A measurement of the ratio of the production cross sections for W and Z bosons in association with jets with the ATLAS detector

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A measurement of the ratio of the production cross sections for $W$ and $Z$ bosons in association with jets with the ATLAS detector

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Abstract The ratio of the production cross sections for $W$ and $Z$ bosons in association with jets has been measured in proton–proton collisions at $\sqrt{s} = 7$ TeV with the ATLAS experiment at the Large Hadron Collider. The measurement is based on the entire 2011 dataset, corresponding to an integrated luminosity of 4.6 fb$^{-1}$. Inclusive and differential cross-section ratios for massive vector bosons decaying to electrons and muons are measured in association with jets with transverse momentum $p_T > 30$ GeV and jet rapidity $|y| < 4.4$. The measurements are compared to next-to-leading-order perturbative QCD calculations and to predictions from different Monte Carlo generators implementing leading-order matrix elements supplemented by parton showers.

1 Introduction

Precise measurements of the production of vector bosons in association with jets are important tests of quantum chromodynamics (QCD) and provide constraints on background processes to Higgs boson studies and to searches for new physics. The measurement of the ratio of $W +$ jets to $Z +$ jets\footnote{In this paper, $W$ means a $W^+$ or $W^-$ boson and $Z$ is defined as a $Z$ or $\gamma^*$ boson.} production cross sections, termed $R_{\text{jets}}$, directly probes the difference between the kinematic distributions of the jet system recoiling against the $W$ or $Z$ bosons.

In comparison to separate $W +$ jets and $Z +$ jets cross section measurements, the $R_{\text{jets}}$ measurement is a more precise test of perturbative QCD (pQCD), since some experimental uncertainties and effects from non-perturbative processes, such as hadronization and multi-parton interactions, are greatly reduced in the ratio. This allows precise comparisons with state-of-the-art Monte Carlo simulations and next-to-leading-order (NLO) perturbative QCD calculations to be made.

At low energies, the difference in vector-boson masses translates to a change in momentum transfer between incoming partons and thus different hadronic radiation patterns. In addition, the parton distribution functions of the proton (PDFs) imply different quark–gluon and quark–antiquark contributions to $W +$ jets and $Z +$ jets processes.

At very high energies, the vector-boson mass difference is not large relative to the momentum transfer, so differences between $W +$ jets and $Z +$ jets production are expected to decrease, even though some differences in the parton distribution functions remain. A precise measurement of $R_{\text{jets}}$ can therefore be used, in the context of searches for new particles or interactions beyond the Standard Model, to infer the $W +$ jets contribution, given $Z +$ jets production in the same phase space, or vice versa. The $R_{\text{jets}}$ measurement may also be sensitive to direct contributions from new particle production, if the new particles decay via $W$ or $Z$ bosons [1]. New physics phenomena are generally expected to appear in various topologies with high-momentum jets or high jet multiplicities, highlighting the importance of studying QCD effects in those regions of phase space.

The ATLAS collaboration performed the first measurement of $R_{\text{jets}}$ as a function of the jet transverse momentum in events with exactly one jet in proton–proton collisions at $\sqrt{s} = 7$ TeV, using a data sample corresponding to an integrated luminosity of 33 pb$^{-1}$ [2]. This result demonstrated that the precision obtained in such a measurement is sufficient to be sensitive to the QCD effects mentioned above. The CMS collaboration performed an $R_{\text{jets}}$ measurement of the jet multiplicity in vector-boson production with up to four associated jets, based on a similar dataset corresponding to an integrated luminosity of 36 pb$^{-1}$ in $pp$ collisions collected at $\sqrt{s} = 7$ TeV [3]. The results reported in this paper are based on a dataset corresponding to an integrated luminosity of 4.6 fb$^{-1}$, collected with the ATLAS detector during the 2011 $pp$ collision run of the LHC at $\sqrt{s} = 7$ TeV. This dataset is over a hundred times larger than the one used in previously published results, allowing improved precision.
over a much larger region of phase space as well as the study of previously inaccessible differential distributions.

The \( R_{\text{jets}} \) measurement is done for the electron and muon decay channels of the \( W \) and \( Z \) bosons for jets with transverse momentum \( p_T > 30 \) GeV and rapidity \( |y| < 4.4 \). The measurements of the electron and muon channels are performed in slightly different phase spaces and combined in a common phase space defined in terms of the \( p_T \) and pseudorapidity \( \eta \) of the leptons, the invariant mass of the \( Z \) boson, the angular separation between the two leptons of the \( Z \) boson decay, and the transverse mass of the \( W \) boson, as presented in Table 1. The \( W \) and \( Z \) selections are based on the \( W + \) jets and \( Z + \) jets cross-section measurements detailed in Ref. [4,5], with a minor update in the \( Z \) selection to further reduce the uncertainty on the \( R_{\text{jets}} \) measurement. In the results reported here, \( R_{\text{jets}} \) is measured as a function of the inclusive and exclusive jet multiplicity \( (N_{\text{jets}}) \) up to four jets. An extensive set of differential measurements is also presented, in which \( R_{\text{jets}} \) is measured as a function of the transverse momentum and the rapidity of the leading jet, which is the one with largest transverse momentum, in events with at least one jet. The ratio \( R_{\text{jets}} \) is also presented as a function of the transverse momentum and rapidity of the second and third leading jets in events with at least two or three jets respectively. A set of differential measurements as a function of dijet observables in events with at least two jets is presented. The measurement of \( R_{\text{jets}} \) as a function of the summed scalar \( p_T \) of the jets (\( S_T \)) for different jet multiplicities is also reported. The results are compared to several Monte Carlo generators and with next-to-leading-order pQCD predictions corrected for non-perturbative effects.

The paper is organized as follows. The experimental setup is described in Sect. 2. Section 3 provides details on the simulations used in the measurement, and Sect. 4 discusses the event selection. The estimation of background contributions is described in Sect. 5, and the procedure used to correct the measurements for detector effects is described in Sect. 6. The treatment of the systematic uncertainties is described in Sect. 7. Section 8 discusses the combination of the electron and muon results. Section 9 provides details on the NLO pQCD predictions. Finally, Sect. 10 discusses the results, and Sect. 11 presents the conclusions.

### 2 The ATLAS detector

The ATLAS detector [6] is a multi-purpose detector with a symmetric cylindrical geometry and nearly \( 4\pi \) coverage in solid angle. The collision point is surrounded by inner tracking devices followed by a superconducting solenoid providing a \( 2 \) T magnetic field, a calorimeter system, and a muon spectrometer. The inner tracker provides precision tracking of charged particles for pseudorapidities \( |\eta| < 2.5 \). It consists of silicon pixel and microstrip detectors and a straw-tube transition radiation tracker. The calorimeter system has liquid argon (LAr) or scintillator tiles as active media. In the pseudorapidity region \( |\eta| < 3.2 \), high-granularity LAr electromagnetic (EM) sampling calorimeters are used. An iron/scintillator tile calorimeter provides hadronic coverage for \( |\eta| < 1.7 \). The endcap and forward regions, spanning \( 1.5 < |\eta| < 4.9 \), are instrumented with LAr calorimeters for both the EM and hadronic measurements. The muon spectrometer consists of three large superconducting toroids, each comprising eight coils, and a system of trigger chambers and precision tracking chambers that provide triggering and tracking capabilities in the ranges \( |\eta| < 2.4 \) and \( |\eta| < 2.7 \) respectively.

The ATLAS trigger system uses three consecutive levels. The Level-1 triggers are hardware-based and use coarse detector information to identify regions of interest, whereas the Level-2 triggers are based on fast online data reconstruction algorithms. Finally, the Event Filter triggers use offline data reconstruction algorithms.

