VERY LOW MASS STELLAR AND SUBSTELLAR COMPANIONS TO SOLAR-LIKE STARS FROM MARVELS. I. A LOW-MASS RATIO STELLAR COMPANION TO TYC

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VERY LOW MASS STELLAR AND SUBSTELLAR COMPANIONS TO SOLAR-LIKE STARS FROM MARVELS.
I. A LOW-MASS RATIO STELLAR COMPANION TO TYC 4110-01037-1 IN A 79 DAY ORBIT

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ABSTRACT

TYC 4110-01037-1 has a low-mass stellar companion, whose small mass ratio and short orbital period are atypical among binary systems with solar-like \( T_{\text{eff}} \approx 6000 \) K primary stars. Our analysis of TYC 4110-01037-1 reveals it to be a moderately aged \((\lesssim 5 \text{ Gyr})\) solar-like star having a mass of \( 1.07 \pm 0.08 \, M_\odot \) and radius of \( 0.99 \pm 0.18 \, R_\odot \). We analyze 32 radial velocity (RV) measurements from the SDSS-III MARVELS survey as well as 6 supporting RV measurements from the SARG spectrograph on the 3.6 m Telescopio Nazionale Galileo telescope obtained over a period of \( \approx 2 \) years. The best Keplerian orbital fit parameters were found to have a period of \( 78.994 \pm 0.002 \) days, an eccentricity of \( 0.1095 \pm 0.012 \), and a semi-amplitude of \( 4199 \pm 5.8 \, \text{m} \, \text{s}^{-1} \). We determine the minimum companion mass (if \( \sin i = 1 \)) to be \( 97.7 \pm 5.8 \, M_{\text{Jup}} \). The system’s companion to host star mass ratio, \( q \approx 0.087 \pm 0.003 \), places it at the lowest end of observed values for short period stellar companions to solar-like \( T_{\text{eff}} \approx 6000 \) K stars. One possible way to create such a system would be if a triple-component stellar multiple broke up into a short period, low \( q \) binary during the cluster dispersal phase of its lifetime. A candidate tertiary body has been identified in the system via single-epoch, high contrast imagery. If this object is confirmed to be comoving, we estimate it would be a \( \text{dM}4 \) star. We present these results in the context of our larger-scale effort to constrain the statistics of low-mass stellar and brown dwarf companions to FGK-type stars via the MARVELS survey.

Key words: binaries: general – stars: individual (TYC 4110-01037-1) – stars: low mass

Online-only material: color figures

1. INTRODUCTION

Observations of the mass distribution of substellar and low-mass stars as a function of orbital separation, using a variety of techniques, provide key constraints which influence our understanding of the process of planetary and star formation (Burgasser et al. 2007; Stamatellos & Whitworth 2009; Kraus et al. 2011; Sahlmann et al. 2011). Early results from the Kepler transit search program, which is sensitive to short to moderate period companions, show the size distribution of candidate companions increases toward smaller planets, reaching a maximum at a few \( R_\oplus \) (Borucki et al. 2011a, 2011b). Numerous large radial velocity (RV) surveys are constraining the prevalence of Jovian-mass giant planets at close and intermediate orbital separations (e.g., California & Carnegie teams, Marcy & Butler 2000; AAPS, Tinney et al. 2001; CORALIE, Udry et al. 2000; HARPS, Mayor et al. 2004) and the prevalence of brown dwarf (BD) and very low mass stellar companions at close and intermediate separations (Marcy & Butler 2000; Mayor et al. 2001; Vogt et al. 2002; Patel et al. 2007; Lee et al. 2011). At much...
larger orbital separations, high contrast imaging surveys inform our understanding of the mass distribution of planets (Kalas et al. 2008; Marois et al. 2008, 2010; Lagrange et al. 2010) and BDs (Thalmann et al. 2009; Biller et al. 2010; Janson et al. 2011; Wahhaj et al. 2011), while the mass distribution of very low mass stellar companions has been explored by high contrast imaging (Kraus et al. 2011), spectroscopic (Duquennoy & Mayor 1991), and interferometric (Raghavan et al. 2010) studies.

Many of the results from these surveys have found interesting, and at times conflicting, trends motivating subsequent programs to investigate their origin. In the BD regime, a deficit of short period \((a \lesssim 5 \text{ AU})\) companions to solar-type primary stars has long been designated the apparent “brown dwarf desert” (Marcy & Butler 2000). Investigations of the BD frequency at larger orbital separations (e.g., Gizis et al. 2001; Metchev & Hillenbrand 2004; McCarthy & Zuckerman 2004; Carson et al. 2005; Metchev & Hillenbrand 2009; Kraus et al. 2011) have led to conflicting assertions as to whether the BD desert extends to larger orbital separations. Multiplicity studies of low-mass stellar companions to solar-like stars have found evidence of a unimodal period distribution with peak periods ranging from \(\sim 180 \text{ years} \) (Duquennoy & Mayor 1991) to \(\sim 300 \text{ years} \) (Raghavan et al. 2010). Interestingly, recent work by Metchev & Hillenbrand (2009) has presented tentative evidence that the companion mass function of BD and low-mass stellar companions around solar-like stars could be represented by a universal function.

At the short-period \((P < 100 \text{ days})\) tail of solar-like \((T_{\text{eff}} \lesssim 6000 \text{ K})\) multiplicity investigations, many studies have reported a paucity of confirmed low-mass stellar or BD companions with mass ratios \((q \equiv M_2/M_1) < 0.2\) (see, e.g., Pont et al. 2005; Bouchy et al. 2011), leading Raghavan et al. (2010) to suggest that short period companions to solar-like stars prefer higher mass ratios, although there is disagreement in the literature regarding this trend (see, e.g., Halbwachs et al. 2003). Burgasser et al. (2007) suggest that the short-period BD desert seems to extend into the M dwarf regime. Raghavan et al. (2010) also note that the majority of the companions surrounding solar-like stars with periods <100 days are triple systems, and thus potentially indicative that such systems experienced orbital migration (Bate et al. 2002). Short-period low-mass ratio binaries are much more commonly observed around slightly more massive F-type stars (Bouchy et al. 2005; Pont et al. 2006; Beatty et al. 2007; Bouchy et al. 2011). Bouchy et al. (2011) have suggested that low \(q\) companions can form at or migrate to short orbital periods around a wide range of stellar primary masses, but suggest that they may not survive around G dwarfs and lesser mass primary stars.

