Steady States and Dynamics of Urokinase-Mediated Plasmin Activation In Silico and In Vitro

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ABSTRACT Plasmin (PLS) and urokinase-type plasminogen activator (UPA) are ubiquitous proteases that regulate the extracellular environment. Although they are secreted in inactive forms, they can activate each other through proteolytic cleavage. This mutual interplay creates the potential for complex dynamics, which we investigated using mathematical modeling and in vitro experiments. We constructed ordinary differential equations to model the conversion of precursor plasminogen into active PLS, and precursor urokinase (scUPA) into active urokinase (tcUPA). Although neither PLS nor UPA exhibits allostERIC cooperativity, modeling showed that cooperativity occurred at the system level because of substrate competition. Computational simulations and bifurcation analysis predicted that the system would be bistable over a range of parameters for cooperativity and positive feedback. Cell-free experiments with recombinant proteins tested key predictions of the model. PLS activation in response to scUPA stimulus was found to be cooperative in vitro. Finally, bistability was demonstrated in vitro by the presence of two significantly different steady-state levels of PLS activation for the same levels of stimulus. We conclude that ultrasensitive, bistable activation of UPA-PLS is possible in the presence of substrate competition. An ultrasensitive threshold for activation of PLS and UPA would have ramifications for normal and disease processes, including angiogenesis, metastasis, wound healing, and fibrosis.

INTRODUCTION

Plasmin (PLS) is a serine protease that is best known for its role in digesting blood clots, but it has many substrates and far-reaching physiological functions in hemostasis (1), angiogenesis (2), wound healing (3,4), and cell motility, including migration and metastasis (5). For example, it activates matrix metalloproteases (MMPs; e.g., MMP1, MMP3, and MMP13 (6,7)) and regulates growth factors (e.g., VEGF (8), HGF (9), and TGF-β1 (10)). Spatiotemporal control of PLS availability occurs through localized activation of the inactive precursor plasminogen (PLG), which is widely available through circulation. The cleavage of PLG to make active PLS occurs at the Arg561-Val562 bond, caused by tissue plasminogen activator (tPA) or urokinase-type plasminogen activator (UPA). tPA influences PLS activation mainly in the connective tissues, whereas UPA plays a more important role in the extracellular matrix (ECM) of tissues (11). Regulation of PLS activity is also controlled by the specific inhibitors α-2-macroglobulin (A2M) or α-2-antiplasmin (A2P) (12).

Protease activation can be categorized according to regulatory motifs such as auto-activation (Fig. 1 A), in which an active protease X cleaves its inactive precursor form. An alternative manner of activation (Fig. 1 B) operates via regulation of an intermediate regulatory enzyme (Y), which also has active and precursor forms. This type of positive feedback is seen in pathways such as caspase activation (13,14), MMP activation (15), and blood clotting (16). Fig. 1 C displays a variant in which the precursor form of Y has some low level of catalytic activity, less than the activated form but not entirely inactive. Urokinase exhibits a low level ofzymogen activity, and the final motif (Fig. 1 C) describes the biochemical relationship between PLS and UPA.

The signaling dynamics of positive feedback loops have been extensively modeled (17,18), most commonly for kinase cascades (19–21). Computational modeling is particularly useful for elucidating the bifurcations, qualitative changes in pathway behavior, and emergent behaviors that arise in a complex system (18–22). Bistability, or the presence of two stable steady states, has been shown to be crucial for making robust yes-or-no decisions in cell cycle and apoptosis (23). Eissing et al. (24) explored the requirements for bistability in a feedback loop with two proteases. Substrate competition has been found to influence bistability for kinases (25), but has not yet been modeled for proteases. Because proteases (e.g., caspas) typically have many competing substrates (26) and sometimes have initialzymogen activity (27), the effects of substrate competition andzymogen activity might be important considerations for future system-level modeling.

