### THE STABILITY OF LOW SURFACE BRIGHTNESS DISKS BASED ON MULTI-WAVELENGTH MODELING

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THE STABILITY OF LOW SURFACE BRIGHTNESS DISKS BASED ON MULTI-WAVELENGTH MODELING

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ABSTRACT

To investigate the structure and composition of the dusty interstellar medium (ISM) of low surface brightness (LSB) disk galaxies, we have used multi-wavelength photometry to construct spectral energy distributions for three low-mass, edge-on LSB galaxies \(V_{\text{rot}} = 88–105 \text{ km s}^{-1}\). We use Monte Carlo radiation transfer codes that include the effects of transiently heated small grains and polycyclic aromatic hydrocarbon molecules to model and interpret the data. We find that, unlike the high surface brightness galaxies previously modeled, the dust disks appear to have scale heights equal to or exceeding their stellar scale heights. This result supports the findings of previous studies that low-mass disk galaxies have dust scale heights comparable to their stellar scale heights and suggests that the cold ISM of low-mass, LSB disk galaxies may be stable against fragmentation and gravitational collapse. This may help to explain the lack of observed dust lanes in edge-on LSB galaxies and their low current star formation rates. Dust masses are found in the range \(1.16–2.38 \times 10^6 \, M_\odot\), corresponding to face-on (edge-on), \(V\)-band, optical depths \(0.034 \lesssim \tau_{\text{face}} \lesssim 0.106\) (0.69 \(\lesssim \tau_{\text{eq}} \lesssim 1.99\)).

Key words: galaxies: ISM – galaxies: spiral – radiative transfer

Online-only material: color figures

1. INTRODUCTION

Low surface brightness (LSB) disk galaxies, whose central, face-on surface brightnesses fall below \(\mu_{B,0} \gtrsim 23.0 \text{ mag arcsec}^{-2}\) in the \(B\) band, account for an important fraction of the luminosity and galactic mass densities of the local universe (Driver 1999; Minchin et al. 2004; O’Neil & Bothun 2000). LSB disk galaxies show a range of masses and morphologies (e.g., Sprayberry et al. 1997; Auld et al. 2006), but the most common are bulgeless, late-type LSB disks with Hubble types Sd–Sdm. These galaxies frequently show signs of being dark matter dominated at nearly all radii (e.g., de Blok & McGaugh 1997; de Blok & Bosma 2002; Banerjee et al. 2010).

LSB galaxies have been extensively studied in the \(H\) 21 cm line. Often their total \(H\) I masses are comparable to or larger than their high surface brightness (HSB) counterparts, while their \(H\) I surface densities are lower by a factor of \(\sim 2\) (van der Hulst et al. 1993). In fact, LSB galaxies are usually found to have most of their \(H\) I disk at surface densities below the Kennicutt (1989) critical values for the formation of massive stars (van der Hulst et al. 1993). This fact may lead to a lower than expected star formation efficiency causing LSB galaxies to evolve more slowly than HSB galaxies. A lack of high-mass stars will slow metal production and indeed McGaugh (1994) find LSB galaxies have metal abundances of \(\sim 1/3\) solar. \(H\) II regions are observed in LSB galaxy disks as traced by \(H\alpha\) emission (Rand 1996; McGaugh et al. 1995; Matthews et al. 1999) and blue disk colors indicating young stars are present (McGaugh et al. 1995; Matthews et al. 1999; Matthews & Uson 2008) suggesting LSB galaxies do have ongoing star formation. However, the conditions and structure of the interstellar medium (ISM) in LSB disk galaxies are still uncertain.

While observations of \(H\alpha\) and \(H\) I have revealed information on the ionized and atomic gas, little is known about the dust and molecular hydrogen in the ISM. Based on observations of \(^{12}\text{CO}(1–0)\) emission in several LSB disk galaxies, Matthews et al. (2005) find that the CO emission, and hence the molecular hydrogen content, depends strongly on the rotational velocity. It appears that the rotational velocity, as well as the surface density, plays an important role in shaping the structure and content of the ISM. This is also suggested by the work of Dalcanton et al. (2004) who find that the gas and dust disk of a galaxy is more stable to the effects of radial instabilities at lower rotational velocity. This limits the ability of perturbations to cause the collapse of the ISM into a thinner layer and may inhibit global star formation by preventing the formation of large numbers of giant molecular clouds.

Due to the difficulties of directly detecting molecular gas in low-mass LSB spirals (see Matthews & Gao 2001; Matthews et al. 2005; Das et al. 2006), an alternative method to investigate the composition and structure of their molecular ISM is to observe far-infrared (FIR) emission produced by dust. The dust and gas are expected to be well mixed and so the highest dust densities should trace the high-density, cool phases of the ISM. In order to interpret the distribution of FIR emission, we require a radiation transfer model to produce synthetic images and spectral energy distributions (SEDs) based on galactic stellar and dust distributions. Previous modeling efforts have focused on fitting the optical and near-infrared (NIR) extinction of HSB galaxies (Kylafis & Bahcall 1987; Xilouris et al. 1997, 1998, 1999; Bianchi et al. 2000; Bianchi 2007) and treating the dust absorption and reemission processes to model the full UV/optical to submillimeter (sub-mm) SED (Popescu et al. 2000, 2011; Misiriotis et al. 2001; Bianchi 2008; Baes et al. 2010). In the present work, we extend this type of analysis for the first time to a sample of LSB galaxies.