The Multi-object APO Radial Velocity Exoplanet Large-area Survey (MARVELS), one of the three surveys being executed during the Sloan Digital Sky Survey (SDSS) III (Eisenstein et al. 2011), is a four-year program which is monitoring the radial velocities of \(\sim 3300 \text{ V} = 7.6–12 \text{ FGK-type dwarfs and subgiants. As described in Lee et al. (2011), the target selection strategy attempts to impose minimal and well-understood biases on targets’ ages and metallicities; hence, the survey provides an ideal, statistically robust means to explore the mass distribution of substellar and very low mass star companions over orbital periods of \(\leq 2 \text{ years} \) from a relatively low-biased target sample. In anticipation of a statistical analysis of global trends in the population of BDs and low-mass binary companions identified by the survey, we are performing detailed and careful characterization of the fundamental parameters of these companions and their host stars (see, e.g., Fleming et al. 2012, in preparation, discussion of MARVELS-2b). The first paper in this series was Lee et al. (2011), which presented an analysis of a short period BD surrounding the F9 star TYC 1240-00945-1. Analogous detailed characterization of individual systems has been shown to be particularly important in refining the radii of Kepler candidate planet-candidates to be more Earth-like than assumed (Muirhead et al. 2011). The advantages of meta-analyzing such well-characterized systems is also demonstrated in Bouchy et al. (2011), who were able to begin to explore the mass–radius relationship from the planetary to BD to very low mass star regimes as well as the mass ratio of companions as a function of primary mass.

In this paper, we present a detailed analysis of the fundamental properties of the solar-like star TYC 4110-01037-1 (hereafter TYC 4110) and report the discovery of a very low mass stellar companion associated with the system. In Section 2, we describe the spectroscopic and photometric data which were used for this analysis. We determine accurate fundamental stellar parameters for the star in Section 3 and describe the basic properties of the very low mass stellar companion in Section 4. We also discuss the detection of a candidate tertiary companion system in Section 4. Finally, we discuss the implications of these results in Section 5.

2. OBSERVATIONS AND DATA REDUCTION

2.1. SDSS-III Radial Velocity Data

Our primary RV observations of TYC 4110 were obtained during the first two years of the SDSS-III MARVELS survey, which uses a dispersed fixed-delay interferometer (Ge et al. 2009) on the SDSS 2.5 m telescope (Gunn et al. 2006). A total of 32 observations were obtained over the course of \(\sim 2 \text{ years} \). Each 50 minute observation yielded two fringing spectra (aka. “beams”) from the interferometer spanning the wavelength regime \(\sim 500–570 \text{ nm} \) with \(R \sim 12,000 \) (Lee et al. 2011) describe the basic data reduction and analysis leading to the production of differential RVs for each beam of the interferometer. We combined these beams for each observation set using a weighted mean. As described in Fleming et al. (2010), we scaled up the RV errors by a “quality factor” \((Q = 5.67 \text{ for TYC 4110})\) based on the rms errors of the other stars observed on the same SDSS-III plate as TYC 4110.

A summary of the relative amplitude RV measurements obtained for TYC 4110 with MARVELS is presented in Table 1.

2.2. TNG Follow-up Radial Velocity Data

Supporting RV observations were obtained with the 3.6 m Telescopio Nazionale Galileo (TNG) using its SARG spectrograph (Gratton et al. 2001). The 0′8 × 5′3 slit provided \(R \sim 57,000 \) spectroscopy between 462–792 nm. We obtained six spectra with an iodine cell (IC), to provide high precision radial velocities (Table 1), and one without the IC to serve as a stellar template. The data were reduced using standard IRAF routines and RVs were measured using the IC technique (Marcy & Butler 2000). Each of 21 SARG spectral orders between 504 and 611 nm were divided in 10 pieces, and RV calculations were derived from each of the 210 resulting pieces. Based on a goodness-of-fit indicator, the best 158 (75%) pieces were selected. Following a 2\(\sigma\) clip, the remaining RV measurements were combined with a weighted average to produce the RV measurements quoted in Table 1.
Two spectra were obtained using the default accurate characterization of stellar fundamental parameters. The with the Apache Point Observatory 3.5 m telescope and ARC 4110 were obtained on UT 2010 September 29 (HJD 2455468)

<table>
<thead>
<tr>
<th>HJD</th>
<th>Instrument</th>
<th>RV (km s(^{-1}))</th>
<th>(\sigma_{RV}) (km s(^{-1}))</th>
</tr>
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<tr>
<td>2454811.815473</td>
<td>M</td>
<td>−2.869</td>
<td>0.053</td>
</tr>
<tr>
<td>2454812.936774</td>
<td>M</td>
<td>−2.386</td>
<td>0.049</td>
</tr>
<tr>
<td>2454816.915562</td>
<td>M</td>
<td>−0.841</td>
<td>0.060</td>
</tr>
<tr>
<td>2454840.868516</td>
<td>M</td>
<td>3.859</td>
<td>0.046</td>
</tr>
<tr>
<td>2454842.900506</td>
<td>M</td>
<td>3.614</td>
<td>0.093</td>
</tr>
<tr>
<td>2454843.814123</td>
<td>M</td>
<td>3.496</td>
<td>0.057</td>
</tr>
<tr>
<td>2454844.776592</td>
<td>M</td>
<td>3.342</td>
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</tr>
<tr>
<td>2454845.778936</td>
<td>M</td>
<td>3.153</td>
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</tr>
<tr>
<td>2454867.724621</td>
<td>M</td>
<td>−2.229</td>
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<tr>
<td>2454868.791455</td>
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<tr>
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<td>−2.786</td>
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<tr>
<td>2454901.671359</td>
<td>M</td>
<td>1.393</td>
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<tr>
<td>2455105.974063</td>
<td>M</td>
<td>−2.454</td>
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<tr>
<td>2455135.969729</td>
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<td>0.417</td>
<td>0.039</td>
</tr>
<tr>
<td>2455141.825627</td>
<td>M</td>
<td>2.508</td>
<td>0.045</td>
</tr>
<tr>
<td>2455142.892315</td>
<td>M</td>
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<td>0.060</td>
</tr>
<tr>
<td>2455143.904775</td>
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<td>0.058</td>
</tr>
<tr>
<td>2455144.904270</td>
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<td>3.187</td>
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</tr>
<tr>
<td>2455161.844226</td>
<td>M</td>
<td>3.115</td>
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</tr>
<tr>
<td>2455199.808399</td>
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</tr>
<tr>
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<tr>
<td>2455206.657591</td>
<td>M</td>
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</tr>
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</tr>
<tr>
<td>2455472.000492</td>
<td>M</td>
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</tr>
<tr>
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<td>M</td>
<td>−1.744</td>
<td>0.066</td>
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<td>0.059</td>
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<tr>
<td>2455516.846851</td>
<td>S</td>
<td>−4.209</td>
<td>0.061</td>
</tr>
<tr>
<td>2455516.579785</td>
<td>S</td>
<td>−4.118</td>
<td>0.033</td>
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<tr>
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<td>M</td>
<td>3.798</td>
<td>0.049</td>
</tr>
<tr>
<td>2455545.783002</td>
<td>M</td>
<td>4.117</td>
<td>0.053</td>
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<td>3.175</td>
<td>0.076</td>
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<td>0.034</td>
</tr>
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<td>S</td>
<td>−4.051</td>
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<tr>
<td>2455698.384891</td>
<td>S</td>
<td>3.375</td>
<td>0.041</td>
</tr>
</tbody>
</table>

Notes. A summary of relative radial velocities obtained with the MARVELS (M) and SARG (S) spectrographs. The quoted \(\sigma_{RV}\) errors for the MARVELS data were first uniformly scaled by a “quality factor” \(Q = 5.67\) (see Fleming et al. 2010), based on the rms of the other stars observed on the same SDSS-III plate. As described in Section 4, the errors of the MARVELS and SARG data were then re-scaled to force our RV fits to have \(P(\chi^2) = 0.5\), in an iterative manner. Note that zero point offsets have been applied to the RVs compiled in column 3 to force the RVs to vary about 0 m s\(^{-1}\).