In this work, we modeled the dynamics of UPA-mediated PLS activation and performed biochemical experiments to test key predictions. The model predicts that UPA-PLS

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activation will be bistable in the presence of positive feedback and cooperativity. An extended model predicts that PLS activation will exhibit significant cooperativity in the presence of substrate competition. We performed in vitro experiments to test the cooperativity of PLS activation, and to measure the bi- or monostability of the PLS steady-state convergence. The results are interpreted in the context of physiological systems in which UPAs and PLSs are known to function.

MATERIALS AND METHODS

Computational methods

We simulated ordinary differential equations (ODEs) using the ODE15s stiff solver of MATLAB (The MathWorks, Natick, MA; http://www.mathworks.com). For simulations with random initial conditions, we generated 100 initial concentrations for all species uniformly at random between the nominal values. We then calculated the number of parameter sets that were capable of bistability using the “going-up” and “coming-down” simulations. For Fig. 6C, the parameter of interest was fixed while all other parameters were randomly perturbed by ±20% or ±50% from the nominal values. A parameter set is considered bistable if the difference between the high and low steady states of PLS is >0.03 μM. Note that 0.007 μM and 0.0375 μM are the two steady states of PLS obtained from the model shown in Table 2 with substrate competition and cooperativity index (ci) = 1.

The Hill coefficient ($n_H$) was calculated with the use of the statistical software GraphPad prism (Graphpad Software; San Diego, CA).

Experimental methods

All solutions were prepared in Tris buffer (0.05 M Tris-HCL, 0.10 M NaCl, 0.01% Tween 80, pH 7.4). The chromogenic substrate of PLS, S2251 (0.4 mM), with chemical formula H-D-Val-Leu-Lys-pNA·2HCl, was purchased from Chromogenix (Milano, Italy). In the presence of PLS, the following reaction occurs, releasing pNA:

$$H-D-Val-Leu-Lys-pNA + PLS \rightarrow H-D-Val-Leu-Lys-OH + pNA.$$  

The color intensity of pNA can be measured at an O.D. of 405 nm. For the test of cooperativity, we used variable amounts of scUPA (0.1–6 nM; American Diagnostica, Greenwich, CT) along with a nonvariable initial concentration of 1 μM PLG (Glu-PLG; Merck, Darmstadt, Germany). The changing color intensity of S2251 (absorbance), which is a direct measure of PLS activity, was measured at O.D. = 405 nm with a Tecan M200 microplate reader. During the experiments, scUPA and PLG were added manually every 15 min at rates of 50 pM/min and 1 nM/min, respectively (in volumes of ~0.2 μL) to simulate the turnover that would occur in a natural system. The total volume of the reaction solution was 200 μL. No S2251 was added. The “going-up” experiments were initiated with PLS (Sigma, St. Louis, MO) and PLG concentrations in the ratio 60% PLG/40%PLS (0.6 μM PLG, 0.4 μM PLS). Various initial concentrations of scUPA were added, and PLS steady state was measured. For the “coming-down” experiments, the ratio was reversed (0.4 μM PLG, 0.6 μM PLS) and the same series of scUPA levels was used.

RESULTS

Construction of the model

UPA is a trypsin-like serine protease that is initially secreted as a single intact chain, scUPA (29–31). The intrinsic enzymatic activity of scUPA is used to initiate the cleavage of inactive PLG (No. 1 in Table 1 and Fig. 2). Cleavage of PLG at the Arg561-Val562 bond releases the active serine protease, PLS. Active PLS can cleave scUPA at the Lys158-Ile159 backbone, releasing a two-chain form (tcUPA;
The interactions between UPA and PLS (Fig. 2 A) were expressed as ODEs (see Table S1 in the Supporting Material) for the concentration change of each species with respect to time. Enzyme kinetics were approximated using linear terms (Table 2).

No. 2 in Table 1 and Fig. 2) in which the two chains are linked by a disulphide bridge. tcUPA has 12-fold higher enzymatic activity than scUPA for cleaving PLG to PLS (No. 3 in Table 1 and Fig. 2 A). The interdependent proteolytic activation of tcUPA and PLS is consistent with the motif of Fig. 1 C.

