted yields for the $Z+1b$-jet and the $Z+2b$-jets categories in eq. (4.1) are corrected for the efficiencies in the selection of the dilepton pair and the b-tagged jets, as well as for the detector resolution effects. Both the application of b tagging and jet reconstruction may induce migrations between the category of events containing one b jet and that containing more than one, since the number of generated b jets and the number of correctly reconstructed b jets are, in general, not the same. In order to estimate the cross sections for the different b-jet multiplicities, the efficiency corrections (or ‘unfolding’) are performed as a function of the number of b jets.

Particle-level b jets are defined by matching generated jets to a b hadron within $\Delta R < 0.5$ of the jet axis. No requirement is placed on the $p_T$ of the hadron, and the generated jet is constructed from particle-level objects which include invisible particles. The generated jets are clustered and selected with the same criteria used for the jets reconstructed in
data. Particle-level leptons are defined as ‘dressed’ leptons, i.e. adding to the lepton all generator-level photons within a cone of $\Delta R < 0.1$.

The selection efficiency is factorised into two parts: the b-tagging efficiency ($\mathcal{E}_b$) and the lepton selection efficiency ($\mathcal{E}_\ell$). The correction for the detector resolution effects ($\mathcal{E}_r$) is dominated by the jet energy resolution. Finally, $\mathcal{E}_m$ corrects for the efficiency loss associated with the selection criterion on the $E_T^{\text{miss}}$ significance in the $Z+2b$-jets event selection.

To account for migrations between different b-jet multiplicities, a $2 \times 2$ matrix equation is used. Each efficiency factor is represented by a matrix (the matrices $\mathcal{E}_b$ and $\mathcal{E}_\ell$ are diagonal). The matrices are applied in an order reflecting the order of the selection requirements.

\begin{equation}
\begin{pmatrix}
\sigma_{Z+1b} \\
\sigma_{Z+2b}
\end{pmatrix} = \frac{1}{\mathcal{L}} \times \mathcal{E}_r^{-1} \times \mathcal{E}_\ell^{-1} \times \mathcal{E}_b^{-1} \times \mathcal{E}_m^{-1} \times
\begin{pmatrix}
N_{\text{sig}}^{Z+1b} \\
N_{\text{sig}}^{Z+2b}
\end{pmatrix}.
\end{equation}

This equation is used to obtain the cross sections for the production of a $Z$ boson in association with exactly one b jet ($\sigma_{Z+1b}$) or at least two b jets ($\sigma_{Z+2b}$) from the numbers of reconstructed signal events in the $Z+1b$-jet and $Z+2b$-jets categories.

The MC signal sample is used to build the matrices, with efficiencies from the simulation rescaled to match the efficiencies observed in the data. The $p_T$ distributions for the leading (in $p_T$) and subleading b jets after the $Z+2b$-jets selection are shown in figure 4. The agreement between data and simulations in figures 2 and 4 justifies the use of this sample for the unfolding procedure.

The inclusive cross section for the production of a $Z$ boson in association with at least one b jet is the sum of the two cross sections in eq. (5.1), namely, $\sigma_{Z+b} \equiv \sigma_{Z+1b} + \sigma_{Z+2b}$. The ratio of this cross section to the cross section for the production of a $Z$ boson with any kind of jet is denoted $\sigma_{Z+b/Z+j}$. The cross sections are defined using the same acceptance for the different lepton flavours: events have leptons with $p_T^{\ell} > 20$ GeV and $|\eta^{\ell}| < 2.4$, a dilepton invariant mass $76 < M_{\ell\ell} < 106$ GeV, and jets with $p_T^j > 25$ GeV and $|\eta^j| < 2.1$, and a separation between the leptons and the jets of $\Delta R(\ell,j) > 0.5$.

The terms in eq. (5.1) related to the b-tagging and $E_T^{\text{miss}}$ efficiencies are found to be very similar for the muon and the electron channels, as expected. For the lepton selection efficiencies, results are found to be almost identical between the two b-jet multiplicity bins, which is expected since the requirement of $\Delta R(\ell,j) > 0.5$ effectively renders the lepton selection insensitive to the jet multiplicity.

\section{Systematic uncertainties}

The following sources of systematic uncertainties are considered:

- Background from light-parton jets: for the estimate of the background due to mistagged b jets, the main source of uncertainty arises from the fit uncertainty in the fraction of b jets in the $Z+1b$-jet and $Z+2b$-jets samples. Another source of uncertainty originates from the ambiguity when estimating the number of events containing zero, one, or two b jets in the $Z+2b$-jets sample. The corresponding systematic uncertainty is estimated by varying the (mis)tagging efficiencies according
Figure 4. The combined muon+electron distributions of the $p_T$ of the leading-$p_T$ (left) and subleading-$p_T$ (right) b-tagged jet for the Z+2b-jets sample. The simulated samples are normalized to the theoretical predictions. The last bin in both distributions contains the overflow, and the uncertainties in the simulations are shown as a hatched band. The data/simulation ratio shows the separate contributions to this uncertainty: the band represents the statistical uncertainty in the simulated yield, and the lines indicate the uncertainties related to the jet energy scale (dashed) and the b-tag scale factors (solid).

Studies show that no significant differences are observed when comparing the $M_{SV}$ templates obtained with different MC generators, and that the template acquired from simulation correctly describes the distribution observed in data [38, 43].