### 3 Monte Carlo simulation

Simulated event samples were used to correct the measured distributions for detector effects and acceptance, to determine some background contributions and to correct theory calculations for non-perturbative effects. Signal samples

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**Table 1** Particle-level phase space of the present \( R_{\text{jets}} \) measurement

<table>
<thead>
<tr>
<th>Particle</th>
<th>Phase Space</th>
</tr>
</thead>
<tbody>
<tr>
<td>Lepton ( p_T ) and pseudorapidity ( \eta )</td>
<td>( p_T &gt; 25 ) GeV, (</td>
</tr>
<tr>
<td>( W ) transverse mass and neutrino ( p_T )</td>
<td>( m_T &gt; 40 ) GeV, ( p_T &gt; 25 ) GeV</td>
</tr>
<tr>
<td>( Z ) invariant mass and lepton–lepton angular separation</td>
<td>( 66 &lt; m_{\ell\ell} &lt; 116 ) GeV, ( \Delta R_{\ell\ell} &gt; 0.2 )</td>
</tr>
<tr>
<td>Jet ( p_T ), rapidity and jet–lepton angular separation</td>
<td>( p_T &gt; 30 ) GeV, (</td>
</tr>
</tbody>
</table>

\( \Delta R \equiv \sqrt{(\Delta \phi)^2 + (\Delta \eta)^2} \).
of $W \rightarrow \ell v +$ jets and $Z \rightarrow \ell \ell +$ jets (where $\ell = e, \mu$) events were generated with ALPGEN v2.13 [7], with up to five additional partons in the final state. It was interfaced to HERWIG v6.520 [8] for parton showering and fragmentation, with JIMMY v4.31 [9] for contributions from multi-parton interactions and with PHOTOS [10] to calculate final-state QED radiation. The CTEQ6L1 [11] PDFs were used with the AUET2-CTEQ6L1 tune [12], a set of specific non-perturbative event generation parameter values. Similar samples were produced with ALPGEN v2.14 interfaced to PYTHIA v6.425 [13] using the PERUGIA2011C [14] tune and PHOTOS. They were used to estimate the uncertainties on non-perturbative corrections for parton-level NLO pQCD predictions. An additional set of signal samples was generated with SHERPA v1.4.1 [15, 16] and CT10 PDFs [17]. Top quark pair production ($tt$) was simulated with ALPGEN [7], with up to five additional partons in the final state. It was interfaced to PYTHIA v6.425 [13] using the PERUGIA2011C [14] tune and PHOTOS. The generated Monte Carlo (MC) samples were overlaid with additional inelastic $pp$ scattering events generated with PYTHIA v6.425, following the distribution of the average number of $pp$ interactions in the selected data. The samples were then passed through the simulation of the ATLAS detector based on GEANT4 [21, 22] and through the related trigger simulation.

All samples were normalized to the inclusive cross section calculated at the highest pQCD order available. The $W/Z +$jets signal samples were normalized to the next-to-next-to-leading-order (NNLO) pQCD inclusive Drell–Yan predictions calculated with the FEWZ [23] program and the MSTW2008 NNLO PDFs [24]. The $tt$ samples were normalized to the cross section calculated at NNLO+NNLL in Refs. [25–30], and the diboson samples were normalized to cross sections calculated at NLO using MCFM [31] with the MSTW2008 PDF set.

The simulated events were reconstructed and analysed with the same analysis chain as the data. Scale factors were applied to the simulated samples to correct the lepton trigger, reconstruction, and identification efficiencies to match those measured in data.

### 4 Event selection

The data samples considered in this paper correspond to a total integrated luminosity of 4.6 fb$^{-1}$, with an uncertainty of 1.8 % [32]. Table 2 summarizes the kinematic requirements for leptons, $W$ bosons, $Z$ bosons, and jets. The selection criteria for $W$ boson candidates were defined using the largest possible coverage of the ATLAS detector for electrons, muons and jets. The selection criteria for $Z$ boson candidates were modified with respect to those in Ref. [5], to be as similar as possible to the $W$ boson selection in order to maximize the cancellation of uncertainties in the $R_{\text{jets}}$ measurement: trig-

<table>
<thead>
<tr>
<th>Electron selection</th>
<th>Muon selection</th>
</tr>
</thead>
<tbody>
<tr>
<td>Lepton $p_T$</td>
<td>$p_T &gt; 25$ GeV</td>
</tr>
<tr>
<td>Lepton pseudorapidity</td>
<td>$</td>
</tr>
<tr>
<td>$W \rightarrow \ell v$ event selection</td>
<td></td>
</tr>
<tr>
<td>Missing transverse momentum</td>
<td>$E_T^{\text{miss}} &gt; 25$ GeV</td>
</tr>
<tr>
<td>Transverse mass</td>
<td>$m_T &gt; 40$ GeV</td>
</tr>
<tr>
<td>$Z \rightarrow \ell \ell$ event selection</td>
<td></td>
</tr>
<tr>
<td>Multiplicity</td>
<td>Exactly two selected leptons</td>
</tr>
<tr>
<td>Charge</td>
<td>Opposite sign</td>
</tr>
<tr>
<td>Invariant mass</td>
<td>$66 &lt; m_{\ell \ell} &lt; 116$ GeV</td>
</tr>
<tr>
<td>Separation</td>
<td>$\Delta R_{\ell \ell} &gt; 0.2$</td>
</tr>
<tr>
<td>Jet selection</td>
<td></td>
</tr>
<tr>
<td>Transverse momentum</td>
<td>$p_T &gt; 30$ GeV</td>
</tr>
<tr>
<td>Jet rapidity</td>
<td>$</td>
</tr>
<tr>
<td>Jet–lepton angular separation</td>
<td>$\Delta R_{ij} &gt; 0.5$</td>
</tr>
</tbody>
</table>
bers requiring at least one lepton were employed, the minimum lepton transverse momentum was raised from 20 GeV to 25 GeV, tighter criteria were used to identify electrons and slightly looser requirements were placed on the second leading lepton with respect to the leading one.

The data were collected using single-electron or single-muon triggers, employing the same requirements for the W and Z data selections. Electron-channel events were selected using a trigger that required the presence of at least one electron candidate, formed by an energy cluster consistent with an electromagnetic shower in the calorimeter and associated to an inner detector track. Electron candidates were required to have a reconstructed transverse energy above 20 GeV or 22 GeV, depending on the trigger configuration of the different data periods. Muon-channel events were recorded using a trigger that required the presence of at least one muon candidate with transverse momentum above 18 GeV. Lepton trigger thresholds were low enough to ensure that leptons with $p_T > 25$ GeV lie on the trigger efficiency plateau.

Events were required to have a primary vertex, defined as the vertex in the event with the highest summed $p_T^2$ of all associated tracks, among vertices with at least three tracks.

Electrons were reconstructed by matching clusters of energy found in the electromagnetic calorimeter to tracks reconstructed in the inner detector. Candidate electrons had to satisfy the “tight” quality requirements defined in Ref. [33], which include requirements on the calorimeter shower shape, track quality, and association of the track with the energy cluster found in the calorimeter. Electron candidates had to have $p_T > 25$ GeV and $|\eta| < 2.47$, where the transition region between barrel and endcap electromagnetic calorimeter sections at $1.37 < |\eta| < 1.52$ was excluded.

Muons were reconstructed from track segments in the muon spectrometer that were matched with tracks in the inner detector [34], and were required to have $p_T > 25$ GeV and $|\eta| < 2.4$. To suppress particles from hadron decays, the leading muon had to be consistent with originating from the primary vertex by requiring $|d_0/\sigma(d_0)| < 3.0$, where $d_0$ is the transverse impact parameter of the muon and $\sigma(d_0)$ is its uncertainty.