The interactions between UPA and PLS (Fig. 2 A) were expressed as ODEs (see Table S1 in the Supporting Material) for the concentration change of each species with respect to time. Enzyme kinetics were approximated using linear terms (Table 2).

The use of linear terms, rather than more complex Michaelis-Menten kinetics, was chosen because the kM parameters are much greater than the substrate concentrations (31–33). Table 2 shows key terms of the equations, numbered to correspond with the arrows in Fig. 2 A. We used constant rates to model production of the precursor forms (scUPA and PLG) and first-order degradation rates for all species, with the rate constants given in Table 2. Production and degradation are particularly important in this model because proteolysis reactions are irreversible and, in the absence of turnover, the steady state of the system would tend toward a trivial, nonphysiological situation of total cleavage. Substrate competition can create cooperativity in enzyme action, apart from the traditional mode of allosteric cooperativity (25). Because PLS has many substrates, we allowed it to have a cooperative effect on UPA with an empirical Hill coefficient (ci > 1) in the equation for PLS enzyme kinetics. In subsequent analysis, the case of ci = 1 will also be explored. Most of the other parameters have values from experimental measurements obtained in previous studies (Table 2).

Model simulation analysis

The model ODEs were simulated with randomly generated initial concentrations between 1e-3 μM and 0.1 μM. The steady states of the model show that PLS converges over time to two different concentrations (0.007 μM or 0.035 μM; Fig. 2 B). The presence of more than one steady state indicates that complex dynamics is an emergent behavior of the system.

For subsequent plots of model behavior, instead of displaying a horizontal time axis, we define the output of each simulation to be simply the final PLS concentration (at steady state). Fig. 2 C shows a projection of many time-series simulations onto a single curve, showing that the transition between the two steady states of PLS can be triggered by changing the initial concentration of the initiator protease scUPA. This abrupt increase in the PLS steady state upon a change in the initial scUPA concentration demonstrates that the model is ultrasensitive, meaning that small perturbations of the parameters can cause significant changes in model output (34). For concentrations of scUPA < 0.7 μM, PLS is maintained at the lower steady state, and for concentrations of scUPA above this threshold value, PLS levels increase abruptly to a higher steady state. One way to understand this behavior is to consider that higher initial concentrations of scUPA can provide greater amounts of PLS and cause more activation of tcUPA. Because tcUPA has a higher catalytic efficiency than scUPA, an increase in PLS generation occurs via the positive feedback loop. In contrast, lower scUPA concentrations would not create PLS quickly enough to overcome the background degradation, and would not increase tcUPA levels enough to exploit the positive feedback loop. These results indicate that, depending on the initial concentrations of model species, the system is ultrasensitive. Ultraspensitve systems have been shown to be capable of bistability (34), and we checked for the presence of bistability in the current system by varying parameter values and following the steady-state behavior.

We simulated PLS steady-state levels using a “going-up” and “coming-down” approach (28). The values of keffPLS (catalytic efficiency of PLS), would control the amount of tcUPA present in the system, and also indirectly regulate the effect of tcUPA on PLG to produce more PLS. keffPLS
was varied along two directions (“going-up” and “coming-down”) and the amounts of PLS in the final steady states (calculated to 50,000 steps) were plotted (Fig. 2 D). A bistable phenomenon was noticed during this simulation. Increasing values of \( k_{effPLS} \) were seen to gradually increase the stable steady-state levels of PLS until \( k_{effPLS} \) reached a second threshold of \( < 33.5 \mu M^{-1}s^{-1} \), and only then did PLS steady-state levels drop down. The region between these two threshold values of \( k_{effPLS} \) is the bistable region; depending on the initial conditions, PLS could achieve steady state at either a higher or lower level. The phenomenon of remembering an earlier state (or an earlier concentration level), even when the stimulus is removed, is called hysteresis.