- Background from $t\bar{t}$: the main source of uncertainty in the estimate of the $t\bar{t}$ background is the statistical uncertainty from the fit. An additional uncertainty originates from the modelling of the signal and background shapes. The probability density functions used in the estimate of the $t\bar{t}$ background are obtained in three distinct ways: with templates based on simulation and on data, and by modelling the contributions with an empirical parameterization. The systematic uncertainty is estimated from the differences between the three methods.

- The ZZ background: the uncertainty in the overall normalization is taken from the CMS measurement [41]. Correlated sources of uncertainties (such as the luminosity) are ignored to avoid double counting.

All background-related systematic uncertainties are listed in table 2, and are propagated to the cross section estimate following eq. (4.1). Other systematic uncertainties, estimated via eq. (5.1), are:
• The b-tagging efficiency and the mistagging fraction: the uncertainties of the b-tagging efficiencies and mistagging fractions are estimated in the data as functions of the $p_T$ and $\eta$ of the jet, combining the various methods discussed in ref. [38]. These uncertainties affect the b-tagging efficiencies as described in section 5. The $p_T$-dependent uncertainties in the jet tagging efficiency, 3–8% for $p_T > 30$ GeV and 12% for $p_T < 30$ GeV, are propagated to the b-tagging data/simulation scale factors, by varying these according to the corresponding uncertainties with the flavor of each jet. The uncertainty in the mistagging fraction, which enters the calculation of the event weight at second order, is found to have a negligible impact.

• Jet energy scale (JES) and resolution (JER): the jet energy calibration is based on MC simulations, while residual corrections are used to account for the small differences between data and simulation. The JES uncertainty is taken from ref. [36] and amounts to 3–5% depending on the $p_T$ and $\eta$ of the jets. The JER uncertainty is taken to be 10%, after degrading the simulated resolution by 10% to match that measured in the data. Both affect $E_T$. Studies of simulated samples show that these JES corrections are good for jets from bottom quarks.

• Effect from pileup: the total inelastic cross section used to infer the pileup in data from the instantaneous luminosity is varied by $\pm 5\%$, thereby affecting the pileup distribution in the simulated samples and covering the uncertainties due to pileup modelling. It is then propagated to the estimation of the unfolding matrices where it affects mainly the lepton efficiency factors through the lepton isolation requirements.

• Requirement on $E_T^{\text{miss}}$: the requirement on the $E_T^{\text{miss}}$ significance removes $\sim 2\%$ of the $Z+2b$-jets signal contribution, which is evaluated from simulation. The systematic uncertainty is estimated by varying each component entering the $E_T^{\text{miss}}$ calculation within its uncertainty. This includes contributions from JES and JER as discussed above, unclustered energy (10%), $\tau$ leptons (3%), electrons and photons (0.6–1.5%), and muons (0.2%) [39].

• MC statistics: while the MC statistics suffice for the $Z+1b$-jet sample, they lead to uncertainties of several percent in correction factors involving the $Z+2b$-jets sample.

• Luminosity: the uncertainty of the integrated luminosity recorded by CMS is 2.2% in the 2011 data set [21].

• Dilepton selection efficiencies: the systematic uncertainty of the scale factor per lepton, which is applied to simulated events to compensate for data/simulation differences, is obtained with the tag-and-probe method, and is less than 0.4% for muons and 1.0% for electrons.

• Theory: the effect of uncertainties in the renormalization and factorization scales is estimated using MCFM [2]. The impact of scale variations on the $p_T$ of the b jets is used in the unfolding procedure to estimate the effect on the cross section. Similarly,
The $p_T$ of the dilepton pair is varied according to the difference observed between data and simulation to estimate the impact on the unfolding.

Furthermore, the effect due to MPIs on the acceptance of $Z+b$-jets events is studied by artificially reducing their contribution by a factor two. This is done by applying a veto on the azimuthal angle $\Delta \phi_{Z, bb}$, which has been shown to be a discriminant observable for MPIs [44]. The effect of this requirement on the cross sections has been found to be less than 0.5%.

Together, this leads to an uncertainty of at most 3% in the cross sections.

- Vertex association: for the estimate of the cross section ratio $\sigma_{Z+b}/\sigma_{Z+j}$, an additional uncertainty arises from the contribution of jets not associated with the primary vertex. After the requirement on the momentum fraction of tracks originating from the primary vertex, the background due to pileup is estimated from simulation to be 2.2%. The efficiency of the requirement is estimated from the distribution of this observable in data before applying the requirement. The corresponding systematic uncertainty is evaluated by comparing the distributions of this observable in data and simulation; it is assumed that the difference observed for the variable used for the vertex association is entirely due to events originating from pileup. This assumption results in a systematic uncertainty of 18% in the pileup contamination, fully correlated between the electron and muon channels.

Table 3. Fractional uncertainties in the measured cross sections, grouped according to the correlation between the channels.
The systematic uncertainties are summarized in table 3. The uncertainties are presented separately for the muon and electron channels, and for the Z+1b-jet and Z+2b-jets measurements.

7 Kinematic observables

One of the observables of interest for searches in the Z+2b-jets final state is the invariant mass of the b-jet pair ($M_{bb}$). This observable is, for example, used in the study of the Higgs boson produced in association with a Z boson and decaying into two b jets, in the $Z(\ell\ell)H(bb)$ final state [4, 5]. Other kinematic observables in the Z+2b-jets final state relevant to searches for undiscovered processes are the transverse momentum of the dilepton ($p_T^{\ell\ell}$) and the dijet ($p_T^{bb}$) pair, and the angle between the dilepton pair and the dijet pair ($\Delta\phi_{Z,bb}$). The distributions of these observables are compared with the predictions from MADGRAPH, including uncertainties due to the jet energy scale and the b-tagging efficiencies, as well as the uncertainties due to limited MC statistics. More than two jets are b-tagged in less than 2% of the Z+2b-jets events, and in this case the two highest-$p_T$ jets are considered.