In order to suppress background from multi-jet events where a jet is misidentified as a lepton, the leading lepton was required to be isolated. An additional $p_T$- and $\eta$-dependent requirement on a combination of calorimeter and track isolation variables was applied to the leading electron, in order to yield a constant efficiency across different momentum ranges and detector regions, as detailed in Ref. [35]. The track-based isolation uses a cone size of $\Delta R = 0.4$ and the calorimeter-based isolation uses a cone size of $\Delta R = 0.2$. The actual isolation requirements range between 2.5 GeV and 4.5 GeV for the calorimeter-based isolation and between 2.0 GeV and 3.0 GeV for the track-based isolation. For muon candidates, the scalar sum of the transverse momenta of tracks within a cone of size $\Delta R = 0.2$ around the leading muon had to be less than 10 % of its transverse momentum.

Reconstructed W candidates were required to have exactly one selected lepton. The missing transverse momentum in the event had to have a magnitude $E_T^{miss}$ greater than 25 GeV, and the transverse mass $m_T$ had to be greater than 40 GeV. The magnitude and azimuthal direction of the missing transverse momentum are measured from the vector sum of the transverse momenta of calibrated physics objects and additional soft calorimeter deposits [36]. Reconstructed Z candidates were required to have exactly two selected leptons of the same flavour with opposite charge. Their invariant mass $m_{\ell\ell}$ had to be in the range $66 \leq m_{\ell\ell} \leq 116$ GeV and the leptons had to be separated by $\Delta R_{\ell\ell} > 0.2$.

Jets were reconstructed using the anti-$k_t$ algorithm [37] with a distance parameter $R = 0.4$ on topological clusters of energy in the calorimeters [38]. Jets were required to have a transverse momentum above 30 GeV and a rapidity of $|y| < 4.4$. Jets within $\Delta R = 0.5$ of a selected lepton were removed. The energy and the direction of reconstructed jets were corrected to account for the point of origin, assumed to be the primary vertex, and for the bias introduced by the presence of additional pp interactions in the same bunch crossing (“pile-up”). The jet energy was then calibrated to account for the different response of the calorimeters to electrons and hadrons and for energy losses in un-instrumented regions by applying correction factors derived from simulations. A final calibration, derived from in-situ techniques using Z+jet balance, $\gamma$+jet balance and multi-jet balance, was applied to the data to reduce residual differences between data and simulations [39].

In order to reject jets from pile-up, a jet selection was applied based on the ratio of the summed scalar $p_T$ of tracks originating from the primary vertex and associated with the jet to the summed $p_T$ of all tracks associated with the jet. Jets were selected if this ratio was above 0.75. This criterion was applied to jets within $|\eta| < 2.4$, so that they are inside the inner tracker acceptance. Comparison between data and simulation for various data periods confirmed that the residual impact of pile-up on the distribution of the jet observables in this analysis is well modelled by the simulation.

The numbers of $W$ + jets and $Z$ + jets candidate events in the electron and muon channels for each jet multiplicity are shown in Tables 3 and 4, together with the corresponding numbers of predicted events. The expected fraction of predicted events from signal and each background source, determined as described in the next section, is also shown.

5 Background estimation

Background processes to W and Z boson production associated with jets can be classified into three categories. The
Table 3: The contribution of signal and background from various sources, expressed as a fraction of the total number of expected events for the $W(\rightarrow e\nu) + \text{jets}$ and $Z(\rightarrow ee) + \text{jets}$ selection as a function of jet multiplicity $N_{\text{jets}}$, together with the total numbers of expected and observed events.

<table>
<thead>
<tr>
<th>$N_{\text{jets}}$</th>
<th>0</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fraction [%]</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$W \rightarrow e\nu$ + jets</td>
<td>94</td>
<td>78</td>
<td>73</td>
<td>58</td>
<td>37</td>
</tr>
<tr>
<td>$Z \rightarrow ee$</td>
<td>0.30</td>
<td>7.5</td>
<td>6.6</td>
<td>6.8</td>
<td>5.4</td>
</tr>
<tr>
<td>$t\bar{t}$</td>
<td>&lt; 0.1</td>
<td>0.30</td>
<td>3.4</td>
<td>18</td>
<td>46</td>
</tr>
<tr>
<td>Multi-jet</td>
<td>4</td>
<td>11</td>
<td>12</td>
<td>11</td>
<td>6.9</td>
</tr>
<tr>
<td>Electroweak (without $Z \rightarrow ee$)</td>
<td>1.9</td>
<td>2.6</td>
<td>3.3</td>
<td>3</td>
<td>1.9</td>
</tr>
<tr>
<td>Single top</td>
<td>&lt; 0.1</td>
<td>0.30</td>
<td>1.7</td>
<td>3.5</td>
<td>3.9</td>
</tr>
<tr>
<td>Total predicted</td>
<td>11 100 000 ± 640 000</td>
<td>1 510 000 ± 99 000</td>
<td>354 000 ± 23 000</td>
<td>89 500 ± 5600</td>
<td>28 200 ± 1400</td>
</tr>
<tr>
<td>Data observed</td>
<td>10 878 398</td>
<td>1 548 000</td>
<td>361 957</td>
<td>91 212</td>
<td>28 076</td>
</tr>
</tbody>
</table>

Table 4: The contribution of signal and background from various sources, expressed as a fraction of the total number of expected events for the $W(\rightarrow \mu\nu) + \text{jets}$ and $Z(\rightarrow \mu\mu) + \text{jets}$ selection as a function of jet multiplicity $N_{\text{jets}}$, together with the total numbers of expected and observed events.

<table>
<thead>
<tr>
<th>$N_{\text{jets}}$</th>
<th>0</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
</tr>
</thead>
<tbody>
<tr>
<td>Fraction [%]</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$W \rightarrow \mu\nu$</td>
<td>93</td>
<td>82</td>
<td>78</td>
<td>62</td>
<td>40</td>
</tr>
<tr>
<td>$Z \rightarrow \mu\mu$</td>
<td>3.4</td>
<td>3.5</td>
<td>3.5</td>
<td>3</td>
<td>2</td>
</tr>
<tr>
<td>$t\bar{t}$</td>
<td>&lt; 0.1</td>
<td>0.20</td>
<td>3.1</td>
<td>19</td>
<td>46</td>
</tr>
<tr>
<td>Multi-jet</td>
<td>1.5</td>
<td>11</td>
<td>10</td>
<td>9.5</td>
<td>6.8</td>
</tr>
<tr>
<td>Electroweak (without $Z \rightarrow \mu\mu$)</td>
<td>1.9</td>
<td>2.7</td>
<td>3.4</td>
<td>2.9</td>
<td>1.9</td>
</tr>
<tr>
<td>Single top</td>
<td>&lt; 0.1</td>
<td>0.20</td>
<td>1.7</td>
<td>3.4</td>
<td>3.8</td>
</tr>
<tr>
<td>Total predicted</td>
<td>13 300 000 ± 770 000</td>
<td>1 710 000 ± 100 000</td>
<td>384 000 ± 24 000</td>
<td>96 700 ± 6100</td>
<td>30 100 ± 1600</td>
</tr>
<tr>
<td>Data observed</td>
<td>13 414 400</td>
<td>1 758 239</td>
<td>403 146</td>
<td>99 749</td>
<td>30 400</td>
</tr>
</tbody>
</table>

Table 4: The contribution of signal and background from various sources, expressed as a fraction of the total number of expected events for the $W(\rightarrow \mu\nu) + \text{jets}$ and $Z(\rightarrow \mu\mu) + \text{jets}$ selection as a function of jet multiplicity $N_{\text{jets}}$, together with the total numbers of expected and observed events.