Bistability in a system has been shown to depend on positive feedback and cooperativity (35). We assessed the significance of positive feedback and cooperativity on model bistability by modifying these parameters. We refer to the rate at which tcUPA converts PLG into PLS as the positive feedback rate, \( k_{eff} \). The parameter \( ci \) is the Hill coefficient of PLS and represents the cooperativity in PLS action due to substrate competition effects. In the absence of positive feedback (\( k_{eff} = 0 \mu M^{-1}s^{-1} \)), increasing \( ci \) increases PLG concentration at the lower steady state because there is not enough conversion of inactive PLG to PLS (Fig. 3 A). When the strength of positive feedback, \( k_{eff} \), is increased to 0.1 \( \mu M^{-1}s^{-1} \), the positive feedback causes increased PLS activation, but PLS is still maintained at a monostable state. When the positive feedback signal, \( k_{eff} \), increases to 0.5, 1, 2, or 3 \( \mu M^{-1}s^{-1} \), PLS exhibits two steady states. The transition between monostability and bistability along the \( ci \) variable is shown by black dots, which denote the values of \( ci \) at which saddle node (SN) bifurcations occur for a given value of \( k_{eff} \). When a value of \( ci \) is chosen between these SN bifurcation points (SN1 and SN2 on the curve for \( k_{eff} = 3 \mu M^{-1}s^{-1} \)), the resulting system has two stable fixed points and one unstable fixed point between them. The gray arrow in Fig. 3 A indicates the evolution of PLS steady state with increasing \( k_{eff} \) values. Increasing the positive feedback strength facilitates bistability in the system and also increases the area of bistability, as illustrated by the two-parameter bifurcation diagram (gray region in Fig. 3 B) in which the parameters \( k_{eff} \) and \( ci \) are perturbed simultaneously. The shaded region indicates bistability, and the models in the other nonshaded portions are monostable. Fig. 3 B indicates that increasing \( k_{eff} \) yields a wider range of \( ci \) values with bistability. The two solid lines bordering the shaded cusp represent SN bifurcations between monostability and bistability.

Although cooperativity and positive feedback are both favorable toward bistability, they can also destroy bistability if they are not balanced with respect to each other. Even as increased values of \( k_{eff} \) cause an increased area of bistability, they require an increase in \( ci \) (rightward shift in Fig. 3, A and B) to maintain the bistability. Bistability is possible when the increased production of PLS (due to higher \( k_{eff} \)) is counterbalanced by increased production of tcUPA (due to higher \( ci \)). Positive feedback between tcUPA and PLS has been described previously (33), and the source of positive feedback is obvious from the reactions of mutual activation. Cooperativity has not been reported for PLS or UPA; therefore, we explored the possibility that cooperativity arises from substrate competition.

**Effect of substrate cooperativity on model dynamics**

We tested whether adding an explicit additional substrate of PLS could create cooperation and reproduce the effect of having a Hill coefficient \( ci > 1 \) in the PLS kinetic equation. Enzyme cooperativity occurs when increasing the concentration of an enzyme causes a nonlinear (greater than additive) increase in activity (36). Cooperativity between multiple phosphorylation sites has been shown to be responsible for bistability in MAPK cascades (20). Another form of kinase-phosphatase cooperativity was discussed by Kim and Ferrell (25), who showed that increasing the substrates of the cell cycle kinase cdk1 caused an intrinsic cooperativity in the action of cdk1 and wee1. This cooperativity in turn could cause the bistable switching of their system.
PLS also has multiple substrates, so we sought to determine whether the activity of PLS on scUPA is cooperative in the presence of competing substrates. We constructed an extended model with a new PLS substrate, X (Fig. 4 A). For the hypothetical analogy between the model and the reality in vivo, species X corresponds to one or more physiological substrates with high affinity for PLS. (For validation experiments in vitro, as described in the following section, an exogenous high-affinity reagent (S2251) will be introduced in the role of species X.)