The distributions of $M_{bb}$ and $p_T^{bb}$, presented in figure 5 (top left and top right, respectively), show agreement with the predictions. The excess of data in the overflow bin at high values of $p_T^{bb}$ is not concentrated in any particular region. The distribution of $\Delta\phi_{Z,bb}$, shown in figure 5 (bottom left), shows agreement with the predictions as well, both in the collinear and back-to-back regions. This is especially relevant with respect to contributions from MPIs, which are expected to have less correlated kinematics than those from the Z+2b-jets process, and will therefore give a uniform distribution in $\Delta\phi_{Z,bb}$.

On the other hand, the $p_T^{\ell\ell}$ distribution shows a harder spectrum in data than predicted, as shown in figure 5 (right bottom). An overall excess of events is observed for $p_T^{\ell\ell} > 80$ GeV, in particular in the region around 100 GeV. This trend is consistent with the earlier CMS publication [9], where a similar discrepancy is observed for the $p_T^{Z}$ observable in the Z+b-jets final state. A harder spectrum for the $p_T^{Z}$ observable is predicted in four-flavour calculations with massive b quarks at NLO [14], which might explain the observed disagreement.

The effect of the disagreement on the estimate of the cross sections has been studied and is included in the systematic uncertainties, as described in section 6. Furthermore, a bin-by-bin reweighting of the predictions according to the observed discrepancy in the $p_T^{\ell\ell}$ observable has been performed, and this improves the agreement in other observables where differences are observed.

8 Cross sections

The cross sections are estimated per b-jet multiplicity bin and for each lepton flavour separately. The results are summarized in table 4.

Using the best linear unbiased estimator [45], results for the $\mu\mu$ and $ee$ channels are found to be consistent with a $\chi^2$ probability of 42% for the Z+1b and 78% for the Z+2b cases. They are therefore combined into a single measurement using the optimal set of
Figure 5. Distributions of kinematic observables for the Z+2b-jets selection of the combined electron and muon samples, and a comparison with the simulated samples that are normalized to the theoretical predictions. Top left: the dijet mass of the two b-tagged jets. Top right: the $p_T$ distribution of the dijet pair. Left bottom: the azimuthal angle $\phi$ between the Z boson and the dijet system. Right bottom: the $p_T$ distribution of the dilepton pair. The right-most bin in the last three plots contains the overflow. Uncertainties in the predictions are shown as a hatched band. The data/simulation ratio shows the separate contributions to this uncertainty: the band represents the statistical uncertainty on the simulated yield, and the lines indicate the uncertainties related to the jet energy scale (dashed) and the b-tagging scale factors (solid).
coefficients that minimise the total uncertainty in the combined result, taking into account statistical and systematic uncertainties and their correlations. The results are summarized in Table 5 and are then compared with various predictions.

The expectations from MadGraph, in both the 5F and the 4F schemes, are estimated using a global K factor to correct the inclusive Drell–Yan cross section for next-to-NLO effects [28]. The expectations from aMC@NLO, at NLO, are also estimated using both 5F calculations and 4F calculations with massive b quarks [14]. The events simulated with MadGraph and aMC@NLO are interfaced with the Pythia parton shower simulation. The settings used for the predictions from MadGraph and aMC@NLO are described in detail in [12].

The NLO prediction from mcfm is at the parton level. The mcfm calculations are estimated with the CTEQ6mE PDF, and the renormalization and factorization scales are set to the invariant mass of the dilepton pair.

Uncertainties in the theoretical predictions are estimated by varying the renormalization and factorization scales by a factor two up and down. For the MadGraph 5F prediction, the scales are varied in a correlated manner, whereas the scales are varied in an uncorrelated way for the other predictions, which leads to a larger estimate for the uncertainty. The uncertainties in the 4F predictions amount to 15–20%, as expected [46], Variations of the PDFs (using MSTW2008 [47], CTEQ6, and CT10 [48] PDF sets), jet matching scale (up to a factor of two), and mass of the b quark (between 4.4 and 5.0 GeV)
all result in smaller uncertainties. A more detailed description of the methods to estimate these uncertainties is given in [12].

The measured cross sections are consistent, within uncertainties, with the expectations in the 5F scheme from both MADGRAPH and aMC@NLO. Compared to the predictions from MADGRAPH and aMC@NLO in the 5F scheme, the predictions from MCFM are approximately 20% lower. The predictions by MADGRAPH and aMC@NLO from calculations in the 4F scheme, compared to the predictions in the 5F scheme, show a reduction of the Z+1b-jet production rate, when the other b jet in the final state is produced outside of the acceptance.

A difference of approximately two standard deviations is observed when comparing to the parton-level prediction from MCFM for the Z+b-jets cross section. Since the correction factor from parton level to hadron level is smaller than one [9], this difference is not explained by hadronization effects. The difference remains when measuring the cross section ratio, which excludes an explanation based on experimental systematic effects that are shared between the Z+jets and the Z+b-jets final states, such as luminosity, and the reconstruction of jets and leptons. These results indicate that the difference observed with MCFM is specific to the modelling of the Z+b-jets final state.