2.3. APO Spectroscopic Data

Two \(R \sim 31,500\) optical (\(\sim 3600–10000 \text{Å}\)) spectra of TYC 4110 were obtained on UT 2010 September 29 (HJD 2455468) with the Apache Point Observatory 3.5 m telescope and ARC Echelle Spectrograph (ARCES; Wang et al. 2003) to enable accurate characterization of stellar fundamental parameters. The two spectra were obtained using the default 1′6 × 3′2 slit and an exposure time of 1200 s. A ThAr lamp exposure was obtained between these integrations to facilitate accurate wavelength calibration. The data were processed using standard IRAF techniques. Following heliocentric velocity corrections, each order was continuum normalized, and the resultant continuum normalized data from each observation were averaged. The final spectrum yielded a signal-to-noise ratio (S/N) of \(\sim 175\) at \(\sim 6500 \text{Å}\).

2.4. HAO Photometric Data

We obtained absolute photometry of TYC 4110 using the Hereford Arizona Observatory (HAO), a private facility in Southern Arizona (observatory code G95 in the IAU Minor Planet Center). HAO employs a 14 inch Meade LX200GPS telescope equipped with a SBIG ST-10XME CCD. Observations in \(B, V, L\) filters were made on 2011 January 15 and 2011 February 10. A total of 22 Landolt standard stars and 9 secondary standards based on Landolt star fields SA98 and SA114 (Landolt 1992) were observed at several airmass values similar to the airmass for TYC 4110. The target’s magnitude was calculated by

\[
M_f = M_{f0} - 2.5 \log_{10}(F_f / g) - (K_f' - m) + (S_f' - C),
\]

where \(M_f\) is the magnitude for each filter \(f\), \(M_0\) is a constant determined from the standard stars, \(F_f\) is star flux using a large photometry aperture, \(g\) is exposure time, \(K_f'\) is zenith extinction coefficient for each filter, \(m\) is air mass, \(S_f\) is the star color sensitivity (determined from the standard stars), and \(C\) is star color \((B-V)\). Solutions for \((B-V)\) were obtained by iterating \(V\) and \(B\) magnitudes from initial values 2–3 times. The resultant absolute photometry for TYC 4110 is summarized in Table 2.
evidence of variability (error-weighted rms $\sim 0.675\%$) over the
timescales sampled by these data. For example, a linear fit to the
entire data set yields negligible variation in flux with a best-fit
slope of $0.040\% \pm 0.030\%$ day$^{-1}$. We also detect no evidence of
a transit. We do caution however that the sampling of these
data is sparse.

3. TYC 4110-01037-1: THE STAR

3.1. Fundamental Stellar Properties

We analyzed moderate resolution spectroscopic data from the
ARCES spectrograph using two separate analysis techniques to
extract fundamental stellar parameters for TYC 4110. We
refer to these different pipeline results as the “IAC” (Instituto
de Astrofísica de Canarias) and “BPG” (Brazilian Participation
Group) results, as described below.

3.1.1. “IAC” Analysis

We derive equivalent widths (EWs) of Fe $\text{i}$ and Fe $\text{ii}$ lines with the
code StePar (Tabernero et al. 2012). This code employs the
2002 version of the MOOG code (Sneden 1973), and a grid of
Kurucz ATLAS9 plane-parallel model atmospheres (Kurucz
1993). StePar iterates until the slopes of $A(\text{Fe} \text{i})$ versus $\chi$ and
$A(\text{Fe} \text{ii})$ versus log(EW $\lambda^{-1}$) are equal to zero, while imposing
the ionization equilibrium condition $A(\text{Fe} \text{i}) = A(\text{Fe} \text{ii})$. A $2\sigma$
rejection of the EWs of Fe $\text{i}$ and Fe $\text{ii}$ lines is performed after a
first determination of the stellar parameters, and then the StePar
program is re-run without the rejected lines (see Tabernero et al.
2012 for further details).

For the ARCES spectrum of TYC 4110, 198 Fe $\text{i}$ lines and 24
Fe $\text{ii}$ lines remain after clipping. These are used to derive $T_{\text{eff}} = 5879 \pm 25$ K, $\log (g) = 4.53 \pm 0.18$, $\text{[Fe/H]} = -0.02 \pm 0.05$, and $v_{\text{micro}} = 0.932 \pm 0.038$ km s$^{-1}$.

Internal uncertainties were also derived for each stellar
parameter. The uncertainty of $v_{\text{micro}}$ was obtained by varying
this parameter until the slope of the linear regression of $A(\text{Fe} \text{i})$
versus log(EW $\lambda^{-1}$) was equal to its standard deviation. The
uncertainty of $T_{\text{eff}}$ was determined by changing this parameter
until the slope of the linear regression of $A(\text{Fe} \text{i})$ versus $\chi$
equal to its standard deviation. The uncertainty of $v_{\text{micro}}$ was also
taken into account when calculating the uncertainty of $T_{\text{eff}}$.
The uncertainty of $\log (g)$ was obtained by varying this parameter
until the difference between the mean abundances from Fe $\text{i}$
and Fe $\text{ii}$ were equal to the standard deviation of the latter. The
contributions from $T_{\text{eff}}$ and $v_{\text{micro}}$ were included. Finally, the
uncertainty of $\text{[Fe/H]}$ is a combination of the standard deviation
of the Fe $\text{i}$ abundance and the variations caused by the errors in
$T_{\text{eff}}$, $\log (g)$, and $\xi_i$, all added in quadrature.

3.1.2. “BPG” Analysis

We assume LTE and use the 2002 version of MOOG (Sneden
1973), along with the one-dimensional plane-parallel model
atmospheres interpolated from the ODFNEW grid of ATLAS9
models (Castelli & Kurucz 2004). Initially, a list of $\sim 150$
isolated and moderately strong (i.e., $5 < \text{EW} < 120$ mA) Fe $\text{i}$
and Fe $\text{ii}$ lines was compiled using the Solar Flux Atlas (Kurucz
et al. 1984), the Utrecht spectral line compilation (Moore et al.
1966), and a Ganymede ARCES spectrum with $S/N = 400$. The
values for the central wavelengths and line excitation potentials
were taken from the Vienna Atomic Line Database (Kupka et al.
1999). We also multiplied the van der Waals damping parameter
“C6” by a factor of two, following Holweger et al. (1991).

The EWs of these lines were automatically measured in the
solar spectrum from fits of Gaussian profiles using the task
$hplot$ in IRAF. The quality of the measurements was checked
by performing two tests. First, since the line depth is expected
to be a linear function of the reduced EW (EW $\lambda^{-1}$) for
non-saturated lines, we eliminated lines that did not follow a linear
relation, using a $2\sigma$ clipping. The second test is based on the
fact that the shapes of the lines are essentially determined by
the instrumental profile at the APO resolution ($\sim 31,500$). Since
the resolution is approximately constant over the entire spec-
trum, we expect the quantity FWHM/ $\lambda^{-1}$ to be approximately
constant for lines of the same species. We therefore perform
a linear fit to this relation and eliminate lines that exhibit $2\sigma$
deviations.