In the extended model, substrate X can bind PLS and form a complex (X.PLS). This complex can dissociate or undergo a catalytic reaction in which PLS consumes X and reverts to the unbound state. All simulations of the extended model were performed with no cooperativity built in explicitly, i.e., \( ci = 1 \). Additional parameters and values are given in Table 2. To analyze the extended model, the PLS parameter \( k_{effPLS} \) was perturbed. The steady-state endpoints for PLS were computed, and these endpoints were compiled into a “going-up”/“coming-down” plot as described in Materials and Methods. The results show that even if \( ci = 1 \), PLS can be bistable (Fig. 4 B). In fact, the area of bistability in this extended model is greater than that in the model with \( ci = 2 \) and no substrate competition (compare with a similar plot from Fig. 2 C). Adding substrates into the model has an overall effect similar to that obtained by increasing the \( ci \), as in Fig. 3 A. Added substrates sequester PLS away from the scUPA, unless PLS can consume the competing substrate more quickly than the turn-over rate. At a threshold level of \( k_{effPLS} \), PLS can finally overcome the competition and the system can move into a higher steady state. Substrate competition creates cooperativity because a small increase in PLS activity tips the balance toward consuming the substrate, releases some PLS from sequestration, and causes a greater-than-additive effect on scUPA.

We next examine the affinity of the competing substrate X, because the relative affinity of X and scUPA for PLS

### Table 1. List of reaction equations

<table>
<thead>
<tr>
<th>Reaction equation terms</th>
<th>Parameters</th>
<th>References</th>
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<tbody>
<tr>
<td>1. ( \text{scupa} + \text{plg} \xrightarrow{k_{effzymogen}} \text{plg} + \text{scupa} )</td>
<td>( k_{effzymogen} ) ( \times ) [scUPA] ( \times ) [PLG] ( = 0.035 \mu M^{-1}s^{-1} ) ( (31) )</td>
<td></td>
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<tr>
<td>2. ( \text{plg} \xrightarrow{k_{effPLS}} \text{plg} + \text{x} )</td>
<td>( k_{effPLS} = 40 \mu M^{-1}s^{-1} ) ( (31) )</td>
<td></td>
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<tr>
<td>3. ( \text{tcupa} + \text{plg} \xrightarrow{k_{effPLS}} \text{plg} + \text{tcupa} )</td>
<td>( k_{effPLS} = 0.9 \mu M^{-1}s^{-1} ) ( (31) )</td>
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<tr>
<td>4. ( \text{plg} \xrightarrow{\mu_1} \text{scupa} )</td>
<td>( \mu_1 = 0.084 s^{-1} ) ( (45, 49) )</td>
<td></td>
</tr>
<tr>
<td>5. ( \text{x} \xrightarrow{\mu_2} \text{plg} )</td>
<td>( \mu_2 = 0.032 s^{-1} ) ( (50, 51) )</td>
<td></td>
</tr>
<tr>
<td>6. ( \text{plg} \xrightarrow{\mu_3} \text{plg} )</td>
<td>( \mu_3 = 0.0032 s^{-1} ) ( (50, 51) )</td>
<td></td>
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<tr>
<td>7. ( \text{tcupa} \xrightarrow{\mu_3} \text{tcupa} )</td>
<td>( \mu_3 = 0.01 s^{-1} ) ( (45, 52) )</td>
<td></td>
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<tr>
<td>8. ( \text{x} \xrightarrow{\alpha_3} \text{x} )</td>
<td>( \alpha_3 = 0.01 s^{-1} ) ( (45, 52) )</td>
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<tr>
<td>9. ( \text{x} \xrightarrow{\alpha_2} \text{x} )</td>
<td>( \alpha_2 = 0.01 s^{-1} ) ( (45, 52) )</td>
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<tr>
<td>10. ( \text{x} \xrightarrow{\alpha_1} \text{x} )</td>
<td>( \alpha_1 = 0.0032 s^{-1} ) ( (45, 52) )</td>
<td></td>
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<tr>
<td>11. ( \text{x} \xrightarrow{\alpha_0} \text{x} )</td>
<td>( \alpha_0 = 0.0032 s^{-1} ) ( (45, 52) )</td>
<td></td>
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<tr>
<td>12. ( \text{x} \xrightarrow{\alpha_2} \text{x} )</td>
<td>( \alpha_2 = 0.01 s^{-1} ) ( (45, 52) )</td>
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Velocity terms \( \nu_1 - \nu_6 \) correspond to the reaction arrows numbered 1–6 in Figs. 2 and 4. Complete differential equations appear in Table S1. Parameters listed as variable were not assigned parameter values from the literature. Initial concentrations of the species in \( \mu M \): scUPA, PLG, PLS, tcUPA, X, and XPLS = 0.002, 0.01, 0, 0, 0.2, and 0, respectively.
can regulate the sequestration effect. As shown in Fig. 4 C, PLS steady-state values were simulated with different values of \( k_1 \) (the rate of substrate X binding to PLS but with \( c_i = 1 \) maintained in all cases. For low substrate binding (\( k_1 = 10 \mu M^{-1}s^{-1} \)), PLS exhibits a monostable high steady state because there is no high-affinity substrate to sequester the enzyme. With increasing values of \( k_1 \) (30 \( \mu M^{-1}s^{-1} \), 50 \( \mu M^{-1}s^{-1} \); Fig. 4 C), i.e., in presence of higher-affinity substrates, sequestration of PLS by the substrates increases, as evidenced by the increased retention of PLS in the lower steady state for higher values of \( \text{keff}_{\text{PLS}} \). For subsequent increased \( k_1 \) values, higher values of PLS enzymatic activity are needed before PLS can make the transition to the higher steady state. However, very high-affinity substrates (e.g., with \( k_1 = 100 \mu M^{-1}s^{-1} \)) keep PLS in a monostable lower steady state. This shows that a high-affinity substrate can sequester PLS and prevent it from triggering the transition to a high steady state. For intermediate values of \( k_1 \), PLS can be bistable, with the area of bistability increasing as \( k_1 \) increases. This shows that substrate competition is capable of producing enough nonlinearity in the PLS kinetics to generate two stable steady states for the system.