<table>
<thead>
<tr>
<th>$N_{\text{jets}}$</th>
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<th>1</th>
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<th>4</th>
</tr>
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<tbody>
<tr>
<td>Fraction [%]</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$Z \rightarrow \mu\mu$</td>
<td>100</td>
<td>99</td>
<td>96</td>
<td>91</td>
<td>84</td>
</tr>
<tr>
<td>$W \rightarrow \mu\nu$</td>
<td>&lt; 0.1</td>
<td>0.10</td>
<td>0.10</td>
<td>0.20</td>
<td>0.20</td>
</tr>
<tr>
<td>$t\bar{t}$</td>
<td>&lt; 0.1</td>
<td>0.30</td>
<td>2.2</td>
<td>6.1</td>
<td>13</td>
</tr>
<tr>
<td>Multi-jet</td>
<td>0.30</td>
<td>0.50</td>
<td>0.90</td>
<td>1.1</td>
<td>1.7</td>
</tr>
<tr>
<td>Electroweak (without $W \rightarrow \mu\nu$)</td>
<td>0.10</td>
<td>0.50</td>
<td>1.3</td>
<td>1.4</td>
<td>1.1</td>
</tr>
<tr>
<td>Single top</td>
<td>&lt; 0.1</td>
<td>&lt; 0.1</td>
<td>0.10</td>
<td>0.20</td>
<td>0.20</td>
</tr>
<tr>
<td>Total predicted</td>
<td>1 300 000 ± 79 000</td>
<td>168 000 ± 12 000</td>
<td>37 800 ± 2800</td>
<td>8100 ± 6600</td>
<td>1750 ± 160</td>
</tr>
<tr>
<td>Data observed</td>
<td>1 302 010</td>
<td>171 200</td>
<td>38 618</td>
<td>8397</td>
<td>1864</td>
</tr>
</tbody>
</table>
first category, referred to as electroweak background, consists of diboson production, vector-boson production with subsequent decay to $\tau$-leptons, and “cross-talk” background, in which the signal $W + j$ events ($Z + j$) production appears as background in the $Z + j$ ($W + j$) sample. These background contributions are relatively small (about 10% in the $W + j$ electron channel, about 6% in the $W + j$ muon channel, and about 1% in $Z + j$, as shown in Tables 3 and 4) and were thus estimated using simulated event samples. The second category consists of events where the leptons are produced in decays of top quarks. The $t\bar{t}$ component completely dominates the background contribution to $W + j$ events at high jet multiplicities, amounting to approximately 20% of the sample with $W + j \geq 3$ jets and increasing to approximately 45% for events with four selected jets. The effect is less dramatic in $Z + j$ events, where the $t\bar{t}$ background contributes about 5% to the sample of events with $Z + j \geq 3$ jets and about 10% to the sample with four jets. The background contribution from single top-quark production is about 4% of the sample in $W + j$ events for events with three or four jets, and smaller at lower jet multiplicities. This contribution is even smaller in $Z + j$ events. Contributions from $t\bar{t}$ events to $W + j$ candidates with at least three jets, where this background dominates, were estimated with a data-driven method as described below in order to reduce the overall uncertainty. The $t\bar{t}$ contributions to $W + j$ candidates with fewer than three jets and to $Z + j$ events were estimated using simulated event samples, as are the contributions from single top quarks.

The third category of background, referred to as multi-jet background, comes from events in which hadrons mimic the signature of an isolated lepton. In the electron channel this includes photon conversion processes, typically from the decay of neutral pions, narrow hadronic jets and real electrons from the decay of heavy-flavour hadrons. In the muon channel, the multi-jet background is primarily composed of heavy-flavour hadron decay processes. This background category dominates at low jet multiplicity in $W + j$ events, amounting to 11% of the selected sample in both the electron and muon channels for events with one jet. Data-driven techniques were used to estimate this background contribution to both the $W + j$ and $Z + j$ jets event samples, as described below. The methods employed to estimate background contributions with data-driven techniques in this analysis are very similar between candidate events with $W$ bosons and $Z$ bosons and between electron and muon channels.

5.1 $t\bar{t}$ background

The $t\bar{t}$ background is the dominant background contribution to $W + j$ events with at least three jets, since each top quark predominantly decays as $t \rightarrow Wb$. The size of the $t\bar{t}$ contribution was estimated with a maximum-likelihood fit to the data.

The $t\bar{t}$ template in this fit was derived from a top–quark-enhanced data sample by requiring, in addition to the selection criteria given in Table 2, at least one $b$-tagged jet in the event, as determined by the MV1 $b$-tagging algorithm of Ref. [40]. The chosen MV1 algorithm working point has a $b$-tagging efficiency of 70%. This data sample is contaminated with $W$ signal events and electroweak and multi-jet backgrounds, amounting to about 40% in events with three jets and 25% in events with four jets. The contribution from $W$ signal events and electroweak background was estimated using simulation. The multi-jet contribution to the top-enriched sample was estimated using the multi-jet background estimation method as outlined in the last part of this section, but with an additional $b$-tagging requirement. Potential biases in the $t\bar{t}$ templates extracted from data were investigated using simulated $t\bar{t}$ events. Since $b$-tagging is only available for jets within $|\eta| < 2.4$ where information from the tracking detectors exists, the $b$-tagging selection biases some of the kinematic distributions, most notably the jet rapidity distribution. To account for this, ALPGEN $t\bar{t}$ simulations were used to correct for any residual bias in the differential distributions; the maximum correction is 30%.

The number of $t\bar{t}$ events was extracted by fitting a discriminant distribution to the sum of three templates: the top-enriched sample after subtracting the contaminations discussed above, the multi-jet template (determined as described below) and the template obtained from simulation of the $W + j$ signal and the other background sources. The chosen discriminant was the transformed aplanarity, given by $\exp(-8A)$, where $A$ is the aplanarity defined as 1.5 times the smallest eigenvalue of the normalized momentum tensor of the leptons and all the jets passing the selection [41]. This discriminant provides the best separation between $t\bar{t}$ and the $W + j$ signal. The fit to the transformed aplanarity distribution was done in the range 0.0–0.85 in each exclusive jet multiplicity of three or more.

Since the top-enriched sample is a sub-sample of the signal sample, statistical correlation between the two samples is expected. Its size was estimated using pseudo-datasets by performing Poisson variations of the signal and top-enriched samples. To account for this correlation, the uncertainty on the fit was increased by 15% for events with three jets and about 30% for events with four jets.

5.2 Multi-jet background

The multi-jet background contribution to the $W + j$ selected events was estimated with a template fit method using a sample enriched in multi-jet events. The templates of the multi-jet background for the fit were extracted from data, by modifying the lepton isolation requirements in both the
increasing trigger rates. In order to build multi-jet template distributions that provide a good representation of the pile-up conditions of the selected data sample, these template distributions were extracted from two distinct data periods with high and low pile-up conditions. The background templates extracted from the two different data periods were fitted separately and then combined into an overall multi-jet estimate.

To select the multi-jet sample in the muon channel, muon candidates were required to be non-isolated. The sum of transverse momenta of tracks in a cone of size $\Delta R < 0.2$ centred on the muon-candidate direction had to be between 10% and 50% of the muon transverse momentum. The contamination from W signal events and electroweak and top backgrounds to the multi-jet sample was subtracted using simulation. It amounts to 1.4% for events with one jet and 4.8% for events with four jets.