When modeling the optical appearance of a disk galaxy an edge-on orientation is advantageous. This viewing geometry allows both the vertical and radial ISM structure to be constrained simultaneously and small-scale features of the galaxy...
are smoothed out due to overlapping sight lines. The effects of dust become more apparent and dark dust lanes can often be seen obscuring stellar emission where the central regions of the galactic disk have become optically thick. This makes the quantification of dust masses and distributions much more straightforward than the more degenerate case of a less inclined disk that is optically thin across most of its area.

In this paper, we further constrain the effects of dust, ISM geometry, and mass on the UV/optical–FIR SEDs of edge-on LSB galaxies using Monte Carlo radiation transfer techniques. In Section 2, we will introduce the sample of galaxies to which the analysis is applied followed by a description of the data available at various wavelengths in Section 3. Section 4 includes a description of the model used in the analysis. The results for our sample of galaxies can be found in Section 5 and a discussion of the key results is presented in Section 6.

2. GALAXY SAMPLE

We have selected three LSB galaxies that have been observed at a wide range of wavelengths to allow the best determination of the shape of the SED. The galaxies are nearby (≤10 Mpc) and are well-resolved in optical imaging. We have selected the galaxies to span a range of central face-on surface brightness (μB,0 = 22.6–23.6 mag arcsec−2) as well as rotational velocity (Vrot = 88–105 km s−1). The three galaxies have similar total H I masses but observations indicate that their molecular hydrogen content decreases with decreasing rotational velocity (Vrot; Matthews et al. 2005), suggesting that the ISM conditions may be different across our sample. Table 1 contains the properties of the galaxies as gathered from the literature. High-resolution optical imaging of the three galaxies can be seen in Figure 1.

2.1. UGC 7321

UGC 7321 is one of the best studied edge-on LSB galaxies. It shows a very thin disk (a/b ∼ 10.3) with signs of clumping of the stellar and dust distributions in the inner galaxy (Matthews & Wood 2001) and a more uniform structure in the outer disk. The disk shows strong (B − R) color gradients in both horizontal and vertical directions that cannot be explained by the effects of dust (Matthews & Wood 2001) and appear to be due to stellar population or metallicity gradients within the disk itself. Hα imaging shows ionized gas is present in a very thin layer that has very little structure and shows no signs of large-scale star-forming regions (Matthews et al. 1999). The H I gas content of UGC 7321 has a greater radial extent than the optical disk of the galaxy (Uson & Matthews 2003) and indicates that the H I disk is also vertically extended (Matthews & Wood 2003).

2.2. IC 2233

IC 2233 is another example of a thin, bulgeless galaxy viewed close to edge-on. It shows no signs of a dust lane in the central regions of its disk with only a few dark clouds visible. Rand (1996) detected Hα emission associated with H II regions across the disk of IC 2233, including a large complex in the outer region of the galaxy, indicating that there is ongoing star formation. In contrast to UGC 7321, the H II regions in IC 2233 are often

### Table 1

<table>
<thead>
<tr>
<th>Name</th>
<th>Type</th>
<th>B-band Luminosity (10^9 L☉)</th>
<th>Distance (Mpc)</th>
<th>Vrot (km s⁻¹)</th>
<th>μB,0 (0)</th>
<th>M_HI (10^6 M☉)</th>
<th>M_H2 (10^7 M☉)</th>
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<td>UGC 7321</td>
<td>Sd</td>
<td>1.1</td>
<td>10</td>
<td>105</td>
<td>23.6</td>
<td>1.1</td>
<td>3.2</td>
</tr>
<tr>
<td>IC 2233</td>
<td>Sd</td>
<td>1.8</td>
<td>10</td>
<td>88</td>
<td>22.6</td>
<td>1.1</td>
<td>&lt;0.1</td>
</tr>
<tr>
<td>NGC 4244</td>
<td>Sd</td>
<td>3.6</td>
<td>4.4</td>
<td>95</td>
<td>23.6</td>
<td>1.3</td>
<td>1.4</td>
</tr>
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</table>

Note. a Value deprojected to face-on.

Observations of the CO(1–0) line emission by Matthews & Gao (2001) confirm the presence of molecular gas in UGC 7321 and this measurement leads to a molecular hydrogen mass of M_H2 × 3.2 × 10^7 M☉, assuming a Galactic CO–H2 conversion factor X = 3.0 × 10⁻²₀ cm⁻² (K km s⁻¹)⁻¹ (Young & Scoville 1991).

2.2. IC 2233

IC 2233 is another example of a thin, bulgeless galaxy viewed close to edge-on. It shows no signs of a dust lane in the central regions of its disk with only a few dark clouds visible. Rand (1996) detected Hα emission associated with H II regions across the disk of IC 2233, including a large complex in the outer region of the galaxy, indicating that there is ongoing star formation. In contrast to UGC 7321, the H II regions in IC 2233 are often
located out of the mid-plane at up to $\sim 0.5 \, Z_\odot$ in the outer parts of the galaxy (Matthews & Uson 2008). Observations by Matthews & Uson (2008) find that H i in IC 2233 is extended vertically and horizontally beyond the optical disk, with evidence for flaring in the outer gas disk. Attempts by Matthews et al. (2005) to detect CO emission from IC 2233 were unsuccessful leading to a 3$\sigma$ upper limit on the mass of molecular hydrogen of $1.4 \times 10^6 \, M_\odot$.