Experimental validation of model-based predictions

We experimentally tested whether ultrasensitivity and bistability could be observed in UPA-mediated PLG activation using a cell-free experimental system. Different concentrations of scUPA were added to a constant 1 nM of PLG and S2251 chromogenic substrate (0.4 mM) to detect PLS activity. S2251 served both to monitor the activity of PLS and as a high-affinity substrate for PLS, because S2251 would compete with scUPA for the active site of PLS. PLS activity was monitored over time until a steady state was reached (in ~4 h; Fig. S2). During the experiment, constant exogenous additions of small quantities of PLG and scUPA were provided to reproduce constant production. PLS steady-state curves (Fig. 5 A) in response to varying initial concentrations of scUPA yielded a sigmoidal curve (Hill coefficient \( n_H = 1.3 \)), demonstrating cooperative behavior.

The above results, however, do not indicate bistability. The presence of hysteresis would be more affirmative evidence for bistability of the system (34). For hysteresis, the system must exhibit two different steady states depending on the initial concentrations, without requiring any alteration of the rates (including synthesis/degradation). The experiment to test hysteresis was performed with two different initial states: one with a low initial concentration of PLS and one with higher PLS. To set up the state with low PLS, we used a 60:40 ratio of PLG/PLS, and for the state with high PLS, we used a 40:60 ratio of PLG/PLS. In other words, the same amount of total PLG/PLS protein was provided to both cases and only the initial extent of PLG/PLS activation was varied. Each of these states was then given a variable dose of scUPA (1–7 nM) and PLS activity was followed. Note that the S2251 chromogenic substrate was present to enable detection of PLS activity, but it also served as a potential source of substrate competition. For very low amounts of added scUPA, PLS reached the same steady-state level, with minimal activation, irrespective of whether we started from a high (60:40 ratio) or low (40:60 ratio) PLS initial condition. Similarly, for very high amounts of initial scUPA, PLS reached high steady-state levels irrespective of the initial PLG/PLS ratio. However, for an intermediate concentration between 2 nM and 7 nM of initial scUPA levels, PLS converged to two different steady states depending on its initial concentration (Fig. 5 B). For example, at 2 nM of scUPA stimulus, the experimental setup of high PLG (i.e., 60:40 ratio) had low PLS and remained at the lower steady state, whereas for the same initial stimulus of 2nM scUPA, the experimental setup with higher initial PLS (i.e., 40:60 ratio) achieved the high steady state of activation. The cell-free experiments therefore demonstrate that scUPA-mediated activation of PLS from PLG is bistable.