The number of multi-jet background events was obtained for each jet multiplicity in the electron and muon channels by fitting the $E_{\text{T}}^{\text{miss}}$ distribution obtained from the $W + jets$ data candidate events (selected before the application of the $E_{\text{T}}^{\text{miss}}$ requirement) to the multi-jet template and a template of signal and electroweak and $t\bar{t}$ backgrounds derived from simulations. The fit range was chosen to ensure significant contributions from both templates, in order to guarantee fit stability under systematic variations described in Sect. 7. The $E_{\text{T}}^{\text{miss}}$ distribution was fitted in the range 15 GeV to 80 GeV in the electron channel and in the range 15 GeV to 70 GeV in the muon channel.

The multi-jet background contribution to the $Z + jets$ selected candidates was estimated using a template fit method similar to the procedure used in the $W + jets$ case. In the electron channel, the template distributions for the multi-jet background were constructed from a data sample collected with electron triggers looser than those used for the nominal $Z \rightarrow ee$ selection. Electrons were then required to satisfy the loose offline identification criteria (as defined in Ref. [33]) but fail to meet the nominal criteria. In the muon channel, the multi-jet template distributions for the multi-jet background were obtained from the nominal signal data sample, after relaxing the impact parameter significance requirement applied to $Z \rightarrow \mu\nu$ events candidates, and selecting events that did not satisfy the isolation criteria applied in the signal selection. The number of multi-jet background events was obtained for each exclusive jet multiplicity by fitting the dilepton invariant mass distribution $m_{\ell\ell}$ in an extended range, $50 < m_{\ell\ell} < 140$ GeV, excluding the $Z$-peak region itself, after all other signal requirements were applied. Due to statistical limitations for jet multiplicities greater than two jets, the normalisation factor obtained from the two-jet bin was consistently applied to the templates for higher jet multiplicities. Potential bias in this procedure was accounted for in the systematic uncertainty estimate.

The evaluation of the systematic uncertainties for each background source is explained in Sect. 7.

### Table 5: Systematic uncertainties in percent on the measured $W + jets / Z + jets$ cross-section ratio in the electron and muon channels as a function of the inclusive jet multiplicity $N_{\text{jets}}$

<table>
<thead>
<tr>
<th>$N_{\text{jets}}$</th>
<th>$\geq 0$</th>
<th>$\geq 1$</th>
<th>$\geq 2$</th>
<th>$\geq 3$</th>
<th>$\geq 4$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$(W \rightarrow e\nu)/(Z \rightarrow ee)$</td>
<td>0.89</td>
<td>0.92</td>
<td>0.93</td>
<td>0.97</td>
<td>1.0</td>
</tr>
<tr>
<td>Electron</td>
<td>0.094</td>
<td>2.0</td>
<td>2.0</td>
<td>3.5</td>
<td>5.7</td>
</tr>
<tr>
<td>JES</td>
<td>0.25</td>
<td>2.4</td>
<td>3.5</td>
<td>4.3</td>
<td>6.4</td>
</tr>
<tr>
<td>JER</td>
<td>0.19</td>
<td>1.7</td>
<td>1.2</td>
<td>1.2</td>
<td>1.0</td>
</tr>
<tr>
<td>$E_{\text{T}}^{\text{miss}}$</td>
<td>0.024</td>
<td>0.23</td>
<td>1.0</td>
<td>4.9</td>
<td>14</td>
</tr>
<tr>
<td>$t\bar{t}$</td>
<td>0.81</td>
<td>1.6</td>
<td>1.5</td>
<td>2.2</td>
<td>6.2</td>
</tr>
<tr>
<td>Multi-jet</td>
<td>0.12</td>
<td>0.57</td>
<td>0.58</td>
<td>0.76</td>
<td>1.0</td>
</tr>
<tr>
<td>Other backgrounds</td>
<td>0.20</td>
<td>0.56</td>
<td>0.86</td>
<td>1.2</td>
<td>1.4</td>
</tr>
<tr>
<td>Unfolding</td>
<td>0.062</td>
<td>0.26</td>
<td>0.27</td>
<td>0.34</td>
<td>0.44</td>
</tr>
<tr>
<td>Total</td>
<td>1.3</td>
<td>4.1</td>
<td>4.8</td>
<td>8.2</td>
<td>18</td>
</tr>
</tbody>
</table>

| $(W \rightarrow \mu\nu)/(Z \rightarrow \mu\nu)$ | 1.1 | 1.2 | 1.1 | 0.86 | 0.87 |
| Muon | 0.10 | 0.84 | 0.71 | 1.8 | 2.6 |
| JES | 0.094 | 1.6 | 1.8 | 2.6 | 4.2 |
| JER | 0.30 | 1.0 | 0.94 | 0.97 | 0.99 |
| $E_{\text{T}}^{\text{miss}}$ | 0.018 | 0.18 | 0.87 | 4.3 | 12 |
| $t\bar{t}$ | 0.20 | 0.60 | 1.1 | 1.7 | 2.7 |
| Multi-jet | 0.21 | 0.24 | 0.28 | 0.42 | 0.60 |
| Other backgrounds | 0.22 | 0.59 | 0.90 | 1.2 | 1.2 |
| Unfolding | 0.10 | 0.12 | 0.11 | 0.088 | 0.023 |
| Total | 1.2 | 2.5 | 3.0 | 5.9 | 13 |
Table 6  The ratio of $W + \text{jets}$ and $Z + \text{jets}$ production cross sections, $R_{\text{jets}}$, as a function of exclusive jet multiplicity in the phase space defined in Table 1

<table>
<thead>
<tr>
<th>$N_{\text{jets}}$</th>
<th>$R_{\text{jets}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>11.24 ± 0.01 (stat.) ± 0.11 (syst.)</td>
</tr>
<tr>
<td>1</td>
<td>8.50 ± 0.02 (stat.) ± 0.24 (syst.)</td>
</tr>
<tr>
<td>2</td>
<td>8.76 ± 0.05 (stat.) ± 0.30 (syst.)</td>
</tr>
<tr>
<td>3</td>
<td>8.33 ± 0.10 (stat.) ± 0.44 (syst.)</td>
</tr>
<tr>
<td>4</td>
<td>7.69 ± 0.21 (stat.) ± 0.70 (syst.)</td>
</tr>
</tbody>
</table>

Table 7  The ratio of $W + \text{jets}$ and $Z + \text{jets}$ production cross sections, $R_{\text{jets}}$, as a function of inclusive jet multiplicity in the phase space defined in Table 1

<table>
<thead>
<tr>
<th>$N_{\text{jets}}$</th>
<th>$R_{\text{jets}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>≥ 0</td>
<td>10.90 ± 0.01 (stat.) ± 0.10 (syst.)</td>
</tr>
<tr>
<td>≥ 1</td>
<td>8.54 ± 0.02 (stat.) ± 0.25 (syst.)</td>
</tr>
<tr>
<td>≥ 2</td>
<td>8.64 ± 0.04 (stat.) ± 0.32 (syst.)</td>
</tr>
<tr>
<td>≥ 3</td>
<td>8.18 ± 0.08 (stat.) ± 0.51 (syst.)</td>
</tr>
<tr>
<td>≥ 4</td>
<td>7.62 ± 0.19 (stat.) ± 0.94 (syst.)</td>
</tr>
</tbody>
</table>

6 Corrections for detector effects

The signal event yields were determined by subtracting the estimated background contributions from the data. After background subtraction, the resulting distributions were corrected for detector effects such that distributions at particle level were obtained. The correction procedure based on simulated samples corrects for jet, $W$ and $Z$ selection efficiency, resolution effects and residual mis-calibrations. While $W + \text{jets}$ and $Z + \text{jets}$ events were separately corrected before forming $R_{\text{jets}}$, the systematic uncertainties were estimated for the ratio itself, as explained in the next section.