After these tests, the final solar line list contained 91 Fe $\text{i}$ and
11 Fe $\text{ii}$ lines. Solar $gf$ values were derived for all these lines
using a solar model atmosphere with the following parameters:

$T_{\text{eff}} = 5777$ K, $\log (g) = 4.44$, $\text{[Fe/H]} = 0.0$, and $v_{\text{micro}} = 1.0$ km s$^{-1}$. The adopted solar abundance for iron is $A(\text{Fe}) = 7.50$ (Asplund et al.
2009).

EWs for 102 Fe lines were measured in the TYC 4110 APO
spectrum and checked with the tests described above. $T_{\text{eff}}$ and
$v_{\text{micro}}$ were iterated until zero slopes were found in the plots
of $A(\text{Fe} \text{i})$ versus $\chi$ and log (EW $\lambda^{-1}$), respectively; i.e., until the
individual Fe line abundances were independent of excitation
potential and reduced EWs. The surface gravity was iterated
until $A(\text{Fe} \text{i}) = A(\text{Fe} \text{ii})$, i.e., until the same average abundances
were given by Fe $\text{i}$ and Fe $\text{ii}$ lines. At the end of this iterative
process, a consistent set of atmospheric parameters ($T_{\text{eff}}$, $\log (g)$,
$\text{[Fe/H]}$, and $v_{\text{micro}}$) was obtained for the star. Note that the
metallicity is simply given by $\text{[Fe/H]} = A(\text{Fe}) - 7.50$, where
7.50 is the solar iron abundance taken from Asplund et al.
(2009). At this point, any lines with abundances that deviated more than $2\sigma$ from the average were removed and the above iteration
was repeated until convergence was achieved.

We derive $T_{\text{eff}} = 5878 \pm 49$ K, $\log (g) = 4.43 \pm 0.17$,
$\text{[Fe/H]} = 0.00 \pm 0.06$, and $v_{\text{micro}} = 1.00 \pm 0.08$ km s$^{-1}$ based
on the ARCES spectrum. The final line list after rejections
contained 60 Fe $\text{i}$ and 8 Fe $\text{ii}$ lines. The internal uncertainties
are calculated in the same way as the “IAC” analysis above.

3.1.3. Final Stellar Parameters

We determined the mean values for $T_{\text{eff}}$, $\log (g)$, $\text{[Fe/H]}$, and
$v_{\text{micro}}$ by combining the results from the IAC and BPG analyses
via a mean, weighted by the inverse of the internal variances.
For each parameter, we add in quadrature a systematic error of
18 K, 0.08, 0.03, and 0.02 km s$^{-1}$ for $T_{\text{eff}}$, $\log (g)$, $\text{[Fe/H]}$, and
$v_{\text{micro}}$, respectively. These systematic errors are calculated based
on the weighted standard deviation of the weighted means of
each parameter using 18 spectra of 13 stars (seven MARVELS
targets and six stars with well-known atmospheric parameters).
These stars span $T_{\text{eff}}$ from 5200–6500 K, $\log (g)$ from 4.0 to 4.7,
$\text{[Fe/H]}$ from $-0.5$ to +0.5 and $v_{\text{micro}}$ from 0.3 to 1.8 km s$^{-1}$. The
final stellar parameters are $T_{\text{eff}} = 5879 \pm 29$ K, $\log g = 4.48 \pm$
Bottom: by constraining stellar parameters determined from analysis of moderate resolution spectra. We also fit these SED data by constraining the fundamental stellar parameters from this fit agreed to within 1σ. Using this A_V, we estimate the distance to TYC 4110-01037-1 to be 125.1 ± 4.6 pc.

(A color version of this figure is available in the online journal.)

Figure 2. Observed stellar parameters for TYC 4110-01037-1 (red data) are compared to a Yonsei-Yale stellar evolutionary track (Demarque et al. 2004) evolutionary track for an M_* = 1.07 M_⊙ star with [Fe/H] = −0.01. Ages of 1.0, 2.0, 5.0, and 6.0 are indicated in blue, and 1σ deviations in the evolutionary track are shown in the shaded region.

(A color version of this figure is available in the online journal.)

0.15, [Fe/H] = −0.01 ± 0.05, and v_micro = 0.94 ± 0.04 km s⁻¹ (Table 2).

To check these parameters using a different observational technique, we constructed a spectral energy distribution (SED) for TYC 4110, using the near UV to Two Micron All Sky Survey (Cutri et al. 2003) and WISE (Wright et al. 2010) IR photometry compiled in Table 2 (see Figure 1). These data were fit with a NextGen model atmosphere (Hauschildt et al. 1999), and we limited the maximum line-of-sight extinction to be A_V = <0.28 from analysis of dust maps from Schlegel et al. (1998). The resultant parameters, T_eff = 6000 ± 200 K, log g = 4.0 ± 1.0, [Fe/H] = 0.0 ± 0.3, and A_V = 0.20 ± 0.08, all agree to within 1σ of the results found via analysis of our moderate resolution spectroscopy. We also fit these SED data by constraining the T_eff and log g values to those derived from our spectroscopic analysis. The resultant fit (reduced \( \chi^2 \) = 2.62; see panel (b) of Figure 1) provides a more robust estimate of A_V, 0.16 ± 0.04. Using this total extinction estimate, and adopting a BCV of −0.19 ± 0.02 (Cox 2000), we estimate the distance to TYC 4110 to be 125.1 ± 4.6 pc (Table 2).

3.2. Stellar Mass and Radius

Using the spectroscopically determined values of T_eff, log g, and [Fe/H] (Table 2), we determined the mass and radius of TYC 4110 using the empirical Torres et al. (2010) relationship. We find M_* = 1.07 ± 0.08 M_⊙ and R_* = 0.99 ± 0.18 R_⊙ (Table 2). Our quoted errors include contributions from the uncertainties in our fundamental stellar parameters, as well as the scatter in the Torres et al. (2010) relationship (σ_M = 0.027 and σ_R = 0.014) and correlations of the best-fit coefficients from Torres et al. (2010) added in quadrature. We did not include covariances between T_eff, log g, and [Fe/H] in this error analysis; however, our final quoted uncertainties for these values do include a systematic error term that conservatively encapsulates any covariance between these parameters. We did however perform a Monte Carlo simulation of our spectroscopically determined stellar parameters and the Torres et al. (2010) relations, and found a stellar mass and radius consistent with the aforementioned values.

3.3. Evolutionary State

We assess the evolutionary state of TYC 4110 by comparing its spectroscopically measured fundamental stellar parameters against a Yonsei–Yale stellar evolutionary track (Demarque et al. 2004) for an M_* = 1.07 M_⊙ star having [Fe/H] = −0.01. This is done in Figure 2, where the shaded region depicts deviations in the evolutionary track which would be expected from a 1σ (0.08 M_⊙) change in the assumed stellar mass, while circles denote different time stamps in the track. TYC 4110 lies near a predicted age of \( \lesssim 5 \) Gyr in Figure 2; we therefore conclude that it is a main-sequence dwarf star. The lack of any detectable Ca ii H and K emission in our ARCES spectra (log(RHK) \( \sim -5.1 \)) indicates the star is relatively inactive, and thus qualitatively consistent with the evolutionary state we derive.