Sensitivity and robustness analyses

The parameters used for model construction (Fig. 4 A) were assembled from different literature sources and therefore should be considered highly approximate. Fig. 6 A is a two-parameter bifurcation diagram that characterizes the robustness of model bistability with respect to variation in the parameters \( k_1 \) (substrate binding) and \( \text{keff}_{\text{PLS}} \) (PLS efficiency). The shaded region inside the cusp represents models with bistability, and the boundary lines represent SN bifurcations. We next generated 100 random parameter sets with \( \pm 20\% \) to \( \pm 50\% \) variation from the 13 nominal parameters in Table 2 (see Materials and Methods). For each parameter vector, bistability was tested with the “going-up” and “coming-down” simulations (28). Fig. 6 B shows the percent bistability, i.e., the proportion of parameter sets that are capable of bistability when all parameters are varied. There is only a threefold decrease in percent bistability when parameters are varied from \( \pm 20\% \) to \( \pm 40\% \) of the nominal
values. Figure S3 shows that not much change in the steady states of species occurs when the parameters are varied, i.e., there is a constant change of 0.04 μM in PLS concentrations between the high and low steady-state values. Fig. 6 C shows the percent bistability for individual parameters when the ± 20% (black bars) and ± 50% (gray bars) parameter variations are compared. The parameters of production and degradation seem to influence bistability more so than other parameters, as the percent bistability decreases three-to fourfold when these parameters are varied.

DISCUSSION

In this work we used computational methods to analyze a system of UPA-mediated PLS activation. PLS is secreted as an inactive precursor and is activated by UPA as part of a positive feedback loop. Biological intuition suggests the existence of a system behavior in which both proteases are off, and another configuration of the system with both proteases strongly activated; however, the transitions and dynamic properties require quantitative analysis.

We built two computational models of the system. The first is an empirical representation of cooperativity in the form of a Hill coefficient for the kinetics of PLS (Fig. 2). The Hill coefficient could account for a wide range of simultaneous substrates with different affinities. The second computational model (Fig. 4) shows explicit substrate competition for a single anonymous competing substrate with hypothetical affinity. Using this pair of models gives us insight into a global effect that includes a vast number of PLS substrates in a true biological system.

Cooperativity and positive feedback are accepted preconditions for the occurrence of bistability and hysteresis in a system (18,35). Lijnen et al. (33) remarked on the existence of positive feedback between PLS and UPA, and we used modeling and experiments to test whether cooperativity and bistability are also present. Model dynamics for a protease system require degradation and production because the constituent reactions are irreversible cleavage effects. Because a system with cleavage enzymatic reactions alone would inevitably tend toward a state of cleavage, synthesis of precursor proteins is required for the existence of any nontrivial equilibrium. Therefore, in the parallel experiments, we introduced exogenous uncleaved proteins at small constant rates to mimic continuous processes in vivo.