At particle level, the lepton kinematic variables in the MC-generated samples were computed using final-state leptons from the $W$ or $Z$ boson decay. Photons radiated by the boson decay products within a cone of size $\Delta R = 0.1$ around the direction of a final-state lepton were added to the lepton, and the sum is referred to as the “dressed” lepton. Particle-level jets were identified by applying the anti-$k_t$ algorithm with $R = 0.4$ to all final-state particles with a lifetime longer than 4 to all final-state particles with a lifetime longer.
than 30 ps, whether produced directly in the proton–proton collision or from the decay of particles with shorter lifetimes. Neutrinos, electrons, and muons from decays of the W and Z bosons, as well as collinear photons included in the “lepton dressing procedure” were excluded by the jet reconstruction algorithm. The phase-space requirements match the selection criteria defining the data candidate events, as presented in Table 2, in order to limit the dependence of the measurement results on theoretical assumptions.

The correction was implemented using an iterative Bayesian method of unfolding [42]. Simulated events are used to generate for each distribution a response matrix to account for bin-to-bin migration effects between the reconstruction-level and particle-level distributions. The Monte Carlo particle-level prediction is used as initial prior to determine a first estimate of the unfolded data distribution. For each further iteration, the previous estimate of the unfolded distribution is used as a new input prior. Bin sizes in each distribution were chosen to be a few times larger than the resolution of the corresponding variable. The ALPGEN W + jets and Z + jets samples provide a satisfactory description of distributions in data and were employed to perform the correction procedure. The number of iterations was optimized to find a balance between too many iterations, causing high statistical uncertainties associated with the unfolded spectra, and too few iterations, which increase the dependency on the Monte Carlo prior. The optimal number of iterations is typically between one and three, depending on the observable. Since the differences in the unfolded results are negligible over this range of iterations, two iterations were used consistently for unfolding each observable.

7 Systematic uncertainties

One of the advantages of measuring $R_{\text{jets}}$ is that systematic uncertainties that are positively correlated between the numerator and denominator cancel at the level of their correlations (higher correlations result in larger cancellations). The impact on the ratio of a given source of uncertainty was estimated by simultaneously applying the systematic variation due to this source to both the W + jets and Z + jets events and repeating the full measurement chain with the systematic variations applied. This included re-estimating the data-driven background distributions after the variations had been applied.
Since the uncertainties were found to be symmetric within the statistical fluctuations, the resulting systematic uncertainties on the \( R_{\text{jets}} \) measurements were fully symmetrized by taking the average value of the upwards and downwards variations.

Uncertainty sources affecting the \( R_{\text{jets}} \) measurements can be assigned to one of the following categories: jet measurements, lepton measurements, missing transverse momentum measurement, unfolding procedure, data-driven background estimates and simulation-based background estimates. These sources of uncertainty feature significant correlations between \( W + \text{jets} \) and \( Z + \text{jets} \) processes, which have been fully accounted for as explained above. The systematic uncertainties on the \( t\bar{t} \) and multi-jet background estimates were considered to be uncorrelated between the \( W + \text{jets} \) and \( Z + \text{jets} \) selections. The uncertainty on the integrated luminosity was propagated through all of the background calculations and treated as correlated between \( W + \text{jets} \) and \( Z + \text{jets} \) so that it largely cancels in the ratio. The contributions from each of the sources mentioned above and the total systematic uncertainties were obtained by adding in quadrature the different components, and are summarized in Table 5. The total uncertainty on \( R_{\text{jets}} \) as a function of the inclusive jet multiplicity ranges from 4% for \( N_{\text{jets}} \geq 1 \) to 18% for \( N_{\text{jets}} \geq 4 \) in the electron channel and from 3% for \( N_{\text{jets}} \geq 1 \) to 13% for \( N_{\text{jets}} \geq 4 \) in the muon channel.

Jet-related systematic uncertainties are dominated by the uncertainty on the jet energy scale (JES) and resolution (JER). The JES uncertainty was derived via in-situ calibration techniques, such as the transverse momentum balance in \( Z + \text{jets} \), multi-jet and \( \gamma - \text{jet} \) events, for which a comparison between data and simulation was performed [39]. The JER uncertainty was derived from a comparison of the resolution measured in dijet data events using the bisector method [38], and the same approach was applied to simulated dijet events. The JER and JES uncertainties are highly correlated between \( W + \text{jets} \) and \( Z + \text{jets} \) observables and are thus largely suppressed compared to the individual measurements. They are nevertheless the dominant systematic uncertainties in the cases where there are one or two jets in the events. The cancellation is not perfect because any changes in JES and JER are consistently propagated to the \( E_T^\text{miss} \) measurement event-by-event. This causes larger associated migrations for the \( W \) selection than for the \( Z \) selection. In addition, the level of

**Fig. 3** The ratio of \( W + \text{jets} \) and \( Z + \text{jets} \) production cross sections, \( R_{\text{jets}} \), normalized as described in the text versus the leading-\( \text{jet} \) transverse momentum, \( p_T \), for \( N_{\text{jets}} \geq 2 \) (left) and \( \geq 3 \) (right). The electron and muon channel measurements are combined as described in the text. Ratios of the BLACKHAT+SHERPA NLO calculation and the ALPGEN and SHERPA generators to the data are shown in the lower panels. Vertical error bars show the respective statistical uncertainties. The hatched error band shows statistical and systematic uncertainties added in quadrature for the data. The solid error bands show the statistical uncertainties for the ALPGEN and SHERPA predictions, and the combined statistical and theoretical uncertainties for the BLACKHAT+SHERPA prediction.
background in the $W+\text{jets}$ sample is larger, resulting in a larger jet uncertainty compared to the $Z+\text{jets}$ selection. The sum of JER and JES uncertainties on the $R_{\text{jets}}$ measurement ranges from 3% to 8% in the electron channel and from 2% to 5% in the muon channel as $N_{\text{jets}}$ ranges from 1 to 4. The difference between the two channels is due to the fact that the $Z \rightarrow e\,e$ background in the $W \rightarrow e\,\nu$ sample is much larger than the corresponding $Z \rightarrow \mu\,\mu$ background in the $W \rightarrow \mu\,\nu$ sample, being about 7% for candidate events with one jet in the electron channel compared to 3% in the muon channel. The $Z \rightarrow e\,e$ background contaminates the $W \rightarrow e\,\nu$ sample because one electron can be misidentified as a jet, contributing to the JES and JER uncertainties. This contribution to the uncertainties does not cancel in $R_{\text{jets}}$.

The uncertainty on the electron and muon selections includes uncertainties on the electron energy or muon momentum scale and resolution, as well as uncertainties on the scale factors applied to the simulations in order to match the electron or muon trigger, reconstruction and identification efficiencies to those in data. Any changes in lepton energy scale and resolution were consistently propagated to the $E_T^{\text{miss}}$ measurement. The energy- or momentum-scale corrections of the leptons were obtained from comparison of the $Z$-boson invariant mass distribution between data and simulations. The uncertainties on the scale factors have been derived from a comparison of tag-and-probe results in data and simulations [33, 34]. Each of these sources of uncertainty is relatively small in the $R_{\text{jets}}$ measurement (about 1% for $N_{\text{jets}}$ ranging from 1 to 4 in both channels).

The uncertainties in $E_T^{\text{miss}}$ due to uncertainties in JES, JER, lepton energy scale and resolution were included in the values quoted above. A residual $E_T^{\text{miss}}$ uncertainty accounts for uncertainties on the energy measurement of clusters in the calorimeters that are not associated with electrons or jets. It was determined via in-situ measurements and comparisons between data and simulation [43]. These systematic uncertainties affect only the numerator of the ratio because no $E_T^{\text{miss}}$ cut was applied to $Z+\text{jets}$ candidate events. The resulting uncertainty on the $R_{\text{jets}}$ measurement is about 1% for $N_{\text{jets}}$ ranging from 1 to 4 in both channels.