3.4. Systemic and Rotational Velocity

We computed the absolute RV of TYC 4110 by cross-correlating the six epochs of SARG spectra against a solar spectrum. After removing the RV contribution at each epoch induced by the presence of TYC 4110’s companion (Table 1), we determine the systemic velocity of TYC 4110, \( v_{\text{systemic}} \), to
be $25.9 \pm 0.2$ km s$^{-1}$ (Table 2). We also compared these SARG data to broadened versions of Kurucz ATLAS synthetic spectra to constrain the rotational velocity, $v_{\text{rot}} \sin i$, of TYC 4110. After considering a range of macroturbulence values, we find $v_{\text{rot}} \sin i \lesssim 3$ km s$^{-1}$, which is slightly below the level of instrumental broadening present in these data ($\sim 5.3$ km s$^{-1}$).

4. TYC 4110-01037-1’S COMPANION

4.1. Binary Companion Detection

Analysis of post-pipeline processed MARVELS data involves searching for periodic behavior which is consistent with Keplerian orbital motion and filtering out “contaminant” RV signals which do not arise from the presence of a companion. One of the first steps in this process is to compute a Lomb–Scargle (LS) periodogram (Lomb 1976; Scargle 1982) and search for periodic signals which significantly exceed a conservative false alarm probability assessment. There have been several implementations of this method (Press & Rybicki 1989); we followed Cumming (2004) which uses the comparison of the $\chi^2$ values between a sinusoidal fit at a given frequency and a fit to the mean to generate the power term (see, e.g., Cumming’s Equation (2)). This form was chosen to be fully extensible by adding linear terms, harmonic terms, or even a fully Keplerian fit. We stepped through frequency space using steps and a search window as appropriate for our data sampling, as described in Press et al. (1992). In order to interpret the significance of this power spectrum, false alarm probabilities were calculated using the techniques in Baluev (2008).

Data from the current MARVELS pipeline have systematic effects present which can mimic a companion signal. We can significantly mitigate this issue by taking advantage of the fact that the MARVELS instrument observes 60 stars at a time. As a result, we can search for periodic signals from all stars on a given plate and use any detected signals to characterize systematics in our data. This is done by taking the sum of the power for each frequency across the entire plate. We then remove the highest power from each frequency (so that actual companions do not skew the average), excluding any power associated with the candidate companion, and compute the average.

Figure 3 indicates TYC 4110 exhibits a strong $\sim 79$ day period signal. The companion to TYC 4110, hereafter referred to as MARVELS-3B, does not match any strong periodic signature identified in the power spectrum of all stars located on the same SDSS-III plate (bottom panel; Figure 3), and is therefore not caused by any known systematic artifact in our instrument or reduction pipeline.

4.2. Radial Velocity Fits

Radial velocities derived from MARVELS and SARG data were fit with the EXOFAST code (J. Eastman et al. 2012, in preparation) to extract detailed Keplerian orbital parameters. We first performed an independent fit of the MARVELS data and re-scaled the MARVELS error bars to force the probability of $\chi^2$, $P(\chi^2) = 0.5$. Since we did not have enough SARG data points to perform an independent fit solely on these data, we then fit the combined (MARVELS + SARG) data, and re-scaled the SARG errors to force $P(\chi^2) = 0.5$. The fitting of the combined data set and re-scaling of the SARG errors were iterated until a convergent solution was achieved. The MARVELS and (MARVELS + SARG) data yielded consistent results to within $1\sigma$ of the fit errors. We also computed the $\chi^2$ of the SARG data about the MARVELS-only fit, and the resultant value ($\chi^2 = 8.47$ for 5 degrees of freedom) indicates such a fit would only happen by chance $\sim 13\%$ of the time. We hereafter only consider the combined MARVELS + SARG fit.

The raw MARVELS and SARG radial velocities were computed on independent, relative scales. We determined that the best offsets to simultaneously analyze these data about a zero point of $0$ m s$^{-1}$ were $1345 \pm 24$ m s$^{-1}$ (SARG) and $8583 \pm 12$ m s$^{-1}$ (MARVELS); the RVs quoted in Table 1 have had these offsets applied. The RV errors listed in Table 1 include the re-scaling factors described above. The inclusion of an additional linear term was explored in the fitting process, but there is no compelling evidence for an acceleration due to another companion, with a best-fit linear slope of $0.096^{+0.039}_{-0.040}$ m s$^{-1}$ day$^{-1}$ observed, corresponding to a $2.4\sigma$ deviation.

As seen in the full RV curve (Figure 4) and in the phase-folded curve (Figure 5), these data are described by a $78.994 \pm 0.012$ day period, a moderately elliptical ($e = 0.1095 \pm 0.0023$) orbit, and a semi-amplitude $K = 4199 \pm 11$ m/s. Full fit parameters for TYC 4110 are presented in Table 3. To search for evidence that MARVELS-3B was a transiting system, we computed an LS periodogram of the available SuperWASP photometry, but found no evidence of variability at the $\sim 79$ day period of MARVELS-3B above a level of $\sim 0.8\%$. 

![Figure 3. Periodogram for RV measurements of TYC 4110-01037-1 (panel a) indicates the strong presence of a $\sim 79$ day periodic signature, indicated by the dashed vertical line. This signal is not seen to coincide with any strong feature in the periodogram for all stars located on the same SDSS-III plate as this object (panel b), indicating it is not caused by a known artifact of our instrument or reduction pipeline.](image-url)
that TP (MγγTP(A color version of this figure is available in the online journal.) of conjunction.

Figure 4. Derived relative radial velocities from the MARVELS (blue squares) and SARG (red circles) spectrographs are overlayed with the best-fit orbital solution described in Section 4 and compiled in Table 3. Residuals to this fit are shown in the bottom panel. (A color version of this figure is available in the online journal.)

Table 3

Properties of MARVELS-3B

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>( T_C ) (BJD\text{TDH}−2,450,000)</td>
<td>5175.97 ± 0.14</td>
</tr>
<tr>
<td>( P ) (days)</td>
<td>78.994 ± 0.012</td>
</tr>
<tr>
<td>( e )</td>
<td>0.1095 ± 0.0023</td>
</tr>
<tr>
<td>( \omega ) (radians)</td>
<td>4.380 ± 0.041</td>
</tr>
<tr>
<td>( K ) (m s(^{-1}))</td>
<td>4199 ± 11</td>
</tr>
<tr>
<td>( \gamma_{\text{NC}} ) (m s(^{-1}))</td>
<td>1338 ± 19</td>
</tr>
<tr>
<td>( \gamma_{\text{APO}} ) (m s(^{-1}))</td>
<td>2945 ± 10</td>
</tr>
<tr>
<td>( \epsilon_{\cos \omega} )</td>
<td>−0.0357 ± 0.0042</td>
</tr>
<tr>
<td>( \epsilon_{\sin i} )</td>
<td>−0.1034 ± 0.0027</td>
</tr>
<tr>
<td>( T_P ) (BJD\text{TDH}−2,450,000)</td>
<td>5210.32 ± 0.50</td>
</tr>
<tr>
<td>( a ) (sin ( i ) = 1)</td>
<td>0.38 AU</td>
</tr>
<tr>
<td>( M ) (( M_{\oplus} ))</td>
<td>&gt;97.7 ± 5.8</td>
</tr>
</tbody>
</table>

Notes. A summary of some of the basic orbital properties of MARVELS-3B. The quoted minimum mass corresponds to the limiting case of \( i = 1 \). Note that \( T_P \) corresponds to the time of periastron while \( T_C \) corresponds to the time of conjunction.