2.3. NGC 4244

NGC 4244 is the closest galaxy in our sample lying at an estimated distance of only $\sim 4.4 \, Mpc$ (Seth et al. 2005a). NGC 4244 shows many dark clouds in optical imaging of its central regions. Despite this, based on NIR photometry Kodaira & Yamashita (1996) conclude that the disk of NGC 4244 suffers from little internal extinction. Continuum subtracted H$\alpha$ imaging obtained by Hoopes et al. (1999) shows H$\alpha$ regions extending up to $\sim 990 \, pc$ from the disk mid-plane. The two largest H$\alpha$ regions are found in the outer galactic disk. The work of Olling (1996) investigating the H$\alpha$ distribution in NGC 4244 shows that the gas distribution appears to be slightly extended radially compared to the stellar disk. Both Matthews & Gao (2001) and Sage (1993) report the detection of CO emission from NGC 4244 and the estimated H$_2$ mass is $1.4 \times 10^7 \, M_\odot$.

3. DATA

All three galaxies have been observed in the optical by the Sloan Digital Sky Survey (SDSS) in $u$, $g$, $r$, $i$, and $z$ bands and the data are available under data release seven (Abazajian et al. 2009). The images were downloaded from the SDSS archive and fluxes in each band were extracted using GAIA’s aperture photometry tool. It was necessary to re-analyze the SDSS images to extract reliable photometry as each galaxy appeared to have been split into multiple components during the SDSS photometric reduction.

We have also made use of $B$-band imaging of UGC 7321 and IC 2233 obtained at the 3.5 m WIYN telescope at Kitt Peak, AZ. These observations are described in Matthews et al. (1999) (UGC 7321) and Matthews & Uson (2008) (IC 2233). The images have been flux calibrated and are of a higher resolution than the SDSS imaging available. In the case of NGC 4244 we do not have access to higher resolution data and so the SDSS $r$-band imaging will be used for the optical comparisons.

High-resolution Hubble Space Telescope (HST) imaging is also available for our three galaxies. NGC 4244 and IC 2233 have previously been observed using the Wide Field Camera (WFC) of the Advanced Camera for Surveys (ACS) with the F606W filter (Seth et al. 2005b). These data were accessed from the Multimission Archive at STScI. Imaging of UGC 7321 is available from the Wide Field Planetary Camera 2 (WFPC2) and we use a composite F702W and F814W image previously presented in Matthews & Wood (2001). HST images of the inner regions of each galaxy can be seen in Figure 1.

The MIR and FIR observations of our three galaxies were obtained with the Spitzer Space Telescope’s IRAC and MIPS imagers. Data were obtained for this project under Spitzer PID 20432 (PI: L. Matthews) along with observations taken from PIDs 3 (PI: G. Fazio) and 40204 (PI: R. Kennicutt). These data have recently been used as part of the Spitzer Local Volume Legacy (LVL) survey (Dale et al. 2009). This provides imaging and photometry for a large sample of galaxies within $\sim 11 \, Mpc$. Data are available for all four IRAC bands (3.6, 4.5, 5.8, and 8.0 $\mu$m) as well as three MIPS bands (24, 70, and 160 $\mu$m) with photometry provided for each band after foreground stars and background galaxies have been removed and aperture corrections applied.

Photometry is also available based on NIR Two Micron All Sky Survey (2MASS) imaging using apertures matched to those used in the extraction of the IRAC and MIPS fluxes. Spitzer LVL survey imaging can be accessed via an online archive (Lee et al. 2011) provide a catalog of matched far- and near-UV (FUV and NUV) observations for galaxies contained in the Spitzer LVL survey that have been observed with Galaxy Evolution Explorer (GALEX). The GALEX bands are centered at 1528 Å (FUV) and 2271 Å (NUV) (Morrissey et al. 2005) and fluxes have been extracted using the apertures obtained from the FIR Spitzer data for consistency. The UV data provide a constraint on the emission from the young stellar population which, due to the higher opacity at UV wavelengths, will play an important role in heating the diffuse dust.

4. RADIATIVE TRANSFER MODEL

In order to produce synthetic images and SEDs for comparison to the data, we adopt a Monte Carlo radiation transfer modeling scheme.

4.1. Emissivity and Dust Distributions

The model allows energy packets emitted within a smooth stellar emissivity distribution to be tracked as they propagate through a dusty medium. For both the emissivity and dust we adopt a smooth “double exponential” distribution:

$$\rho(\sigma, z) \propto \exp(-|z|/Z) \exp(-\sigma/R),$$

where $\rho(\sigma, z)$ is the density at a point in the galaxy specified by $\sigma$, the cylindrical radius, and $|z|$, the height above or below the galactic plane. The scale lengths $R$ and $Z$ can be independently varied for both components as necessary. The stellar emissivity and dust density are discretized across a three-dimensional spherical grid of cells to allow our Monte Carlo radiation transfer routines to be used. To reduce the number of free parameters in the model no attempt has been made to take account of clumpy substructure within either the emissivity or dust distributions, which may be important in reproducing the optical properties of galactic disks (Matthews & Wood 2001; Bianchi et al. 2000; Pierini et al. 2004). This also allows the use of a lower resolution grid of cells, reducing the memory requirements of each radiation transfer simulation.