The uncertainty on the unfolding has a component of statistical origin that comes from the limited number of events...
in each bin of the Monte Carlo inputs. This component was estimated from the root mean square of $R_{\text{jets}}$, normalized as described in the text versus the scalar sum $p_T$ of jets, $S_T$, for $N_{\text{jets}} = 2$ (left) and $\geq 2$ (right). The electron and muon channel measurements are combined as described in the text. Ratios of the BLACKHAT+SHERPA NLO calculation and the ALPGEN and SHERPA generators to the data are shown in the lower panel. Vertical error bars show the respective statistical uncertainties. The hatched error band shows statistical and systematic uncertainties added in quadrature for the data. The solid error bands show the statistical uncertainties for the ALPGEN and SHERPA predictions, and the combined statistical and theoretical uncertainties for the BLACKHAT+SHERPA prediction.

For backgrounds estimated using simulation, the uncertainty on the cross-section calculation was taken into account. The combined impact of these uncertainties on the $R_{\text{jets}}$ measurement is typically less than 1% for the different jet multiplicities.

For $t\bar{t}$ predictions taken from the ALPGEN sample, the uncertainty on the cross-section calculation is considered, as well as a shape uncertainty by comparing to the POWHEG-BOX $t\bar{t}$ sample. The largest contribution to the total uncertainty from the data-driven $t\bar{t}$ estimate is from the statistical uncertainty on the fit. The systematic uncertainty on the data-driven $t\bar{t}$ estimate also covers uncertainties on the contamination of the background template by signal events, on the choice of fit range and other small uncertainties. The latter include the uncertainties on the $b$-tagging efficiencies and uncertainties on the bias in the $t\bar{t}$ distributions when applying the $b$-tagging. The uncertainty on the contribution from $W+$ heavy-flavour events to the $t\bar{t}$ template, modelled...
by ALPGEN Monte Carlo samples, was evaluated by varying the $W+c$ cross section and the combined $W+cc$ and $W+bb$ cross sections. The size of the variations is a factor of 0.9 and 1.3 respectively. These factors were obtained from fits to the data in two control regions, defined as one or two jets and at least one $b$-tagged jet. This uncertainty, which is 3% of the number of $t\bar{t}$ events for $N_{\text{jets}} \geq 3$, is largest at lower jet multiplicities where the contribution from $W+heavy$ flavour is most significant. The upper limit of the fit range in transformed aplanarity was varied from 85 to 0.

### 8 Combination of electron and muon channels

In order to increase the precision of the $W+$ jets to $Z+$ jets differential cross-section ratio measurements the results obtained for each observable in the electron and the muon
channels were statistically combined, accounting for correlations between the sources of systematic uncertainties affecting each channel. Since the electron and muon measurements were performed in different fiducial regions, bin-by-bin correction factors, estimated using ALPGEN Monte Carlo samples, were applied to each measured distribution to extrapolate the measurements to the common phase space defined in Table 1. The corrections to the $R_{\text{jets}}$ measurement are of the order of 6% in the electron channel and 1% in the muon channel. The uncertainties on the acceptance corrections are below 0.5%, as determined by using SHERPA instead of ALPGEN. By comparing distributions computed at LO and NLO, it was checked with MCFM that NLO effects on the extrapolation to the common phase space are negligible. Before the combination was performed, the individual results of the two channels were compared to each other after extrapolation; the results are compatible within their respective uncertainties.

The method of combination used is an averaging procedure described in Refs. [45,46]. The distributions for each observable were combined separately by minimising a $\chi^2$ function which takes into account the results in the extrapolated electron and muon channels and all systematic uncertainties on both channels. The uncertainties on the modelling in the unfolding procedure, the integrated luminosity, the background contributions estimated from simulations except for $Z + \text{jets}$ and $W + \text{jets}$ backgrounds and systematic uncertainties on the data-driven $\tilde{t}\tilde{t}$ estimation were treated as correlated among bins and between channels. The lepton systematic uncertainties were assumed to be correlated between bins of a given distribution, but uncorrelated between the two lepton channel measurements. The statistical uncertainties of the data, the statistical uncertainty of the unfolding procedure, and the statistical uncertainty of the $\tilde{t}\tilde{t}$ fit were treated as uncorrelated among bins and channels. The systematic uncertainties on multi-jet backgrounds, which contain correlated and uncorrelated components, are also treated as uncorrelated among bins and channels. This choice has little impact on the final combined results and was chosen as it is slightly more conservative in terms of the total uncertainty of the combined results. Finally, the uncertainties from the jet energy scale, the jet energy resolution, the $E_T^{\text{miss}}$ calculation and the $Z + \text{jets}$ and $W + \text{jets}$ background contributions were treated as fully correlated between all bins and do not enter...
order calculation is performed at parton level only, without radiation and hadronization effects. Renormalisation and factorisation scales were evaluated at $H_T/2$, where $H_T$ is defined as the scalar sum of the transverse momenta of all stable particles in each event. The PDF set used was CT10 \cite{17}. Partons were clustered into jets using the anti-$k_T$ algorithm with $R = 0.4$.

The effect of uncertainties on the prediction has been computed for $R_{\text{jets}}$, accounting for correlation between the individual $W +$ jets and $Z +$ jets processes. The uncertainties on the theoretical predictions are significantly reduced in this procedure, with the statistical uncertainty on the samples often dominating.

Uncertainties on the renormalisation and the factorisation scales were evaluated by varying these scales independently to half and twice their nominal value. The PDF uncertainties were computed from the CT10 eigenvectors, derived with the Hessian method at 68% confidence level \cite{17}. The changes in $R_{\text{jets}}$ due to these PDF variations were combined and used as the uncertainty. In addition, the nominal value of the strong coupling constant, $\alpha_s = 0.118$, was varied by $\pm 0.0012$, and the impact of this variation was taken into account in the PDF uncertainty. All the uncertainty components mentioned above were then added in quadrature. The total systematic uncertainty on the prediction ranges from 0.3% to 1.8% for inclusive jet multiplicities ranging from one to four, and from 2% to 6% for leading-jet $p_T$ ranging from 30 GeV to 700 GeV.

In order to compare the BLACKHAT+SHERPA parton-level predictions with the measurements at particle level, a set of non-perturbative corrections was applied to the predictions. Corrections for the underlying event (UE) were calculated using samples generated with ALPGEN+HERWIG+JIMMY. The ratio of samples where the UE has been switched on and off was evaluated in each bin of each distribution. Corrections for the hadronization of partons to jets were computed using similar samples by forming the ratio of distributions obtained using jets clustered from hadrons versus jets clustered from partons. In $R_{\text{jets}}$, the hadronization and UE corrections have opposite signs and are quite small (typically 2% to 3% for the exclusive jet multiplicity), so the overall correction factor is close to unity. Additional ALPGEN+PYTHIA samples were used to estimate the uncertainties due to these non-perturbative corrections, which are typically well below 1%.

Finally, corrections for QED final-state radiation were calculated as the ratio of $R_{\text{jets}}$ derived from “dressed” leptons to $R_{\text{ jets}}$ defined before any final-state photon radiation, using ALPGEN samples interfaced to PHOTOS. These corrections range between 1% and 2% for both the electron and the muon channel. Systematic uncertainties were derived by comparing with corrections obtained using SHERPA, which calculates final-state QED radiation using the YFS method \cite{50}. The

The measured distributions of all the observables considered in the analysis are compared at particle level to various pQCD predictions in the phase space defined in Table 1.