We determined the mass for MARVELS-3B using

\[
\frac{(M_\star \sin i)^3}{(M_\star + M_\gamma)^2} = \frac{K^3(1 - e^2)^{3/2}P}{2\pi G} 
\]

and the fit parameters compiled in Table 3. This yields a minimum companion mass (if \( i = 1 \)) of 97.7 ± 5.8 \( M_{\oplus} \), which places MARVELS-3B slightly above the generally accepted BD upper mass limit of 80 \( M_{\oplus} \) and into the low-mass star regime. The minimum mass ratio, \( q \), of the companion to the primary is 0.087 ± 0.003.

4.3. Binary Companion Mass

The true mass of the companion depends on the inclination \( i \) of the orbit, which is unknown. However, we can estimate the posterior probability distribution of the true companion mass, given an isotropic distribution of orbits, and adopting a prior for the distribution of the companion mass ratios. We proceed to do this using a Monte Carlo method, following the methodology described in detail in Fleming et al. (2010) and Lee et al. (2011), which we briefly summarize here. We combine the posterior distribution of orbital parameters \( K, e, \) and \( P \) obtained from the Markov Chain Monte Carlo (MCMC) fit to the RV data, with an estimate of the joint distribution of the primary mass and radius obtained using the spectroscopically determined \( T_{\text{eff}}, \log g, \) and [Fe/H] combined with the Torres et al. (2010) relations, accounting for all sources of uncertainty in the measured values and the relations themselves. We draw values of \( \cos i \) from a uniform distribution. The values of \( K, e, \) and \( P \) determine the mass function \( (M_\star \sin i)^3/(M_\gamma + M_\star)^2 \), and then the value of \( i \) along with the primary mass \( M_\star \) determines \( M_\gamma \). Finally, we appropriately weight the resulting distribution of \( M_\gamma \) by our prior on the mass ratio \( q \).

As described in Section 1, the mass ratio of companions around G dwarfs is not well constrained by current observations and MARVELS-3B likely lies in a relatively underpopulated region of mass ratio parameter space. Nevertheless, we consider several different priors on the companion mass ratio which we suggest are reasonable given current observations (see, e.g., Grether & Lineweaver 2006) of the form: \( dN/dq \propto q^{-1} \), \( dN/dq \propto q^{-4} \), and \( dN/dq \propto q^{-1} \) constant. We note that massive companions are ruled out by the lack of a statistically significant infrared excess in the SED (Figure 1) and the lack of a secondary component in our high-resolution optical spectra (see discussion below). We include this constraint by weighting the resulting distribution of \( M_\gamma \) by \( \exp[-0.5\Delta K/\Delta K_{\text{max}}^2] \), where \( \Delta K_{\text{max}} \) is the upper limit on the excess flux (in magnitudes) in the \( K \) band, and \( \Delta K \) is the excess flux contributed by a companion of mass \( M_\gamma \) and a primary of mass \( M_\star \), as determined using the Baraffe et al. (1998) solar metallicity, \( Y = 0.275, 1 \) Gyr mass–magnitude relations (note that we could have adopted any isochrone in the range of 1–10 Gyr with negligible difference). We caution the reader that this specific constraint does not fully and uniformly represent the prior for every possible configuration of the companion, but rather is a reasonable, simplifying set of conditions. We did not observe a statistically significant IR excess flux in TYC 4110’s SED (Figure 1); thus, we used the 3\( \sigma \) standard deviation (0.06 mag) of the \( K \)-band data for \( \Delta K_{\text{max}} \). We note that the IR flux contribution from the wider separation candidate tertiary companion, discussed in more detail in Section 4.4, is less than this \( \Delta K_{\text{max}} \) and therefore does not influence our mass estimate.

The resultant cumulative distributions of the true mass are shown in Figure 6, and we summarize the median mass for each

Figure 5. Phase-folded radial velocity curve is shown, for a MARVELS-3B period of 78.994 ± 0.012 days and eccentricity of 0.1095 ± 0.0023. Based on the derived stellar mass of 1.07\( ^{+0.08}_{−0.06} \) \( M_\odot \) (Table 2), we determine the minimum (\( sin i = 1 \)) mass of MARVELS-3B to be >97.7 ± 5.8 \( M_{\oplus} \). (A color version of this figure is available in the online journal.)
Table 4

MCMC Properties of MARVELS-3B

<table>
<thead>
<tr>
<th>Assumed Prior</th>
<th>Mass of MARVELS-3B</th>
<th>Transit Probability</th>
<th>q (Mass Ratio)</th>
</tr>
</thead>
<tbody>
<tr>
<td>None (sin $i$ = 1)</td>
<td>97.7 $M_{Jup}$</td>
<td>1</td>
<td>&gt;0.087 ± 0.003</td>
</tr>
<tr>
<td>$dN/dq \propto q^{+1}$</td>
<td>166.2 $M_{Jup}$</td>
<td>0.0055</td>
<td>0.149</td>
</tr>
<tr>
<td>$dN/dq \propto q^{-1}$</td>
<td>113.0 $M_{Jup}$</td>
<td>0.0129</td>
<td>0.100</td>
</tr>
<tr>
<td>$dN/dq = \text{const}$</td>
<td>125.9 $M_{Jup}$</td>
<td>0.0092</td>
<td>0.112</td>
</tr>
</tbody>
</table>

Notes. A summary different mass estimates of MARVELS-3B and the resultant mass ratio for different assumed priors on the statistical companion mass ratio around G dwarfs and our MCMC analysis. The prior “none” corresponds to the minimum mass of MARVELS-3B, simply assuming sin $i$ = 1. For all other priors, the quoted companion mass and $q$ values are the median mass determined from our MCMC analysis described in Section 4 and shown in Figure 6.

Figure 6. Cumulative probability that the mass of MARVELS-3B is less than a given mass is shown, for four different priors on the companion mass ratio described in Section 4.