When different initial conditions (different initial activation levels of PLS) were used for the dose response to scUPA, we observed experimentally that the system could exhibit two different steady states, and hysteresis was verified. In our cell-free assay of PLS activation with different doses of UPA, we observed a sigmoidal activation response in the presence of the high-affinity S2251 chromogenic reagent for measuring PLS activity. S2251 is a substrate for PLS, and it can be presumed to occupy the active site, in competition with UPA. Competition between substrates was recently found to create cooperativity as an emergent
property of a system (25) even in the absence of allosteric cooperativity. Our experiments validate that a small change in scUPA concentration can indeed cause large absolute changes in PLS activity, with an empirical behavior of cooperativity and ultrasensitivity in the system. The PLS concentrations that show bistability in simulations (0.03–0.05 μM) would be reasonable in vivo because the total pool of PLS plus PLG was previously measured to be 0.5–2 μM (37–40). The level of scUPA needed to cause a state transition in simulations (0.7 μM) is significantly above the empirical range of 0.1 nM to 0.1 μM measured for total urokinase (tcUPA plus scUPA) (41–44). Many factors could be responsible for the difference between simulated and measured urokinase values, including the greater activity of tcUPA compared with scUPA, different tissue types, and different measurement methods.

Using a Hill coefficient $ci$ to capture various possible sources of cooperativity, we analyzed the contributions of cooperativity and positive feedback to creating bistability (Fig. 3). For example, increasing the feedback strength in the model by increasing the $keff_{pos}$ parameter caused an increased area of bistability. Of interest, increasing the $keff_{pos}$ parameter also requires an increase in the $ci$ cooperativity parameter to maintain bistability.

The robustness analysis showed that bistability was robust to a significant range of parameter perturbations but sensitive to the production, degradation, and binding rate of the competing substrate $X$. Certainly the sensitivity to substrate $X$ affinity is understandable, because a low-affinity substrate would not sequester PLS away from scUPA. The turnover of substrate $X$ may initially seem far removed from the essence of UPA-PLS activation, but this turnover is important for determining how strong the PLS activity must be before PLS can escape the suppressive effects of sequestration, either through abundance of the PLS (out-numbering the substrate $X$ stoichiometrically) or through catalytic efficiency (consuming the substrate $X$ faster than it gets produced). The synthesis and degradation of substrate $X$ regulate the threshold level at which PLS becomes cooperative because they determine the initial abundance of $X$ and the rate at which enzymatic consumption of $X$ is replenished.

Because the inclusion of competing substrates made the system more cooperative, it is possible that many competing substrates in a physiological context would reinforce the PLS cooperativity rather than dilute it. It is difficult to discuss steady states in a physiological context; however, certain stable and self-perpetuating modes of behavior in vivo are analogous to stable steady states. Ultrasensitive transitions between self-perpetuating modes of behavior would be in vivo analogs of bistability. Our discovery that PLS and UPA can be bistable could have important ramifications for the systems in which they participate, including angiogenesis, tumor metastasis, wound healing, and fibrosis. In other bistable signaling pathways, such as apoptosis or cell cycle control, bistability permits a variety of input stimuli to be integrated into a single coordinated decision (18,45). It is interesting to speculate that the bistability of PLS and UPA might facilitate the switch-like decision of angiogenesis (46). The process of growing new blood vessels is tightly regulated by a variety of factors and occurs through an unknown switch-like decision. Because UPA and PLS are involved in various aspects of angiogenesis, such as activation of pro-angiogenic growth factors and increased degradation of interstitial matrix, these proteins are well positioned to play a coordinating role in the decisions of angiogenesis (46,47).

A bistable switch for UPA-PLS would also be useful for regulating the tight balance between inflammation and remodeling, which is needed for proper wound healing (4). The proposed switch might also have implications for healthy cell migration and pathological cell invasion, because cell motility involves coordination of proteases and other extracellular factors to remodel the ECM. PLS and UPA can act directly on the ECM (47), and also indirectly by activating many members of the canonical ECM-regulating family, the MMPs. Finally, it is important to note that bistability implies an important negative consequence, namely, that UPA and PLS would be relatively insensitive to perturbations when they are not near the ultrasensitive threshold. This negative insight may be helpful for understanding why the wound-healing response fails to switch off in fibroproliferative diseases. The bistability of the UPA/PLS subsystem may have far-reaching consequences that should be investigated in future work.

SUPPORTING MATERIAL
Two figures and a table are available at http://www.biophysj.org/biophysj supplemental/S0006-3495(11)01067-8.

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