The largest discrepancy is observed when comparing the measured Z+1b-jet cross section with the predictions in the 4F scheme. In particular, the prediction from aMC@NLO in the 4F scheme shows a discrepancy of more than two standard deviations compared to the measurement.

9 Conclusions

The production of Z(ℓℓ)+b-jets, with ℓℓ = µµ or ee, has been studied for events containing leptons with \( p_T^{ℓ} > 20 \text{ GeV} \), \( |η^{ℓ}| < 2.4 \), a dilepton invariant mass \( 76 < M_{ℓℓ} < 106 \text{ GeV} \), jets with \( p_T^{j} > 25 \text{ GeV} \) and \( |η^{j}| < 2.1 \), and a separation between the leptons and the jets of \( ΔR(ℓ,j) > 0.5 \). The Z+b-jets cross sections have been measured, at the level of stable final-state particles, for a Z boson produced with exactly one or at least two b jets. In addition, a cross section ratio has been extracted for a Z boson produced with at least one b jet relative to a Z boson produced with at least one jet.

The cross section measurements are in agreement with the expectations from MADGRAPH and aMC@NLO in the five-flavour scheme. A difference of approximately two standard deviations is observed when comparing the cross sections with the predictions from MCFM at the parton level, and the comparison with the cross section ratio indicates that the difference is specific to the modelling of the Z+b-jets final state. Comparisons with the predictions in the four-flavour scheme, in particular from aMC@NLO, show a disagreement of more than two standard deviations in the Z+1b-jet final state.

Comparisons of the kinematic properties of Z+2b-jets production with the predictions from MADGRAPH in the five-flavour scheme show potential limitations of the existing MC event generators that employ the matrix element plus parton shower approach at leading order with massless b quarks. While these observations should be confirmed with more data, next-to-leading-order simulations and/or simulations with massive quarks could possibly provide a better description of the data in certain regions of phase space.
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References


[11] D0 collaboration, V.M. Abazov et al., Measurement of the ratio of inclusive cross sections \( \sigma(p\bar{p} \rightarrow Z + b\text{-quark jet})/\sigma(p\bar{p} \rightarrow Z + \text{jet}) \) at \( \sqrt{s} = 1.96 \) TeV, Phys. Rev. D 83 (2011) 031105 [arXiv:1010.6203] [inSPIRE].


[15] D0 collaboration, V.M. Abazov et al., Measurement of the ratio of differential cross sections \( \sigma(p\bar{p} \rightarrow Z + b\text{-jet})/\sigma(p\bar{p} \rightarrow Z + \text{jet}) \) in pp collisions at \( \sqrt{s} = 1.96 \) TeV, Phys. Rev. D 87 (2013) 092010 [arXiv:1301.2233] [inSPIRE].


[26] CMS collaboration, Measurement of the underlying event activity at the LHC with \( \sqrt{s} = 7 \) TeV and comparison with \( \sqrt{s} = 0.9 \) TeV, JHEP 09 (2011) 109 [arXiv:1107.0330] [inSPIRE].


[31] CMS collaboration, Commissioning of the particle-flow event reconstruction with the first LHC collisions recorded in the CMS detector, CMS-PAS-PFT-10-001 (2010).


Figueiredo, L. Mundim, H. Nogima, W.L. Prado Da Silva, A. Santoro, A. Sznajder, E.J. Tonelli Manganote, A. Vilela Pereira

Universidade Estadual Paulista \textsuperscript{a}, Universidade Federal do ABC \textsuperscript{b}, São Paulo, Brazil

C.A. Bernardes\textsuperscript{b}, F.A. Dias\textsuperscript{a,7}, T.R. Fernandez Perez Tomei\textsuperscript{a}, E.M. Gregores\textsuperscript{b}, C. Lagana\textsuperscript{a}, P.G. Mercadante\textsuperscript{b}, S.F. Novaes\textsuperscript{a}, Sandra S. Padula\textsuperscript{a}

Institute for Nuclear Research and Nuclear Energy, Sofia, Bulgaria

V. Genchev\textsuperscript{2}, P. Iaydjiev\textsuperscript{2}, S. Piperov, M. Rodozov, G. Sultanov, M. Vutova

University of Sofia, Sofia, Bulgaria

A. Dimitrov, R. Hadjiiska, V. Kozhuharov, L. Litov, B. Pavlov, P. Petkov

Institute of High Energy Physics, Beijing, China


State Key Laboratory of Nuclear Physics and Technology, Peking University, Beijing, China

C. Asawatangtrakuldee, Y. Ban, Y. Guo, Q. Li, W. Li, S. Liu, Y. Mao, S.J. Qian, D. Wang, L. Zhang, W. Zou

Universidad de Los Andes, Bogota, Colombia

C. Avila, C.A. Carrillo Montoya, L.F. Chaparro Sierra, J.P. Gomez, B. Gomez Moreno, J.C. Sanabria

Technical University of Split, Split, Croatia

N. Godinovic, D. Lelas, R. Plestina\textsuperscript{8}, D. Polic, I. Puljak

University of Split, Split, Croatia

Z. Antunovic, M. Kovac

Institute Rudjer Boskovic, Zagreb, Croatia

V. Brigljevic, K. Kadija, J. Luetic, D. Mekterovic, S. Morovic, L. Tikvica

University of Cyprus, Nicosia, Cyprus

A. Attikis, G. Mavromanolakis, J. Mousa, C. Nicolaou, F. Ptochos, P.A. Razis

Charles University, Prague, Czech Republic

M. Finger, M. Finger Jr.

Academy of Scientific Research and Technology of the Arab Republic of Egypt, Egyptian Network of High Energy Physics, Cairo, Egypt