4.1.1. Emission Sources

To begin the radiative transfer process, it is necessary to sample an initial wavelength of emission for each photon packet. Wavelengths are chosen to reproduce the intrinsic unattenuated stellar SEDs produced by the population of stars present in each galaxy. For this purpose a set of synthetic stellar SEDs was constructed using the GALEV11 codes (Kotulla et al. 2009). These are shown in Figure 2. Each model initially has a constant

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6 This value has been re-scaled to the distance adopted in this paper (4.4 Mpc).
7 http://www.SDSS.org/dr7/
8 http://archive.stsci.edu/index.html
9 http://www.ipac.caltech.edu/2mass/
10 http://irsx.ipac.caltech.edu/data/Spitzer/LVL/
11 http://www.galev.org/
which are in agreement with Jimenez et al. (1998) who suggest observed stellar SED, we have found that a wide range of ages consistent. We also include the effects of continuum and line emission from gas within the model SEDs.

\begin{figure}
\centering
\includegraphics[width=\textwidth]{figure2.png}
\caption{Intrinsic stellar emission templates used for our three galaxies. The fluxes have been scaled for comparison. The important property of each template is its shape, as this is used within our models to correctly sample the stellar emission. Each galaxy required a different intrinsic stellar template to match the observation in the UV, optical, and NIR. The templates were produced using GALEV (Kotulla et al. 2009) and model parameters can be found in Table 2.}
\end{figure}

\begin{table}
\centering
\begin{tabular}{|l|c|c|c|c|c|}
\hline
Name & Initial SFR & Burst Mass$^a$ & Burst Time$^b$ & Age$^c$ & SFR$^d$ \\
(M$_\odot$ yr$^{-1}$) & Fraction & (10$^6$ yr) & (10$^7$ yr) & (10$^9$ yr) & (M$_\odot$ yr$^{-1}$) \\
\hline
UGC 7321 & 0.02 & 0.1 & 7 & 8.6 & 0.02 \\
IC 2233 & 0.005 & 0.1 & 8 & 9.1 & 0.04 \\
NGC 4244 & 0.03 & 0.2 & 7.5 & 9.4 & 0.04 \\
\hline
\end{tabular}
\caption{Intrinsic Stellar Template Model Parameters}
\end{table}

\begin{figure}
\centering
\includegraphics[width=\textwidth]{figure3.png}
\caption{Template for the emission from compact sources between 10 and 2000$\mu$m. The solid line shows the model output SED as it varies with wavelength. The model comprises of a central star ($T=36,000$ K) heating a constant density shell of gas and dust surrounding it. The shell extends from $10^{-4}$ to 2.3 pc and has a $V$-band optical depth of $\tau_V \sim 88$. The total luminosity included in each cloud model is $2.5 \times 10^3 L_\odot$ and each has a dust mass of $2 \times 10^3 M_\odot$. Data points represent the median observed properties of 56 compact H\textsc{ii} regions found by Chini et al. (1986) at 12, 25, 60, 100, and 1300$\mu$m. Error bars show the range of values observed at each wavelength.}
\end{figure}

Notes.

$^a$ Fraction of remaining gas converted to stars during burst.

$^b$ Age of the galaxy at the time of the star formation burst.

$^c$ Age of the galaxy adopted to fit the broadband fluxes.

$^d$ SFR at adopted age.

star formation rate (SFR) for several Gyr which is followed by an exponentially decreasing burst of star formation with an e-folding time of 1 Gyr. Table 2 lists the values used within the model for each galaxy. In all cases a Salpeter initial mass function with slope $\alpha = -2.35$ is used and the metallicity of the gas is allowed to change with time to remain chemically consistent. We also include the effects of continuum and line emission from gas within the model SEDs.

In searching for appropriate stellar populations to model the observed stellar SED, we have found that a wide range of ages can provide adequate fits. This has previously been noted by other authors (Zackrisson et al. 2005; Vorobyov et al. 2009) who suggested that, based on additional information such as $H\alpha$ equivalent widths and oxygen abundance gradients, old stellar populations are more probable in samples of blue LSB galaxies. The ages adopted here range from 8.6 to 9.4 Gyr which are in agreement with Jimenez et al. (1998) who suggest ages larger than 7 Gyr for LSB galaxies. We note, however, that our conclusions on the dust masses and distributions are most sensitive to the shape of the intrinsic stellar SED and will not be significantly altered by the exact age, metallicity, or star formation history of the underlying stellar population that produces it.

The SFRs for UGC 7321 and IC 2233 have previously been estimated based on the observed $H\alpha$ emission. SFRs of $\sim 0.02$ and $0.05 M_\odot$ yr$^{-1}$ have been found for UGC 7321 (Matthews & Wood 2003) and IC 2233 (Matthews & Uson 2008), respectively, which are in reasonable agreement with the values in Table 2. We have estimated the SFR of NGC 4244 based on the $H\alpha$ luminosity, $L_{H\alpha} = 10^{40}$ erg s$^{-1}$ (Kennicutt et al. 2008), and the SFR–$H\alpha$ relation taken from Kennicutt (1998). Together these yield an SFR $\sim 0.079 \pm 0.023 M_\odot$ yr$^{-1}$ which is roughly consistent with the value adopted for the template stellar SED.

A single stellar SED is assumed for each galaxy modeled. No account of stellar gradients, which may be important in LSB galaxies (Matthews & Wood 2001), is made in order to reduce the complexity of the model. We do not believe that the stellar gradients will have a significant impact on the SED and derived dust disk properties.