Figure 7. Continuum normalized spectrum of HD153458 was subtracted from the continuum normalized spectrum of TYC 4110-01037-1. The $1\sigma$ Poisson errors in the data are illustrated with gray boxes. As discussed in Section 4.3, we note that minor mismatches between the properties of the reference and science spectra could produce noticeable subtraction residuals in line wings, which suggests that only strong, repeatable deviations in these difference spectra should be interpreted as real contributions from companion(s). An M3-type companion would have contributed a $2\%$ flux enhancement to the system. However, the difference spectrum does not exhibit $>3\sigma$ deviations above the level of the Poisson noise ($0.8\%$) and continuum normalization uncertainties present in the data, which sets the lower mass limit for MARVELS-3B that can be ascertained from these specific data. (A color version of this figure is available in the online journal.)

4.4. Candidate Tertiary Companion

Triple star systems are a relatively common outcome of the star formation process (see, e.g., Tokovinin 2004). To further assess the multiplicity of TYC 4110, we acquired adaptive optics images on 2012 January 7 using NIRC2 (PI: Keith Matthews) at...
the Keck Observatory in natural guide star mode. Our initial data set consisted of nine dithered images taken in the $K'$ filter. Inspection of the raw frames showed evidence for a faint candidate companion located to the southwest of TYC 4110.

We measured an accurate position for the candidate companion using the technique described in Crepp et al. (2012). We first fit Gaussian functions to the stellar and companion point-spread functions to locate their centroids in each frame. The primary star was not saturated in any of our dithered images. We then correct for distortion in the NIRC2 focal plane (narrow camera mode) using the publicly available software provided by the Keck Observatory astrometry support page. The results are averaged and the uncertainty in the separation and position angle is taken as the standard deviation, taking into account uncertainty in the plate scale and orientation of the array by propagating these errors to the final calculated position. Adopting a plate scale of $9.963 \pm 0.006$ mas pixel$^{-1}$ and instrument orientation relative to the sky of $0:13 \pm 0:02$, as measured by Ghez et al. (2008), we find a companion separation and position angle of $\rho = 986 \pm 4$ mas and P.A. = 218:1 \pm 0:3, respectively.

Upon noticing the companion, we obtained additional images in the $J$ and $H$ bands to facilitate characterization. Our aperture photometry indicates that the object has red colors: $\Delta J = 4.219 \pm 0.104$, $\Delta H = 3.940 \pm 0.032$, and $\Delta K' = 3.805 \pm 0.027$ mag. Table 5 lists its apparent magnitude as measured relative to the primary star, taking into account the combined light from each source.

Both the $(J - H) = 0.55$ and $(J - K') = 0.75$ colors indicate a spectral type of $\sim$M3V (Leggett et al. 2002). Assuming the candidate is situated at the same distance as the primary, we find that the absolute magnitudes, $M_J = 8.10 \pm 0.21$, $M_H = 7.55 \pm 0.32$, $M_K = 7.36 \pm 0.13$, are each consistent with an $\sim 0.25 M_\odot$ star when compared to the Girardi et al. (2002) evolutionary models, which corresponds to a main-sequence spectral type of $\sim$dM4. The relations from Table 5 of Kraus & Hillenbrand (2007) yield the same result (dM4), though with a possibly lower mass estimate of $\sim$0.20 $M_\odot$.

Given the R.A., decl., and distance of TYC 4110, the a priori likelihood of detecting a background star within 1''0 is $\sim$0.8%. With a proper motion of $[-0.20, -99.40]$ mas yr$^{-1}$, a time baseline of several months will be sufficient to assess its association with the primary star. We note that the detection and mass constraints placed on MARVELS-3B in this paper hold regardless of whether or not this candidate tertiary companion is confirmed to be comoving with the primary star.

### 5. DISCUSSION

We discuss some of the derived properties for MARVELS-3B in the context of previous studies of low-mass companions to solar-like stars. Both Duquennoy & Mayor (1991) and Raghavan et al. (2010) demonstrate that companions to solar-like stars having orbital periods $\lesssim 12$ days are circular; however, companions having orbital periods similar to that of MARVELS-3B, $\sim 79$ days, exhibit eccentricities from 0 to 0.6 (Duquennoy & Mayor 1991; Mayor et al. 1992; Raghavan et al. 2010). MARVELS-3B’s modest eccentricity of $\sim 0.11$ is therefore clearly consistent with that observed for other similar period companions.

Arguably the most distinctive feature of TYC 4110 is its extremely low mass ratio, $q$, of $\geq 0.087 \pm 0.003$, given its relatively short $\sim 79$ day period. As illustrated in Figure 9, previous statistical investigations of binarity in solar-like ($T_{\text{eff}} \lesssim 6000$ K) stars have found evidence that the short period BD desert extends in mass toward the low-mass star regime (Burgasser et al. 2007; Bouchez et al. 2011; Sahlmann et al. 2011). A similar desert of short period, low $q$ companions to low-mass K and M dwarf stars has also been observed (Figure 9; see also Burgasser et al. 2007). The studies of companions around solar-like stars by both Duquennoy & Mayor (1991) and Raghavan et al. (2010) report no firm detection of low $q$ binary companions with orbital periods $< 100$ days. The closest short period analog observed by Raghavan et al. (2010; see, e.g., their Figure 17) is a multiple (>2 components) $q \sim 0.23$ system with an orbital period of $\sim 50$ days, while the closest short period binary is a $\sim 1$ day period object with a $q$ of $\sim 0.4$. All other low $q$ binaries in their sample have orbital periods $\gtrsim 5000$ days. Mayor et al. (2001) also report a sparse number of low $q$ binary companions to solar-like stars, but do not quantify the orbital periods of these objects.

The absolute “dryness” of the low-mass ratio, short-period desert for solar-like ($T_{\text{eff}} \lesssim 6000$ K) illustrated in Figure 9 is a subject of active investigation and debate in the literature. G 357 (Pont et al. 2005), Kepler-16b (Doyle et al. 2011), and vB 69 (Bender & Simon 2008) are short period, low $q$,
solar-like binary systems that populate this parameter space. The statistical frequency of objects like OGLE-TR-122b and Kepler-16b have not been quantified by the OGLE or Kepler surveys; hence, it is plausible that they are indeed rare. We note that there are distinct lack of low q binaries at short orbital periods is present. A similar trend is also observed in the distribution of confirmed binaries around solar-like (0.8 $M_\odot < M < 1.1 M_\odot$) stars (filled green squares), as seen in data reproduced from tabulated data in literature (Halbwachs et al. 2003; Bender & Simon 2008; Rucinski & Pribulla 2008; Dimitrov & Kjurkchieva 2010; J. R. A. Davenport et al. 2012, in preparation) and at http://www.vlm binaries.org. Among these low-mass stars, a distinct lack of low q binaries at short orbital periods is present. A similar trend is also observed in the distribution of confirmed binaries around solar-like (0.8 $M_\odot < M < 1.1 M_\odot$) stars (filled green squares), as seen in data reproduced from tabulated data in literature (Halbwachs et al. 2003; Bender & Simon 2008; Raghavan et al. 2010; Sahlmann et al. 2011). The mass ratio of the TYC 4110 (large red cross and an arrow of arbitrary size), OGLE-TR-122 (small black cross; adopted from Pont et al. 2005), Kepler-16 (small black cross; adopted from Doyle et al. 2011), and vB 69 (small black cross; adopted from Bender & Simon 2008) systems are unique in that they lie within this mass-ratio–period deficit.