A.A. Abdelalim\textsuperscript{9}, Y. Assran\textsuperscript{10}, S. Elgammal\textsuperscript{11}, A. Ellithi Kamei\textsuperscript{12}, M.A. Mahmoud\textsuperscript{13}, A. Radi\textsuperscript{11,14}

National Institute of Chemical Physics and Biophysics, Tallinn, Estonia

M. Kadastik, M. Müntel, M. Murumaa, M. Raidal, L. Rebane, A. Tiko
University of Ioánnina, Ioánnina, Greece
X. Aslanoglou, I. Evangelou, G. Flouris, C. Foudas, P. Kokkas, N. Manthos, I. Papadopoulos, E. Paradas

Wigner Research Centre for Physics, Budapest, Hungary
G. Bencze, C. Hajdu, P. Hidas, D. Horvath, F. Sikler, V. Veszpremi, G. Vesztergombi, A.J. Zsigmond

Institute of Nuclear Research ATOMKI, Debrecen, Hungary
N. Beni, S. Czellar, J. Molnar, J. Palinkas, Z. Szillasi

University of Debrecen, Debrecen, Hungary
J. Karancsi, P. Raics, Z.L. Trocsanyi, B. Ujvari

National Institute of Science Education and Research, Bhubaneswar, India
S.K. Swain

Panjab University, Chandigarh, India
S.B. Beri, V. Bhatnagar, N. Dhingra, R. Gupta, M. Kaur, M.Z. Mehta, M. Mittal, N. Nishu, A. Sharma, J.B. Singh

University of Delhi, Delhi, India
Ashok Kumar, Arun Kumar, S. Ahuja, A. Bhardwaj, B.C. Choudhary, S. Malhotra, M. Naimuddin, K. Ranjan, P. Saxena, V. Sharma, R.K. Shivpuri

Saha Institute of Nuclear Physics, Kolkata, India

Bhabha Atomic Research Centre, Mumbai, India
A. Abdulsalam, D. Dutta, S. Kailas, V. Kumar, A.K. Mohanty, L.M. Pant, P. Shukla, A. Topkar

Tata Institute of Fundamental Research - EHEP, Mumbai, India

Tata Institute of Fundamental Research - HECR, Mumbai, India
S. Banerjee, S. Dugad

Institute for Research in Fundamental Sciences (IPM), Tehran, Iran
H. Arfaei, H. Bakhshiansohi, S.M. Etesami, A. Fahim, A. Jafari, M. Khakzad, M. Mohammadi Najafabadi, S. Paktinat Mehdibadi, B. Safarzadeh, M. Zeinali

University College Dublin, Dublin, Ireland
M. Grunewald
University of Seoul, Seoul, Korea
M. Choi, J.H. Kim, C. Park, I.C. Park, S. Park, G. Ryu

Sungkyunkwan University, Suwon, Korea

Vilnius University, Vilnius, Lithuania
I. Grigelionis, A. Juodagalvis

Centro de Investigacion y de Estudios Avanzados del IPN, Mexico City, Mexico

Universidad Iberoamericana, Mexico City, Mexico
S. Carrillo Moreno, F. Vazquez Valencia

Benemerita Universidad Autonoma de Puebla, Puebla, Mexico
H.A. Salazar Ibarguen

Universidad Autónoma de San Luis Potosí, San Luis Potosí, Mexico
E. Casimiro Linares, A. Morelos Pineda, M.A. Reyes-Santos

University of Auckland, Auckland, New Zealand
D. Krofcheck

University of Canterbury, Christchurch, New Zealand
P.H. Butler, R. Doesburg, S. Reucroft, H. Silverwood

National Centre for Physics, Quaid-I-Azam University, Islamabad, Pakistan
M. Ahmad, M.I. Asghar, J. Butt, H.R. Hoorani, W.A. Khan, T. Khurshid, S. Qazi, M.A. Shah, M. Shoail

National Centre for Nuclear Research, Swierk, Poland

Institute of Experimental Physics, Faculty of Physics, University of Warsaw, Warsaw, Poland

Laboratório de Instrumentação e Física Experimental de Partículas, Lisboa, Portugal

Joint Institute for Nuclear Research, Dubna, Russia
Petersburg Nuclear Physics Institute, Gatchina (St. Petersburg), Russia

Institute for Nuclear Research, Moscow, Russia

Institute for Theoretical and Experimental Physics, Moscow, Russia
V. Epshteyn, M. Erofeeva, V. Gavrilov, N. Lychkovskaya, V. Popov, G. Safronov, S. Semenov, A. Spiridonov, V. Stolin, E. Vlasov, A. Zhokin

P.N. Lebedev Physical Institute, Moscow, Russia

Skobeltsyn Institute of Nuclear Physics, Lomonosov Moscow State University, Moscow, Russia
A. Belyaev, E. Boos, V. Bunichev, M. Dubinin, L. Dudko, A. Ershov, V. Klyukhin, O. Kodolova, I. Lokhtin, A. Markina, S. Obraztsov, S. Petrushanko, V. Savrin, A. Snigirev

State Research Center of Russian Federation, Institute for High Energy Physics, Protvino, Russia

University of Belgrade, Faculty of Physics and Vinca Institute of Nuclear Sciences, Belgrade, Serbia
P. Adzic, M. Djordjevic, M. Ekmedzic, D. Krpic, J. Milosevic