Also included is a secondary emission component from obscured star formation regions that may be necessary to account for the total FIR emission. As such emission takes place from compact regions that are below the resolution of the spherical grid currently employed in the radiation transfer, a separate model has been created. The regions are approximated by a single central star surrounded by a shell of dust and gas. The shell has a $V$-band optical depth of $\tau_V \sim 88$ and extends from a distance $d = 10^{-4}$ pc out to 2.3 pc. The size of the shell was chosen to best reproduce the shape of the observed FIR emission of star-forming regions observed by Chini et al. (1986). The shell is exposed to internal heating from a stellar source, with emissivity sampled from a model atmosphere (Kurucz 1993) of temperature $T = 36,000$ K. The shell is also illuminated from the exterior by a radiation field approximating the mean intensity in the plane of the galaxy model. Due to the size of the clouds, however, the luminosity incident on the exterior is typically much smaller than the luminosity of the central source and hence diffuse illumination has little effect on the overall SED. The output SED can be seen in Figure 3 along with observed data points of 56 Galactic compact H\textsc{ii} regions taken from Chini et al. (1986). A single SED is used to approximate all compact sources in the galaxy. The spatial distribution of compact sources is an exponential disk (Equation (1)) with $Z = 0.1$ kpc and $R = 1.8$ kpc in all models. This secondary emission component, from obscured star-forming regions, has previously been found necessary to reproduce the FIR emission.
in HSB galaxies (Popescu et al. 2000, 2011; Misiriotis et al. 2001). Other methods to account for such emission include utilizing sub-grid resolution models for individual star-forming regions (Jonsson et al. 2010) or the inclusion of adaptive grids to allow radiation transfer on the small size scales needed. Current adaptive grid models, however, lack the resolution to resolve individual star-forming regions (Bianchi 2008).

4.1.2. Dust Model

The dust content of the model galaxy is treated in a two-component manner as described by Wood et al. (2008) in order to take account of both large grains and small transiently heated grains. Large grains with sizes $>200\,\text{Å}$ are assumed to have attained radiative equilibrium temperatures. In the case of these grains the Bjorkman & Wood (2001) method is used to update the temperature of the cell and correctly sample the emissivity for the re-emitted photon packet when an interaction takes place. The advantage of this method lies in the way the frequency of the re-emitted photon is sampled to correct the frequency distribution of the photons previously emitted from the cell to the new cell temperature. The SED of the cell then relaxes to the equilibrium value, as the simulation progresses, without the need for iteration. The composition and size distribution of the large grains is taken from the work of Kim et al. (1994) who used a mixture of silicate and graphite grains to fit the observed extinction in the Milky Way. This treatment of large dust grains, without the extensions added to treat transient heating of very small grains (VSGs) and polycyclic aromatic hydrocarbon (PAH) molecules, has previously been used by Savoy et al. (2009) to investigate the dust content of early-type galaxies.

The Bjorkman & Wood (2001) method cannot, however, be applied to transiently heated VSGs and PAH molecules that are not at equilibrium temperatures. Emission from these grains is important in reproducing the MIR emission. For photon packet interactions with grains that are smaller than $200\,\text{Å}$ the methods introduced in Wood et al. (2008) are used. The emission from PAH molecules and VSGs is calculated from precomputed emissivity files from Draine & Li (2007). The emissivity is assumed to vary only with the mean intensity of the radiation field and not with the spectral shape. The cutoff in the grain size at $200\,\text{Å}$ is somewhat arbitrary but it is thought that grains above this will normally reach equilibrium temperatures (Draine & Li 2007). In order to correctly sample the emissivity of the PAH molecules and VSGs a value for the mean intensity in the cell where the interaction took place is needed. This requires an iterative process where initially a value of $J = 1$ is used, $J$ being the value of the mean intensity relative to the Mathis et al. (1983) value of the local interstellar radiation field (ISRF) of $J_{\text{ISRF}} = 2.17 \times 10^{-2} \, \text{erg cm}^{-2} \, \text{s}^{-1}$. Consecutive iterations then use the mean intensity computed for each cell on the previous iteration to calculate the emissivity of the PAH molecules and VSGs. Due to the small contribution of photon packets reprocessed by PAH molecules and VSGs to the total mean intensity, it is found that typically three iterations are required (Wood et al. 2008).

As the ISM conditions of LSB galaxies are likely different from those found in the Milky Way, it is possible that our treatment of the PAH/VSG dust components may be inappropriate. It is known that the strength of the PAH emission relative to that from VSGs, estimated using the $f_c(8\,\mu\text{m})/f_c(24\,\mu\text{m})$ color, decreases with decreasing metallicity (Engelbracht et al. 2005; Madden et al. 2006). This is likely due to either the delayed formation of PAH molecules in low-metallicity environments (Galliano et al. 2008) or destruction/processing caused by the harder radiation field (Gordon et al. 2008; Madden et al. 2006). It is therefore possible that our treatment, which assumes Milky Way abundances, may overestimate PAH emission relative to that of the VSGs. The fraction of the total dust mass contributed by PAH/VSGs is also fixed to a value calculated for the Milky Way. This could affect the relative strength of the MIR and FIR emission.

To model the appearance and SED of each galaxy we can alter the following free parameters of the model: stellar scale length, stellar scale height, dust scale length, dust scale height, stellar luminosity, total dust mass, inclination, and the luminosity of the obscured star formation component.

The overall fitting process was done manually to find the set of parameters that could provide adequate fits to both the optical and the UV–FIR SED.

5. RESULTS

Initial values for the fitting process were taken from sources in the literature. Matthews & Wood (2001) have previously investigated UGC 7321 using a three-dimensional Monte Carlo scattered light code and their parameters for a smooth stellar and dust distribution were adopted as initial values in this case. Matthews & Uson (2008) and Fry et al. (1999) have previously estimated the scale lengths of IC 2233 and NGC 4244, respectively, by fitting an exponential function to the observed surface brightness profiles. While the functions used take no account of the effects of dust on the galaxy profiles they should provide reasonable initial estimates for the stellar distributions assuming that dust effects are not severe. From the work of Xilouris et al. (1999) on HSB, edge-on, galaxies we initially adopted the relation that the dust scale heights would be approximately half the stellar scale heights and the dust scale lengths around 1.4 times larger than the stellar values.