(A color version of this figure is available in the online journal.)

Figure 9. Mass ratio, $q$, versus orbital period distribution of binary stars having periods $<10,000$ years and primary star $T_{\text{eff}} \lesssim 6000$ K is shown. Filled blue circles represent K and M dwarf primary stars and is based on data compiled in literature (Halbwachs et al. 2003; Mace roni & Mont balan 2004; Burgasser et al. 2007; Becker et al. 2008; Bender & Simon 2008; Rucinski & Pribulla 2008; Dimitrov & Kjurkchieva 2010; J. R. A. Davenport et al. 2012, in preparation) and at http://www.vlm binaries.org. Among these low-mass stars, a distinct lack of low $q$ binaries at short orbital periods is present. A similar trend is also observed in the distribution of confirmed binaries around solar-like ($0.8 \ M_\odot < M < 1.1 \ M_\odot$) stars (filled green squares), as seen in data reproduced from tabulated data in literature (Halbwachs et al. 2003; Bender & Simon 2008; Raghavan et al. 2010; Sahlmann et al. 2011). The mass ratio of the TYC 4110 (large red cross and an arrow of arbitrary size), OGLE-TR-122 (small black cross; adopted from Pont et al. 2005), Kepler-16 (small black cross; adopted from Doyle et al. 2011), and vB 69 (small black cross; adopted from Bender & Simon 2008) systems are unique in that they lie within this mass-ratio–period deficit.

As noted in Section 1, short-period, low $q$ companions have been reported around stars slightly more massive that the Sun (F-type stars; Bouchy et al. 2005; Pont et al. 2006; Beatty et al. 2007; Bouchy et al. 2011). Bouchy et al. (2011) propose that short-period low $q$ companions might form around a wide mass range of stars, including G-type stars, but suggest that weaker magnetic disk braking during the early formation history of F-type stars might transfer less angular momentum to their companion bodies, thereby preventing catastrophic decays of their orbits. Conversely, Bouchy et al. (2011) propose that a stronger disk braking in young G-type stars might distribute more angular momentum to their companion bodies, causing (initially) short period companions to migrate inward and become engulfed by the primary. While intriguing, this proposed evolutionary scenario would clearly benefit by a more robust assessment of how “dry” the short-period, low $q$ desert is around GKM dwarfs as compared to F dwarfs.

The precise mass ratio of MARVELS-3B is not known due to the unknown inclination of the system, thus our observations only set a lower limit of $q$ of $>0.087 \pm 0.003$. However, as demonstrated in Section 4, our Bayesian analysis of the system using four plausible prior assumptions all indicate the likely median mass of MARVELS-3B is a dM star, yielding mass ratios of $0.087 < q < 0.149$ (Figure 6 and Table 4). Like OGLE-TR-122b (Pont et al. 2005) and Kepler-16b (Doyle et al. 2011), MARVELS-3B therefore seems likely to be an outlier to the mass-ratio–period relationships commonly observed for both solar-like stars and lower-mass dM stars (Figure 9).

In this context, we note that analyses of the period distribution of exoplanets have revealed a deficit of such bodies having orbital periods of 10–100 days, aka the “period valley” (Udry et al. 2003; Jones et al. 2003). Wittenmyer et al. (2010) suggest that this observed deficit is real for the giant planet population ($M > 100 M_\oplus$), but that any deficit of lower mass planets (10–100 $M_\oplus$) in this period regime might be the result of selection effects. One possible explanation for the dearth of giant planets in 10–100 day orbits is a decrease in the amount of orbital migration which such objects experience (see, e.g., Trilling et al. 1998).

Migration could also play a role in setting the observed period distribution of the low-mass stellar binary regime. The orbital evolution of binaries has been explored computationally, and stellar accretion, the interaction between binaries with their natal gas disks, and interactions between triple components can influence these systems (see, e.g., Bate et al. 2002; Stam atellos & Whitworth 2009; Kratter 2011). Bate et al. (2002), for example, found such processes were successful at producing short-period binaries in high-mass ratio systems ($q \geq 0.3$), but it is uncertain as to whether these specific simulations could produce short-period, low $q$ systems like MARVELS-3B.

$N$-body simulations of the early evolution of stellar clusters which include instantaneous gas removal (Mocek & Bate 2010) are beginning to better reproduce the number of unequal mass solar-like binaries observed (Duquennoy & Mayor 1991; Raghavan et al. 2010). Potentially relevant for MARVELS-3B, Mocek & Bate (2010) showed that one simulated triple system comprised of a 0.96 and 0.73 $M_\odot$, 2 AU separation binary with a 0.21 $M_\odot$ tertiary at 12 AU, broke up into a tight (0.1 AU separation) binary system comprised of the 0.21 and 0.73 $M_\odot$ components (e.g., a mass ratio, $q$, of 0.29). We therefore speculate that it is possible that the short period, low $q$ MARVELS-3B binary was initially part of a tertiary (or larger) system with much different initial orbital parameters and only achieved its final orbital configuration following the dispersal of the cluster in which it formed. Although our analysis of available SuperWASP photometry and MARVELS+SARG RV data exhibited no evidence of the presence of additional, long-period ($\geq 2$ years) bodies in...
the system, our single-epoch detection of a candidate tertiary body in the system via high contrast imaging could support this interpretation. Additional epochs of imagery should be pursued to establish if this body is comoving with the TYC 4110 system. Although beyond the scope of this paper, future simulations of binary migration and orbital evolution during cluster dispersal should explore the limits and frequency at which they can reproduce short-period, low-mass ratio binaries for solar-like stars.

6. CONCLUSIONS

We present a detailed analysis of the fundamental properties of the solar-like star TYC 4110-01037-1 and its very low mass stellar companion. This analysis was performed in the context of our long-term goal of performing a detailed statistical analysis of global trends in the population of well vetted and characterized BDs and low-mass binary companions identified by the MARVELS survey. We find:

1. TYC 4110-01037-1 is a $\lesssim 5$ Gyr solar-like star characterized by $T_{\text{eff}} = 5879 \pm 29$ K, log $g = 4.48 \pm 0.15$, and $[\text{Fe/H}] = -0.01 \pm 0.05$. We determine the stellar mass to be $1.07 \pm 0.08 M_\odot$ and stellar radius to be $0.99 \pm 0.18 R_\odot$.

2. MARVELS-3B is a $\gtrsim 97.7 \pm 5.8 M_{\text{Jup}}$ ($\sin i$) companion to TYC 4110-01037-1, which follows a moderately elliptical ($e = 0.1095 \pm 0.0023$), 78.994 ± 0.012 day orbital period.

3. The mass ratio, $q$, of the companion to the primary is $\gtrsim 0.087 \pm 0.003$. MARVELS-3B therefore resides in a short period, low $q$ desert analogous to the short-period BD desert.

4. We speculate that MARVELS-3B might have initially formed in a tertiary system with much different orbital parameters and achieved its present-day configuration following the dispersal of the cluster in which it formed. A candidate tertiary body has been identified via single-epoch, high contrast imagery. If this object is confirmed to be comoving, we estimate it would be a dM4 star.

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