Centro de Investigaciones Energéticas Medioambientales y Tecnológicas (CIEMAT), Madrid, Spain

Universidad Autónoma de Madrid, Madrid, Spain
C. Albajar, J.F. de Trocóniz

Universidad de Oviedo, Oviedo, Spain
Instituto de Física de Cantabria (IFCA), CSIC-Universidad de Cantabria, Santander, Spain


CERN, European Organization for Nuclear Research, Geneva, Switzerland


Paul Scherrer Institut, Villigen, Switzerland


Institute for Particle Physics, ETH Zurich, Zurich, Switzerland


Universität Zürich, Zurich, Switzerland

C. Amsler, V. Chiochia, C. Favaro, M. Ivoica Rikova, B. Kilminster, B. Millan Mejias, P. Robmann, H. Snoek, S. Taroni, M. Verzetti, Y. Yang

National Central University, Chung-Li, Taiwan

National Taiwan University (NTU), Taipei, Taiwan
P. Bartalini, P. Chang, Y.H. Chang, Y.W. Chang, Y. Chao, K.F. Chen, C. Dietz, 
U. Grundler, W.-S. Hou, Y. Hsiung, K.Y. Kao, Y.J. Lei, R.-S. Lu, D. Majumder, 

Chulalongkorn University, Bangkok, Thailand
B. Asavapibhop, N. Suwonjandee

Cukurova University, Adana, Turkey
A. Adiguzel, M.N. Bakirci, S. Cerci, C. Dozen, I. Dumanoglu, E. Eskut, S. Girgis, 
G. Gokbulut, E. Gurbpinar, I. Hos, E.E. Kangal, A. Kayis Topaksu, G. Onengut, 
K. Ozdemir, S. Ozturk, A. Polatoz, K. Sogut, D. Sunar Cerci, B. Tali, H. Topakli, 
M. Vergili

Middle East Technical University, Physics Department, Ankara, Turkey
I.V. Akin, T. Aliev, B. Bilin, S. Bilmis, M. Deniz, H. Gamsizkan, A.M. Guler, 
M. Zeyrek

Bogazici University, Istanbul, Turkey
E. G€ulmez, B. Isildak, M. Kaya, O. Kaya, S. Ozkorucuklu, N. Sonmez

Istanbul Technical University, Istanbul, Turkey
H. Bahtiyar, E. Barlas, K. Cankocak, Y.O. G€unaydin, F.I. Vardarli, M. Yücel

National Scientific Center, Kharkov Institute of Physics and Technology, 
Kharkov, Ukraine
L. Levchuk, P. Sorokin

University of Bristol, Bristol, United Kingdom
J.J. Brooke, E. Clement, D. Cussans, H. Flacher, R. Frazier, J. Goldstein, M. Grimes, 
K. Nirunpong, S. Paramesvaran, A. Poll, S. Senkin, V.J. Smith, T. Williams

Rutherford Appleton Laboratory, Didcot, United Kingdom
K.W. Bell, A. Belyaev, C. Brew, R.M. Brown, D.J.A. Cocklerill, J.A. Coughlan, 

Imperial College, London, United Kingdom
R. Bainbridge, O. Buchmuller, D. Burton, D. Colling, N. Cripps, M. Cutajar, P. Dauncey, 
G. Davies, M. Della Negra, W. Ferguson, J. Fulcher, D. Fuyuan, A. Gilbert, A. Guneratne, 
Bryer, G. Hall, Z. Hatherell, J. Hays, G. Iles, M. Jarvis, G. Karapostoli, M. Kenzie, 
R. Lane, R. Lucas, L. Lyons, A.-M. Magnan, J. Marrouche, B. Mathias, R. Nandi, 
J. Nash, A. Nikitenko, J. Pela, M. Pesaresi, K. Petridis, M. Pioppi, D.M. Raymond, 
S. Rogerson, A. Rose, C. Seez, P. Sharp, A. Sparrow, A. Tapper, M. Vazquez Acosta, 
T. Virdee, S. Wakefield, N. Wardle
Brunel University, Uxbridge, United Kingdom

Baylor University, Waco, U.S.A.
J. Dittmann, K. Hatakeyama, A. Kasmi, H. Liu, T. Scarborough

The University of Alabama, Tuscaloosa, U.S.A.
O. Charaf, S.I. Cooper, C. Henderson, P. Rumerio

Boston University, Boston, U.S.A.
A. Avetisyan, T. Bose, C. Fantasia, A. Heister, P. Lawson, D. Lazic, J. Rohlf, D. Sperka, J. St. John, L. Sulak

Brown University, Providence, U.S.A.

University of California, Davis, Davis, U.S.A.

University of California, Los Angeles, U.S.A.

University of California, Riverside, Riverside, U.S.A.

University of California, San Diego, La Jolla, U.S.A.