One of the main difficulties in modeling the dust distributions of LSB galaxies is that their disks appear to be optically thin, even when viewed edge-on. When modeling the appearance of HSB galaxies, the effects of the dust distribution can be quantified based on the presence of a dust lane along the galactic mid-plane. As none of our galaxy sample shows any sign of a dust lane the problem becomes more degenerate. Initially, we increased the dust mass in the adopted geometry until the effects of the dust became obvious and the optical profiles of the model galaxy no longer matched the shape of the observed data. It was found that the dust mass required to reprocess the stellar light and reproduce the observed FIR emission could not be located in an average HSB-type dust disk without revealing its presence by flattening the optical profile in the central region of the galaxy.

We find that the optical appearance and total FIR emission of the LSB galaxies can be reproduced by removing the constraint that the dust be more concentrated in the galactic mid-plane than the stars. If the dust scale height is taken to be equal to the stellar scale height then it is also possible to fit the optical appearance of the galaxy adequately. In this case, however, a significantly larger dust mass can be accommodated within the dust disk without the appearance of a dust lane. In order to reproduce the observed FIR flux distribution, it was also necessary to increase the dust scale length. When the dust is vertically extended into a disk with a larger scale height that is well mixed with the stellar population, the exact radial distribution of the dust becomes poorly constrained from optical data alone. We have found that
Figure 4. Observed (left) and synthetic (right) images of UGC 7321 at, from top to bottom: B band, 3.6 μm, 8 μm, 70 μm, and 160 μm. (A color version of this figure is available in the online journal.)

Table 3
Fitted Galaxy Parameters

<table>
<thead>
<tr>
<th>Name</th>
<th>R_s (kpc)</th>
<th>Z_s (kpc)</th>
<th>R_d (kpc)</th>
<th>Z_d (kpc)</th>
<th>L_s (10^8 L⊙)</th>
<th>M_d (10^6 M⊙)</th>
<th>i (°)</th>
<th>L_cloud (10^8 L⊙)</th>
<th>τ_face</th>
<th>τ_eq</th>
</tr>
</thead>
<tbody>
<tr>
<td>UGC 7321</td>
<td>1.8</td>
<td>0.12</td>
<td>4.30</td>
<td>0.12</td>
<td>14.5</td>
<td>2.25</td>
<td>88.5</td>
<td>0.67</td>
<td>0.072</td>
<td>1.99</td>
</tr>
<tr>
<td>IC 2233</td>
<td>1.7</td>
<td>0.18</td>
<td>4.50</td>
<td>0.18</td>
<td>19.3</td>
<td>1.16</td>
<td>88.5</td>
<td>0.01</td>
<td>0.034</td>
<td>0.69</td>
</tr>
<tr>
<td>NGC 4244</td>
<td>1.9</td>
<td>0.2</td>
<td>3.4</td>
<td>0.2</td>
<td>33.5</td>
<td>2.38</td>
<td>84.5</td>
<td>1.0</td>
<td>0.106</td>
<td>1.57</td>
</tr>
</tbody>
</table>

The dust scale length is between 1.8 and 2.6 times the stellar scale length for our LSB disk galaxies.

The best-fit parameters for our models of each galaxy can be found in Table 3. R_s and R_d are the radial scale lengths of the stars and dust while Z_s and Z_d are the vertical scale heights. L_s is the intrinsic bolometric luminosity of the stellar population. M_d represents the total dust mass and i the inclination angle. L_cloud gives the luminosity emitted from the template of compact dust emission (see Section 4.1.1). τ_face and τ_eq give the V-band face-on and equatorial optical depths, respectively.12

Figures 4–6 show a comparison of the B (or r), 3.6 μm, 8 μm, 70 μm, and 160 μm data (left panel) and synthetic images (right panel). In general, the B (or r) and 3.6 μm model images match the large-scale morphology of the data reasonably well. Differences are, however, apparent in the longer wavelength emission at 8, 70, and 160 μm that is dominated by emission from PAHs and dust grains. IC 2233 and NGC 4244 show significant structure in their 8 and 70 μm images, suggesting that perhaps a more complex non-axisymmetric dust distribution is needed. In both galaxies several small point-like sources in the outer disk are prominent at 70 μm. These are likely star-forming regions as they appear brighter at shorter wavelengths and show associated emission in GALEX FUV and Hα imaging. The 160 μm emission from all three of our model galaxies shows a significant deviation from the data. The models predict a centrally concentrated 160 μm image while the data suggest a more diffuse distribution. Figures 7–9 show B (or r) band intensity profiles parallel to the minor axes of the galaxies at various points while Figures 10–12 show the output model SEDs for the three LSB galaxies.

Overall the models are able to reproduce the global properties of the data. The surface brightness slices parallel to the minor axis and along the major axis show a similarity to the data and deviations are likely caused by the comparison of smooth emission at 8, 70, and 160 μm that is dominated by emission from PAHs and dust grains. IC 2233 and NGC 4244 show significant structure in their 8 and 70 μm images, suggesting that perhaps a more complex non-axisymmetric dust distribution is needed. In both galaxies several small point-like sources in the outer disk are prominent at 70 μm. These are likely star-forming regions as they appear brighter at shorter wavelengths and show associated emission in GALEX FUV and Hα imaging. The 160 μm emission from all three of our model galaxies shows a significant deviation from the data. The models predict a centrally concentrated 160 μm image while the data suggest a more diffuse distribution. Figures 7–9 show B (or r) band intensity profiles parallel to the minor axes of the galaxies at various points while Figures 10–12 show the output model SEDs for the three LSB galaxies.