Next-to-leading-order pQCD predictions were calculated with BLACKHAT+SHERPA \cite{47–49} at parton level for various parton multiplicities, from zero to four. In this calculation BLACKHAT is used for the computation of the virtual one-loop matrix elements, while SHERPA is used for the real emission part and the phase-space integration.
The theoretical predictions described in Sect. 9 are compared in Sect. 6. Individual ratios of the BLACKHAT+SHERPA, ALPGEN, and SHERPA predictions to unfolded data make it possible to disentangle the important features of each theoretical prediction. The $R_{\text{jets}}$ results highlight the ability of these Monte Carlo programs to model the differences between $Z + \text{jets}$ and $W + \text{jets}$ processes.

10 Results and discussion

The theoretical predictions described in Sect. 9 are compared to the experimental data unfolded to particle level, as defined in Sect. 6. Individual ratios of the BLACKHAT+SHERPA, ALPGEN, and SHERPA predictions to unfolded data make it possible to disentangle the important features of each theoretical prediction. The $R_{\text{jets}}$ results highlight the ability of these Monte Carlo programs to model the differences between $Z + \text{jets}$ and $W + \text{jets}$ processes.

Figure 1 shows $R_{\text{jets}}$ as a function of exclusive and inclusive jet multiplicity. The values are detailed in Tables 6 and 7, respectively.\footnote{Tabulated values of the results are also available in the Durham HepData Project: http://hepdata.cedar.ac.uk.} The theoretical predictions describe the data fairly well, given the experimental uncertainties, with few exceptions. At high jet multiplicities, where the effects of hard QCD radiation are tested, the SHERPA prediction is about 1.5 standard deviations (1.5$\sigma$) of the experimental error greater than the measurement. BLACKHAT+SHERPA is able to describe $R_{\text{jets}}$ measured as a function of exclusive jet multiplicity, within the theoretical uncertainties, although it is about 1$\sigma$ greater than the measurement at high inclusive jet multiplicities; this is expected since it does not include all contributions for events with at least four jets.

In the following figures, $R_{\text{jets}}$ is normalized to the ratio of the $W$ and $Z$ cross sections in the corresponding jet multiplicity bin presented in Fig. 1, so that the shapes of the distributions can be compared. Figure 2 shows the $R_{\text{jets}}$ ratio versus the leading-jet $p_T$ for $N_{\text{jets}} = 1$ and $N_{\text{jets}} \geq 1$. At low transverse momentum ($p_T < 200$ GeV), the $R_{\text{jets}}$ distribution

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**Fig. 9** The ratio of $W + \text{jets}$ and $Z + \text{jets}$ production cross sections, $R_{\text{jets}}$, normalized as described in the text versus the leading-jet rapidity, $y$, for $N_{\text{jets}} \geq 1$ (left) and second-leading-jet $y$ for $N_{\text{jets}} \geq 2$ (right). The electron and muon channel measurements are combined as described in the text. Ratios of the BLACKHAT+SHERPA NLO calculation and the ALPGEN and SHERPA generators to the data are shown in the lower panels. Vertical error bars show the respective statistical uncertainties. The hatched error band shows statistical and systematic uncertainties added in quadrature for the data. The solid error bands show the statistical uncertainties for the ALPGEN and SHERPA predictions, and the combined statistical and theoretical uncertainties for the BLACKHAT+SHERPA prediction.
falls as the leading-jet $p_T$ increases, indicating that the shapes in $W + jets$ and $Z + jets$ events are different. This is due to the $W$ and $Z$ boson mass difference, which affects the scale of the parton radiation, and the different vector-boson polarizations, which affect the kinematics of their decay products. In the small region very close to the minimum value of the jet $p_T$ considered in the analysis, where radiative parton shower effects play a major role, all of the predicted shapes exhibit trends different from those in the data, but the ALPGEN predictions still show the best agreement.

Figure 3 shows $R_{jets}$ versus the leading-jet $p_T$ for $N_{jets} \geq 2$ and $N_{jets} \geq 3$. The $R_{jets}$ distribution falls less steeply the more jets are in the event. This is due to the smaller average vector-boson $p_T$, which reduces the effects arising from differences in boson masses and polarizations. At the lowest $p_T$ values considered the comparison with the data shows a tendency for different behaviour of the theoretical predictions, especially in events with at least three jets. The effect, which is most pronounced for BLACKHAT+SHERPA, is expected in case of lack of resummation of soft and collinear parton emissions, as in this calculation.

Figure 4 shows $R_{jets}$ versus the second- and third-leading-jet $p_T$ for $N_{jets} \geq 2$ and $N_{jets} \geq 3$ respectively. The various predictions agree with the data distributions, given the uncertainties, except for small deviations in the second-leading-jet $p_T$ for $N_{jets} \geq 2$.

The next kinematic observable studied is $S_T$, the scalar sum of all jet transverse momenta in the event. This observable is often used in searches for new high-mass particles. Figure 5 shows $R_{jets}$ versus $S_T$ for $N_{jets} = 2$ and $N_{jets} \geq 2$, while Fig. 6 shows $R_{jets}$ versus $S_T$ for $N_{jets} = 3$ and $N_{jets} \geq 3$. At the lowest values of $S_T$ the predicted distributions are different from the measured distributions, particularly for SHERPA, but in the higher-$S_T$ region the theoretical predictions describe the data well. The central value of the fixed-order BLACKHAT+SHERPA calculation does not reproduce the $S_T$ distributions for $W + jets$ and $Z + jets$ separately as well as the inclusive calculation, corroborating the previous observations in Refs. [4,5]. The tensions are due to the missing higher-order contributions which cancel almost completely in $R_{jets}$.

Figure 7 shows the separation $\Delta R_{(1,2)}$ and the azimuthal angular distance $\Delta \phi_{(1,2)}$ between the two leading jets, and Fig. 8 shows their invariant mass $m_{12}$ for $N_{jets} \geq 2$. At the lowest $\Delta R_{(1,2)}$ and $m_{12}$ values, the predicted shapes differ from the measured ones. This is interpreted as a weak sensitivity to non-perturbative effects enhancing the difference in soft QCD radiation between $W$ and $Z$ events, but not cancelling completely in $R_{jets}$.

Figure 9 shows the leading-jet rapidity for $N_{jets} \geq 1$, and the second-leading-jet rapidity for $N_{jets} \geq 2$, while Fig. 10 shows the third-leading-jet rapidity for $N_{jets} \geq 3$. The different trends between predictions at high leading-jet rapidity can be due to the effects of the parton shower and, in some cases, different PDF sets. These effects, which do not cancel completely in $R_{jets}$, are moderated by the presence of extra jets.

11 Conclusions

Measurements of the ratio of $W + jets$ to $Z + jets$ production cross sections have been performed by the ATLAS experiment using a data sample of proton–proton collisions corresponding to an integrated luminosity of 4.6 fb$^{-1}$ collected at a centre-of-mass energy of $\sqrt{s} = 7$ TeV at the LHC. The data were unfolded to particle level and compared to predictions from Monte Carlo simulations. By being sensitive to differences between $W + jets$ and $Z + jets$ events, and through large cancellations of experimental systematic uncertainties and non-perturbative QCD effects, the $R_{jets}$ measurements provide information complementary to individual $W + jets$
and $Z + \text{jets}$ measurements. This $R_\text{jets}$ measurement significantly improves on previous results by probing kinematic distributions for the first time in events with jet multiplicity up to four jets. It also allows a detailed comparison with state-of-the-art NLO pQCD Monte Carlo calculations, which agree well with the observed data except in a few specific regions. In particular, the BLACKHAT+SHERPA predictions for $R_\text{jets}$ at high jet multiplicity and large leading-jet momenta are validated with this large dataset and are consistent with the results from tuned event generators. This new measurement highlights the success of recent theoretical advances and the opportunity for further tuning to improve the description of the production of vector bosons in association with jets.

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