University of California, Santa Barbara, Santa Barbara, U.S.A.
California Institute of Technology, Pasadena, U.S.A.
A. Apresyan, A. Bornheim, J. Bunn, Y. Chen, E. Di Marco, J. Duarte, D. Keira, Y. Ma,
A. Mott, H.B. Newman, C. Pena, C. Rogan, M. Spiropulu, V. Timciuc, J. Veverka,
R. Wilkinson, S. Xie, R.Y. Zhu

Carnegie Mellon University, Pittsburgh, U.S.A.
V. Azzolini, A. Calamba, R. Carroll, T. Ferguson, Y. Iiyama, D.W. Jang, Y.F. Liu,
M. Paulini, J. Russ, H. Vogel, I. Vorobiev

University of Colorado at Boulder, Boulder, U.S.A.
K. Stenson, K.A. Ulmer, S.R. Wagner

Cornell University, Ithaca, U.S.A.
J. Alexander, A. Chatterjee, N. Eggert, L.K. Gibbons, W. Hopkins, A. Khukhunaishvili,
B. Kreis, N. Mirman, G. Nicolas Kaufman, J.R. Patterson, A. Ryd, E. Salvati, W. Sun,
W.D. Teo, J. Thom, J. Thompson, J. Tucker, Y. Weng, L. Winstrom, P. Wittich

Fairfield University, Fairfield, U.S.A.
D. Winn

Fermi National Accelerator Laboratory, Batavia, U.S.A.
S. Abdullin, M. Albrow, J. Anderson, G. Apollinari, L.A.T. Bauerick, A. Beretvas,
J. Berryhill, P.C. Bhat, K. Burkett, J.N. Butler, V. Chethuru, H.W.K. Cheung, F. Chlebana,
S. Cihangir, V.D. Elvira, I. Fisk, J. Freeman, Y. Gao, E. Gottschalk, L. Gray,
D. Green, O. Gutsche, D. Hare, R.M. Harris, J. Hirschauer, B. Hooberman, S. Jindariani,
M. Johnson, U. Joshi, K. Kaadze, B. Klima, S. Kunori, S. Kwan, J. Linacre, D. Lincoln,
R. Lipton, J. Lykken, K. Maeshima, J.M. Marraffino, V.I. Martinez Outschoorn,
V. O’Dell, O. Prokofyev, N. Ratnikova, E. Sexton-Kennedy, S. Sharma,
W.J. Spalding, L. Spiegel, L. Taylor, S. Tkaczyk, N.V. Tran, L. Uplegger, E.W. Vaandering,
R. Vidal, J. Whitmore, W. Wu, F. Yang, J.C. Yun

University of Florida, Gainesville, U.S.A.
D. Dobur, A. Drozdetskiy, R.D. Field, M. Fisher, Y. Fu, I.K. Furic, J. Hugon,
B. Kim, J. Konigsberg, A. Korytov, A. Kropivnitskaya, T. Kypreos, J.F. Low, K. Matchev,
P. Milenovic, G. Mitselmakher, L. Muniz, R. Remington, A. Rinkevicius, N. Skhirtladze,
M. Snowball, J. Yelton, M. Zakaria

Florida International University, Miami, U.S.A.
V. Gaultney, S. Hewamanage, S. Linn, P. Markowitz, G. Martinez, J.L. Rodriguez

Florida State University, Tallahassee, U.S.A.
T. Adams, A. Askew, J. Bochenek, J. Chen, B. Diamond, S.V. Gleyzer, J. Haas,
S. Hagopian, V. Hagopian, K.F. Johnson, H. Prosper, V. Veeraraghavan, M. Weinberg
University of Nebraska-Lincoln, Lincoln, U.S.A.

State University of New York at Buffalo, Buffalo, U.S.A.

Northeastern University, Boston, U.S.A.

Northwestern University, Evanston, U.S.A.

University of Notre Dame, Notre Dame, U.S.A.

The Ohio State University, Columbus, U.S.A.
L. Antonelli, B. Bylsma, L.S. Durkin, C. Hill, R. Hughes, K. Kotov, T.Y. Ling, D. Puigh, M. Rodenburg, G. Smith, C. Vuosalo, B.L. Winer, H. Wolfe

Princeton University, Princeton, U.S.A.

University of Puerto Rico, Mayaguez, U.S.A.
E. Brownson, A. Lopez, H. Mendez, J.E. Ramirez Vargas

Purdue University, West Lafayette, U.S.A.

Purdue University Calumet, Hammond, U.S.A.
N. Parashar

Rice University, Houston, U.S.A.
A. Adair, B. Akgun, K.M. Ecklund, F.J.M. Geurts, W. Li, B. Michlin, B.P. Padley, R. Redjimi, J. Roberts, J. Zabel

University of Rochester, Rochester, U.S.A.
B. Betchart, A. Bodek, R. Covarelli, P. de Barbaro, R. Demina, Y. Eshaq, T. Ferbel, A. Garcia-Bellido, P. Goldenzweig, J. Han, A. Harel, D.C. Miner, G. Petrillo, D. Vihnevskiy, M. Zielinski
The Rockefeller University, New York, U.S.A.
A. Bhatti, R. Ciesielski, L. Demortier, K. Goulianos, G. Lungu, S. Malik, C. Mesropian

Rutgers, The State University of New Jersey, Piscataway, U.S.A.

University of Tennessee, Knoxville, U.S.A.

Texas A&M University, College Station, U.S.A.

Texas Tech University, Lubbock, U.S.A.
N. Akchurin, C. Cowden, J. Damgov, C. Dragoiu, P.R. Dudero, K. Kovitanggoon, S.W. Lee, T. Libeiro, I. Volobouev

Vanderbilt University, Nashville, U.S.A.

University of Virginia, Charlottesville, U.S.A.

Wayne State University, Detroit, U.S.A.
S. Gollapinni, R. Harr, P.E. Karchin, C. Kottachchi Kankanamge Don, P. Lamichhane, A. Sakharov

University of Wisconsin, Madison, U.S.A.