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Figure 6. Observed (left) and synthetic (right) images of NGC 4244 at, from top to bottom: r band, 3.6 μm band, 8 μm, 70 μm, and 160 μm. (A color version of this figure is available in the online journal.)

Figure 7. The top two plots show UGC 7321 B-band surface brightness slices parallel to the minor axis at the galaxy center (top), and 3 kpc radial distance along the major axis (middle). The bottom panel shows the surface brightness variation along the major axis. All slices are average values taken across a ~60 pc region. Solid lines show the predicted intensity based on our best-fitting Monte Carlo radiation transfer models and crosses represent the data taken from the B-band image.

Figure 8. Same as in Figure 7, but for IC 2233.

axisymmetric models to observations of a galaxy that shows a clear clumpy structure (see Figure 1). The main discrepancies found between the surface brightness of the model and data generally occur in the central regions of the galaxies. As can be
seen in Figure 1 these are also the regions that show the greatest number of dark clouds and bright star clusters. Our smooth axisymmetric model is not able to reproduce such structures and so only a relatively poor fit can be achieved in the central regions.

The short dashed line in Figure 10 shows the result of fitting the optical imaging of UGC 7321 using the average HSB galaxy stellar-to-dust scaling relation of Xilouris et al. (1999). In order to produce the required 70 μm emission a large luminosity is assigned to the obscured star formation template (see Section 4.1.1). However, this scenario underestimates the 160 μm emission by a factor \( \sim 2 \).

In the SEDs the shorter wavelength data from the UV through to NIR originate in the underlying stellar populations and can be highly attenuated by the diffuse dust in the ISM. Most of the photons absorbed by the dust, in our models, originated as short-wavelength UV emission. This can be seen in Figure 10 as the difference between the intrinsic stellar emission (long dashed line) and the observed emission (solid line) once the photons have propagated through the dusty ISM. The amount of absorption tends to decrease with increasing wavelength as the dust opacity decreases and the photons are able to travel through the ISM with a lower probability of interaction. Our models can reproduce the observed optical and NIR fluxes well but show slight discrepancies in the FUV emission. The models are also unable to reproduce the \( z \)-band flux (0.893 μm). We believe this may be due to the lower signal-to-noise ratio in the \( z \) band combined with the intrinsic LSB of the galaxies, leading to galaxy flux being lost during removal of the sky background.

The 5.8 and 8.0 μm IRAC bands trace emission from PAH molecules while the MIPS 24 μm emission is produced primarily by the warm VSGs. In all three cases the 8.0 μm emission is overpredicted by our models. The 24 μm flux is overpredicted...
by the model of UGC 7321, and underpredicted for IC 2233. This behavior in the MIR is likely a result of our treatment of the PAH/VSG emission which is based on Milky Way abundances and illuminating radiation field shape (see Section 4.1.2). Both the relative abundances of PAH molecules and VSGs in LSBs and the shape of the ISRF in LSBs are likely different, causing the discrepancies observed in the MIR.

The larger, cooler dust grains are responsible for the peak of the FIR emission bracketed by the MIPS observations at 70 and 160 $\mu$m. In all three cases we have been able to reproduce the FIR 70 and 160 $\mu$m emission, within the quoted photometry errors, using our models.

6. DISCUSSION

The model outputs suggest that it is possible to provide a good global fit to the optical appearance of LSB galaxies, while at the same time reproducing the observed FIR emission. At some locations, however, such as the central region of UGC 7321 (Figure 7, top) there is a clear discrepancy between the data and the model. In most cases this occurs due to structure in the galaxy that is not included in our models, such as star clusters, $\text{H}^\text{ii}$ regions, and optically thick dust clumps.

6.1. Implications of the Models

In our analysis, we have found that in order to accommodate the mass of dust required to reprocess the FIR emission seen in our sample of three LSB galaxies it is necessary for the dust to be located in a diffuse disk with a scale height at least equal to that of the stellar population. This is in contrast to the dust distributions obtained by previous studies of HSB galaxies (see Section 5), which find the dust to be located in a diffuse disk with approximately half the scale height of the stellar disk. The main observational signature of the smaller vertical extent of the dust in HSB galaxies is the central dust lane observed when the inclination approaches edge-on. Dalcanton et al. (2004) have previously noted that in a sample of edge-on galaxies that spans a range in $V_{\text{rot}}$ there appears to be a remarkably sharp divide between galaxies that contain dust lanes and those that do not at around $V_{\text{rot}} = 120$ km s$^{-1}$, with no abrupt change in the stellar or $\text{H}^\text{ii}$ surface densities. They attribute this sharp divide to the onset of radial instabilities in galactic disks causing the vertical collapse of the ISM when perturbed by spiral structure. The collapse leads to a higher gas density in the central galaxy having the effect of increasing the star formation rate and surface brightness. The increased gas density also causes a corresponding increase in the dust density in the galactic mid-plane which, when viewed edge-on, will produce the pronounced dust lanes observed. From Table 1 it can be seen that all three of our LSB galaxies have $V_{\text{rot}} < 120$ km s$^{-1}$ and so from the results of Dalcanton et al. (2004) would be expected to be stable across most of their disks. This result suggests that as the disks are stable the gas and dust disk should have a scale height comparable to or larger than the stellar value, which is what we have found from our modeling of the optical, NIR, and FIR data.