†: Deceased
1: Also at Vienna University of Technology, Vienna, Austria
2: Also at CERN, European Organization for Nuclear Research, Geneva, Switzerland
3: Also at Institut Pluridisciplinaire Hubert Curien, Université de Strasbourg, Université de Haute Alsace Mulhouse, CNRS/IN2P3, Strasbourg, France
4: Also at National Institute of Chemical Physics and Biophysics, Tallinn, Estonia
5: Also at Skobeltsyn Institute of Nuclear Physics, Lomonosov Moscow State University, Moscow, Russia
6: Also at Universidade Estadual de Campinas, Campinas, Brazil
7: Also at California Institute of Technology, Pasadena, U.S.A.
8: Also at Laboratoire Leprince-Ringuet, Ecole Polytechnique, IN2P3-CNRS, Palaiseau, France
9: Also at Zewail City of Science and Technology, Zewail, Egypt
10: Also at Suez Canal University, Suez, Egypt
11: Also at British University in Egypt, Cairo, Egypt
12: Also at Cairo University, Cairo, Egypt
13: Also at Fayoum University, El-Fayoum, Egypt
14: Now at Ain Shams University, Cairo, Egypt
15: Also at National Centre for Nuclear Research, Swierk, Poland
16: Also at Université de Haute Alsace, Mulhouse, France
17: Also at Joint Institute for Nuclear Research, Dubna, Russia
18: Also at Brandenburg University of Technology, Cottbus, Germany
19: Also at The University of Kansas, Lawrence, U.S.A.
20: Also at Institute of Nuclear Research ATOMKI, Debrecen, Hungary
21: Also at Eötvös Loránd University, Budapest, Hungary
22: Also at Tata Institute of Fundamental Research - EHEP, Mumbai, India
23: Also at Tata Institute of Fundamental Research - HECR, Mumbai, India
24: Now at King Abdulaziz University, Jeddah, Saudi Arabia
25: Also at University of Visva-Bharati, Santiniketan, India
26: Also at University of Ruhuna, Matara, Sri Lanka
27: Also at Isfahan University of Technology, Isfahan, Iran
28: Also at Sharif University of Technology, Tehran, Iran
29: Also at Plasma Physics Research Center, Science and Research Branch, Islamic Azad University, Tehran, Iran
30: Also at Laboratori Nazionali di Legnaro dell’INFN, Legnaro, Italy
31: Also at Università degli Studi di Siena, Siena, Italy
32: Also at Purdue University, West Lafayette, U.S.A.
33: Also at Universidad Michoacana de San Nicolas de Hidalgo, Morelia, Mexico
34: Also at St. Petersburg State Polytechnical University, St. Petersburg, Russia
35: Also at Faculty of Physics, University of Belgrade, Belgrade, Serbia
36: Also at Facoltà Ingegneria, Università di Roma, Roma, Italy
37: Also at Scuola Normale e Sezione dell’INFN, Pisa, Italy
38: Also at University of Athens, Athens, Greece
39: Also at Rutherford Appleton Laboratory, Didcot, United Kingdom
40: Also at Paul Scherrer Institut, Villigen, Switzerland
41: Also at Institute for Theoretical and Experimental Physics, Moscow, Russia
42: Also at Albert Einstein Center for Fundamental Physics, Bern, Switzerland
43: Also at Gaziosmanpasa University, Tokat, Turkey
44: Also at Adiyaman University, Adiyaman, Turkey
45: Also at Cag University, Mersin, Turkey
46: Also at Mersin University, Mersin, Turkey
47: Also at Izmir Institute of Technology, Izmir, Turkey
48: Also at Ozyegin University, Istanbul, Turkey
49: Also at Kafkas University, Kars, Turkey
50: Also at Suleyman Demirel University, Isparta, Turkey
<table>
<thead>
<tr>
<th>Number</th>
<th>Affiliation</th>
</tr>
</thead>
<tbody>
<tr>
<td>51</td>
<td>Also at Ege University, Izmir, Turkey</td>
</tr>
<tr>
<td>52</td>
<td>Also at Mimar Sinan University, Istanbul, Istanbul, Turkey</td>
</tr>
<tr>
<td>53</td>
<td>Also at Kahramanmaras Sütçü Imam University, Kahramanmaras, Turkey</td>
</tr>
<tr>
<td>54</td>
<td>Also at School of Physics and Astronomy, University of Southampton, Southampton, United Kingdom</td>
</tr>
<tr>
<td>55</td>
<td>Also at INFN Sezione di Perugia; Università di Perugia, Perugia, Italy</td>
</tr>
<tr>
<td>56</td>
<td>Also at Utah Valley University, Orem, U.S.A.</td>
</tr>
<tr>
<td>57</td>
<td>Also at Institute for Nuclear Research, Moscow, Russia</td>
</tr>
<tr>
<td>58</td>
<td>Also at University of Belgrade, Faculty of Physics and Vinca Institute of Nuclear Sciences, Belgrade, Serbia</td>
</tr>
<tr>
<td>59</td>
<td>Also at Argonne National Laboratory, Argonne, U.S.A.</td>
</tr>
<tr>
<td>60</td>
<td>Also at Erzincan University, Erzincan, Turkey</td>
</tr>
<tr>
<td>61</td>
<td>Also at Yildiz Technical University, Istanbul, Turkey</td>
</tr>
<tr>
<td>62</td>
<td>Also at Texas A&amp;M University at Qatar, Doha, Qatar</td>
</tr>
<tr>
<td>63</td>
<td>Also at Kyungpook National University, Daegu, Korea</td>
</tr>
</tbody>
</table>