In the case of the LSB galaxies studied here an alternative explanation for the comparable scale heights of the dust and stellar disks is that the scale height of the stellar disk is comparatively smaller than that found in HSB galaxies, contributing to the thin appearance of the galaxies. In this case the dust and gas disk scale height may be comparable to more massive galax-
From our total dust masses (Table 3) and the H I and molecular hydrogen masses from the literature (Table 1), we can calculate global gas-to-dust ratios. After accounting for the contribution of helium (assuming \( Y = 0.25 \)) we find global gas-to-dust ratios of \( \sim 666 \) (UGC 7321), 734 (NGC 4244), and 1266 (IC 2233). These values are significantly higher than the Galactic value of \( \sim 140 \) (Whittet 1992). The gas-to-dust ratios of UGC 7321 and NGC 4244 fall between those found for the Large Magellanic Cloud (Koornneef 1982) and the Small Magellanic Cloud (SMC; Bouchet et al. 1985) while the value for IC 2233 is consistent with that of the SMC.

6.2. Model Limitations and Future Prospects

It is somewhat unclear what effect the adoption of a clumpy dust and emissivity distribution would have on the FIR emission of our galaxy sample. Matthews & Wood (2001) found that in order to reproduce the optical appearance of UGC 7321 it was necessary to allocate approximately 50% of the dust mass to a clumpy component. The effect that such a two-phase diffuse dust distribution may have on the FIR emission would depend on the associated emissivity distributions. Such dense clumps could be “quiescent” and represent overdense regions of the ISM illuminated only by the diffuse ISRF, but recent evidence suggests that such clouds are optically thin and will contribute little to the attenuation and dust emission (Molinari et al. 2010). However, if the dark clouds seen in HST imaging are star-forming molecular clouds then they will be illuminated by both the ISRF and by young stars embedded within them. It is thought that in the case of LSB galaxies the optical depths of the clumps are similar to those found for diffuse molecular clouds in the Milky Way (Matthews & Wood 2001). In this case the clumpy component may provide a significant contribution to the FIR emission, reducing the need to have a radially extended dust disk as is found using smooth density distributions.

It has also been shown by Indebetouw et al. (2006) that the observed SED of young stellar objects (YSOs) that are embedded in clumpy circumstellar material can have a strong dependence on the observer’s viewing angle (azimuth) and inclination. The observed MIR flux was found to vary by up to two orders of magnitude for the same highly embedded system viewed along a different sightline. The effects are more severe at shorter wavelengths. Although the case of YSOs is very different to the galactic environment studied here it should be noted that the effects of a clumpy galactic ISM containing optically thick clouds may cause viewing angle and inclination dependent effects on the MIR SEDs that are not accounted for in our smooth, axisymmetric models.

Currently, we have no observations of our galaxy sample in the sub-mm wavelength regime. It has been found that in order to reproduce the sub-mm emission observed from some LSB galaxies it becomes necessary to include an additional dust mass (Popescu et al. 2000, 2011; Misiriotis et al. 2001). The additional dust mass reveals its presence through sub-mm emission that is underestimated by models which can adequately describe the SED to \( \sim 100 \) \( \mu m \). Further evidence for an extended cold dust component is also found by Holwerda et al. (2005) based on attenuation of background galaxies in face-on disks. Until observations become available we cannot be sure that our models do not lack cold dust emission at longer wavelengths.

13 In the case of IC 2233, we use the upper limit H 2 mass of \( 1.4 \times 10^6 \, M_\odot \).

7. SUMMARY

We have utilized multi-wavelength imaging and photometry in conjunction with sophisticated Monte Carlo radiation transfer codes to investigate the structure of three edge-on, LSB disk galaxies. The galaxies have been chosen to span a range in central, optical surface brightness and molecular hydrogen masses.

We have been able to reproduce the global, optical appearance of all three galaxies using smooth emissivity and dust distributions. We find that the composition and size distribution of dust grains adopted, which are based on Milky Way extinction, provide a good match to the observed properties in our sample of LSB disk galaxies. Our models also reproduce the total emission at 70 and 160 \( \mu m \) for all three galaxies. However, the FIR morphology of our models appears more centrally concentrated than the more diffuse distribution suggested by the data. We find that the dust mass appears to be distributed in an exponential disk with a scale height comparable to or exceeding that of the stellar disk. This is in contrast to the findings for HSB galaxies where the dust disk is found have a vertical scale height of approximately half the stellar disk (Xilouris et al. 1999). The comparable scale heights in the dust and stellar disks are likely associated with the increased stability of the ISM in LSB disks against vertical collapse (Dalcanton et al. 2004) and the thin nature of the stellar disks, which suggests minimal dynamical heating.

The dust masses and distributions derived suggest dust masses in the range \( (1.16–2.38) \times 10^6 \, M_\odot \) corresponding to face-on, V-band, optical depths between \( \tau_{face} = 0.034–0.106 \).

In future work we hope to develop our radiation transfer models to include small-scale non-axisymmetric structures which may shed further light on the structure of the ISM and star formation processes in LSB disk galaxies. The inclusion of radial variations in the dust disk scale heights, associated with a flaring gas disk, could also prove important. Additional sub-mm observations may also allow us to uncover cold dust that is associated with the extended H I, as has been found in some HSB galaxies (Popescu & Tuffs 2003; Hinze et al. 2006).

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REFERENCES